**Transport signatures of Fermi surface topology change in BiTeI**

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Transport signatures of Fermi surface topology change in BiTeI

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We report a quantum magnetotransport signature of a change in the Fermi surface topology in the Rashba semiconductor BiTeI with a systematic tuning of the Fermi level $E_F$. Beyond the quantum limit, we observe a marked increase (decrease) in electrical resistivity when $E_F$ is above (below) the Dirac node that we show originates from the Fermi surface topology. This effect represents a measurement of the electron distribution on low-index ($n = 0, -1$) Landau levels and is uniquely enabled by the finite bulk $k_z$ dispersion along the $c$ axis and strong Rashba spin-orbit coupling strength of the system. The Dirac node is independently identified by Shubnikov–de Haas oscillations as a vanishing Fermi surface cross section at $k_z = 0$. Additionally, we find that the violation of Kohler’s rule allows a distinct insight into the temperature evolution of the observed quantum magnetoresistance effects.

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Recently, Dirac’s matrix equation of relativistic electrons [1] has been found to be profoundly linked to the dynamics of electrons in solids. Application of this formalism has been proven key in describing the intertwined (pseudo)spin degrees of freedom [2–4]. One striking experimental implication of the linear dispersion is that in laboratory magnetic fields, it significantly enlarges low-index Landau level energy separations compared to parabolic bands generated by a comparable tight-binding transfer integral, making emergent Dirac fermion systems an ideal platform to study quantum Landau level effects. Observations of this range from the discovery of Shubnikov–de Haas (SdH) oscillations in elemental Dirac fermion systems an ideal platform to study quantum magnetoresistance [6] to a vanishing Fermi surface cross section at $k_z = 0$. Additionally, we find that the violation of Kohler’s rule allows a distinct insight into the temperature evolution of the observed quantum magnetoresistance effects.

We study the system BiTeI that possesses a Dirac node generated by Rashba-type spin-orbit coupling $\alpha \cdot (\sigma \times k)$ [8,9], where $\alpha$ is the structure-specific Rashba parameter, and $\sigma$ and $k$ are the spin and momentum operators, respectively. This layered semiconductor breaks inversion symmetry by crystallizing in the polar space group $P3m1$ so that the spin-orbit interaction takes the form of a Rashba term in the bulk three-dimensional (3D) band structure. This has been confirmed by angle-resolved photoemission spectroscopy [10] and relativistic ab initio calculations [11]. In this system, both the conduction band minimum and the valence band maximum are located near the $A$ point in the hexagonal prism-shaped Brillouin zone [Fig. 1(a)]; taking $A$ as the origin, the conduction electrons near the band edge can be described by the Hamiltonian

$$\mathcal{H} = \frac{\hbar^2 k^2}{2m_z} + \frac{\hbar^2 k_z^2}{2m_0} + \alpha \cdot (\sigma \times k_1),$$

where the momentum $k$ is decomposed into $k_1$ in the $A-L-H$ plane and $k_z$ parallel to $A-F$ as well as $\alpha$. The quasi-two-dimensionality (quasi-2D) of the crystal structure leaves $\mathcal{H}$ dominated by the dispersion of $k_1$. The band parameters are taken as $m_0 = 0.095m_e$, $|\alpha| = 3.85$ eV Å, and $m_z/m_0 \sim 5$, as inferred from photoemission [10], optical [12], and transport [13] studies. To emphasize the competition between the spin splitting $\alpha \cdot (\sigma \times k_1)$ and the kinetic energy, $E_F$ is zeroed at the band crossing point at $A$, which is also the neutrality point of an effective Dirac fermion with the Fermi velocity $v_F \approx 5.35 \times 10^5$ m/s [12]. Here, the Dirac point defines a change of Fermi surface topology [Fig. 1(b)] from a spinless torus ($E_F > 0$) through a horn torus ($E_F = 0$) to a ring torus ($E_F < 0$). The inner Fermi surface (IFS) and outer Fermi surface (OFS) are defined at each $k_z$ slice, as shown in Fig. 1(b); the OFS is always electronlike while the IFS is bipolar, depending on $E_F$ and $k_z$.

Stoichiometric BiTeI is expected to be semiconducting while in reality it is often $n$-type degenerate with $E_F$ above the Dirac point [10,12]. The well-defined FS in this regime, and its progressive evolution shown in Fig. 1(b), can be explored by chemical modification. Motivated by Ref. [14], single crystals of BiTeI were grown intentionally doped with Cu to improve electron mobility $\mu_e$ and vary $E_F$. Different from Ref. [14], we adopted the vertical Bridgman growth identical to the conditions used in Ref. [10] starting from Cu : Bi : Te : I = 1 : x : 1 : 1 : 1 ($x = 0.025–0.1$). MR and Hall effects with current on the cleaved quasi-2D plane are measured in four-probe configurations in a Quantum Design physical property measurement system with $B$ applied along the polar $c$ axis [ [$A$–$F$", see Fig. 1(a)]. Compared with preceding studies [13–15], our BiTeI samples exhibit a relatively large resistivity ratio $\rho_{300K}/\rho_{1K} = 4–5.8$ [Fig. 1(c)].
and enhanced low temperature $\mu_e$ typically between 800 and 3000 cm$^2$/V s. The carrier density $n_e$ varies within the range of 1.2–6 $\times$ 10$^{10}$/cm$^3$ for samples taken from the same ampoule, implying a composition gradient intrinsic to Bridgman growth [16]. Though the microscopic role of Cu in improving the electronic quality of crystals is still being investigated, from powder x-ray diffraction the addition of Cu changes the lattice constants of BiTeI from 854 Å [10] to observed values of 4.334 Å and 6.868 Å $\leq c \leq 6.896$ Å, implying that the role of Cu is to expand the $c$-axis lattice constant (up to +0.6%) while leaving the in-plane lattice constant unchanged within a small variation ($\pm 0.2\%$). At the lowest temperature, we observe clear SdH oscillations over an extended range of $E_F$, as shown for selected samples in Fig. 2(a).

SdH oscillations is a common means to probe the FS in metals [17], whose frequency $f$ gives the extremal FS size $S_k$ via $f = hS_k/2\pi e$, where for a simple isotropic FS $S_k = \pi(3\pi^2n_e)^{2/3}$. In Fig. 2(a), SdH of two different $f$ are traceable in all normalized MR curves $[\Delta \rho/\rho_0 = \rho(B) - \rho(0)]/\rho(0)$. One consists of broad bumps starting from $B \sim 1$ T, and the other oscillates rapidly for $B \gtrsim 10$ T. These represent two coexisting FS extrema of distinct size and are assigned to the IFS and OFS at $k_z = 0$, in accordance with Refs. [13–15]. The broad IFS oscillations are also seen in Fig. 2(b), our simulation of the IFS density of states as described below. $E_F$ is estimated [18] by comparing $f^{\text{OFS}}$ and $f^{\text{IFS}}$ to Eq. (1) with $m_0 = 0.095m_e$, $|\alpha| = 3.85$ eV Å. Following the descending $f^{\text{OFS}}$ from 414 T (sample A) to 233 T (sample H), i.e., $E_F$ from 79 to 46 meV [see Fig. 2(c)], the field corresponding to the last IFS oscillation (defined as the IFS quantum limit $B^{QL}$, denoted by triangles in Fig. 2(a))] approaches $B = 0$ in samples A–E, then moves toward higher fields in samples F–H, consistent with the closing and opening of the inner FS pocket across $E_F = 0$ in Fig. 1(b).

Beyond the IFS quantum limit, we observe distinctly different behavior for $E_F > 0$ and $E_F < 0$. It is most illuminating to contrast in Fig. 2(a) samples E (18 meV) and F ($-24$ meV) which bracket the Dirac point. In sample E, at $B > B^{QL}$, the MR grows rapidly above 2 T with a steeper slope than $B < B^{QL}$, while in sample F, the MR at $B > B^{QL}$ is strongly suppressed relative to $B < B^{QL}$. This distinction is systematically visible in samples B–D and G–H with higher $B^{QL}$. Apparently the MR beyond the quantum limit (QL) provides a sensitive probe of the sign of $E_F$ and corresponding Fermi surface topology in BiTeI. This quantum transport behavior and its connection to FS topology are the main results of this Rapid Communication.

We suggest that the physical origin of this bifurcation is the quantum transport of the relevant Landau levels (LLs) for the density of states (DOS) at $E_F$ [17]. Figure 2(d) shows the in-plane electronic states (without upper axis) and with (lower axis) $B$. The quantized LL energies are given by [8,19]

$$E_n = |n|\frac{h e B}{m_0} \pm \sqrt{\frac{\hbar^2 c^2 B^2}{4m_0^2} + 2n|\alpha|^2-eB},$$

where $n$ is the LL index, including $n = 0$ ($E_0 = h e B/2m_0$). Selected LLs ($n = -40$ to 4) are shown in Fig. 2(d) and are divided into two groups colored blue and green, whose successive intersection with $E_F$ gives rise to the IFS and OFS oscillations, respectively. We note that because $E_n(B)$ for $n < 0$ are nonmonotonic, in increasing $B$ these LLs experience a transition from IFS-like to OFS-like. We illustrate this with the change in color of the negative LLs in Fig. 2(d). Blue (IFS) LLs resemble those of a Dirac fermion with a slightly $B$-dispersive $n = 0$ LL due to the zero-point energy of the parabolic band with the effective mass $m_0$. Green (OFS) LLs can be seen as a reservoir to restrict the overall chemical potential within a weak variation.

In contrast to this quantization in transverse $k_z$, the longitudinal $k_z$ is unaffected, recalling a residual one-dimensional contribution from every LL satisfying $E_n < E_F$ [20]. As the OFS LLs are insensitive to the sign of $E_F$, we focus on the IFS to understand the observed MR behavior. The IFS density of states $D^{IFS}$ is given by

$$D^{IFS}_{E=E_F} = \frac{n^{\text{IFS}}}{E_{n < E_F}} \sqrt{\frac{2m_e}{\hbar^2 c^2 B^2}} \frac{1}{\sqrt{E_F - E_n}} \frac{eB}{2\pi \hbar},$$

with $E_n$ explicitly expressed in Eq. (2) and $E_F$ taken as $B$ independent for each sample. In Eq. (3), $\sum\sqrt{2m_e/\hbar^2 c^2 B^2} \sqrt{E_F - E_n}$ counts the states at each cyclotron motion guiding center and $eB/2\pi \hbar$ counts the number of guiding centers. Note that we include the partial contribution of the lowest LL consistent with our definition of IFS, as discussed above. The simulated $D^{IFS}$ for samples A–H from Eq. (3) are displayed in Fig. 2(b) with each $E_n$ broadened with a Lorentzian 40 K wide.

Figure 2(b) reproduces the essential results in Fig. 2(a), including the bifurcation between samples with $E_F > 0$ and $E_F < 0$. This remarkable agreement suggests that the MR behavior reflects a quantum Landau level effect and is a measure of $D^{IFS}$. In Eq. (3) the inverse square root $1/\sqrt{E_F - E_n}$ is most sensitive to the uppermost LL below $E_F$. Thus $D^{IFS}$ at $B > B^{QL}$ captures the difference between
independently in the conductivity tensor (it may be expected that the IFS and OFS would simply add the Dirac node in BiTeI from that in graphene. Conventionally, by the spin with a large OFS also distinguishes the transport of graphite [22].

in the context of the Nernst effect near the quantum limit in dispersion at of states

Triangles denote the IFS quantum limit and the dashed lines are extrapolations of the MR below the quantum limit. (b) Simulated IFS density

\( \Delta \sigma \) due to LL formation would follow \( D^{\text{IFS}} \). The agreement of Figs. 2(a) and 2(b), however, shows empirically that \( \Delta \rho \sim D^{\text{IFS}} \). We hypothesize that this is caused by the large difference in size of the spin-polarized IFS and OFS, which becomes extreme near the Dirac point. Considering such a scattering phase space, for the IFS the inter-IFS-OFS backscattering events dominate over the intraband backscattering. While we can still consider the IFS and OFS contributions to \( \sigma \) additively, a common relaxation time may not apply. The major role of the IFS, among the total electrical current carried almost completely by the OFS, is then through \( D^{\text{IFS}} \) modulations that affect the interband scattering rate \( 1/\tau_{\text{I-O}} \) for the OFS (and thus \( \rho \)).

The above identification of FS topology is independently supported by the observed SdH oscillations. The vanishing size of the IFS approaching the Dirac point can be seen in a plot of the FS radii \( k^{\text{IFS}} \) and \( k^{\text{OFS}} \) \( (k = \sqrt{\mathbf{S}_{\mathbf{k}}/\pi}) \), as shown in Fig. 3(a). The points above and below the Dirac point can be linearly fitted by \( k^{\text{OFS}} = 1.01(5) k^{\text{IFS}} + 0.0951(6) \) and \( k^{\text{OFS}} = -0.81(9) k^{\text{IFS}} + 0.0961(7) \), respectively. We note that these line fits are consistent with the Rashba model, which couples the IFS and OFS:

\[
\begin{align*}
D^{\text{IFS}} - D^{\text{OFS}} &= 2k_a \quad \text{for } E_F > 0, \\
D^{\text{IFS}} + D^{\text{OFS}} &= 2k_a \quad \text{for } E_F < 0.
\end{align*}
\]

The term \( k_a = m_0|\alpha|/\hbar^2 \) is the offset of band minimum generated by \( \alpha \cdot (\mathbf{\sigma} \times \mathbf{k}_l) \), which performs a pure translation.
FIG. 3. (Color online) (a) OFS and IFS radii at $k_z = 0$ ($k_{\text{OFS}}$ and $k_{\text{IFS}}$) for all measured samples with line fits for $E_F > 0$ and $E_F < 0$, respectively. The Rashba bands are shown in the inset. (b) IFS index plot of samples A, B, C, D, G, and H. The inset shows the oscillatory resistivity after background subtraction.

[gray arrow in the Fig. 3(a) inset] between two spin branches on any $k$-space cut through the $k_z$ axis. Equation (4) is a natural consequence of Eq. (1), confirming that this expression effectively describes the electrons near $E_F = 0$. The average $k_\alpha$ is estimated to be 0.0476(6) Å. This agrees within 3% with $m_0 = 0.095m_e$, $|\alpha| = 3.85$ eV Å which we have used in the calculation above, reassuring that the Cu doping which improves the carrier mobility preserves the Rashba band structure to a small variation, consistent with the trend observed for the in-plane lattice constant $a$. The IFS SdH senses both positive and negative low-index LLs across the Fermi surface topology change, as shown in the index plot of Fig. 3(b).

We next discuss the temperature ($T$) dependence of the observed quantum transport behaviors. The effect of $T$ on SdH oscillations is a useful probe of the Landau levels and associated carrier effective mass and scattering [17]. We have found that Kohler’s rule [7], which states that $\Delta \rho/\rho_0$ depends only on the Hall angle $\omega_c\tau$ and thus $B/\rho_0$, provides an incisive tool for isolating the LL contribution to transport across the QL. The Kohler’s plot of MR curves taken at various $T$ of four different Fermi surfaces (samples A, C, F, and G) are shown in Fig. 4. First, for $B < B^{\text{QL}}$, the MR curves of each FS fall onto a single trace despite oscillatory deviations, implying that the scattering is hardly affected by $B$ or $T$. Taking this collapsed curve as the background $\rho_{\text{Back}}$ onto which the SdH is superimposed assists the IFS index analysis in Fig. 3(b). We note that a previous work [14] adopts a similar procedure in studying SdH in BiTeI.

The validity of Kohler’s rule within the QL restricts the most plausible cause of the violation [at high fields beyond the QL in Figs. 4(b)–4(d)] to quantum effects. We suggest that these violations are consistent with the unconventional Dirac LLs, in particular, the $n = 0$ and $n = -1$. MR of samples C and F is notably enhanced with elevated $T$, reflecting thermal excitation from the $n = 0$ LL both upward and downward [see the inset of Fig. 4(d)]. In sample G, although the IFS SdH appears weaker compared to C or A, the suppressed Kohler’s curve upon warming implies that the broad shoulderlike feature in the MR is an intrinsic peak

FIG. 4. (Color online) (a)–(d) Temperature evolution of MR captured by the Kohler’s plot of samples A, C, F, and G; black triangles denote the Kohler’s plot of samples A, C, F, and G; black triangles denote the position of $E_F$ at 14 T for each sample.
associated with the meeting of the coherent $n = -1$ LL with the $E_F$. Additionally, the contrary $T$ evolution of samples C and G, despite their similar $B_{QL}$, demonstrates the asymmetry of quantum transport above and below the Dirac node. In this way it can be seen that Kohler’s scaling brings out the LL effects beyond the QL, which would otherwise be overlooked.

The uniqueness of BiTeI lies in the particularly large value of $a$ compared to other Rashba systems [10, 11]. This strengthens the Dirac fermion behaviors observed above and determines the large inter-LL scale: At 14 T, $E_1 - E_0 \approx 88$ meV, while $E_0 - E_{-1} \simeq 71$ meV. Furthermore, the Dirac point is located $\sim 94$ meV above the conduction band minimum, making $E_F < 0$ accessible at an appreciable doping level without entering the localization regime [23].

We note that this $E_F < 0$ regime in Rashba systems is of intense theoretical interest from the standpoint of enhanced superconducting instabilities [24], spin torque efficiency [25], and superconductivity with peculiar symmetry [26]. Our present transport identification of the $E_F < 0$ FS topology with high electronic mobility thus paves the way for realizing the material host for these exciting proposals.

In conclusion, we have established the quantum magnetotransport properties of the Dirac node in BiTeI, which is markedly asymmetric for $E_F > 0$ and $< 0$. This effect is the result of a change in the bulk FS topology. Kohler’s scaling is shown to be an effective tool to analyze the unconventional low-index Landau levels. We predict the latter effect will be useful in the general study of band crossings in multiband systems.

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[18] We first determine the sign of $E_F$ by comparing $f^{\text{OFS}}$ to $m_0 = 0.095 m_e$, $|a| = 3.85$ eVÅ with the critical point for FS topology $f^{\text{IFS}} = 314$ T. To better describe the IFS behavior that dominates the present $B$ range, the value of $E_F$ is adjusted to fit $f^{\text{IFS}}$ (IFS quantum limit) with the above parameter set.
[19] The influence of the external Zeeman effect on the orbital motion is neglected because near the Dirac point the internal spin-orbit field $B_{\alpha} \simeq 2 m_0 |a|/g \mu_B h^2 = 3200$ T ($g = 2$) is much larger than the applied $B$.