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Multiband gravitational-wave searches for ultralight bosons

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Gravitational waves may be one of the few direct observables produced by ultralight bosons, conjectured dark matter candidates that could be the key to several problems in particle theory, high-energy physics and cosmology. These axionlike particles could spontaneously form "clouds" around astrophysical black holes, leading to potent emission of continuous gravitational waves that could be detected by instruments on the ground and in space. Although this scenario has been thoroughly studied, it has not been yet appreciated that both types of detector may be used in tandem (a practice known as "multibanding"). In this paper, we show that future gravitational-wave detectors on the ground and in space will be able to work together to detect ultralight bosons with masses $25 \lesssim \mu/(10^{-15} \text{ eV}) \lesssim 500$. In detecting binary-black-hole inspirals, the LISA space mission will provide crucial information enabling future ground-based detectors, like Cosmic Explorer or Einstein Telescope, to search for signals from boson clouds around the individual black holes in the observed binaries. We lay out the detection strategy and, focusing on scalar bosons, chart the suitable parameter space. We study the impact of ignorance about the system's history, including cloud age and black hole spin. We also consider the tidal resonances that may destroy the boson cloud before its gravitational signal becomes detectable by a ground-based follow-up. Finally, we show how to take all of these factors into account, together with uncertainties in the LISA measurement, to obtain boson mass constraints from the ground-based observation facilitated by LISA.

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I. INTRODUCTION

The existence of axions, or other ultralight bosons, could potentially solve the strong charge-parity problem [1–3], serve as stabilizing moduli in extra dimensional models [4,5], and explain the nature of dark matter [6–14]. Gravitational waves (GWs) could be counted among the few observables linked to these elusive particles [15–22], a realization that has motivated a flurry of research on how ground- and space-based GW detectors could join in the hunt [18–31]. However, no study has yet explored the gains from simultaneously leveraging both types of GW instruments (a practice commonly known as "multibanding"). In this paper, we show that a coordinated use of ground- and space-based detectors will increase our chances of detecting GWs from ultralight bosons: observations of a binary inspiral signal detected by LISA [32] will provide crucial information enabling targeted searches for ultralight bosons with third-generation (3G) GW detectors such as the Einstein Telescope (ET) [33] or Cosmic Explorer (CE) [34-36].

The physical phenomenon at the core of this program is the proposed superradiant amplification of ultralight-boson fields around fast-spinning black holes (BHs) [15–22]. Indeed, if a boson exists whose Compton wavelength is commensurate with the size of astrophysical BHs, its presence could be revealed by the spontaneous growth of a macroscopic, coherent quantum state in the BH potential well—a "cloud," containing up to ~10% of the mass of its BH host [37-39]. After a short period of exponential growth, the cloud is expected to stabilize and emit quasi-monochromatic ("continuous") GWs, potentially detectable by instruments on the ground or in space. In the absence of boson self-interactions, this continuous GW signal may persist for a long time $(1-10^4 \text{ yr for our})$ parameters of interest) until the totality of the cloud has been radiated away [21,22],

Detectors on the ground are most sensitive to GWs between $\sim [10, 10^3]$ Hz, which makes them suitable probes of boson masses in the range $[10^{-14}, 10^{-12}]$ eV [18,21]. Although clouds formed by such bosons would not be directly detectable by LISA, the BH harboring the cloud may itself lie in a binary [40–43]; the binary would, in turn, emit GWs in the LISA band of $\sim [10^{-3}, 1]$ Hz during its inspiral. As explored below, this can happen for binaries

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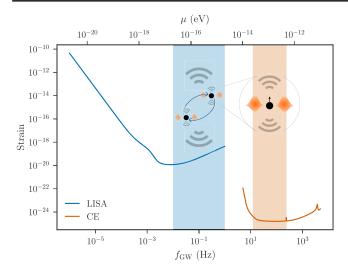


FIG. 1. By analyzing BBH inspirals with GW frequencies $0.01 \lesssim f_{\rm GW}/{\rm Hz} \lesssim 1$ (shaded blue band), LISA will be able to provide crucial information for the search of GW signals from bosons with masses $25 \lesssim \mu/(10^{-15}~{\rm eV}) \lesssim 500$ (shaded orange band) using CE, or other 3G detectors, on the ground. Solid curves mark the expected amplitude spectral densities of LISA (blue) and CE (orange). We explore the details of this application of multibanding starting in Sec. III, after providing some background in Sec. II.

with total mass in the range $\sim [100, 6000]~M_{\odot}$, and bosons with masses within $\sim [25, 500] \times 10^{-15}$ eV (Fig. 1 and Table I).

Searches for continuous GWs are drastically simpler by knowledge of the source sky location and orientation, as well as estimates of the expected signal frequency and frequency derivative—all of which can be obtained from the inspiral signal. This means that LISA will provide the information required for 3G detectors on the ground, like ET and CE, to conduct directed follow-up searches for ultralight-boson signals. For simplicity, we will treat the case of LISA and a single CE instrument on the ground, but our conclusions are easily generalizable to arbitrary detector networks.

We begin by reviewing some essential background on the dynamics of boson condensates and their associated GW signals in Sec. II. We then outline our proposed observation strategy in Sec. III, describing how a BBH detection in LISA can inform a continuous wave (CW) follow-up by CE. In Sec. IV, we report our results on the feasibility of this measurement across the accessible

TABLE I. Relevant parameters (approximate ranges).

Boson rest mass	μ	$[25,500] \times 10^{-15} \text{ eV}$
CW frequency (CE)	$f_{\rm CW}$	[12, 240] Hz
Binary total mass	$M_{ m tot}$	$[100,6000] M_{\odot}$
CBC frequency (LISA)	$f_{ m LISA}$	[0.001, 1] Hz

parameter space, including the effect of tidal resonances, and discuss its interpretation in Sec. V. We offer concluding remarks in Sec. VI.

II. BACKGROUND

In this section, we describe how an ultralight boson field can interact with a fast-spinning BH to spontaneously give rise to a macroscopic boson cloud (Sec. II A), which in turn proceeds to radiate CWs for a long time (Sec. II B) if it is not disrupted by tidal resonances (Sec. II C).

A. Cloud formation

Excited states of a boson field with mass $m_b \equiv \mu/c^2$, and angular frequency $\omega \approx \omega_b \equiv \mu/\hbar$, will be superradiantly scattered off a Kerr BH if [5,44–47]

$$\omega/m < \Omega_{\rm BH},$$
 (1)

where m is the azimuthal quantum number of the boson's total angular momentum along the BH spin direction, and $\Omega_{\rm BH}$ is the angular frequency of the hole's exterior horizon (see, e.g., [48]). A boson state that satisfies this superradiant condition will emerge with an enhanced amplitude (increased occupancy number) from interactions with the BH [5,15,21,22,46,47,49–54], by extracting energy from its ergoregion in a manner fully analogous to the classical Penrose process [44,45,55–58]. (See [47] for a review on superradiance.)

A boson with Compton wavelength $(\lambda_{\mu} \equiv hc/\mu)$ comparable to the BH size $(r_g \equiv GM/c)$, may support semibound states in the BH potential, with an energy-level structure analogous to the electronic levels in the hydrogen atom [49–52]. The level spacing is controlled by a system-specific parameter α with the same role as the fine-structure constant in the hydrogen atom. This is given by the ratio of the two relevant length scales:

$$\alpha \equiv \frac{r_g}{\lambda_u} = \frac{GM}{c} \frac{m_b}{\hbar} = \frac{GM}{c^3} \omega_b, \tag{2}$$

where $\lambda_{\mu} \equiv \lambda_{\mu}/(2\pi)$ and M is the BH mass. For superradiant energy levels to exist, Eq. (1) demands

$$\alpha < \frac{1}{2}m\chi \left(1 + \sqrt{1 - \chi^2}\right)^{-1} < \frac{m}{2},$$
 (3)

where χ is the BH's dimensionless spin, and the second inequality is obtained by noting $0 \le \chi < 1$.

If a superradiant state exists and boson self-interactions can be neglected, the occupancy number of the superradiant level will grow exponentially at the expense of the BH [50–52,58–61]. Superradiant growth can begin spontaneously, starting from quantum fluctuations in the field, and can continue to extract up to $\sim 10\%$ of the BH mass [37,38,54]. The process efficiently harvests angular

momentum, greatly reducing the BH spin, until superradiance shuts down when Eq. (1) is saturated. As this happens, the final BH spin χ_f asymptotically approaches

$$\chi_f = \frac{4\alpha_f m}{4\alpha_f^2 + m^2},\tag{4}$$

with α_f computed for the final BH mass. If only one level is populated, then the final cloud mass will be [21]

$$M_c = M_i - M_f \approx M_i \frac{\alpha_i \chi_i}{m}, \tag{5}$$

where M_i and M_f are the initial and final BH masses, χ_i is the initial BH spin, and the approximate equality holds for $\alpha_i \lesssim 0.1$. In these approximations, the α computed for the initial BH mass, α_i is larger than α_f by ~10%. A more exact value for this quantity may be obtained by numerically solving a set of differential equations, e.g., Eqs. (17)–(21) in Ref. [46], assuming a quasiadiabatic evolution. In this paper we follow this numerical approach, applying the same methods as in Ref. [24].

Although a given system may support multiple superradiant levels, the different growth rates usually ensure that there is a single, fastest-growing state that is relevant at any given time. For a field with spin-weight s=0, 1 and a BH with dimensionless angular frequency $\bar{\Omega}_{\rm BH} \equiv \chi/(2+2\sqrt{1-\chi^2})$, the level with the fastest superradiant growth will have angular quantum numbers $\{j,l,m\}$ such that $j=l+s=m={\rm ceil}(\alpha/\bar{\Omega}_{\rm BH})$ [24], and the smallest possible radial quantum number that yields a boson energy satisfying Eq. (1). Consequently, the fastest-possible growing level over all values of α and χ will be j=l+s=m=1, n=0. In this paper, we will focus on scalar bosons (s=0), for which the overall dominant level has $\ell=m=1, n=0$.

The time it takes a single-level cloud to achieve its full size can be characterized by the *e*-folding time in the occupation number of the relevant quantum state, $\tau_{\rm inst}$. For the dominant scalar level, in the nonrelativistic limit $(\alpha_i \ll 1)$, this is [21]

$$\tau_{\text{inst}}^{(s)} \approx 27 \text{ days} \left(\frac{M_i}{10 M_{\odot}}\right) \left(\frac{0.1}{\alpha_i}\right)^9 \frac{1}{\chi_i - \chi_f}.$$
 (6)

Once superradiance has shut down and the cloud has reached its maximum size, the BH and boson condensate become energetically decoupled. The cloud may persist for a long time, until its energy is depleted through GW emission or resonant perturbations, as we review below.

B. Dissipation due to GW emission

The macroscopic, coherent quantum state that makes up the boson cloud can be thought of as a classical system, with a time-varying stress-energy tensor corresponding to the square-density of the field amplitude [15–22]. This time-varying stress-energy leads to the emission of GWs, which slowly carry away the energy contained in the cloud, as bosons annihilate into gravitons [15,18]. For the dominant scalar level, it may be shown that this results in the emission of a quasimonochromatic CW, with initial frequency approximated by $(\alpha_i \ll 1)$

$$f \approx \frac{\mu}{\hbar \pi} \approx 645 \text{ Hz} \left(\frac{10 M_{\odot}}{M}\right) \left(\frac{\alpha_i}{0.1}\right),$$
 (7)

and corresponding initial (angle-averaged) strain amplitude

$$h_0 \approx 8 \times 10^{-28} \left(\frac{M_i}{10 M_{\odot}}\right) \left(\frac{\alpha_i}{0.1}\right)^7 \left(\frac{\text{Mpc}}{D_L}\right) \left(\frac{\chi_i - \chi_f}{0.1}\right), \quad (8)$$

where D_L is the cloud's luminosity distance [17,19,46]. For $\alpha_i \gtrsim 0.1$, this approximation breaks down and Eq. (8) tends to overestimate the GW power [21]. Instead, we estimate h_0 more accurately using the numerical results from [20,21]. We define the strain amplitude for the quadrupolar mode following the usual LIGO-Virgo convention for the CW plus and cross polarizations, ¹

$$h_{+} = \frac{1}{2}h_{0}(1 + \cos^{2}\iota)\cos[\Phi(t)], \tag{9}$$

$$h_{\times} = h_0 \cos \iota \sin[\Phi(t)], \tag{10}$$

where ι is the source inclination (angle between the BH spin axis and the line of sight), and $\Phi(t)$ is the sinusoidal phase evolution implied by f. For a BBH with aligned spins, i.e., spins parallel to the orbital angular momentum, the cloud's inclination ι is the same as the inclination ι of the binary's orbital plane. In general, ι and ι orb need not be equal for a BBH with precessing spins.

Since GW emission removes energy-momentum from the cloud, the cloud mass gradually decreases, causing the signal frequency and amplitude to evolve [41]. Initially, the GW frequency increases with an approximate time derivative (with respect to the proper time)

$$\dot{f} \approx 3 \times 10^{-14} \text{ Hz/s} \left(\frac{10 M_{\odot}}{M_i}\right)^2 \left(\frac{\alpha_i}{0.1}\right)^{19} (\chi_i - \chi_f)^2, \quad (11)$$

for $\alpha_i \ll 1$ [22,24]. This spin up is characteristic of gravitationally bound systems, and distinguishes boson clouds from other potential CWs sources, like nonaxisymmetric neutron stars (see [62] for a review). The frequency derivative itself evolves slowly, following $\dot{f} \propto -\dot{M}_c(t) \propto (1+t/\tau_{\rm GW})^{-2}$, where $\tau_{\rm GW}$ is a characteristic timescale [22,24],

¹We factor in the correction in the Erratum of [24].

$$\tau_{\rm GW} \approx 6.5 \times 10^4 \text{ yr} \left(\frac{M_i}{10 M_{\odot}}\right) \left(\frac{0.1}{\alpha_i}\right)^{15} \frac{1}{\chi_i - \chi_f}.$$
 (12)

We incorporate this trend approximately by writing

$$f(t) \approx f_0 + \dot{f}_0 \tau_{\text{GW}} \left(1 - \frac{1}{1 + t/\tau_{\text{GW}}} \right),$$
 (13)

where f_0 and \dot{f}_0 are the initial frequency and frequency derivative, respectively. Besides affecting the frequency, the reduction in the boson cloud mass causes the GW amplitude to decay [41],

$$h(t) \propto h_0 (1 + t/\tau_{\rm GW})^{-1},$$
 (14)

with the initial h_0 determined numerically.

C. Depletion due to orbital resonances

The tidal perturbation of a massive companion in a corotating (counterrotating) orbit may introduce hyperfine (Bohr) resonances in the boson energy levels. This occurs when the orbital frequency matches the energy gap between superradiant and decaying modes (that is, modes with a positive imaginary part of their eigenfrequencies) [40–43]. If this occurs, then the boson cloud depletes through the excitation of a decaying mode. The characteristic strength and timescale of the depletion depends on the ratio between the mass of the perturber and the BH hosting the cloud. As a conservative estimate, we will assume that the cloud becomes totally depleted once the orbit hits a resonance frequency. This is generally valid for equal mass BBH systems, for which the decay rate of the resonant mode is high and the decay timescale is much shorter than the orbital timescale [40-43]. To a good approximation, the observable result of this resonance will be to instantaneously turn off the GW signal.

For a BBH system in which the components have similar masses but opposite spins, the frequency associated with the hyperfine resonance will always be lower than of the Bohr resonance [41,42]. This means that, as a binary evolves from larger to smaller separations, the former will be the first to become relevant. Hence, we restrict our attention to hyperfine resonances, the inspiral GW frequency of which is given by

$$f_{\rm res} = \frac{1}{12\pi} \mu \chi_f \alpha_f^5, \tag{15}$$

where χ_f is the BH spin at the saturation of superradiance given by Eq. (4). For $\alpha_i \ll 1$, $\chi_f \approx 4\alpha_i$, and

$$f_{\rm res} \approx \frac{1}{3\pi M_i} \alpha_i^7. \tag{16}$$

Because of resonances, the presence of a binary companion can restrict the CW power that may be expected from a boson cloud around a given BH: the boson mass that

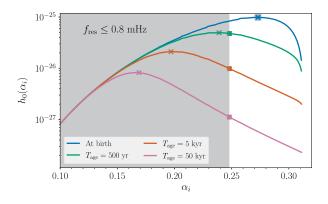


FIG. 2. Strain amplitude as a function of α_i for $M_i = 1000~M_\odot$, $\chi_i = 0.9$, and $D_L = 400~$ Mpc. The grey area indicates the α_i s that are not observable by our technique due to resonant depletion. Solid lines with different colors correspond to various $T_{\rm age}$'s: zero age (blue), 500 yr (green), 5 kyr (orange), and 50 kyr (pink). On each colored line, the cross marker denotes the optimal α_i which generates the maximum amplitude without resonance, while the square marker corresponds the best α_i conditioned by resonance. Two maxima are the same only for zero age. The optimal α_i s before resonance are not observable for other $T_{\rm age}$.

would produce the strongest signal for an isolated BH may also lead to resonances that destroy the cloud if the BH is in a binary. We illustrate this in Fig. 2 for a BH with $M_i = 1000 M_{\odot}, \chi_i = 0.9$, and $D_L = 400$ Mpc. The different curves represent the CW amplitude h_0 , as in Eqs. (9) and (10), for different boson masses (parametrized by α_i), with color representing the cloud age $T_{\rm age}$, i.e., the time after the end of superradiance. For a given $T_{\rm age}$ the emission peaks for the value of α_i that corresponds to a boson optimally matching the BH, which we indicate by a cross. Higher α s lead to faster depletion by Eq. (12), so the crosses move left as T_{age} increases in Fig. 2. If we rely on LISA to identify potential CW sources, then the cloud needs to persist at least until the binary enters the LISA frequency band. As we will see below, this means that the resonances should not occur at frequencies $f_{\rm res} < 0.8$ Hz, or the system will not be detected (gray region in Fig. 2). Depending on the cloud age, this means that the loudest CW we expect to see from a BH in a binary is generally weaker than it would have been if the BH had been isolated (marked by boxes in Fig. 2). For our example system, this is the case for all shown T_{age} 's except $T_{age} = 0$ (blue curve).

Cloud resonances may backreact on the binary's orbit, inducing a dephasing on inspiral GW waveforms [40,43]. Looking for such kind of dephasing may be another smoking-gun evidence of the existence of boson. However, as we will discuss below, our observation strategy requires a sufficiently long segment of inspiral in LISA and CW in CE before the resonance occurs. Therefore, we ignore the effect of backreaction on either the inspiral waveform or the cloud emission.

Finally, the above calculations for resonant depletion assume a perturbation of a weak tidal field generated by the companion object. When the orbital separation reaches the Roche radius, the strong tidal perturbation may also disrupt the boson cloud significantly [63]. According to Ref. [63], the critical frequency $f_{\rm crit}$ of this tidal disruption for an equal-mass binary is

$$f_{\rm crit} \approx \frac{1}{\sqrt{250}\pi M_i} \alpha_i^3. \tag{17}$$

Comparing to Eq. (16), the ratio of this critical frequency to the resonance frequency is

$$\frac{f_{\text{crit}}}{f_{\text{res}}} \approx 0.2\alpha_i^{-4}.\tag{18}$$

Since the α_i s we will be interested lie in the range $\sim [0.15, 0.45]$ (Sec. IVA), we expect the boson clouds we target to deplete due to orbital resonances before having a chance of being tidally disrupted.

III. OBSERVATION STRATEGY/SCENARIO

A BBH signal detected by LISA can provide crucial information about the location and properties of the component BHs, allowing detectors on the ground to conduct a directed follow-up for ultralight bosons. For this to be possible, the binary must do the following:

- (i) have a total mass and initial orbital separation such that the inspiral signal remains in the LISA frequency band sufficiently long to be detectable;
- (ii) have component BHs in the stellar-mass range so as to potentially host boson clouds radiating GWs in the CE (or ET) frequency band.

These conditions can be satisfied by equal-mass binaries with total mass $M_{\rm tot}$ in the range $\sim [100,6000]~M_{\odot}$. Assuming a signal-to-noise ratio (SNR) threshold of 8, LISA can detect such systems over a 4 yr observation period if the initial orbital separation yields a starting GW frequency of $f_{\rm LISA}^{\rm ini} \sim 0.01$ Hz. Meanwhile, component BHs with masses in the range $\sim [50,3000]~M_{\odot}$ may host boson clouds sourcing GWs with frequencies in the range $\sim [12,240]$ Hz [cf. Eq. (7)], well within the most-sensitive band of future ground-based detectors. Assuming $\alpha_i \approx 0.1$, this corresponds to bosons with rest masses μ within $\sim [25,500] \times 10^{-15}$ eV [cf. Eq. (2)]. (See Fig. 1 and Table I.)

As the binary inspirals towards merger, the orbit may reach the resonance frequency of the cloud and destroy it (Sec. II C). If this takes place before the BBH signal has entered the LISA frequency band, the cloud will have depleted before CE has had a chance to observe it. Therefore, for our strategy to be successful, the pair of M_f and μ must lead to resonances that only take place after the binary has entered the LISA band. Even then,

resonances may hinder the CE follow-up: if the resonance occurs during the LISA observation, the cloud CW will be terminated sooner and CE's available observation period will be reduced. Below, we will factor this effect by computing the reductions in CE SNR expected from the resonances.

If at least one of the BHs in the binary indeed harbors a boson cloud actively emitting CWs, its detectability by CE will further depend on the source sky location, orientation and distance from Earth, as well as the BBH orbital parameters. All of these properties can be inferred based on the LISA signal. Below, we describe how the two measurements, by LISA and CE, would take place.

A. LISA measurement

LISA will be able to detect the inspiral stage of compact binaries with total mass above $10~M_{\odot}$. Such signals will carry information about the masses and spins of the component BH, as well as the system's sky location, luminosity distance, and orbital parameters (including semimajor axis, orbital phase, and eccentricity). How well these properties can be extracted from the data will depend, in part, on the SNR of each particular signal.

To calculate inspiral SNRs in LISA, we follow Ref. [64] and assume the full, 2.5-million-km-long, three-arm configuration as proposed for the ESA L3 mission [32]. For a face-on binary, i.e., one whose orbital plane is perpendicular to the line of sight, the optimal sky-averaged SNR of LISA is given by

$$\rho_{\rm LISA} = 8 \int_{f_{\rm LISA}^{\rm ini}}^{f(T_{\rm LISA})} \frac{A^2(f)}{S_{\rm LISA}(f)} df, \tag{19}$$

where $f_{\rm LISA}^{\rm ini}$ is the initial GW frequency, $T_{\rm LISA}$ is the observation duration, A(f) is the amplitude of the inspiral waveform, and $S_{\rm LISA}(f)$ is the instrument's noise power spectral density (PSD). We consider an inspiral signal to be detectable if $\rho_{\rm LISA} \geq 8$. We assume the sky-location-averaged sensitivity from the analytical fit in Ref. [64] (Fig. 1), which accounts for both instrumental and galactic confusion noise, and assume an observation time $T_{\rm LISA} = 4$ years.

Since the binaries we are interested in only inspiral in the LISA band, merging at much higher frequencies, we use the stationary phase approximation for a circular, non-spinning quadruple system to write [65]

$$A(f) = \sqrt{\frac{5}{24}} \frac{\mathcal{M}f^{-7/6}}{\pi^{2/3}D_L},\tag{20}$$

where $\mathcal{M} = (1+z)(M_1M_2)^{3/5}/M_{\rm tot}^{1/5}$ is the redshifted chirp mass and D_L is the luminosity distance. For a given $T_{\rm LISA}$ and $f_{\rm LISA}^{\rm ini}$, we evolve the system to obtain the final frequency $f(T_{\rm LISA})$, using Peters's formula [66]. Since $f_{\rm LISA}^{\rm ini}$ only depends on the initial binary separation, LISA

may observe binaries with any $f_{\rm LISA}^{\rm ini}$ within its sensitive frequency band. However, to select systems with minimal loss due to resonant depletion, we demand $f_{\rm LISA}^{\rm ini}$ to be the lowest possible, so as to get $\rho_{\rm LISA}=8$. Hence $f_{\rm LISA}^{\rm ini}$ is different for different $M_{\rm tot}$, e.g., $f_{\rm LISA}^{\rm ini}\approx 1$ mHz for $M_{\rm tot}\approx 1000~M_{\odot}$ but $f_{\rm LISA}^{\rm ini}\approx 6$ mHz for $M_{\rm tot}\approx 100~M_{\odot}$, assuming $D_L=400$ Mpc.

To estimate the impact of LISA measurement uncertainty in the observable range of boson mass, we take the typical 1σ component mass and distance uncertainties to be $\sim 10\%$ and $\sim 20\%$, from Refs. [67,68], respectively. For concreteness, below we restrict our attention to nearly equal mass binaries.

If, in addition to the BBH masses, LISA could accurately determine the component spins $\chi_{1,2}$, Eq. (4) would immediately exclude boson masses with $\chi_f(\mu) \leq \chi_{1,2}$. This would further narrow down CE's potential search space. While the spin magnitude measurement can be as good as $\Delta \chi \approx 0.1$ for massive binaries of $\geq 10^4~M_{\odot}$ [69], there is a lack of detailed studies on the spin measurement for intermediate mass binaries. In the following sections, we do not consider the constraint from individual spin measurements.

B. Ground-based follow-up

The strategy for CE follow-up is similar to that of boson clouds forming around compact binary coalescence (CBC) remnants [24,25]: information about the source location from LISA vastly simplifies what would otherwise be an extremely expensive all-sky search for CWs from boson clouds, and information about the BH mass significantly narrows down the expected frequency space, through Eq. (7). Unlike in the case of a CBC remnant, however, LISA would provide us with post-, not pre-, superradiance BH parameters (assuming a cloud is present). This follows from the fact that, rather than newly born boson clouds, we should expect LISA to detect systems long after the cloud has formed.

Following up a BH in a binary involves some additional complications with respect to solitary BHs. Most prominently, the orbital motion will be imprinted in the boson CW through a time-varying Doppler shift (Rømer delay). In the frequency domain, this has the effect of spreading the signal power over orbital sidebands centered around the intrinsic signal frequency f_{CW} . An orbit with period P, semimajor axis a and inclination ι will spread the GW power over a bandwidth (see Sec. III E in Ref. [72])

$$B \approx \frac{4\pi a |\sin \iota| f_{\text{CW}}}{cP}$$
$$= 2|\sin \iota| f_{\text{CW}} \left(\frac{GM_{\text{tot}}}{c^3} f_{\text{LISA}}\right)^{1/3}, \tag{21}$$

where we have assumed the orbit is Keplerian to write B in terms of $M_{\rm tot}$ and $f_{\rm LISA}$, the GW inspiral frequency that would be seen by LISA. For example, for an equal-mass binary with $M_{\rm tot}=1000~M_{\odot}$ inspiraling at $f_{\rm LISA}\sim 1~{\rm mHz}$, and a boson cloud radiating at $f_{\rm CW}=40~{\rm Hz}$, the bandwidth is roughly $B\approx 1.3|\sin\iota|$ Hz.

There exist several established methods for detecting CWs from sources in binaries with known sky locations [70,72–75], all of which can collect the power distributed across the orbital sidebands. In principle, knowledge of the orbital parameters (including the phase) can be used to fully demodulate the signal and recover all signal power, so that the search sensitivity is not impacted by the orbital motion. In our scenario, this will be made possible by the precise characterization of the orbit through the LISA inspiral measurement. We will thus base our CE sensitivity estimates on previous studies for boson signals from isolated sources in Ref. [24].

The projections of [24] were obtained through the search method described in Refs. [70,71,75], although optimized for signals with a positive frequency derivative to accommodate Eq. (11). When targeting binary systems, uncertainties in the orbital parameters may be marginalized over with minimal impact on the sensitivity [75]. The measurement of ι is correlated with D_L since both parameters affect the overall amplitude of the inspiral signal, and a recent case study suggests a full Bayesian parameter estimate may return a poor ι measurement ~1 rad for SNR ~ 10 [76]. However, the usual implementation of this particular method parallelizes the search by splitting the frequency band in a way that requires $B \leq 0.5$ Hz, which would limit accessible inclinations (e.g., $\iota \lesssim 10^{\circ}$ for the 1000 M_{\odot} binary considered above). This limitation can be circumvented by reducing parallelization, at the expense of increased computing cost.

Although the search for boson signals in CE data is conceptually no different from other directed CW searches, one feature sets our scenario apart: depending on the mass ratio, we could expect CWs from clouds around *both* binary components. In fact, if the two BHs have near-equal masses and similar histories, they should both be compatible with the same set of boson masses and, thus, lead to CWs signals with the same intrinsic frequency given by Eq. (7). The amplitudes of the two signals would depend on the individual BH masses and histories (i.e., cloud age and presuperradiance spin), following Eqs. (8) and (14). Assuming the two clouds are formed simultaneously, the amplitude ratio of the two CW signals $h_0^{(2)}/h_0^{(1)}$ has a steep dependence on the binary mass ratio,

$$h_0^{(2)}/h_0^{(1)} \approx (M_2/M_1)^8,$$
 (22)

for component masses $M_{1,2}$. With a small asymmetry in BH masses $M_2/M_1=0.9$, the amplitude ratio drops to ~40%.

²There will also be relativisite effects, like the Shapiro delay, but those are not relevant for semicoherent CW searches [70,71].

Therefore, we generally expect one of the putative CW signals to dominate.

Having two overlapping CW signals could, at best, enhance the effective SNR available to the search. Assuming that the power is added incoherently (as would be the case for the methods mentioned above), the improvement could be up to a factor of $\sqrt{2}$ for $M_1 = M_2$. Methods could be developed in the future to coherently track both signals, taking into account orbital phase, and thus achieve a factor of 2 improvement instead. In any case, an amplitude enhancement is degenerate with a reduction in the luminosity distance, so all quantities of interest (like detection horizons) can be scaled trivially. Therefore, in the detectability discussions below, we will simply assume a single signal is present at a time.

Below, we assume a single CE instrument operating at the design sensitivity projected in [35,77], and shown in Fig. 1. While CE may observe boson CWs within $D_L \sim 10$ Gpc [24] for the BH masses of interest, LISA may detect binaries within $D_L \sim 400$ Mpc (~ 1000 Gpc) for $M_{\rm tot} = 100~M_{\odot}(6000~M_{\odot})$, respectively [78]. Therefore, we expect our observation technique to be limited by LISA (CE) in the lower (upper) mass end, respectively.

IV. DETECTABLE PARAMETER SPACE

Assuming LISA has detected a given BBH, we would now like to quantitatively characterize the conditions needed for CE to detect a CW from a putative cloud in the system, and identify the boson masses that can be probed by such a measurement. As mentioned above, the first requirement is that the total mass of the system be in the range

$$100 \lesssim M_{\text{tot}}/M_{\odot} \lesssim 6000.$$
 (23)

This is however not a sufficient condition: BH age, presuperradiance spin, and tidal resonances may all limit the expected CW amplitude and, thus, its detectability. In this section, we explore how these factors affect potential boson-mass constraints (Sec. IV A); we discuss the effect of uncertainties in the LISA measurement (Sec. IV B); and, finally, we present detection horizons over parameter space (Sec. IV C).

Throughout, we consider that CE is able to detect a given CW if its amplitude exceeds a threshold $h_{\rm thr}$, estimated using the scaling provided in Eq. (38) of Ref. [24] for one detector, namely

$$h_{\text{thr}}(f) = 1.7 \times 10^{-26} \left[\frac{S_n(f)}{S_{\text{ref}}} \right]^{\frac{1}{2}} \left[\frac{8 \text{ d}}{T_{\text{drift}}} \right]^{\frac{1}{4}} \left[\frac{1 \text{ yr}}{T_{\text{obs}}} \right]^{\frac{1}{4}}, \quad (24)$$

where $S_n(f)$ is the noise PSD, $S_{\text{ref}} = 1.6 \times 10^{-47} \text{ Hz}^{-1}$ is a reference value, T_{drfit} is the period of coherent segments of the CW, and T_{obs} is the total observation time. For the case of multiple detectors, $S_n(f)$ should be replaced by the

harmonic mean of the corresponding PSDs. As in Ref. [24], we rescale $T_{\rm drift}=(2\dot{f})^{-1/2}$ to be the largest value allowable by the expected frequency evolution of Eq. (11) for a given boson mass. We also take into account that the cosmological redshift scales down the detector frame \dot{f} by $1/(1+z)^2$, as well as f by 1/(1+z). Throughout this study, we choose $T_{\rm obs}=1$ yr.

In order to estimate the CW amplitude expected from a given system, we approximate the presuperradiance BH mass by its postsuperradiance value, as would be provided by LISA. This is equivalent to assuming a $\sim 10\%$ error on the mass, which is comparable to the projected uncertainty in LISAs component mass measurement (see Sec. III A).³

A. Idealized measurement

Let us first assume that LISA has detected a suitable BBH and perfectly measured the masses of its components, as well as the orbital and extrinsic parameters. The expected GW strain produced by a boson cloud around one of the BHs will depend on the particle mass, μ (or, equivalently, α_i), and the presuperradiance spin of the host BH, γ_i , approximately following Eq. (8). With knowledge of the BH mass, we may thus chart the values of χ_i and α_i that would yield a detectable signal in CE, i.e., $h_0 \ge h_{\text{thr}}$. Assuming we observe the cloud at birth, the blue region in Fig. 3 demonstrates this for two example BH masses at $D_L = 400$ Mpc. For a given value of α_i , higher χ_i s are more favorable, since those values lead to a larger initial cloud (the boson can extract more energy momentum from the BH), and hence a stronger CW signal. The boundary at large α_i s can be understood from Eq. (4), which sets the critical spins; the boundary at small α_i s comes from the α_i^{γ} scaling in Eq. (8), which causes the signal amplitude to shrink rapidly as α_i decreases.

Unfortunately, it is safe to assume that LISA will not observe a boson cloud at birth, since simulations of BBH populations show that the typical inspiral timescale is longer than $\mathcal{O}(\mathrm{Myr})$ before entering the LISA band [79–86]. Rather, the observation will occur some (long) time T_{age} after superradiance has taken place. Since the GW amplitude decreases with time following Eq. (14), this will have a strong impact on detectability. For $T_{\mathrm{age}} \gg \tau_{\mathrm{GW}}$, the observed strain amplitude at $t = T_{\mathrm{age}}$ is $h(T_{\mathrm{age}}) \approx h_0 \tau_{\mathrm{GW}} / T_{\mathrm{age}}$ from Eq. (14), ignoring the frequency drift. In the limit of $\alpha_i \ll 1$, combining Eqs. (8) and (12) gives a scaling relation $h(T_{\mathrm{age}}) \propto \alpha_i^{-8}$. Hence, the strain amplitude in the large- α_i region is unlikely to be detected above the threshold if the BH is too old. In Fig. 3, we use different

³If needed, we could always (albeit at significant computational expense) remove this approximation by recursively solving the cloud evolution equations to find the presuperradiance parameters that would yield a final BH mass compatible with the LISA measurement.

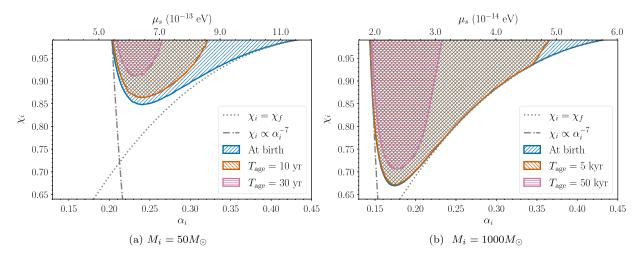


FIG. 3. Detectable parameter space (α_i, χ_i) at $D_L = 400$ Mpc for two example of M_i 's. Each hatched region corresponds to the detectable space for a host BH at different $T_{\rm age}$'s: 10 yr (orange) and 30 yr (pink) for 50 M_{\odot} ; 5 kyr (orange) and 50 kyr (pink) for $1000~M_{\odot}$. Older clouds have had time to dissipated more energy momentum, and (since the strain amplitude is proportional to the cloud mass) the detectable region decreases as $T_{\rm age}$ increases. The grey dotted line shows χ_f as a function of α_i , which is the limit below which Eq. (1) is violated and superradiance cannot occur. The grey dashed-dotted line shows the $\chi_i \propto \alpha_i^{-7}$ scaling in Eq. (8), which suppresses the low α_i amplitude due to insufficient cloud mass. In this and all other figures, we assume a CW observation time of T obs = 1 yr.

colors to show the detectable region for different values of T_{age} . As expected, the higher α_i region is most affected by the age of the cloud.

Besides age, we should consider the effect of orbital resonances. If the orbit hits a resonant frequency, cloud depletion may truncate the CW signal during the ground-based observation, or possibly even before the binary would be detected at all. Therefore, we must require that the initial observation frequency in LISA, $f_{\rm LISA}^{\rm ini}$, satisfy

$$f_{\text{LISA}}^{\text{ini}} \le f_{\text{res}},$$
 (25)

for a possible CW observation. If $f_{LISA}^{ini} > f_{res}$, the cloud vanishes due to resonant decay before the inspiral enters the LISA band and multibanding will be impossible. The inequality Eq. (25) is not strictly necessary if there is archival CE data before the start of LISA's observation. However, the current timeline suggests that CE will be online after the launch of LISA [36]. Therefore we require Eq. (25) to be conservative. From Eq. (16), the resonance frequency scales as α_i^7 for a fixed BH mass. This implies that resonant depletion happens at an earlier stage in the inspiral and is more likely to hinder the CE observation in the small- α_i region. The inspiral frequency at the time of the initial observation by LISA, f_{LISA}^{ini} , is largely arbitrary, since each BBH system is formed at a different reference time and initial separation. Even if $f_{\rm LISA}^{\rm ini} < f_{\rm res}$, we may still miss the CW signal: because the SNR of a CW signal scales as $T_{\rm obs}^{1/4}$ for a semicoherent search, the truncation may prevent CE from accumulating enough SNR to reach a detectable level. (The possibility would remain, however, of observing the CW signal in archival ground-based GW

data, assuming the resonance depletion occurred within a timescale where such archival data exists.)

In Fig. 4, we show the detectable region for component masses of 50 M_{\odot} and 1000 M_{\odot} at $D_L = 400$ Mpc, accounting for resonances. For systems with the parameters within the blue-hatched region but outside the greenhatched region, the boson clouds would totally deplete before the inspiral signal could be observed by LISA. In contrast, systems with parameters enclosed by the greenhatched region do not experience resonance depletion; in this case, both the CW and inspiral emissions are observable in CE and LISA, respectively. We notice that there is a sharp cutoff in the small α_i region when resonant depletion turns on. This is because $f_{\rm res}$ has a strong dependence of α_i^7 as shown in Eq. (16), which suggests that f_{res} depends on α_i almost exclusively. Therefore, the criterion of $f_{\rm res} \ge f_{\rm LISA}^{\rm ini}$ prevents the observation of CW emission from systems with small α_i s, irrespective of γ_i .

B. Measurement uncertainties

We have, so far, assumed that LISA can provide perfect measurements of the luminosity distance D_L , inclination ι , and BH mass $M_{\rm obs}$. However, true LISA measurements will have uncertainties that will impact the CE follow-up. For example, an underestimated distance would lead to an overestimation of the CW detectable region and, correspondingly, the range of boson masses μ that can be probed.

To map how LISA uncertainties affect detectability, we calculate the detectable region corresponding to the boundaries of the projected 90%-credible intervals for M_i and D_L . To simulate such a measurement, we assume the LISA posteriors are well represented by independent Gaussians

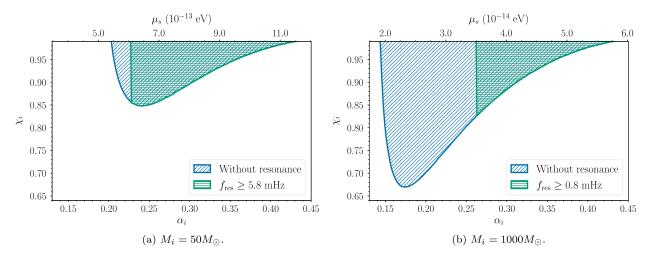


FIG. 4. Detectable parameter space (α_i, χ_i) at $D_L = 400$ Mpc for two example M_i 's. The blue hatched region is the detectable space without considering orbital resonances and is identical to the blue hatched region in Fig. 3. The green hatched region corresponds to the detectable space that remains after imposing $f_{\rm res} \geq f_{\rm LISA}^{\rm ini}$, where $f_{\rm LISA}^{\rm ini}$ is the minimum initial frequency that yields $\rho_{\rm LISA} = 8$: $f_{\rm LISA}^{\rm ini} = 5.8$ mHz (0.8 mHz) for $M_i = 50$ M_{\odot} (1000 M_{\odot}). As $f_{\rm res}$ increases almost monotonically with α_i , the detectable region is truncated sharply at $\alpha_i \approx 0.25$.

with standard deviations given as fractions of the true values, $\sigma_{M_i}/M_i^{\text{true}} = 0.1$ and $\sigma_{D_L}/D_L^{\text{true}} = 0.2$ for the mass and distance, respectively (see Sec. III A).

We represent the effect of measurement uncertainty in Fig. 5. For reference, the solid blue curve encloses the parameters that we would know accessible to CE if we had a perfect measurement of M_i and D_L from LISA, assuming $T_{\rm age}=0$. Similarly, the solid orange (green) curve encloses parameters that are accessible to CE for a perfect LISA measurement, assuming only cloud dissipation (only resonant depletion) is present. Since $T_{\rm age}\gg T_{\rm LISA}$, we expect only the systems in the overlap region within both the resonance and age boundaries to be suitable sources.

In Figs. 5(a) and 5(b), we show how such the uncertainty in the LISA distance measurement affects the expected detectable region for two example BH masses: M_i = 50 M_{\odot} and 1000 M_{\odot} . Each light-colored band surrounding the solid curve of the same color shows the variation of the boundary corresponding to the measurement uncertainty in D_L , for a fixed M_i . We compute this from the projected 90%-credible interval as described above: the upper (lower) bound of the light-blue band corresponds to the 95th (5th) percentile of the D_L posterior for a BH with zero T_{age} . The light-orange band reflects the same projection of 90%-credible interval of D_L posterior, but T_{age} increases to 10 (5000) years for $M_i = 50 \ M_{\odot} \ (1000, M_{\odot})$. Since the strain amplitude scales as the inverse distance, the inferred detectable region is larger for a smaller distance measurement.

On the other hand, the right (left) bound of the light-green band corresponds to the 95th (5th) percentile of the D_L posterior. This correspondence comes from the general correlations and interdependencies between D_L , $f_{\rm LISA}^{\rm ini}$ and

 $ho_{\rm LISA}$. For a constant $ho_{\rm LISA}=8$, the inferred $f_{\rm LISA}^{\rm ini}$ increases with larger D_L . If $f_{\rm LISA}^{\rm ini}$ is kept fixed in the analysis, $ho_{\rm LISA}$ decreases with larger D_L . Finally, for sources at a constant D_L , $ho_{\rm LISA}$ increases with larger $f_{\rm LISA}^{\rm ini}$ until $f_{\rm LISA}^{\rm ini}\sim0.1$ Hz, after which the inspiral falls out the sensitive band of LISA. For $f_{\rm LISA}^{\rm ini}$ greater than this bound, it is not possible to accumulate enough $ho_{\rm LISA}$ in the available observation time of the LISA mission to claim a detection.

By the same token, Figs. 5(c) and 5(d) shows the variation of the expected detectable regions due to the uncertainty in LISA mass measurement. The upper (lower) bound of the light-blue and light-orange band corresponds to 5th (95th) percentile of the M_i posterior. As the boson cloud will extract more energy and momentum from heavier BHs, the strain amplitude increases with the BH mass, and the detectable region expands accordingly if we allow for higher BH masses. The right (left) bound of the light-green band corresponds to 5th (95th) percentile of the M_i posterior, since the resonance frequency is higher for smaller mass.

Generally speaking, both uncertainties on M_i and D_L have a similar effect on the inferred detectable region. The ignorance of the uncertainties on M_i and D_L does not matter for the boundary of χ_f which only depends on χ_f . However, this will affect the inference of μ_s since $\mu_s \propto \alpha_i/M_i$. We also note that the variation does not exceed the boundary set by the final spin at the saturation of superradiance in Eq. (4), since the superradiance condition is not satisfied for $\chi_i < \chi_f$. Due to the sharp cutoff by the resonance boundary at low α_i , we conclude that the uncertainties on M_i and D_L have a smaller impact on the detectable region compared BH aging and resonant depletion.

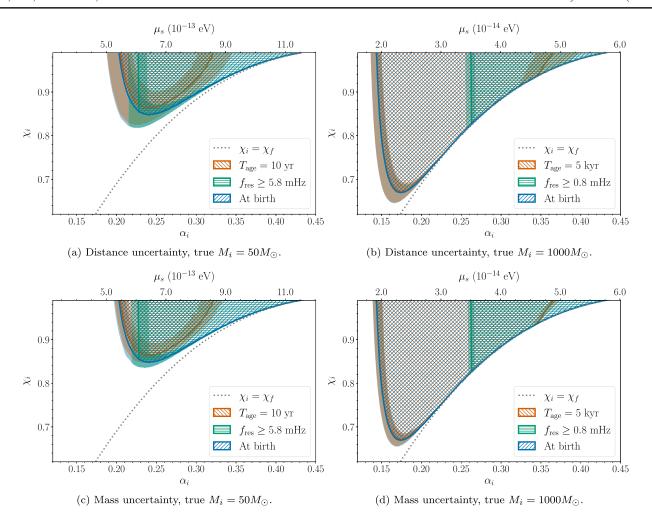


FIG. 5. Impact of LISA measurement uncertainties on the detectable parameter space (α_i, χ_i) for two example M_i 's, with true $D_L = 400$ Mpc and face-on inclination. In each panel, the blue (cf. Fig. 3), orange (cf. Fig. 3), and green (cf. Fig. 4) hatched regions bounded by solid lines correspond to the detectable parameter space without resonant depletion or cloud dissipation, with cloud dissipation only, and with resonant depletion only, respectively. (The assumed $T_{\rm age}$ and $f_{\rm LISA}^{\rm ini}$ are the same as in Figs. 3 and 4.) The regions hatched with all colors mark parameters that remain detectable after accounting for both cloud age and orbital resonances. The semitransparent color bands around the edge of the hatched regions encode the variation in the boundary of the inferred detectable space due to LISA measurement uncertainty in the distance [panels (a) and (b)], or mass [panels (c) and (d)]; the width of the bands corresponds to the LISA 90%-credible interval. When the detectable regions approach the $\chi_i < \chi_f$ constraint (dotted line), the error bands shrink until disappearing; this is because χ_f is independent of M_i and D_L , and hence uncertainty in those parameters does not affect our conclusions about detectability. The vertical light-green band around the true $f_{\rm LISA}^{\rm ini}$ corresponds to variations in the inferred $f_{\rm LISA}^{\rm ini}$ linked to the M_i or D_L uncertainty. For $M_i = 1000~M_\odot$, the light-blue and light-orange bands overlap almost completely at small α_i s, because $\tau_{\rm GW} \gg T_{\rm age}$ in this region.

Finally, we consider the effect of inclination, which we have so far assumed to be optimal. In general, the effect of orbital precession could be included in the inspiral waveform to obtain the actual cloud's inclination ι at any given time, apart from the orbital inclination $\iota_{\rm orb}$. Here, we consider the simpler spin-aligned case in which $\iota_{\rm orb} = \iota$ and we can directly take the LISA $\iota_{\rm orb}$ measurement as a measurement of ι . The observed polarization content varies with the inclination angle with respect to the line of sight. For an interferometer with an interarm angle of 90°, such as CE, the observed amplitude at some inclination angle ι relative to a face-on emission scales as

$$h(i) \propto \sqrt{(1 + \cos^2 i)^2 F_+^2 + 4 \cos^2 i F_\times^2},$$
 (26)

from the quadrature addition of Eqs. (9) and (10) weighed by the antenna pattern F_+ and F_\times defined in Eq. (57) of Ref. [65]. F_+ and F_\times depend on the zenith and azimuthal angles (θ,ϕ) of the source's sky location, as well as the polarization angle ψ . The inclination angle then affects the detectable region, as shown in Fig. 6. To simplify the relation, we chose the source location such that $F_+ = F_\times$. Regardless of intrinsic parameters, the expected amplitude is the largest for face-on $(\iota=0^\circ)$ emission, and the smallest

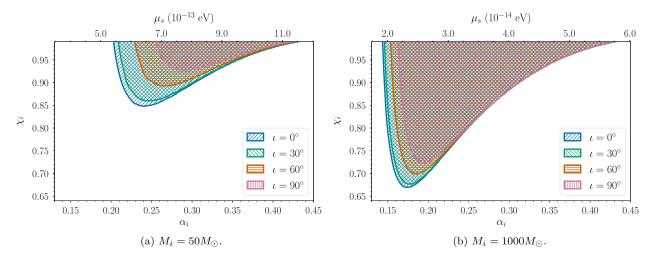


FIG. 6. Detectable parameter space (α_i, χ_i) for a BH with different inclination angles $\iota = 0^\circ$ (blue), 30° (green), 60° (orange), and 90° (pink), for two examples BH masses M_i , and D_L again fixed at 400 Mpc. The strain amplitude is weaker when a source is seen edge on $(\iota = 90^\circ)$, leading the detectable parameter space to shrink as ι increases.

for edge-on ($\iota = 90^{\circ}$) emission. Hence the detectable region shrinks gradually from $\iota = 0^{\circ}$ to $\iota = 90^{\circ}$.

C. Detection horizon

In the investigations above, we held the source distance fixed. The amplitudes of GW emission from the cloud and the binary both decrease as the distance increases. Therefore, we expect that the mostly overlapped regions in Fig. 5 shrink until no system can be observed. To quantify the reach of our technique, we now investigate the detection horizon as a function of M_i and $T_{\rm age}$. We define the detection horizon to be the largest distance such that both SNR thresholds, of CE and LISA, are satisfied. Thus, the detection horizon is a measure of the volume of space within the reach of our analysis technique. For a given expected rate of BBH mergers as a function of redshift, this quantity also informs us about the number of systems that

we may expect to detect during a fixed observation period. Unfortunately, there is large uncertainty in rates for BBH mergers in the mass range of interest [87,88], so we do not attempt to compute a number of expected detections.

We compute horizons assuming $\chi_i = 0.9$, and assume the same definition of $f_{\rm LISA}^{\rm ini}$ as in Sec. III A. For each BH, we identify the boson mass that generates the loudest CW. This results in an optimal α_i that maximizes the horizon for each M_i . To include the amplitude decay due to BH aging, we calculate the horizons for four ages: $T_{\rm age} = 0$, 500 yr, 5 kyr, and 50 kyr.

Figures 7(a) and 7(b) show the detection horizon as a function of M_i without and with resonant depletion, respectively. The color scale shows the value of α_i that yielded maximum strain amplitude for each $(M_i, D_L, T_{\rm age})$. There are some features shared by both figures. First, since we require both detections in LISA and CE, irrespective of

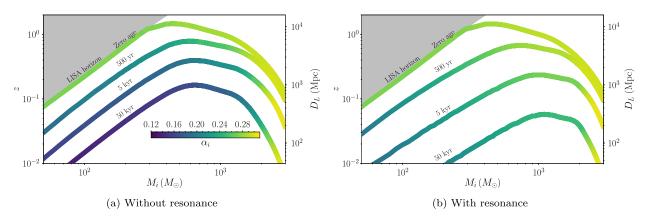


FIG. 7. Detection horizon as a function of M_i for $\chi_i = 0.9$ and for various $T_{\rm age}$ s, as indicated next to each curve. Color encodes the best α_i as described in the Sec. IV C. Equal-mass BBHs inside the grey region are not detectable by LISA ($\rho_{\rm LISA} < 8$). Panel (a) shows the horizons when resonant depletion is neglected, while panel (b) includes both the effects of resonant depletion and cloud dissipation. Orbital resonances have the general effect of reducing horizons.

resonances, systems with $M_i \lesssim 500~M_\odot$ are limited by the LISA SNR threshold if $T_{\rm age} \sim 0$, because the CE horizon lies outside the LISA one (gray region in Fig. 7) for those systems; otherwise, our observation is limited by the CE SNR threshold. Second, all curves follow a similar shape, reflecting the features of CE's PSD (cf. Fig. 1): for $M_i \lesssim 500~M_\odot$ ($f_{\rm CW} \gtrsim 20~{\rm Hz}$) CE's sensitivity is roughly constant and, because $h_0 \propto M_i/D_L$, the detection horizon increases with M_i ; then, as M_i increases further, $f_{\rm CW}$ falls out of the CE frequency band, and the detection horizon decreases. Third, and last, α_i increases with M_i in both panels: this is because CE is only sensitive to CW frequencies $\sim [10,300]$ Hz, and so $\alpha_i \propto M_i$ to stay within that range following Eq. (7).

There are also some features unique to both Figs. 7(a) and 7(b), which reflect the impact of resonances on detectability. The horizons are generally closer and the overall scale of α_i is higher in Fig. 7(b). This is because systems with the true optimal α_i experience resonant depletion before entering the LISA band, leaving us only with suboptimal configurations. As shown in Fig. 2, resonances prevent us from observing clouds with the overall optimal α_i 's (crosses) for $T_{\rm age} \gtrsim 1$ kyr; the best among the leftover α_i s (squares) lead to weaker signals.

V. INTERPRETATION

The results of the CW search must be translated into a statement about boson masses. Doing this is straightforward if a signal is indeed found: in that case, we would be able to establish that an ultralight boson exists and accurately infer its mass from a measurement of the CW frequency. Detailed tracking of the frequency and amplitude evolution would allow us to study the depletion of the cloud, infer its age, and potentially look for evidence of boson self-interactions. The CE measurement would also provide us with estimates of the BH spin before and after superradiance, complementing information provided by LISA. After establishing that at least one CW signal is present, the information gained could be used in a targeted search to determine whether both BHs are hosting a boson cloud each.

On the other hand, if a CW signal is not found by CE but an inspiral signal is observed by LISA, then we would want to cast upper limits on the strain amplitude into boson mass constraints. The translation is hindered by our lack of knowledge about the individual histories of the targeted BHs: ignorance about the cloud age and presuperradiance BH spin preclude a direct mapping from boson mass to expected CW strain (see Sec. IV). Thus, unless additional information is provided by other means, we will be limited to constraints on the χ_i - μ - $T_{\rm age}$ space (Figs. 3–6).

A significant limiting uncertainty in the interpretation of a null CW result in CE (with the presence of an inspiral in LISA) is the difficulty to reliably quantify $T_{\rm age}$ for any individual BH. The predicted lifetime of a cloud is in

general expected to be many orders of magnitude shorter than the time between BH formation in a supernova and the eventual merger of a BH binary. For simulated populations of BBHs formed in a galactic field, typical distributions of times between BBH formation and merger are $\mathcal{O}(Gyr)$ or larger, with a small-number tail reaching down to $\mathcal{O}(Myr)$ [79–82]. The majority of BBHs formed through dynamical interactions in dense stellar environments would, again from simulated populations, exhibit similar timescales [83–86], especially for binaries ejected from their formation environments (through supernova kicks). If such a binary is not ejected however, then the additional strong dynamical encounters to which the binary would be exposed would significantly decrease the time to merger and, thus, increase the possibility that a binary with BHs harboring boson clouds survive long enough for us to observe it. Binaries originating in dynamical environments can also be formed with significant eccentricities, or through direct captures [89–93], which would decrease the time to merger compared to an equivalent quasicircular orbit, and similarly increase the potential detectability of the two GW signals. Additionally, self-interactions of the boson field could lead to a prolonged cloud lifetime [94,95].

If there is no inspiral detection in LISA, then we cannot carry out a CW follow-up in CE, and hence can make no statements about bosons either.

Finally, the multiband technique proposed in this paper, specifically a ground-based CW follow-up of a space-based inspiral observation, is not limited to the search of ultralight bosons. Another possible application may be a CW follow-up of individual neutron stars in binaries observed by LISA to look for GWs from nonaxisymmetries in their moments of inertia [96].

VI. CONCLUSION

Future GW detectors on the ground and in space, like CE and LISA, will be able to work together to detect ultralight bosons with masses $25 \lesssim \mu/(10^{-15} \text{ eV}) \lesssim 500$. In detecting BBH inspirals, LISA will provide crucial information enabling CE to search for continuous GWs from boson clouds hosted by the component BHs (Fig. 1).

In this paper, we have laid out the detection strategy (Sec. III), explored the relevant parameter space (Sec. IV), and discussed the interpretation of possible measurement outcomes (Sec. V). Focusing on dominant ($\ell = m = 1$) scalar clouds, we have studied limitations on potential boson constraints imposed by ignorance about the histories of the individual systems, like their age and spin evolution (Fig. 3). We have also quantified the impact of orbital resonances, which may destroy the boson cloud before its CW signal becomes detectable by a CE follow-up (Fig. 4). We have shown how to take all of these factors into account, together with uncertainty in the parameters measured by LISA, in order to obtain boson mass constraints from the CE observation (Figs. 5–6). Finally, we plot

detection horizons as a function of component BH mass (Fig. 7). Although we focused on scalars, the conclusions can easily be extended to vectors, which lead to similar phenomenology with faster timescales and greater CW power.

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- R. D. Peccei and H. R. Quinn, Phys. Rev. Lett. 38, 1440 (1977).
- [2] R. D. Peccei and H. R. Quinn, Phys. Rev. D 16, 1791 (1977).
- [3] S. Weinberg, Phys. Rev. Lett. 40, 223 (1978).
- [4] M. Goodsell, J. Jaeckel, J. Redondo, and A. Ringwald, J. High Energy Phys. 11 (2009) 027.
- [5] A. Arvanitaki, S. Dimopoulos, S. Dubovsky, N. Kaloper, and J. March-Russell, Phys. Rev. D **81**, 123530 (2010).
- [6] J. Preskill, M. B. Wise, and F. Wilczek, Phys. Lett. 120B, 127 (1983).
- [7] L. Abbott and P. Sikivie, Phys. Lett. **120B**, 133 (1983).
- [8] M. Dine and W. Fischler, Phys. Lett. 120B, 137 (1983).
- [9] M.S. Turner and F. Wilczek, Phys. Rev. Lett. **66**, 5 (1991).
- [10] M. P. Hertzberg, M. Tegmark, and F. Wilczek, Phys. Rev. D 78, 083507 (2008).
- [11] J. Jaeckel and A. Ringwald, Annu. Rev. Nucl. Part. Sci. 60, 405 (2010).
- [12] R. Essig et al., in Proceedings, 2013 Community Summer Study on the Future of U.S. Particle Physics: Snowmass on the Mississippi (CSS2013): Minneapolis, MN, USA (2013), https://www.slac.stanford.edu/econf/C1307292/ docs/IntensityFrontier/NewLight-17.pdf.
- [13] L. Hui, J. P. Ostriker, S. Tremaine, and E. Witten, Phys. Rev. D 95, 043541 (2017).
- [14] A. Arvanitaki, S. Dimopoulos, M. Galanis, L. Lehner, J. O. Thompson, and K. Van Tilburg, Phys. Rev. D 101, 083014 (2020).
- [15] A. Arvanitaki and S. Dubovsky, Phys. Rev. D 83, 044026 (2011).
- [16] H. Yoshino and H. Kodama, Prog. Theor. Exp. Phys. 2014, 043E02 (2014).
- [17] H. Yoshino and H. Kodama, Prog. Theor. Exp. Phys. 2015, 061E01 (2015).
- [18] A. Arvanitaki, M. Baryakhtar, and X. Huang, Phys. Rev. D 91, 084011 (2015).
- [19] A. Arvanitaki, M. Baryakhtar, S. Dimopoulos, S. Dubovsky, and R. Lasenby, Phys. Rev. D 95, 043001 (2017).

- [20] R. Brito, S. Ghosh, E. Barausse, E. Berti, V. Cardoso, I. Dvorkin, A. Klein, and P. Pani, Phys. Rev. Lett. 119, 131101 (2017).
- [21] R. Brito, S. Ghosh, E. Barausse, E. Berti, V. Cardoso, I. Dvorkin, A. Klein, and P. Pani, Phys. Rev. D 96, 064050 (2017).
- [22] M. Baryakhtar, R. Lasenby, and M. Teo, Phys. Rev. D 96, 035019 (2017).
- [23] P. S. B. Dev, M. Lindner, and S. Ohmer, Phys. Lett. B 773, 219 (2017).
- [24] M. Isi, L. Sun, R. Brito, and A. Melatos, Phys. Rev. D 99, 084042 (2019).
- [25] S. Ghosh, E. Berti, R. Brito, and M. Richartz, Phys. Rev. D 99, 104030 (2019).
- [26] S. D'Antonio et al., Phys. Rev. D 98, 103017 (2018).
- [27] V. Dergachev and M. A. Papa, Phys. Rev. Lett. 123, 101101 (2019).
- [28] C. Palomba et al., Phys. Rev. Lett. 123, 171101 (2019).
- [29] L. Tsukada, T. Callister, A. Matas, and P. Meyers, Phys. Rev. D 99, 103015 (2019).
- [30] J. Huang, M. C. Johnson, L. Sagunski, M. Sakellariadou, and J. Zhang, Phys. Rev. D 99, 063013 (2019).
- [31] K. K. Ng, O. A. Hannuksela, S. Vitale, and T. G. Li, arXiv: 1908.02312.
- [32] P. Amaro-Seoane *et al.* (LISA Collaboration), arXiv: 1702.00786.
- [33] M. Punturo *et al.*, Classical Quantum Gravity **27**, 194002 (2010).
- [34] S. Dwyer, D. Sigg, S. W. Ballmer, L. Barsotti, N. Mavalvala, and M. Evans, Phys. Rev. D 91, 082001 (2015).
- [35] B. P. Abbott *et al.* (LIGO Scientific Collaboration), Classical Quantum Gravity **34**, 044001 (2017).
- [36] D. Reitze et al., Bull. Am. Astron. Soc. 51, 035 (2019).
- [37] W. E. East and F. Pretorius, Phys. Rev. Lett. **119**, 041101 (2017).
- [38] C. A. R. Herdeiro and E. Radu, Phys. Rev. Lett. 119, 261101 (2017).
- [39] W. E. East, Phys. Rev. Lett. 121, 131104 (2018).
- [40] J. Zhang and H. Yang, Phys. Rev. D 99, 064018 (2019).

- [41] D. Baumann, H. S. Chia, and R. A. Porto, Phys. Rev. D 99, 044001 (2019).
- [42] E. Berti, R. Brito, C. F. Macedo, G. Raposo, and J. L. Rosa, Phys. Rev. D 99, 104039 (2019).
- [43] D. Baumann, H. S. Chia, R. A. Porto, and J. Stout, Phys. Rev. D 101, 083019 (2020).
- [44] J. D. Bekenstein, Phys. Rev. D 7, 949 (1973).
- [45] J. D. Bekenstein and M. Schiffer, Phys. Rev. D 58, 064014 (1998).
- [46] R. Brito, V. Cardoso, and P. Pani, Classical Quantum Gravity 32, 134001 (2015).
- [47] R. Brito, V. Cardoso, and P. Pani, Lect. Notes Phys. 906, 1 (2015).
- [48] S. A. Teukolsky, Classical Quantum Gravity 32, 124006 (2015).
- [49] I. M. Ternov, V. R. Khalilov, G. A. Chizhov, and A. B. Gaina, Izv. Vuz. Fiz. 21, 109 (1978) [Sov. Phys. J. 21, 1200 (1978)].
- [50] T. J. M. Zouros and D. M. Eardley, Ann. Phys. (N.Y.) 118, 139 (1979).
- [51] S. L. Detweiler, Phys. Rev. D 22, 2323 (1980).
- [52] S. R. Dolan, Phys. Rev. D 76, 084001 (2007).
- [53] H. Witek, V. Cardoso, A. Ishibashi, and U. Sperhake, Phys. Rev. D 87, 043513 (2013).
- [54] W. E. East, Phys. Rev. D 96, 024004 (2017).
- [55] R. Penrose, Riv. Nuovo Cimento 1, 252 (1969) [Gen. Relativ. Gravit. 34, 1141 (2002)].
- [56] Y. B. Zel'dovich, Pis'ma Zh. Eksp. Teor. Fiz. 14, 270 (1971)[JETP Lett. 14, 180 (1971)].
- [57] Y. B. Zel'dovich, Zh. Eksp. Teor. Fiz. 62, 2076 (1972) [Sov. Phys. JETP 35, 1085 (1972)].
- [58] W. H. Press and S. A. Teukolsky, Nature (London) 238, 211 (1972).
- [59] T. Damour, N. Deruelle, and R. Ruffini, Lett. Nuovo Cimento 15, 257 (1976).
- [60] H. Furuhashi and Y. Nambu, Prog. Theor. Phys. 112, 983 (2004).
- [61] M. J. Strafuss and G. Khanna, Phys. Rev. D **71**, 024034 (2005).
- [62] K. Riles, Mod. Phys. Lett. A 32, 1730035 (2017).
- [63] V. Cardoso, F. Duque, and T. Ikeda, Phys. Rev. D 101, 064054 (2020).
- [64] T. Robson, N. J. Cornish, and C. Liu, Classical Quantum Gravity 36, 105011 (2019).
- [65] B. Sathyaprakash and B. Schutz, Living Rev. Relativity 12, 2 (2009).
- [66] P. C. Peters, Phys. Rev. 136, B1224 (1964).
- [67] A. Sesana, Phys. Rev. Lett. 116, 231102 (2016).
- [68] W. Del Pozzo, A. Sesana, and A. Klein, Mon. Not. R. Astron. Soc. 475, 3485 (2018).
- [69] A. Klein et al., Phys. Rev. D 93, 024003 (2016).
- [70] S. Suvorova, L. Sun, A. Melatos, W. Moran, and R. J. Evans, Phys. Rev. D 93, 123009 (2016).
- [71] L. Sun, A. Melatos, S. Suvorova, W. Moran, and R. Evans, Phys. Rev. D 97, 043013 (2018).

- [72] L. Sammut, C. Messenger, A. Melatos, and B. J. Owen, Phys. Rev. D 89, 043001 (2014).
- [73] C. Messenger and G. Woan, Classical Quantum Gravity 24, S469 (2007).
- [74] J. T. Whelan, S. Sundaresan, Y. Zhang, and P. Peiris, Phys. Rev. D 91, 102005 (2015).
- [75] S. Suvorova, P. Clearwater, A. Melatos, L. Sun, W. Moran, and R. Evans, Phys. Rev. D 96, 102006 (2017).
- [76] S. Marsat, J. G. Baker, and T. Dal Canton, arXiv: 2003.00357.
- [77] B. P. Abbott *et al.* (LIGO Scientific Collaboration), Instrument Science White Paper, LIGO Laboratory Tech. Report No. LIGO-T1600119, 2016.
- [78] K. Jani, D. Shoemaker, and C. Cutler, Nat. Astron. 4, 260 (2019).
- [79] M. Dominik, K. Belczynski, C. Fryer, D. Holz, E. Berti, T. Bulik, I. Mandel, and R. O'Shaughnessy, Astrophys. J. 759, 52 (2012).
- [80] M. Mapelli, N. Giacobbo, E. Ripamonti, and M. Spera, Mon. Not. R. Astron. Soc. 472, 2422 (2017).
- [81] M. Mapelli, N. Giacobbo, F. Santoliquido, and M. C. Artale, Mon. Not. R. Astron. Soc. 487, 2 (2019).
- [82] C. J. Neijssel, A. Vigna-Gómez, S. Stevenson, J. W. Barrett, S. M. Gaebel, F. Broekgaarden, S. E. de Mink, D. Szécsi, S. Vinciguerra, and I. Mandel, Mon. Not. R. Astron. Soc. 490, 3740 (2019).
- [83] M. J. Benacquista and J. M. Downing, Living Rev. Relativity 16, 4 (2013).
- [84] C. L. Rodriguez, P. Amaro-Seoane, S. Chatterjee, and F. A. Rasio, Phys. Rev. Lett. 120, 151101 (2018).
- [85] K. Kremer, C. S. Ye, N. Z. Rui, N. C. Weatherford, S. Chatterjee, G. Fragione, C. L. Rodriguez, M. Spera, and F. A. Rasio, Astrophys. J. Suppl. Ser. 247, 48 (2020).
- [86] F. Antonini and M. Gieles, Mon. Not. R. Astron. Soc. 492, 2936 (2020).
- [87] J. E. Greene, J. Strader, and L. C. Ho, arXiv:1911.09678.
- [88] B. P. Abbott *et al.* (LIGO Scientific and Virgo Collaborations), Phys. Rev. D **100**, 064064 (2019).
- [89] K. Breivik, C. L. Rodriguez, S. L. Larson, V. Kalogera, and F. A. Rasio, Astrophys. J. **830**, L18 (2016).
- [90] C.-J. Haster, F. Antonini, V. Kalogera, and I. Mandel, Astrophys. J. 832, 192 (2016).
- [91] K. Kremer et al., Phys. Rev. D 99, 063003 (2019).
- [92] M. Zevin, J. Samsing, C. Rodriguez, C.-J. Haster, and E. Ramirez-Ruiz, Astrophys. J. 871, 91 (2019).
- [93] J. Samsing, A. S. Hamers, and J. G. Tyles, Phys. Rev. D 100, 043010 (2019).
- [94] H. Yoshino and H. Kodama, Prog. Theor. Phys. 128, 153 (2012).
- [95] H. Yoshino and H. Kodama, Classical Quantum Gravity 32, 214001 (2015).
- [96] B. Abbott *et al.* (LIGO Scientific and Virgo Collaborations), Phys. Rev. D **100**, 024004 (2019).