Measurement of transverse hyperfine interaction by forbidden transitions

The MIT Faculty has made this article openly available. Please share how this access benefits you. Your story matters.

<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>As Published</td>
<td><a href="http://dx.doi.org/10.1103/PhysRevB.92.020101">http://dx.doi.org/10.1103/PhysRevB.92.020101</a></td>
</tr>
<tr>
<td>Publisher</td>
<td>American Physical Society</td>
</tr>
<tr>
<td>Version</td>
<td>Final published version</td>
</tr>
<tr>
<td>Accessed</td>
<td>Thu Dec 06 03:11:48 EST 2018</td>
</tr>
<tr>
<td>Citable Link</td>
<td><a href="http://hdl.handle.net/1721.1/97692">http://hdl.handle.net/1721.1/97692</a></td>
</tr>
<tr>
<td>Terms of Use</td>
<td>Article is made available in accordance with the publisher's policy and may be subject to US copyright law. Please refer to the publisher's site for terms of use.</td>
</tr>
<tr>
<td>Detailed Terms</td>
<td></td>
</tr>
</tbody>
</table>
Quantum technologies promise to revolutionize many fields, ranging from precision sensing to fast computation. The success of novel technologies based on quantum effects rests on engineering quantum systems robust to noise and decoherence and on controlling them with high precision. Solid-state systems comprising nuclear spins have emerged as promising candidates, since the nuclear spin qubits are only weakly coupled to external fields and thus exhibit long coherence times. In order for nuclear spins to be used as good qubits, there are two important requirements: Their Hamiltonians need to be known with very high precision, as this would enable applying, e.g., optimal control methods [1,2], and strong driving should be available, in order to achieve fast gates. Here we show how to meet these two requirements by exploiting nominally forbidden transitions in a hybrid electronic-nuclear spin system associated with the nitrogen-vacancy center in diamond [3]. Specifically, we use second-order effects due to mixing of the electronic and nuclear spin states [4] in order to identify with high precision their coupling strength and to enhance the nuclear spin nutation rate [5].

The nitrogen-vacancy (NV) center is a naturally occurring point defect in diamond [6]. Owing to its optical properties and long coherence times, it has emerged as a versatile system for quantum sensing [7–9], quantum information [10,11], and photonics applications [12,13]. The nuclear 14N spin often plays an important role in these applications. Not only can it serve as a qubit in small quantum algorithms [14–16], but it can also be used to enhance the readout fidelity of the NV electronic spin [17] and achieve more sensitive detection of magnetic fields [18,19] and rotations [20,21]. These applications are made possible by the hyperfine interaction between the NV electronic and nuclear spins.

While the secular part of the NV-14N Hamiltonian has been well characterized before [22–24], the transverse hyperfine coupling is more difficult to measure [25] and published values do not match well [26–28]. The most precise characterization to date has been achieved by ensemble electron spin resonance (ESR) techniques [27]. In that work, the ESR spectrum of an ensemble of NV centers was measured by induction methods while applying a magnetic field along the (110) direction to amplify nominally forbidden transitions. This method is not applicable to single NV centers, since the strong transverse field would quench the spin-dependent optical contrast.

Here we propose a different strategy to measure the transverse hyperfine coupling that can be carried out with optically detected magnetic resonance. Owing to this method we can determine the value of the transverse coupling with high precision. The method is not restricted to the NV spin system, but could be applied more generally to other electronic-nuclear spin systems, such as phosphorus [29] or antimony [30] donors in silicon, defects in silicon carbide [31,32], or quantum dots [33]. Precise knowledge of the hyperfine interaction tensor would enable achieving more precise control, elucidating modulations of the NV echo dynamics or, as we show here, achieving faster Rabi nutation of the nuclear spin.

**Theoretical model.** The NV ground state is a two-spin system given by the electronic spin of the NV center ($S = 1$) and the nuclear spin ($I = 1$) of the substitutional 14N adjacent to the vacancy that comprise the defect. In the experiments, we are only interested in two of the nuclear spin levels ($m_I = +1.0$) that we drive on resonance, while the third level can be neglected. Then, the Hamiltonian of the reduced system [34,35] is given by $\mathcal{H} = \mathcal{H}_{\parallel} + \mathcal{H}_{\perp}$, where the secular, $\mathcal{H}_{\parallel}$, and nonsecular, $\mathcal{H}_{\perp}$, terms are

$$\mathcal{H}_{\parallel} = \Delta S_s^2 + \left( \gamma_e B_z + A_{1/2} \right) S_z + (Q + \gamma_n B_z) I_z + A_{1/2} S_z I_z,$$

$$\mathcal{H}_{\perp} = \sqrt{2} A_{\perp} (S_z I_z + S_y I_y).$$

(1)

Here, $S$ and $I$ are the electron spin-1 and nuclear spin-1/2 operator, respectively. Also, $\Delta = 2.87$ GHz is the zero-field splitting and $Q = -4.945$ MHz [23] is the nuclear quadrupolar interaction. The NV spin is coupled to the nuclear spin by a hyperfine interaction with a longitudinal component $A_{1/2} = -2.162$ MHz [23] and a transverse component $A_{\perp}$ which we...
want to estimate. A magnetic field $B_z$ is applied along the NV crystal axis [111] to lift the degeneracy of the $m_z = \pm 1$ level, yielding the electron and nuclear Zeeman frequencies $\gamma_e B_z$ and $\gamma_n B_z$, where $\gamma_e = 2.8 \text{ MHz/G}$ and $\gamma_n = -0.308 \text{ kHz/G}$.

Let $|m_e, m_n\rangle$ be eigenstates of $\mathcal{H}_r$. The transverse coupling $A_\perp$ mixes states connected via zero-quantum (ZQ) transitions, $|+1, 0\rangle \leftrightarrow |0, 1\rangle$ and $|0, 0\rangle \leftrightarrow |-1, 1\rangle$. Diagonalization of the total Hamiltonian can then be achieved by rotating the two ZQ subspaces with a unitary transformation $U_{\text{ZQ}} = e^{-i(\sigma^e_z \hat{\omega} + \gamma_n B_z)}$, where we defined $\sigma^e_z = i(|+1, 0\rangle, |0, 1\rangle - |0, 1\rangle, |+1, 0\rangle)$, $\sigma^- = i(|0, 0\rangle, |-1, 1\rangle - |-1, 1\rangle, |0, 0\rangle)$, and the rotation angles are

$$
\tan(2\theta^+) = \frac{2A_\perp}{\Delta + \gamma_e B_z - \gamma_n B_z - \mathcal{Q}},
$$

$$
\tan(2\theta^-) = \frac{-2A_\perp}{\Delta - \gamma_e B_z - \gamma_n B_z + \mathcal{Q}}.
$$

Because of this level mixing, a field on resonance with the nuclear spin transition also drives electronic transitions. Although the electronic spin state is unchanged to first order, the nominally forbidden transitions result in an enhancement of the nuclear state population. As a result, a 1 $\mu$s laser excitation polarizes the NV-14N system into the $|0, 1\rangle$ state.

Then, the NV spin is prepared in the desired Zeeman state by a strong microwave (MW) pulse ($\tau_p \approx 50$ ns) before coherently driving the nuclear spin by an rf field on resonance with the nuclear transition $|m_n, 1\rangle \leftrightarrow |m_n, 0\rangle$, for a duration $\tau$ (see Fig. 1). Finally, the nuclear spin state is detected by employing a MW selective pulse ($\tau_p \approx 700$ ns) that maps the nuclear spin state onto the NV spin, which in turn can be read out optically due to spin-dependent fluorescence emission intensity. The nuclear Rabi oscillations in Fig. 2 clearly show that for a fixed driving strength, the effective Rabi frequency is quite different in the three electronic spin manifolds.

Here, $\alpha_{\text{enh}}$ denote the enhancement factors in each manifold of the NV spin,

$$
\alpha_{+1} \approx 1 + \frac{\gamma_e}{\gamma_n} \frac{A_\perp}{\Delta + \gamma_e B_z - \gamma_n B_z - \mathcal{Q}},
$$

$$
\alpha_0 \approx 1 - \frac{\gamma_e}{\gamma_n} \left( \frac{A_\perp}{\Delta - \gamma_e B_z - \gamma_n B_z + \mathcal{Q}} \right),
$$

$$
\alpha_{-1} \approx 1 + \frac{\gamma_e}{\gamma_n} \frac{A_\perp}{\Delta - \gamma_e B_z - \gamma_n B_z + \mathcal{Q}},
$$

where we show expressions exact up to the first order in $\vartheta^\pm$ (see Ref. [34] for the exact expressions). The Hamiltonian $\mathcal{H}_e$ can be neglected since electronic spin transitions are far off resonance.

Owing to the strong dependence of the enhancement factors on the transverse hyperfine coupling, we can determine $A_\perp$ with high precision from measurement of the 14N Rabi oscillations.

**Experiments.** We used a home-built confocal microscope to measure the transverse hyperfine interaction of a single NV center in an electronic grade diamond sample (Element Six, 14N concentration $n_{14N} < 5$ ppb, natural abundance of 13C). The NV center is chosen to be free from close-by 13C. We worked at magnetic fields (300–500 G) close to the excited state level anticrossing so that during optical illumination at 532 nm, polarization of the NV spin can be transferred to the nuclear spin by their strong hyperfine coupling in the excited state [36]. As a result, a 1 $\mu$s laser excitation polarizes the NV-14N system into the $|0, 1\rangle$ state.

The new frame by a caret, we obtain $\hat{\mathcal{H}}_r$. The nutation frequency, as we explain below.

**FIG. 1.** (Color online) Left: Energy levels of the reduced NV-14N spin system, showing the transitions that are mixed by transverse hyperfine coupling. Right: Experimental sequence used to measure the nuclear 14N Rabi frequency in the three NV manifolds.

MO CHEN, MASASHI HIROSE, AND PAOLA CAPPPELLARO

**PHYSICAL REVIEW B 92, 020101(R) (2015)**

020101-2
To confirm the expected dependence of the Rabi enhancement factors on the external magnetic field and the NV state, we measured the Rabi oscillations at the three electronic spin manifolds with varying magnetic field $B_z$. As shown in Fig. 3, the measured Rabi frequencies match well with the theoretical model. It is worth noting that contrary to the static pseudonuclear Zeeman effect [4], there is a large enhancement ($\alpha_0 \approx 16$, $\alpha_{\pm 1} \approx -9$) even at zero field. Also, close to the ground state avoided crossing ($B \approx 0.1$ T), the enhancement can become very large, exceeding 100. The validity of our approximation in this regime can be confirmed by numerical simulations [34].

While these experiments could be used to extract $A_\perp$, this is not a practical method to obtain a good enough estimate. The range of magnetic field is restricted by the need to be close to the excited state level anticrossing to achieve a good polarization of the nuclear spin. The number of acquired points is limited by the time it takes to change and properly align the external magnetic field. In addition, there might be variations in the bare Rabi frequency in the three manifolds, because of different responses of the electronics used to drive the nuclear spins at the different frequencies.

In order to avoid these difficulties, we fixed the magnetic field to 509 G and instead linearly swept the amplitude of the rf driving ($B_1$). With this procedure, we do not need an independent measure of the bare Rabi frequency in order to extract the transverse hyperfine coupling strength. The relative rf amplitudes $B_1$ obtained when varying the driving strength can be measured at each nuclear resonance frequency by monitoring the rf voltage with an oscilloscope, confirming its linear dependence with applied power.

We thus measure the effective nuclear Rabi frequency as a function of the normalized rf amplitude $B_1 / |B_{1,\text{max}}|$ in all three electronic manifolds (Fig. 4). The measured Rabi frequency $\Omega_m$ is related to its on-resonance value by $\Omega_m = \sqrt{\Omega^2 + \delta^2}$, where $\delta$ is the detuning from the nuclear spin resonance frequency. We incorporate this unknown, small detuning in our model and fit the experimental data with the Rabi enhancement formulas (5)–(7). From the fit, we obtain an estimate of the transverse hyperfine coupling, $A_\perp = -2.62 \pm 0.05$ MHz, in good agreement with recently published values and with better precision.

In order to achieve even better precision, we need to consider all the sources of uncertainty and errors. We find that small errors from imperfect MW π pulses and nuclear polarization only contribute to a reduced fluorescent contrast, but do not affect the estimate of the Rabi frequency under our experimental condition. The detuning of the selective MW and rf pulses from resonance and uncertainty in $A_\parallel$ contributes only linearly to the uncertainty. All these minor errors and uncertainties hardly affect the final uncertainty in the estimate of $A_\perp$ [34]. The major source of error arises instead from the uncertainty in the measured Rabi frequency, which is limited by the photon shot noise of the optical readout process. Therefore, the precision of the estimate could be improved with more averaging, at the expense of a longer measurement time. Currently, our total measurement time is limited by the stability of the experimental setup, yielding $\delta A_\perp \sim 50$ kHz. Improving the stability of the setup by reducing thermal fluctuations will further improve the precision of our results.

FIG. 2. (Color online) $^{14}$N Rabi oscillations at $B = 450$ G, $B_1 \approx 3.3$ G in the three NV manifolds (red solid line, $m_s = 0$; black dashed line, $m_s = -1$; gray dotted line, $m_s = +1$). Here, the dots are the experimental results, while the lines are fits to cosine oscillations. The different baseline of the $m_s = -1$ curve is due to small differences in the fluorescence emission of different nuclear manifolds [36].

FIG. 3. (Color online) $^{14}$N Rabi frequency in the three NV manifolds (red solid line, $m_s = 0$; black dashed line, $m_s = -1$; gray dotted line, $m_s = +1$) as a function of the bare Rabi frequency at $B = 509$ G.

FIG. 4. (Color online) Measured enhanced $^{14}$N Rabi frequency in the three NV manifolds (red solid line, $m_s = 0$; black dashed line, $m_s = -1$; gray dotted line, $m_s = +1$) as a function of the bare Rabi frequency at $B = 509$ G.
tations and noise in the driving field (also using decoupling schemes [37,38]), or by employing small ensembles or more efficient optical readout methods such as solid-immersion lenses [39] and charge-state sensing [40], could provide higher precision. Then, the limit would come from uncertainties in $\gamma_n$ and $\gamma_a$, with a relative error of $10^{-4}$ [26,41], yielding an uncertainty in $A_{\perp}$ of a few hundred Hz [34].

**Conclusions.** In conclusion, we observed enhanced nuclear Rabi oscillations in the NV-14N system due to level mixing between electronic and nuclear spin states. We harness the strong dependence of this enhancement on the transverse hyperfine coupling to determine its value with high precision. Theoretical analysis predicts an enhancement factor of almost three orders of magnitude when the magnetic field is close to the ground state level anticrossing, promising fast manipulation of the nuclear spin qubit at $\sim$MHz rates, with only moderate driving strengths. More broadly, the method presented here can be applied to many other electron-nuclear hybrid spin systems to similarly characterize their interaction Hamiltonian with high precision. Our results indicate that taking into account the nonsecular parts of a system’s Hamiltonian is crucial to achieving faster and more accurate control of the quantum system.

This work was supported in part by the U.S. Air Force Office of Scientific Research Grant No. FA9550-12-1-0292 and by the U.S. Office for Naval Research Grant No. N00014-14-1-0804. M.C. and M.H. contributed equally to this work.


