ABSTRACT

A growing number of close binary stars are being discovered among central stars of planetary nebulae. Recent and ongoing surveys are finding new systems and contributing to our knowledge of the evolution of close binary systems. The push to find more systems was largely based on early discoveries which suggested that 10%–15% of all central stars are close binaries. One goal of this series of papers is confirmation and classification of these systems as close binaries and determination of binary system parameters. Here we provide time-resolved multi-wavelength photometry of the central star of Abell 65 as well as further analysis of the nebula and discussion of possible binary–nebula connections. Our results for Abell 65 confirm recent work showing that it has a close, cool binary companion, though several of our model parameters disagree with the recently published values. With our longer time baseline of photometric observations from 1989 to 2009 we also provide a more precise orbital period of 1.0037577 days.

Key words: binaries: close – planetary nebulae: individual (Abell 65)

1. INTRODUCTION

The complex shapes of planetary nebulae (PNe) provide a valuable and narrow evolutionary window through which we can study the life cycles of intermediate mass stars (typically 1–8 $M_\odot$). Binary interactions are known to play an important role but the extent to which such interactions are needed to make a non-spherical PN is still unclear (for a review see De Marco 2009). Studies have shown that approximately 10%–20% of all PNe harbor close binary stars with orbital periods typically less than 3 days (Bond 2000; Miszalski et al. 2009a). Such close binaries are the result of a common envelope (CE) interaction (Paczynski 1976). The sample of known close binary central stars of planetary nebulae (CSPNe) more than doubled with the work of Miszalski et al. (2009a). However, stellar and system parameters for these objects are very poorly known (De Marco et al. 2008; Hillwig et al. 2010, Papers I and II). Until this situation is alleviated we cannot study this phenomenon statistically. Miszalski et al. (2009b) use this close binary sample to conclude that the nebular morphologies of PNe with close binary central stars tend to be bipolar (see also Bond & Livio 1990). Also, Hillwig (2010) provides a first look at the binary parameters of the known systems and the relationship to similar systems which have no observed PN (either because they are more evolved, or because they did not form a visible PN at all). Additionally, there is increasing observational evidence for a class of intermediate-period CSPN binaries (with periods of months to years). These binaries are discovered directly from radial velocity studies (e.g., Van Winckel et al. 2014), or otherwise inferred via evidence of mass transfer from the PN’s progenitor star onto a companion (e.g., Bond et al. 2003; Miszalski et al. 2012, 2013b; Tyndall et al. 2013). For a review, see Van Winckel et al. (2014).

PNe with post CE binaries are also extremely useful as probes of the CE interaction. Not only do they provide us with recent post CE binaries, where the period has not had time to evolve further, but they also show us the ejected envelope itself. As such, they are extremely useful in understanding the CE efficiency (De Marco et al. 2011), but also in the timing of the various CE phases and the energetics of the ejecta (Tocknell et al. 2014). For the latter purpose we need to know not only the details of the central binary, but also of the surrounding nebula (see for instance, Jones et al. 2014).

One of the goals of this series of papers is to further our understanding of the binary system parameters for known binary CSPNe. Connections between the binary parameters and the surrounding PN can then be explored, whether on a system-by-system basis, or through a statistical analysis of the larger sample. The former can be done as each model is produced. The latter depends on relatively few objects which currently have parameters derived from system modeling. We present here a study of the binary central star of Abell 65, with a discussion of the surrounding PN and links between the two.

2. BACKGROUND

Abell 65 (PN G017.3–21.9) was first discovered by Sharpless (1959) and independently cataloged as a PN by
Abell (1966). The 15th mag central star was identified by Abell, who presented UBV photometry. Curiously, Abell did not note variability of the star, based on 4 separate observations, even though he did report variability for several other nuclei which was confirmed later. The variations of the Abell 65 nucleus were first discovered by H.E.B. in 1989. It soon became clear that the star was a close binary with an orbital period very close to 1 day, as was reported by Bond & Livio (1990). The ~1 day period probably explains why the large-amplitude variability was not detected by Abell: the orbital phase will be nearly the same at the same sidereal time every night during a short observing run! A later paper by Walsh & Walton (1996) erroneously classified the CS as an eclipsing binary. Walsh & Walton (1996) also suggested that the CS was a cataclysmic variable (CV) star based on strong Balmer emission lines observed in the spectrum. Improved light curves (Shimansky et al. 2009; Louie & Hillwig 2010) along with phase-resolved stellar spectra (Shimansky et al. 2009) have since confirmed that the photometric variability is due to a strong irradiation effect, rather than eclipses, and that the irradiation effect is also the source of the strong emission lines observed in the optical spectrum. Those papers also confirmed a period very close to one day.

Physical values for the nebula such as distance, size, and age are given by a number of authors (e.g., Walsh & Walton 1996; Phillips 2005; Frew 2008; Frew et al. 2015). Huckvale et al. (2013) also provide a three-dimensional model of the nebula. They show a clearly bipolar nebula with both inner and outer structures (the outer shell was first identified by Longmore 1977). As noted by Miszalski et al. (2009b, based on an image from Hua et al. 1998), Huckvale et al. (2013) confirm that while the bright nebular structure may resemble a toroidal waist, it is actually a set of bipolar lobes with fainter outer lobes (see their Figure 5). The inclination of the symmetry axis of these structures in their model are 68° ± 10° and 55° ± 10° for the inner and outer lobes, respectively. They also calculate kinematic ages for the inner and outer shells respectively, dependent on the distance to the nebula, of (8000 ± 3000)(d/1 kpc) years and 15,000 ± 5000(d/1 kpc) years, where d is the distance of the PN. Distances to the nebula range from d = 1.17 kpc from Frew (2008) to d = 1.67 kpc from (Stanghellini et al. 2008). Hereafter we adopt the updated distance of Frew et al. (2015), d = 1.4 kpc with a reported uncertainty of 20%. The values of Huckvale et al. (2013) and this distance give ages of the nebular shells of 11,200 and 21,000 years.

To determine a reddening value we started with a weighted mean of the nebular Balmer decrement estimates from Acke et al. (1992), Kaler (1983), Perinotto et al. (1994), Walsh & Walton (1996), and Pollacco & Bell (1997) to determine $E(B-V) = 0.10$. An independent value can be calculated from a comparison of the integrated 1.4 GHz radio continuum and Hα fluxes from Condon et al. (1998) and Frew et al. (2013), respectively; we do so to determine $E(B-V) = 0.13 ± 0.06$. Also, the asymptotic reddening on this sight-line from the revised reddening maps of Schlafly & Finkbeiner (2011) is $E(B-V) = 0.09 ± 0.03$. However, a strong IR signature in the PN from dust found in WISE and IRAS data suggests a potentially strong nebular contribution to reddening. This is confirmed by IUE LWP and SWP spectra. The two spectra, taken at different times show clearly different fluxes, but neither match the slope of a hot CS unless a reddening value $E(B-V) ≥ 0.18$ is adopted. Using the reddening model of Valencic et al. (2004, 2014) we find the best match for $E(B-V) = 0.20$ and adopt this as the reddening value for our modeling.

In Figure 1 we show the reddening corrected IUE spectra, $V$, $R$, and $I$ fluxes from this work, and 2MASS (Skrutskie et al. 2006), WISE, and IRAS (Tajitsu & Tamura 1998) fluxes. Tajitsu & Tamura (1998) use corrected IRAS fluxes to determine a dust temperature of 65 K. Their correction assumes extended dust emission over the entire optical nebula, so they scale the emission up from the size of the aperture to the full size of the nebula. Here we simply use the reported values, two of which are upper limits, as shown in the figure.

Using the ephemeris in Section 4.1 we find that the SWP spectrum was obtained at phase 0.90, or close to minimum light (which occurs at orbital phase $\phi = 0$). The LWP spectrum, obtained at $\phi = 0.78$, has greater flux than the SWP spectrum, suggesting that part of the heated hemisphere of the companion is hot enough to affect the near-UV spectrum. We find that this requires a temperature of at least 20,000 K on some portion of the companion. Our final reddening value quoted above was found using the SWP spectrum along with our minimum light $V$ and $I$ values. The remaining data from 2MASS, WISE, and IRAS were not obtained at minimum light so we do not expect them to match the included model, but they are shown to demonstrate the IR-excesses due to the companion and dust in the nebula. In particular, the WISE and IRAS bands use large apertures and so include both thermal dust emission and fine-structure line emission, as well as light from the central binary. Indeed, in the WISE3 and WISE4 band images, the nebula
overwhelms the star in brightness. In the three IRAS bands, the magnitude difference between the observations and our stellar/dust model are 0.82, 0.99, and 1.09 mag in the J, H, and K bands respectively. The IRAS data were obtained at orbital phase 0.77 based on our ephemeris given below. For that orbital phase, these values are slightly higher than we would expect based on the irradiation effect alone. Likewise, the WISE1 and WISE2 band values are 1.37 and 1.55 mag above our minimum-light model, higher than expected from irradiation. However, these values are within a reasonable range when nebular contamination is also considered. We label these data points in Figure 1 as upper limits to remind the reader that due to nebular contamination and not being obtained at minimum light, they are upper limits for the model shown in the plot. The WISE bands are used, along with the IRAS fluxes, to estimate the dust component of the system.

Without higher resolution in the infrared it is difficult to determine the source of the dust emission. However, given that our best fitting reddening value is significantly higher than values from a number of other methods as described above, it seems likely that there may be an additional compact dust source around the CS that contributes to the reddening, such as the dust disks reported for a number of PNe (e.g., Biliková et al. 2012). In Figure 1 we show a two cool dust components: a 115 K blackbody to fit the WISE3 and WISE4 bands, and 40 K blackbody fit to the IRAS 60 and 100 μm bands. The cooler component roughly matches with the Tajitsu & Tamura (1998) dust emission from the nebula, while the warmer component is similar to dust disks seen in these systems, which average around 150 K. In both cases, it would appear that there is an additional reddening contribution by dust in the nebula.

In Section 4 we further discuss several of the literature values for the Abell 65 nebula in the context of our binary star modeling.

3. OBSERVATIONS AND REDUCTIONS

The photometric data consist of images obtained over twenty years at four different telescopes in the V, R, and I filters. The Cerro Tololo Inter-American Observatory (CTIO) 0.9 m and 1.3 m telescopes, the SARA 0.9 m telescope at Kitt Peak National Observatory, and the Perth Observatory 24 inch telescope were all used to collect data. The data include the original discovery observations described in Bond & Livio (1990) and follow-up observations by H. E. Bond on the CTIO 0.9 m telescope. These data were collected in 1989 September, 1990 June, 1991 September, and 1992 May (V, R, and I filters). The SARA 0.9 m telescope12 was used to make observations from the northern hemisphere at multiple epochs in 2007 and 2008 (R filter). The CTIO 0.9 m and Perth 24 inch telescopes were used to observe the CS of Abell 65 on three consecutive nights in 2008 August, providing coverage of almost 70% of the orbit each day (V, R, and I filters). The CTIO 1.3 m provided observations in queue observing mode from 2008 August to October and 2009 June and July (R filter). The Perth 24 inch telescope also provided observations in queue observing mode from 2008 June to August (I filter).

All images were bias subtracted and flat fielded (and dark subtracted, when necessary). The IRAF/DAOPHOT package was used to perform aperture photometry on the images. The 2007–2008 observations were then jointly analyzed using incomplete inhomogeneous ensemble photometry (Honeycutt 1992). The ensemble photometry used all of the stars in a template image to perform differential photometry. The large number of stars of various colors produces an effective color correction for slight differences in system throughput between the four different telescope, filter, and camera combinations. The success of this method was confirmed in the final light curve by the seamless overlap of the 2007–2008 data from the four telescopes in the phase-folded light curves (Figure 2). The 1989–1992 data were analyzed by single star differential photometry with two check stars. The earlier data were then shifted to the same magnitude zero-point as the more recent data (see Section 4.1 below). Some of these earlier data do not align well with the 2007–2008 data, especially in the V filter. These differences could be a result of different CCD and filter combinations, or could be intrinsic to the system (see Section 4.2 for more discussion). The two data sets were combined to provide a more precise orbital ephemeris.

The resulting light curves are in an instrumental magnitude system. However, the photometric data were then shifted to apparent magnitudes using the V = 15.80 and I = 15.39 mag from the Hubble Space Telescope (HST) observations of Ciardullo et al. (1999). The final ephemeris for the binary system was used to determine the phase of the HST images (0.81 and 0.79 for V and I, respectively) and our photometric data were shifted to those values at the determined phases based on our final binary model light curves. Given the high precision of our ephemeris, we adopt a magnitude zero-point uncertainty of 0.06 mag based on the small uncertainty in orbital phase and the slope of the light curve at that phase. To determine the shift necessary for our R filter data, we use a log fit between the V and I de-reddened fluxes to extrapolate an R magnitude value for Abell 65. The resulting zero-point is thus

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12 Based on observations obtained with the SARA Observatory 0.9 m telescope at Kitt Peak, which is owned and operated by the Southeastern Association for Research in Astronomy (saraobservatory.org).
slightly less well constrained, but should still be reliable to within 0.1 mag. The result gives apparent magnitudes at minimum light of $V = 16.04$, $R = 15.80$, and $I = 15.66$. These minimum brightness values provide the best observable measure of the combined brightness of the two stars in the system with a minimum irradiation contribution. They are used with the IUE SWP spectrum to arrive at a value for interstellar reddening, as shown in Figure 1.

The spectrum of the CS of Abell 65 was obtained on 2008 July 11 with the UVES high resolution spectrograph on the Very Large Telescope (VLT; Dekker et al. 2000). The exposure time was 1200 s with a spectral resolution of $R \sim 60,000$ and covering the range of 4800–6800 Å. The spectrum was obtained at an airmass of 2.285 with the slit at the parallactic angle of 105°. The seeing was 1.38 arcsec. The spectrum was reduced with the standard ESO UVES pipeline. Details of the spectrum are discussed in Section 4.3.

4. ANALYSIS

4.1. Orbital Ephemeris

Because we were unable to analyze the early epoch data using the same method as the more recent data (see Section 3 above) the two data sets had magnitude scales with different zero points. To correct this a preliminary model of the binary system was produced using only the recent data with the Wilson–Devinney code (Wilson & Devinney 1971; Wilson 1990) in the $V$, $R$, and $I$ filters. The resulting model was then fit to the early epoch data, allowing only the magnitude zero-point to change. The derived zero-point offset was applied to the early epoch data to shift them to the same zero point as the more recent data. Having all of the data on the same zero point scale allowed us to calculate the orbital ephemeris to our highest possible precision. To do so we used the Wilson–Devinney code to fit the photometric data with only the time at phase $\phi = 0$, $T_0$, and the orbital period, $P_{\text{orb}}$, as variables. The resulting binary system ephemeris is then

$$T = 2454301.3244(38) + 1.0037577(10) \times \phi$$

where $\phi = 0$ is taken to be at inferior conjunction of the cool secondary star (what would amount to primary eclipse if this were an eclipsing system). This phase also corresponds to minimum light. The values in parentheses reflect the uncertainties in the last two digits of each number. The complete phase-folded $V$-, $R$-, and $I$-band light curves are shown in Figure 2, where each has also been shifted to the apparent magnitude scale as described above.

4.2. Binary System Parameters

Shimansky et al. (2009) use their spectra and $V$-band light curve to calculate a model for the binary system confirming that it is indeed an irradiated binary with a hot central star and cool companion. However, we believe that with our light curves in the $V$, $R$, and $I$ bands along with some additional information described below, we are able to produce a more accurate model of the system. Because of the large number of parameters, binary system modeling often requires that a number of those parameters be estimated independently and used as fixed values in the modeling in order to reduce the degeneracy of the solution. Shimansky et al. (2009) use the size and expansion rate of the PN to arrive at a nebular age and then use the evolutionary tracks of Blöcker (1995) to derive a radius of the central star. The primary difference in our approach to modeling the system occurs at this point. With our determined apparent magnitudes at minimum light, the published distances to Abell 65, and interstellar absorption values we determine the absolute magnitudes for the combined light from the binary CS of Abell 65. We then constrain our models to match these values.

Using minimum light in the $V$ band ($V = 16.04$), the smallest distance value in the literature ($d = 1.71$ kpc, Frew 2008) and our adopted reddening (giving $A_V = 0.62$), we find $M_V = 5.09$ for the CS in Abell 65. Using the largest value of distance, $d = 1.67$ kpc (Stanghellini et al. 2008) we find an alternative minimum absolute magnitude for the CS of $M_V = 4.31$. And with our adopted distance from Frew et al. (2015) of $d = 1.4$ kpc, $M_V = 4.69$.

The binary parameters of Shimansky et al. (2009) result in an absolute magnitude, $M_V = 3.2$, well outside our range of $4.55 \leq M_V \leq 5.33$. It appears that the major cause of the discrepancy comes from their calculation of the age of the nebula (and thus the radius of the CS). They quote a radius for the extended halo of Abell 65 from Walsh & Walton (1996) of 2 pc. However, Walsh & Walton (1996) use a distance of 1.5 kpc to arrive at a diameter for the nebula of 2 pc rather than a radius. The Shimansky et al. (2009) resulting age then is a factor of two too large. Using an assumed expansion velocity and a larger distance than our adopted value of 1.4 kpc from Frew (2008) leads to additional discrepancies in age. The result is that their value for the age of the nebula of 130,000 years is considerably different than the result from Huckvale et al. (2013) of 21,000 and 11,200 years for the outer and inner nebular shells, respectively (for our adopted distance). Even with the difference in age it is not clear how Shimansky et al. (2009) arrive at their primary radius of 0.12 $R_\odot$. Extrapolating between masses of $0.546 M_\odot$ and 0.565 $M_\odot$ from the models of Schönberner (1983) used by Blöcker (1995) one could find a value of the mass for which the CS radius would be approximately 0.12 $R_\odot$, but the basis for their claim that it is the most likely radius is not made clear. However, their final model mass is 0.56 $M_\odot$ for which an age of 130,000 years places the CS much closer to the WD cooling track with a radius approximately a factor of five smaller. It is largely due to the sensitive relationship between CS mass, radius, and age that we have added the absolute magnitude as a constraint on our

### Table 1

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$q$</td>
<td>$0.40 \pm 0.10$</td>
</tr>
<tr>
<td>$T_{\text{CS}}$ ($\times 10^3$ K)</td>
<td>$1.10 \pm 0.10$</td>
</tr>
<tr>
<td>$T_2$ ($\times 10^3$ K)</td>
<td>$4.95 \pm 1.0$</td>
</tr>
<tr>
<td>$M_{\text{CS}}$ ($M_\odot$)</td>
<td>$0.56 \pm 0.04$</td>
</tr>
<tr>
<td>$M_2$ ($M_\odot$)</td>
<td>$0.22 \pm 0.04$</td>
</tr>
<tr>
<td>$R_{\text{CS}}$ ($R_\odot$)</td>
<td>$0.056 \pm 0.008$</td>
</tr>
<tr>
<td>$R_2$ ($R_\odot$)</td>
<td>$0.41 \pm 0.05$</td>
</tr>
<tr>
<td>$\log g_{\text{CS}}$ (cgs)</td>
<td>$6.7 \pm 0.2$</td>
</tr>
<tr>
<td>$\log g_2$ (cgs)</td>
<td>$4.6 \pm 0.2$</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>$61 \pm 5$</td>
</tr>
<tr>
<td>$a$ ($R_\odot$)</td>
<td>$3.90 \pm 0.10$</td>
</tr>
<tr>
<td>$\log(L_{\text{CS}}/L_\odot)$</td>
<td>$2.61$</td>
</tr>
<tr>
<td>$\log(L_2/L_\odot)$</td>
<td>$-1.05$</td>
</tr>
</tbody>
</table>
models. However, as discussed below we do use theoretical evolutionary tracks to help guide our modeling.

Using the Wilson–Devinney code with our photometric data and the radial velocities of Shimansky et al. (2009) we find a best-fit solution for the system parameters. In order to limit the possible parameter space we use the absolute magnitude constraint described above along with the temperature of the cool companion star found from Shimansky et al. (2009) from their spectra, \( T_c = 4950 \) K. The best-fit values from our modeling are given in Table 1 and over-plotted with the data in Figure 2. Because the uncertainties in fitting the data in binaries such as this are dominated by systematic effects, the uncertainties given for each parameter are not statistical errors for that individual parameter, but represent the range over which each parameter can vary in correlation with the other parameters. The resulting uncertainties are larger than those found by holding all other parameters constant while varying only one, but provide a more physically significant range for each value.

In order to properly fit the light curves we departed from using, for the secondary star, the internally calculated limb-darkening values in the Wilson–Devinney code. We found that lower values were necessary to reproduce the light curve shapes and amplitudes. The model shown in Figure 2 uses the internally calculated limb-darkening values for both the \( R \) and \( I \) bands, but the \( V \) band value has been reduced slightly. The change in limb darkening required to fit the observed light curves for any combination of parameter values in the ranges given in Table 1 is within 10% for all three bands.

We note several discrepancies in the photometry visible in Figure 2. Both the \( V \) and \( R \) data on the increasing brightness side fall slightly above the model, though the effect is most evident in \( V \). The asymmetry is real and while most of the data in that portion of the light curve are from a single night, there are a few data points from three different nights, suggesting that the discrepancy is not instrumental or due to atmospheric conditions. We find that we cannot match the discrepancy with our modeling. The source of the asymmetry could potentially be due to non-synchronous rotation of the secondary and some of the irradiated hemisphere rotating around toward the back hemisphere. The greater effect with decreasing wavelength, the effect is not noticeable in the \( I \) data, would suggest an increase due to higher temperatures, as would be expected from asynchronous rotation. The orientation is also in the correct sense for prograde rotation of the secondary at a rate greater than the orbital period. There is no corresponding dip in the light curve below our model on the decreasing brightness side of the light curve, as might be expected if synchronous rotation is moving the irradiated portion of the atmosphere. However, an asymmetry in that portion of the curve would only occur if the irradiation time scale is on the order of the rotation time scale. If the irradiation timescale is much shorter, then no such asymmetry would be expected. We cannot at this point determine whether non-synchronous rotation is the culprit, but it would seem to produce the observed features. Another possible explanation would be a bright spot on the cool companion, though a consistent bright spot at the same longitude on the star would seem unlikely.

We also find slight discrepancies in the peak of each light curve. In \( R \) and \( I \) the data were taken on different nights with the Perth telescope and the small brightness change appears to be inherent to the system. Finally, the \( V \) data on the decreasing brightness branch from the early CTIO data (obtained in the 1990s) lie clearly below the model while the early \( R \) data fall above the model. The \( I \) data from the 1990s line up with the more recent data. It is possible that a difference in filter response is responsible. Or there may be real changes in the amplitude over time.

The light curve amplitudes from our model are \( \Delta V = 0.882 \) mag, \( \Delta R = 0.912 \) mag, and \( \Delta I = 0.914 \) mag. The relative amplitude difference follows the relationship we presented in Paper I.

The resulting absolute magnitude of the system from our model values is \( M_V = 4.70 \) which agrees well with the value found above \( (M_V = 4.69) \) using the distance of Frew et al. (2015). As discovered by Shimansky et al. (2009), a hot and bright CS is required to fit the data, and we find that we are able to fit the data for relatively large ranges of temperature and radius of both the CS and companion. However, the degeneracy in the models is reduced dramatically by using an assumed system brightness.

In addition to our modeled absolute magnitude, several other system parameters differ from those of Shimansky et al. (2009). We find a companion with a lower mass, \( M_2 = 0.22 \pm 0.04M_\odot \) and radius, \( R_2 = 0.41 \pm 0.05R_\odot \) compared to their values of \( M_2 = 0.33 \pm 0.06M_\odot \) and \( R_2 = 0.59 \pm 0.08R_\odot \), respectively. As with many other cool secondary companions in close binary CSPNe, we find that the secondary in Abell 65 has a higher temperature and radius than expected for a main sequence star of similar mass. Thus the secondary is over-luminous by about a factor of 20–30. Our \( M_2 \) value suggests a companion spectral type M4V while the temperature would be equivalent to a K2V star and the radius is appropriate for an M2–3 V spectral type. So both the temperature and radius are large compared to those expected for a main sequence star based on our modeled mass.

The temperature of the CS of 110,000 K is larger than, but consistent with the Zanstra temperatures we calculate using the integrated H\(\alpha \) flux from Frew et al. (2013) and the reddened He ii/He i ratio averaged from the references given in Section 2. The results are \( T_{c, \text{He}} = 49 \pm 7 \) K and \( T_{c, \text{He}} = 93 \pm 12 \) K (the large discrepancy between the hydrogen and ionized helium Zanstra temperatures indicates the nebula is optically thin). It is also slightly higher than that of Shimansky et al. (2009), but the two agree to within the uncertainties. However, we find a CS radius more than a factor of 2 smaller than theirs. As a consistency check we use our resulting \( M_{CS}, R_{CS}, \log(T_{CS}), \) and \( \log(L_{CS}/L_\odot) \) with the evolutionary tracks of Schönberner (1983) and Blöcker (1995). The results are highly consistent with those tracks and lead to a CS age of about 22,000 years which, within the uncertainties in mass, radius, temperature, and distance, is in good agreement with the nebular age estimated by Huckvale et al. (2013) of 21,000 \( \pm \) 7000 years (for the outer nebular shell, scaled to our distance). The value of 11,200 \( \pm \) 4200 years from Huckvale et al. (2013) for the inner shell is younger than the age we find from the evolutionary tracks. This may be significant in that we would expect a CS that underwent CE evolution to evolve much faster than a non-CE star (cf. Passy et al. 2012; Ricker & Taam 2012). So if the CS in Abell 65 began its post-AGB evolution at a time consistent with ejection of the inner nebular shell, then we see a much shorter actual age than the predicted evolutionary age assuming a single star. Because the models of Huckvale et al. (2013) are based on spatio-kinematic model
we consider their ages to be the most reliable. Even for the largest published distance for Abell 65 the age of the inner shell is still younger than the evolutionary age of the CS. We do note however, that small deviations in the CS mass will produce a large change in the evolutionary age, making this comparison a consistency check for our results, rather than an absolute comparison.

Our inclination, $i = 61 \pm 5^\circ$, is lower than that of Shimansky et al. (2009) ($i = 68.0 \pm 2^\circ$), as a result of the different stellar parameters. Our value though is in better agreement with the nebular inclination for the inner shell from Huckvale et al. (2013), $i = 55 \pm 10^\circ$, and also agrees with their value for the inclination of the outer shell, $i = 68 \pm 10^\circ$. As Huckvale et al. (2013) state, the connection between close binary CSPNe and their host nebula is becoming clearer. For the handful of systems that have had both nebular and binary inclinations determined, the two values are within the uncertainties in every case: Abell 41 (Jones et al. 2010), Abell 63 (Mitchell et al. 2007), NGC 6337 (García-Díaz et al. 2009; Hillwig et al. 2010), HaTr 4 (Tyndall et al. 2012, also T.C. Hillwig 2015a, in preparation), NGC 6778 (Miszalski et al. 2011; Guerrero & Miranda 2012), Henize 2–428 (Santander-García et al. 2015), and Sp 1 (Jones et al. 2012, also T.C. Hillwig 2015b, in preparation).

4.3. The Spectrum of the Central Star of Abell 65

In Figure 3 we show a high resolution nebular subtracted spectrum of the CS of Abell 65 (see Section 3 for details) in the regions around H$\beta$ and H$\alpha$. The spectrum was obtained at orbital phase $\phi = 0.255$ based on our ephemeris. What immediately stands out are the very broad H$\alpha$ lines with central absorption. These lines are reminiscent of those seen in the CS of HFG 1 (Exter et al. 2005) with very broad double peaked H$\alpha$ lines. The line shape is reminiscent of the double-peaked H$\alpha$ profiles of accretion disks in CVs, thus the occasional classification of HFG 1 and Abell 65 as CVs. However, this broad double-peaked line profile is well described for irradiated atmospheres by Barman et al. (2004) with the central absorption due to non-LTE effects in the upper atmosphere of the irradiated companion star (see their Figure 7). The consistent change in equivalent width of these lines through the orbit (see Figure 4 in Shimansky et al. 2009) further confirms that the origin is not an accretion disk, for which the line strength would only change appreciably in the event of an eclipse. Furthermore, the minimum light spectrum from Shimansky et al. (2009) shows the hot star to be H-normal, giving an inferred spectral type of O($\gamma$). The strong irradiation effect is also evidence of the non-CV nature of Abell 65 since for a CV the system brightness would be dominated by the disk, thus swamping the irradiation effect and greatly reducing the observed variability amplitude.

We measured the radial velocity of the central absorption of the H$\alpha$ lines in the VLT spectrum and the narrow C$\text{ii}$ emission lines at 6578 and 6583 Å, both of which originate from the secondary star. The central absorption in H$\alpha$ could be effected by incomplete or over subtraction of the nebulosity, but we find radial velocity values consistent with the narrow C$\text{ii}$ lines, suggesting that any nebular subtraction effect is small. The resulting velocity point is plotted in Figure 4 with the data of Shimansky et al. (2009) and our best-fit model parameters. The VLT radial velocity point agrees well with both the previous data and our model.

5. CONCLUSION

Shimansky et al. (2009) have shown conclusively that the CS of Abell 65 is an irradiated close binary CSPN. Due to the
large parameter space available for binary system modeling, determining a final parameter set typically requires more information than radial velocity and light curves. With our three-color photometry we find that the parameters of Shimansky et al. (2009) do fit well. However, we believe that our use of luminosity as an initial fitting requirement results in a more accurate and more consistent parameter set than their initial requirement of CS radius based on nebular age and CS mass. Our results do not change the overall identification of the system as a hot central star and cool, irradiated companion. However, we believe that our final set of physical parameters more accurately reflects the make-up of the binary system. And we believe that what may seem relatively small differences in some of these parameters are important for future interpretations of the increasing body of close binary CSPNe.

Obtaining precise physical parameters for these systems can allow us to explore several interesting areas. First, we find that in cases where both the nebular inclination and binary inclination are known, the values show a very strong correlation. As the number of systems with known inclinations increases we will be able to say more about the likelihood that close binary interactions dominate the shaping mechanism in the resulting PN. Second, as we increase the statistical significance of the close binary CSPN sample we can begin to explore the birthrates of CVs and SN Ia progenitors of various types. Based on our results, the binary CS of Abell 65 will reach the semi-detached stage at a period of approximately 0.29 days and become a CV in approximately $9 \times 10^8$ years due to magnetic braking, based on calculations in Warner (1995). The time to a possible single or double degenerate SN Ia is longer than a Hubble time, as is expected for systems with periods of more than about half a day.

As is the case for the large majority of post-CE CSs, this binary CS in Abell 65 has a period smaller than three days. CE simulations (e.g., Passy et al. 2012; Ricker & Taam 2012) predict a broader range of post-CE binary separations than is observed. It is this type of comparison that has alerted us to the fact that our model of the CE phase is far from complete. The irradiation properties of the companions in post-CE binaries are also going to serve as constraints of the CE interaction. Here too, CSs of PNe are unique, because the bright and hot primaries result in the brightest irradiation effects. One parameter that may be constrained is the amount of accreted angular momentum on the companion. Irradiation theory should be able to tell us whether the companion is synchronized or not, and hence give us information on its rotation properties. These properties connect to both its magnetic field, which is currently held responsible for bright and hard X-ray emission (e.g., Montez et al. 2010; Kastner et al. 2012) and the amount of accretion that may take place before or during the CE (e.g., Miszalski et al. 2013a). Finally, as with most other secondary stars in close binary CSPNe, the secondary star here is both heated and expanded, thus over-luminous, compared to a main sequence star of similar mass. This characteristic of close binary CSPNe is likely a result of the CE phase, though it is not clear why the stars have not returned to thermal equilibrium. Increasing the statistical sample of over-luminous secondaries will hopefully lead to a better understanding of the CE and post-CE phase effects on the companion star.

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