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Flexible reconfiguration of existing urban water infrastructure systems

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Abstract

This paper presents a practical methodology for flexible reconfiguration of existing water distribution infrastructure, which is adaptive to the water utility constraints and facilitates in operational management for pressure and water loss control. The network topology is reconfigured into *star*-like topology, where the center node is a connected subset of transmission mains, that provides connection to water sources, and the nodes are the sub-systems that are connected to the sources through the center node. In the proposed approach, the system is first decomposed into the main and sub systems based on graph theory methods and then the network reconfiguration problem is approximated as a single-objective linear programming problem, which is efficiently solved using a standard solver. The performance and resiliency of the original

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and reconfigured systems is evaluated through direct and surrogate measures. The methodology is demonstrated using two large-scale water distribution systems showing the flexibility of our approach. The results highlight the benefits and disadvantages from network decentralization.

Introduction

Non-revenue water loss is the difference between the volume of water distributed through the system and the authorized/billed water consumption. Water losses include both real losses due to leaks in the pipes and apparent losses due to meter inaccuracy and unauthorized uses¹. Water losses in distribution systems constitute a major inefficiency in water supplies due to wastage of treated water and energy resources, increases in operating costs, and reductions in revenue.

District metered areas (DMAs) are a cost-effective technology that has proven highly successful for water loss control and leakage management^{2,3}. A DMA is a precisely defined sub-network, in which the inter-connecting pipes are monitored and the quantities of water entering and leaving the district are metered (enabling a better detectability of water losses through night flow diagnostics)⁴. In addition, pressure management is aided by installing pressure reducing valves (PRV) at the inlet of each DMA⁵⁻⁷. The control of pressures in each DMA leads to a reduction in leakage through pipe joints and connections. DMAs were first introduced in the UK water industry in the early 1980 and have been reported to achieve a 85% reduction in measured leakage^{3,8}. From water security perspective, some studies have suggested that in the event of a large scale contamination incident, the DMA structure would limit the spread of contamination and minimize the extent of response actions required for the system to restore to its normal pre-event conditions. The principal criteria of a DMA design are: (i) connectedness to the water source, (ii) size limits for each sub-network, (iii) minimum number of inter-connections, (iv) independence of the sub-networks, (v) minimum investment for the installation of isolation valves, and (vi) conserving system performance.

The design of DMAs results in a *star*-like topology of the water distribution network comprising independent sub-systems that directly or through transmission mains are connected to water sources.

A number of methods for reconfiguration of water systems into DMAs have been previously suggested. These vary from manual trial and error approaches⁹ to automated tools integrating network analysis¹⁰, graph theory^{11–13}, complex networks^{14,15}, and heuristic methods^{15,16}. The common workflow for DMA design is to identify water mains, partition the network into sub-networks, and isolate inter-connecting lines using simulation-based heuristics to minimize the number of connections and dependencies between the sub-networks. Table 1 in the Supporting Information (SI) presents a non-exhaustive list of recent research related to DMA design and their key features. The main drawbacks the prior methods for DMA design are that all of the studies link heuristic-based approaches with external simulation tool (e.g., EPANET¹⁷, WDNNetXL¹⁸), which are typically time consuming especially for large-scale water systems, and none of the works consider the location of existing valves assuming that any pipe in the system can be uniquely isolated, which is impractical for real application.

Our work contributes to previous works by: (i) allowing only existing valves to be closed, thus avoiding capital costs for installation of additional valves, (ii) approximating the network flow and link isolation as linear programming (LP) problem, which can be efficiently solved for large-scale systems using standard solvers (e.g. MOSEK¹⁹, Gurobi²⁰), and (iii) performing a rigorous analysis of network performance and resiliency using a suite of direct and surrogate measures. The methodology is applied and demonstrated using two large-scale water networks that, although supply similar daily demand, exhibit different topological properties.

Methods

In our approach for automated network reconfiguration into sub-networks, the control variables are the existing valves that can be closed, the input parameters are the diameter and flow thresholds for identifying the mains, the lower and upper bounds for identifying the sub-networks, and the minimum desired operating pressure at network nodes. The outcome of our approach is precisely defined sub-network structure achieved by closing a selected subset of valves, such that each sub-network has a minimum number of inter-connections, desired demand range, and its nodal pressures are above a desired minimum. Our approach consists of two main steps: (i) topology decomposition – the system is initially decomposed into the main and sub networks and (ii) optimization problem – the network flow and reconfiguration problem is approximated as a single-objective linear programming (LP) optimization problem. The feasibility of the resulting solution is validated by solving the full nonlinear flow model using EPANET¹⁷ hydraulic solver, and the performance of the original and the reconfigured network is evaluated and compared using direct and indirect measures.

Network topology decomposition

The topology of water distribution systems is composed of mixed branched and looped configurations. Transmission mains convey large flows from the water sources to distribution mains of the interior system and typically comprise larger diameter pipes. The distribution mains further distribute water to end consumers and typically comprise smaller diameter pipes²¹. Network decomposition consists of two main phases: (i) identifying transmission mains and (ii) defining sub-networks, as described next.

Transmission mains

The primary step towards DMA configuration is to identify the connected subset of transmission mains (pipes, valves, pumps) that connect the water sources (reservoirs, tanks, wells)

to the interior of the network. For real systems, classification of transmission mains based solely on pipes' diameters¹⁰ may be inadequate as these pipes may not be fully connected and smaller pipes may carry large volumes of flow as well. We identify transmission mains as the connected subset of links with diameters, D , and flows, q , higher than the specified thresholds, D_c and q_c , respectively. Given a network graph G , a set of nodes N consisting of source N_s and demand N_d nodes, and a set of links E consisting of pipes E_p and valves E_v :

1. Find the subset of links, $E_D \subset E$, with diameters above a given threshold: $E_D = \{(u, v) \in E \mid D(u, v) \geq D_c\}$.
2. Find the subset of links, $E_F \subset E$, with flows higher than a given threshold: $E_F = \{(u, v) \in E \mid q(e) \geq q_c\}$, where q can be computed by solving the full set on nonlinear flow equations²² or using hydraulic simulator¹⁷:
3. Combine both sets, $E_C = \{E_D \cup E_F\}$, and find the largest connected component, G_{main} , in the subgraph $G(N_C, E_C)$ where $N_C = \{u \mid (u, v) \in E_C\}$, that is accessible from the sources. A connected component is a subgraph that contains a path between every pair of distinct nodes and can be found using the breadth first search (BFS) algorithm²³ and setting each source node as the root node. Consequently, the subgraph G_{main} is composed of the transmission mains and is connected to the sources.
4. Extend the connected subgraph of transmission mains such that it has only valves in its edge-cut. We define an *edge-cut* as the set of all links that have one node that belongs to a given subset of nodes N_i and the other belongs to $N \setminus N_i$. Let $N_{main} = \{u \in N(G_{main})\}$ be the set of all nodes in the main subgraph, $E_{main} = \{(u, v) \in E(G_{main}) \mid u, v \in N_{main}\}$ be the set of all links in the main subgraph, and $E_{cut-main} = \{(u, v) \in E \setminus E_{main} \mid u \in N_{main}, v \in N \setminus N_{main}\}$ be the main edge-cut. Then the extended subgraph $\tilde{G}_{main}$ has only valves on its boundary connections and its edge-cut contains only valves, with $\tilde{E}_{cut-main} = \{(u, v) \in E_v \mid u \in \tilde{N}_{main}, v \in N \setminus \tilde{N}_{main}\}$, $\tilde{N}_{main} = \{u \in N(\tilde{G}_{main})\}$, $\tilde{E}_{main} = \{(u, v) \in E(\tilde{G}_{main}) \mid u, v \in \tilde{N}_{main}\}$. This is

achieved by traversing network links in a BFS manner starting from each boundary node of the initial transmission main, G_{main} , and exploring all adjacent links until the closest existing valves are reached.

The outcome of the first step is the subgraph $\tilde{G}_{main}$ which is the center node of the *star*-topology and will connect all sub-networks to the water sources.

Graph decomposition

The next step is to decompose the rest of the network, $G[N \setminus \tilde{N}_{main}]$, into sub-graphs such that each sub-graph is within a specified size range, has a connection to the source, has a minimum number of inter-connecting links, i.e. small edge-cut size, and all inter-connecting links are existing valves to avoid any additional retrofit costs. We treat inter-connecting valves as a hard constraint and the rest of the constraints as soft constraints, i.e. can be violated. We combine graph search and partitioning algorithms to decompose the water network, taking the following steps:

1. Identify all subgraphs G_i connected to the main subgraph using BFS starting from each boundary node of $\tilde{G}_{main}$. Set counter $m = 2$.
2. Compute the demand, $d(N_i)$, of each subgraph identified previously, where $N_i = N(G_i)$ is the set of nodes belonging to the subgraph, G_i . Given the minimum and maximum desired total demands, $\underline{d}$ and $\bar{d}$, respectively, check if:

- $d(N_i) < \underline{d} \Rightarrow$ merge small sub-networks with the main $\tilde{G}_{main} = \{\tilde{G}_{main} \cup G_i\}$
- $\underline{d} < d(N_i) < \bar{d} \Rightarrow$ create new sub-network $G_m = G_i, m = m + 1$
- $d(N_i) > \bar{d} \Rightarrow$ further partition G_i into k subgraphs, using a graph partitioning algorithm (METIS^{24,25}) with $k = \lfloor d(N_i)/\bar{d} \rfloor$. The graph partitioning algorithm is adopted from distributed computing for allocating tasks to multiple processors and it divides the given graph with $|N|$ nodes into k clusters, such that the number of inter-connections between different clusters is minimized and the clusters

are roughly the same size. This graph partitioning approach has been previously successfully applied to water distribution systems²⁶. Finally, as previously, each subgraph is refined to have only valves in its edge-cut.

The outcome of this step is a *star*-configuration of the water network based solely on topological properties, where $\tilde{G}_{main}$ and G_m , $m = 1, \dots, K$, are main and the sub-networks of the full water system and all inter-connections between the sub-networks are valves, $E_{cut-m} = \{(u, v) \in E_v \mid u \in N(G_m), v \in N \setminus N(G_m)\}$. Let $E_{cut-M} \subset E_v$ be the union of all valves in the edge-cut of each sub-network. Note, although in this application we focused on sub-network *size* in terms of demand, any function can be applied such as number of nodes or number of connections.

Optimization problem formulation

Next, we approximate the network reconfiguration as a linear programming (LP) problem, where the decision variables are the boundary valves in the edge-cut, the system is subject to hydraulic and operational constraints, and the objective function minimizes the number of open boundary valves.

Network flow

For each node $i \in N$ in the network, the conservation of water is written as:

$$\sum_{k \in E_{i,in}} q_k - \sum_{k \in E_{i,out}} q_k = d_i \quad \forall i \in N \quad (1)$$

where q_k is the flow in link k , $E_{i,in}$ and $E_{i,out}$ are the links coming in and out of the node i , and d_i is the nodal demand.

Then for each link $k \in E$ the conservation of hydraulic energy is written as:

$$h_k + H_j - H_i = 0 \quad \forall k \in E \quad (2)$$

where H_i, H_j are the hydraulic head at the start and end nodes $i, j \in N$, respectively, and h_k is the head loss or gain of the hydraulic element. For network pipes, the headloss is a monotonically increasing power function of the flow rate that can be estimated using the Hazen-Williams model²⁷ as:

$$h_k = R_k q_k^\alpha \quad \forall k \in E_p \quad (3)$$

where R_k is the pipe's roughness coefficient, $\alpha = 1.852$, and E_p is the set of pipes. The headloss for valves follows the same power function (Eq. 3) with different parameters R and α depending its characteristics.

The given network flow problem results in a set on nonlinear equations an embedding them into an optimization problem will result in a nonlinear nonconvex optimization problem. Several modeling and solution approaches have been suggested in past years exhibiting a clear trade-off between modeling complexity and efficiency of the solution approach. The main approaches rely either on some approximation of the flow model, such as linear relaxations^{28,29}, which can then be efficiently solved using modern solvers, or solving the nonlinear models using heuristics or evolutionary algorithms^{16,30} but without solution guarantees. Additionally, the evolutionary algorithms tend to suffer from computational burden as the size of the optimization problem increases. To achieve a practical and efficient solution method we suggest a linear approximation of the nonlinear head loss function around an operating point taking the form:

$$\tilde{h}_k = a_{1k} q_k + a_{0k} \quad \forall k \in E \quad (4)$$

where a_{1k}, a_{0k} are a function of selected operating point q_k^{op}, h_k^{op} and R_k pipe's characteristics, as shown in Figure 1 of the SI. Within the operating range, the linear model of a single pipe slightly overestimates the headloss. Outside the operating range with the flow in the same direction, the linear model underestimates the headloss, and significantly overestimates if the direction of flow changes. We later show, that we validate the feasibility of our final solution by solving the full set of nonlinear equations.

182 Substituting Eq. (4) into Eq. (2), the approximated model of the hydraulic energy over
 183 network links takes the following form for all pipes and valves except the valves that are in
 184 the final edge-cut:

$$a_{1k}q_k + a_{0k} + H_j - H_i = 0 \quad \forall k \in E \setminus E_{cut-M} \quad (5)$$

For each boundary valve in the edge-cut $k \in E_{cut-M}$, that can be closed, we modify Eq. (5) to model zero flow. If the flow in the valves is zero, $q_j = 0$, then according to Eq. (5), the head difference between the two previously adjacent nodes (before isolation) is strictly equal to a_{0k} , which is obviously false. To model zero flow in isolated valves, for each valve, we introduce two additional variables y_k, u_k and two additional constraints (6b-c) representing valve's state (open or closed) and the head difference between disconnected nodes in case of a closed valve. The set of new constraints is formulated as:

$$a_{1k}q_k + a_{0k} + H_j - H_i + u_k = 0 \quad \forall k \in E_{cut-M} \quad (6a)$$

$$(1 - y_k)\underline{q_k} \leq q_k \leq \overline{q_k}(1 - y_k) \quad \forall k \in E_{cut-M} \quad (6b)$$

$$-My_k \leq u_k \leq My_k \quad \forall k \in E_{cut-M} \quad (6c)$$

$$y_k \in \{0, 1\}, u_k \in \mathbb{R}$$

185 where u_k is a continuous variable representing head difference between disconnected nodes,
 186 y_k is a binary variable representing the state of the valve (1 – closed, 0 – open), M is a large
 187 number, and E_{cut-M} is the set of boundary valves.

188 The set of equations in (6) is reduced to two cases: (i) $y_k = 1 \Rightarrow q_k = 0, u_k \in \mathbb{R}$ – the
 189 valve is closed, the flow rate is zero, $q_k = 0$, and the head difference between the two adjacent
 190 nodes is a real-valued number and (ii) $y_k = 0 \Rightarrow q_k \in \mathbb{R}, u_k = 0$ – the valve is open, the
 191 dummy variable u_k is zero and Eq. (6a) preserves its original form as in Eq. (5).

Linear programming formulation

Given a *star*-topology with inter-connecting valves, the problem is to find the largest subset of valves that can be closed such pressures are maintained above a desired minimum value.

Combining Eqs. (1)-(6), the following LP problem is formulated:

$$\begin{aligned}
& \underset{\mathbf{q}, \mathbf{H}, \mathbf{y}, \mathbf{u}}{\text{minimize}} && N_v - \sum_{k \in E_{cut-M}} y_k \\
& \text{subject to} && (1), (5), (6) \\
& && \underline{H}_i \leq H_i \leq \overline{H}_i \quad \forall j \in N \\
& && 0 \leq \mathbf{y} \leq 1
\end{aligned} \tag{7}$$

where $N_v = |E_{cut-M}|$ is the number of boundary valves and $\underline{H}_i, \overline{H}_i$ are the lower and the upper pressure constraints, respectively. Note, that we relax the integer constraint and allow y to vary between 1 and 0, this is to capture the inaccuracies resulting from the linearization of the headloss function.

In the final solution, the valves corresponding $y = 1$ are closed and the rest are left open and the feasibility of the solution is validated by solving the full set of nonlinear flow equations, e.g. using EPANET¹⁷.

Performance evaluation

Several measures have been previously suggested for analyzing the performance of water networks. These can be classified into direct measures of hydraulic reliability, e.g. minimum pressure and water age, surrogate physical metrics computed as a function of the energy dissipated in a system³¹, and complex networks indexes that analyze the structural robustness of water distribution networks³². Next, we briefly review the measures we use for analyzing network performance.

Direct measures

1. *Worst cut-size (WCS)* – is the largest edge-cut of an individual sub-network, $|E_{cut-m}|$, $m = 1, \dots, K$. This measure indicates the maximum number of meters and control valves that are needed to control an individual sub-network and the extent of response actions in the event that the sub-network needs to be isolated.
2. *Total cut-size (TCS)* – is the size of the edge-cut of the network $|E_{cut-M}|$, i.e. the total number of boundary valves. This number indicates the overall investment required for network retrofit (flow meters and pressure control valves) and needs to be minimized.
3. *Pressure* – the performance of the system can be naturally evaluated based on the pressure distribution before and after reconfiguration.
4. *Water age (WA)* – water age is an indicator for water quality and is also used to evaluate network performance.

Physical surrogate measures

1. *Resilience index*³³ – I_R is a measure of excess system power based on the power loss in a system and can be computed as:

$$I_R = 1 - \frac{P_{loss}}{P_{loss}^{max}} = 1 - \frac{\sum_{i \in N_s} H_i d_i - \sum_{i \in N_d} H_i d_i}{\sum_{i \in N_s} H_i d_i} \quad (8)$$

where P_{loss} is the actual power loss in the network and P_{loss}^{max} is the maximum feasible power loss in the network. Higher values of the resilience index I_R indicate a more efficient distribution of flows in term of power dissipation.

2. *Network resilience index*³⁴ – I_N is a modified resilience index taking into account changes in pipe diameters:

$$I_N = 1 - \frac{P_{loss}^{adj}}{P_{loss}^{max}} = 1 - \frac{\sum_{i \in N_s} H_i d_i - \sum_{i \in N_d} U_i H_i d_i}{\sum_{i \in N_s} H_i d_i} \quad (9)$$

where

$$U_i = \frac{\sum_{k \sim (i,j)} D_k}{|k| \cdot \max\{D_1, \dots, D_k\}} \quad (10)$$

where P_{loss}^{adj} is the modified actual power loss in the network adjusted to pipe diameters, D is pipe diameter, $|k|$ is the number of pipes connected at node i , and $U_i \leq 1$ is a scale factor penalizing changes in diameters. Higher values of the network resilience index I_N indicate a more efficient distribution of flows in terms of power dissipation and network design.

Complex network measures

1. *Meshedness coefficient*³⁵ – R_m is defined as the fraction of the actual number of loops to the maximum possible number of loops in a planar graph: $R_m = (m - n + 1)/(2n - 5)$, where m is the number of links and n is the number of nodes in the graph. This is a surrogate metric of path redundancy in a network.
2. *Spectral gap*³⁶ – $\Delta\lambda$ is the difference between first and second eigenvalues of graphs adjacency matrix A . A small spectral gap could indicate the presence of articulation points whose removal may split the network into isolated parts.
3. *Algebraic connectivity*³⁷ – λ_2 is the second smallest eigenvalue of normalized Laplacian matrix of the network. A larger value of algebraic connectivity denotes the network robustness and tolerance against efforts to decouple the network.

Network reconfiguration schemes and suggested performance analysis are demonstrated in Figure 2 in the SI using an illustrative example adopted from Alperovits and Shamir³⁸.

Applications and results

The suggested approach was applied to two large-scale water networks – EXNet³⁹ and BWS-NII⁴⁰. We randomly added valves to both networks to test our approach, as the original

Figure 1: EXNet topology

Table 1: Data for water systems

System	#Pipes	#Valves	#Nodes	Demand [$10^6 gal/day$]	#sub networks	Full* cut-size	Reduced** cut-size
EXNet	1,546	872	1891	37	42	130	47
BWSNII	11,024	3,295	12,523	28.2	36	206	49

* full network before closing valves; ** reduced network after closing valves;

networks do not contain any valves, additionally, for the EXNet, we reduced the nodal demand by half since this network was developed for rehabilitation design to supply future demands. The complete EPANET¹⁷ files are available in the SI. The system data and design parameters used in this work are:

Network model. The required inputs include network topology, properties of network nodes and links (i.e., length, diameters, roughness of pipes, nodal elevations and daily demands). This information can also be read directly from the EPANET¹⁷ .inp network files. Summary of networks' data is given in Table 1 (first five columns). The EXNet is a smaller network in terms of number of pipes and nodes, but it supplies slightly higher daily demand than BWSNII, which almost seven times larger in size.

Design parameters. For both networks, the demonstrated results are for the parameters: (i) threshold diameter $D_c = 16[inch]$ and threshold flow q_c is the top 1% of network flows, (ii) minimum and maximum sub-network size $\underline{d} = 10^5[\frac{gal}{day}]$ and $\bar{d} = 10^7[\frac{gal}{day}]$, and (iii) minimum

265 nodal pressure $\underline{P}_i = 10[psi]$, where the pressure head, H_i , is equal to the pressure plus the
 266 elevation of node i .

Figure 2: BWSNII mains and sub-networks topology

267 *Network decomposition.* Figure 1 shows the topology of the EXNet network and its
 268 sources. Figure 1a shows (bold blue) the identified transmission mains in the first step of the
 269 algorithm. Next, based on the graph decomposition steps described previously, the network
 270 was partitioned into 42 sub-networks with 130 boundary valves connecting the different sub-
 271 networks, as shown in Figure 1b and listed in Table 1 in columns six and seven. Table 2
 272 in the SI gives a detailed list of the demand, mean pressure, water age, and the size cut of
 273 each sub-network. All sub-networks are within the desired demand range and all, excluding
 274 32, 34, 38, and 40, which are located farther from the mains (shown in dashed line), have a
 275 direct connection to the transmission mains.

276 The BWSNII was partitioned into 36 sub-networks with 206 boundary valves. The layout
 277 of the BWSNII network, its transmission mains, and sub-networks are shown in Figure 2.
 278 As previously, all sub-networks are within the desired demand range and all have a direct

connection to the transmission mains. Table 4 in the SI shows the demand, mean pressure, water age, and the size cut for each sub-network.

Optimization problem. We formulate the optimization problem based on (7). The EXNet has a single loading condition, hence for each pipe, we use two-point linear approximation with $[Q_1 \ Q_2] = [0.5q \ 1.5q]$, where q is the flow in each pipe. An example for the two-point linearization is given in Figure 1 of the SI. The LP model results in 4,569 decision variables and 4,829 constraints. The Gurobi solver²⁰ is used to solve the optimization problem with a solution time around 0.6[sec] (Intel Core i7 2.9 GHz 16 GB of RAM). The solution is the list of valves that can be isolated, i.e. with corresponding dummy variables equal to one, $y_k = 1$. We refer to the *full model* as the network before closing valves and to the *reduced model* – after closing valves. For EXNet, 83 valves were identified for a potential isolation for network reconfiguration, with only 47 valves remaining open (Table 1, last column). As mentioned before, to validate the solution of the LP problem we solve the full set of nonlinear flow equations using EPANET¹⁷. All results demonstrated below are computed based on the hydraulic simulations using EPANET. The *.inp* file of the reconfigured network can be found in the SI. A full list of the number of connections (cut-size) for each of the sub-networks before and after optimization is given in Table 2 of the SI and the detailed list of boundary valves at the solution is given in Table 3 of the SI.

For BWSNII we take the minimum and the maximum flows during the extended period simulation for the linear approximation of the headloss function and formulate the optimization problem for the peak demand condition. The LP model results in 16,521 decision variables and 16,538 constraints, with the solution time of approximately of 5.5[sec]. For BWSNII, 157 valves were closed, with only 49 remaining open (Table 1, last column). The solution was again validated using EPANET¹⁷ simulations and the new *.inp* file can be found in the SI. The detailed lists are given in Tables 4 and 5 of the SI.

Performance evaluation. Next, we analyze the performance of the full and reduced models based on the different measures. Figure 3a shows the cut-size and Figure 3b the average

Figure 3: EXNet sub-networks' performance: full model (black squares) and reduced model (blue fill rectangles)

pressures of each of the sub-networks for the full (black squares) and reduced (blue circles) models of EXNet based on the full hydraulic simulation. It can be observed that the cut size is significantly reduced after the optimization followed by a reduction in the average pressures in the system, although still above the minimum required. The average water age for each sub-network is reported in Table 2 in the SI, however, no apparent changes were observed between the full and reduced models for this network. Figure 3 in the SI demonstrates the pressure distribution in the network before (black-white) and after (blue) reconfiguration. As expected, the distribution of pressures is shifted to lower values after closing additional valves, since the energy losses in the system increase.

Figure 4 demonstrates similar analysis for BWSNII, although the number of boundary valves is greatly reduced after optimization (Figure 4a), there is only slight reduction in the average pressures for each sub-network (Figure 4b) and no apparent change in the water age. Figure 4 in the SI demonstrates the shift in the pressure distribution to lower values, similar to previous application.

Finally, Table 2 lists the different performance metrics explained previously. For both EDNet and BWSNII, we can observe the great reduction in the number of boundary connections, in terms of the total and the worst cut-size. This indicates the number of flow meters and pressure control valves that should be installed in the inlet of each sub-network for

water loss and pressure control on the network. A slight reduction is observed in both physical and complex network performance measures comparing the reduced and the full models. For BWSNII, the reduction in all measures is less significant than for the EXNet network, particularly the topological indicators, indicating that for large physical networks these measures are less informative.

Figure 4: BWSNII sub-networks' performance: full model (black squares) and reduced model (blue fill rectangles)

Table 2: Performance evaluation measures

Metric	EXNet		BWSNII	
	Full	Reduced	Full	Reduced
WCS	16	4	23	4
TCS	130	47	206	49
I_R	0.72	0.64	0.98	0.96
I_N	0.66	0.59	0.92	0.90
λ_2	0.0004	0.0002	-1.00	-1.00
$\Delta\lambda$	0.2612	0.2560	0.0062	0.0062
R_m	0.1391	0.1172	0.0715	0.0652

In this paper, we introduce a practical and efficient approach for flexible water network reconfiguration facilitating water loss control and pressure management. In our approach, the network reconfiguration problem combines graph theory algorithms and is formulated as a LP problem, which is efficiently solved for large-scale networks. We examine the resiliency and robustness of different reconfiguration schemes based on common resiliency measures. Our results demonstrate the benefits and disadvantages from network decentralization. The

presented approach provides a decision support tool for water utilities facilitating in infrastructure management.

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Supporting Information Available

Auxiliary data providing the full networks data, related work, linear approximation, illustrative example for performance metrics, and results are provided in the SI.

This material is available free of charge via the Internet at <http://pubs.acs.org/>.

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441 **Graphical TOC Entry**

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Flexible reconfiguration of existing urban water infrastructure systems

Supporting Information

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Table 1: Summary of methodologies for DMA design

Paper	Design criteria	Solution method	Performance evaluation
Murray et al. (2010)	Connectedness to source Adding/closing pipes Size constraints	Manual DDA, EPANET	Water security Water age Resilience index Fire flow
Ferrari et al. (2013)	Connectedness to source Closing pipes Size constraints	BFS DDA, EPANET Heuristics	Minimum pressure
Diao et al. (2013)	Closing pipes Size constraints	Modularity DDA Heuristics	Minimum pressure Water age Fire flow
DiNardo et al. (2013)	Connectedness to source Closing pipes	DFS PDA, WDNEXL GA	Resilience index Pressure index Flow index
DiNardo et al. (2013)	Closing pipes Number of zones	Graph partitioning GA DDA & PDA	Resilience index Pressure index Flow index
Alvisi and Franchini (2014)	Closing pipes Size constraints	BFS DDA Enumeration	Minimum pressure Resilience index
This paper	Connectedness to source Closing valves Size constraints Minimum connections	Graph partitioning LP	Hydraulic measures Robustness metrics Resilience indexes

BFS - Breadth first search; DFS - Depth first search; DDA - Demand driven analysis; PDA - Pressure driven analysis;
GA - Genetic algorithms; LP - linear programming;

Physical surrogate measures

Power loss in flow networks is defined by the summation over all links of the headloss h_j multiplied by the flow q_j . It can be shown that an equivalent formulation is the summation over all nodes of the head H_i multiplied by the nodal demand b_i , and formulated as:

$$\sum_{j \in E} h_j q_j = h^T q = (AH)^T q = H^T A^T q = H^T d = \sum_{i \in N} H_i d_i \quad (1)$$

where A is network connectivity matrix.

The right hand side of (1) can be further decomposed into P_{in} , the power input by the network sources N_s , and P_{out} , the power output to network consumers N_d .

$$\sum_{j \in E} h_j q_j = \sum_{i \in N_s} H_i d_i - \sum_{i \in N_d} H_i d_i \quad (2)$$

$\Downarrow$

$$P_{loss} = P_{in} - P_{out} \quad (3)$$

Figure 1: Linear approximation of the flow-headloss function. Figures a and b demonstrate linear approximation of the nonlinear flow-headloss function for pipes 2055 and 2056 of the EXNet network given an operating domain $[Q_1, Q_2]$. The operating domain is determined based on flows during normal operation. The linear model is computed as: $\tilde{h}(q) = \frac{h(Q_2) - h(Q_1)}{Q_2 - Q_1}q + \frac{h(Q_1)Q_2 - h(Q_2)Q_1}{Q_2 - Q_1} = a_1q + a_0$.

	a	b	c
<i>WCS</i>	3	2	1
<i>TCS</i>	5	4	3
<i>P_{min}</i>	29.01	29.00	26.92
<i>I_R</i>	0.927	0.927	0.914
<i>I_N</i>	0.708	0.847	0.835
<i>R_m</i>	0.222	0.111	0.000
$\Delta\lambda$	1.221	1.090	0.844
λ_2	0.365	0.265	0.232

WCS - worst cut size; TCS - Total cut size; P_{min} - minimum pressure; I_R - resiliency index;
 I_N - network resiliency index; R_m - meshedness coefficient; $\Delta\lambda$ - spectral gap; λ_2 - algebraic connectivity;

Figure 2: Illustrative example – Network reconfiguration into a *star*-like topology and multi-criteria performance metrics. Transmission mains are highlighted in subfigures a1-c1. The corresponding *star*-structure is shown in subfigures a2-c2, each time removing a boundary connection, i.e. closing the boundary valves. The table lists the measures for the three reconfigurations.

Figure 3: Pressure distribution in EXNet: full model (black-white) and reduced model after optimization (blue)

Table 2: EXNet - sub-networks' data

Sub-network	Demand [10 ⁵ gal/day]	Full model		Reduced model		$\overline{WA}$ [hr]
		Cut-size	$\overline{P}$ [psi]	Cut-size	$\overline{P}$ [psi]	
<i>main</i>	114.53	103	63.03	42	61.08	10.41
2	14.34	5	52.85	1	12.88	3.85
3	11.33	4	61.57	4	60.79	11.47
4	6.82	3	54.00	1	47.16	9.05
5	5.76	3	71.48	1	70.20	10.72
6	5.74	2	58.64	1	58.74	8.82
7	4.98	1	43.71	1	43.84	6.99
8	4.59	2	59.02	2	59.18	9.27
9	4.23	2	83.28	1	78.85	14.80
10	3.95	4	64.29	1	60.31	14.18
11	3.87	2	49.78	1	41.36	11.06
12	3.64	1	68.97	1	64.47	13.38
13	3.58	1	52.08	1	52.25	10.63
14	3.45	3	64.29	1	63.39	9.65
15	3.42	4	69.38	1	68.11	13.33
16	3.39	1	52.75	1	52.91	9.31
17	3.28	3	55.01	1	51.59	9.08
18	2.91	3	60.91	1	60.29	7.97
19	2.85	1	44.22	1	44.38	6.91
20	2.84	1	42.45	1	42.60	8.85
21	2.80	1	67.95	1	68.13	10.46
22	2.77	1	62.76	1	62.45	13.22
23	2.70	4	72.88	1	69.42	11.79
24	2.66	4	46.31	1	40.28	5.40
25	2.59	1	65.12	1	65.49	10.43
26	2.52	2	43.58	1	43.40	7.05
27	2.08	4	67.99	1	69.34	12.67
28	1.60	1	49.72	1	49.83	4.08
29	21.71	14	75.53	1	52.67	13.39
30	11.06	16	66.74	2	52.60	11.80
31	14.96	9	78.33	1	52.14	13.48
32	1.40	3	71.35	1	50.75	10.92
33	6.68	4	66.16	2	62.34	13.81
34	10.85	7	69.54	2	50.71	12.40
35	4.64	2	73.55	1	74.00	12.62
36	4.58	2	73.25	1	72.26	11.88
37	7.03	6	69.09	2	62.82	13.03
38	2.06	1	76.27	1	33.81	16.26
39	17.35	7	79.37	2	59.72	14.90
40	10.55	3	75.72	2	33.24	17.34
41	13.54	5	76.35	1	20.16	13.35
42	11.13	9	75.00	1	63.89	13.16
43	3.65	5	76.40	1	19.14	14.02

$\overline{P}$ - average pressure; $\overline{WA}$ - average water age;

Table 3: EXNet - boundary valves at final solution

Valve ID	Start sub-network	End sub-network
5164	1	2
2187	1	3
2269	1	3
2283	1	3
2599	1	3
4913	1	4
3532	1	5
3783	1	6
5132	1	7
3593	1	8
2271	1	8
2605	1	9
2760	1	10
4878	1	11
2197	1	12
2424	1	13
2313	1	14
3634	1	15
2122	1	16
3859	1	17
5076	1	18
5153	1	19
3500	1	20
2397	1	21
2298	1	22
4015	1	23
4156	1	24
5220	1	25
3213	1	26
2364	1	27
2939	1	28
4875	1	30
2806	1	31
3021	1	33
2217	1	33
5004	30	34
3129	32	34
3853	1	35
2256	1	36
2600	1	37
2679	29	37
2407	1	39
4194	38	40
5305	39	40
5089	1	41
2945	1	42
2182	1	43

Figure 4: Pressure distribution in BWSNII: full model (black-white) and feduced model after optimization (blue)

Table 4: BWSNII - sub-networks' data

Sub-network	Demand [$10^5 gal/day$]	Full model		Reduced model		$\overline{WA}$ [hr]
		Cut-size	$\overline{P}[psi]$	Cut-size	$\overline{P}[psi]$	
<i>main</i>	110.30	202	82.12	49	81.82	15.00
2	14.47	23	79.91	4	78.46	9.41
3	9.18	5	100.70	1	99.17	21.17
4	8.29	14	80.83	2	79.37	13.31
5	7.64	21	74.46	2	70.82	12.78
6	4.82	16	83.47	1	83.05	22.47
7	4.73	3	81.09	2	80.95	22.63
8	4.61	1	67.17	1	67.16	7.55
9	4.55	3	68.60	1	67.22	11.24
10	4.49	3	95.70	1	95.05	22.69
11	4.01	4	88.40	2	88.08	16.43
12	3.27	1	89.46	1	89.15	14.59
13	2.70	1	86.21	1	86.06	14.85
14	2.56	4	81.87	1	81.32	13.14
15	2.49	1	73.71	1	73.70	17.53
16	2.32	6	85.84	1	85.38	9.31
17	2.04	6	68.94	1	68.52	14.31
18	2.02	5	69.97	1	69.96	7.51
19	2.01	5	101.21	4	101.06	23.17
20	1.80	8	88.51	1	88.03	22.55
21	1.72	2	83.22	1	83.25	6.40
22	1.41	1	75.06	1	74.75	14.94
23	1.40	1	93.88	1	93.55	22.20
24	1.18	2	99.58	1	99.29	22.04
25	1.18	1	69.95	1	69.88	9.37
26	1.07	5	62.25	1	62.07	23.64
27	1.05	2	95.73	1	95.50	23.07
28	1.02	2	92.23	1	91.80	22.06
29	1.01	1	95.85	1	95.70	18.05
30	1.01	2	86.75	2	86.45	20.26
31	12.43	16	82.09	2	74.69	10.72
32	12.11	5	77.05	1	76.48	6.11
33	8.08	3	75.88	1	75.38	16.01
34	12.71	8	65.90	2	64.52	10.04
35	10.10	3	84.38	1	84.35	6.49
36	13.52	11	77.11	1	74.38	19.96
37	2.94	15	81.41	1	80.57	15.38

Table 5: BWSNII - boundary valves at final solution

Valve ID	Start sub-network	End sub-network
LINK-200	1	2
LINK-6446	1	2
LINK-9623	1	2
LINK-13127	1	2
LINK-2848	1	3
LINK-1385	1	4
LINK-1783	1	4
LINK-13867	1	5
LINK-13955	1	5
LINK-10321	1	6
LINK-11131	1	7
LINK-11137	1	7
LINK-7355	1	8
LINK-11433	1	9
LINK-320	1	10
LINK-6107	1	11
LINK-7218	1	11
LINK-6411	1	12
LINK-3939	1	13
LINK-5124	1	14
LINK-9195	1	15
LINK-6750	1	16
LINK-14278	1	17
LINK-8131	1	18
LINK-4374	1	19
LINK-4542	1	19
LINK-5783	1	19
LINK-10904	1	19
LINK-3705	1	20
LINK-9248	1	21
LINK-5276	1	22
LINK-6342	1	23
LINK-784	1	24
LINK-9581	1	25
LINK-4194	1	26
LINK-10795	1	27
LINK-5835	1	28
LINK-12170	1	29
LINK-6464	1	30
LINK-6845	1	30
LINK-978	1	31
LINK-14243	1	31
LINK-7723	1	32
LINK-14516	1	33
LINK-8072	1	34
LINK-8406	1	34
LINK-9228	1	35
LINK-13681	1	36
LINK-6891	1	37