THE THREE-DIMENSIONAL STRUCTURE OF INTERIOR EJECTA IN CASSIOPEIA A AT HIGH SPECTRAL RESOLUTION

KARL ISENSEE1, LAWRENCE RUDNICK1, TRACEY DELANEY2, J. D. SMITH3, JEONGHEE RH04, WILLIAM T. REACH4, TAKASHI KOZASA5, AND HALEY GOMEZ6

1 Astronomy Department, University of Minnesota, Minneapolis, MN 55455, USA; isensee@astro.umn.edu, larry@astro.umn.edu
2 Massachusetts Institute of Technology, Kavli Institute for Astrophysics and Space Research, 77 Massachusetts Avenue, NE80, Cambridge, MA 02139, USA; tdelaney@space.mit.edu
3 Ritter Astrophysical Observatory, University of Toledo, Toledo, OH 43606, USA; jd.smith@utoledo.edu
4 Spitzer Science Center, California Institute of Technology, MS 220-6, Pasadena, CA 91125, USA; rhou@ipac.caltech.edu, reach@ipac.caltech.edu
5 Department of Cosmosciences, Graduate School of Science, Hokkaido University, Sapporo 060-0810, Japan; kozasa@mail.sci.hokudai.ac.jp
6 School of Physics and Astronomy, University of Wales, P.O. Box 913, Cardiff CF24 3YB, UK; haley.morgan@astro.cf.ac.uk

Received 2009 August 12; accepted 2010 May 31; published 2010 December 3

ABSTRACT

We used the Spitzer Space Telescope’s Infrared Spectrograph to create a high-resolution spectral map of the central region of the Cassiopeia A (Cas A) supernova remnant, allowing us to make a Doppler reconstruction of its three-dimensional structure. The ejecta responsible for this emission have not yet encountered the remnant’s reverse shock or the circumstellar medium, making it an ideal laboratory for exploring the dynamics of the supernova explosion itself. We observe that the O, Si, and S ejecta can form both sheet-like structures and filaments. Si and O, which come from different nucleosynthetic layers of the star, are observed to be coincident in velocity space in some regions, and separated by 500 km s⁻¹ or more in others. Ejecta traveling toward us are, on average, ~900 km s⁻¹ slower than the material traveling away from us. We compare our observations to recent supernova explosion models and find that no single model can simultaneously reproduce all the observed features. However, models of different supernova explosions can collectively produce the observed geometries and structures of the interior emission. We use the results from the models to address the conditions during the supernova explosion, concentrating on asymmetries in the shock structure. We also predict that the back surface of Cas A will begin brightening in ~30 years, and the front surface in ~100 years.

Key words: infrared: general – ISM: individual objects (Cassiopeia A) – ISM: supernova remnants – supernovae: general

Online-only material: color figure

1. INTRODUCTION

Cassiopeia A (Cas A) is the second youngest known supernova remnant (SNR) in our galaxy, with only the recently discovered G1.9+0.3 being younger (Reynolds et al. 2008). Extensive observations in the radio, infrared, optical, and X-ray give an estimated explosion date of around 1680 AD (Thorsten & 2001; Fesen et al. 2006). Emission at most wavelengths, including the infrared, is dominated by a ~120° radius “Bright Ring,” which corresponds to ~2 pc at Cas A’s estimated distance of 3.4 kpc (Reed et al. 1995). This 30° thick Bright Ring is formed when ejecta encounter Cas A’s reverse shock and are heated and ionized. It consists of undiluted ejecta rich in O, Si, S, Ne, Ar, Ca, and Fe (Chevalier & Kirshner 1978; Doivan et al. 1999; Hughes et al. 2000; Willingdale et al. 2003; Hwang & Laming 2003; Laming & Hwang 2003; Morse et al. 2004). Optical, radio, and X-ray observations have revealed the presence of a jet and counterjet in Cas A. These jets consist of a bipolar outflow nearly in the plane of the sky (Fesen & Gunderson 1996). Also visible in the X-ray is a central compact object, presumed to be the neutron star from the supernova explosion (Tananbaum 1999).

Cas A also contains central emission that is not the result of the reverse shock interaction. This material was first discovered via free–free absorption at low radio frequencies (Kassim et al. 1995) and has since been detected in the infrared (Rho et al. 2008; Smith et al. 2009). This material was demonstrated to be in substantially different physical conditions than recently shocked material on the Bright Ring through a combination of Doppler analysis and line ratio measurements (Smith et al. 2009). The material is likely photoionized by ultraviolet and X-ray emission from the Bright Ring (Hamilton & Sarazin 1984; Hamilton & Fesen 1998; Smith et al. 2009), and is relatively poorly studied and understood since it is only visible at select wavelengths. These ejecta are usually referred to as “unshocked ejecta” since they have yet to encounter the remnant’s reverse shock. That is not an entirely accurate label since Cas A’s forward shock, as well as shocks during the supernova explosion itself, have heated this material in the past. The central emission is ideal for exploring the conditions of the supernova explosion because ejecta interior to the Bright Ring have not yet interacted with the remnant’s reverse shock or circumstellar material, leaving them in a relatively pristine state.

Recent studies of optical spectra of the explosion near peak light obtained with light echoes have led to the observation of weak hydrogen lines, indicating a supernova Type IIb origin for Cas A (Krause et al. 2008). In this scenario, Cas A’s progenitor was the explosion of a red supergiant that had lost most, but not all, of its hydrogen envelope. The estimated oxygen mass of 1–3 M⊙ points to a main-sequence mass of about 15–25 M⊙ (Youn & Vink et al. 1996). X-ray studies indicate a total ejecta mass of less than 4 M⊙. If one adds to this the mass of the central compact object, presumed to be a neutron star (Chakrabarty et al. 2001), Cas A’s progenitor had a total mass of about 6 M⊙ immediately prior to the supernova explosion.
Spectropolarimetric observations of supernovae have shown that all observed core-collapse supernovae contain intrinsic polarization, indicating that there is a departure from spherical symmetry (Wheeler et al. 2005). An axisymmetric geometry, perhaps induced by jets, can be used to explain some features in some core-collapse supernovae, but significant departures from axial symmetry are needed to explain most observations (Wang & Wheeler 2008).

1.1. Previous Three-dimensional Studies

Global mappings of Cas A have been carried out in the optical, infrared, and X-ray. In the optical, three-dimensional Doppler reconstructions of the ejecta geometry primarily used S and O emission lines (Lawrence et al. 1995; Reed et al. 1995) and showed that ejecta on the Bright Ring lie on a spherical shell but do not uniformly fill that shell; most of the ejecta lie nearly in the plane of the sky. They also observe that the center of expansion of the ejecta is offset from the geometrical center of the spherical shell by \( \sim 0.36 \) pc, indicating that the ejecta are not traveling at the same velocity in all directions with respect to the central compact object. This is consistent with previous results which indicated a non-spherical expansion for the ejecta (e.g., Braun 1987; Willingdale et al. 2002). The three-dimensional reconstructions give us a selective “snapshot” of ejecta in the sense that only material that has recently encountered the remnant’s reverse shock will emit strongly in the infrared and especially in the optical and X-ray. Emission from material that has yet to reach the remnant’s reverse shock is not visible in the X-ray and optical. Currently, ejecta must be traveling at \( \sim 5000 \) km s\(^{-1}\) in order to be encountering the remnant’s reverse shock (Patnaude & Fesen 2007).

DeLaney et al. (2010) utilized a spectral mapping of Cas A from the Spitzer Space Telescope and the Chandra X-ray Observatory to make a three-dimensional infrared and X-ray map of the remnant. They found a similar distribution of ejecta to that seen in the optical and consistent with a model in which the remnant’s reverse shock is a nearly spherical structure \( \sim 1.5 \) pc in radius that is offset from the geometrical center of the remnant both in projection and along the line of sight (LOS).

X-ray Si/S and O emission is observed to be co-located in most regions (e.g., Ennis et al. 2006) in both the X-ray and infrared. This indicates that the two layers have very similar velocities (less than 80 km s\(^{-1}\) difference) so that they arrive at the remnant’s reverse shock at approximately the same time. However, strong evidence of elemental differentiation is found in some directions in the X-ray (e.g., Hughes et al. 2000), the optical (Fesen et al. 2006), and the IR (e.g., Smith et al. 2009; Ennis et al. 2006), which was likely caused by the different layers of the star being ejected at different velocities in those directions, thus encountering the remnant’s reverse shock at different times. In some regions, only material associated with the Si/S layer is currently encountering the remnant’s reverse shock, indicating that that layer has the “correct” velocity of \( \sim 5000 \) km s\(^{-1}\).

In other directions, Fe is currently seen at the remnant’s reverse shock, indicating that the Si/S and O layers may have a large enough velocity to have already passed through the remnant’s reverse shock and ionized up to states which are not detectable in the X-ray. Ennis et al. (2006) found regions where only Ne and O are encountering the reverse shock, indicating that the Si/S layer is traveling slowly enough that it has yet to reach the remnant’s reverse shock. Differentiation was also observed by Smith et al. (2009) in the form of variations in the Ar versus O + Ne abundances. The velocity separation between the various layers needs to be several hundreds of km s\(^{-1}\) in order for the layers to reach the reverse shock years apart and produce the differentiation observed.

We emphasize that we can only observe mixing or separation in velocity space. Simulations predict that the relevant nucleosynthetic layers will be \(<10^{11} \) cm thick prior to the explosion (e.g., Joggerst et al. 2009). If two such layers are ejected with different velocities, their physical separation will grow with time, and we can detect them individually as they sequentially encounter the reverse shock. However, if the layers were ejected at the same velocity, they would still form adjacent 10\(^{11} \) cm thick shells as they encountered the reverse shock, and we could not separate them. In addition to the overall shell velocity, there is likely small-scale turbulence which would stretch and broaden clumps and filaments to their observed widths of \( \ll 1'' \) (\( \sim 10^{-16} \) cm). If this turbulence also mixes the shells, but does not separate them in velocity space, then the layers will encounter the reverse shock at the same time/place. Thus, if we see separate layers, we know that there was a significant velocity difference between them. If we do not see separate layers, then either their velocities were the same, or they were physically mixed; we cannot separate those two situations.

1.2. Interior Emission

Previous IR observations also contain information about ejecta that have yet to encounter the remnant’s reverse shock (e.g., Smith et al. 2009). These are visible because some IR ionic lines, like the 34.81 \( \mu m \) [Si ii] line, will be photoionized by X-rays and UV light from the Bright Ring even if they have yet to reach the remnant’s reverse shock. They can therefore be visible interior to the remnant’s reverse shock or far beyond it if the ejecta passed through it decades ago (Chevalier & Oishi 2003).

In the case of Cas A, these interior ejecta give it a filled center appearance (Smith et al. 2009), as opposed to being dominated by the Bright Ring. DeLaney et al. (2010) show that this interior emission is organized into a “Thick Disk” structure, tilted at \( \sim 70° \) from the LOS. The material is moving perpendicular to that plane at \( \sim 2500 \) km s\(^{-1}\), indicating that it is only about half-way to the remnant’s reverse shock. Figure 1 illustrates the relationship between the remnant’s reverse shock, the Bright Ring, and the interior ejecta.

We present an analysis of a new, higher resolution Spitzer mapping of the ejecta toward the center of Cas A. In Section 2, we present the Spitzer observations. In Section 3, we discuss the methods used in our analysis and we describe those results in Section 4. Section 5 contains a discussion of the physical implications.

2. SPITZER OBSERVATIONS

The Spitzer Infrared Spectrograph (IRS) was used on 2007 August 30 to spectrally map select relatively bright regions of Cas A. This paper will address only the central map whose location is shown in Figure 2; a follow-up paper will address the other regions. High-resolution spectra (\( R \sim 600 \)) for all wavelengths were taken between 10–20 \( \mu m \) and 20–35 \( \mu m \) using the Short–High (SH) and Long–High (LH) modules, respectively. The full width at half-maximum of the lines at

---

7 Movies showing this three-dimensional structure are available at http://chandra.harvard.edu/photo/2009/casa2/animations.html.
No. 2, 2010 THE THREE-DIMENSIONAL STRUCTURE OF INTERIOR EJECTA IN CASSIOPEIA A 2061

Figure 1. Two-dimensional projection cartoon of the shock and ejecta structure showing the connection between the observations presented here and the model of DeLaney et al. (2010) as viewed from the top. The remnant’s reverse shock is a nearly spherical structure, while the ejecta are flattened nearly perpendicular to the plane of the sky. Only part of the reverse shock is observable, while sections of the remnant’s reverse shock that are not currently encountering ejecta are not currently observable (dashed black). Ejecta that are currently encountering the remnant’s reverse shock will be visible as mixed X-ray, IR, and optical emission (hashed and red), while ejecta interior to the remnant’s reverse shock will only be visible in select IR lines (gray). The approximate field of view of the current observations is indicated by the (green) box, within which are the different structures as discussed in Section 4.

(A color version of this figure is available in the online journal.)

Figure 2. 34.81 μm [Si ii] Spitzer IRS map and X-ray Si Chandra map of Cas A. The region of high-resolution data discussed in this text is indicated.

Figure 3. Typical spectra from the SH and LH Spitzer IRS modules of central emission of Cas A.

The spectra were reconstructed at each slit position, the background was subtracted, and three-dimensional cubes were created using the S17 version of the IRS pipeline and the CUBISM software package (Smith et al. 2007). The statistical uncertainties for each LOS were calculated using standard error propagation of the BCD level errors from the standard IRS pipeline.

In general, our uncertainties were limited by the undersampling of the IRS modules, which is worst at the short-wavelength end. This is a systematic error that exists in the wavelength calibration data themselves. It limits our obtainable absolute wavelength accuracy to roughly 1/2 of a spectral bin, or about 100 km s⁻¹, although the relative wavelengths for a given line can be measured with higher accuracy.

3. DATA ANALYSIS

Cas A’s infrared spectrum is dominated by bright ionic emission lines as shown in Figure 3. The LH observation contains lines from [O iv] and/or [Fe ii] at 25.9 μm, [S iii] at 33.48 μm, and [Si ii] at 34.81 μm. The SH observation has an [S iv] line at 10.5 μm, [Ne ii] at 12.8 μm, and another [S iii] line at 18.7 μm. The lines observed in the LH module typically have peak fluxes from 200 to 4000 MJy sr⁻¹, with an rms noise of ~ 15. Lines in the SH module have peak fluxes from 12 to 250 MJy sr⁻¹ and a typical rms noise of ~ 8. We also tentatively identify the 17.94 μm [Fe ii] line with 2σ significance when we spatially bin all pixels over the entire central region.

Observed emission near 25.9 μm could be from either the 25.89 μm [O iv] line or the 25.98 μm [Fe ii] line. In order to differentiate between the two lines, we compared the Doppler structure of the 25.9 μm line to that of the [Si ii] and 33.48 μm [S iii] lines for several LOSs. In Figure 4, we display the results for one LOS, showing the velocity structure of the [Si ii] line at 34.81 μm, the [S iii] line at 33.48 μm, as well as the 25.9 μm line under the assumption that it is composed entirely of either [O iv] or [Fe ii] emission. We obtain an excellent match...
under the assumption of [O iv], but a poor match under the assumption of [Fe ii]. The mismatch in Doppler structure under the assumption of [Fe ii] cannot be due to [Fe ii] simply having different velocities than [Si ii] and [S iii] since the [Fe ii] ejecta would have to be moving more rapidly than [Si ii]/[S iii] on the front side of the remnant and more slowly on the back side in order to produce the observed spectrum. Thus, it is clear that the velocity structure is consistent with the line being composed entirely of [O iv]. We find no LOSs that are consistent with having a substantial contribution from Fe. We assume for the remainder of this paper that the 25.9 μm line is entirely due to [O iv] emission.

The above analysis is based on the assumption of 25.8913 μm for the rest wavelength of the [O iv] line (Feuchtgruber et al. 1997). This differs from the earlier value of 25.913 μm (Froese Fischer 1983). Feuchtgruber et al. (1997) note that their results substantially improve upon the accuracy of previous values which were primarily based on energy level differences reconstructed from UV and optical spectroscopy.

Although [Si ii] and [O iv] match up well along single LOSs, the relative strength of [Si ii] and [O iv] varies considerably from place to place. Therefore, the total line shapes from all interior emission are considerably different for the two ions as shown in Figure 5.

### 3.1. Doppler Deconvolution

After background subtraction, we performed a Doppler deconvolution of the spectral lines from each ion separately using a spectral CLEAN algorithm (Ding et al. 1999) for each LOS. SH data cubes were binned 2 × 2 pixels (approximately 2′′ × 2′′) to increase the signal-to-noise ratio (S/N). A careful deconvolution is preferable to simpler techniques like measuring the peak wavelength of emission lines because the spectral CLEAN algorithm is able to separate partially blended components. An example of a CLEANed spectrum is shown in Figure 6. Note that flux in neighboring spectral bins was assumed to be from the same Doppler component. In this case, we combined the bins and determined the peak wavelength of the Doppler component by taking a weighted average of the wavelengths of the combined bins.

The spectral CLEAN was applied to each spatial pixel that had a signal greater than three times the offline rms. We note that at our spatial resolution (∼2′′), we may be binning over many individual knots. At the remnant’s reverse shock ejecta knots which have typical sizes as small as 0′′2–0′′4 are observed (Fesen et al. 2001). We do not know the spatial size of any clumping in the interior ejecta.

Uncertainties in Doppler velocity for a given Doppler component were determined by applying the spectral CLEAN to synthetic line data with a realistic range of S/Ns, and using actual line-free data for the noise model. From these simulations, we determined the rms error in velocity as a function of line strength and location of the line peak within a spectral bin. In all cases, the uncertainty in velocity for a single, isolated Doppler component was determined to be less than 25 km s⁻¹. This means that our uncertainties in the absolute velocities are limited by the systematic errors in the calibration of about 100 km s⁻¹ rather than random uncertainties, while the relative velocities for any given line are less than 25 km s⁻¹. We could not detect two separate components that were within 65 km s⁻¹ of one another in synthetic data.

We assume that the ejecta have been freely expanding at a constant velocity in order to determine their spatial coordinate perpendicular to the plane of the sky. This assumption is still valid despite the fact that the ejecta were likely decelerated by shocks during the supernova explosion itself—any deceleration happened at the time of the explosion (that is, near t = 0, z = 0, where z is the spatial coordinate perpendicular to the plane of the sky), so the behavior is virtually identical to free expansion at a reduced velocity. We transformed our Doppler velocities to z-axis spatial coordinate in Figure 7, but leave the z-axis in velocity units in Figures 8–13. The flux from each component is displayed by varying the transparency; the brightest voxel for a given ionic line is 80% opaque, while the opacity of all other voxels is linearly scaled downward as a function of the intensity of the Doppler component.

We note that our results are consistent with the lower spectral resolution results of DeLaney et al. (2010). When plotted on the same axes, the ejecta detected in both observations trace out similar structures as shown in Figure 7, although our superior
4. RESULTS

4.1. Three-dimensional Map

We plot the Doppler components from the three strongest lines in Figures 8–10—the 25.89 μm [O iv] line, the 34.81 μm [Si ii] line, and the 33.48 μm [S iii] line. The other lines are either very weak (in the case of Ne and Fe) or trace out identical structures as other lines from the same element (in the case of the other S lines). The velocity axis has been stretched by a factor of 1.8 in order to highlight the velocity structures discussed in the text. The thinness of the Sheet is shown in the figure to the right, where the Sheet’s thickness is roughly the minimum thickness allowed by the plotting symbols.

The most striking aspect of this emission is that the center of the remnant is not uniformly filled, but consists of distinct structures. We label the material on the back side of the remnant spectral resolution ($R \sim 600$ versus $R \sim 100$) allows us to detect many details that were previously not observed.
Figure 9. Three-dimensional plot of the 34.81 μm [Si ii] line. The central solid box (red) denotes the location of the central compact object. The velocity axis has been stretched by a factor of 1.8 to highlight the velocity structures discussed in the text.

Figure 10. Three-dimensional plot of the 33.48 μm [S iii] line. The central solid box (red) denotes the location of the central compact object. The velocity axis has been stretched by a factor of 1.8 to highlight the velocity structures discussed in the text.

Figure 11. Three-dimensional [Si ii] (green) and [S iii] (yellow) map on the same axes. The two lines overlap very strongly.

4.2. Ejecta Structure Asymmetry

There is a striking front–back asymmetry in the geometrical structure of the ejecta. The Si, S, and O ejecta in the Sheet have a very narrow velocity profile—along any given LOS all of the material has only one Doppler component. The structure itself is remarkably well formed in that in almost all places it is <65 km s\(^{-1}\) thick—the minimum thickness allowed by our observations. The ratio between the O and Si lines varies considerably—some regions appear almost entirely in one line or the other. As will be discussed in Section 5.5, we do not know if this is due to actual elemental abundance variations or variations in line strength due to density and temperature variations. The structure is nearly continuous except for a hole in the structure in both Si and O (indicated in Figure 8).

In the Filament Band, the material forms an interwoven filamentary structure. About half of the LOSs contain more than one Doppler component. In general, the filaments are nearly as narrow as possible given our spectral and spatial resolution as the “Sheet,” the material on the front side of the remnant as the “Filament Band,” and the material between the two as the “Bridge.” The Si and S lines trace out essentially identical structures as seen in Figure 11.

The Filament Band and the Sheet are orientated at 10°4 and 16°4, respectively, with respect to the plane of the sky. This is consistent with the range of ∼25° ± 15° in orientation across the Thick Disk observed in the low-resolution study (DeLaney et al. 2010).
The velocities of ejecta in the Sheet vary from ~2000 to 4600 km s\(^{-1}\), going from east to west. The strongest concentration of Si emission is at ~3000 km s\(^{-1}\), while the O is spread more evenly over the velocity range.

The average velocity of the ejecta in the Filament Band region ranges from ~1500 to ~3800 km s\(^{-1}\), going from west to east. The strongest concentration of Si emission in the Filament Band is at ~1600 km s\(^{-1}\), much slower than the Si in the Sheet. The O has a larger spread in velocities, but there is substantial O flux at velocities around ~1500 km s\(^{-1}\), 500 km s\(^{-1}\) slower than any O emission in the Sheet.

Put together, our observations indicate that ejecta in the Filament Band region are typically traveling ~900 km s\(^{-1}\) more slowly than ejecta in the Sheet region.

### 4.4. Radial Velocity Profile Asymmetry

We define the radial velocity profile across nucleosynthesis layers as the mass of the ejecta that are traveling at a given radial velocity for each element. Examples of two radial velocity profiles are shown in Figure 13. We can characterize the radial velocity profiles of the original supernova explosion by determining if different nucleosynthetic layers are separated in velocity space. If we observe that Si and O are separated, then we know that Si and O were ejected at different velocities and thus have different radial velocity profiles.

We can qualitatively see a variety of radial velocity profiles in our data. The O and Si in the Sheet appear to be strongly overlapping in Figure 12 where [O \(\text{iv}\)] and [Si \(\text{ii}\)] emission are plotted on the same axes, indicating that two elements were ejected at the same velocity. We quantify the velocity separation between Si and O in the Sheet as follows: for each Si component with flux greater than 100 MJy sr\(^{-1}\), we found the nearest O component along the same LOS provided that its velocity was within 1000 km s\(^{-1}\) of the Si velocity and its flux was greater than 100 MJy sr\(^{-1}\). We plotted the Si velocity vs. O velocity from all LOSs in Figure 14. If the elemental layers had identical velocity profiles, the velocities would be equal. We find that the slope of the best-fit line of the combined data and forced to pass through the origin is 1.015 \(\pm\) 0.0025. This corresponds to the O having a mean velocity 45 \(\pm\) 14 km s\(^{-1}\) greater than the Si at the average position of the Sheet. Since any separation between Si and O is less than the \(\sim\)100 km s\(^{-1}\) uncertainty induced by systematic errors, we conclude that the mean Si and O velocities are identical, within that limit, when both elements are visible.

The rms scatter of the points about the best-fit line is 75 km s\(^{-1}\). This is much larger than the random uncertainty.
in velocity, which is always less than 25 km s\(^{-1}\) in both O and Si velocities. This indicates that the scatter is not statistical or instrumental in nature, but is a real variation in the supernova ejecta itself. However, this scatter is very small—it represents a variation of only \(\sim 1\%\) in the average ejecta velocity in the Sheet.

Turning now to the Filament Band, in roughly half of the filaments we find no separation between the O and Si velocities. The other half of the filaments are composed almost entirely of either O or Si. The filaments have characteristic separations of order 500 km s\(^{-1}\). This separation cannot be due to contributions from both [O \(iv\)] and [Fe \(ii\)] since we would be able to individually resolve both the [Fe \(ii\)] and [O \(iv\)] lines if both elements were present. We are also not mistaking the [O \(iv\)] emission for [Fe \(ii\)] since the difference in rest wavelengths would result in a velocity change of \(\sim 1000\) km s\(^{-1}\). Thus, the filaments would still be separated even if we were detecting Fe emission.

We do not attempt to directly compare the Si and O velocities in the Bridge or Filament Band overall, since the ejecta from each element in those regions are often in completely different structures.

We note that the radial velocity profile for every LOS in the Sheet must be very strongly peaked in both Si and O because we observe one and only one velocity for both elements. However, the radial velocity profile in the Filament Band is much broader since we can see a range of velocities in many LOSs.

### 4.5. Line Fluxes

We determine line ratios of the 18 and 33 \(\mu m\) [S \(iii\)] lines for several LOSs. These lines can be used to determine the density of the ejecta (assuming that they are at a high enough density and temperature) by balancing the collisional excitation and de-excitation rates as well as radiative transitions into and out of the relevant energy levels (e.g., Osterbrock & Ferland 2006). Smith et al. (2009) used this diagnostic on data that had not been deprojected and found that all LOSs in our field of view had ejecta with electron densities \(< 100\) cm\(^{-3}\), the lower limit of this density diagnostic. We attempted to identify any Doppler components with densities \(> 100\) cm\(^{-3}\) by determining the [S \(iii\)]/S \(iv\) ratio for the five Doppler components with the strongest 18 \(\mu m\) line. However, in all cases we found that the electron density is \(< 100\) cm\(^{-3}\), confirming the results of Smith et al. (2009).

We give the integrated line fluxes for two Doppler components from the same LOS in Table 1 as an example of typical values. Note the variation in the [S \(iii\)]/S \(iv\) ratio between the two components, which demonstrates that it is often necessary to deconvolve the data before attempting to extract information from line ratios. We find that this [S \(iii\)]/S \(iv\) ratio varies between roughly 0.02 and 0.4 for deconvolved components, with most ratios around a value of 0.05. Since we do not yet have the appropriate models to determine physical conditions from these line ratios, we defer further discussion of line ratios to a future paper. We address the need for additional modeling in Section 5.5.

### 4.6. [Ne \(ii\)] Map

Although the 12.8 \(\mu m\) [Ne \(ii\)] line is too weak to extract a substantial number of individual Doppler components, we can map the [Ne \(ii\)] flux distribution over our field of view. We compare this map to a 25.9 \(\mu m\) [O \(iv\)] flux map in Figure 15. Naively, we expect substantial similarities between the two maps since the elements come from the same nucleosynthetic layer. However, the two maps do not show a strong correlation. We briefly address potential reasons for these differences in Section 5.5.

### 5. DISCUSSION

#### 5.1. Supernova Model Background

One of the great outstanding problems in theoretical astrophysics is the basic nature of core-collapse supernova explosions. In contrast, the structure of the star before the supernova explosion is relatively similar for all models. As the massive star fuses different elements during hydrostatic burning, it should produce denser and denser concentric nucleosynthesis layers, forming the classic “onion-skin” model of the star. We concentrate on the central layers of the star—the dense Fe/Ni core, the Si/S layer immediately above the core, and the O/Ne layer above the Si/S.

Any mixing between the layers during the supernova explosion itself could be caused by either partial explosive O burning (Chevalier & Kirshner 1979) or mixing between layers caused by large-scale Rayleigh–Taylor instability fingers created by...
The shocks during the supernova explosion (Winkler et al. 1991). However, our observations indicate that the Rayleigh–Taylor filament scenario is more likely since we observe filamentary structures in ejecta which have not yet encountered the remnant’s reverse shock and there is no obvious way that partial explosive O burning could create Si filaments radially flanked by O filaments. Therefore, we do not further discuss any scenarios based on mixing by explosive nucleosynthesis.

Although the initial conditions are well understood, the nature of the piston responsible for the explosion itself is not, with most groups proposing neutrino-driven shocks, while others utilize diffusive, magnetic buoyancy or neutrino-bubble instabilities (Janka et al. 2007). Regardless of the exact nature of the piston, many predictions about the early shock structure of the supernova explosion can be made. As the primary piston drives outward, it causes a forward shock and eventually sweeps up enough material in the star to form a reverse shock within the star itself (Herant & Woosley 1994). This “Explosion Reverse Shock” forms about $10^3$–$10^4$ s after the beginning of the supernova explosion and takes ~$10^2$ s to reach the center of the star (Joggerst et al. 2009). This is different to the “Remnant Reverse Shock,” which formed ~$10^2$ years later in Cas A when the forward shock swept up enough material to cause the Remnant Reverse Shock to separate (Miles 2009), and has not yet reached the center of the remnant. Figure 16 illustrates the distinction between these two reverse shocks.

The Explosion Reverse Shock forms in the outer layers of the star and propagates toward the center of the star, forcing the less dense outer nucleosynthetic layers into the denser layers deeper within the star. This can cause mixing between the layers and potentially forms filaments from Rayleigh–Taylor instabilities (Herant & Woosley 1994). The amount of mixing and degree of filamentation depend on the speed of the reverse shock, which can vary by roughly an order of magnitude in models of stars with different masses (Joggerst et al. 2009). A strong and fast Explosion Reverse Shock can cause complete mixing between many layers and prevents the production of filaments because it sweeps by so quickly that filaments do not have time to grow. The signature of this phenomenon is well-mixed sheets of ejecta. On the other hand, a slower Explosion Reverse Shock can result in large filaments because it moves slowly enough that the filaments have time to develop. A very weak shock would not be strong enough to cause much mixing at all between most elements, leaving the nucleosynthetic layers spatially separated (Joggerst et al. 2009).

The Explosion Reverse Shock simultaneously modifies the radial velocity profile of the ejecta across concentric nucleosynthetic layers. Elements that have been well mixed by the Explosion Reverse Shock (indicating a strong and fast Explosion Reverse Shock) should have nearly identical velocities upon ejection, while unmixed layers (indicative of a weaker and slower Explosion Reverse Shock) can have velocities that differ by 1000s of km s$^{-1}$. This is a key distinguishing feature between supernova models. Some models predict that the Si/S and O layers will have essentially identical velocities, while other models predict that the layers can be separated by 1000s of km s$^{-1}$ (Figure 14—Joggerst et al. 2009; Kifonidis et al. 2006). Even within very similar models, the separation between layers can be a function of the initial conditions within the explosion—Joggerst et al. (2009) predict that the Si/S and O layers will have nearly identical velocities for 25 M$_\odot$ solar metallicity stars, while they will be separated by ~1000 km s$^{-1}$ for 15 M$_\odot$ solar metallicity stars.

An alternative to spherical shocks is a jet-induced supernova explosion (e.g., Burrows et al. 2007). In this scenario, the explosion is dominated by magnetohydrodynamic jets created in rapidly rotating stars. When these stars explode, the jets induce a bipolar outflow and create powerful bow shocks as they move through the star. These transverse shocks eventually collide at or near the equator of the star, leading to a torus of ejecta about the star’s equator (e.g., Khokhlov et al. 1999). Stars with moderate
rotation may have supernovae with both spherical and weak transverse jet-induced shocks (Burrows et al. 2007).

5.2. Nature of the Explosion

We can use supernova explosion models as a guide to which physical properties may influence the observed asymmetries. The fundamental cause of the ejecta structure, the ejecta velocity, and the radial velocity profile asymmetries described in this paper may be variations in the Explosion Reverse Shock, which were potentially caused by the variations in the forward shock. In this model, the Explosion Reverse Shock was very strong and moving very quickly in some directions, leading to the Sheet structure where the elements are mixed in velocity space and no filaments are seen. In other directions it was slower, leading to filaments composed of both Si and O. In yet other directions it was very weak and slow, leading to well-separated filaments.

Other potential sources of asymmetries are those that form in the forward shock within the first ~100 ms in the models of Burrows et al. (2007) as well as the standing acoustic shock instability (SASI) models of Blondin et al. (2003). These instabilities allow the initially steady-state, spherically symmetric forward shock to become highly asymmetric in just a few crossing times (Blondin et al. 2003). The origin of these instabilities is the response of the post-shock pressure to changes in the forward shock radius and happens while the forward shock is roughly stationary and still very near the core of the star. If the pressure in one region becomes only slightly higher than the pre-shock ram pressure profile, positive feedback and a shock displacement leads to smaller pressure behind the forward shock. In this model, the Explosion Reverse Shock was very symmetric forward shock to become highly asymmetric in just a few crossing times (Blondin et al. 2003). The origin of these instabilities is the response of the post-shock pressure to changes in the forward shock radius and happens while the forward shock is roughly stationary and still very near the core of the star. If the pressure in one region becomes only slightly higher than the pre-shock ram pressure profile, positive feedback and a shock displacement leads to smaller pressure behind the forward shock. In this model, the Explosion Reverse Shock was very symmetric.

Jet-induced supernova explosions do not appear to be an attractive alternative for explaining our observations of Cas A. The distinct, tilted front/back structures that we report here and are part of the DeLaney et al. (2010) “Thick Disk” are not orientated correctly to be formed as a torus in a jet-induced supernova explosion. They are nearly in the same plane as the jet/counterjet, not perpendicular to it as the jet models require. While the jets do produce a slight bipolar asymmetry in the ejecta, there is no obvious way in which the jets cause most of the ejecta asymmetries described in Section 4. Furthermore, Cas A’s jets do not appear to have enough kinetic energy in order to cause the supernova explosion (Laming et al. 2006).

Wheeler et al. (2008) propose that the structures normally called the “jet” and “counterjet” are not the main jets, but rather secondary instabilities. In this model, the jets responsible for the explosion are two notable Fe blowouts located in the southeast and northwest of the remnant. However, the three-dimensional reconstructions of DeLaney et al. (2010) show that these two blowouts do not form an axis. The Fe blowouts are also not nearly perpendicular to the “Thick Disk” as expected in a jet-induced explosion.

We do not consider jets as the source of Cas A’s asymmetries any further since neither jet-induced scenario seems to be plausible.

Other models can also produce ejecta asymmetries from rotation without using jets to induce the supernova explosion. However, the published results of such models (e.g., Kifonidis et al. 2006) do not document any of the key asymmetries in ejecta structure, velocity, and radial velocity profile that we need to compare with the current observations. It is clear that one key to understanding and reproducing the asymmetries is to have models that predict the average ejecta velocity as well as the radial velocity profile as a function of direction.

5.3. Relationship Between the O and Si/S Layers

X-ray observations have led to the suggestion that Cas A’s nucleosynthetic layers have undergone large-scale overturning in some regions, causing less dense layers to be interior to layers which originated closer to the star’s core (e.g., Hughes et al. 2000). In most directions, we find no evidence of this overturning as the O and Si/S layers are nearly perfectly correlated in velocity space (see Figures 12 and 14). This is consistent with IR and X-ray observations that indicate that Si/S and O emission is co-located on much of the Bright Ring (e.g., Ennis et al. 2006). However, in part of the Filament Band we do find substantial separation between nucleosynthetic layers. This is roughly consistent with the separation between layers seen in the X-ray, but does not correspond to a simple overturning of the layers since the O layer is observed on both sides of the initially denser Si/S layer in velocity space.

While this intertwining of O and Si/S layers may be evidence of some sort of mixing between nucleosynthetic layers in some parts of the star, it does not apply in other directions. Future supernova explosion models that better address the asymmetries seen in Cas A may shed light on this interesting phenomenon.

We also note that our results are similar to those of Fesen et al. (2006). Based on Hubble Space Telescope observations of select regions of the remnant, they also concluded that there was substantial spatial variation in the degree of mixing of the layers in Cas A. Their data consisted of knots composed of lighter elements that originated in the outer layers of the star; our results show that the variability in mixing remains even down to the denser interior layers.

5.4. Velocity Offset

Previous authors observing ejecta in the optical found that the center of expansion of the ejecta was offset along the LOS from the geometrical center of the partial spherical shell (caused by ejecta interacting with the Remnant Reverse Shock) by ~770 km s\(^{-1}\) (Reed et al. 1995). Our new IR results are roughly consistent with this result—we find an offset of ~900 km s\(^{-1}\) along our LOS in the same direction. However, Reed et al. (1995) speculated that this was due to a difference in density of the circumstellar material between the back and front of the remnant. This is inconsistent with our data—the interior ejecta visible in the infrared are unaffected by the circumstellar material because they have not yet encountered the Remnant Reverse Shock. Thus, we believe that this velocity offset is the result of an asymmetry in the supernova explosion itself rather than an asymmetry in the circumstellar material.

5.5. Interior Conditions

Our observations raise an interesting puzzle with respect to Fe. We do not definitively detect any Fe in the interior, despite Fe II, Fe III, and Fe VII lines within the wavelengths accessible to Spitzer’s IRS module. This could be due either to a lack of Fe in the interior of the remnant or because the Fe present is not in the correct physical conditions to emit detectable lines.
We believe that the latter scenario is more likely since recently shocked Fe is observed on the Bright Ring (e.g., Hughes et al. 2000; Eriksen et al. 2009) and we know of no mechanism which would force all the Fe, and only the Fe, to be ejected only in a narrow torus.

One possible solution to this puzzle is that the Fe is at lower density than the observed Si and O. There are multiple explanations for how this may occur, but we will discuss only one here. Although the Ni/Fe layer is initially more dense than the Si/S and O layers, it may not have experienced the same modifications to its density distribution as the outer layers. For example, if the Explosion Reverse Shock lost most of its energy before it reached the Fe/Ni core, it would not cause the Rayleigh–Taylor filamentation that is likely responsible for the dense knots of Si/S/O that we observe in the interior. The phenomenon of density enhancements to outer layers but not the core is seen in some of the models of Joggerst et al. (2009). Fe may not be observable without this density enhancement. A similar puzzle arises with respect to the Si and O lines. In some regions with coherent structure like the Sheet, we see emission which is almost entirely O or Si. These variations in line strengths could be due to either variations in local abundance ratios between the elements or density and temperature variations. We find that the brightness of a region in Si is uncorrelated with how bright it is in O and vice versa.

Similarly, we observe that the [Ne II] and [O IV] maps show substantial differences although both elements came from the same nucleosynthetic layer. We speculate that this is because the emissivity of the two lines is a function of density and temperature, and the variation in line flux is therefore reflecting a variation in physical conditions.

We look forward to future models which balance photoionization rates (as opposed to the collisional ionization rates used in the usual 18/33 μm [S II] diagnostic) in order to determine line ratios as a function of temperature and density. These models should be able to probe the low temperatures and densities present in Cas A’s center. Not only will we be able to better address the puzzles presented above, but we will also be able to better constrain the temperature and density of the interior ejecta.

5.6. Predictions for the Next 30–500 Years

Cas A’s appearance in the X-ray is dominated by ejecta which have recently encountered the Remnant Reverse Shock. Thus, the central ejecta arriving at the Remnant Reverse Shock will mark a transition after which Cas A will contain bright central emission in the optical and X-ray. This situation will be analogous to the SNRs N132D (Blair et al. 2000) and Puppis A (Winkler & Kirschner 1985). Like in N132D, we will observe a ring of ejecta with arcs and clumps of bright, recently shocked ejecta interior to the ring. We note that the two scenarios are not an exact analog since N132D’s appearance is dominated by its forward shock interacting with the surrounding environment. The remnant will still be a shell morphology remnant (since the ring will be limb brightened), but a substantial fraction of the overall X-ray emission will be from shocked ejecta in the interior. However, like in Puppis A, we expect the central ejecta to be O rich since our IR observations detect strong O lines in the interior ejecta.

We can make explicit predictions about when the central ejecta should encounter the Remnant Reverse Shock with our knowledge of the current velocity structure of the ejecta and by assuming, in the limiting case, that the Remnant Reverse Shock is roughly stationary in the current epoch (Morse et al. 2004). On the back side of the remnant, we expect the Sheet to begin arriving at the Remnant Reverse Shock in slightly under 30 years at about R.A. 23:23:25 and decl. 58:48:5. The X-ray and optical emission may initially be dominated by O group emission, since the part of the Sheet with the highest velocity is dominated by O emission in our observations. The greatest concentration of Si group emission on the back side of the remnant should arrive at the Remnant Reverse Shock in approximately 220 years. If the Remnant Reverse Shock actually begins moving inward in the external reference frame during this period, then these times will be shorter.

On the front of the remnant, the ejecta in the Filament Band will begin to arrive at the Remnant Reverse Shock in about 100 years. The ejecta in the Filament Band with the largest velocity are the overlapping filaments, so the emission will initially be strong in both O and Si. The separated filaments will begin to arrive at the reverse shock in about 260 years. The emission will initially be dominated by O. The Si group emission should begin about 500 years from the present time in this direction and will be followed by more O group dominated emission several decades later. We note that the substantial separation in arrival times of the O and Si groups in this direction is consistent with the Ennis et al. (2006) result in which emission in some regions is observed to contain almost exclusively O and Ne, with little Si.

6. CONCLUSIONS

We create a three-dimensional reconstruction of the central ejecta of Cas A at unprecedented spectral resolution using photoionized infrared ionic lines. We observe a large number of asymmetries that are most likely caused by asymmetries in the supernova explosion itself rather than the circumstellar environment. Si and O emission with nearly identical velocities are seen in co-located sheets less than 100 km s\(^{-1}\) thick on the back side of the remnant. Toward the front, by contrast, we observe filaments with both Si and O present, while along different LOSs we observed well-separated Si and O filaments that are roughly consistent with X-ray observations. The average velocity of all ejecta varies strongly as a function of direction. We observe that the interior emission is offset by \(\sim 900\) km s\(^{-1}\) along our LOS as was previously observed in the optical. However, we do not believe that this asymmetry was caused by the circumstellar environment because the interior ejecta cannot be affected by the interstellar medium until they reach the forward shock. We hypothesize that the asymmetries could be produced by asymmetries in the Explosion Reverse Shock.

Photoionization models are required in order to determine the density, temperature, and ionization state of the center of the remnant. These models are likely to be produced in the near future and will allow us to further address the central conditions of the remnant. One key question to be answered is whether or not the lack of a detection of any Fe lines indicates a lack of interior Fe, or that the Fe is present, but not in the correct physical state to produce observable lines.

Finally, we note that Cas A will provide an even more fertile ground for future observations as the interior ejecta encounter the front and back Remnant Reverse Shocks, starting in \(\sim 30\) years.

This work is based on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion
Laboratory, California Institute of Technology under NASA contract 1407. This work was supported in part by NASA/SAO Award AR5–66008X and NASA/JPL through award 1265552 to the University of Minnesota.

K.I. thanks Alex Heger for valuable conversations concerning supernova explosion physics. K.I. also thanks Kris Eriksen for his insights concerning photoionization models of the interior emission in Cas A. We also appreciate the useful comments of the referee.

REFERENCES

Tananbaum, H. 1999, IAU Circ., 7246, 1