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Orientation of aromatic residues in amyloid cores: Structural insights into prion fiber diversity

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Structural conversion of one given protein sequence into different amyloid states, resulting in distinct phenotypes, is one of the most intriguing phenomena of protein biology. Despite great efforts the structural origin of prion diversity remains elusive, mainly because amyloids are insoluble yet noncrystalline and therefore not easily amenable to traditional structural-biology methods. We investigate two different phenotypic prion strains, weak and strong, of yeast translation termination factor Sup35 with respect to angular orientation of tyrosines using polarized light spectroscopy. By applying a combination of alignment methods the degree of fiber orientation can be assessed, which allows a relatively accurate determination of the aromatic ring angles. Surprisingly, the strains show identical average orientations of the tyrosines, which are evenly spread through the amyloid core. Small variations between the two strains are related to the local environment of a fraction of tyrosines outside the core, potentially reflecting differences in fibril packing.

Significance

Amyloids, which are protein fiber aggregates, are often associated with neurodegenerative diseases such as Alzheimer’s, but they can also be beneficial, as in yeasts, where they help cells adapt to environmental changes. Intriguingly, the same protein has the ability to aggregate into different fiber forms, known as strains, that generate distinct biological phenotypes. Structurally, little is known about strains. Using polarized light spectroscopy, we provide structural information on two distinct phenotypic strains of the yeast translation termination factor, Sup35. Remarkably, they show similar orientation of aromatic residues in the fiber core relative to the fiber direction, suggesting similar structures. Small variations are observed, indicating different local environments for aromatic residues outside the core, reflecting differences in fiber packing.


The authors declare no conflict of interest.

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Here LD is the differential absorbance of orthogonal forms of polarized light at wavelength $\lambda_i$, $A_{is0}$ is the absorbance of the isotropic sample, $\phi(\lambda_i)$ is the angle between the fiber axis and the direction of the transition moment, and $S$ is an order parameter defining the degree of orientation of fibers in the sample. In the case of a prion fiber we regard $S$ as the product of two order parameters, allowing some disorder owing to the arrangement of regularly structured protein monomers inside the fibrous aggregate (for details, see Supporting Information):

$$S = S_0 S_1,$$

where $S_0$ is the macroscopic (global) order parameter of fibrous aggregates and $S_1$ is an internal order parameter characterizing the orientation of local monomeric aggregates within a fiber. $S_1$ is thus a “mesoscopic” orientation factor relating the orientation of the monomers to a local fiber axis direction, $p$, and the factor $S_0$ relates $p$ to the stretching direction (the long axis of the fiber). In the limit of high shear rates in solution, or infinite stretch of the polymer matrix, $S_0 = 1$ corresponds to a perfect orientation of the fibrous particles parallel with the flow direction or the stretch direction in the two systems, respectively. $S_1$ can be seen as a measure of hydrodynamic properties of the fibrous assemblies in solution or their straightness in the gel matrix. $S_1$ takes also values between the limits 0 and 1, corresponding, respectively, to isotropic and to perfect orientation of the unique axis of the monomer parallel to the local polymer axis.

The tyrosine orientation angles are obtained by determining the parameter $S$ and then solving Eq. 1 for the angle $\phi(\lambda_i)$. $S_0$ is directly related to the second moment ($P_2$) of the orientation distribution function of the fibers, which we here determine using two independent approaches. In the flow experiments, $S_0$ is calculated using an orientation distribution model for rigid ellipsoidal particles in laminar flow (see Supporting Information for details). In the PVA gel, $S_1$ is determined by a distribution model for uniaxial stretch deformation (29, 30). There is a significant difference between the two alignment methods: The stretch angular distribution does not depend on the length of the particles, whereas the hydrodynamic model does, and the longer the particles the better their flow orientation. For the prion fibers there is naturally a length distribution, which will affect $S_1$ in solution but not in a PVA gel. There is also a characteristic morphology, affecting $S_0$ which potentially depends on the fiber assembly mechanisms and fibrilization history. Similar $S_1$ values suggest similar morphological behaviors. However, different $S_1$ values will reflect morphological differences with respect to fiber organization. Independent evidence from the nonempirical determination of orientation parameter $S_0$ in PVA as well as from the sucrose flow experiment (Supporting Information) allows $S_1$ to be determined.

### Fiber Order Parameters and Angular Orientation of Tyrosines

The $S$ factor of the fibers was first obtained in aqueous solution in the presence of ThT from the LD and absorbance spectra (Fig. 2). Upon binding to amyloid fibers the transition moment of ThT is oriented nearly parallel to the fiber axis, $\phi(\lambda) = 0-20^\circ$, and thus the $L/D_{iso}$ at 440 nm can be used to determine $S$ from Eq. 1 (31).

Knowing the $S$ factor, calculated by using ThT, the angle $\phi(\lambda)$ for tyrosine $L_b$ was obtained from the $L/D_{iso}$ amplitude at 278 nm (Fig. 2) and was about 30° for both strains (Table 1). Because the $L_b$ transition lies in the plane of a phenyl ring of tyrosine (Fig. 1) and might thus be subject to more or less free rotation, the $L_b$ transition is also required to uniquely identify the orientation of a tyrosine moiety in a 3D structure. Owing to strong light scattering at shorter wavelength and overlapping absorption

$$LD(\lambda_i)/A_{iso}(\lambda_i) = 1.5 S(3\cos^2(\phi(\lambda_i)) - 1).$$

[1]

Fig. 1. Principles of polarized light measurements. (A) Sequence of NM domain (residues 1–253) of yeast Sup35 prion protein. N domain is shown in blue with tyrosine (Y) residues (whose orientation is detected by LD) highlighted with yellow. (B) Transition dipole moments of UV transitions $L_a$ and $L_b$ of tyrosine chromophore. (C and D) The two alignment techniques used in the study: orientation in a stretched film (C) and in a Couette shear flow cell (D).
in the presence of ThT, the $L_a$ band is completely obscured under these conditions. Hence, spectra of fibers were recorded, without ThT bound, in aqueous sucrose solution under shear flow and in a stretched PVA matrix. Sucrose works as a refractive index matching medium reducing the light scattering from fibers and increases the flow orientation of the fibers. The use of refractive index matching solvents in LD has been previously suggested for samples of phosphatidylcholine vesicles to detect LD bands in the peptide-absorbing region (200–230 nm) (32). Sucrose reduced the scattering induced by liposomes without significantly altering their properties and increased the LD signal owing to increased viscous shear forces. Measurements using PVA and sucrose solution provide independent modes of determining the orientation parameter $S_C$. $S_i$ values are then obtained from Eq. 1 by inserting $S_C$ (as a component of $S$) and the tyrosine $L_b$ angle value, experimentally determined using ThT probe.

The spectra of the two fiber forms were similar for both orientation techniques and showed the characteristic positive LD in the $L_b$ band region 250–290 nm, a negative LD in the $L_a$ region 220–250 nm, and identical $L_a/L_b$ intensity ratio (Fig. 3). Accordingly, the angle $L_b$ of the long axis of tyrosine, which coincides with Cβ–Cγ bond, was also similar for both strains and was 60° (Table 1). The $S_i$ factor is higher in the presence of sucrose and PVA than in aqueous solution owing to a better alignment of the fibers in those conditions. $S_C$ values obtained from the flow experiments reflect the length variation of the fibers. $S_C$ of weak strain resulted in estimated lengths twice as long as the strong fibers, a conclusion that is in harmony with their different physical properties and defines their different activities in vivo (33, 34). There is no significant difference between the $S_i$ values of strong and weak fiber forms, which is an indication of similar arrangement of structured protein monomers in the two strains.

LD reports on angular orientation only of oriented residues; other randomly oriented chromophores will have zero LD signal. Our data indicate that the fraction of well-oriented tyrosine residues is in similar structural environments in both strains. The small value of the $L_b$ angle of tyrosine residues in prion fibers suggests a rather narrow angular coordinate distribution. If there had been free rotation around the Cβ–Cγ bond, an $L_b$ angle close to 50° would have been obtained, given the 60° of the $L_a$ transition moment angle. The narrow angle distribution is consistent with the stacking arrangements of the aromatic side chains.

**Local Environments of Tyrosine Residues.** Whereas the global character of the spectra suggested a general structural motif for the organization of aromatic rings in amyloid fibers, LD was sensitive enough to report on structural variations owing to different underlying environments between fiber forms. We observed for the $L_b$ transition a difference between the LD and absorption bands, resulting in a wavelength dependence of the ratio $L_b/A_{iso}$, more pronounced in the weak prion. The $L_b$ LD band exhibits a more pronounced vibrational structure than the absorption band. This result indicates that the orientation distribution of tyrosine $L_b$ transition moment is also accompanied by some environmental distribution. Whereas the absorption band is broader owing to inhomogeneous broadening—different tyrosine chromophores experiencing somewhat different environments—the LD band reflects a systematic correlation between environment and orientation. The variation of $L_b/A_{iso}$ ratio with the wavelength may be accounted for by an inhomogeneous solvent effect in terms of curve modeling (Fig. 4). The analysis is based on a spectrum of p-methoxynaphthalene in hexane, taken as a model of tyrosine in a nonpolar environment (note the pronounced vibrational fine structure of the $L_b$ band, Fig. 4B). This well-resolved spectrum can be made similar to the absorption and LD spectra that we observe for the prion samples by simply overlaying a set of copies with infinitesimally different wavelength shifts (i.e., simulating many slightly different local environments that tyrosine side chains might experience). As opposed to the absorption bands, the LD bands of the strains have different profiles, which indeed supports the fact that some tyrosine residues are experiencing different environments. This is consistent with recent studies that establish that many side chains in the two fiber forms are exposed to different chemical environments (25). From amide hydrogen/deuterium exchange

![Fig. 2. Binding of ThT to prion fibers. Absorbance (A) and LD (B) spectra of weak (solid line) and strong (dashed line) Sup35NM fibers in aqueous solution in presence of ThT under an applied shear force of 3,100 s⁻¹. The transition dipole moments of the electronic transitions of ThT are depicted at the bottom.](image)

### Table 1. Angles of tyrosine transition dipole moments, $L_a$ and $L_b$, relative to the fiber axis, and order parameters $S$, $S_g$, and $S_i$ of weak and strong Sup35 prion strains

<table>
<thead>
<tr>
<th>Alignment technique</th>
<th>Phenotype</th>
<th>$L_a$ (232 nm), °</th>
<th>$L_b$ (278 nm), °</th>
<th>$S$</th>
<th>$S_g$</th>
<th>$S_i$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aqueous solution with ThT</td>
<td>Weak</td>
<td>N/A</td>
<td>31–36</td>
<td>0.06</td>
<td>N/A</td>
<td>N/A</td>
</tr>
<tr>
<td></td>
<td>Strong</td>
<td>N/A</td>
<td>27–33</td>
<td>0.017</td>
<td>N/A</td>
<td>N/A</td>
</tr>
<tr>
<td>Sucrose solution</td>
<td>Weak</td>
<td>58–59</td>
<td>31–36</td>
<td>0.13</td>
<td>0.60</td>
<td>0.22</td>
</tr>
<tr>
<td></td>
<td>Strong</td>
<td>59–61</td>
<td>27–33</td>
<td>0.09</td>
<td>0.42</td>
<td>0.20</td>
</tr>
<tr>
<td>PVA humid gel</td>
<td>Weak</td>
<td>60–61</td>
<td>31–36</td>
<td>0.14</td>
<td>0.63</td>
<td>0.22</td>
</tr>
<tr>
<td></td>
<td>Strong</td>
<td>61–62</td>
<td>27–33</td>
<td>0.12</td>
<td>0.62</td>
<td>0.19</td>
</tr>
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*As determined in solution in the presence of ThT or in sucrose solution and in stretched humid PVA matrix. Angle ranges refer to error estimates of LD and $S$ (see Fig. S1 for details). N/A, not assessed.*
of amylin (islet amyloid polypeptide) suggested that the beta-sheets are stacked side-by-side and the aromatic rings are facing the hydrophobic core of the fiber with distances between the rings of adjacent sheets of <6.5 Å (36). Our Φ angles for tyrosine residues in Sup35NM fibers are consistent with stacking interactions that preferentially orient the tyrosine planes parallel with the fiber axis, as proposed in those previous studies (Fig. 5).

LD data point to a common structural arrangement of the aromatic side chains in the weak and strong strains of Sup35 prions, which might be extended to other amyloid-prone sequences because the LD spectra of glucagon (27), β2-microglobulin (26), and a short sequence of the amyloid-β peptide (28) closely resemble those observed here for the Sup35 strains.

Differences between amyloid-based prion strains are thought to be a result of differences in packing interactions in the fiber. Our analysis of the LD/A-abs ratio shows that some tyrosines in the prion fiber forms experience environmental variations. According to quantum chemical calculations for p-methylphenol, a chromophore of tyrosine, a symmetric broadening of UV bands is expected in a hydroxyl polar environment: Hydrogen bonding between the phenol OH hydrogen and an external oxygen atom is predicted to give a red shift, whereas hydrogen bonding between phenol oxygen and a hydrogen of an OH group is expected to give a blue shift of similar magnitude (2–4 nm) (38). If all tyrosines had been oriented at the same angle and exposed to similar local environments, then the LD spectrum would have had the same shape as the (smeared) absorption spectrum, and LD/A-abs would have been constant. However, if differently shifted tyrosines are also somehow differently oriented, the characteristic wavelength dependence that is observed in the prion LD spectrum can be reproduced. Only a superposition of LD spectra with different amplitudes [different ϕ(λ) values] and with shapes corresponding to differently shifted absorptions can explain the observations (23, 25).

**Discussion**

We have outlined a generally applicable method to gain further structural insight into the structure of amyloid fibers. Amyloid fibers are defined by their beta-sheet content. We add that a general feature of this fold is the stacking of aromatic rings with a relatively defined geometry. This work suggests that in addition to a cross-beta arrangement of the protein backbone aromatic rings are arranged at a 60°/30° orientation relative to the fiber axis (Fig. 5). Moreover, this sensitive spectroscopic technique further permits detection of local environmental variations of amino acid side groups that are likely at the core of the prion strain phenomena.

Determining the spatial arrangement of aromatic residues in amyloid fibers will help to build models of fiber structure. It has been proposed that aromatic residues may have an important role in fiber assembly (35, 36). The attractive nonbonded interactions—π-stacking interactions—between the aromatic rings are suggested to contribute to stacking energy and order of amyloid fibers (35). The most common π-stacking geometry in proteins is the off-centered parallel orientation (parallel displaced) (37). Distance constraints attained by solid-state NMR spectroscopy for the phenylalanine residue of a short sequence of amylase (islet amyloid polypeptide) suggested that the beta-sheets are stacked side-by-side and the aromatic rings are facing the hydrophobic core of the fiber with distances between the rings of adjacent sheets of <6.5 Å (36). Our Φ angles for tyrosine residues in Sup35NM fibers are consistent with stacking interactions that preferentially orient the tyrosine planes parallel with the fiber axis, as proposed in those previous studies (Fig. 5).

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observed wavelength dependence of the LD spectrum (39). For both prion strains the simulation of the absorption and LD spectra (Fig. 4 C and D) is consistent with one dominating blue-shifted fraction of tyrosines oriented near 30° (for L_s) in a non-polar environment (presumably in the interior of the hydrophobic fiber core). The remaining tyrosines may be blue-shifted or red-shifted, depending on whether they are hydrogen bond donors or hydrogen bond acceptors (38). We think that tyrosines located in “intermediate” regions of the amyloid core (25) are able to adopt different orientations compared with the residues that are buried in the interior of the rigid regions (Fig. 5). In proteins, aromatic rings in exposed regions are considered to have less constraint in their motion than buried rings (40). According to solid-state NMR spectroscopy studies of Sup35NM fibers, tyrosine residues outside the amyloid rigid core are in beta-strand conformation but in a different environment compared with the core residues (24). Additionally, the aromatic interactions outside the amyloid core are considered to drive the aggregation of different Sup35NM monomers (41). If aromatic rings outside the amyloid core are freely rotating they will not contribute to the LD signal. However, if they are somehow oriented but their environment is different this will cause a shift in the transition energies, resulting in a shift of the LD band compared to the absorption band and accordingly in a variation of the LD/A_friends with wavelength. This indicates that in Sup35 prion strains there is some heterogeneity in orientation and environment of the tyrosine residues, which will contribute to differentiate the strains. The different biological performance of the strains can thus originate from variations in packing of beta-sheet building blocks, which is to say that the building blocks find different ways of sticking together depending on the environmental conditions.

The present approach provides insight about organization and assembly of amyloid-prone protein aggregates. LD is capable of detecting variations in the tyrosine chromophore location, solvent-exposed vs. buried tyrosines, reflecting on the packing of the prion core. We are only beginning to understand how aromatic residues are spatially arranged in amyloid fibers. We cannot determine yet which tyrosine residues are differentially oriented in the two strains, but the replacement of a single tyrosine by phenylalanine will allow obtaining angular data in a corresponding way for a series of selected residues (site-selected LD). LD promises thus to have broad application to structural investigations of amyloids.

**Materials and Methods**

**Sample Preparation.** Recombinant prion domain of the yeast prion protein Sup35NM was expressed and purified as described elsewhere (42). The protein concentration was determined by UV/visible using a theoretical extinction coefficient of 25,600 M⁻¹·cm⁻¹. Purified protein in 8 M urea was desalted by addition of five volumes of methanol, storage at ~80 °C, and centrifugation at 4 °C for 15 min at 15,000 × g. Protein was recovered as a white pellet. Yeast prion fiber seeds were prepared from an in vivo prion template as described elsewhere (25). Strain-specific prion fiber samples were prepared by resuspending methanol-precipitated NM protein in 5% (monomer concentration) solutions of strain-specific seeds and incubation at either 4 °C (strong prion fibers) or 37 °C (weak prion fibers) in 10 mM Tris HCl (pH 7.4) and 150 mM sodium chloride. The prion fiber samples (5 mg/mL) were diluted to a concentration of 0.5 mg/mL either with ultrapure water containing 0.1% SDS or with 50% wt/vol sucrose aqueous solution for LD flow experiments. The polymer matrix was prepared with 10 wt/wt% of PVA (with molecular weight ca. 80,000) (Elvanol 71-30; DuPont) in ultrapure water, heated to about 90 °C with vigorous stirring for 2 h. PVA solution was allowed to cool down to room temperature and, after careful mixing with prion fiber sample, the solution was spread on a glass surface as a thin layer and left to dry at room temperature for at least 2 d. The final concentration of fibers was 0.5 mg/mL.

**LD and Absorbance Measurements.** LD and absorbance spectra were recorded on a Chirascan instrument (Applied Photophysics Ltd.) in two different media: (i) in aqueous solution subjected to shear flow and (ii) in a humid gel of PVA subjected to mechanical stretch. To avoid artifacts owing to different monochromator dispersion and different scattering angles, LD and absorbance spectra were measured on the same instrument. The spectra were corrected by subtracting a scattering profile represented by a Rayleigh scattering model (Supporting Information).

Flow solution experiments were performed with a Couette cell that consists of two concentric quartz (fused silica, Suprasi; Hellma) cylinders, one static (the inner one) and one rotating (the outer one) (Fig. 1). Light passes through both cylinders along the radius of the cylinders, thereby passing two times through the sample, which is contained in the annular gap between the cylinders (cell path length is 1 mm and the sample volume is about 2.0 mL). To improve the measuring sensitivity in the far UV region sucrose was added as a refractive index matching agent. This is found to eliminate or strongly reduce the light scattering but also to improve the orientation as a result of increased solvent viscosity and thereby attenuated rotary diffusion (increased ratio G/D_0).

Stretched PVA hydrogel experiments were performed with the help of a stretching device (Fig. 1). A Fragment, ca. 2 x 2 cm, was cut from the dry film and mounted in a stretching device, which was then inserted into a humidity chamber and allowed to equilibrate with a pure water solution at the bottom of the chamber, giving 100% relative humidity. In practice this was found to yield a PVA hydrogel containing about 50% water. The humid film was stretched at room temperature to various degrees of stretch, defined as the length ratio l_0/l, being the total length of the stretched film, l_0 the length in unstretched state. We shall denote l_0 as R_0, which is connected to the “stretch ratio” R_0 in the Kratyky model according to the relation R_0 = (R_0)^3/2 (30).

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