Digital Signaling and Hysteresis Characterize Ras Activation in Lymphoid Cells

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SUMMARY

Activation of Ras proteins underlies functional decisions in diverse cell types. Two molecules, RasGRP and SOS, catalyze Ras activation in lymphocytes. Binding of active Ras to SOS’ allosteric pocket markedly increases SOS’ activity establishing a positive feedback loop for SOS-mediated Ras activation. Integrating in silico and in vitro studies, we demonstrate that digital signaling in lymphocytes (cells are “on” or “off”) is predicated upon feedback regulation of SOS. SOS’ feedback loop leads to hysteresis in the dose-response curve, which can enable a capacity to sustain Ras activation as stimuli are withdrawn and exhibit “memory” of past encounters with antigen. Ras activation via RasGRP alone is analog (graded increase in amplitude with stimulus). We describe how complementary analog (RasGRP) and digital (SOS) pathways act on Ras to efficiently convert analog input to digital output. Numerous predictions regarding the impact of our findings on lymphocyte function and development are noted.

INTRODUCTION

Activated Ras proteins regulate several cellular processes by acting on many substrates to affect signaling through diverse pathways (e.g., the MAPK pathway) (Campbell et al., 1998; Mor and Philips, 2006). Membrane-bound Ras proteins shuttle between inactive (GDP-bound) and active (GTP-bound) states. RasGDP binding to guanine nucleotide exchange factors (GEFs) results in nucleotide release, enabling nucleotide-free Ras to bind more abundant cellular GTP (Campbell et al., 1998). The intrinsic GTPase activity of Ras is enhanced by Ras GTPase-activating proteins (RasGAPs) that promote Ras deactivation (Campbell et al., 1998).

Ras activation is important for the development of T and B lymphocytes and for their effector functions directed against invading pathogens (Genot and Cantrell, 2000). Antigen receptor stimulation of lymphocytes triggers uniquely high levels of Ras activation (Genot and Cantrell, 2000). Two families of RasGEFs are well studied in lymphocytes: RasGRP1 and RasGRP3 (Ras guanyl nucleotide release protein) and SOS1 and SOS2 (Son of Sevenless) (Ebinu et al., 2000; Roose et al., 2005, 2007). RasGRP proteins, mainly restricted to the nervous and hematopoietic systems, are activated by binding to membrane-localized diacylglycerol and by phosphorylation by protein kinase C (see Figures 2A and 4A). SOS proteins are ubiquitous and are recruited to sites of receptor or adaptor tyrosine phosphorylation. SOS’ activity is regulated by membrane localization and is greatly accelerated upon binding of active RasGTP to a noncatalytic (allosteric) site (Margarit et al., 2003). The functional consequences of such feedback regulation of SOS’ activity, and its interplay with the other GEF, RasGRP, were unknown.

An important issue in cell biology is to understand how cells respond in a decisive manner (digital) to the graded (analog) input of increasing amounts of receptor stimulation. Employing synergistic in silico and in vitro methods, we find that signaling in a population of lymphocytes is digital in character, i.e., a bimodal response emerges as stimulus is increased past a threshold. Digital signaling in individual cells requires SOS-mediated Ras activation. A further unanticipated characteristic of Ras activation via SOS is hysteresis in the dose-response curve, i.e., the response to the same stimulus dose depends upon whether the prevailing level of stimulus is achieved by increasing or decreasing the stimulus from its previous value. Our results
suggest that bimodal responses and hysteresis also provide a mechanism for short-term molecular “memory,” making it easier to activate membrane-proximal signaling in previously stimulated cells. This may enable T lymphocytes to integrate signals from serial encounters with rare antigen-bearing cells.

We find that Ras activation via RasGRF alone increases in a graded fashion with stimulus (analog) and does not exhibit hysteresis. This is because, unlike SOS, RasGRF’s activity is not regulated by a positive feedback loop. Our results show how tuning the interplay between two complementary digital and analog signaling modules that activate the same substrate (Ras) leads to more efficient digital responses than if the digital pathway alone was employed. This may be a principle used broadly in biology.

Positive feedback regulation is one of many nonlinear mechanisms that can result in “digital” responses of gene regulation programs and signaling networks (Barkai and Leibler, 2000; Bhalla and Iyengar, 1999; Elf and Ehrenberg, 2004; Ferrell, 2002; Khodolenko et al., 2002; Kussell et al., 2005; McAdams and Arkin, 1997). We describe an example of how positive feedback regulation of a signaling module embedded in a complex signaling network leads to functionally important consequences in cells that orchestrate adaptive immunity. The concepts revealed by our study lead to a number of testable predictions pertinent to lymphocyte development and their ability to be activated in vivo by small doses of stimulatory ligands.

RESULTS

A Positive Feedback Loop that Regulates SOS Activity

Results in Digital Signaling

Stimulated tyrosine kinase receptors (e.g., growth factor receptors, T cell receptors) recruit SOS to the plasma membrane by the adaptor molecule, Grb2 (Genot and Cantrell, 2000). The Rem and Cdc25 domains in SOS are required for its GEF catalytic activity (Figure 1A), and we refer to them together as SOScat (SOS catalytic domain). SOS itself has very low GEF activity. Crystallographic and biochemical studies as well as experiments with cell lines show that the activity of SOScat is strongly influenced by a second Ras binding site that is distal to the GEF catalytic site (Margaret et al., 2003). Binding of RasGRF to this allosteric pocket results in a 5-fold increase in GEF activity, whereas binding of RasGTP effects a much larger (~75-fold) increase (Freedman et al., 2006; Sondermann et al., 2004). Thus, SOS-mediated Ras activation involves positive feedback regulation by its own catalytic product, RasGTP (Figure 1A).

The activity of full-length SOS is inhibited by both N-terminal and C-terminal regions that flank SOScat (Figure S2A available online). Recruitment of SOS to the plasma membrane results in conformational changes that relieve this inhibition and allow RasGDP to bind to SOS’ catalytic site (Corbalan-Garcia et al., 1998). Binding of membrane phosphatidylinositol-4,5-bisphosphate (PIP2) to SOS’ N-terminal PH domain further augments SOS’ activity (Gureasko et al., 2008). In agreement, expression of SOS1cat without these flanking sequences results in Ras signaling without the need for membrane targeting or external stimulus (Roos et al., 2007). We explored the consequences of positive feedback regulation of SOS by developing a mathematical model for the signaling module in Figure 1B wherein SOScat is uninhibited.

We first ignored stochastic fluctuations (van Kampen, 1992) in the number of molecules participating in signaling and developed a deterministic model describing the temporal evolution of the most probable number (or concentration) of the proteins involved in Ras activation via SOScat (Figure 1B). Table 1 summarizes the values of rate parameters that appear in the equations (Experimental Procedures). Only the ratios of certain parameters had been measured. Varying the individual parameters by factors of at least ten while keeping the ratio fixed did not affect the qualitative results (Figures S2–S4).

Figure 1C shows the theoretical steady-state dose-response curve for Ras activity as the amount of SOScat (a) is varied. For low or high levels of SOScat, there is one possible state characterized by low or high levels of active Ras, respectively. However, for intermediate levels of SOScat, three states of Ras activity are possible. The states shown in blue are unstable to small perturbations, and these states could exist only fleetingly. Therefore, for intermediate levels of SOScat, two possible dominant states of Ras activity could be simultaneously observed, i.e., a bistability is predicted. As the amount of SOScat is increased, the system could follow the lower stable branch until this was no longer possible, and then there would be a large jump in Ras activity (at point A). Thus, the dose-response curve could be very sharp. Importantly, bistability and the concomitant sharp threshold are abrogated if the positive feedback loop regulating SOS’ GEF activity is removed from the model (green line in Figures 1D and S2E).

Formulas obtained from a detailed analytical study (Supplemental Data, Section VI) suggest that, in addition to feedback regulation of SOS, the minimal requirements for bistable Ras activity are (1) catalytic Ras activation by SOS, with RasGTP bound to the allosteric site and (2) catalytic deactivation of RasGTP by RasGAPs. These features are true. The analytical treatment of simplified models also supports our numerical parameter sensitivity studies, which show that our qualitative results are robust to wide variations in parameters as long as the basic ingredients described above are present.

We then investigated the potential effect of Ras activation via RasGRF1 on the bistable Ras activity driven by SOScat. A GEF, RasGRF, which is structurally related to RasGRF, is not dependent on feedback regulation by Ras (Freedman et al., 2006). So, we assumed that Ras is activated by RasGRF without feedback and used the measured rate parameters for RasGRF since those for RasGRF are unknown. As shown in Figure 1E, bistability and sharp responses are predicted to disappear if RasGRF levels (or activity) are very high. This is because RasGRF activity, which is not subject to feedback regulation, can convert most Ras molecules to its active form before the SOS feedback loop is engaged. Figure 1E also shows that low levels of RasGRF activity reduce the threshold for SOScat (a) to induce a sharp response. We show later that this is because absence of RasGRF makes it difficult to ignite the positive feedback loop regulating SOS’ GEF activity. These results suggest that an optimal level of expression or activity of RasGRF, the analog route to Ras activation, enables efficient deployment of feedback regulation of SOS, which leads to bistability.

To explore the manifestations of these characteristics of Ras activation in lymphocytes (where stochastic variations between stimulated cells can be important), we carried out stochastic computer simulations of signaling events that might occur in lymphocytes (Figure 2A). The simulations were carried out using the Gillespie algorithm (Gillespie, 1977), which has been used...
RasGTP emerges; the histogram is bimodal (Figure 2B). Thus, are either "on" or "off" with regard to Ras activation. Such as the MAPK pathway (Ferrell, 2002; Kholodenko et al., 2007), but activation of signaling molecules downstream of CD69 by individual cells using flow cytometry. CD69 levels examined upregulation of a cell-surface activation marker must be activated by endogenous Ras molecules. In this type of assay, not all transfected cells start to express SOS1cat synchronously and SOS1cat-expressing cells transit from low CD69 to high CD69 expression. It is therefore difficult to ascertain whether the response is bimodal or not by visual inspection. We adapted Hartigan’s test (Hartigan and Hartigan, 1985), which allows for a qualitative determination of whether a response in a population of cells is bimodal or unimodal. The generated histograms were divided into 120 equal portions and the mean fluorescence of CD69 and the number of cells in each portion were determined. Hartigan’s test confirmed that intermediate levels of SOS1cat when combined with H-RasG9E38, but not with WT H-Ras, restored bimodal signaling to higher values of RasGTP. Rather, beyond a threshold value of low levels of SOScat, all simulations result in low levels of RasGTP, resulting in a single corresponding peak in the histogram. As SOScat is increased, this peak does not gradually move to higher values of RasGTP. Rather, beyond a threshold value of SOScat, a second peak corresponding to a much higher level of RasGTP emerges; the histogram is bimodal (Figure 2B). Thus, the sharp threshold and bistability shown in Figure 1C are manifested as digital signaling. The prediction is that lymphocytes are either "on" or "off" with regard to Ras activation.

To test these predictions, we used a Jurkat T cell line into which we introduced Ras molecules like H-RasV12C40 (Roose et al., 2007). Individual cell assays are required to compare experimental results with the histograms shown in Figure 2B. Analysis of active Ras for individual cells in a population is not possible in this transfection experiment, and so we examined upregulation of a cell-surface activation marker CD69 by individual cells using flow cytometry. CD69 levels correlate with the strength of Ras-ERK signaling (Roose et al., 2007), but activation of signaling molecules downstream of Ras could be influenced by feedback regulation of modules such as the MAPK pathway (Ferrell, 2002; Khodolenko et al., 2002). We will address this issue directly below.

Low or high levels of SOS1cat expression led to unimodal cell populations with low or high levels of CD69 induction (Figures 2C and S21B). Intermediate levels of SOS1cat (red) induced a bimodal CD69 expression pattern in wild-type (WT) Jurkat T cells (Figure 2C). SOS1cat-induced bimodality was not observed for a control marker that is Ras unresponsive (Figure S21C). These results in cells mirror the predictions of the computer simulations in that signaling is digital. We next tested the hypothesis emerging from our calculations (Figures 1C and S2E) that the origin of digital signaling is feedback regulation of SOS-mediated Ras activation.

Experiments carried out with RasGRP1-deficient JPRM441 cells indicate the importance of this feedback loop. In contrast to WT cells (Figure 2C), intermediate levels of SOS1cat induced high CD69 expression levels in very few JPRM441 cells (13% in Figure 3A, top row). Similarly, intermediate levels of SOScat did not generate a bimodal response in computer simulations of the RasGRP-deficient state (Figure 3B). Basal RasGRP1-mediated activation of Ras is not subject to feedback regulation but can "ignite" the SOS feedback loop (Roose et al., 2007) by providing RasGTP that can bind SOS’ allosteric pocket and increase its activity 75-fold. Consistent with our computational results (Figure 1E), in RasGRP-deficient JPRM441 cells, lower basal levels of RasGTP make it more difficult to ignite the SOS feedback loop. Sufficiently high levels of SOScat can induce bimodal responses without RasGRP1 (Figures 3A, 3B, 1E, and S22) because RasGTP produced by the GEF activity of SOScat with RasGDP bound to the allosteric pocket can ultimately prime SOS’ feedback loop.

The computer simulation results suggested that a bimodal response would re-emerge in RasGRP-deficient cells for intermediate levels of SOS1cat if exogenous RasGTP molecules that bind to SOS’ allosteric pocket were added. To test this, we introduced Ras molecules like H-RasV12C40 (Roose et al., 2007) or H-RasG59E38 (Boykevisch et al., 2006) that are predominantly GTP loaded (because of the V12 or G59 mutation) and thus bind SOS’ allosteric pocket to increase GEF activity. These molecules also contain a second mutation (C40 or E38) that impairs binding to RAF and so do not directly activate the RAF-MEK-ERK-CD69 pathway, i.e., downstream pathways must be activated by endogenous Ras molecules.

| Table 1. Rate Constants Used for Model in Figure 1 |
| k<sub>1</sub> | k<sub>-1</sub> | k<sub>2</sub> | k<sub>-2</sub> | k<sub>3</sub><sup>cat</sup> | k<sub>3</sub><sup>un</sup> | k<sub>4</sub><sup>cat</sup> | k<sub>4</sub><sup>un</sup> | k<sub>5</sub><sup>cat</sup> | k<sub>5</sub><sup>un</sup> |
| 1.8 × 10<sup>-4</sup> (mols)(μm)<sup>3</sup>/s<sup>-1</sup> | 3.0 s<sup>-1</sup> | 1.7 × 10<sup>-4</sup> (mols)(μm)<sup>3</sup>/s<sup>-1</sup> | 0.4 s<sup>-1</sup> | 0.038 s<sup>-1</sup> | 1.64 × 10<sup>3</sup> (mols)/(μm)<sup>3</sup> | 0.003 s<sup>-1</sup> | 9.12 × 10<sup>3</sup> (mols)/(μm)<sup>3</sup> | 0.1 s<sup>-1</sup> | 1.07 × 10<sup>2</sup> (mols)/(μm)<sup>3</sup> |
| Sondermann et al., 2004 | Sondermann et al., 2004 | Sondermann et al., 2004 | Friedmann et al., 2006 | Sondermann et al., 2004; Boykevisch et al., 2006 | Sondermann et al., 2004; Boykevisch et al., 2006 | Gideon et al., 1992; Trahey and McCormick, 1987 | Gideon et al., 1992; Trahey and McCormick, 1987 |

Parameters used for the equations. Rates are calculated from the catalytic rates and/or the dissociation constants (K<sub>D</sub>) reported in the literature. For additional information, see Supplemental Data, Section I.
in RasGRP-deficient cells (Figure 3C, bottom row; Bimodal with p < 0.01). The same level of SOS1cat or H-RasG59E38 alone also did not result in high CD69 expression (Figure 3C, top row, unimodal; Up < 0.01). Importantly, when the allosteric pocket in SOScat is mutated (SOS1cat-W729E), so that it can no longer interact with nucleotide-associated Ras proteins, adding H-RasG59E38 does not result in a bimodal pattern of signaling (Figure 3C, bottom row). Similar results were obtained with H-RasV12C40 (data not shown). Modeling Ras activation in this cell biological experiment is in concurrence with these results (Figure 3D). Therefore, the digital signaling we observe for ERK-CD69 signaling requires feedback regulation of SOS-mediated Ras activation.

There are two possible reasons for why digital signaling in lymphocytes originates in SOS-mediated Ras activation: (1) Ignition of the SOS feedback loop is necessary for generating...
Figure 3. A RasGTP Mimetic Restores Efficient SOS\textsubscript{cat}-Induced Bimodal Signals in RasGRP-Deficient Cells

(A) Analysis of the efficiency of SOS\textsubscript{cat}-induced Ras signaling in a RasGRP1-deficient Jurkat T cell line (JPRM441) and its WT RasGRP1-reconstituted derivative line (JPRM441-WTRasGRP1). Experimentation and analysis as in Figure 2C, see also Figure S21B. Intermediate SOS\textsubscript{cat} induces high levels of CD69 expression in only 13% of the JPRM441 cells. This relative defect in JPRM441 cells is restored to 60% in the JPRM441-WTRasGRP1 cells.

(B) Stochastic simulations as in Figure 2B. Histograms of RasGTP simulating a RasGRP-deficient state are depicted. Increments of SOS\textsubscript{cat} between the plots are 2-fold. Note the lack of a bimodal distribution in "cells" with intermediate SOS\textsubscript{cat}.

(C) JPRM441 (RasGRP1-deficient Jurkat T cells)

(D) RasGRP deficient + H-RasG59E38 intermediate SOS\textsubscript{cat}
sufficiently high levels of RasGTP required to prime downstream feedback loops that cause digital signaling (e.g., those associated with the MAPK pathway [Bhalla and Iyengar, 1999; Ferrell, 2002; Kholodenko et al., 2002]). (2) Digital signaling is controlled by feedback regulation of Ras activation by SOS. Whereas signaling is undoubtedly influenced by feedback regulation of downstream signaling modules, results described below suggest that, in lymphocytes, the latter scenario is true.

Receptor Stimulation Results in Digital Signaling with SOS and Analog Responses with RasGRP Alone

The strength of lymphocyte receptor stimulation impacts outcomes (e.g., T cell activation, thymocyte development; Starr et al., 2003). Therefore, we studied how SOS and RasGRP influence cellular responses as the amount of stimulatory ligands is varied.

We studied a simplified computational model for processes upstream of Ras activation (See Section III, Supplemental Data). In short (see Figure 4A), receptor stimulation and phosphorylation generate activated ZAP-70 molecules. Activated ZAP-70 phosphorylates the adaptor molecule LAT, which recruits both PLCγ and Grb2/SOS. PLCγ is then phosphorylated, and this generates IP3 and DAG. Induced DAG enhances RasGRP recruitment and activation. We do not incorporate cooperative effects associated with Grb2/SOS recruitment to LAT (Houtman et al., 2006). Including this feature would lead to sharper cellular responses (Prasad et al., 2009).

For weak receptor stimulation, as might occur under physiologic antigen receptor stimulation (Figure 4B), WT systems that have low initial levels of active Ras exhibit a bimodal pattern of signaling after a short time that ultimately becomes a unimodal distribution with high RasGTP (Figure 4B, left column). For very strong stimulation, a unimodal state of high RasGTP is rapidly reached (Figure 4C, left column). Without RasGRP, signaling is inhibited. Importantly, without SOS such systems demonstrate a graded response, indicating the analog character of RasGRP-mediated Ras activation (Figure 4C, middle column). Changing the values of the parameters (e.g., the numbers of RasGRP and SOS molecules) used to obtain the results shown in Figure 4 does not lead to qualitative changes (Tables S12 and S13, Figures S13–S20).

To test these predictions, we determined the pattern of ERK phosphorylation in individual cells. First, 20,000 Jurkat T cells were either stimulated via the T cell receptor (TCR) or by phorbol myristate acetate (PMA). The latter mimics a DAG–PKC–RasGRP pathway but does not target SOS. Engagement of the TCR generated a unimodal P-ERK response at early time points that transitioned to a bimodal response at 3 min after stimulation (Figure 5A). In contrast, even strong stimulation via PMA never induced a bimodal ERK phosphorylation pattern and, instead, exhibited an analog response (Figure 5B).

Experiments with cells wherein genes of interest were deleted further support these results. Peripheral T cells do not develop in RasGRP1-deficient mice (Dower et al., 2000), and a selective SOS1/SOS2 peripheral T cell model to circumvent lethality due to SOS1 deficiency has not been generated (Wang et al., 1997). Therefore, we used a chicken DT40 B cell line in which pertinent genes have been genetically inactivated (Oh-hora et al., 2003). We analyzed the ERK phosphorylation pattern of 20,000 cells (WT, SOS1/SOS2, and RasGRP1−/− RasGRP3−/−) that were stimulated with increasing levels of B cell receptor (BCR) crosslinking-M4 monoclonal antibody.

WT cells stimulated by low levels of M4, mimicking physiological lymphocyte stimulation by antigen, exhibited a bimodal pattern of ERK activation at the 3 and 10 min time points (Figure 5C “WEAK” and Figure S24). Hartigan’s tests (Hartigan and Hartigan, 1985) confirmed that the response is bimodal. In contrast, SOS1−/− SOS2−/− DT40 B cells did not exhibit bimodal distributions at any time point regardless of stimulus level (Figure 5C, middle column). Thus, without SOS, signaling is analog in character regardless of strength of stimulus. Furthermore, while PMA-induced responses were severely impaired in RasGRP1−/− RasGRP3−/− cells (Figure 5D, right column), PMA induced very similar analog patterns of ERK phosphorylation in WT and SOS1−/− SOS2−/− DT40 B cells (Figure 5D, left and middle columns). These results reveal analog ERK responses from RasGRP-induced Ras activation, and that there is no intrinsic defect preventing SOS1/SOS2−/− DT40 B cells from turning on the Ras-ERK pathway.

This behavior in cell lines was mirrored in primary CD4-positive peripheral T cells. Ex vivo TCR stimulation of primary cells results in a digital pattern of ERK phosphorylation (Figure 5E), but PMA stimulation results in analog signaling (Figure 5F).

Thus, in Jurkat T cells, DT40 B cells, and primary lymph node T cells digital signaling requires engagement of the SOS pathway for Ras activation (Figures 2–5). Notably, for all systems, the ERK response to PMA stimulation was analog at all doses tested, including those that generate high levels of RasGTP. This implies that the predicted analog Ras response in the absence of SOS (Figure 4C, middle column) is not translated to digital responses by downstream signaling modules. If ignition of the positive feedback loop associated with SOS-mediated Ras activation only served to generate high levels of RasGTP that can stimulate digital signaling in a downstream module such as the MAPK pathway, a bimodal pattern of ERK activation should have been observed upon strong PMA stimulation. Since this is not so (Figures 5B and 5D), our results suggest that the digital signaling we observe for ERK and CD69 is not only predicated on positive feedback regulation of SOS-mediated Ras activation (Figures 3 and 4C) but is controlled by it.

(C) Introduction of a RasGTP mimetic overcomes RasGRP1 deficiency in JPRM441 cells. JPRM441 cells were transfected with GFP together with SOScat, SOScat-W729E (allosteric pocket mutant), H-RasG95E38 (RasGTP mimic), H-Ras, or combinations thereof. CD69 expression was analyzed by FACS and depicted as histograms for the intermediate GFP-expressing cells. Histograms were subsequently analyzed by a Hartigan’s statistical test to examine universal bimodality. See Figure S24. H-RasG95E38 synergizes with SOScat to produce a bimodal pattern (Hartigan’s test; Bimodal: p < 0.01) but not with SOScat-W729E. For detailed description and expression levels of introduced proteins see Figure S23. Figure 3C is representative of results in three independent experiments.

(D) Stochastic simulations introducing an H-RasG95E38 molecule into the mathematical model. Note the reappearance of a bimodal response in “cells” with intermediate SOScat, compared to (B).
Prediction of Hysteresis in Ras Activation

Due to technical limitations, we are not able to carry out single-cell assays of Ras activity. However, another related, but unanticipated characteristic that derives from our model, hysteresis, can be assessed by measuring Ras activation at the population level. Hysteresis is a direct consequence of bistability due to positive feedback regulation of SOS-mediated Ras activation (Figure 1), and the phenomenon and its biochemical origin are shown in Figure 6.

Figure 4. Digital Antigen Receptor Induced Ras Activation In Silico

(A) Representation of the Ras signaling network in T lymphocytes that is simulated by our stochastic simulation algorithm. Lck phosphorylates TCRζ leading to recruitment of ZAP-70. ZAP-70 phosphorylates LAT resulting in the recruitment of Grb2-SOS and PLCγ1. DAG produced by PLCγ1 leads to phosphorylation of RasGRP1 by PKCζ. Both SOS and RasGRP produce RasGTP signaling downstream to RAF, MEK, and ERK. B lymphocytes express PLCγ2 and downstream signaling events are very similar to those in T lymphocytes.

(B) Ras activation in 8000 "cells" in simulation induced by weak receptor signals over time. A bimodal RasGTP pattern emerges in WT but not SOS- or RasGRP-deficient states.

(C) Same as in (B) but simulating strong receptor signals. RasGTP levels rapidly increase in the WT "cells." A graded increase in RasGTP is observed in the SOS-deficient system. See Supplemental Data, Section III (Tables S9–S13, Figures S13–S20) for additional information, parameters, and parameter variation tests.

When previously unactivated cells are stimulated, RasGTP levels are low. Hence, the allosteric site of most SOS molecules is occupied by RasGDP and SOS‘ GEF activity is low. Increasing stimulus results in more RasGTP production and an increase in the number of SOS molecules with RasGTP bound to the allosteric pocket, resulting in ignition of the positive feedback loop and a sharp increase in active Ras levels. These processes result in the black dose-response curve in Figure 6A, which is obtained from computer simulations where the initial RasGTP levels are set to zero.
A very different dose-response curve (red curve in Figure 6A) is predicted by computer simulations where the initial RasGTP level was set to a large value, and then the responses to smaller stimulus levels were calculated. This is the predicted dose response for cells that are first robustly stimulated such that a high RasGTP level is realized, then the stimulus is quickly...
reduced (as in removal of antigen), and the response assessed after a time period that is sufficient for a new active Ras level to be established. When cells that have been previously robustly activated are exposed to lower stimulus levels, most SOS molecules have RasGTP bound to the allosteric site and are characterized by high GEF activity. So, for the same stimulus level (or SOS targeted to the membrane), previously stimulated cells will exhibit a higher level of active Ras than previously unstimulated cells because in the former situation SOS is a more active enzyme. Concomitantly, the threshold stimulus required for robust Ras activation shifts to lower values (Figures 6A and 6B) for previously stimulated cells. However, this hysteretic effect will only be manifested for a finite period of time. Ultimately, RasGTP molecules bound to the allosteric site of SOS in
previously stimulated cells will be displaced by RasGDP molecules as the amount of RasGTP in the cell declines because of lower stimulus levels. If the second stimulus level falls below a threshold, this process occurs very rapidly, and this is why hysteresis is not predicted for weak receptor stimulation.

**SOS-Dependent Hysteresis in Ras Activation**

Experimental results for Jurkat T cells and DT40 B cells (Figures 6C–6L) demonstrate the predicted hysteresis in Ras activation, and that it is due to the feedback loop associated with SOS and not due to feedback from downstream signaling modules.

Stimulation of Jurkat T cells using a maximal dose of TCR crosslinking antibody results in near maximal Ras activation after 3 min of stimulation (Figure S27A). Cells were also exposed to increasing concentrations of Src kinase inhibitor (PP2) to inhibit Lck (see Figure 4A) and interrupt signaling events upstream of Ras activation in a dose-dependent manner. PP2 was introduced simultaneously with the stimulus (t = 0 min) or after cells reached maximal levels of RasGTP (t = 3 min). RasGTP was analyzed at 3 min for PP2 added at t = 0 min. If PP2 was added at t = 3 min, RasGTP was assayed at 7 min, thereby allowing a new balance with the reduced stimulus to be established. Computer simulations (Figure S27D) show that this protocol should allow us to test whether hysteresis occurs at the level of Ras as predicted in Figure 6A.

Figure 6C shows that TCR-induced RasGTP levels in WT Jurkat cells decrease when PP2 is added simultaneously with the stimulus, demonstrating a dependence on Src kinases (or stimulus level) for RasGTP generation that is akin to the black curve in Figure 6A for previously unstimulated cells. However, when PP2 is added at 3 min (stimulus lowered after stimulation), RasGTP levels are high at 7 min even at high doses of PP2. This is akin to the red curve in Figure 6A and demonstrates hysteresis because, in previously stimulated cells, RasGTP levels are relatively high between 3 and 7 min in spite of a lower stimulus. After a sufficiently long time, as predicted, hysteresis is not observed (data not shown).

Importantly, these effects were not determined by feedback loops originating downstream of Ras. Preloading of cells with MEK1/2 inhibitor, U0126, efficiently blocks MEK and ERK phosphorylation but allows for RasGTP generation, albeit with slightly delayed kinetics (Figure S27A), but hysteresis was still observed (Figure 6D).

By using the doubly SOS-deficient DT40 cells, we also tested the prediction that SOS-mediated Ras activation underlies hysteresis. Maximal BCR crosslinking leads to similarly high levels of RasGTP at 3 min in WT and SOS1−/−SOS2−/− cells (Figure S27B). Of note, RasGTP production is clearly impaired in moderately stimulated SOS1−/−SOS2−/− cells (Figure S27C). RasGTP levels in WT DT40 cells were sensitive to PP2 inhibition at the initiation of BCR stimulation. When cells were allowed to generate RasGTP for the first 3 min prior to PP2 addition, hysteresis was observed since RasGTP levels were high when compared to cases where the same dose of PP2 was added at the initiation of BCR stimulation (Figure 6E). In sharp contrast, SOS1−/−SOS2−/− cells do not exhibit hysteresis, and RasGTP levels decrease with increasing amounts of PP2 on the way up (PP2 at t = 0) and the way down (PP2 at t = 3) (Figure 6F).

**Bistability and Hysteresis Provide Ras Signaling Memory during Serial Stimulation**

T cell activation may require integration of membrane-proximal signals from sequential contacts (each approximately 3 min in duration) that occur between T cells and antigen-presenting cells (APCs) in lymphoid tissues (Bouso and Robey, 2003; Henriksen et al., 2008; Skokos et al., 2007). A molecular mechanism that enables T cells to “remember” past encounters with antigen is not known.

Suppose during a T cell-APC contact the quality and quantity of encountered pMHC ligands is sufficient to stimulate engagement of the SOS feedback loop and robust Ras activation but insufficient for other events necessary for T cell activation. The T cell disengages from the APC and is not subject to stimulation until it encounters another APC. During this period the stimulus is “off,” and active Ras levels decline because phosphatases act on RasGRP (Figure 4) causing SOS to disengage from the membrane, RasGAPs reduce RasGTP levels during the time that the stimulus is “off,” etc. Suppose that during the next encounter of this T cell with an APC it encounters a weak stimulus that would not result in robust Ras activation if this T cell had not been previously robustly stimulated. We asked whether the existence of an underlying bistable steady-state structure due to feedback regulation of SOS (Figure 1) would result in restoration of robust Ras activation upon weaker restimulation. If so, bistability and hysteresis would be manifested as a molecular memory that enables integration of serially encountered weak signals after exposure to a strong stimulus.

To explore this idea, we carried out calculations with the minimal model shown in Figure 1. Robust stimulation of active Ras due to high levels of SOScat was followed by suddenly removing the stimulus. We then studied the dynamics of restimulation with a weak stimulus (green) after the originally strong stimulus has been “off” for a certain time (Figure 6G). Increasing the duration of the resting phase reduces the RasGTP level at the time of restimulation because of the RasGAPs present in our model. Figure 6G shows that maximal activation is recovered upon restimulation with a subsequent weaker stimulus, provided that RasGTP does not decline below the level of the unstable steady state (blue points in Figure 1C). If RasGTP levels decline to baseline during the duration when the stimulus is “off,” then RasGTP levels are low upon restimulation (Figure 6G, 500 s rest period). If there is no bistability and hysteresis as when SOScat is not subject to feedback regulation (or Ras is activated via RasGRP), restimulation with a weak stimulus results in low levels of Ras activation regardless of prior stimulation, i.e., there is no memory (Figure 6H).

Stimulation of Jurkat T cells or B cells with the plant lectin Concanavalin A (Con A) results in robust calcium responses that rely on binding of Con A to the TCR or BCR (Weiss et al., 1987). Importantly, binding of Con A can be relatively rapidly abrogated by addition of α-methyl-mannoside (α-MM), a competitive carbohydrate. We used this protocol to test the predictions in Figures 6G and 6H. Because T and B cells respond similarly to this protocol, we used the DT40 system as it enables testing the effects of SOS by genetic deletion (Figure 6I).

Con A stimulation resulted in robust Ras activation in both WT and SOS1−/−SOS2−/− DT40 B cells at 3 min (Figure 6J). Addition
of α-MM treatment to robustly stimulated WT cells resulted in a decline in RasGTP levels. It is important to note that at 12 min, RasGTP levels still remained moderately above the basal level. Next, we tested the effect of a very weak stimulus of anti-BCR crosslinking antibody given at this 12 min time point (see Figure 6K). Priming with Con A followed by α-MM treatment resulted in hyperresponsive RasGTP levels induced by this weak second signal that did not elicit a response when WT DT40 B cells were primed with PBS as a negative control (Figure 6K). In contrast, when doubly deficient SOS1−/− SOS2−/− DT40 B cells were primed through the same regimen, we observed only minimal RasGTP stimulation by the second signal mediated by the BCR (Figure 6L). These data are consistent with the prediction (Figures 6G and 6H) that the underlying bistability and hysteresis due to feedback regulation of SOS confer memory to the dynamic responses of previously stimulated lymphoid cells.

DISCUSSION

Major Findings

We combined theoretical analyses and stochastic computer simulations to study membrane-proximal signaling in lymphocytes, with a view toward understanding how activation of a key signaling intermediate in diverse cell types (Ras) is regulated. Experimental tests of these predictions using diverse approaches and further in silico and in vitro studies lead to the following conclusions. A feedback loop associated with SOS-mediated Ras activation is necessary for digital signaling in lymphoid cells, and hysteresis in the dose-response curve for Ras activation. Digital signaling and hysteresis may also confer lymphocytes with short-term molecular memory of encounters with antigen (Figure 7). Alone, RasGRP-mediated Ras activation results in analog signaling in cell lines and lymph node T cells and does not exhibit hysteresis. But, intermediate levels of RasGRP activity lead to more efficient digital responses than with SOS alone. The interplay of differential activities of these two RasGEFs leading to efficient and varied cellular responses may be a principle that is employed more broadly and could have important implications for lymphocyte function. Our in silico and in vitro studies predict many phenomena that should be explored further.

Further Experimental Tests of Predicted Ras Signaling Characteristics

We have demonstrated that digital Ras-ERK signaling requires SOS in cell lines (Figure 5). Similar TCR-induced digital signals operate in primary T cells, but currently a direct demonstration of the involvement of SOS’ positive feedback loop in primary cells is lacking. Future work to address this point will be aided by the generation of the appropriate mouse models.

Compartmentalized Ras signaling has received considerable recent interest (Campbell et al., 1998; Mor and Philips, 2006). SOS activates Ras exclusively at the plasma membrane, but RasGRP can also function on internal membranes. It will of interest to investigate how analog (RasGRP) and digital (SOS) mechanisms of Ras activation occur in time and space as well as whether recently observed spatial nanoclustering of active Ras proteins (Tian et al., 2007) is influenced by positive feedback regulation of Ras activation.

In other cell types, digital signaling has been reported to rely on a positive feedback loop between MAPK and phospholipase A2 (Bhalla and Iyengar, 1999). Phospholipase A2 is, however, not expressed in T and B lymphocytes (Gilbert et al., 1996). This may be why digital signaling in lymphocytes is controlled by feedback regulation of SOS’ GEF activity. Nonetheless, feedback loops present in the MAPK pathway (Ferrell, 2002;
Experimental Procedures

Mean-Field Equations for the Minimal Model Shown in Figure 1

The minimal model is based on the following reactions shown in Figure 1A. The mass action rate equations corresponding to those reactions are

\[
\frac{d[S]}{dt} = -k_1[S][R_0] + k_{4}[SR_0] - k_2[S][R_T] + k_{3}[SR_T]
\]

\[
\frac{d[SR_T]}{dt} = k_2[S][R_T] - k_{4}[SR_T]
\]

\[
\frac{d[R_T]}{dt} = -k_2[S][R_T] + k_{3}[SR_T] + \frac{k_{cat}[R_0][SR_0]}{K_{m} + [R_0]} - \frac{k_{cat}[R_0][SR_0]}{K_{m} + [R_0]} - \frac{k_{cat}[R_0][SR_0]}{K_{m} + [R_T]} + \frac{k_{cat}[R_0][SR_0]}{K_{m} + [R_T]}
\]

The total number of SOS and Ras molecules are conserved, which leads to the following constraints:

\[
\alpha = [S] + [SR_0] + [SR_T]
\]

\[
\beta = [R_0] + [R_T] + [SR_0] + [SR_T]
\]

In the above equations, \([X]\) represents the concentration of the species, \(X\). The abbreviations used for different species are as follows:

\(S = \text{SOS} R_0 = \text{Ras} - \text{GDP} R_T = \text{Ras} - \text{GTP}\)

\(SR_0 = \text{SOS} - \text{Ras} - \text{GDP} SR_T = \text{SOS} - \text{Ras} - \text{GTP}\)

\(R_{GAP} = \text{Ras} - \text{GAP}\)

The Michaelis constants are defined as \(K_{m} = (k_{cat} + k_{-3})/k_{3}\); \(K_{m} = (k_{cat} + k_{-4})/k_{4}\); \(K_{m} = (k_{cat} + k_{-5})/k_{5}\), where \(k_{-3}\), \(k_{-4}\), and \(k_{-5}\) are the binding, unbinding, and catalytic rates of the substrate (S) to the enzyme (E), respectively, and \(k_{cat}\) is the rate of production of the product (P) from the complex (ES). The reaction is shown schematically below:

\[E + S \stackrel{k_{m}}{\rightleftharpoons} ES \stackrel{k_{cat}}{\rightarrow} E + P\]

\(K_{m}, K_{m},\) and \(K_{m}\) are calculated from Table S1. For the ordinary differential equations (ODE) in Equation 1A, reactions #1 and #2 in Table S1, for Equation 1B, reaction #2 in Table S1, and for Equation 1C, reactions #2, #3, and #5 are used. For the reactions in #2, #4, and #5 in Table S1, we used the Michaelis Menten form, and the Michaelis constants are calculated from the binding, unbinding, and the catalytic rates of the reactions as described above. In many cases, the \(K_{p} = k_{cat}/K_{m}\) values are known for the reactions but the binding \(k_{m}\) and unbinding \(k_{u}\) rates are not known. Therefore, we carried out parameter sensitivity analyses, and our results are robust to up to 10-fold variations of the parameters. Details of this analysis are shown in Table S3. The left-hand sides of Equations 1A–1C are set to zero and the algebraic equations are solved for the steady-state concentrations.

Stochastic Simulations of the Model Shown in Figures 2 and 4

We used the Gillespie algorithm (Bortz et al., 1975; Gillespie, 1977; McAdams and Arkin, 1997) to perform stochastic simulations that effectively solve the Master equation (van Kampen, 1992) corresponding to the chemical reactions in the signaling network shown in Figure 2A. Simulation details and rather

\[\text{Kholodenko et al., 2002} \text{ undoubtedly further modulate our measurements of CD69 and ERK activation, and it will be important to examine how. Such investigations could help resolve puzzles as why in SOS1−/− SOS2−/− cells RasGTP levels are lower when PP2 is added after robust stimulation compared to when the inhibitor is added at } t = 0, \text{ or why WT Jurkat and DT40 cells exhibit more pronounced hysteresis for higher doses of PP2 (Figure 6). These studies may also resolve whether delayed action of nuclear phosphatases that turn off ERK cause apparent hysteresis in ERK activation in SOS−/− DT40 cells without bistability (Figure S28).} \]
exhaustive parameter sensitivity analyses are provided in the Supplemental Data (Sections II and III).

**Cell Lines, Stimulations, Inhibitors, Plasmids, and Transfections**

Human Jurkat leukemic T cells, chicken DT40 B cell lines, and derived lines were generated and cultured as described before (Oh-hora et al., 2003; Roose et al., 2005). Stimulation were done in PBS at 37°C with PMA, C305 (anti-TCR), or M4 (anti-BCR) or stimulated with Con A followed by α-MM treatment (Weiss et al., 1987). Cell lines were transfected as described before (Roose et al., 2005). For more details, see Supplemental Data, Section IV.

**Western Blot Analysis and FACS Analysis**

Protein expression was determined by western blot analysis of 1% NP40 lysates. Cell equivalents were analyzed per sample using the following antibodies: RasGRP1 (A176), Phospho-MEK1/2, Phospho-p44/42 MAP Kinase, Myc-tag (Cell Signaling), α-tubulin (Sigma), Ras (Upstate Biotechnologies), and Pan-Ras (Calbiochem) for detection of human or chicken Ras. Proteins were visualized using Western Lightning reagent plus (Perkin Elmer) and a Kodak Image Station 440CF and Kodak ID Image Analysis Software 3.5 to quantify expression levels. FACS assays were carried out as described before (Roose et al., 2005). For more details, see Supplemental Data, Section IV.

**Ras Activation Assays**

Activation of Ras was analyzed by a RasGTP pull-down assay essentially according to the manufacturer’s instructions (Upstate). For more details, see Supplemental Data, Section IV.

**SUPPLEMENTAL DATA**

Supplemental Data include 31 figures, 13 tables, and Supplemental Experimental Procedures and can be found with this article online at http://www.cell.com/supplemental/S0092-8674(08)01631-0.

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