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Sub-hertz optomechanically induced transparency with a kilogram-scale mechanical oscillator

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Optical interferometers with suspended mirrors are the archetype of all current audio-frequency gravitational-wave detectors. The radiation pressure interaction between the motion of the mirrors and the circulating optical field in such interferometers represents a pristine form of light-matter coupling, largely due to 30 years of effort in developing high-quality optical materials with low mechanical dissipation. However, in all current suspended interferometers, the radiation pressure interaction is too weak to be useful as a resource, and too strong to be neglected. Here, we demonstrate a meter-long interferometer with suspended mirrors, of effective mass 125 g, where the radiation pressure interaction is enhanced by strong optical pumping to realize a cooperativity of 50. In conjunction with modest resolved-sideband operation, this regime is efficiently probed via optomechanically induced transparency of a weak on-resonant probe. The low resonant frequency and high- Q of the mechanical oscillator allows us to demonstrate transparency windows barely 100 mHz wide at room temperature. Together with a near-unity ($\approx 99.9\%$) out-coupling efficiency, our system saturates the theoretical delay-bandwidth product, rendering it an optical buffer capable of seconds-long storage times.

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Interferometers with suspended end-mirror cavities are one of today's most sensitive instruments [1]. Suspending the optics isolates them from technical noises of seismic and anthropic origin. Once classical noises are mitigated, the sensitivity of the interferometer increases with the intensity of the optical field circulating within. However, high-power operation is limited by classical and quantum mechanical effects of radiation pressure [2–4]. The longitudinal motion of the suspended end mirror, considered as a harmonic oscillator, is susceptible to two effects arising from the coupling between its motion and the circulating optical field. Classically, a radiation pressure force that depends on the oscillator position—due to feedback from the arm cavity delay—can lead to parametric instability [5,6]. Quantum mechanically, the fluctuations in the number of photons recoiling off of the end mirror—quantum radiation pressure noise—can perturb the oscillator [7–10]. Whilst the former effect can be described as a modification of the susceptibility of the oscillating mirror due to its coupling to the optical field, the latter is a fluctuating force originating from the same coupling. Generally it can be shown that the two effects scale identically with power [11]. This scaling is described by the dimensionless radiation pressure coupling strength, quantified by the *cooperativity* C (to be defined below). At present in the Advanced Laser Interferometer Gravitational-Wave Observatory (LIGO), the radiation pressure coupling between a higher-order mechanical mode and transverse optical mode has been shown to be strong enough ($C \approx 1$) to initiate parametric instability [6],

yet weak enough that quantum radiation pressure noise is buried tantalizingly beneath technical noises [1,12].

Here we demonstrate a suspended-mirror interferometer with a radiation pressure cooperativity an order of magnitude larger ($C \approx 50$) than what has previously been directly observed in such an instrument [5,6,13–15]. In contrast to nanofabricated optomechanical systems [16,17], our system consists of a mechanical oscillator of effective mass 125 g—9 orders of magnitude more massive—susceptible to the recoil-type radiation pressure coupling, and an interferometer that is formed by a 1 m long suspended cavity, both of which make it a mock-up of an Advanced LIGO arm. This system serves as a general experimental platform for audio-band optomechanics in a radiation-pressure-dominated regime [5,14,15].

The basic challenge of operating such an interferometer in the high-cooperativity regime is the ability to store enough photons in the cavity to amplify the radiation pressure force without destabilizing it by other means. In order to retain sufficient photons in the cavity with practical input laser powers, it is necessary that the end-mirror optical losses—already at a state-of-the-art level of a few ppm—be diluted by elongating the cavity. Operating a long cavity with suspended mirrors introduces additional challenges that must be overcome. In particular, maintaining alignment requires seismic isolation whose fundamental suspension mode is low frequency. Thermal noise requirements demand the suspending fibers be thin. Thus, the suspensions are necessarily “soft”, and their torsional modes are susceptible to a radiation-pressure torque instability [18,19]—an effect that has been a limiting factor in the high-power operation of suspended interferometers [20–22]. On the one hand, the magnitude of the resonant round-trip gain for the

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radiation-pressure-induced longitudinal coupling between cavity frequency and length is the cooperativity

$$C \equiv \frac{4g^2}{\kappa\Gamma_m}, \quad (1)$$

where $g = (\partial\omega_c/\partial x)\sqrt{\hbar n_c/(2m\Omega_m)}$ is the optomechanical coupling rate for an end mirror of effective mass m , oscillating at frequency Ω_m , which leads to a cavity frequency fluctuation $\partial\omega_c/\partial x = \omega_c/L$ for a cavity of length L , loaded with n_c photons on average. On the other hand, the gain for the torque coupling scales as $\kappa n_c L/M$, where M is the moment of inertia [19]. The ratio of the round-trip gains of the two processes (longitudinal and torsional radiation pressure) scale as $m^{-2}L^{-3}$ —heavier mirrors reduce the susceptibility to radiation pressure force, while longer cavities enhance the effect of radiation pressure torque.

The competing demands of being radiation-pressure-dominated longitudinally while still maintaining angular stability are met in our experimental system, depicted in Fig. 1. The optical cavity of interest is formed by two mirrors: an end mirror (EM) weighing 1 g with a transmission of 3 ppm, and an input mirror (IM) weighing 250 g with a transmission 800 ppm—suspended on 1 Hz pendulums placed 1 m apart. To suppress extraneous beam-pointing noise, the experiment is mounted on an actively damped seismic vibration isolation platform, similar to the one used in Advanced LIGO [23], which attenuates ground motion to a level of $\approx 10^{-9}$ m/ $\sqrt{\text{Hz}}$ above a few Hz. The cavity is driven by laser light from a master-oscillator power amplifier (MOPA) capable of delivering 10 W of continuous output at 1064 nm [24]. Extraneous power fluctuations are reduced to a relative intensity noise of $\approx 10^{-8}/\sqrt{\text{Hz}}$ above 100 Hz; this, together with carefully centering of the beam position on the mirrors (by minimizing the transduction of the suspension pitch mode onto the phase of the light leaking out of the cavity), reduces torque fluctuations to insignificant levels. The laser is frequency-stabilized to an independent reference cavity. In this configuration, optical torque instabilities are not expected to limit high-power operation, and it should be possible to realize $C \gtrsim 100$.

Exploiting the slew of technical capabilities originally developed for LIGO, we observe optomechanically induced transparency (OMIT) [25–29] due to the coupling between the drumhead mode of the IM [see Fig. 1(b)] and the intracavity field. Modulating the incident laser at a variable frequency offset Ω from its carrier creates an intracavity radiation pressure at the same frequency. When $\Omega = \Omega_m \approx 2\pi \times 27$ kHz, the drumhead mode is resonantly excited by this intracavity radiation pressure force; this displacement gets transduced as phase-modulation sidebands back on the intracavity field, which can interfere with the injected modulation sideband. When the carrier is detuned from the cavity resonance by the mechanical frequency (i.e., $\Delta = \Omega_m$), the interference is perfectly destructive.

In the experiment we probe the cavity response from within the feedback loop used to stabilize its length. First, we acquire lock of the cavity length to the laser by using a Pound-Drever-Hall signal in reflection [see Fig. 1(a)]; we then hand over the length control from the reflection signal to the transmission signal in order to be able to red-detune by $\Delta = -\Omega_m$. The cavity response is then probed by frequency-modulation

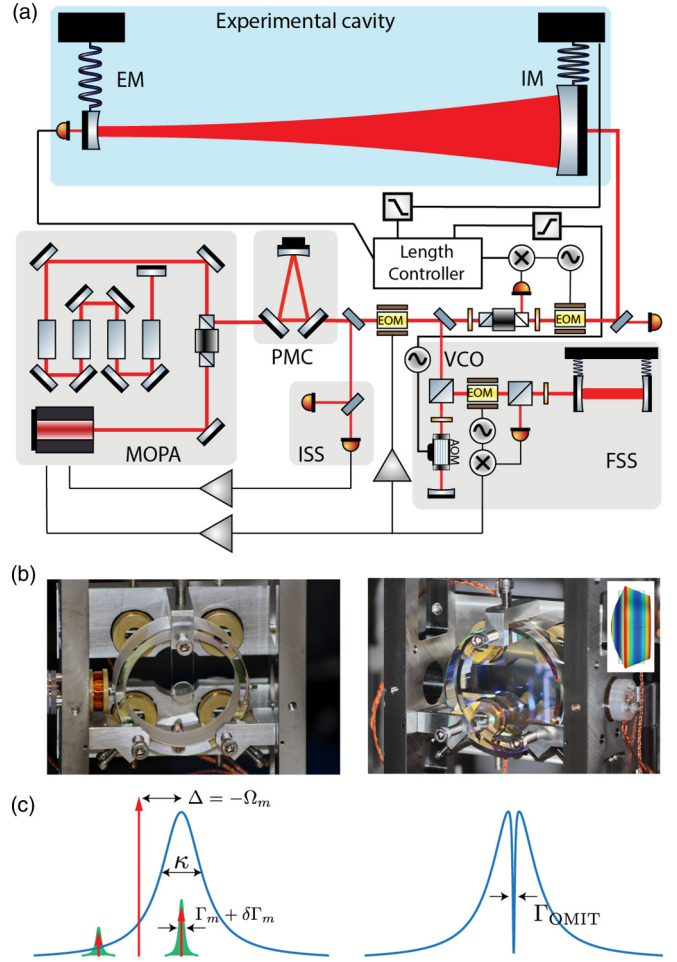


FIG. 1. Experimental system and schematic. (a) Laser light for the experiment is derived from a master-oscillator power amplifier (MOPA) that was developed for Initial LIGO. The 10 W output, at 1064 nm, is spatially filtered by a pre-mode cleaner (PMC); subsequently, its intensity (ISS) and frequency (FSS) are stabilized using respective servos. The light then enters the experimental cavity, whose reflection and transmission are monitored and used for stabilizing the laser-cavity detuning. (b) Left: Picture of the end mirror (EM), consisting of a 1.27 cm diameter mirror, weighing 1 g, suspended as a double pendulum. Right: Picture of the input mirror (IM), consisting of a 7.3 cm diameter mirror, weighing 250 g, suspended as a single pendulum. Inset shows finite-element model of the mirror's fundamental drumhead mode, which is the mechanical oscillator relevant to this work. (c) Simple scheme of optomechanically induced transparency (OMIT). Left shows the bare cavity response (blue), pumped by laser light red-detuned by a mechanical linewidth ($\Delta = -\Omega_m$), and its two sidebands filtered by the cavity; the radiation-pressure-induced displacement is transduced as additional sidebands (green), which interferes with the injected sidebands. Right shows the resulting effective cavity response.

sidebands generated by dithering the frequency servo error point, and demodulating the signal out of the photodetector in transmission. We verify the detuning by fits to the broadband response of the cavity (see Appendix B). Finally, we measure the response in the vicinity of the cavity resonance in a high-resolution scan to observe the narrow OMIT feature. However, the response observed in this manner needs to be

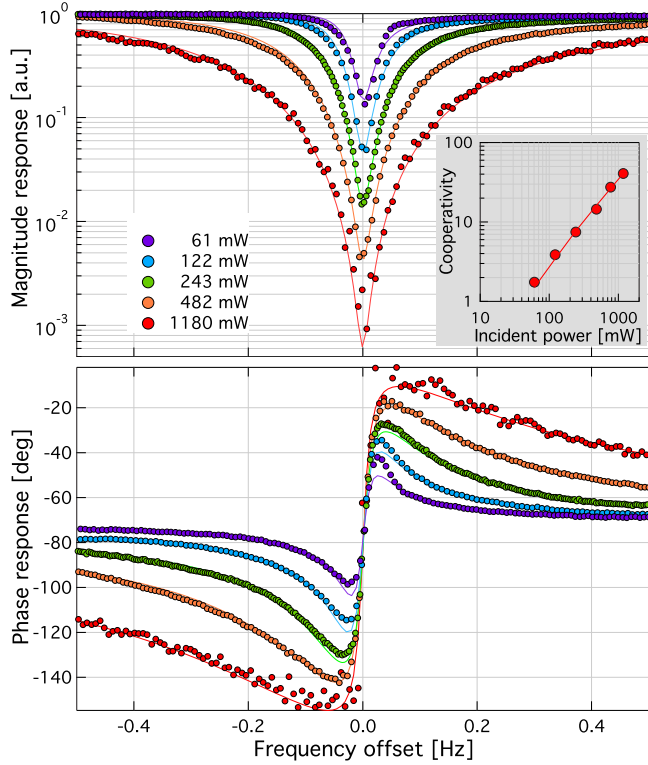


FIG. 2. Sub-hertz optomechanically induced transparency: main figure shows zoom-in of the magnitude (top) and phase response (bottom) of the cavity transmission in a 1 Hz span around resonance at several values of the incident power (legend). Solid lines show model curves. Inset shows the optomechanical cooperativity inferred from the model.

corrected for the response of the frequency stabilization loop through which both the probe and the measurement are made (see Appendix B for details). Figure 2 shows the magnitude and phase of this corrected response as the power in the incident laser is increased. The gross features of the cavity transmission can be understood from the approximate model,

$$T[\Omega] \approx T_0[\Omega] \left(1 - \frac{\delta\Gamma_m/2}{(\Gamma_m + \delta\Gamma_m)/2 + i(\Omega_m - \Omega)} \right), \quad (2)$$

where $T_0[\Omega]$ is the cavity transmission without any optomechanical coupling, and $\delta\Gamma_m \approx \Gamma_m C_{\text{eff}}$, is the optically damped contribution to the mechanical decay rate; here $C_{\text{eff}} = C/[1 + (\kappa/4\Omega_m)^2]$ is the effective cooperativity taking into account the finite sideband resolution $\Omega_m/\kappa \approx 1.4$, which gives, $C_{\text{eff}} \approx 0.97C$. The bare cavity transmission T_0 is a Lorentzian of width κ , while the second factor describes an OMIT window of width given by the effective mechanical linewidth, on cavity resonance. As the cooperativity increases, $T[\Omega_m]/T_0[\Omega_m] \approx 1/(1 + C_{\text{eff}}) \rightarrow 0$. The expression in Eq. (2) is, however, an approximation that disregards the finite sideband resolution; in fact, it only describes the contribution to the transmitted photodetector signal that arises from the upper sideband of the intracavity field. A full model accounting for both sidebands is shown as the fits in Fig. 2 (see Appendix A for the full model). These fits allow us to extract the cooperativity, shown as the inset in the figure. At

the highest incident power of 1.2 W, we realize $C \approx 50$ (see inset of Fig. 2).

Our results demonstrate the narrowest OMIT windows yet observed of $\Gamma_{\text{OMIT}}/2\pi \lesssim 100$ mHz (a recent experiment at dilution refrigerator temperature is comparable [30]). This is largely due to the ability to operate an optomechanical system in the high-cooperativity regime using a mechanical oscillator with a long decay time. We achieve this by using a low-frequency oscillator featuring a high intrinsic mechanical quality factor of $Q_m = \Omega_m/\Gamma_m \approx 10^6$, consistent with expectations for bulk fused silica [31,32].

The sub-hertz OMIT feature is beneficial for various applications ranging from frequency-agile ultra-narrow filter cavities [33], to coherent frequency converters [34,35], to slow-light optical buffers [36] and quantum memories. In the following we discuss the potential of our system as a highly efficient slow-light buffer capable of seconds-long delays.

An optical buffer for coherent classical signals is characterized by the maximum possible delay that it can provide, and the usable bandwidth; they are not independent for passive systems, and in fact the delay-bandwidth product (DBP) is bounded [36–40]. Further, if the buffer also features a near-unity storage and retrieval efficiency, it may be used to store weak incoherent classical signals. In the limit that the signal is encoded in a pure quantum state—as required for various quantum information processing tasks—the optical buffer becomes a quantum memory [41,42], if in addition to the above requirements, it also features a coherence time longer than the storage time.

In the case of OMIT, the group delay, $\tau = (-\partial\phi[\Omega]/\partial\Omega)_{\Omega=\Omega_m}$, where ϕ is the phase response, is explicitly given by

$$\tau = \frac{2C_{\text{eff}}}{\Gamma_{\text{OMIT}}} \times \begin{cases} -1, & \text{transmission,} \\ \frac{\eta_R}{1-\eta_R+C_{\text{eff}}}, & \text{reflection.} \end{cases} \quad (3)$$

It is negative (advance) or positive (delay) depending on whether the signal sideband is transmitted or reflected [26,27,43]. Note that $\eta_R = \kappa_1/\kappa \approx 0.999$ is the efficiency of the reflection port, given by the fractional contribution of the input-mirror decay rate κ_1 to the total cavity decay rate. From the measured phase response, we are able to extract the delay in transmission and reflection, shown in the inset of Fig. 3. The inferred absolute delays, in the range of several (tens of) seconds, are more than an order of magnitude larger than what has previously been demonstrated using an optomechanical system [43], and approaching what has been demonstrated using atomic EIT [44]. Further, the signal efficiency in our system is near-ideal ($\eta_R \approx 0.999$), largely due to the pristine optical quality, and significantly exceeds prior demonstrations of OMIT and even atomic EIT [45], to the best of our knowledge. Finally, the combination of long delays, and near-ideal coupling efficiency, allows for a delay-bandwidth product (DBP) that is very large. From Eq. (3), the DBP is given by

$$\text{DBP} = \tau\Gamma_{\text{OMIT}} = 2C_{\text{eff}} \times \begin{cases} -1, & \text{transmission,} \\ \frac{\eta_R}{1-\eta_R+C_{\text{eff}}}, & \text{reflection.} \end{cases} \quad (4)$$

The DBP takes a maximum value of 2 for readout in reflection. Figure 3 shows that our system saturates this upper

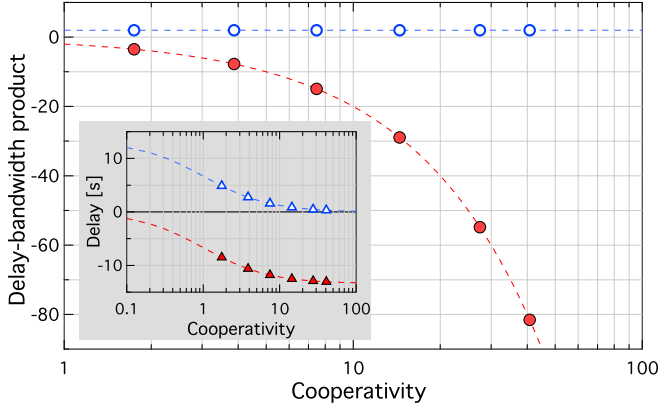


FIG. 3. Plot shows delay-bandwidth product in transmission (red) and reflection (blue); dashed lines show models based on Eq. (4). Inset shows the delay in transmission (red) and reflection (blue), with dashed lines showing models based on Eq. (3).

bound, which is also comparable with what is in principle achievable with atomic EIT systems [36,37].

The potential of our system as a quantum memory is currently limited by the decoherence time of the mechanical mode ($\approx 0.2 \mu\text{s}$), and the associated thermal noise. Recent work has demonstrated record low-noise quantum memory using an intracavity Raman medium to suppress nonlinear mixing processes [46], however, at the expense of efficiency. In principle, optomechanical systems with macroscopic oscillators and low-loss mirrors can be free of optical and mechanical nonlinearities—respectively of the Duffing and thermal types—while preserving optical efficiency. With further improvements employing recently demonstrated techniques for mechanical Q enhancement [47,48], it is conceivable that the regime of quantum coherent mechanical oscillation ($Q \gtrsim n_{\text{th}}$, where n_{th} is the average thermal phonon occupation of the oscillator) can be achieved even in a suspended-optic interferometer. In conjunction with adiabatically varying the pump amplitude [49,50], a long-lived on-demand OMIT-based quantum memory may be realized.

The ability to realize an optically tunable nearly lossless dispersive element that shares the same footprint and technology of the LIGO interferometer makes our system intriguing for other applications in LIGO that do not rely on thermal noise reduction to the few-quantum level. For example, a tunable signal-recycling cavity—which determines the broadband response of the interferometer and is at present fixed by choice of mirror transmissivity—could be realized that can be used to dynamically track astrophysical signals as they transit the detection band.

Ultimately, the combination of high cooperativity and ideal out-coupling efficiency are also the same requirements for using radiation pressure quantum fluctuations as a useful metrological resource in an interferometer [51]. At the moment, the cooperativity we achieve is limited by a new source of angular instability. Our observations are consistent with the conjecture that surface roughness on the cavity mirror leads to scattering of the cavity's fundamental mode into a few higher-order modes, which causes radiation pressure torques. With mitigation of this problem we expect the current system to be a

test bed for studying and reducing the effects of quantum noise on a suspended interferometer with macroscopic test masses.

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APPENDIX A: THEORETICAL MODEL FOR OMIT

In the following we recapitulate the model used to interpret the OMIT data presented in Fig. 2 of the main manuscript. The presentation largely follows the standard treatment adopted in the cavity optomechanics community [26,27].

The basic optomechanical Hamiltonian that describes the radiation pressure interaction between the cavity field (a), end-mirror displacement (x), and the driving laser field (a_{in}) is [17]

$$H = \hbar(\omega_c - Gx)a^\dagger a + \left(\frac{p^2}{2m} + \frac{m\Omega_m^2 x^2}{2} \right) + i\hbar\sqrt{\kappa_1}(a_{\text{in}}(t)a^\dagger - a_{\text{in}}^*(t)a), \quad (\text{A1})$$

where

ω_c	bare cavity resonance frequency
G	bare optomechanical coupling strength $G \equiv \partial\omega_c/\partial x = \omega_c/L_c$
x, p	displacement and momentum of the oscillator
m	effective mass of oscillator
Ω_m	frequency of oscillator
a_{in}	input laser field (in units of $\sqrt{\text{photons/s}}$)
$\kappa_{1,E}$	cavity loss rate through IM/EM $\kappa_{1,E} = \frac{c}{4L_c} T_{1,E}; T_{1,E}$ —IM/EM transmission

The Heisenberg equations that follow from Eq. (A1) are

$$\begin{aligned} \frac{da}{dt} &= \left(i\omega_c - \frac{\kappa}{2} \right) a - iGxa + \sqrt{\kappa_1}a_{\text{in}}, \\ \frac{dx}{dt} &= \frac{p}{m}, \\ \frac{dp}{dt} &= -m\Omega_m^2 x - \Gamma_m p - \hbar Ga^\dagger a, \end{aligned} \quad (\text{A2})$$

where Γ_m is the mechanical decay rate, and $\kappa = \kappa_E + \kappa_{\text{int}} + \kappa_1$ is the total loss rate of the cavity including from the EM, any internal loss, and the IM. Note that since the mechanical oscillator is high Q ($Q_m \approx 10^6$), and since we are only interested in its response near resonance, we have adopted a velocity-damped model for its loss. Further, since we are interested in the driven response of the system, optical and mechanical input noises are omitted.

The input field that drives the cavity (a_{in}) is derived from a laser oscillating at ω_ℓ with sidebands δa_{in} imprinted on it; it is

thus described by

$$a_{\text{in}}(t) = [(\bar{a}_{\text{in}} + \delta a_{\text{in}}(t))e^{-i\omega_\ell t}]. \quad (\text{A3})$$

When Eq. (A3) is substituted into the equation of motion in Eq. (A2), we arrive at a set of coupled nonlinear equations that describe the full radiation pressure optomechanical dynamics which features a static optical bistability and static spring shifts of the mechanical oscillator. In the regime where the carrier flux is fixed and much larger than the sideband, i.e., $|\bar{a}_{\text{in}}| \gg |\delta a_{\text{in}}|$, these equations can be linearized about a given operating point. These linearized equations, expressed in the frame rotating at the laser frequency ω_ℓ , take the form

$$\left(\frac{d}{dt} - i\bar{\Delta} + \frac{\kappa}{2}\right)\delta a = -iG\bar{a}\delta x + \sqrt{\kappa_1}\delta a_{\text{in}},$$

$$m\left(\frac{d^2}{dt^2} + \Gamma_m\frac{d}{dt} + \Omega_m^2\right)\delta x = -\hbar G\bar{a}(\delta a + \delta a^\dagger). \quad (\text{A4})$$

Here, we have defined an effective detuning,

$$\bar{\Delta} = (\omega_\ell - \omega_c) - G\bar{x},$$

that contains the bare laser-cavity detuning (first term) and a term due to the static cavity frequency shift from radiation pressure coupling; \bar{x} is the static mirror displacement, while

$$\bar{a} = \frac{\sqrt{\kappa_1}\bar{a}_{\text{in}}}{-i\bar{\Delta} + \kappa/2} \quad (\text{A5})$$

is the mean intracavity field amplitude; and $\delta x, \delta a$ are the fluctuations on top of these mean values. [Note that we have omitted the phase of the intracavity field in Eq. (A4) with the understanding that it is a constant offset from the phase of the input laser for fixed detuning.] It is convenient to express Eq. (A5) in terms of the incident power, $P_{\text{in}} = \hbar\omega_\ell|\bar{a}_{\text{in}}|^2$, and the mean intracavity photon number, $n_c = |\bar{a}|^2$, as

$$n_c = \frac{4\eta_1}{\kappa} \frac{P_{\text{in}}/\hbar\omega_\ell}{1 + (2\bar{\Delta}/\kappa)^2}, \quad (\text{A6})$$

where we have defined $\eta_1 = \kappa_1/\kappa$, the cavity coupling efficiency from the incident port. Henceforth we will redefine $\bar{\Delta} \mapsto \Delta$ for notational convenience; further, we take \bar{a} to be real by absorbing its (frequency-independent) phase, $\tan^{-1}(2\Delta/\kappa)$, into the input, with the understanding that such static phase shifts are irrelevant in our measurement.

The OMIT phenomenon entails a modification of the cavity response via its radiation pressure interaction with the end mirror. In the experiment, we measure the magnitude and phase of this modified response at frequency offsets Ω from the incident pump laser, using probe sidebands at these frequencies, described by

$$\delta a_{\text{in}}(t) = \delta A_{\text{in}}^+ e^{-i\Omega t} + \delta A_{\text{in}}^- e^{i\Omega t}, \quad (\text{A7})$$

where δA_{in}^\pm are the amplitudes of the upper and lower sideband, respectively; since the sidebands are imprinted by phase modulation,

$$\delta A_{\text{in}}^- = -\delta A_{\text{in}}^+ = -(\delta A_{\text{in}}^+)^* = (\delta A_{\text{in}}^-)^*. \quad (\text{A8})$$

Such a drive produces intracavity fields and oscillator displacements at the same frequency since the equations of

motion in Eq. (A4) are linear. In order to track these we introduce the ansatz

$$\delta a = \delta A^+ e^{-i\Omega t} + \delta A^- e^{i\Omega t}, \quad \delta x = \delta X e^{-i\Omega t} + \delta X^* e^{i\Omega t}, \quad (\text{A9})$$

into Eq. (A4), and separate out terms oscillating at the two sideband frequencies; this gives the closed set of coupled equations:

$$\chi_c^{-1}[\Omega + \Delta]\delta A^+ = -iG\bar{a}\delta X + \sqrt{\kappa_1}\delta A_{\text{in}}^+,$$

$$\chi_c^{-1}[\Omega - \Delta](\delta A^-)^* = +iG\bar{a}\delta X + \sqrt{\kappa_1}(\delta A_{\text{in}}^-)^*,$$

$$2m\Omega_m\chi_m^{-1}[\Omega - \Omega_m]\delta X = -i\hbar G\bar{a}[\delta A^+ + (\delta A^-)^*], \quad (\text{A10})$$

where we have defined the optical and mechanical susceptibilities,

$$\chi_c^{-1}[\Omega] = \frac{\kappa}{2} - i\Omega, \quad \chi_m^{-1}[\Omega] = \frac{\Gamma_m}{2} - i\Omega. \quad (\text{A11})$$

Note that in going to Eq. (A10), we have approximated the mechanical susceptibility using a single-pole response,

$$m(\Omega_m^2 - \Omega^2 - i\Omega\Gamma_m) = m[(\Omega_m - \Omega)(\Omega_m + \Omega) - i\Omega\Gamma_m]$$

$$\approx m(-2i\Omega_m)\left(\frac{\Gamma_m}{2} + i(\Omega_m - \Omega)\right),$$

which is effectively a rotating-wave approximation valid in the high- Q limit, $Q_m = \Omega_m/\Gamma_m \gg 1$.

Solving Eq. (A10) for the mechanical motion excited by the intracavity field,

$$2m\Omega_m\chi_{m,\text{eff}}^{-1}[\Omega]\delta X$$

$$= -i\hbar G\bar{a}\sqrt{\kappa_1}[\chi_c[\Omega + \Delta]\delta A_{\text{in}}^+ + \chi_c[\Omega - \Delta](\delta A_{\text{in}}^-)^*], \quad (\text{A12})$$

where the effective mechanical susceptibility,

$$\chi_{m,\text{eff}}^{-1}[\Omega] = \chi_m^{-1}[\Omega - \Omega_m] + g^2(\chi_c[\Omega + \Delta] - \chi_c[\Omega - \Delta]), \quad (\text{A13})$$

describes the radiation pressure modification of the mechanical response, whose strength scales with the optomechanical coupling rate, $g = G\bar{a}\sqrt{\hbar/2m\Omega_m}$. When optomechanical coupling is weak enough to not lead to normal-mode splitting (i.e., when $g \lesssim \kappa$), the effective mechanical susceptibility can be approximated in terms of a modified mechanical linewidth (optical damping) and resonance frequency (optical spring), viz.,

$$\chi_{m,\text{eff}}^{-1}[\Omega - (\Omega_m + \delta\Omega_m)] \equiv \frac{\Gamma_m + \delta\Gamma_m}{2} - i[\Omega - (\Omega_m + \delta\Omega_m)],$$

where $\delta\Gamma_m$ and $\delta\Omega_m$ are identified by separating the real and imaginary parts of the second term in Eq. (A13). We are interested in these expressions for the case of red-sideband pumping, i.e., $\Delta = -\Omega_m$; in this case,

$$\frac{\delta\Gamma_m}{\Gamma_m} = C \frac{(4\Omega_m/\kappa)^2}{1 + (4\Omega_m/\kappa)^2}, \quad \frac{\delta\Omega_m}{\Omega_m} = \frac{2C}{Q_m} \frac{4\Omega_m/\kappa}{1 + (4\Omega_m/\kappa)^2}, \quad (\text{A14})$$

where

$$C \equiv \frac{4g^2}{\kappa\Gamma_m} \quad (\text{A15})$$

is the optomechanical cooperativity, which quantifies the fractional effect of the radiation-pressure modification of the mechanical susceptibility. Note that in our case, characterized by $Q_m > C > 1$, the optical spring is weak for red-sideband pumping, and we henceforth neglect $\delta\Omega_m$. The oscillator response is thus described by $\chi_{m,\text{eff}}[\Omega - \Omega_m]$ featuring a modified linewidth.

The effect of the modified oscillator is to scatter phase-modulation sidebands on the intracavity field, which can then interfere with the sidebands already present from the modulation imprinted on the incident field. The resulting intracavity field can be obtained by inserting Eq. (A12) back into Eq. (A10) and solving for δA^\pm , viz.,

$$\delta A^\pm = \sqrt{\kappa_1} \chi_c[\Omega \pm \Delta] \delta A_{\text{in}}^\pm \times \begin{cases} K[\Omega - \Omega_m] \\ K^*[\Omega - \Omega_m], \end{cases} \quad (\text{A16})$$

where

$$K[\Omega] \equiv \frac{\chi_m^{-1}[\Omega]}{\chi_{m,\text{eff}}^{-1}[\Omega]} \approx 1 - \frac{\delta\Gamma_m}{(\Gamma_m + \delta\Gamma_m) - 2i\Omega}. \quad (\text{A17})$$

In writing these expressions, we have used the fact that the input laser is phase-modulated. Note that in the absence of optomechanical coupling (i.e., $g = 0$), $\chi_{m,\text{eff}} = \chi_m$, and Eq. (A16) simply describes the cavity response χ_c filtering the incident field. The effect of optomechanical coupling is captured by the factor $K[\Omega]$ —featuring the shape of the modified mechanical susceptibility—which is superimposed on top of the (relatively) slowly varying cavity response. It is this superimposed feature that manifests as an optomechanically induced transparency window. Note that as the optomechanical coupling is increased by strong pumping, $\delta\Gamma_m \gg \Gamma_m$, we have on resonance, $K[\Omega - \Omega_m]|_{\Omega \rightarrow \Omega_m} \rightarrow 0$, leading to complete transparency.

The experimentally observed fields are the ones leaking out of the cavity, either in transmission or in reflection. The transmitted and reflected fields are [52]

$$a_{\text{out},T}(t) = \sqrt{\kappa_E} a(t), \quad a_{\text{out},R}(t) = a_{\text{in}} - \sqrt{\kappa_1} a(t), \quad (\text{A18})$$

where $a(t) = |\bar{a}| + \delta a(t)$ is the intracavity field in the rotating frame of the input laser. In the following we focus on the transmitted field, with the understanding that the reflected field can be computed similarly. Using Eqs. (A5), (A8), and (A16) in Eq. (A18), the transmitted field is

$$\begin{aligned} a_{\text{out},T}(t) = & \sqrt{\kappa_E \kappa_1} \bar{a}_{\text{in}} (\chi_c[\Delta] \\ & + \chi_c[\Omega + \Delta] K[\Omega - \Omega_m] e^{-i\Omega t} \beta \\ & - \chi_c[\Omega - \Delta] K^*[\Omega - \Omega_m] e^{+i\Omega t} \beta), \end{aligned} \quad (\text{A19})$$

where $\beta \equiv \delta A_{\text{in}}^+ / \bar{a}_{\text{in}}$ is the modulation index. The first term in parentheses describes the portion of the input pump that is transmitted, while the second and third terms describe the upper and lower sidebands, respectively. Equation (2) of the main text is just the second term, describing the transmission of the upper sideband alone. However, due to the finite sideband resolution of our system, a sizable fraction,

$|\chi_c[\Omega - \Delta] / \chi_c[\Omega + \Delta]|$, of the lower sideband is also transmitted. In our experiment, where the pump is red-detuned ($\Delta = -\Omega_m$) and at Fourier frequencies close to mechanical resonance ($\Omega = \Omega_m$), this ratio is $(\kappa/4\Omega_m)^2 \approx 3.8\%$.

When the transmitted field is detected on a photodetector, the detector output voltage is $V_T(t) \propto |a_{\text{out},T}(t)|^2$; in the experiment we detect the voltage that is phase-coherent with the input modulation. We are thus interested in the in-phase and quadrature-phase components of the voltage oscillating at Ω . This oscillating component is

$$\begin{aligned} \delta V_{\text{out},T}(t) & \propto \sqrt{\kappa_E \kappa_1} \text{Re}(\chi_c[\Omega + \Delta] K[\Omega - \Omega_m] e^{-i\Omega t} \\ & - \chi_c[\Omega - \Delta] K^*[\Omega - \Omega_m] e^{+i\Omega t}) \\ & \equiv \delta V_{\text{out},T}^I[\Omega] \cos(\Omega t) + \delta V_{\text{out},T}^Q[\Omega] \sin(\Omega t). \end{aligned} \quad (\text{A20})$$

Note that here we have omitted the phase of $\chi_c[\Delta]$ which is a frequency-independent phase offset. The final line in Eq. (A20) implicitly separates out the in-phase and quadrature-phase components of the photodetector signal measured by the network analyzer; the complex response—the measured cavity transmission coefficient—is then $T[\Omega] \equiv \delta V_{\text{out},T}^I[\Omega] + i\delta V_{\text{out},T}^Q[\Omega]$. Explicitly computing this gives

$$T[\Omega] = \sqrt{\kappa_E \kappa_1} (\chi_c[\Omega + \Delta] - \chi_c^*[\Omega - \Delta]) K[\Omega - \Omega_m], \quad (\text{A21})$$

which can be understood as the upper sideband contribution diminished by the undesired lower sideband transmitted by the cavity. This is the full model used to fit the data in the main text. The reflection coefficient $R[\Omega]$ can be calculated in a similar fashion.

1. Delay, bandwidth, and their product

Both cavity outputs, transmission and reflection, feature the conventional cavity response χ_c on top of which is superimposed the OMIT feature described by $K[\Omega]$. The former varies in frequency over a scale given by the cavity FWHM κ , while the latter varies within a much smaller interval, which can be read off from Eq. (A17) to be the modified mechanical linewidth $\Gamma_m + \delta\Gamma_m$. Thus the bandwidth of the OMIT feature is

$$\Gamma_{\text{OMIT}} = \Gamma_m + \delta\Gamma_m \approx \Gamma_m(1 + C_{\text{eff}}), \quad (\text{A22})$$

where we have defined the effective cooperativity,

$$C_{\text{eff}} \equiv C \frac{(4\Omega_m/\kappa)^2}{1 + (4\Omega_m/\kappa)^2}, \quad (\text{A23})$$

which characterizes the efficacy of dynamical radiation pressure effects for a system with finite sideband resolution. In the limit of infinite sideband resolution, i.e., $\Omega_m \gg \kappa$, we have $C_{\text{eff}} \rightarrow C$, and the expression for Γ_{OMIT} reduces to the one in the literature [26–28,53].

The delay experienced by the probe depends on whether it is detected in transmission or reflection. When detected in transmission, the resonant group delay is given by

$$\tau_T = \left[-\frac{\partial}{\partial \Omega} (\arg T[\Omega]) \right]_{\Omega=\Omega_m}.$$

Evaluating this using the expression for the transmission coefficient [Eq. (A21)] and the expression for K [Eq. (A17)],

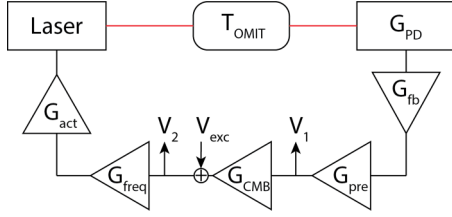


FIG. 4. Loop diagram of the OMIT measurement. Red shows optical path, black shows electronic path.

we get

$$\tau_T = -\left(\frac{2}{\kappa} + \frac{2C_{\text{eff}}}{\Gamma_{\text{OMIT}}}\right) \approx -\frac{2C_{\text{eff}}}{\Gamma_{\text{OMIT}}}, \quad (\text{A24})$$

where the first term is the delay due to the effect of the bare cavity, while the second term is from OMIT. Since $\kappa \gg \Gamma_{\text{OMIT}}$ (in the weak-coupling regime we operate in), we can safely neglect the first term.

When detected in reflection, as in the case of single-port cavities [26–28,53], the group delay is affected by the out-coupling efficiency. To wit,

$$\begin{aligned} \tau_R &= \left[-\frac{\partial}{\partial \Omega} (\arg R[\Omega]) \right]_{\Omega=\Omega_m} \\ &\approx \frac{2C_{\text{eff}}}{\Gamma_{\text{OMIT}}} \frac{\eta_I}{1 + C_{\text{eff}} - \eta_I}. \end{aligned} \quad (\text{A25})$$

The delay-bandwidth product (DBP),

$$\text{DBP} \equiv \tau \Gamma_{\text{OMIT}}, \quad (\text{A26})$$

is thus different when the probe is measured in transmission or reflection. In fact,

$$\text{DBP}_T = -2C_{\text{eff}}, \quad \text{DBP}_R = \frac{2C_{\text{eff}}\eta_I}{1 + C_{\text{eff}} - \eta_I}. \quad (\text{A27})$$

Note that when the out-coupling efficiency through the reflection port is ideal ($\eta_I \rightarrow 1$), $\text{DBP}_R \rightarrow 2$.

APPENDIX B: EXPERIMENTAL DETAILS

1. Calibration of OMIT response

In the experiment, both the excitation to probe the cavity and the readout are done inside the frequency stabilization servo loop, as shown in Fig. 4. To isolate the OMIT response it is necessary to measure and calibrate out the responses of the other elements of the loop.

In the experiment, a network analyzer (SR785) is used to apply a stimulus V_{exc} at the input of the “common-mode board” (CMB)—a custom-built configurable electronic hardware [54] used as the length control servo here—which causes the laser frequency to modulate via the FSS (frequency stabilization servo) loop. This modulation is incident on the cavity, essentially sensing the OMIT response T_{OMIT} , and gets detected at a photodiode (with response G_{PD}). The resulting signal is processed via an analog loop filter with response G_{fb} and a pre-amplifier (SR560) with response G_{pre} . A part of the output (V_1) is detected phase coherently with the excitation using the network analyzer, while the rest is passed onto the CMB (with response G_{CMB}). A part of the CMB’s output is

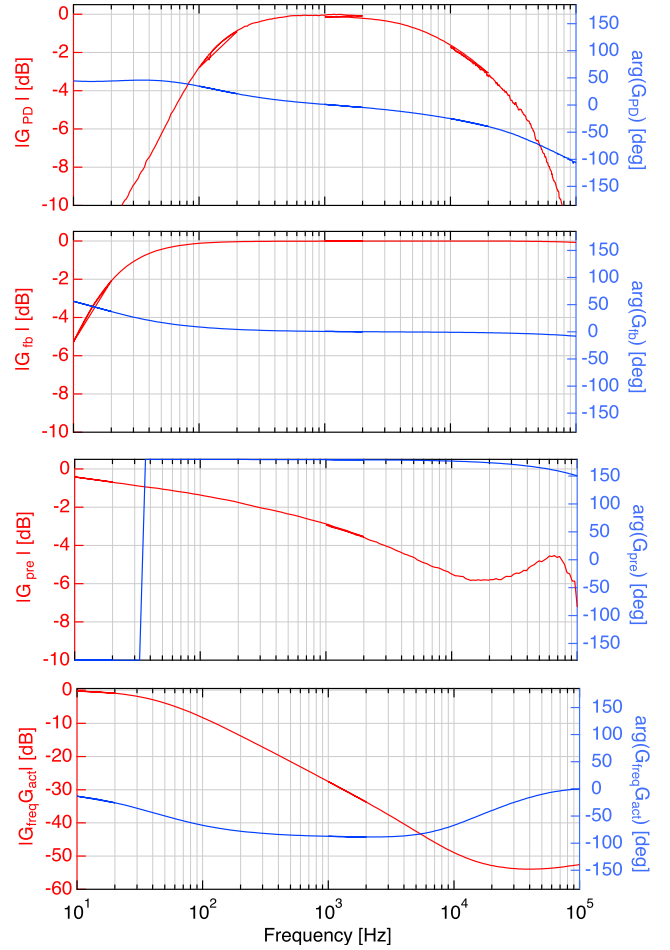


FIG. 5. Measured responses of the various elements in the measurement loop.

also picked off after being summed with the excitation (V_2) to be independently detected using the same network analyzer. This loop is shown in Fig. 4.

We use the network analyzer to measure the response V_1/V_2 (*vis-à-vis* the ratio of the two response measurements V_1/V_{exc} and V_2/V_{exc}). From the loop diagram we can understand how to disentangle the information we need—the OMIT response—from this measurement. Going around the loop diagram we find for V_1

$$(V_1 G_{\text{CMB}} + V_{\text{exc}}) G_{\text{freq}} G_{\text{act}} T_{\text{OMIT}} G_{\text{PD}} G_{\text{fb}} G_{\text{pre}} = V_1,$$

which implies

$$V_1 = V_{\text{exc}} \frac{G}{1 - G} \frac{1}{G_{\text{CMB}}} \quad (\text{B1})$$

where $G = G_{\text{CMB}} G_{\text{freq}} G_{\text{act}} T_{\text{OMIT}} G_{\text{PD}} G_{\text{fb}} G_{\text{pre}}$ is the open-loop gain of the loop.

Performing a similar calculation for V_2 gives

$$V_2 = V_{\text{exc}} \frac{1}{1 - G}. \quad (\text{B2})$$

Combining Eqs. (B1) and (B2),

$$\frac{V_1}{V_2} = \frac{G}{G_{\text{CMB}}}, \quad (\text{B3})$$

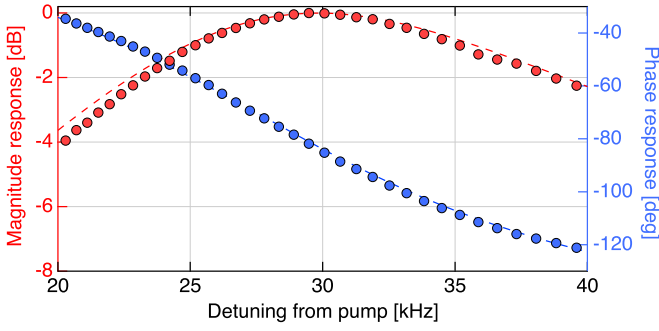


FIG. 6. Example of a wide-band response measurement of the cavity taken at 60 mW incident power. The dashed line shows fits. Note that due to the sparse sampling of frequency, the OMIT dip is not visible in such measurements.

and so

$$T_{\text{OMIT}} = \frac{V_1/V_2}{G_{\text{freq}} G_{\text{act}} G_{\text{PD}} G_{\text{fb}} G_{\text{pre}}}. \quad (\text{B4})$$

Figure 5 shows the measured responses that are used in conjunction with Eq. (B4) to infer the OMIT response. Note that we are interested in the shape of the OMIT response and

not its absolute magnitude, which can be established from the independently measured broadband cavity transmission (shown in Fig. 6); thus the measured responses in Fig. 5 omit overall dimensions for G_{PD} .

2. Data analysis

After the data have been corrected, we adopt the following procedure to extract the relevant optomechanical parameters. The broadband cavity response, such as the one shown in Fig. 6, is used to infer the detuning Δ and the total cavity linewidth κ . Using these values, we then fit the narrow-band cavity response, containing the OMIT feature, to extract the mechanical frequency Ω_m , its effective linewidth $\Gamma_m + \delta\Gamma_m$, and effective mass m , while the bare optomechanical coupling $G = \omega_c/L \approx 2\pi \times 0.28 \text{ GHz}/\mu\text{m}$ is assumed. The fits to the data at each value of the incident power give the following estimates for the various parameters:

$\kappa/2\pi$	$21.4 \pm 0.3 \text{ kHz}$
$\Gamma_m/2\pi$	$23.8 \pm 3.2 \text{ mHz}$
$\Omega_m/2\pi$	27.5 kHz
m	$133.7 \pm 9.6 \text{ g}$
Δ/Ω_m	-0.96 ± 0.01

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