

MIT Open Access Articles

Thermal Expansion Coefficient of Monolayer Molybdenum Disulfide Using Micro-Raman Spectroscopy

The MIT Faculty has made this article openly available. **Please share** how this access benefits you. Your story matters.

As Published: 10.1021/ACS.NANOLETT.9B01829

Publisher: American Chemical Society (ACS)

Persistent URL: <https://hdl.handle.net/1721.1/134770>

Version: Author's final manuscript: final author's manuscript post peer review, without publisher's formatting or copy editing

Terms of Use: Article is made available in accordance with the publisher's policy and may be subject to US copyright law. Please refer to the publisher's site for terms of use.



Thermal Expansion Coefficient of Monolayer Molybdenum Disulfide Using Micro-Raman Spectroscopy

Lenan Zhang, Zhengmao Lu, Youngsup Song, Lin Zhao, Bikram Bhatia, Kevin R. Bagnall, Evelyn N. Wang*

Department of Mechanical Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

* Corresponding author: enwang@mit.edu

ABSTRACT

Atomically thin two-dimensional (2D) materials have shown great potential for applications in nanoscale electronic and optical devices. A fundamental property of these 2D flakes that needs to be well characterized is the thermal expansion coefficient (TEC), which is instrumental to the dry transfer process and thermal management of 2D material-based devices. Yet, most of current studies of 2D materials' TEC extensively rely on simulations due to the difficulty of performing experimental measurements on an atomically thin, micron-sized, and optically transparent 2D flake. In this work, we present a three-substrate approach to characterize the TEC of monolayer molybdenum disulfide (MoS_2) using micro-Raman spectroscopy. The temperature dependence of the Raman peak shift was characterized with three different substrate conditions, from which the in-plane TEC of monolayer MoS_2 was extracted based on lattice symmetries. Independently from two different phonon modes of MoS_2 , we measured the in-plane TECs as $(7.6 \pm 0.9) \times 10^{-6}$ 1/K and $(7.4 \pm 0.5) \times 10^{-6}$ 1/K, respectively, which are in good agreement with previously reported values based on first principle calculations. Our work is not only useful for thermal mismatch reduction during material transfer or device operation, but provides a general experimental method that does not rely on simulations to study key properties of 2D materials.

1
2
3 **KEYWORDS:** 2D materials, MoS₂ monolayer, thermal expansion coefficient, micro-Raman
4 spectroscopy, three-substrate approach, phonon deformation potential
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56

1
2
3 Recent advances in atomically thin two-dimensional (2D) materials, such as graphene and
4 transition-metal dichalcogenide (TMD) have attracted particular interest due to their exceptional
5 properties¹⁻⁵ and promising applications in nanoscale devices.⁶⁻¹¹ It is of both fundamental and
6 practical significance to understand the thermal expansion coefficient (TEC) of such materials. On
7 one hand, TEC provides access to general anharmonic vibrational behavior of low-dimensional
8 systems.^{12,13} On the other hand, it is instrumental to reducing thermal mismatch, optimizing the
9 dry transfer process, and avoiding device failure during operation.¹⁴ However, direct
10 measurements of the TEC of 2D materials remain limited to date for various reasons. (1) These
11 atomically thin 2D materials are, more often than not, attached to thick substrates which
12 unfortunately dominate the thermal expansion behavior. Even though it is possible to suspend the
13 sample on microfabricated holes or slots ($\sim 10 \mu\text{m}^2$ in area), the corresponding free expansion can
14 hardly be observed. (2) Most 2D materials are optically transparent, which makes it difficult to
15 measure the TEC using conventional optical approaches.¹⁵ Accordingly, current understanding of
16 the TEC for 2D materials relies on either pure theoretical calculations^{16,17} or more recently,
17 combining experimental characterization (such as electron energy-loss (EEL) spectroscopy¹⁸) with
18 first-principle modeling which still depends on the choice of *ab initio* simulation methods.^{12,16-18}
19 In addition, Bao *et al.* characterized the TEC of a graphene membrane using scanning electron
20 microscope, which utilized graphene's negative TEC to create a sagging membrane on a trench
21 and finite element simulation to estimate the TEC of the trench.¹⁹

22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50 In this work, we propose a method that experimentally determines the TEC for 2D materials in
51 which the only necessary input is the lattice symmetry group. Specifically, we use micro-Raman
52 spectroscopy, which is capable of probing optical phonons at the microscale and is widely applied

1
2
3 to materials characterization and thermometry.^{2,20–28} Raman spectroscopy has advantages to study
4 the TEC of 2D materials as it can directly measure the phonon frequency shift due to the
5 perturbation of the strain field induced by thermal expansion.²⁹ In particular, Yoon *et al.* reported
6 the substrate effect on the phonon frequency shift of graphene and showed the coupling between
7 the thermal stress and thermal expansion.³⁰ The negative TEC of graphene was measured which
8 agrees well with Bao *et al.*'s measurement at room temperature.³⁰ However, Yoon *et al.*'s approach
9 requires biaxial strain coefficient and intrinsic temperature coefficient as inputs, which necessitates
10 additional experimental and theoretical efforts.³⁰ In this work, we propose a pure experimental
11 approach to measure TEC that can decouple the effect of thermal stress, in-plane thermal
12 expansion and out-of-plane thermal expansion effect on the Raman peak position and does not
13 require theoretically computed parameters as inputs. As an example, we demonstrated the
14 capability of our method by measuring the TEC of monolayer molybdenum disulfide (MoS₂). We
15 chose MoS₂ monolayer since it is one of the most representative TMDs^{3,4} which is widely used in
16 nanoscale devices.^{6–8} Many theoretical results of MoS₂ are also available to validate our
17 approach.^{16,17} We theoretically analyzed a temperature and stress dependent Raman spectrum of
18 monolayer MoS₂ through the phonon deformation potential and group theory, which describes the
19 effect of substrates on the supported 2D flakes. This unified theoretical framework was then used
20 to decouple the thermal stress, in-plane and out-of-plane thermal expansion effect and guide the
21 TEC measurement. Next, we extracted the TEC by characterizing the temperature-dependent
22 Raman spectra of monolayer MoS₂ flakes which were transferred onto three different substrates:
23 one suspended (or supported on an “air substrate”), one on fused silica, and another on copper.
24 The measured TEC using this three-substrate method shows good agreement with previous
25 theoretical calculations. This work presents a simple yet purely experimental method to measure
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60

1
2
3 the TEC of monolayer MoS₂, which can also be widely applied to study the thermophysical
4 properties of many other 2D materials and thin films.
5
6
7
8
9

10
11 We performed our measurements on single crystalline monolayer MoS₂ which was grown using
12 chemical vapor deposition (CVD). The MoS₂ monolayer was characterized using optical and
13 spectroscopic approaches (Section I of the Supporting Information for more details). Figure 1(a)
14 shows an optical image of the MoS₂ flake over the 300 nm thick thermal oxide layer. The
15 monolayer nature of this flake was confirmed by atomic force microscopy (AFM) characterization,
16 where the thickness was determined to be about $t = 1$ nm (Figure 1(b)). As shown in Figure 1(c),
17 monolayer MoS₂ has a hexagonal lattice structure which belongs to the D_{3h} point group.^{25,31} Each
18 unit cell consists of one molybdenum atom and two sulfur atoms. Consequently, monolayer MoS₂
19 has three Raman active optical phonon modes, *i.e.*, A'_1 , E' and E'' where the E'' mode is forbidden
20 in the back-scattering configuration.³² The A'_1 mode represents the out-of-plane vibration of atoms
21 whereas both E' and E'' modes represent the in-plane vibrations which have two-fold degeneracies
22 (Figure 1(c)). Figure 1(d) shows a typical Raman spectrum of monolayer MoS₂ at room
23 temperature where the characteristic peak positions of A'_1 and E' modes are at about 405 cm⁻¹ and
24 385 cm⁻¹ respectively. According to the symmetry group of the lattice structure, the irreducible
25 representation of the Raman active optical phonon modes Γ_{ph} at the Γ point can be decomposed
26 as,³¹
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49

$$\Gamma_{ph} = A'_1 + E'. \quad (1)$$

50
51
52
53
54
55
56
57
58
59
60

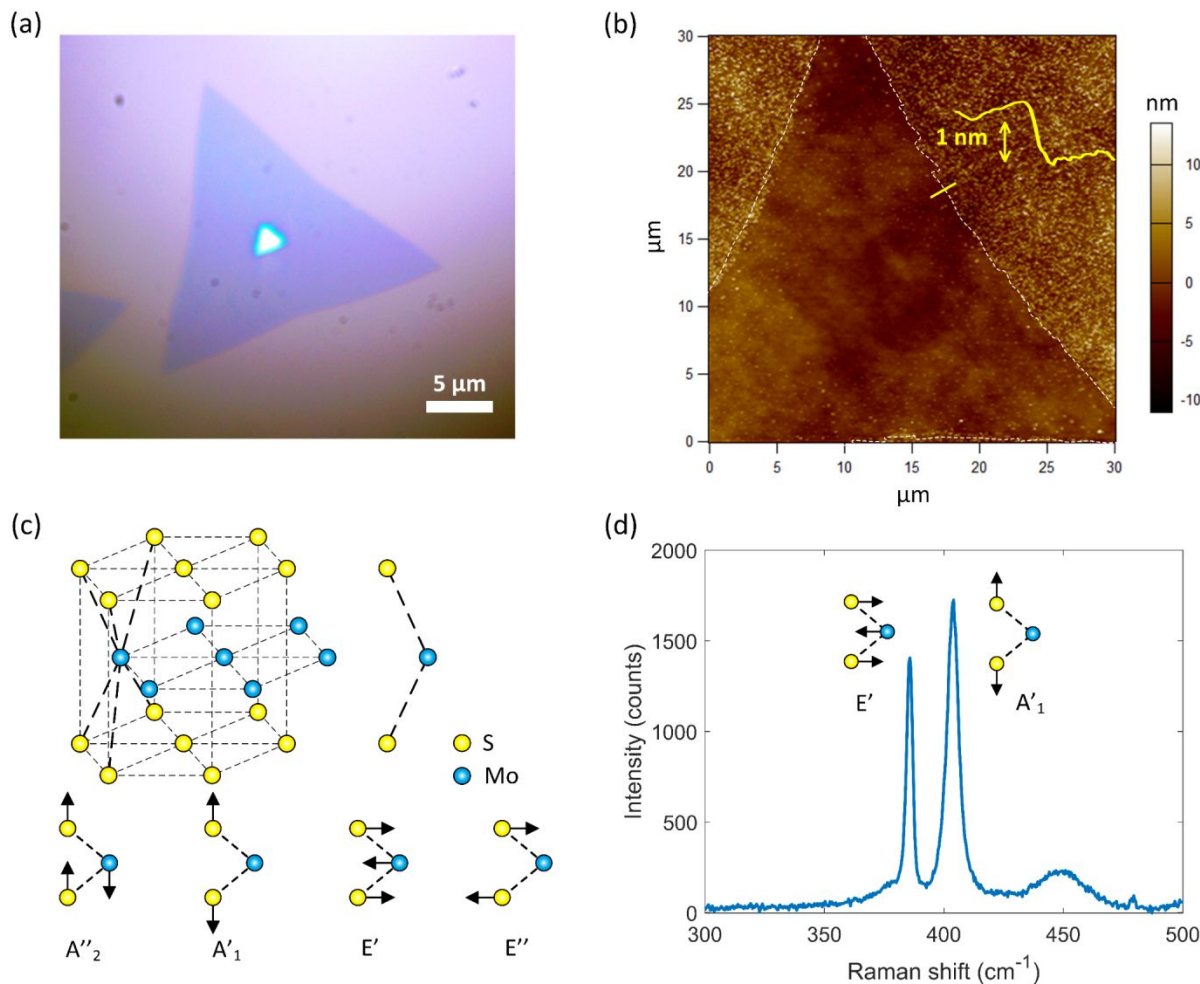


Figure 1 (a) Optical image of a CVD grown single crystalline monolayer MoS₂ flake on a 300 nm thick oxide layer from thermal oxidation of heavily doped silicon. The silicon substrate underneath is 1 mm thick. The bright small triangle at the center of the flake indicates the multilayer region which is more reflective than the monolayer region. (b) AFM image of a representative monolayer MoS₂ flake. Inset: The step height measurement from the monolayer to the substrate along the yellow line. The measurement results ($t \approx 1$ nm thickness) confirmed that the MoS₂ flake studied in this work is a single layer. (c) Lattice structure, unit cell, and Γ point phonon modes of the monolayer MoS₂. The monolayer MoS₂ belongs to the D_{3h} group. The A'_1 (~ 405 cm⁻¹) and E' (~ 385 cm⁻¹) modes were detected in the backscattering configuration. (d)

Typical Raman spectrum of the monolayer MoS₂ flake on the thermal oxide substrate. Schematic shows the corresponding vibrational modes of A₁' and E' peaks.

To understand the role of TEC in the phonon frequency shift, we performed symmetry and perturbation analysis on the monolayer MoS₂. According to the basis functions of the D_{3h} group (see character table of D_{3h} group in Supporting Information Section II), the perturbation potential V under an arbitrary strain field $\{\varepsilon_{ij}\}$ can be explicitly expressed as,

$$V = \sum V_{ij} \varepsilon_{ij} = \frac{1}{2}(V_{xx} + V_{yy})(\varepsilon_{xx} + \varepsilon_{yy}) + \frac{1}{2}(V_{xx} - V_{yy})(\varepsilon_{xx} - \varepsilon_{yy}) + V_{zz}\varepsilon_{zz} + 2(V_{xy}\varepsilon_{xy} + V_{yz}\varepsilon_{yz} + V_{zx}\varepsilon_{zx}), \quad i, j = x, y \text{ or } z, \quad (2)$$

where $\{\varepsilon_{ij}\}$ and $\{V_{ij}\}$ are the symmetric second rank tensors representing the strain perturbation and the corresponding deformation potentials, respectively. More specifically, the $V_{xx} + V_{yy}$ and V_{zz} terms belong to A₁', $V_{xx} - V_{yy}$ and V_{xy} belong to E', and V_{yz} and V_{zx} belong to E'', and therefore the perturbation potential V can be represented by $\Gamma_V = A_1' + E' + E''$. The shift of phonon frequency due to the perturbation potential V is given by the matrix element,³³

$$\Delta\omega^{(n)} = \frac{1}{\hbar} \langle \Gamma^{(n)} | V | \Gamma^{(n)} \rangle, \quad n = A_1' \text{ or } E' \quad (3)$$

where $\Delta\omega^{(n)}$ is the change of phonon frequency of A₁' or E' mode, $\Gamma^{(n)}$ is the corresponding wavefunction, and \hbar is the reduced Planck's constant. Plugging Eq. (2) into Eq. (3) and applying

orthogonality relationships (*i.e.*, calculating the direct product $\Gamma_{ph} \otimes \Gamma_V$),³³ Eq. (3) can be further simplified as (see Supporting Information Section II for detailed derivations),

$$\Delta\omega^{A_1'} = a^{A_1'}(\varepsilon_{xx} + \varepsilon_{yy}) + b^{A_1'}\varepsilon_{zz} \quad (4)$$

$$\Delta\omega^{E'} = a^{E'}(\varepsilon_{xx} + \varepsilon_{yy}) + b^{E'}\varepsilon_{zz} \pm c^{E'}[(\varepsilon_{xx} - \varepsilon_{yy})^2 + 4\varepsilon_{xy}^2]^{\frac{1}{2}} \quad (5)$$

where $a^{A_1'}$ and $b^{A_1'}$ are the phonon deformation potential constants (PDP) of the A_1' mode, and $a^{E'}$, $b^{E'}$ and $c^{E'}$ are the PDP of the E' mode. The \pm shown in Eq. (5) arises from the two-fold degeneracy of the E' mode. As $\{\varepsilon_{ij}\}$ is related to the thermal expansion and mechanical stress through the constitutive relation, we can obtain the general expressions describing the temperature and stress dependent phonon frequency (see Eqs. S(6) and S(8) in the Supporting Information). Note that the above analysis is valid for most of the TMD monolayers that belong to the D_{3h} point group (such as MoSe_2 , MoTe_2 , WS_2 and WSe_2). Additionally, for other symmetry point groups, this general theoretical framework still applies as we change the phonon modes and perturbation potential accordingly. In the thermal measurement, all of the stresses arose from thermal mismatch as no external mechanical forces were applied.³⁴ Accordingly, the MoS_2 flake was in a biaxial stress state with equal in-plane normal stress components ($\sigma_{xx} = \sigma_{yy} = \sigma$) and negligible shear stress ($\sigma_{xy} \approx 0$). In addition, the normal stress component σ_{zz} was negligible because the top of the flake was free to expand along c-axis. Consequently, we obtained the phonon frequency shift as a function of the in-plane thermal stress σ and temperature rise ΔT :

$$\Delta\omega^{(n)} = K^{(n)}\sigma + A^{(n)}\Delta T, \quad n = A_1' \text{ or } E' \quad (6)$$

1
2
3 where $K^{(n)}$ is known as the biaxial stress coefficient of A_1' or E' mode, and $A^{(n)}$ represents the
4 temperature coefficients of the corresponding modes. It can be clearly seen from Eq. (6) that the
5 thermal expansion can affect the phonon frequency through both the in-plane thermal stress σ and
6 the temperature coefficient $A^{(n)}$. In this work, we eliminated the need to know the thermal stress
7 σ or the biaxial stress coefficient $K^{(n)}$ from Eq. (6) using a three-substrate method.

18 Figure 2 shows the concept of the three-substrate method. The single crystalline monolayer MoS₂
19 flake was firstly transferred to a substrate consisting of 300 nm thick thermal oxide and 1 mm thick
20 silicon with holes patterned in it (see Figure 2(a)). The diameter of the hole is $D = 5 \mu\text{m}$. As the
21 suspended MoS₂ monolayer has a very large aspect ratio ($D/t \approx 5000$), the possible compressive
22 stress can be relaxed through buckling. Thus, the suspended area should be nearly free-of-stress
23 (see Supporting Information Section III for detailed assessment of the stress-free condition).^{2,20-22}

24 Since this region (on the 5 μm diameter hole) is larger than the laser spot size ($\approx 1 \mu\text{m}$), we can
25 perform the temperature-dependent Raman measurements and obtain the temperature coefficient
26 $A^{(n)}$. Next, monolayer MoS₂ flakes were transferred onto 1 mm thick fused silica substrate
27 (MolTech GmbH Molecular Technology) and 1 mm thick pure copper (99.999% purity, CU-M-
28 05-WF American Elements) wafers, respectively (Figures 2(b) and (c)). As the fused silica has
29 very low TEC ($\alpha_{SiO_2} = 0.55 \times 10^{-6} \text{ 1/K}$), compressive thermal stress $\sigma_{SiO_2} < 0$ was induced
30 within the MoS₂ flakes when temperature rose. On the other hand, the thermal mismatch due to
31 the very high TEC of pure copper ($\alpha_{Cu} = 16.5 \times 10^{-6} \text{ 1/K}$) led to tensile stress $\sigma_{Cu} > 0$ acting on
32 the MoS₂ flakes. Since the supporting substrates were much thicker than the MoS₂ flakes, *i.e.*, 1
33 mm \gg 1 nm, the substrates experienced free expansion with temperature rise. Note that no slip

between the MoS₂ flakes and the substrates is expected when the strain rate was relatively low due to the strong van der Waals (vdW) interaction (see Supporting Information Section III for detailed assessment of the no-slip condition).^{22,35,36} The strain-stress relations of the flakes supported on different substrates can be expressed as

$$\varepsilon_{SiO_2} = \alpha\Delta T + \frac{1-\nu}{E}\sigma_{SiO_2} = \alpha_{SiO_2}\Delta T \quad (7)$$

$$\varepsilon_{Cu} = \alpha\Delta T + \frac{1-\nu}{E}\sigma_{Cu} = \alpha_{Cu}\Delta T \quad (8)$$

where ε_{SiO_2} and ε_{Cu} are the in-plane thermal strain within the MoS₂ flake when they were supported by fused silica and pure copper substrates respectively. σ_{SiO_2} and σ_{Cu} are the corresponding in-plane thermal stress within the flake on the fused silica and pure copper substrates, which were induced by the thermal mismatches. α , E , and ν represent the in-plane TEC, Young's modulus, and Poisson ratio of the monolayer MoS₂ flake, respectively. Inserting Eqs. (7) and (8) into Eq. (6), the effect of TEC on phonon frequency shift through thermal stresses σ_{SiO_2} and σ_{Cu} can be explicitly shown as,

$$\Delta\omega_{SiO_2}^{(n)} = \left(\frac{K^{(n)}(\alpha_{SiO_2} - \alpha)E}{1-\nu} + A^{(n)} \right) \Delta T = A_{SiO_2}^{(n)} \Delta T, \quad n = A'_1 \text{ or } E' \quad (9)$$

$$\Delta\omega_{Cu}^{(n)} = \left(\frac{K^{(n)}(\alpha_{Cu} - \alpha)E}{1-\nu} + A^{(n)} \right) \Delta T = A_{Cu}^{(n)} \Delta T, \quad n = A'_1 \text{ or } E'. \quad (10)$$

Eqs. (9) and (10) suggest that we can relate the TEC to temperature coefficients of Raman measurements ($A_{SiO_2}^{(n)}$ and $A_{Cu}^{(n)}$) and eliminate the biaxial stress coefficient $K^{(n)}$. Further, for each symmetry class, we can explicitly express α as a function of $A_{SiO_2}^{(n)}$, $A_{Cu}^{(n)}$ and $A^{(n)}$ (Supporting Information II for detailed derivations):

$$\alpha = \frac{(A_{Cu}^{(n)} - A^{(n)})\alpha_{SiO_2} - (A_{SiO_2}^{(n)} - A^{(n)})\alpha_{Cu}}{A_{Cu}^{(n)} - A_{SiO_2}^{(n)}}, \quad n = A'_1 \text{ or } E'. \quad (11)$$

where $A^{(n)}$, $A_{SiO_2}^{(n)}$, and $A_{Cu}^{(n)}$ can all be determined experimentally and α_{SiO_2} and α_{Cu} are the bulk properties (characterized by the substrate suppliers in this work). Eq. (11) also suggests that we can obtain the in-plane TEC from either the A'_1 or E' mode independently. Since α determined from different modes should ideally be the same, this was used as a criterion to assess the consistency of our method.

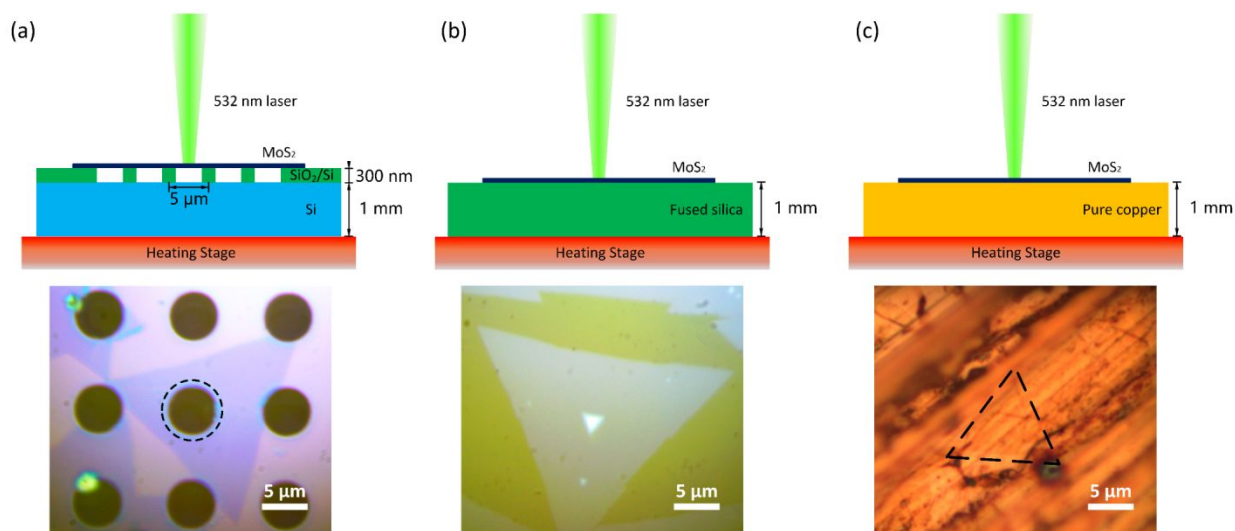


Figure 2 Schematics of the concept of three-substrate method for TEC characterization. (a) Temperature-dependent Raman measurement on monolayer MoS₂ suspended over 5 μm diameter holes. Bottom: 100X magnification optical image of a monolayer MoS₂ flake transferred onto the holey substrate. The dashed-circle indicates the suspended free expansion area where the measurement was performed. (b) Temperature-dependent Raman measurement on monolayer MoS₂ supported by a 1 mm-thick fused silica substrate. Bottom: 100X magnification optical image of a monolayer MoS₂ flake transferred onto the fused silica substrate. (c) Temperature-dependent

1
2
3 Raman measurement on monolayer MoS₂ supported by a 1 mm-thick pure copper substrate.
4
5 Bottom: 100X magnification optical image of a monolayer MoS₂ flake transferred onto pure
6
7 copper substrate. The dashed-triangle indicates the position of the flake (see Figure S1 for details).
8
9

10
11
12
13
14 The temperature-dependent Raman measurements were performed to characterize the temperature
15
16 coefficients for different substrates (Supporting Information Section IV for details about the micro-
17
18 Raman system). The Raman scattering was excited by a 532 nm wavelength diode laser (05-01
19
20 series, Cobolt). The 100X, $NA = 0.8$ microscope objective (LMPlanFL N, Olympus) was used to
21
22 focus the laser excitation and collect the Raman scattering. The corresponding laser spot size was
23
24 $\approx 1 \mu\text{m}$. The laser power was maintained at $< 0.1 \text{ mW}$ for the suspended flakes measurement and
25
26 at $< 1 \text{ mW}$ for the supported flakes measurements to avoid excessive laser heating. The samples
27
28 were heated by a temperature control stage with $0.01 \text{ }^\circ\text{C}$ stability (HCP621 V, Instec). Raman peak
29
30 positions were measured with temperature increasing from $20 \text{ }^\circ\text{C}$ to $200 \text{ }^\circ\text{C}$ for both the suspended
31
32 and fused silica supported sample. The pure copper supported flakes were heated up to $160 \text{ }^\circ\text{C}$ to
33
34 avoid copper oxidation. Figure 3 shows that the Raman peak positions of A'_1 and E' modes vary
35
36 with the temperature rise on different substrates. Variations of the peak position at $20 \text{ }^\circ\text{C}$ can be
37
38 seen on different substrates which is attributed to the residual stress during sample preparation.
39
40 However, these variations only affect the bias of the temperature dependent phonon frequency
41
42 curve and do not change the intrinsic and substrate dependent temperature coefficients (see
43
44 Supporting Information V for detailed explanations). The corresponding temperature coefficients
45
46 extracted using linear fitting are listed in Table 1. The effect of thermal stress on the phonon
47
48 frequency shift was confirmed experimentally. The temperature coefficients of the suspended
49
50
51
52
53
54
55
56

1
2
3 MoS₂ flakes were $A^{A_1} = -0.0148 \pm 0.0001 \text{ cm}^{-1}/\text{K}$ and $A^{E'} = -0.0145 \pm 0.0002 \text{ cm}^{-1}/\text{K}$,
4
5 which agrees with previously reported values.^{20,32,37} For the A_1' mode, the temperature coefficient
6
7 changed to $-0.0125 \pm 0.0002 \text{ cm}^{-1}/\text{K}$ when the MoS₂ flakes were transferred to the fused silica
8
9 substrate (see Figures 3(a) and (b)), indicating a compressive thermal stress acting on the flakes
10
11 according to Eqs. (6) and (9). On the pure copper substrate, however, the temperature coefficient
12
13 became $-0.0177 \pm 0.0005 \text{ cm}^{-1}/\text{K}$ due to the tensile thermal stress (see Eqs. (6) and (10)).
14
15 Similar trends were found for the E' mode as well (Table 1). The no-slip condition mentioned
16
17 above was also confirmed through the temperature-dependent Raman measurements, since the
18
19 temperature coefficient highly depends on the TEC of the substrate and no kinks were observed in
20
21 Figure 3 (see Supporting Information Section III for detailed analysis). In addition, it is worth
22
23 noting that the change of temperature coefficients due to the in-plane thermal stress for the E' mode
24
25 was more significant than that for the A_1' mode because the in-plane vibrational mode E' was more
26
27 sensitive to the in-plane perturbation than the out-of-plane vibrational mode A_1' . Using Eq. (11),
28
29 the in-plane TEC of monolayer MoS₂ was $(7.6 \pm 0.9) \times 10^{-6} \text{ 1/K}$ determined from the A_1' mode,
30
31 while using E' mode resulted in $(7.4 \pm 0.5) \times 10^{-6} \text{ 1/K}$. The agreement between these two
32
33 independent calculations demonstrates the consistency of the proposed method. Note that
34
35 measurements from the E' mode had smaller uncertainty because the change of temperature
36
37 coefficients of E' mode is larger than that of A_1' mode (Supporting Information Section VI for
38
39 uncertainty analysis).
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60

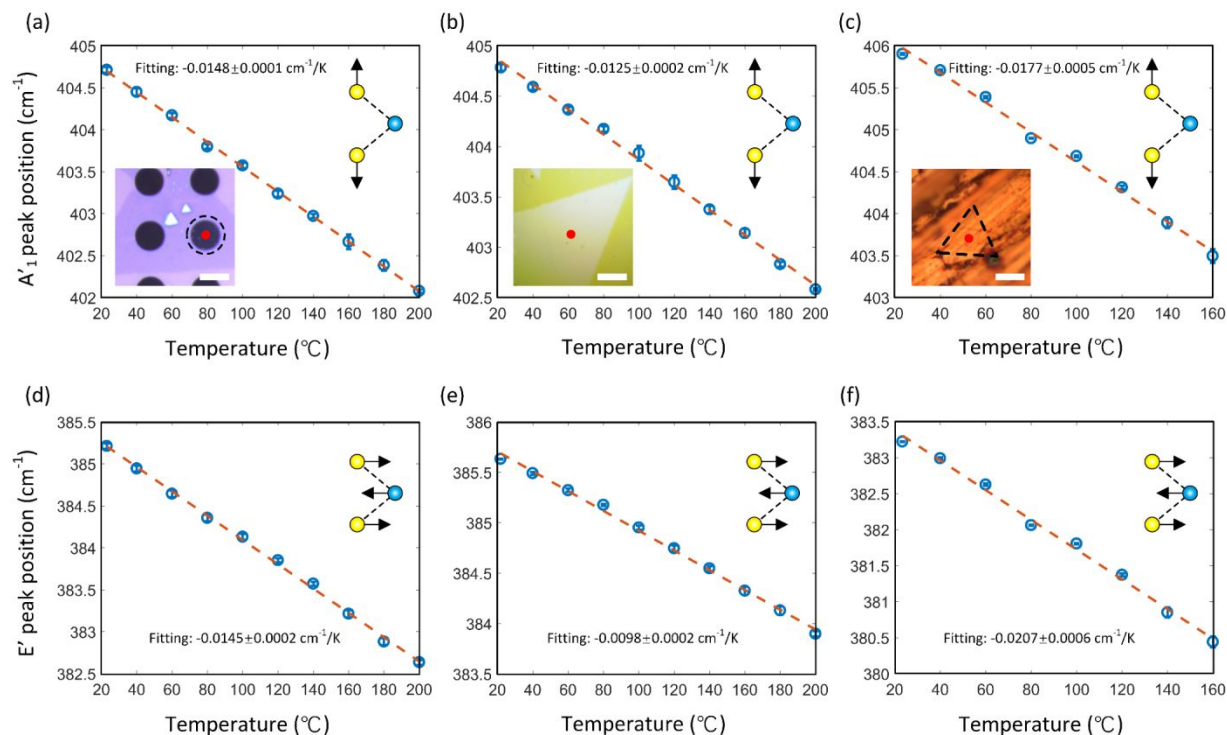


Figure 3 Temperature-dependent Raman measurements for A'_1 and E' modes on different substrates. (a)-(c) Raman peak position of A'_1 mode as a function of temperature on (a) suspended, (b) fused silica supported and (c) pure copper supported monolayer MoS₂ flakes. Inset: schematic of the out-of-plane A'_1 vibrational mode. Inset: 100X magnification optical images the monolayer MoS₂ flakes on three corresponding substrates. Scale bars represent 5 μm . The red dots indicate where the laser excitation was focused. (d)-(e) Raman peak position of E' mode as a function of temperature on (d) suspended, (e) fused silica supported and (f) pure copper supported monolayer MoS₂ flakes. Inset: schematic of the in-plane E' vibrational mode. The y-axis error bars represent random errors from multiple measurements.

Table 1. Temperature coefficients for A'_1 and E' optical phonon modes of single crystalline monolayer MoS₂ flakes on different substrates.

MoS ₂ samples	A^{A_1} (cm ⁻¹ /K)	$A^{E'}$ (cm ⁻¹ /K)
suspended	-0.0148±0.0001	-0.0145±0.0002
fused silica supported	-0.0125±0.0002	-0.0098±0.0002
pure copper supported	-0.0177±0.0005	-0.0207±0.0006
glass supported	-0.0152±0.0004	-0.0151±0.0003

Moreover, we transferred the MoS₂ flakes on a glass substrate which has the TEC ranging from $7.5 \times 10^{-6} \text{ 1/K}$ to $8.5 \times 10^{-6} \text{ 1/K}$,³⁸ very close to the TEC of monolayer MoS₂ measured in this work. Based on the TEC of monolayer MoS₂ reported with our method, the thermal mismatch is minimal in this case. Therefore, we expect the temperature coefficients to be very similar to the one measured on the suspended flakes, which we confirmed with experimental data (row 5 of Table 1). This result further validates our three-substrate method (see Supporting Information Section VII for details of the measurement result and full analysis). We compared our measurement results with literature values listed in Table 2. Previous theoretical calculations used different density functional theory (DFT) methods such as the quasi-harmonic approximation (QHA) method^{12,16,18,39,40} and the symmetry-preserving deformations (SPD) method.¹⁷ As shown in Table 2, the calculated TEC varied from $6.7 \times 10^{-6} \text{ 1/K}$ to $7.3 \times 10^{-6} \text{ 1/K}$ depending on the choice of computation method, which shows excellent agreement with our measurement. The measured TEC of MoS₂ monolayer is larger than the bulk value ($4.9 \times 10^{-6} \text{ 1/K}$) characterized by Murray and Evans⁴¹ due to the absence of the interlayer vdW interaction, which is an agreement with the theoretical prediction by Gan *et al.*¹⁷ However, the unusually high TEC of the MoS₂ monolayer ($64.9 \times 10^{-6} \text{ 1/K}$) reported in Hu *et al.*'s work¹⁸ was not observed in our measurement. Since our approach might be further extended to study the TEC of other thin films or 2D materials

including those belonging to D_{3h} point group and other symmetry groups, we list experimentally measured temperature coefficients by other works for reference (Supporting Information Section VIII).

Table 2. Comparison of the in-plane TEC of monolayer MoS₂ obtained from this work and previous literature presented data.

References	Methods	TECs (10^{-6} 1/K)
Sevik (2014) ¹⁶	DFT-QHA (theoretical)	7.2
Huang <i>et al.</i> (2014) ³⁹	DFT-QHA (theoretical)	7.2
Gan <i>et al.</i> (2016) ¹⁷	DFT-SPD (theoretical)	6.7
Wang <i>et al.</i> (2015) ⁴⁰	DFT-QHA (theoretical)	7.3
This work	Micro-Raman (experimental)	7.6 ± 0.9 (A'_1), 7.4 ± 0.5 (E')

In summary, we proposed an experimental approach to measure the in-plane TEC of 2D materials and demonstrated its application by measuring the monolayer MoS₂ flakes. Based on symmetry analysis, we showed that the TEC can affect the Γ point optical phonon frequency through both the in-plane thermal stress and temperature coefficients due to the contribution of thermal mismatch and free expansion, respectively. We decoupled these two effects using the three-substrate method, where the monolayer flakes were transferred on a holey substrate, fused silica substrate, and pure copper substrate. Temperature-dependent Raman measurements were carried out on all three substrates, and the corresponding temperature coefficients for each mode were characterized. We extracted the in-plane TEC from two different phonon modes, *i.e.*, A'_1 and E' , independently and showed consistent results. The TEC that we measured in this work agrees well

1
2
3 with previously reported values obtained from theoretical or semi-experimental approaches. We
4 demonstrated a useful method for thermal mismatch analysis of MoS₂ based devices. More
5 specifically, our procedure involves: (1) deriving the temperature and stress dependent phonon
6 frequency based on crystal symmetry; (2) obtaining the expression for the TEC of 2D flakes with
7 three carefully chosen substrates; (3) performing temperature-dependent Raman measurement on
8 the three substrates to solve for the coefficients. This is a general framework for TEC measurement
9 that can be applied to many other 2D materials or thin films.
10
11
12
13
14
15
16
17
18
19
20
21
22

23 ASSOCIATED CONTENT

24 25 26 **Supporting Information**

27
28
29 The Supporting Information is available free of charge on the ACS Publications website at DOI:
30
31
32
33
34
35

36 Single crystalline monolayer MoS₂ preparation and characterization, temperature and stress
37 dependent phonon frequency analysis of monolayer MoS₂, micro-Raman spectroscopy
38 experimental setup, uncertainty analysis of experimental results, and temperature-dependent
39 micro-Raman study on the glass substrate
40
41
42
43
44
45
46
47
48

49 AUTHOR INFORMATION

50 51 52 **Corresponding Author**

53
54
55 *E-mail: enwang@mit.edu
56
57
58
59
60

ACKNOWLEDGEMENT

L. Zhang gratefully acknowledges funding support from the MIT/MTL GaN Energy Initiative and the Singapore-MIT Alliance for Research and Technology (SMART) LEES Program. Z. Lu acknowledges funding support from the Air Force Office of Scientific Research with Dr. Ali Sayir as the program manager under Award No. FA9550-15-1-0310.

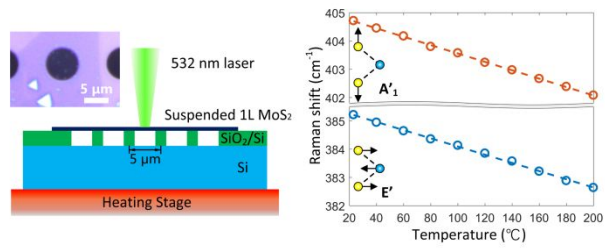
REFERENCES

1. Geim, A. K.; Novoselov, K. S. The Rise of Graphene. *Nat. Mater.* **2007**, *6*, 183
2. Balandin, A. A.; Ghosh, S.; Bao, W.; Calizo, I.; Teweldebrhan, D.; Miao, F.; Lau, C. N. Superior Thermal Conductivity of Single-Layer Graphene. *Nano Lett.* **2008**, *8*, 902-907.
3. Manzeli, S.; Ovchinnikov, D.; Pasquier, D.; Yazyev, O. V.; Kis, A. 2D Transition Metal Dichalcogenides. *Nature Reviews Materials* **2017**, *2*, 17033.
4. Butler, S. Z.; Hollen, S. M.; Cao, L.; Cui, Y.; Gupta, J. A.; Gutiérrez, H. R.; Heinz, T. F.; Hong, S. S.; Huang, J.; Ismach, A. F.; Johnston-Halperin, E.; Kuno, M.; Plashnitsa, V. V.; Robinson, R. D.; Ruoff, R. S.; Salahuddin, S.; Shan, J.; Shi, L.; Spencer, M. G.; Terrones, M.; Windl, W.; Goldberger, J. E. Progress, Challenges, and Opportunities in Two-Dimensional Materials Beyond Graphene. *ACS Nano* **2013**, *7*, 2898-2926.
5. Guo, L.; Wu, M.; Cao, T.; Monahan, D. M.; Lee, Y.-H.; Louie, S. G.; Fleming, G. R. Exchange-Driven Intravalley Mixing of Excitons in Monolayer Transition Metal Dichalcogenides. *Nat. Phys.* **2019**, *15*, 228.
6. Fiori, G.; Bonaccorso, F.; Iannaccone, G.; Palacios, T.; Neumaier, D.; Seabaugh, A.; Banerjee, S. K.; Colombo, L. Electronics Based on Two-Dimensional Materials. *Nat. Nanotechnol.* **2014**, *9*, 768.
7. Wang, Q. H.; Kalantar-Zadeh, K.; Kis, A.; Coleman, J. N.; Strano, M. S. Electronics and Optoelectronics of Two-Dimensional Transition Metal Dichalcogenides. *Nat. Nanotechnol.* **2012**, *7*, 699.
8. Radisavljevic, B.; Radenovic, A.; Brivio, J.; Giacometti, V.; Kis, A. Single-Layer MoS₂ Transistors. *Nat. Nanotechnol.* **2011**, *6*, 147.
9. Han, W.; Kawakami, R. K.; Gmitra, M.; Fabian, J. Graphene Spintronics. *Nat. Nanotechnol.* **2014**, *9*, 794.
10. Das, S.; Prakash, A.; Salazar, R.; Appenzeller, J. Toward Low-Power Electronics: Tunneling Phenomena in Transition Metal Dichalcogenides. *ACS Nano* **2014**, *8*, 1681-1689.
11. Ling, X.; Lin, Y.; Ma, Q.; Wang, Z.; Song, Y.; Yu, L.; Huang, S.; Fang, W.; Zhang, X.; Hsu, A. L. Parallel Stitching of 2D Materials. *Adv. Mater.* **2016**, *28*, 2322-2329.

- 1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60
12. Late, D. J.; Shirodkar, S. N.; Waghmare, U. V.; Dravid, V. P.; Rao, C. Thermal Expansion, Anharmonicity and Temperature-Dependent Raman Spectra of Single- and Few-Layer MoSe₂ and WSe₂. *ChemPhysChem* **2014**, *15*, 1592-1598.
 13. Su, L.; Zhang, Y.; Yu, Y.; Cao, L. Dependence of Coupling of Quasi 2-D MoS₂ with Substrates on Substrate Types, Probed by Temperature Dependent Raman Scattering. *Nanoscale* **2014**, *6*, 4920-4927.
 14. Yan, Z.; Liu, G.; Khan, J. M.; Balandin, A. A. Graphene Quilts for Thermal Management of High-Power GaN Transistors. *Nat. Commun.* **2012**, *3*, 827.
 15. James, J.; Spittle, J.; Brown, S.; Evans, R. A Review of Measurement Techniques for the Thermal Expansion Coefficient of Metals and Alloys at Elevated Temperatures. *Meas. Sci. Technol.* **2001**, *12*, R1.
 16. Sevik, C. Assessment on Lattice Thermal Properties of Two-Dimensional Honeycomb Structures: Graphene, h -BN, h -MoS₂, and h -MoSe₂. *Phys. Rev. B* **2014**, *89*, 035422.
 17. Gan, C. K.; Liu, Y. Y. F. Direct Calculation of the Linear Thermal Expansion Coefficients of MoS₂ via Symmetry-Preserving Deformations. *Phys. Rev. B* **2016**, *94*, 134303.
 18. Hu, X.; Yasaei, P.; Jokisaari, J.; Ögüt, S.; Salehi-Khojin, A.; Klie, R. F. Mapping Thermal Expansion Coefficients in Freestanding 2D Materials at the Nanometer Scale. *Phys. Rev. Lett.* **2018**, *120*, 055902.
 19. Bao, W.; Miao, F.; Chen, Z.; Zhang, H.; Jang, W.; Dames, C.; Lau, C. N. Controlled Ripple Texturing of Suspended Graphene and Ultrathin Graphite Membranes. *Nat. Nanotechnol.* **2009**, *4*, 562.
 20. Yan, R.; Simpson, J. R.; Bertolazzi, S.; Brivio, J.; Watson, M.; Wu, X.; Kis, A.; Luo, T.; Hight Walker, A. R.; Xing, H. G. Thermal Conductivity of Monolayer Molybdenum Disulfide Obtained from Temperature-Dependent Raman Spectroscopy. *ACS Nano* **2014**, *8*, 986-993.
 21. Luo, Z.; Maassen, J.; Deng, Y.; Du, Y.; Garrelts, R. P.; Lundstrom, M. S.; Peide, D. Y.; Xu, X. Anisotropic In-Plane Thermal Conductivity Observed in Few-Layer Black Phosphorus. *Nat. Commun.* **2015**, *6*, 8572.
 22. Luo, Z.; Tian, J.; Huang, S.; Srinivasan, M.; Maassen, J.; Chen, Y. P.; Xu, X. Large Enhancement of Thermal Conductivity and Lorenz Number in Topological Insulator Thin Films. *ACS Nano* **2018**, *12*, 1120-1127.
 23. Cai, W.; Moore, A. L.; Zhu, Y.; Li, X.; Chen, S.; Shi, L.; Ruoff, R. S. Thermal Transport in Suspended and Supported Monolayer Graphene Grown by Chemical Vapor Deposition. *Nano Lett.* **2010**, *10*, 1645-1651.
 24. Yalon, E.; Aslan, Ö. B.; Smithe, K. K. H.; McClellan, C. J.; Suryavanshi, S. V.; Xiong, F.; Sood, A.; Neumann, C. M.; Xu, X.; Goodson, K. E.; Heinz, T. F.; Pop, E. Temperature-Dependent Thermal Boundary Conductance of Monolayer MoS₂ by Raman Thermometry. *ACS Appl. Mater. Interfaces* **2017**, *9*, 43013-43020.
 25. Huang, S.; Liang, L.; Ling, X.; Puzos, A. A.; Geohegan, D. B.; Sumpter, B. G.; Kong, J.; Meunier, V.; Dresselhaus, M. S. Low-Frequency Interlayer Raman Modes to Probe Interface of Twisted Bilayer MoS₂. *Nano Lett.* **2016**, *16*, 1435-1444.
 26. Late, D. J. Temperature Dependent Phonon Shifts in Few-Layer Black Phosphorus. *ACS Appl. Mater. Interfaces* **2015**, *7*, 5857-5862.
 27. Pawbake, A. S.; Island, J. O.; Flores, E.; Ares, J. R.; Sanchez, C.; Ferrer, I. J.; Jadkar, S. R.; van der Zant, H. S. J.; Castellanos-Gomez, A.; Late, D. J. Temperature-Dependent Raman Spectroscopy of Titanium Trisulfide (TiS₃) Nanoribbons and Nanosheets. *ACS Appl. Mater. Interfaces* **2015**, *7*, 24185-24190.

- 1
2
3 28. M, T.; Late, D. J. Temperature Dependent Phonon Shifts in Single-Layer WS₂. *ACS Appl.*
4 *Mater. Interfaces* **2014**, 6, 1158-1163.
- 5 29. Rice, C.; Young, R. J.; Zan, R.; Bangert, U.; Wolverson, D.; Georgiou, T.; Jalil, R.;
6 Novoselov, K. S. Raman-Scattering Measurements and First-Principles Calculations of Strain-
7 Induced Phonon Shifts in Monolayer MoS₂. *Phys. Rev. B* **2013**, 87, 081307.
- 8 30. Yoon, D.; Son, Y.-W.; Cheong, H. Negative Thermal Expansion Coefficient of Graphene
9 Measured by Raman Spectroscopy. *Nano Lett.* **2011**, 11, 3227-3231.
- 10 31. Cai, Y.; Lan, J.; Zhang, G.; Zhang, Y.-W. Lattice Vibrational Modes and Phonon Thermal
11 Conductivity of Monolayer MoS₂. *Phys. Rev. B* **2014**, 89, 035438.
- 12 32. Sahoo, S.; Gaur, A. P. S.; Ahmadi, M.; Guinel, M. J. F.; Katiyar, R. S. Temperature-
13 Dependent Raman Studies and Thermal Conductivity of Few-Layer MoS₂. *J. Phys. Chem. C* **2013**,
14 117, 9042-9047.
- 15 33. Dresselhaus, M. S.; Dresselhaus, G.; Jorio, A., *Group theory: application to the physics of*
16 *condensed matter*; Springer Science & Business Media: 2007.
- 17 34. Bagnall, K. R.; Moore, E. A.; Badescu, S. C.; Zhang, L.; Wang, E. N. Simultaneous
18 Measurement of Temperature, Stress, and Electric Field in GaN HEMTs with Micro-Raman
19 Spectroscopy. *Rev. Sci. Instrum.* **2017**, 88, 113111.
- 20 35. Bertolazzi, S.; Brivio, J.; Kis, A. Stretching and Breaking of Ultrathin MoS₂. *ACS Nano*
21 **2011**, 5, 9703-9709.
- 22 36. Lee, C.; Wei, X.; Kysar, J. W.; Hone, J. Measurement of the Elastic Properties and Intrinsic
23 Strength of Monolayer Graphene. *Science* **2008**, 321, 385-388.
- 24 37. Lanzillo, N. A.; Glen Birdwell, A.; Amani, M.; Crowne, F. J.; Shah, P. B.; Najmaei, S.;
25 Liu, Z.; Ajayan, P. M.; Lou, J.; Dubey, M; Nayak, S. K.; O'Regan, T. P. Temperature-Dependent
26 Phonon Shifts in Monolayer MoS₂. *Appl. Phys. Lett.* **2013**, 103, 093102.
- 27 38. Hidnert, P. Thermal Expansion of Five Selected Optical Glasses. *J. Res. Natl. Bur. Stand.*
28 **1954**, 52, 311.
- 29 39. Huang, L. F.; Gong, P. L.; Zeng, Z. Correlation between Structure, Phonon Spectra,
30 Thermal Expansion, and Thermomechanics of Single-Layer MoS₂. *Phys. Rev. B* **2014**, 90, 045409.
- 31 40. Wang, Z.-Y.; Zhou, Y.-L.; Wang, X.-Q.; Wang, F.; Sun, Q.; Guo, Z.-X.; Jia, Y. Effects of
32 In-Plane Stiffness and Charge Transfer on Thermal Expansion of Monolayer Transition Metal
33 Dichalcogenide. *Chin. Phys. B* **2015**, 24, 026510.
- 34 41. Murray, R.; Evans, B. The Thermal Expansion of 2H-MoS₂ and 2H-WSe₂ between 10 and
35 320 K. *J. Appl. Crystallogr.* **1979**, 12, 312-315.
- 36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60

TOC Graphic



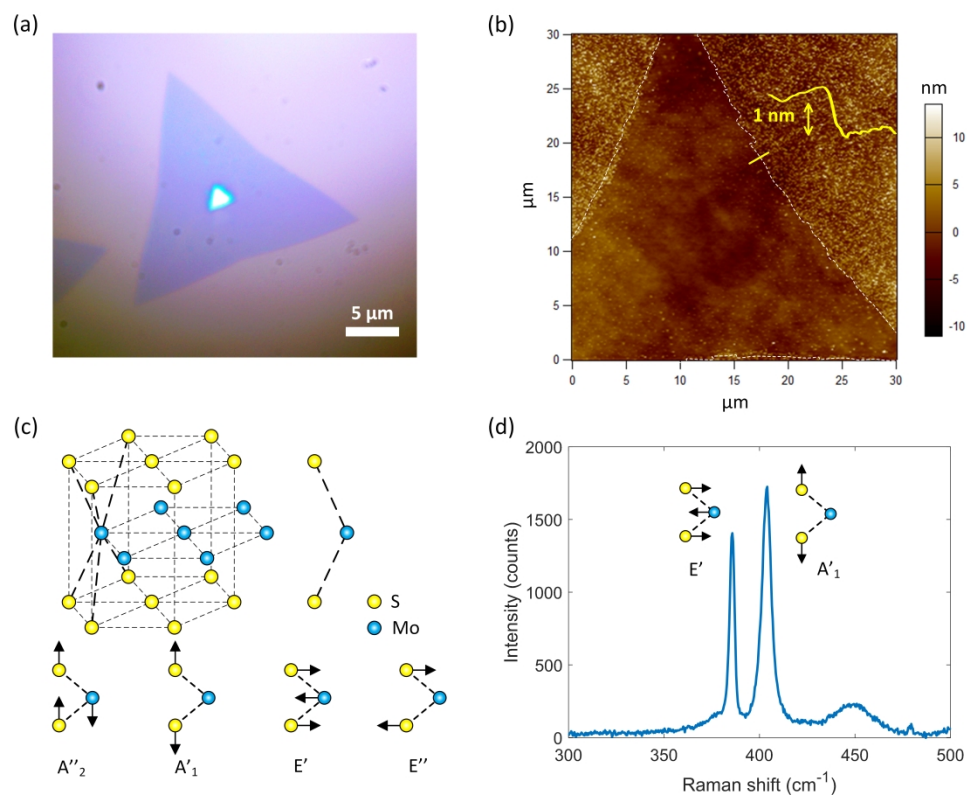


Figure 1

522x413mm (300 x 300 DPI)

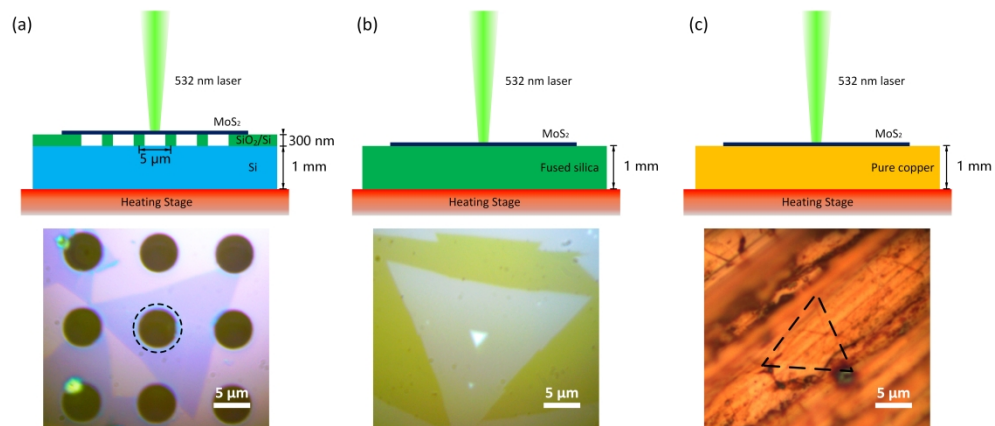


Figure 2

663x279mm (300 x 300 DPI)

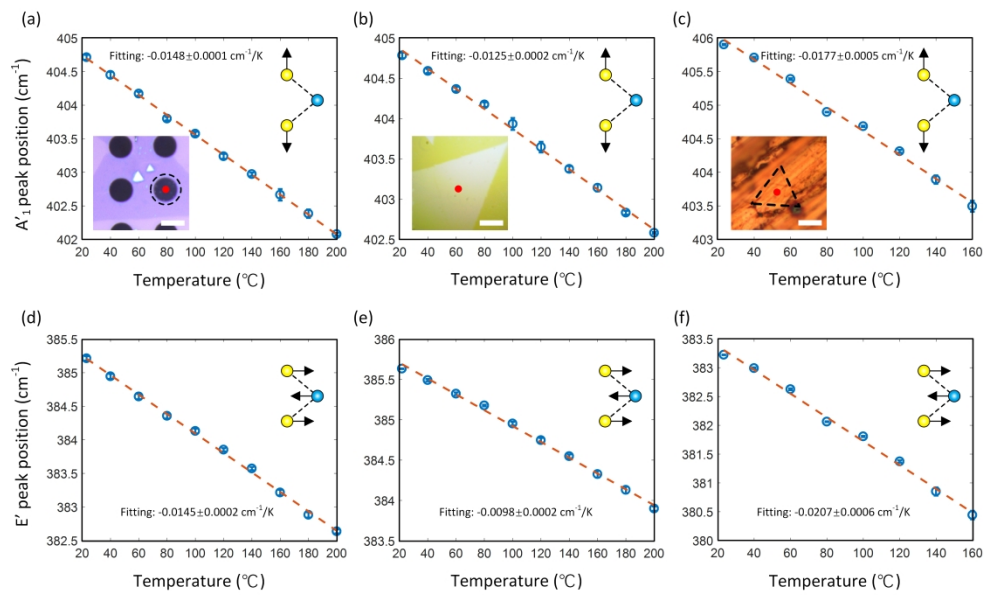
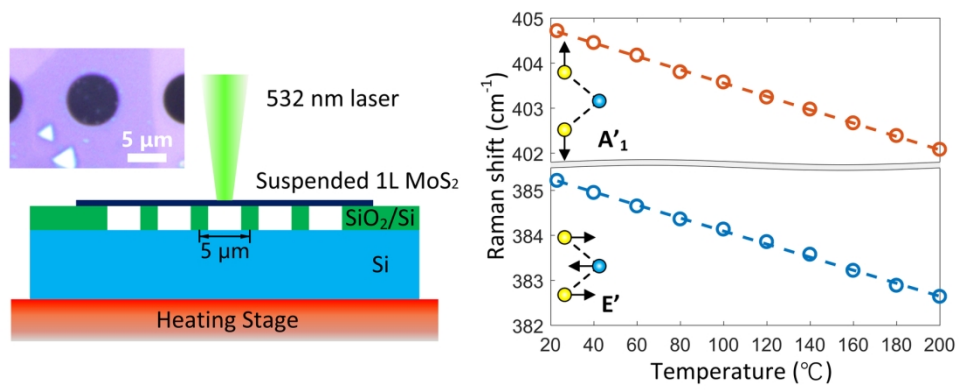


Figure 3

689x412mm (200 x 200 DPI)

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58
59
60



TOC graphic

82x33mm (600 x 600 DPI)