Measurements of jet multiplicity and differential production cross sections of $Z + \text{jets}$ events in proton-proton collisions at $s = 7$ TeV

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Measurements of jet multiplicity and differential production cross sections of $Z + \text{jets}$ events in proton-proton collisions at $\sqrt{s} = 7$ TeV

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(Received 13 August 2014; published 11 March 2015)

Measurements of differential cross sections are presented for the production of a $Z$ boson and at least one hadronic jet in proton-proton collisions at $\sqrt{s} = 7$ TeV, recorded by the CMS detector, using a data sample corresponding to an integrated luminosity of $4.9 \text{ fb}^{-1}$. The jet multiplicity distribution is measured for up to six jets. The differential cross sections are measured as a function of jet transverse momentum and pseudorapidity for the four highest transverse momentum jets. The distribution of the scalar sum of jet transverse momenta is also measured as a function of the jet multiplicity. The measurements are compared with theoretical predictions at leading and next-to-leading order in perturbative QCD.

DOI: 10.1103/PhysRevD.91.052008

PACS numbers: 13.87.-a, 13.85.-t, 14.70.-e

I. INTRODUCTION

Measurements of the production cross section of a $Z$ boson with one or more jets in hadron collisions, hereafter $Z + \text{jets}$, can be compared with predictions of perturbative quantum chromodynamics (pQCD). Analyses of data collected during the first run of the CERN LHC have used two main theoretical approaches, developed in the last decade, for the complete description of the associated production of vector bosons and jets up to stable particles in the final state. Multileg matrix elements, computed at leading order (LO) in pQCD, have been combined with parton showers (PS), merging different final jet multiplicities together. Alternatively, next-to-leading order (NLO) matrix elements have been interfaced with parton showers for final states of fixed jet multiplicity. CMS has relied on MadGraph [1] and POWHEG-BOX [2–4] as main implementations of the former and latter approaches, respectively. In the last few years, novel techniques have been developed in order to merge NLO calculations for several final-state multiplicities in a theoretically consistent way, and interface them with PS, as formerly done for LO matrix elements. This approach may provide a NLO accuracy for a range of complex topologies, overcoming the limitations of fixed order NLO calculations, which cannot in general describe completely inclusive distributions receiving contributions by final states of different jet multiplicity. Furthermore, a description of these final states up to stable particles is possible, since hadronization models can be used in combination with these calculations. The $Z + \text{jets}$ final state provides jet kinematic distributions that are ideal for testing these different options for theoretical predictions.

Also, this process contributes a large background to many standard model processes, like top production or diboson final states, e.g., the associated production of a Higgs boson and a $Z$, where the former decays in $b\bar{b}$ pairs and the second in charged leptons [5,6]. Searches for phenomena beyond the standard model may also be sensitive to this process, which plays a particularly important role as the main background in the study of supersymmetric scenarios with large missing transverse momentum. This has been one of the main motivations for a previous analysis of the angular distributions in $Z + \text{jets}$ events presented by CMS [7], and the study presented in this paper is complementing it with the measurement of jet spectra.

Measurements of $Z + \text{jets}$ production were published by the CDF and D0 collaborations based on a sample of proton-antiproton collisions at $\sqrt{s} = 1.96$ TeV [8,9], and by the ATLAS [10] and CMS [11] collaborations from a sample of proton-proton collisions at $\sqrt{s} = 7$ TeV collected at the LHC, corresponding to an integrated luminosity of $0.036 \text{ fb}^{-1}$. ATLAS has reported an updated measurement at the same center-of-mass energy with a data set corresponding to an integrated luminosity of $4.6 \text{ fb}^{-1}$ [12].

In this paper, we update and expand upon the results obtained by the CMS Collaboration at $\sqrt{s} = 7$ TeV with a data sample corresponding to an integrated luminosity of $4.9 \pm 0.1 \text{ fb}^{-1}$ [13] collected in 2011. We present fiducial cross sections for $Z + \text{jets}$ production as a function of the exclusive and inclusive jet multiplicity, where the $Z$ bosons are identified through their decays into electron or muon pairs. The contribution from $Z/\gamma^{\ast}$ interference is considered to be part of the measured signal. We measure the differential cross sections as a function of the transverse momentum $p_T$ and pseudorapidity $\eta$ of the four highest-$p_T$ jets in the event. The pseudorapidity is defined as $\eta = -\ln \tan[\theta/2]$, where $\theta$ is the polar angle with respect...
to the counterclockwise-rotating proton beam. We also present results for the distribution of $H_T$, the scalar sum of jet transverse momenta, measured as a function of the inclusive jet multiplicity. The jet $p_T$ and $\eta$ differential cross sections are sensitive to higher order QCD corrections. $H_T$ is an observable characterizing globally the QCD emission structure of the event, and it is often used as a discriminant variable in searches for supersymmetric scenarios, to which $Z + \text{jets}$ contribute as a background. The measurement of its distribution is therefore of great interest.

The paper is organized as follows. Section II presents a description of the CMS apparatus and its main characteristics. Section III provides details about the simulation used in this analysis. Section IV discusses the event reconstruction and selection. Section V is devoted to the estimation of the signal event selection efficiency and to the subtraction of the background contributions. The procedure used to correct the measurement for detector response and resolution is presented in Sec. VI. Section VII describes the estimation of the systematic uncertainties, and in Sec. VIII the results are presented and theoretical predictions are compared to them.

II. THE CMS DETECTOR

The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter that provides a magnetic field of 3.8 T. The field volume contains a silicon tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass/scintillator hadron calorimeter; each subdetector in the barrel section is enclosed by two end caps. The magnet flux-return yoke is instrumented with gas-ionization tracking devices for muon detection. In addition to the barrel and end cap detectors, CMS has an extensive forward calorimetry system. CMS uses a two-level trigger system. The first level is composed of custom hardware processors, and uses local information from the calorimeters and muon detectors to select the most interesting events in a fixed time interval of less than 4 $\mu$s. The high-level trigger is a processor farm that further decreases the event rate from a maximum of 100 kHz to roughly 300 Hz, before data storage. A detailed description of the CMS detector can be found in Ref. [14].

Here we briefly outline the detector elements and performance characteristics that are most relevant to this measurement. The inner tracker, which consists of silicon pixel and silicon strip detectors, reconstructs charged-particle trajectories within the range $|\eta| < 2.5$. The tracking system provides an impact parameter resolution of 15 $\mu$m and a $p_T$ resolution of 1.5% for 100 GeV particles. Energy deposits in the ECAL are matched to tracks in the silicon detector and used to initiate the reconstruction algorithm for electrons. The tracking algorithm takes into account the energy lost by electrons in the detector material through bremsstrahlung. In the energy range relevant for $Z$-boson decays, the electron energy resolution is below 3%. Muon trajectories are reconstructed for $|\eta| < 2.4$ using detector planes based on three technologies: drift tubes, cathode-strip chambers, and resistive-plate chambers. Matching outer muon trajectories to tracks measured in the silicon tracker provides an average $p_T$ resolution of 1.6% for the $p_T$ range used in this analysis. For the jets reconstructed in this analysis, the $p_T$ resolution is better than 10% and the energy scale uncertainty is less than 3% [15].

III. PHYSICS PROCESSES AND DETECTOR SIMULATION

Simulated events are used to correct the signal event yield for detector effects and to subtract the contribution from background events. Simulated Drell–Yan $Z/\gamma^*$, $t\bar{t}$, and $W + \text{jets}$ events are generated using the MadGraph 5.1.1 [1] event generator. The package provides a tree level matrix-element calculation with up to four additional partons in the final state for vector boson production, and three additional partons for $t\bar{t}$ events. The leading-order CTQ6L1 parton distribution functions (PDF) [16] are used with MadGraph. The residual QCD radiation, described by a parton shower algorithm, and the hadronization, which turns the partons into a set of stable particles, are implemented with Pythia 6.424 [17] using the Z2 underlying event and fragmentation tune [18]. The default $\alpha_S$ value of the PDF set used is adopted for the event generator. The matrix-element and parton shower calculations are matched using the $k_T$-MLM algorithm [19].

Decays of the $\tau$ lepton are described by the Tauola 1.27 [20] package. Diboson events ($WW$, $WZ$, $ZZ$) are modeled entirely with Pythia. Single-top events in the $Wt$ channel are simulated using Powheg-box [2–4,21], and followed by Pythia to describe QCD radiation beyond NLO and hadronization. An alternative description of the Drell–Yan signal is used for the evaluation of systematic uncertainties that is based on the Sherpa 1.4 [22–25] tree level matrix-element calculation, which has up to four additional partons in the final state, and uses the NLO CTEQ6.6M [26] PDF set.

The total cross sections for the $Z$ signal and the $W$ background are normalized to the next-to-next-to-leading-order (NNLO) predictions that are obtained with Fewz [27] and the MSTW2008 [28] PDF set. The $t\bar{t}$ cross section is normalized to the NNLO prediction from Ref. [29]. Diboson cross sections are rescaled to the NLO predictions obtained with MCFM [30].

The interaction of the generated particles in the CMS detector is simulated using the Geant4 toolkit [31,32]. During data collection, an average of nine additional interactions occurred in each bunch crossing (pileup). Pileup events are generated with Pythia and added to the generated hard-scattering events. The evolution of beam conditions during data taking is taken into account by reweighting the Monte Carlo (MC) simulation to match the
distribution of the number of pileup interactions observed in data.

IV. EVENT RECONSTRUCTION AND SELECTION

The production of a Z boson is identified through its decay into a pair of isolated leptons (electrons or muons). Trigger selection requires pairs of leptons with $p_T$ exceeding predefined thresholds; these thresholds were changed during the data acquisition period because of the increasing instantaneous luminosity. For both lepton types threshold pairs of 17 and 8 GeV are used for most of the data sample. The electron triggers include isolation requirements in order to reduce the misidentification rate. Triggered events are reconstructed using the particle-flow algorithm [33,34], which combines the information from all CMS subdetectors to reconstruct and classify muons, electrons, photons, charged hadrons, and neutral hadrons.

Electrons are selected with $p_T > 20$ GeV in the fiducial region of pseudorapidity $|\eta| < 2.4$, but excluding the region $1.44 < |\eta| < 1.57$ between the barrel and the end caps of ECAL to ensure uniform quality of reconstruction. The electron identification criteria [35,36] comprise requirements on the distance in $\eta - \phi$ space between the cluster barycenter and the electron track extrapolation, where $\phi$ is the azimuthal angle measured in the plane transverse to the beams, and the size and the shape of the electromagnetic shower in the calorimeter. Electron-positron pairs consistent with photon conversion are rejected. Electron isolation is evaluated using all particles reconstructed with the particle-flow algorithm within a cone around the electron direction of radius $\Delta R = 0.3$, where $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}$ is the distance in the $\eta - \phi$ plane. An isolation variable is defined as $I_{\text{rel}} = (I_{\text{charged}} + I_{\text{photon}} + I_{\text{neutral}})/p_T$, where $I_{\text{charged}}$, $I_{\text{photon}}$, $I_{\text{neutral}}$ are respectively the $p_T$ sums of all charged hadrons, photons, and neutral hadrons in the cone of interest, and $p_T^e$ is the electron transverse momentum. The selection requires $I_{\text{rel}} < 0.15$. Isolation variables are sensitive to contamination from pileup events and thus a correction for this effect is necessary for the high pileup environment of the LHC collisions. Only the particles consistent with originating from the reconstructed primary vertex of the event, the vertex with the largest quadratic sum of its constituent tracks’ $p_T$, are included in the calculation of $I_{\text{charged}}$. The $I_{\text{photon}}$ and $I_{\text{neutral}}$ components are corrected using the jet area subtraction approach [37].

The selected muons must have $p_T > 20$ GeV and $|\eta| < 2.4$. Muon identification criteria are based on the quality of the global track reconstruction, which includes both tracker and muon detectors. Muons from cosmic rays are removed with requirements on the impact parameter with respect to the primary vertex. In order to evaluate the isolation, the variables $I_{\text{charged}}$, $I_{\text{photon}}$, and $I_{\text{neutral}}$ are computed within a cone of radius $\Delta R = 0.4$ around the trajectory of the muon candidate, and $I_{\text{rel}}$ is required to be less than 0.2. Charged hadrons from pileup interactions are rejected by requiring their tracks to be associated with the primary vertex. The transverse momentum sum of the charged hadrons that are not associated with the primary vertex is used to estimate the contribution from the neutral particles produced in the pileup interactions; half of this sum is subtracted from the isolation variable.

The two highest-$p_T$, same-flavor, oppositely charged, and isolated leptons are selected to form the Z-boson candidate if their invariant mass lies between 71 and 111 GeV. The lepton pair is required to be associated with the primary vertex of the event. Leptons associated with the primary vertex and passing the isolation criteria are removed from the collection of particles used for jet clustering.

For jet reconstruction, charged-particle tracks not associated with the primary vertex are removed from the collection of particles used for clustering. In this way, the dominant part of the pileup contamination of the events of interest is suppressed. The remaining particles are used as input to the jet clustering, which is based on the anti-$k_T$ algorithm [38] as implemented in the FastJet package [39,40], with a distance parameter in the rapidity-azimuth plane of 0.5. In order to reject reconstructed jets and instrumental noise, identification quality criteria are imposed on the jets based on the energy fraction of the charged, electromagnetic, and neutral hadronic components, and requiring at least one charged particle in the jet.

Several effects contribute to bias the measured jet energy, compared with the value it would acquire by clustering stable particles originating from the fragmented hard-scattered partons and from the underlying event. The sources of energy bias are pileup interactions, detector noise, and detector response nonuniformities in $\eta$ and nonlinearities in $p_T$. The jet energy scale (JES) calibration [15] relies on a combination of PYTHIA multijet simulations and measurements of exclusive dijet and photon+jet events from data. The corrections are parametrized in terms of the uncorrected $p_T$ and $\eta$ of the jet, and applied as multiplicative factors scaling the four-momentum vector of each jet. These factors include the correction for the contribution from neutral pileup particles using the jet area approach [37], and corrections for residual discrepancies between data and simulation. The correction factors range between 1.0 and 1.2, depend mostly on $p_T$, and are approximately independent of $\eta$.

Furthermore, the jet energy resolution (JER) in data is known to be worse than in the simulation; therefore the simulated resolution is degraded to compensate for this effect. The difference between the reconstructed jet transverse momentum and the corresponding generated one is scaled in the simulation so as to reproduce the observed resolution.

A minimum threshold of $p_T > 30$ GeV is required for the jets to reduce contamination from the underlying event. Only jets with $|\eta| < 2.4$ are considered, and jets are
required to be separated from each lepton of the Z candidate by $\Delta R \geq 0.5$ in the $\eta - \phi$ plane.

V. SIGNAL EFFICIENCY AND BACKGROUND

A “tag-and-probe” technique [41] is used to estimate efficiencies for trigger selection, event reconstruction, and the offline selection of the $Z + \text{jets}$ sample. Scaling factors derived from the ratio between the data and simulation efficiencies are used to reweight simulated events in order to compensate for the residual data-simulation differences. The correction is determined as a function of $p_T$ and $\eta$ of the leptons, and background components are resolved using a binned extended maximum-likelihood fit of the dilepton invariant-mass distribution between 60 and 120 GeV. The signal component of the distribution, which is taken from the Drell-Yan simulated sample, is convolved with a Gaussian function to account for the resolution difference between data and simulation. The background contribution is modeled by an exponential function multiplied by an error function describing the kinematic threshold due to binning of the probe lepton $p_T$. The combined single-flavor identification efficiency is the product of contributions from the trigger, event reconstruction, and offline selection. The same technique is used on the data and in the simulation. The trigger efficiency of the data ranges between 94 and 99% for electrons and between 82 and 97% for muons. The combined identification and isolation efficiency depends on the $p_T$ and $\eta$ of the leptons; it ranges between 68 and 91% for electrons and between 86 to 99% for muons.

The fiducial acceptance for muons and electrons is different, since the latter are not well reconstructed in the transition region between the barrel and end cap electromagnetic calorimeters. In order to facilitate the combination of results from the $Z \rightarrow e^+e^-$ and $Z \rightarrow \mu^+\mu^-$ final states, this difference is evaluated using the simulation, giving a correction to the $e^+e^-$ cross section, applied within the unfolding procedure described in the next section, that amounts to 8%.

Several background processes can produce or mimic two reconstructed opposite-sign same-flavor leptons. The largest contribution comes from $t\bar{t}$ production, while diboson production contributes near the $Z$-boson invariant-mass peak. Other minor contributions arise from $Z \rightarrow \tau^+\tau^-$ as well as single-top and $W + \text{jets}$ events. The contamination from multijet events produced through the strong interaction is negligible, as established with a control sample in which the two leptons in each event have the same charge [7]. The total contribution of the backgrounds is approximately 1% of the total yield of the selected events, and it increases as a function of jet multiplicity. At the highest measured jet multiplicities it reaches values up to 10%.

The background subtraction procedure is performed after scaling the number of background events to the integrated luminosity in the data sample using the corresponding cross section for each background process.

The exclusive jet multiplicity in the selected events is shown in Fig. 1. For both leptonic decay channels, the data show overall agreement with combined signal and background samples from the simulation. The ratio between the cross sections as a function of jet multiplicity in data and in

![FIG. 1 (color online). Distributions of the exclusive jet multiplicity for the electron channel (upper plot) and muon channel (lower plot). Data are compared to the simulation, which is the sum of signal and background events. Scale factors have been used to correct simulation distributions for residual efficiency differences with respect to data. No unfolding procedure is applied. Only statistical uncertainties are shown.](image-url)
signal plus background simulation, shown in the bottom part of the figure, is compatible with unity within the uncertainties.

VI. UNFOLDING

The distributions of the observables are corrected for event selection efficiencies and for detector resolution effects back to the stable particle level, in order to compare with predictions from event generators simulating Z + jets final states. Particles are considered stable if their proper average lifetime $\tau$ satisfies $c \tau > 10$ cm. The correction procedure is based on unfolding techniques, as implemented in the RooUNFOLD toolkit [42], which provides both the “singular value decomposition” (SVD) method [43] and the iterative algorithm based on Bayes’ theorem [44]. Both algorithms use a “response matrix” that correlates the values of the observable with and without detector effects.

The response matrix is evaluated using Z + jets events, generated by MadGraph followed by Pythia, with full detector simulation. For generator-level events, leptons and jets are reconstructed from the collection of all stable final-state particles using criteria that mimic the reconstructed data. Electrons and muons with the highest $p_T$ above 20 GeV in the pseudorapidity range $|\eta| < 2.4$ are selected as Z-boson decay products. In order to include the effects of final-state electromagnetic radiation in the generator-level distributions, the electron and muon candidates are reconstructed by clustering the leptons with all photons in a cone of radius $\Delta R = 0.1$ in the $\eta - \phi$ plane. Leptons from Z-boson decay are removed from the particle collection used for the jet clustering at generator level. The remaining particles, excluding neutrinos, are clustered into jets using the anti-$k_T$ algorithm. A generated jet is included in the analysis if it satisfies $p_T > 30$ GeV, $|\eta| < 2.4$; the jet must contain at least one charged particle, to match the jet reconstruction quality requirements used for data analysis, and the distance of the jet from the leptons forming the Z-boson candidate is larger than $\Delta R = 0.5$.

The unfolded distributions are obtained with the SVD algorithm. As a cross check, the unfolding of the distributions is also performed with the D’Agostini method, which leads to compatible results within statistical uncertainties. The unfolding has a small effect on the jet $\eta$ distributions, with migrations among the bins of a few percent for central jets and up to 10% in the outer regions. Larger unfolding effects are observed in the other distributions: up to 20% for the jet multiplicity, between 10 and 20% for the jet $p_T$, and between 10 and 30% for the $H_T$ distribution.

VII. SYSTEMATIC UNCERTAINTIES

The sources of systematic uncertainties that affect the Z + jets cross section measurement are divided into the following categories: JES and JER [15], unfolding procedure, efficiency correction and background subtraction, pileup reweighting procedure, and integrated luminosity measurement.

Jet energy scale and resolution uncertainties affect the jet $p_T$ reconstruction and the determination of $H_T$. Each JES correction factor has an associated uncertainty that is a function of the $\eta$ and $p_T$ of the jet. The difference in the distribution of an observable, after varying the JES both up and down by one standard deviation, is used as an estimate

<table>
<thead>
<tr>
<th>Systematic uncertainty (%)</th>
<th>$\sigma(Z/\gamma^* + \text{jets})$</th>
<th>$d\sigma/dp_T$ (1st jet)</th>
<th>$d\sigma/dp_T$ (2nd jet)</th>
<th>$d\sigma/dp_T$ (3rd jet)</th>
<th>$d\sigma/dp_T$ (4th jet)</th>
</tr>
</thead>
<tbody>
<tr>
<td>JES + JER</td>
<td>2.0–18</td>
<td>4.9–8.7</td>
<td>6.3–16</td>
<td>8.8–15</td>
<td>15–23</td>
</tr>
<tr>
<td>Efficiency</td>
<td>1.7–9.2</td>
<td>1.3–22</td>
<td>0.5–21</td>
<td>0.8–13</td>
<td>0.3–12</td>
</tr>
<tr>
<td>Background</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
</tr>
<tr>
<td>Pileup</td>
<td>0.1–25</td>
<td>0.1–0.4</td>
<td>0.6–1.8</td>
<td>0.6–1.0</td>
<td>0.9–1.5</td>
</tr>
<tr>
<td>Total systematic uncertainty (%)</td>
<td>2.7–32</td>
<td>5.1–24</td>
<td>9.0–27</td>
<td>10–20</td>
<td>17–23</td>
</tr>
<tr>
<td>Statistical uncertainty (%)</td>
<td>0.7–6.4</td>
<td>0.1–7.2</td>
<td>1.4–12</td>
<td>3.0–13</td>
<td>4.3–19</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Systematic uncertainty (%)</th>
<th>$d\sigma/d\eta$ (1st jet)</th>
<th>$d\sigma/d\eta$ (2nd jet)</th>
<th>$d\sigma/d\eta$ (3rd jet)</th>
<th>$d\sigma/d\eta$ (4th jet)</th>
</tr>
</thead>
<tbody>
<tr>
<td>JES + JER</td>
<td>3.5–8.2</td>
<td>7.2–8.9</td>
<td>9.4–12</td>
<td>13–15</td>
</tr>
<tr>
<td>Unfolding</td>
<td>6.5–13</td>
<td>8.4–11</td>
<td>5.0–12</td>
<td>6.4–13</td>
</tr>
<tr>
<td>Efficiency</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
<td>0.3</td>
</tr>
<tr>
<td>Background</td>
<td>0.2</td>
<td>0.3–0.5</td>
<td>0.6–1.1</td>
<td>0.9–1.0</td>
</tr>
<tr>
<td>Pileup</td>
<td>0.2–0.4</td>
<td>0.3–0.5</td>
<td>0.3–0.7</td>
<td>0.5–1.2</td>
</tr>
<tr>
<td>Total systematic uncertainty (%)</td>
<td>7.8–17</td>
<td>11–15</td>
<td>11–19</td>
<td>15–23</td>
</tr>
<tr>
<td>Statistical uncertainty (%)</td>
<td>0.6–1.0</td>
<td>0.9–1.4</td>
<td>2.4–3.6</td>
<td>7.6–12</td>
</tr>
</tbody>
</table>

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of the JES systematic uncertainty. Similarly, the effect of the systematic uncertainties in the scaling factor used in the JER degradation is estimated by varying its value up and down by one standard deviation.

The uncertainty in the unfolding procedure is due to both the statistical uncertainty in the response matrix from the finite size of the simulated sample and to any dependence on the signal model provided by different event generators.

The statistical uncertainty is computed using a MC simulation, which produces variants of the matrix according to random Poisson fluctuations of the bin contents. The entire unfolding procedure is repeated for each variant, and the standard deviation of the obtained results is used as an estimate of this uncertainty. The systematic uncertainty due to the generator model is estimated from the difference between events simulated with MadGraph and Sherpa at detector response level. The overall unfolding uncertainty is taken to be either the statistical uncertainty alone, in the case where the results from the two event generators agree within one standard deviation, or the sum in quadrature of the simulation statistical uncertainty and the difference between the two MC generators.

Additional uncertainty arises from the efficiency corrections and from the background subtraction. The contribution due to efficiency corrections is estimated by adding and subtracting the statistical uncertainties from the tag-and-probe fits. The systematic uncertainty from the background subtraction procedure is small relative to the other sources. For $\bar{t}$ and diboson processes, the uncertainty in the normalization arises from both the theoretical uncertainty in the inclusive cross section and the difference between the theoretical prediction of the cross section (as in Sec. III) and the corresponding CMS measurement [45–48]. The largest
FIG. 3 (color online). Unfolded differential cross section as a function of $p_T$ for the first (top left), second (top right), third (bottom left), and fourth (bottom right) highest $p_T$ jets, compared with SHERPA, POWHEG, and MADGRAPH predictions. Error bars around the experimental points represent the statistical uncertainty, while cross-hatched bands represent statistical plus systematic uncertainty. The bands around theory predictions correspond to the statistical uncertainty of the generated sample and, for NLO calculations, to its combination with systematic uncertainty related to scale variations.
FIG. 4 (color online). Unfolded differential cross section as a function of the jet absolute pseudorapidity $|\eta|$ for the first (top left), second (top right), third (bottom left), and fourth (bottom right) highest $p_T$ jets, compared with SHERPA, POWHEG, and MADGRAPH predictions. Error bars around the experimental points represent the statistical uncertainty, while cross-hatched bands represent statistical plus systematic uncertainty. The bands around theory predictions correspond to the statistical uncertainty of the generated sample and, for NLO calculations, to its combination with systematic uncertainty related to scale variations.
FIG. 5 (color online). Unfolded differential cross section as a function of $H_T$ for events with at least one (top left), two (top right), three (bottom left), and four (bottom right) jets compared with SHERPA, POWHEG, and MADGRAPH predictions. Error bars around the experimental points represent the statistical uncertainty, while cross-hatched bands represent statistical plus systematic uncertainty. The bands around theory predictions correspond to the statistical uncertainty of the generated sample and, for NLO calculations, to its combination with systematic uncertainty related to scale variations.
of these two values is taken as the magnitude of the uncertainty. As observed in previous studies [7], the single-top quark and \( W^\pm \) jets contributions are at the sub-per-mil level, and they are assigned a 100% uncertainty. Since the background contribution as a function of the jet multiplicity is theoretically less well known than the fully inclusive cross section, control data samples are used to validate the simulation of this dependence. The modeling of the dominant \( t\bar{t} \) background as a function of the jet multiplicity is compared with the data using a control sample enriched in \( t\bar{t} \) events. This sample is selected by requiring the presence of two leptons of different flavors, i.e., \( e\mu \) combinations, and an agreement is found between data and simulation at the 6% level [7]. The CMS measurement of the \( t\bar{t} \) differential cross section [49], using an event selection compatible with the study presented in this paper, leads to a production rate for events with six jets in simulation overestimated by about 30%. This difference is used as the estimated uncertainty for the six-jets subsample. Variations in the MADGRAPH prediction for \( t\bar{t} \) production from a change in the renormalization, factorization, and matching scales, as well as from the PDF choice, show that data and simulation agree within the estimated uncertainties.

The systematic uncertainty of the pileup reweighting procedure in MC simulation is due to the uncertainties in the minimum-bias cross section and in the instantaneous luminosity of the data sample. This uncertainty is evaluated by varying the number of simulated pileup interactions by \( \pm 5\% \). The measurement of the integrated luminosity has an associated uncertainty of 2.2% that directly propagates to any cross section measurement. The systematic uncertainties (excluding luminosity) used for the combination of the electron and muon samples are summarized in Tables I–III.

VIII. RESULTS AND COMPARISON WITH THEORETICAL PREDICTIONS

The results presented for observable quantities are obtained by combining the unfolded distributions for both leptonic channels into an uncertainty-weighted average for a single lepton flavor. Correlations between systematic uncertainties for the electron and muon channels are taken into account in the combination. Fiducial cross sections are shown, without further corrections for the geometrical acceptance or kinematic selection, for leptons and jets. All the results are compared with theoretical distributions, produced with the RIVET toolkit [50], obtained with the generator-level phase space definition and on final-state stable particles as discussed in Sec. VI. Neutrinos are excluded from the collection of stable particles.
FIG. 7 (color online). Unfolded differential cross section as a function of $p_T$ for the first (top left), second (top right), third (bottom left), and fourth (bottom right) highest $p_T$ jets, compared with SHERPA predictions based on the PDF sets CT10, MSTW2008, and NNPDF2.1. Error bars around the experimental points represent the statistical uncertainty, while cross-hatched bands represent statistical plus systematic uncertainty. The bands around theory predictions correspond to the statistical uncertainty of the generated sample and to its combination with the theoretical PDF uncertainty.
FIG. 8 (color online). Unfolded differential cross section as a function of the jet absolute pseudorapidity $|\eta|$ for the first (top left), second (top right), third (bottom left), and fourth (bottom right) highest $p_T$ jets, compared with SHERPA predictions based on the PDF sets CT10, MSTW2008, and NNPDF2.1. Error bars around the experimental points represent the statistical uncertainty, while cross-hatched bands represent statistical plus systematic uncertainty. The bands around theory predictions correspond to the statistical uncertainty of the generated sample and to its combination with the theoretical PDF uncertainty.
FIG. 9 (color online). Unfolded differential cross section as a function of \(H_T\) for events with at least one (top left), two (top right), three (bottom left), and four (bottom right) jets compared with SHERPA predictions based on the PDF sets CT10, MSTW2008, and NNPDF2.1. Error bars around the experimental points represent the statistical uncertainty, while cross-hatched bands represent statistical plus systematic uncertainty. The bands around theory predictions correspond to the statistical uncertainty of the generated sample and to its combination with the theoretical PDF uncertainty.
Theoretical predictions at leading order in pQCD are computed with the MadGraph 5.1.1 generator followed by PYTHIA 6.424 with the Z2 tune and CTEQ6L1 PDF set for fragmentation and parton shower simulation. For the MadGraph simulation, the factorization and renormalization scales are chosen on an event-by-event basis as the transverse mass of the event, clustered with the $k_T$ algorithm down to a $2 \rightarrow 2$ topology, and $k_T$ at each vertex splitting, respectively [19,51]. The MadGraph predictions are rescaled to the available NNLO inclusive cross section [27], which has a uniform associated uncertainty of about 5% that is not propagated into the figures.

Predictions at next-to-leading order in QCD are provided by SHERPA 2.72 [22–25,52], using the CT10 NLO PDF set [53], in a configuration where NLO calculations for $Z + 0$ and $Z + 1$ jet event topologies are merged with leading-order matrix elements for final states with up to four real emissions and matched to the parton shower. The NLO virtual corrections are computed using the BlackHat library [54]. In this calculation, the factorization and renormalization scales are defined for each event by clustering the $2 \rightarrow n$ parton level kinematics onto a core $2 \rightarrow 2$ configuration using a $k_T$-type algorithm, and using the smallest invariant mass or virtuality in the core configuration as the scale [52]. The default configuration for the underlying event and fragmentation tune is used.

The third theoretical prediction considered is the NLO QCD calculation for the $Z + 1$ jet matrix element as provided by the POWHEG-BOX package [2–4,55], with CT10 NLO PDF set, and matched with the PYTHIA parton shower evolution using the Z2 tune. In this case, the factorization and renormalization scales in the inclusive cross section calculation are defined on an event-by-event basis as the $Z$-boson $p_T$, while for the generation of the radiation they are given by the $p_T$ of the produced radiation.

The comparisons of these predictions with the corrected data are presented in Figs. 2–5. The effect of PDF choice is shown in Figs. 6–9. The error bars on the plotted data points represent the statistical uncertainty, while cross-hatched bands represent the total experimental uncertainty (statistical and systematic uncertainties summed in quadrature) after the unfolding procedure. Uncertainties in the theoretical predictions are shown in the ratio of data to simulation only. For the NLO prediction, theoretical uncertainties are evaluated by varying simultaneously the factorization and renormalization scales up and down by a factor of two (for SHERPA and POWHEG). For the SHERPA prediction only, the resummation scale is changed up and down by a factor $\sqrt{2}$ and the parton shower matching scale is changed by 10 GeV in both directions. The effect of the PDF choice is shown for SHERPA, by comparing the results based on CT10 PDF set with those based on the alternative NLO PDFs MSTW2008 and NNPDF2.1 [56]. The theoretical part of the plotted uncertainty band for each PDF choice includes both the intrinsic PDF uncertainty, evaluated according to the prescriptions of the authors of each PDF set, and the effect of the variation of $\pm 0.002$ in the value of the strong coupling constant $\alpha_s$ around the central value used in the PDF.

A. Jet multiplicity

Figure 2 shows the measured cross sections as a function of the exclusive and inclusive jet multiplicities, for a total number of up to six jets in the final state. Beyond the sixth jet, the measurement is not performed due to the statistical limitation of the data and simulated samples. The trend of the jet multiplicity represents the expectation of the pQCD prediction for a staircaselike scaling, with an approximately constant ratio between cross sections for successive multiplicities [57]. This result confirms the previous observation, which was based on a more statistically limited sample [11]. Within the uncertainties, there is agreement between theory and measurement for both the inclusive and the exclusive distributions.

B. Differential cross sections

The differential cross sections as a function of jet $p_T$ and jet $\eta$ for the first, second, third, and fourth highest $p_T$ jet in the event are presented in Figs. 3 and 4, respectively. In addition, the differential cross sections as a function of $H_T$ for events with at least one, two, three, or four jets are presented in Fig. 5. The pQCD prediction by MadGraph provides a satisfactory description of data for most distributions, but shows an excess in the $p_T$ spectra for the first and second leading jets at $p_T > 100$ GeV. SHERPA tends to underestimate the high $p_T$ and $H_T$ regions in most of the spectra, while remaining compatible with the measurement within the estimated theoretical uncertainty. POWHEG predicts harder $p_T$ spectra than those observed in the data for the events with two or more jets, where the additional hard radiation is described by the parton showers and not by matrix elements. This discrepancy is also reflected in the $H_T$ distribution. Figures 6–9 show no significant dependence of the level of agreement between data and the SHERPA prediction on the PDF set chosen. Hence the PDF choice cannot explain the observed differences with data.

IX. SUMMARY

The fiducial production cross section of a $Z$ boson with at least one hadronic jet has been measured in proton-proton collisions at $\sqrt{s} = 7$ TeV in a sample corresponding to an integrated luminosity of 4.9 fb$^{-1}$. The measurements comprise inclusive jet multiplicities, exclusive jet multiplicities, and the differential cross sections as a function of jet $p_T$ and $\eta$ for the four highest $p_T$ jets of the event. In addition, the $H_T$ distribution for events with different minimum numbers of jets has been measured. All measured differential cross sections are corrected for detector effects and compared with theoretical predictions at particle level.
The predictions of calculations combining matrix element and parton shower can describe, within uncertainties, the measured spectra over a wide kinematical range. The measured jet multiplicity distributions and their NLO theoretical predictions from the SHERPA and POWHEG generators are consistent within the experimental and theoretical uncertainties. However, SHERPA predicts softer $p_T$ and $H_T$ spectra than the measured ones, while POWHEG shows an excess compared to data in the high $p_T$ and $H_T$ regions. In particular, the POWHEG spectra are harder for the highest jet multiplicities, which are described only by parton showers. The tree level calculation based on MADGRAPH predicts harder $p_T$ spectra than the measured ones for low jet multiplicities.

ACKNOWLEDGMENTS

We congratulate our colleagues in the CERN accelerator departments for the excellent performance of the LHC and thank the technical and administrative staffs at CERN and at other CMS institutes for their contributions to the success of the CMS effort. In addition, we gratefully acknowledge the computing centers and personnel of the Worldwide LHC Computing Grid for delivering so effectively the computing infrastructure essential to our analyses. Finally, we acknowledge the enduring support for the construction and operation of the LHC and the CMS detector provided by the following funding agencies: the Austrian Federal Ministry of Science, Research and Economy and the Austrian Science Fund; the Belgian Fonds de la Recherche Scientifique, and Fonds voor Wetenschappelijk Onderzoek; the Brazilian Funding Agencies (CNPq, CAPES, FAPERJ, and FAPESP); the Bulgarian Ministry of Education and Science; CERN; the Chinese Academy of Sciences, and the Chinese Academy of Sciences, and the Russian Foundation for Basic Research; the Ministry of Education, Science and Technological Development of Serbia; the Secretaría de Estado de Investigación, Desarrollo e Innovación and Programa Consolider-Ingenio 2010, Spain; the Swiss Funding Agencies (ETH Board, ETH Zurich, PSI, SNF, UniZH, Canton Zurich, and SER); the Ministry of Science and Technology, Taipei; the Thailand Center of Excellence in Physics, the Institute for the Promotion of Teaching Science and Technology of Thailand, Special Task Force for Activating Research and the National Science and Technology Development Agency of Thailand; the Scientific and Technical Research Council of Turkey, and Turkish Atomic Energy Authority; the National Academy of Sciences of Ukraine, and State Fund for Fundamental Researches, Ukraine; the Science and Technology Facilities Council, United Kingdom; the U.S. Department of Energy, and the U.S. National Science Foundation. Individuals have received support from the Marie Curie program and the European Research Council and EPLANET (European Union); the Leventis Foundation; the A.P. Sloan Foundation; the Alexander von Humboldt Foundation; the Belgian Federal Science Policy Office; the Fonds pour la Formation à la Recherche dans l’Industrie et dans l’Agriculture (FRIA-Belgium); the Agentschap voor Innovatie door Wetenschap en Technologie (IWT-Belgium); the Ministry of Education, Youth and Sports (MEYS) of the Czech Republic; the Council of Science and Industrial Research, India; the HOMING PLUS program of Foundation for Polish Science, cofinanced by the European Union, Regional Development Fund; the Compagnia di San Paolo (Torino); the Consorzio per la Fisica (Trieste); MIUR Grant No. 20108T4XTM (Italy); the Thalis and Aristeia programs cofinanced by EU-ESF and the Greek NSRF; and the National Priorities Research Program by Qatar National Research Fund.
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