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# Optimizing phosphorus diffusion for photovoltaic applications: Peak doping, inactive phosphorus, gettering, and contact formation

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The phosphosilicate glass (PSG), fabricated by tube furnace diffusion using a POCl<sub>3</sub> source, is widely used as a dopant source in the manufacturing of crystalline silicon solar cells. Although it has been a widely addressed research topic for a long time, there is still lack of a comprehensive understanding of aspects such as the growth, the chemical composition, possible phosphorus depletion, the resulting in-diffused phosphorus profiles, the gettering behavior in silicon, and finally the metal-contact formation. This paper addresses these different aspects simultaneously to further optimize process conditions for photovoltaic applications. To do so, a wide range of experimental data is used and combined with device and process simulations, leading to a more comprehensive interpretation. The results show that slight changes in the PSG process conditions can produce high-quality emitters. It is predicted that PSG processes at 860 °C for 60 min in combination with an etch-back and laser doping from PSG layer results in high-quality emitters with a peak dopant density  $N_{\text{peak}} = 8.0 \times 10^{18} \text{ cm}^{-3}$  and a junction depth  $d_j = 0.4 \,\mu\text{m}$ , resulting in a sheet resistivity  $\rho_{\text{sh}} = 380 \,\Omega/\text{sq}$  and a saturation current-density  $J_0$  below 10 fA/cm<sup>2</sup>. With these properties, the POCl<sub>3</sub> process can compete with ion implantation or doped oxide approaches. *Published by AIP Publishing*. [http://dx.doi.org/10.1063/1.4949326]

## I. INTRODUCTION

The *n*-type emitter of most crystalline *p*-type silicon solar cells is formed by phosphorus diffusion. A common P diffusion method is to expose Si wafers in a furnace at about 800–900 °C to an atmosphere of POCl<sub>3</sub> and O<sub>2</sub> (with N<sub>2</sub> as a carrier gas), forming a phosphosilicate glass (PSG) on the wafer surfaces. This process step is usually called predeposition, and the resulting PSG provides a source of P dopants that diffuse into the Si wafer. Most commonly, an additional process step, called drive-in, follows the predeposition, where the supply of dopant gases is disconnected, and P from the existing PSG diffuses further into the Si wafer.

To find optimum process conditions for photovoltaic applications, three different effects have to be considered. First, the in-diffusion of P from the PSG, and its presence in electrically active and inactive states in the Si wafer, which increases Shockley-Read-Hall (SRH) recombination. Second, the gettering of impurities in Si in the direction toward the PSG. Third, the metal contact formation of the P-rich Si region to the external circuit. These three effects can be described as follows.

P diffusion is usually performed at 800–900  $^{\circ}$ C. At this temperature the solubility limit of active P (the dopant

concentration) in silicon is around  $3 \times 10^{20} \text{ cm}^{-3.1}$  Because the PSG is a high-concentration P source, this solubility limit is usually exceeded; thus inactive P also diffuses<sup>2</sup> and may form P clusters and after prolonged high-temperature treatment even precipitates.<sup>3–8</sup> See Fig. 1 for an overview. As a result, two different profiles diffuse into Si, an electrically active P profile, which is the emitter creating the p-n junction in the p-type wafer, and an inactive P profile.<sup>9</sup> The inactive P in the form of interstitial P, clusters of P, and possibly SiP precipitates causes an increase in SRH recombination<sup>10-12</sup> and a decrease in the collection efficiency of photogenerated carriers in the Si solar cell. Consequently, reducing the inactive P concentration can increase solar cell performance. In Refs. 13 and 14 it is shown that the inactive P concentration can be lowered significantly by reducing the POCl<sub>3</sub> flow rates during the PSG process. In Ref. 13 this reduction in inactive P concentration has resulted in an increase of up to 10 mV in open-circuit voltage ( $V_{OC}$ ) in a solar cell. Other approaches<sup>15,16</sup> show that etching the PSG and then performing a drive-in reduces the inactive P concentration significantly.

The POCl<sub>3</sub> and its PSG layer are technologically successful because impurities are not likely to enter the Si, because (i) their vapor pressure in the glassy matrix is lowered by the melting process and (ii) they are nearly immobile in the glass.<sup>19</sup> This is in contrast to other dopant sources, such as gases, vaporized liquids, spin-on liquids, and some

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FIG. 1. Limit between activation of P (dopants) and inactive P (red solid line) as well as the solubility limit between inactive P and precipitating P (blue dashed line), as measured in thermal equilibrium in Refs. 2, 17, and 18.

other solid sources, where great care must be taken that impurities do not contaminate the Si. In turn, the PSG process is also essential for gettering of impurities from the Si bulk material,<sup>20</sup> which occurs at the same time and temperature conditions as the diffusion. The gettered impurities leave the base region and accumulate in the emitter region. Because the minority-carrier concentrations are lower in the emitter region than in the base region, the total amount of SRH recombination in the device is reduced. Further it may be possible that the impurities in the emitter are in a different phase (i.e., precipitated) which also reduces SRH recombination. Consequently, this improves the excess carrier lifetime in the base region. Especially for low-lifetime material, such as conventional multicrystalline silicon, this effect is essential to achieve higher bulk lifetimes. In Refs. 21-24 gettering of a variety of impurities in different Si materials is reported. Especially accumulation of Cu, Ni, Fe, and Cr in the emitter is shown.<sup>22,23</sup> In Ref. 25, it is shown that the gettering process conditions have to be adapted for high concentrations of Fe impurities. In general it can be followed that for a specific type of impurity and specific concentrations, individual PSG process conditions have to be adapted to maximize gettering efficiency. On the other hand, these process conditions must also create a high-quality emitter, requiring a low concentration of inactive P.

Screen-printing is conventionally used to contact a PSGdiffused emitter. In general, three different paths<sup>26–29</sup> exist for electron transport from Si via the contact to the external grid. First, direct current flow due to direct contact between Ag crystals and the grid. Second, tunneling through very thin PbO glass layers between Ag crystals and the grid. Third, current flow through the PbO glass layer by tunneling via metal impurities dispersed in the PbO glass layer. These transport mechanisms are assessed in Ref. 30. Contacting a lowly doped emitter is reported to be difficult because the contact resistivity is high.<sup>31,32</sup> Another possible problem is that with decreasing P concentration, the indiffused Ag profile can overcome the P profile and may shunt the emitter region.<sup>28</sup> Hence, in addition to high efficiency and metal impurity gettering, contact formation has to be considered when finding optimum process conditions for PSGs.

All three effects have their own optimum process conditions, but they are not independent from each other. This paper focuses on co-optimizing PSG formation for obtaining low saturation currents, effective gettering, and good contact formation. We start by showing optimized process conditions for forming the emitter, and then we show the limitations for gettering and contact formation. This strategy for identifying optimum process conditions can be adapted to other materials and more advanced process conditions.

### **II. PHOSPHORUS EMITTER IN SILICON**

To understand the P emitter formed in silicon by the PSG, we discuss in this section the following fundamental issues in PSGs. First, the growth of a PSG to estimate its thickness. Second, how P moves within the PSG and the silicon crystal. Third, electrically active and inactive P in Si as a function of the POCl<sub>3</sub> flow. Fourth, possible depletion of P in PSG layers.

#### A. Growth model for the PSG layer

We will see in Secs. II B and III B that PSG layers rarely stay so thin that they become depleted of P during the drivein. Hence, the PSG layer thickness  $x_{PSG}$  is not a critical parameter. However, the following quantitative model of  $x_{PSG}$ is viable for the etching of the PSG in advanced emitter structures, for optical inspection, and quality control in fabrication.

The PSG layer thickness  $x_{PSG}$  (including the SiO<sub>2</sub> layer at the interface between PSG and Si) depends on various process parameters such as deposition time *t* and deposition temperature *T*, the flows of N<sub>2</sub>, POCl<sub>3</sub>, and O<sub>2</sub>, as well as the temperature of the POCl<sub>3</sub> bubbler  $T_{bubbler}$ . Typical thicknesses of PSGs are reported to be 10–80 nm.<sup>13,33</sup>

The growth behavior of the PSG layer obeys the parabolic law,<sup>34</sup> indicating that the rate controlling process is diffusion. To discuss the relative importance of the parameters describing the growth, we use a simple empirical equation for  $x_{PSG}$ , proposed by Negrini *et al.*<sup>4</sup>

$$\chi_{PSG} = \sqrt{B_0 \cdot \exp(-E_0/k_B T) \cdot t},\tag{1}$$

where the constant  $E_0$  is 1.7 eV, *t* the deposition time [min], *T* the deposition temperature [K] and the parameter  $B_0$  [nm<sup>2</sup>/min] empirically describes the influence of the gas flow rates on  $x_{PSG}$ . Unfortunately,  $B_0$  cannot be given as a universal function of N<sub>2</sub>, POCl<sub>3</sub>, and O<sub>2</sub> flow rates.

To derive  $B_0$  as a function of POCl<sub>3</sub> flow rate, we calibrate it on our experimental data for different PSG thicknesses  $x_{PSG,Exp}$  published in Refs. 13, 33, and 35, where the POCl<sub>3</sub> flow rate was varied from 125 to 1500 sccm by



FIG. 2. Measured<sup>13,33,35</sup> and empirically fitted PSG thicknesses under various process conditions: (a) for different deposition times and temperatures, with constant N<sub>2</sub>, POCl<sub>3</sub> and O<sub>2</sub> flows; and (b) for different POCl<sub>3</sub> flows, times, and temperatures, with constant N<sub>2</sub> and O<sub>2</sub> flows. The experimental values (symbols) are measured with different techniques, and the empirical fits (lines) are obtained with Eqs. (1) and (2).

holding the N<sub>2</sub> and O<sub>2</sub> flows constant.  $x_{PSG,Exp}$  was measured with four different experimental techniques:<sup>33</sup> atomic force microscopy (AFM), profilometry, scanning electron microscopy (SEM), and spectroscopic ellipsometry. The measurement uncertainties were lowest (near 2 nm) for AFM and SEM and highest (4 nm) for the ellipsometer. From the calibration procedure we got the following expression for  $B_0$  as a function of the POCl<sub>3</sub> flow  $\Phi$  [sccm]

$$B_0 = a_1 \cdot (\sqrt{\Phi})^{a_2} \tag{2}$$

with  $a_1 = 1.03561 \times 10^7 \text{ [nm}^2/\text{min sccm}^{a2/2]}$  and  $a_2 = 1.51449$ .

In a separate study,<sup>35</sup> we analyzed the influence of  $x_{PSG,Exp}$  from the O<sub>2</sub> flow while keeping the POCl<sub>3</sub> flow constant. It was found that  $x_{PSG,Exp}$  is rather independent of the O<sub>2</sub> flow: only for very small O<sub>2</sub> flows the formation of a PSG is suppressed, and for larger O<sub>2</sub> flows,  $x_{PSG}$  is influenced by only 1 nm (for flows up to 500 sccm).

Another parameter that might influence  $x_{PSG,Exp}$  is the POCl<sub>3</sub> bubbler temperature  $T_{bubbler}$ . We varied in Ref. 36  $T_{bubbler}$  from 15.5 to 24.5 °C and found that the  $x_{PSG,Exp}$  varies only by 4 nm. Because of this small influence we did not include the bubbler temperature in Eq. (1).

In Fig. 2 our experimental data from Refs. 13, 33, and 35 for  $x_{PSG,Exp}$  and the calculated  $x_{PSG}$  from Eqs. (1) and (2) are presented. Overall a good fit of the experimental data can be obtained with Eqs. (1) and (2). Further improvements of a growth model may be achieved by taking N<sub>2</sub>, O<sub>2</sub>, and  $T_{bubbler}$  into account.

#### B. Phosphorus in the PSG layer and in silicon

In Section II A it was shown that the PSG thickness is influenced by several process parameters, mainly by time, t, temperature, T, and the POCl<sub>3</sub> flow rate. These process parameters also influence the P diffusion in Si and within the PSG. The influence of t and T on the diffusion profile in Si has been investigated thoroughly (for a review, see Ref. 1). However, please note that such diffusion models of P within Si require the peak dopant density at the Si surface as input parameter and, accordingly, have limited predictive power. Therefore, we focus here on setting up a model that quantifies how the P profile is influenced directly by the POCl<sub>3</sub> flow. For a better knowledge of this dependence, the P flow within the PSG and through the interface to Si needs to be better understood, as is done in the following. During the pre-deposition process, POCl<sub>3</sub> and O<sub>2</sub> accumulate on top of Si and create the PSG. After a PSG diffusion process, usually a layer structure described as PSG/SiO<sub>2</sub>/Si is observed,<sup>37</sup> as shown in secondary ion mass spectrometry (SIMS) measurements shown in Fig. 3(a). The signal intensity of P is rather constant in the PSG, is minimal in the SiO<sub>2</sub> layer, and has a strong pile up at the interface between SiO<sub>2</sub> and Si.

The observed minimum of phosphorus in the SiO<sub>2</sub> layer can be explained as follows. On the one hand, the original Si surface is moved into the Si due to oxidation. On the other hand, a high segregation of P between SiO<sub>2</sub> and Si is reported.<sup>38,39</sup> This means that during the growth of the SiO<sub>2</sub> layer P is continuously pushed away from SiO<sub>2</sub> into the direction of Si. At the PSG/SiO<sub>2</sub> interface, instead, the situation is more complex. A possible explanation might be that segregation works in the direction of the PSG and diffusion in the direction of the SiO<sub>2</sub>. It seems that both processes balance each other and as a result the observed minimum in the SiO<sub>2</sub> layer appears.

The strong pile-up at the SiO<sub>2</sub>/Si interface can be explained as follows. Two processes are working in parallel: first, P is pushed into Si via segregation and second, P diffuses from the PSG/SiO<sub>2</sub> system in the direction of Si. The solubility limit of electrically active P is usually reached in Si and inactive P in various forms is observed.<sup>2,3,5–8</sup> This means that the overall P concentration is limited in Si and once this limit is achieved, P accumulates and piles up at the SiO<sub>2</sub>/Si interface.

To analyze the influence of POCl<sub>3</sub> on phosphorus in the PSG/SiO<sub>2</sub>/Si system, the POCl<sub>3</sub> flow was varied from 250 to 1000 sccm, while all other parameters were kept constant: t = 40 min,  $T = 840 \,^{\circ}\text{C}$ , and  $O_2 = 250 \text{ sccm.}^{37}$  In Fig. 3(b) a small variation of P signal intensity in the PSG can be observed and a rather strong variation at the pile-up of P at the SiO<sub>2</sub>/Si interface. This effect may be explained as follows. It is known<sup>39</sup> that the in-diffusion of P from the PSG in SiO<sub>2</sub> is stronger with a higher P content in PSG. This results in a higher content of P in the SiO<sub>2</sub> region and consequently a larger amount of diffused P from the SiO<sub>2</sub> into the Si. Finally, the solubility limit of P in Si is further exceeded and a stronger pile-up of P at the SiO<sub>2</sub>/Si interface can be observed.

The previously described results explain why there is a variation in the amount of electrically active and inactive P



FIG. 3. SIMS measurements of phosphorus in the PSG/SiO<sub>2</sub>/Si layer structure fabricated with different POCl<sub>3</sub> flows from Ref. 37. (a) SiO<sub>2</sub> layer between PSG and Si after 40 min of diffusion at 840 °C, with POCl<sub>3</sub> = 500 sccm and  $O_2 = 250$  sccm. (b) Measurements on structures with the same process conditions as before, but different POCl<sub>3</sub> flows. A difference in P concentration is observable in the PSG layer and a stronger pile-up of P at the SiO<sub>2</sub>/Si interface with higher POCl<sub>3</sub> flows. This leads to a stronger in-diffusion of inactive P into Si (cf. Fig. 4).

in Si. We analyzed the results in more detail for different POCl<sub>3</sub> flows.<sup>13</sup> In Fig. 4 SIMS measurements show the total amount of P in Si, and electrochemical capacitance voltage (ECV) measurements of the same samples show only the electrically active P concentration.<sup>40</sup> In this experiment four different POCl<sub>3</sub> flows were used while holding all other process parameters constant. The results show a decreasing inactive P profile (SIMS data) with decreasing POCl<sub>3</sub> flows, as can be explained with the discussion above. Compared with the SIMS data, the changes in electrically active P profile (ECV data) are less, because the temperature is kept constant and so is the solubility limit of P in Si. The P profile becomes shallower, but drops only for very low POCl<sub>3</sub> flows.

Note that in Fig. 4 the inactive P penetrates deeper into Si than the plateau at the solubility limit of the active P profile. This has been observed also in other laboratories,<sup>14,41</sup> but is not always the case.<sup>16,42</sup> Possible reasons for a deeper penetration of inactive P are: (i) the SIMS profile contain P clusters, which are stable and mobile. They are sufficiently stable, so they do not dissolve when diffusing deeper than



FIG. 4. The total P concentration in Si measured with SIMS (filled symbols) and the electrically active P concentration measured with ECV (empty symbols) for different POCl<sub>3</sub> flow rates. The profiles are obtained from PSG diffusions at 840 °C for 40 min with  $O_2 = 250$  sccm and varied POCl<sub>3</sub> flows from Ref. 13. The calculation with the carrier mobility model from Refs. 43 and 44 leads to the sheet resistivities of 60, 70, 75, and 105  $\Omega$ /sq.

the plateau of the solubility-limited active P; (ii) the SIMS profile contains very small precipitates, which do not dissolve quickly and therefore do not dissolve when diffusing into deeper regions where the solubility limit of P is not reached; these precipitates may form only during cool down of the samples while the solubility limit is lowered in an Arrhenius-like manner; (iii) the SIMS profile may contain large precipitates, which grow over time and penetrate more deeply into Si than the plateau. Under conventional process conditions in photovoltaics, usually no precipitates are formed, but the mobile clusters of interstitial phosphorus.

The above discussed ECV and SIMS measurements were taken on samples at room temperature after the PSG process. In Ref. 45 it is described that the PSG layer is viscous at process temperatures between 800 and 1200 °C. This means that during the process a liquid-like PSG could exist on top of SiO<sub>2</sub> and Si. It might be that also part of the SiO<sub>2</sub> may be viscous, because the viscosity of SiO<sub>2</sub> is strongly influenced by its P content and possibly by other elements like N, C, and H. Even under these conditions the above described diffusion processes still exist. The segregation from SiO<sub>2</sub> to a viscous PSG would also be strong, so does the diffusion from the high concentration PSG region to the low concentration SiO<sub>2</sub> region.

Another open question is whether the PSG's P content can be depleted during conventional process conditions. In Ref. 13 typical P doses in the PSG between 1 and 5  $\times 10^{16}$  cm<sup>-2</sup> and doses in Si between 1 and 7  $\times 10^{15}$  cm<sup>-2</sup> are reported. This means that after a conventional process of, e.g., 840 °C for 40 min, still a large amount of P remains in the PSG. It is questionable whether this amount can still diffuse into Si for two reasons. First, the strong pile-up of P at the SiO<sub>2</sub>/Si interface may act like a diffusion barrier for P from the PSG. Second, the growing SiO<sub>2</sub> layer between PSG and Si may act like a diffusion barrier. We assume that a pure SiO<sub>2</sub> layer is sandwiched between the PSG layer and Si. Using a diffusivity model<sup>46</sup> for P in SiO<sub>2</sub>, we simulate a process of 40 min at 840 °C with a peak concentration of 8  $\times 10^{21}$  cm<sup>-3</sup> P atoms<sup>13</sup> at the PSG/SiO<sub>2</sub> interface: the concentration of P decreases to almost zero within the first 1 nm in SiO<sub>2</sub>. This means that pure SiO<sub>2</sub> is an almost perfect diffusion barrier for P under the typically applied PSG process conditions. It seems likely that the growing SiO<sub>2</sub> layer during the PSG process begins to act as a diffusion barrier for P from PSG in the direction of Si. Nevertheless the SiO<sub>2</sub> layer contains a high amount of P that can diffuse into Si.

# III. PERC SOLAR CELL SIMULATION WITH ELECTRICALLY ACTIVE AND INACTIVE PHOSPHORUS PROFILES

As discussed above, it is well known that different process conditions for the PSG formation produce different electrically active P profiles (emitters) and different electrically inactive profiles in Si. It is evident that inactive P should be avoided for a high quality emitter to reduce SRH recombination. Further, the peak concentration of the electrically active profiles should be lowered to reduce Auger recombination. Considering the effects discussed in Section II, we will simulate the PERC (passivated emitter and rear cell) solar cells as described below with various emitter and inactive P profiles to give a perspective of what can be achieved with PSG processes and to show an upper limit for a nearly ideal emitter (optimized Gaussian shaped emitter for the simulated PERC cell).

# A. Simulation model details

A PERC solar cell<sup>47</sup> is simulated in Sections III B and IV to discuss different aspects of emitters fabricated with a PSG layer. The specifications are as follows: The simulated PERC solar cell is 180  $\mu$ m thick and is simulated in the unit domain shown in Ref. 48. A distance of 1.2 mm is assumed between the front grid finger contacts, which have a width of  $45\,\mu\text{m}$ . Three rear-finger contacts are placed between two front contacts, which have a width of 90  $\mu$ m. We assume a rear surface recombination velocity  $S_{rear} = 10 \text{ cm/s}$  at the rear passivation, a value which has been experimentally realized with Al<sub>2</sub>O<sub>3</sub>, e.g., in Ref. 49. The B doping in the base is 2  $\Omega$ cm, equivalent to a B concentration of 7.12  $\times$  10<sup>15</sup> cm<sup>-3</sup>. All cells have the same local Al-BSF<sup>50</sup> (back surface field) covering the rear finger-shaped contacts. The Si bulk SRH lifetime is set to 1 ms, assuming high-quality Cz Si material in a deactivated state of the B-O complex. SRH recombination due to inactive P is modeled with parameters from Ref. 12. The remaining model parameters for Si, such as band diagram parameters and recombination models, are taken from Ref. 48 (including Fermi–Dirac statistics and Schenk's band gap narrowing model).

All simulations are carried out at 1 Sun and 300 K, using the software Sentaurus TCAD (Version C-2012.06, from Synopsys, Inc.). The optical generation within the textured wafers is modeled by ray tracing using the software Sunrays.<sup>51</sup> The resulting IV-curves are corrected by metal shading and resistive losses in the metalization that are typical for  $15.6 \times 15.6$  cm<sup>2</sup> solar cells.

To show the effect of the emitter and inactive P on the described PERC solar cell, several emitters and inactive P profiles from the literature are used. First, the profiles from Fig. 4 are used. Similar results were observed by Lee *et al.*,<sup>14</sup> where lowering the POCl<sub>3</sub> flow rate results in lower inactive P concentrations in Si. Khandelwal *et al.*<sup>15</sup> show that after removing the PSG and performing an additional drive-in (oxidation) step, the inactive P can be resolved entirely.

Prajapati *et al.*<sup>16</sup> also show that additional drive-in steps (oxidations) can decrease or entirely dissolve the inactive P in Si. Cabrera *et al.*<sup>52</sup> present two possible PSG diffused emitters where the amount of inactive P is reduced significantly in one case. Our work<sup>53</sup> presents an optimized emitter profile including lower inactive P concentration.

Bentzen et al.<sup>42</sup> present a model that simulates the inactive P and the emitter from a fixed surface concentration. In this model, the variation of the POCl<sub>3</sub> flow is only included empirically by a variation of the P concentration at the PSG/ Si interface. As we know the P concentration from our experiments, the model is used here to simulate both profiles. Using the above experimental results, we vary the surface concentration from  $5 \times 10^{19} \text{ cm}^{-3}$  to  $7.5 \times 10^{20} \text{ cm}^{-3}$  and keep the diffusion process constant at 840 °C and 30 min, followed by a ramp down to 500  $^\circ\mathrm{C}$  in steps of 17 K/min. As ideal emitter we choose a Gaussian profile with a peak concentration of  $1 \times 10^{19}$  cm<sup>-3</sup>, a depth of 0.4  $\mu$ m, and an ideal front surface recombination velocity  $s_{\text{front}}$  of 1 cm/s. The sfront values for emitters without inactive P are taken from Ref. 54, and the  $s_{\text{front}}$  values for emitters containing inactive P from Ref. 12. The additional SRH recombination due to inactive P is simulated using the capture cross sections from Ref. 12. The inactive P and emitter profiles from all the above-listed references are used to simulate the PERC solar cells as described above. It should be noted that only the emitter and inactive P profiles are varied, and all other parameters are held constant.

#### **B. Simulation results**

Figure 5 shows results of simulated PERC solar cells with different emitters and inactive phosphorus profiles as explained in Section III A. Plotted are the cell efficiency  $\eta$  as a function of open-circuit voltage  $V_{\rm OC}$  and  $\eta$  as a function of short-circuit current density  $J_{\rm SC}$ . The dashed line represents the boundary between emitters with and without inactive P. In general, the following conclusions can be drawn: With decreasing inactive P concentration, the SRH recombination in the emitter region decreases and consequently  $V_{\rm OC}$  and  $\eta$  increase. Further increase in  $V_{\rm OC}$  is due to lower peak concentrations of the electrically active profile (emitter) and, with this, the lowering of Auger recombination. Additionally, the surface recombination velocity is reduced with lower peak concentration. The ideal emitter represents hereby an upper limit.

 $J_{\rm SC}$  shows the same general trends. With decreasing the inactive P concentration,  $J_{\rm SC}$  increases due to a better collection efficiency of photo-generated carriers (better blue response). Further increase is possible due to lower Auger recombination rates. Because the collection efficiency of highly-doped emitters depends sensitively on their dopant profile and their profile of inactive P, the simulated  $J_{\rm sc}$  values scatter to some extent.

Based on these results, the optimal strategy would be to reduce the inactive P concentration as much as possible and in addition lower the peak concentration of the electrically active emitter. As mentioned earlier, this simple approach has two problems. First, the gettering efficiency of the



emitter may be reduced. Second, contact formation may pose a serious problem. We are going to show limitations of these two issues in Sections IV–V.

### **IV. DEFECT GETTERING WITH THE PSG PROCESS**

The in-diffusion of P into Si from a PSG layer is strongly coupled to the gettering process. Impurities pile up under the in-diffused P profile, while the recombination activity of these gettered impurities is strongly reduced in the emitter region as mentioned in Section I. Consequently, the Si bulk lifetime increases. Section III showed that lowering the P peak concentration in Si is an effective way to increase PERC solar cell efficiency. We will show now that gettering may become inefficient if the peak concentration of P is significantly reduced. We perform another simulation study, using Fe as a representative impurity which is well known to limit solar cell performance.<sup>55</sup> See Refs. 56–58 for comprehensive review of several models of iron impurity evolution during solar cell processing.

The gettering of Fe is simulated with the Impurity-to-Efficiency simulator<sup>59,60</sup> where the simulated P in-diffusion is based on the model from Bentzen et al.42 and the Fe segregation in the P layer on the one developed by Haarahiltunen et al.<sup>61</sup> We assume an initial homogeneous contamination of interstitial iron (Fe<sub>i</sub>) in the Si bulk material of  $1.0 \times 10^{11}$  cm<sup>-3</sup> and a total iron concentration Fe of  $1.0 \times 10^{13} \text{ cm}^{-3}$ . The initial radius of the Fe precipitates is set to 25 nm, within the range of sizes that have been observed experimentally in mc-Si.<sup>62,63</sup> For a representative PSG process we simulate the following diffusion and gettering scenario. The process occurs at 840 °C for 30 min, with a variable cool down ramp in 5, 10, 15,..., 100 min to 500 °C, which corresponds to 68 K/min (5 min) to 3.4 K/min (100 min). In addition, the P peak concentration was varied to simulate a reduction of P in the PSG. We simulated a peak concentration of  $7.5 \times 10^{20} \text{ cm}^{-3}$  including inactive P and peak concentrations of  $2.5 \times 10^{20} \text{ cm}^{-3}$ , 1.0  $\times$  10<sup>20</sup> cm<sup>-3</sup>, and 5.0  $\times$  10<sup>19</sup> cm<sup>-3</sup> without inactive P. A potential deactivation of part of the P during the slow ramps is considered not to be significant as compared with the other factors influencing the gettering process. The resulting emitter and inactive P profiles are implemented in the PERC solar cells as described in Section III.

The results are shown in Fig. 6. Plotted is the efficiency  $\eta$  of the PERC cells over the average bulk Fe<sub>i</sub> concentration in Si after gettering. This average Fe<sub>i</sub> concentration is the

FIG. 5. Simulated I-V-curve parameters from PERC solar cells using various P emitter dopant profiles and inactive P profiles from the literature as indicated. (a) Cell efficiency  $\eta$  over  $V_{OC}$ ; the PERC cells without inactive P have a higher  $\eta$  due to lower SRH recombination. (b) A similar trend can be observed in  $J_{SC}$  over  $\eta$ ; the inactive P lowers the collection probability of photogenerated carriers and reduces  $J_{SC}$ .

average in bulk Si, as simulated from  $2 \,\mu m$  to  $180 \,\mu m$  depth, which excludes the pile-up of Fe<sub>i</sub> in the emitter region. In general, the following statements can be drawn. First, the cool-down ramp rate is highly important for the gettering efficiency. A slower cool down leads to a better gettering of Fe<sub>i</sub>, which means lower Fe<sub>i</sub> bulk concentration for all peak concentrations. These trends have also been observed experimentally, for example, in Refs. 64-66. A very fast cool down can result in even higher Fe<sub>i</sub> concentrations after the gettering process. This can be explained as follows. During the process, e.g., at 840 °C, Fe<sub>i</sub> approaches its solubility limit in Si and will segregate to the emitter region. During a slow cool down, the solubility limit is decreasing slowly, giving Fe<sub>i</sub> the opportunity to diffuse to the emitter region or precipitate in the bulk. During a fast cool down the fast reduction of temperature precludes that Fe<sub>i</sub> can diffuse to the emitter region or to a precipitate, leading to a Fei concentration in the base that is even higher than that of the as-grown state.

Second, with decreasing P peak concentrations, gettering is weaker because the gettering efficiency is coupled to



FIG. 6. Simulated PERC solar cell efficiencies for different emitter peak concentrations and cool down rates during P gettering. Plotted is the efficiency  $\eta$  over the average Fe<sub>i</sub> concentration in the Si bulk after gettering. Each line represents the situation for a specific P peak, and each symbol represents a different cooling rate. Symbols on the very left have a slow cool down rate, 100 min (3.4 K/min) from 840 °C to 500 °C, while symbols on the right side have a fast cool down rate, 68 K/min (in 5 min) from 840 °C to 500 °C.

the P peak concentration. This effect has also been observed experimentally.<sup>67,68</sup> Consequently, a longer cool down is needed to achieve the same Fe<sub>i</sub> concentration.

Other impurities, such as Ag, Ti, Mn, Co, Cr, Ni, Mo, and Cu, are gettered during P diffusion as well.<sup>21–24</sup> These impurities might behave similarly to Fe<sub>i</sub>, according to their respective diffusivity and solubility limit values, and the ability to getter them may also depend on the cooling rate and peak concentration of P, among other factors. Note that part of the impurities can re-diffuse into the base region during the final firing step, which is not taken into account here.

In summary, if the P concentration in the PSG is significantly lowered, higher efficiencies are possible due to lower inactive P and lower Auger and surface recombination velocities, but gettering could be less efficient. Longer cool down ramps may enable co-optimization of inactive P concentration and impurity gettering.

# **V. CONTACT FORMATION AND PSGs**

As outlined in the introduction, the metal contact formation by screen-printing is still a subject of investigation. In general, contacts to emitters with a low concentration of inactive phosphorus may suffer from high contact resistivities (larger than 4 m  $\Omega$  cm<sup>2</sup>) causing low fill factors (FF) of the IV curve. In this section, we focus on the lower limits of electrically inactive P concentration.

To investigate the influence of the inactive P on contact formation, we processed solar cells having several different densities of inactive P in their emitter, as shown in Fig. 4. After alkaline texturization and cleaning, several POCl<sub>3</sub> diffusion processes have been applied by adjusting the POCl<sub>3</sub>-N<sub>2</sub> gas flow during the pre-deposition phase, as discussed in Section III. The flow was varied in three different rates: 250, 375, and 500 sccm for five samples each. Afterward, the PSG was removed by Hydrofluoric acid, and a 70 nm thick layer of PECVD  $SiN_x$  with a refractive index of 2.0 at a wavelength of 633 nm was deposited on the front side. The metalization was realized by a standard screen-printing procedure with a 3-busbar front side design. The rear side was metalized with a full-area thick-film Al paste to form the Al-BSF. The base material for this study is Cz boron-doped (100) silicon wafers with a base resistivity of 2.7  $\Omega$  cm and a thickness of 170  $\mu$ m.

Fig. 7 shows the results. Plotted are the fill factor and series resistance  $R_s$  over the POCl<sub>3</sub> flow. With decreasing

POCl<sub>3</sub>, the FF drops because  $R_s$  increases. Microscopic investigations in Ref. 31 indicate that a concentration between approximately  $5 \times 10^{20} \text{ cm}^{-3}$  and  $7 \times 10^{20} \text{ cm}^{-3}$  of inactive P is necessary to form a high-quality contact. Already years ago, very lightly doped emitters with a surface P concentration as low as  $4.0 \times 10^{19}$  cm<sup>-3</sup> could be contacted with affordable contact resistivities.<sup>32</sup> From recent screenprinting pastes it is reported<sup>31</sup> that the Ag crystallite density is independent of the emitter doping, but the Ag crystallite size increases as a function of the thickness of the plateau. This might be because emitters with a short plateau are likely to be etched by the Ag paste and this might generally lead to contact problems, which could explain the low FF when strongly lowering the POCl<sub>3</sub> flow (this was not the case in the cells investigated here). Another general possibility is that with decreasing P the in-diffused Ag profile might overcome the P profile, shunting the emitter region.<sup>28</sup> However, a detailed study<sup>69</sup> showed that this effect is not expected to be significant in the emitters discussed here. A further possibility may be the onset of band bending at the interface between Si and the PbO glass layer of the screen-printed contact.<sup>30</sup> In summary, while the P density at the Si surface is not anymore the limiting factor for contacting with low contact resistivity, care must be taken in experiments and in mass production that the emitter is sufficiently deep beneath the contacts. We take this into account in the proposed design of a high-efficiency emitter in Section VI.

# VI. HIGH-EFFICIENCY EMITTER FABRICATED WITH PSG

Fig. 3(b) indicates that, with varying the POCl<sub>3</sub> flow, only a limited change in the P concentration in the PSG layer seems possible. On the other hand, we also show that such a limited change in P concentration in the PSG layer strongly determines the resulting dopant profile in Si (cf. Fig. 4) and in many circumstances causes a significant amount of inactive P. The question arises, whether it is at all possible with POCl<sub>3</sub> to form a high efficiency emitter, like one that is close to the emitter implemented in PERL (passivated emitter, rear locally diffused) cells having efficiencies of up to 25%.<sup>70</sup> The  $n^+$  part of the emitter in these cells has a Gaussian shape with a very low peak concentration at the surface of  $N_{\text{peak}} = 5.0 \times 10^{18} \text{ cm}^{-3}$  but a considerable junction depth of  $d_j = 1 \,\mu\text{m}$ , resulting in a sheet resistivity near  $\rho_{\text{sh}} = 200 \,\Omega/\text{sq}$ and a saturation current  $J_0$  near 6 fA/cm<sup>2</sup>. Our simulations



FIG. 7. Fill factor and series resistance of solar cells as a function of  $POCl_3$ flow rate. Using standard screenprinting Ag paste and firing profiles, an adequate contact cannot be formed with low  $POCl_3$  flows and leads to a dramatic decrease in the fill factor.

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with Bentzen's model<sup>42</sup> show that such an emitter would require diffusion times longer than one hour and therefore too long for standard mass production. Our simulations predict, however, that an emitter with  $N_{\text{peak}} = 8.0 \times 10^{18} \text{ cm}^{-3}$ and  $d_i = 0.4 \,\mu\text{m}$  comes very close to the PERL emitter, resulting in  $\rho_{\rm sh} = 380 \,\Omega/\text{sq}$  and a  $J_0$  below 10 fA/cm<sup>2</sup> if passivated with a stack of a thin SiO<sub>2</sub> capped with a usual PECVD SiN<sub>x</sub> layer. This P profile requires a diffusion process at 860 °C for 60 min instead of conventional 840 °C for 30–40 min. During these 60 min, the SiO<sub>2</sub> layer of Fig. 2(a)may form a diffusion barrier for P. Nevertheless, there is a sufficient amount of P available for in-diffusion.

To be contacted, the PSG layer must be locally laserfired<sup>71</sup> before removal to form the  $n^{++}$  region, as for example, described in Ref. 72. The width of this  $n^{++}$  region depends on the alignment tolerances but is typically  $150 \,\mu m$ wide. Our simulations predict a minimum  $J_0$  of 215 fA/cm<sup>2</sup> in the metalized part and a  $J_0$  near 80 fA/cm<sup>2</sup> (Auger limit) in the passivated part of the n<sup>++</sup> region if the laser-induced defect density is insignificant. Afterward, the entire emitter (including the laser-fired part) must be homogeneously etched back by 240 nm to remove the highly doped region near the textured surface and all the inactive P, and is subsequently passivated.<sup>73,74</sup> This approach also enables the PSG to getter impurities sufficiently, because the peak concentration before etch-back is adequately high. The predicted optimum finger pitch is 900  $\mu$ m for 30  $\mu$ m wide and 15  $\mu$ m high metal fingers, and in this case  $J_0$  of the entire emitter (n<sup>+</sup> and n<sup>++</sup> part) is predicted to be 25 fA/cm<sup>2</sup>. Hence, our process and device simulations suggest that a high-efficiency emitter is indeed possible with POCl<sub>3</sub> diffusion in mass production if a suitable metalization can be achieved.<sup>15,75</sup>

# **VII. CONCLUSIONS**

With applying numerical simulations, it is possible to combine various experimental findings into a model, such as the composition of the phosphorus rich glass (PSG), inactive phosphorus in Si and its distribution, the gettering ability, and metal contact formation. Such a detailed model allows us to make specific forecasts that with slightly different PSG process times and temperatures (860°C for 60 min) an emitter with a saturation current density of only 25 fA/cm2 can be achieved (10 fA/cm2 in the lowly doped part and 80 fA/cm2 in the highly doped part). Hereby the gettering ability even for multicrystalline Si is sufficiently strong to be suitable for solar cells (down to peak dopant concentrations of  $5 \times 1019 \,\mathrm{cm}^{-3}$ ). More critical remains the question if emitters with low content of inactive P can be contacted with sufficiently low contact resistivities (below 4 m  $\Omega$  cm<sup>2</sup>). As possible well-known solution we suggest an additional laser doping from the PSG layer for increasing the dopant concentration at the metal contacts, followed by a homogeneous etch-back of the emitter.

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