Precision measurements of $A^{n \over 1}$ in the deep inelastic regime

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Precision measurements of $A_{11}^p$ in the deep inelastic regime

The Jefferson Lab Hall A Collaboration

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Ever since the European Muon Collaboration determined that the quark-spin contribution was insufficient to account for the spin of the proton [1,2], the origin of the nucleon spin has been an open puzzle; see Ref. [3] for a recent review. Recently, studies of polarized proton–proton collisions have found evidence for a non-zero contribution from the gluon spin [4,5] and for a significantly positive polarization of $\bar{u}$ quarks [6]. The possible contribution of parton orbital angular momentum (OAM) is also under investigation. In the valence quark region, combining spin-structure data obtained in polarized-lepton scattering on protons and neutrons allows the separation of contributions from up and down quarks and permits a sensitive test of several theoretical models.

In inelastic scattering (DIS), nucleon structure is conventionally parameterized by the unpolarized structure functions $F_1(x, Q^2)$ and $F_2(x, Q^2)$, and by the polarized structure functions $g_1(x, Q^2)$ and $g_2(x, Q^2)$, where $Q^2$ is the negative square of the four-momentum transferred in the scattering interaction and $x$ is the Bjorken scaling variable, which at leading order in the infinite-momentum frame equals the fraction of the nucleon momentum carried by the struck quark. One useful probe of the nucleon spin structure is the asymmetry $A_1 = (\sigma_{1/2} - \sigma_{3/2})/(\sigma_{1/2} + \sigma_{3/2})$, where $\sigma_{1/2,3/2}$ is the cross section of virtual photoproduction of the corresponding quark (for a total spin projection of 1/2 or 3/2) along the virtual-photon momentum direction. At finite $Q^2$, this asymmetry may be expressed in terms of the nucleon structure functions as [7]

$$A_1(x, Q^2) = [g_1(x, Q^2) - \gamma^2 g_2(x, Q^2)] / F_1(x, Q^2),$$

where $\gamma^2 = 4M^2 x^2 / Q^2$ and $M$ is the nucleon mass. For large $Q^2$, $\gamma^2 < 1$ and $A_1(x) \approx g_1(x) / F_1(x)$; since $g_1$ and $F_1$ have the same $Q^2$ evolution at leading order and at next to leading order (NLO) [8–10], $A_1$ may be approximated as a function of $x$ alone. Through Eq. (1), measurements of $A_1$ on proton and neutron targets also allow extraction of the flavor-separated ratios of polarized to unpolarized parton distribution functions (PDFs), $(\Delta q(x) + \Delta \bar{q}(x))/(q(x) + \bar{q}(x))$. Here, $q(x) = q^1(x) + q^2(x)$ and $\Delta q(x) = q^1(x) - q^2(x)$, where $q^1(x)$ is the probability of finding the quark $q$ with a given value of $x$ and with spin (anti)parallel to that of the nucleon. This Letter reports a high-precision measurement of the neutron $A_1$, $A_1^n$, in a kinematic range where theoretical predictions begin to diverge.

A variety of theoretical approaches predict that $A_1^n \to 1$ as $x \to 1$. Calculations in the relativistic constituent quark model (RCQM), for example, generally assume that SU(6) symmetry is broken via a color hyperfine interaction between quarks, lowering the energy of spectator-quark pairs in a spin singlet state relative to those in a spin triplet state and increasing the probability that, at high $x$, the struck quark carries the nucleon spin [11].

In perturbative quantum chromodynamics (pQCD), valid at large $x$ and large $Q^2$ where the coupling of gluons to the struck quark is small, the leading-order assumption that the valence quarks have no OAM leads to the same conclusion about the spin of the struck quark [12,13]. Parameterizations of the world data, in the context of pQCD models, have been made at NLO both with and without this assumption of hadron helicity conservation. The LSS (BBS) parameterization [14] is a classic example of the former; Avakian et al. [15] later extended that parameterization to explicitly include Fock states with nonzero quark OAM. Both parameterizations enforce $A_1^n(x \to 0) < 0$ and $A_1^n(x \to 1) \to 1$ and predict $\lim_{x \to 1} (\Delta d + \Delta \bar{d})/(d + \bar{d}) = 1$. However, the OAM-inclusive parameterization predicts that $(\Delta d + \Delta \bar{d})/(d + \bar{d})$, which is negative at low $x$, crosses zero at significantly higher $x$ than predicted by LSS (BBS). Recently, the Jefferson Lab Angular Momentum (JAM) Collaboration performed a global NLO analysis at $Q^2 = 1$ (GeV/c)^2 to produce a new parameterization [16], and then systematically studied the effects of various input assumptions [17]. Without enforcing hadron helicity conservation, JAM found that the ratio $(\Delta d + \Delta \bar{d})/(d + \bar{d})$ remains negative across all $x$; regardless of this initial assumption, the existing world data can be fit approximately equally well with or without explicit OAM terms of the form given by Ref. [15]. The scarcity of precise DIS neutron data above $x \approx 0.4$, combined with the absence of such data points for $x \geq 0.6$, leaves the pQCD parameterizations remarkably unconstrained.

The statistical model treats the nucleon as a gas of massless partons at thermal equilibrium, using both chirality and DIS data to constrain the thermodynamical potential of each parton species. At a moderate $Q^2$ value of 4 (GeV/c)^2, $A_1^n(x \to 1) \to 0.6 - \Delta u(x)/\bar{u}(x) \sim 0.46$ [18]. Statistical-model predictions are thus in conflict with hadron helicity conservation. A modified Nambu–Jona-Lasinio (NJL) model, including both scalar and axial-vector diquark channels, yields a similar prediction for $A_1^n$ as $x \to 1$ [19]. A recent approach based on Dyson–Schwinger equations (DSE) predicts $A_1^n(x = 1) = 0.34$ in a contact-interaction framework, and 0.17 in a more realistic framework in which the dressed-quark mass is permitted to depend on momentum [20]; the latter prediction is significantly smaller than either the statistical or NJL prediction at $x = 1$. However, existing DIS data do not extend to high enough $x$ to definitively favor one model over another.

Measurements of the virtual-photon asymmetry $A_1$ can be made via doubly polarized electron–nucleon scattering. With both
beam and target polarized longitudinally with respect to the beamline, $A_L = (\sigma^{1+} - \sigma^{1-})/(\sigma^{1+} + \sigma^{1-})$ is the scattering asymmetry between configurations with the electron spin anti-aligned (↓) and aligned (↑) with the beam direction. Meanwhile, $A_\perp = (\sigma^{1+} - \sigma^{1-})(\sigma^{1+} + \sigma^{1-})$ is measured with the target spin oriented horizontally, perpendicular to the incident beam direction and on the side of the scattered electron. $A_1$ may be related to these asymmetries through [7]:

$$A_1 = \frac{1}{D(1 + \eta \epsilon)} A_{\parallel} - \frac{\eta \epsilon}{D(1 + \eta \epsilon)} A_{\perp}, \quad (2)$$

where the kinematic variables are given in the laboratory frame by $D = (E - E')/(E(1 + \epsilon R))$, $\eta = \epsilon \sqrt{Q^2}/(E - \epsilon E')$, $d = D\sqrt{2f_{1+}(1 + \epsilon)}$, and $\epsilon = \eta(1 + \epsilon)/2\epsilon$. Here, $E$ is the initial electron energy; $E'$ is the scattered electron energy; $\epsilon = 1/(1 + 2(1 + 1/\gamma^2)\tan^2(\theta/2))$; $\theta$ is the electron scattering angle, shown in Fig. 1; and $R = \sigma_r/\sigma_t$, parameterized via R1998 [21], is the ratio of the longitudinal to the transverse virtual photoabsorption cross sections.

Experiment E06-014 ran in Hall A of Jefferson Lab in February and March 2009 with the primary purpose of measuring a twist-3 matrix element of the neutron [22]. Longitudinally polarized electrons were generated via illumination of a strained superlattice GaAs photocathode by circularly polarized laser light [23] and delivered to the experimental hall with energies of 4.7 and 5.9 GeV. The rastered 12–15 µA beam was incident on a target of $^3$He gas [24], polarized in the longitudinal and transverse directions via spin-exchange optical pumping of a Rb–K mixture [25] and contained in a 40-cm-long glass cell. The left high-resolution spectrometer [26] and BigBite spectrometer [27] independently detected scattered electrons at angles of $45^\circ$ on beam left and right, respectively.

The longitudinal beam polarization was monitored continuously by Compton polarimetry [28,29] and intermittently by Müller polarimetry [30]. In three run periods with polarized beam, the longitudinal beam polarization $P_L$ averaged 0.74 ± 0.01 $E = 5.9$ GeV), 0.79 ± 0.01 $E = 5.9$ GeV), and 0.63 ± 0.01 $E = 4.7$ GeV). A feedback loop limited the charge asymmetry to within 100 ppm. The target polarization $P_T$, averaging about 50%, was measured periodically using nuclear magnetic resonance [31] and calibrated with electron paramagnetic resonance; in the longitudinal orientation, the calibration was cross-checked with nuclear magnetic resonance data from a well-understood water target.

The raw asymmetry $A_{raw}^{1+(\perp)}$ was corrected for beam and target effects according to $A_{corr}^{1+(\perp)} = A_{raw}^{1+(\perp)}/(P_L P_T f_{N_2}(\cos \phi))$. The dilution factor $f_{N_2} \approx 0.920 \pm 0.003$, determined from dedicated measurements with a nitrogen target and found to be approximately constant across our x range, corrects for scattering from the small amount of N$_2$ gas added to the $^3$He target to reduce depolarization effects [32]. The angle $\phi$, which appears in $A_{corr}^{1+}$, is defined in Fig. 1.

Data for the asymmetry measurements were taken with the BigBite detector stack, which in this configuration included eight wire planes in three orientations, a gas Čerenkov detector [33], a pre-shower + shower calorimeter, and a scintillator plane between the calorimeter layers. The primary trigger was formed when signals above threshold were registered in geometrically overlapping regions of the gas Čerenkov and calorimeter. Wire-plane data allowed momentum reconstruction with a resolution of 1% [33]. With an angular acceptance of 65 msr, BigBite continuously measured electrons over the entire kinematic range of the experiment, and the sample was later divided into x bins of equal size. The variation over the BigBite acceptance of the measured asymmetry in each bin was found to be negligible [33].

Pair-produced electrons, originating from $\pi^\pm$ decay, contaminated the sample of DIS electrons, especially in the lowest x bins. We measured the yield of this process by reversing the BigBite polarity to observe $e^+$ with the same acceptance as that seen by $e^-$ in normal running. A fit to these data, combined with data from the left high-resolution spectrometer and with CLAS EGiB [34] data taken at a similar scattering angle, was used to fill gaps in the kinematic coverage of these special measurements. The resulting correction $f_{pos} = N_{俄罗斯}/N_{大比基}$ quantified the contamination of the electron sample with pair-produced electrons. The underlying double-spin asymmetry $A^{\pi^+\pi^-}$ of the $\pi^\sigma$ production process was measured to be 1–2% using the positron sample obtained during normal BigBite running, and cross-checked against the reversed-polarity positron asymmetry for the available kinematics.

The contamination of the scattered-electron sample with $\pi^-$ was below 3% in all x bins, limited primarily by the efficiency of the gas Čerenkov in eliminating pions from the online trigger. Due to the low contamination level, the asymmetry in pion production had a negligible ($<1\%$) effect on $A_1$ and $A_\perp$, and the pion correction to the asymmetry was therefore treated as a pure dilution $f_{\pi^-}$. Contamination of the positron sample with $\pi^+$ resulted in the dilution factor $f_{\pi^+}$. Particle identification was the dominant overall source of systematic error in this measurement.

The final physics asymmetries $A_{H(\perp)}$, which are listed in Table 1, include internal and external radiative corrections $\Delta A_{H(\perp)}^{RC}$ as well as background corrections:

$$A_{H(\perp)}^{corr} = A_{H(\perp)}^{corr} - f_{\pi^-} A_{H(\perp)}^{\pi^+} + f_{\pi^+} A_{H(\perp)}^{\pi^-} + \Delta A_{H(\perp)}^{RC}.$$  

To compute $\Delta A_{H(\perp)}^{RC}$, the asymmetries were reformulated as polarized cross-section differences using the F1200 [35] parameterization for the radiated unpolarized cross section. The polarized elastic tail was computed [36] and found to be negligible in both the parallel and perpendicular cases; therefore, this tail was not subtracted. Radiative corrections were then applied iteratively, according to the formalism first described by Mo and Tsai [37,38] for the unpolarized case, and checked by the Akushievich et al. [39] formalism for the polarized case. The DSSV global NLO analysis [40,41] was used as an input for the DIS region; the integration phase space was completed in the resonance region with the MAID model [42], and in the quasi-elastic region with the Bosted nucleon form factors [43] smeared with a scaling function [44]. The final results were then converted back to asymmetries. The contribution of these corrections to the uncertainty on $A_{H(\perp)}$, estimated by varying the input models and radiation thicknesses of materials in the beamline and along the trajectory of the scattered electrons, was $<2\%$. Energy-loss calculations were performed within the radiative-correction framework and not as part of the acceptance calculation; the effect of interbin migration due to energy loss was found to be small, and was neglected in the analysis. Smearing effects across individual x bins, due to the finite detector resolution, contributed a negligible amount to the uncertainty.
A detailed discussion of the radiative corrections may be found in Ref. [45].

Polarized $^3$He targets are commonly used as effective polarized neutron targets because, in the dominant $S$ state, the spin of the $^3$He nucleus is carried by the neutron. To extract the neutron asymmetry $A^p_n$ from the measured asymmetry $A^{1\text{He}}$ on the nuclear target, we used a model for the $^3$He wavefunction incorporating $S$, $S'$, and $D$ states as well as a pre-existing $\Delta(1232)$ component [46]:

$$A^1_p = \frac{F_2^{1\text{He}}}{F_2^{\text{SLAC}}} \left[ A^{1\text{He}}_1 - \frac{F_0^{p}}{F_0^{1\text{He}}} P_n A^p_1 \left( 1 - \frac{0.014}{2F_p} \right) \right].$$

The effective proton and neutron polarizations were taken as $P_p = -0.028^{+0.009}_{-0.004}$ and $P_n = 0.860^{+0.036}_{-0.020}$ [47], $F_2$ was parameterized with FIF209 [35] for $^3$He and with CJ12 [48] for the neutron and proton, while $A^p_1$ was modeled with a $Q^2$-independent, three-parameter fit to world data [1,2,34,49-53] on proton targets. Eq. (4) was applied separately to the data from the two beam energies, at an average measured $Q^2$ value of $2.59$ (GeV/c)$^2$ ($E = 4.7$ GeV) and $3.67$ (GeV/c)$^2$ ($E = 5.9$ GeV). The resulting neutron asymmetry, the statistics-weighted average of the asymmetries measured at the two beam energies, is given as a function of $x$ in Fig. 2 and Table 2 and corresponds to an average $Q^2$ value of $3.078$ (GeV/c)$^2$. Table 2 also gives our results for the structure-function ratio $g_1^p/F_1^p = \langle y (1 + R) \rangle / \langle (1 - \bar{R}) (2 - y) \rangle \cdot \langle A_1 + \tan(\theta/2) A_{1\perp} \rangle$, where $y = (E - E')/E$ in the laboratory frame. This ratio was extracted from our $^3$He data in the same way as $A^1_p$.

Combining the neutron $g_1^p/F_1^p$ with measurements on the proton allows a flavor decomposition to separate the polarized-to-unpolarized-PDF ratios for up and down quarks, giving greater sensitivity than $A^p_1$ to the differences between various theoretical models. When the strangeness content of the nucleon is neglected, these ratios can be extracted at leading order as

$$\frac{\Delta u + \Delta \bar{u}}{u + \bar{u}} = \frac{4}{15} \frac{g_1^p}{F_1^p} \left( 4 + R^{du} \right) - \frac{g_1^p}{15F_1^p} \left( 1 + 4R^{du} \right) \tag{5}$$

$$\frac{\Delta d + \Delta \bar{d}}{d + \bar{d}} = -\frac{1}{15} \frac{g_1^p}{F_1^p} \left( 4 + R^{du} \right) + \frac{4}{15} \frac{g_1^p}{F_1^p} \left( 1 + 4R^{du} \right) \tag{6}$$

where $R^{du} = (d + \bar{d})/(u + \bar{u})$ and is taken from the CJ12 parameterization [48]; $g_1^p/F_1^p$ was modeled with world data [34,51,52,57,59] in the same way as $A^p_1$. Measurements of $g_1^p$ alone were not included in the fit so as not to introduce a model dependence in the choice of $F_1$. An uncertainty of $< 0.009$ for $\Delta u + \Delta \bar{u}/u + \bar{u}$ and $< 0.02$ for $\Delta d + \Delta \bar{d}/d + \bar{d}$ was attributed to the neglect of systematic uncertainties. Other systematic uncertainties were determined from the change in the result from varying each input within its uncertainty. Our results are given in Table 3, and plotted in Fig. 3 along with previous world DIS data and selected model predictions and parameterizations. The $(\Delta u + \Delta \bar{u})/(u + \bar{u})$ results, shown here for reference, are dominated by proton measurements. The semi-inclusive DIS ratios from HERMES [60] and COMPASS [61] are constructed from the published polarized PDFs, using the same unpolarized PDF parameterizations that were applied in the original analyses: CTEQ5L [62] in the case of the HERMES data, and MRST 2006 [63] for the COMPASS data. The uncertainties are therefore slightly larger than could be achieved from the raw data.

Two dedicated DIS $A^3_p$ experiments [64,65] have been approved to run at Jefferson Lab in the coming years; one will use an...
open geometry spectrometer [64]. These experiments will push to higher $x$, achieving greater sensitivity via improved targets and particle identification, and will test the assumption of $Q^2$ independence over a broad kinematic range; such tests are necessary as $A_1^u$ measurements begin to probe quark OAM and higher-twist effects.

Our results for $A_1^u$ and $(\Delta d + \Delta u)/(d + u)$ support previous measurements in the range $0.277 \leq x \leq 0.548$. The $A_1^u$ data are consistent with a zero crossing between $x = 0.4$ and $x = 0.55$, as reported by the Jefferson Lab E99-117 measurement [56]. Our data disfavor the original LSS (BBS) PQCD parameterization [14], while they are consistent with an extension that explicitly includes quark OAM [15]. Our leading-order extraction of $(\Delta d + \Delta u)/(d + u)$ shows no evidence of a transition to a positive slope, as was eventually required by hadron helicity conservation, in the $x$ range probed. It is not yet possible to definitively distinguish between modern models - pQCD, statistical, NJL, or DSE - in the world data to date, but our data does suggest further work in the high-$x$ regime. Our results were obtained with a new measurement technique, relying on an open geometry spectrometer deployed at a large scattering angle with a gas Čerenkov detector to limit the charged-pion background.

Our data, in combination with previous measurements, suggest that additional neutron DIS measurements in the region $0.5 \leq x \leq 0.8$ will be of particular interest in establishing the high-$x$ behavior of the nucleon spin structure; in addition, an extension of the DSE-based approach [20] to $x < 1$ would be valuable. It is our hope that our data will inspire further theoretical work in the high-$x$ DIS region.

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