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1 Adaptive Task Allocation for Multi-UAV Systems based
2 on Bacteria Foraging Behaviour

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12 **Abstract**

13 The foraging behaviour of bacteria in colonies exhibits motility patterns that
14 are simple and reasoned by stimuli. Notwithstanding its simplicity, bacteria
15 behaviour demonstrates a level of intelligence that can feasibly inspire the
16 creation of solutions to address numerous optimisation problems. One such
17 challenge is the optimal allocation of tasks across multiple unmanned aerial
18 vehicles (multi-UAVs) to perform cooperative tasks for future autonomous
19 systems. In light of this, this paper proposes a bacteria-inspired heuristic
20 for the efficient distribution of tasks amongst deployed UAVs. The usage of
21 multi-UAVs is a promising concept to combat the spread of the red palm
22 weevil (RPW) in palm plantations. For that purpose, the proposed bacteria-
23 inspired heuristic was utilised to resolve the multi-UAV task allocation prob-
24 lem when combatting RPW infestation. The performance of the proposed
25 algorithm was benchmarked in simulated detect-and-treat missions against
26 three long-standing multi-UAV task allocation strategies, namely opportunist-
27 ic task allocation, auction-based scheme, and the max-sum algorithm, and
28 a recently introduced locust-inspired algorithm for the allocation of multi-
29 UAVs. The experimental results demonstrated the superior performance of
30 the proposed algorithm, as it substantially improved the net throughput and
31 maintained a steady runtime performance under different scales of fleet sizes
32 and number of infestations, thereby expressing the high flexibility, scalability,
33 and sustainability of the proposed bacteria-inspired approach.

34 *Keywords:* Task allocation, unmanned aerial vehicles, distributed systems,
35 multi-UAV systems, bacteria inspiration, optimisation problem.

36 1. Introduction

37 The devastating economical impact of red palm weevil (RPW, *Rhyn-*
38 *chophorus ferrugineus* - Curculionidae: Coleoptera) infestation is recognised
39 globally, as it affects various palm species in 54 countries [1]. Mature beetles
40 burrow to a palm's stem and crown where they lay their eggs. At its larvae
41 stage, an RPW is at its most damaging stage, as it prospers within the palm,
42 damaging its vascular system [2, 3]. Early detection is difficult due the cryptic
43 feeding behaviour of the larvae and the palm's lack of visual symptom of
44 infestation. Nevertheless, early detection is crucial to combating the spread
45 of the infestation when it can still be treated by pesticides. Several techniques
46 are used to ease detecting RPW infestations, including chemo/olfactory sens-
47 ing by dogs, X-ray imaging, thermal imaging, and acoustic detection of RPW
48 larvae [4, 5, 6]).

49 The use of fleets of unmanned aerial vehicles (UAVs) is becoming in-
50 creasingly compelling for detect-and-treat (DAT) missions, where they are
51 utilised to assist in eradicating agricultural pests (e.g., [7, 8, 9]) and are con-
52 tinuously being improved, for instance, in terms of reducing communication
53 disturbances and improving synchronisation (e.g., [10, 11]). One of the major
54 challenges to this approach is the optimal partitioning of tasks across UAVs
55 such that the objective of the DAT mission is optimised. As a special case of
56 the NP-hard multi-robot task allocation (MRTA) problem, the multi-UAV
57 task allocation (MUTA) problem has attracted notable attention and is of-
58 ten approached using heuristics because of their fast development and ease
59 of application [12]. However, unlike optimal algorithms, heuristics are best
60 assessed empirically under controlled experimental conditions [13].

61 NP-hard problems, such as MRTA and MUTA, are typically approached
62 using heuristics that suggest 'good' solutions such as max-sum, auction-
63 based, and bio-inspired algorithms (e.g., [14, 15, 16]). The majority of such
64 approaches can be categorised as problem-independent heuristics, i.e., meta-
65 heuristics. A metaheuristic starts with a random solution that is iteratively
66 optimised until a near-optimal solution is reached. Implementing a meta-
67 heuristic is relatively easy because one algorithm can be utilised for every
68 agent, where parametrisation and neighbouring strategies can also be used to

69 reflect different behaviours. However, the iterative nature of metaheuristics
70 increases the power and time consumptions, thereby significantly impact-
71 ing the overall performance of the algorithm. The solution proposed in this
72 paper falls under the second category, i.e., it is a problem-dependent heuris-
73 tic. While more difficult to implement (multiple algorithms), a problem-
74 dependent heuristic is tailored to the specific problem, and its best-effort
75 approach attempts to achieve a good guess sans iterative improvements [17].
76 The choice between problem-dependent and problem-independent heuristics
77 is dependent on the nature of the optimisation problem and the trade-off
78 between the cost of implementation and runtime operation.

79 Optimisation problems can grow more difficult in a distributed setting and
80 are known as distributed constraint optimisation problems (DCOPs). The
81 max-sum metaheuristic is an approach that provides satisfactory approxi-
82 mate solutions to challenging decentralised optimisation problems [18]. The
83 metaheuristic approaches the optimisation problem by breaking its maximis-
84 ing function iteratively into a sum of smaller functions, where agents max-
85 imise the global utility based on their variables and constraints [19]. Max-sum
86 has been applied to many UAV application domains (e.g., [20, 14]); however,
87 the algorithm’s exponential running time, $O(m^n)$ (where m is the number
88 of agents and n is the number of tasks), and lack of support for situational
89 awareness are its main drawbacks. This is because the max-sum algorithm
90 does not take the dynamic environment into account nor does it consider
91 multiple task allocation objectives; thus, solutions are re-calculated in their
92 entirety to account for changes in the environment [21].

93 Auction-based heuristics offer a less expensive alternative to DCOPs and
94 decentralised decision making [22, 23, 16]. Auction-based heuristics approach
95 the MUTA problem by offering tasks for auction, where UAVs bid for allo-
96 cation pertaining to the cost of running the task. To solve conflicts and
97 determine the winning bid, a consensus approach is often implemented. The
98 adoption of auction-based allocation results in numerous issues such as the
99 complexity introduced by auctioning off new tasks. The heuristic is also
100 reputed to be time and resource consuming, as bids are calculated by each
101 UAV and a winning bid is chosen; resulting in quadratic time complexity
102 $O(n^2m)$, where m is the number of agents and n is the number of tasks [24].

103 Bio-inspired algorithms are based on the natural behaviour of simple
104 agents as they interact amongst themselves and exhibit favourable features,
105 such as self organisation, adaptiveness, and robustness [25]. This natural
106 behaviour is governed by simple rules that support their implementation and

107 economical execution. The majority of bio-inspired algorithms are concrete
108 mathematical and probabilistic models that quantify natural features that
109 are based on a certain set of predefined assumptions (e.g. [26]). Never-
110 theless, there has been a growing interest in utilising problem dependent
111 heuristics for overcoming complex optimisation problems. Recently, LIAM
112 was presented as a locust-inspired problem-dependent heuristic to optimise
113 the allocation of multi-UAVs in SAR missions [27, 17]. Locusts in nature
114 dynamically adapt to internal and external stimuli between solitary and gre-
115 garious roles. LIAM mimics the adaptive behaviours of locusts, which are
116 demonstrated in the system’s fully autonomous UAVs. The performance of
117 LIAM was comparatively assessed against auction, max-sum, ant colony op-
118 timisation (ACO), and opportunistic task allocation (OTA), where LIAM
119 was proven to be superior given the dynamic nature of SAR missions with a
120 higher net throughput and a shorter mean rescue time.

121 The simple behaviour of bacteria has continually been an inspiration for
122 computational practices and optimisation heuristics. Specifically, two heuris-
123 tics, bacteria foraging optimisation (BFO) [28] and bacterial chemotaxis (BC)
124 [29], have broadened the application scope of bacteria optimisation. The BFO
125 algorithm is inspired by the social foraging behaviour of bacteria and was ap-
126 plied to the continuous function optimisation problem domains [30]. In the
127 same year, the bacterial chemotaxis (BC) heuristic simulated the movement
128 of a single bacterium and evolutionary concepts to improve optimisation
129 strategies and problem-solving capabilities. Since the development of BFO
130 and BC, there has been a growing number of extensions that attempt to
131 hybridise the algorithms with other metaheuristics and computational intel-
132 ligence algorithms (e.g., [31, 32, 33, 34, 15]).

133 The bacterial colony chemotaxis (BCC) algorithm is based on the infor-
134 mation interactive model between bacteria via chemo-attractants [35]. Sev-
135 eral assumptions are made about bacterial colony correspondence: locomo-
136 tion self-regulation based on information from approximate bacteria and mi-
137 gration simulations. The algorithm has been applied to solve optimisation
138 problems in various fields, e.g., machine learning and inverse air-foil design
139 [36]. A scheduling algorithm, the super-bug algorithm (SuA), was similarly
140 inspired by bacteria [37], in particular, the antibiotic resistance developed
141 from bacterial mutation. SuA was comparatively assessed against other tech-
142 niques on the flexible manufacturing scheduling problem, where it performed
143 better in most cases. The viral infection process motivated the proposal of
144 the viral system algorithm, which consists of replication and infection mech-

145 anisms [38]. These mechanisms are used to generate meta-heuristics that
146 overcome computer security problems and virus elimination.

147 Inspired by bacteria-based algorithms, this paper presents a multi-UAV
148 task allocation for RPW combat based on bacteria behaviour (UTARB) al-
149 gorithm. Its main advantages over other MUTA approaches is the adaptive
150 behaviour of the UAVs and the autonomic nature of control and decision
151 making. Unlike other approaches, UTARB targets non-clairvoyant tasks and
152 is tailored to the particularities of DAT missions and tasks. By adopting a
153 problem-dependent heuristic approach, the proposed model ensures that the
154 optimization algorithm is easier and quicker to implement and more robust in
155 its adaptation. This is made possible by the algorithm as computationally ex-
156 pensive parameters are ignored, while simpler parameters that are indirectly
157 correlated with system performance are relied upon [39, 13]. Accordingly, the
158 proposed approach does not aim to prove a first-order relationship between
159 the proposed heuristic and the desired results.

160 A simulation model was built for DAT missions to thoroughly assess the
161 performance of the proposed algorithm and three long-standing heuristics:
162 auction-based, max-sum, and opportunistic coordination schemes, as a well
163 as a recently introduced locust-inspired heuristic for multi-UAV task alloca-
164 tion in search and rescue missions (LIAM) [17]. The experimental results
165 demonstrated the superiority of UTARB over the benchmark algorithms,
166 where it yielded a significant increase in the percentage of detected infesta-
167 tion at reduced runtimes. This paper extends on previous work [40] that
168 highlight the development of UTRAB to further signify its efficiency.

169 The main contributions of this paper can be summarised as follows:

- 170 • A new bacteria-inspired heuristic for MUTA problems, UTARB, is pro-
171 posed. The proposed algorithm is a problem-specific heuristic inspired
172 by the foraging behaviour of bacterial colonies for addressing the special
173 challenges of DAT missions.
- 174 • A well-controlled experimental framework for evaluating UTARB in
175 DAT missions is developed.
- 176 • A thorough investigation of the performance of UTARB is conducted
177 against well-established benchmark algorithms and a problem depen-
178 dent bio-inspired algorithm with different numbers of infested palms
179 and deployed UAVs.

180 The remainder of this paper is organised as follows. Section 2 reviews
181 existing work regarding the scheduling problem inspired by the behaviour of
182 fish and bio-inspired heuristics that were developed to address the problem
183 of multi-robot or multi-UAV task allocation. The following section, Section
184 3, describes the bacteria inspiration behind this work. Section 4 illustrates
185 the system model. Section 5 introduces UTARB’s search algorithms. Section
186 6 describes the experimental configuration and procedure for conducting the
187 simulations. Section 7 presents and explains the results of the comparative
188 evaluations. Finally, Section 8 concludes the paper and briefly discusses
189 future work.

190 2. Related Work

191 The past few decades have seen a shift of focus in the field of robotics
192 toward investigating problems of coordinating multiple robots. This is due
193 to the increasing complexity of multi-robot and multi-UAV systems as fleets
194 expand in size while agents and tasks increase in heterogeneity. As a re-
195 sult, the problems of multi-robot and multi-UAV coordination have received
196 significant attention. This section reviews numerous works that address the
197 MRTA and MUTA problems in various scenarios. The review is not meant
198 to be exhaustive, as it focuses on solutions proposed by the benchmark al-
199 gorithms (such as auction and max-sum heuristics) and biologically inspired
200 heuristics.

201 The max-sum algorithm was initially proposed for DCOPs in multi-agent
202 systems [41] and has since been utilised to address several other optimisa-
203 tion problems such as the allocation of tasks to multi-UAV fleets. Agents
204 in max-sum-based approaches can generate a consistent task allocation plan
205 by exchanging and adjusting the utility function, thus enabling cooperation
206 when performing tasks. A max-sum coordination mechanism was proposed
207 for a fleet of autonomous UAVs as they survey a disaster area to provide aerial
208 images [42, 43]. The task allocation problem is addressed asynchronously, by
209 which a computed utility value is maintained by the UAVs for each task.
210 The proposed model was assessed and exhibited promising potential, as it
211 provided a favourable trade-off between the quality and quantity of tasks
212 performed. Hardware tests were also conducted to assess the coordination
213 mechanism proposed using commercial off-the-shelf hexacopter UAVs de-
214 ployed in the real world, the results of which confirmed the performance of
215 the max-sum algorithm in coordinating UAVs in real-world situations. Nev-

216 ertheless, the empirical tests were not time constrained and were restricted
217 to ten surveying UAVs in a limited disaster area. The traceability of this
218 solution increases in difficulty as the number of tasks and agents sufficiently
219 increases due to the exponential number of constraints.

220 For urban disaster environments, a binary max-sum algorithm was pro-
221 posed for clustering-based task allocation [21]. Tasks in the proposed algo-
222 rithm are distributed using a distance metric between the agents' features
223 and tasks, along with the benefits of facto graphs with THOPs to optimise
224 a global objective function. The modelled heuristic was comparatively as-
225 sessed against an optimised multi-team task allocation model. The result
226 of the assessment demonstrated the algorithm's superiority, as it reduced
227 communication costs and non-concurrent constraint checks. The max-sum
228 algorithm was also adapted for decentralised coordination for the purpose of
229 considering constraints imposed by a human operator [44]. The algorithm
230 supports accountability for both human- and agent-based decision making
231 by providing a fully tracked provenance infrastructure in a disaster manage-
232 ment system prototype. Assessments were performed to address the inter-
233 action between agent and human operators, where the system demonstrated
234 improved performance as strong control is given to the user over autonomy
235 when allocating tasks.

236 Auction-based algorithms are one class of decentralised combinatorial al-
237 gorithms that have been utilised to efficiently produce suboptimal solutions
238 for the allocation of tasks over a team of agents. The algorithm is at times
239 augmented with a consensus protocol to resolve assignment conflicts among
240 agents. One such example is a consensus-based auction algorithm (CBBA)
241 that was proposed to negotiate between agents by forming an initial greedy
242 task allocation [45]. CBBA utilises an auction approach and a consensus pro-
243 cedure for task selection and conflict resolution, respectively. The final task
244 allocation is determined by achieving a consensus on the winning bid, thus
245 reducing computation costs and improving convergence. Experiment were
246 performed to assess the performance of CBBA against an existing sequential
247 auction algorithm. The performance of CBBA proved to be superior, showing
248 better convergence properties. Clustering-based task allocation was proposed
249 as a simulation model involving task priority and balancing in multi-robot
250 systems [46]. The model attempts to obtain a balanced exploration path by
251 considering the costs of robot travel and idleness, thus minimising the av-
252 erage waiting and completion times. The proposed methodology consists of
253 K-means clustering and auction-based mechanisms to achieve an appropriate

254 balance. Increased cluster numbers were found to significantly affect total
255 cost, and further studies are required to analyse their effect.

256 Several auction-based approaches were compared to assess their perfor-
257 mance for the efficient allocation of tasks for multi-robot teams in a dynamic
258 environment [22]. The effectiveness of the auction mechanisms in this study
259 considered the total distance of travel, cost of task execution, as well as how
260 well the task was executed. More recently, a cooperative rescue plan for
261 search and rescue missions is devised using an auction-based allocation ap-
262 proach [16]. The proposed auction approach is used to best allocate tasks to
263 rescue teams for the purpose of enhancing cooperation. A landslide post dis-
264 aster environment was built to demonstrate the performance of the proposed
265 algorithm with a non-cooperation rescue plan and F-max-sum. Findings
266 show that the proposed auction-based approaches increases the ratio of res-
267 cued survivors and the probability of survival. Additional evaluations were
268 conducted to determine the robustness and sensitivity of the proposed solu-
269 tion. Robustness analyses have shown that efficiency is significantly affected
270 by the search radius and, thus, that a high level of cooperation should be
271 maintained. The sensitivity analysis identified trade-offs between cooper-
272 ation, independent rescue searches and search coverage that greatly affect
273 rescue efficiency.

274 The collective behaviours of social insect colonies and animal groups are
275 characterised by self-organised control and collaboration, elastic properties
276 and effective interaction schemes [47]. These behaviours analogically align
277 themselves with distributed optimisation problems such as task allocation
278 and path planning. Bio-inspired algorithms that address the task allocation
279 problem considerably diverge depending on the species that they simulate.
280 These include, but are not limited to, algorithms inspired by the foraging
281 behaviours of locusts [17], ants [26] and honeybees [48] and the brood para-
282 sitism of cuckoos [49].

283 Locusts exhibit adaptable morphological and behavioural forms as they
284 advance through their lifecycle. Their behaviour is dramatically altered in
285 response to internal and external stimuli between two main phases: solitari-
286 ous and gregarious. Although there are few heuristics inspired by this type of
287 behaviour, a locust-inspired algorithm for task allocation in a multi-UAV dis-
288 tributed system performing SAR missions was recently proposed [27]. Locust
289 behaviour ideally maps to the main roles of SAR missions, search and rescue,
290 which behaviourally imitate solitary and gregarious locusts, respectively.
291 The effectiveness of the locust-based algorithm was compared against OTA in

292 terms of net throughput, survivor rescue time, and runtime performance. The
293 findings revealed the proposed algorithm’s superior net throughput compared
294 to the benchmark. The work was recently extended to best demonstrate the
295 adaptive behaviour of autonomous UAVs in multi-UAV SAR missions [17].
296 The locust-inspired task allocation (LIAM) algorithm was extensively tested
297 under various conditions of area scale, numbers of survivors, and the size
298 of the multi-UAV fleet. The experimental results demonstrated the superi-
299 ority of LIAM compared to well-established algorithms, primarily auction,
300 max-sum, ACO, and OTA algorithms. The proposed algorithm maintained
301 a significantly higher percentage of rescued survivors and reduced task com-
302 pletion time.

303 ACO is based on the behaviours of ant colonies as they forage for food.
304 Ants leave a trail of chemical pheromones to guide other ants to discovered
305 food sources; paths with strong concentrations of pheromones are given pri-
306 ority to support the search for the shortest path between the colony’s nest
307 and the food source [26]. ACO was proposed for MRTA, which utilises two
308 ant colony processes that use pheromones to allocate tasks to robots and
309 determine each robot’s task processing sequence [50]. A simulation environ-
310 ment was built for multi-robots transporting containers at a dock, where the
311 proposed ant-inspired algorithm was comparatively tested against another
312 algorithm that unified the problems of task allocation and path planning.
313 Several comparative scenarios were implemented with a variable number of
314 containers. The processing time of the proposed algorithm was comparatively
315 short, likely due to its simultaneous scheduling capability.

316 The ACO algorithm was also adapted to combat the task allocation
317 problem in multi-agent environments, thereby reducing processing times and
318 achieving global optimisation [51]. The proposed algorithm, collection path
319 ACO (CPACO), extends ACO by modifying the heuristic by establishing a
320 3-dimensional pheromone path to resolve the MUTA problem. The perfor-
321 mance of CPACO was comparatively assessed against gravitational search
322 and the forward optimisation heuristic. Although CPACO consumed more
323 time than the forward optimisation heuristic, CPACO’s efficiency was sub-
324 stantially better. Nonetheless, the proposed algorithm was sensitive to the
325 initial parameters and the number of ants to convergence. The dynamic
326 ant colony labour division (DACLC) algorithm was proposed to solve the
327 task allocation problem in a dynamic battlefield with a swarm of combat
328 multiple UAVs [52]. The proposed algorithm is based on the fixed response
329 threshold model (FRTM) that addressed the problem of adapting the system

330 to various demand levels. The effectiveness of DACLD was determined in
331 several simulated scenarios with varying numbers of targets and emerging
332 threats. DACLD was found to be robust and flexible in its dynamic alloca-
333 tion of tasks with a high degree of self-organisation. DACLD remains to be
334 compared against well-established algorithms.

335 As prokaryote, bacteria behave simply and in patterns that can easily be
336 described and mimicked computationally. The typical behaviours of bacte-
337 ria during their lifecycle, i.e., chemotaxis, communication, reproduction, and
338 migration, have inspired several general optimisation algorithms (e.g., BFO
339 [28] and BC [29]) that have since been applied to multi-robot mission optimi-
340 sation. An adapted implementation of BFO was proposed for a multi-robot
341 search and mapping of chemical gas concentration [53]. The robots in the
342 proposed algorithm perform the search autonomously via bacterial chemo-
343 taxis behaviour and send their sensed data to a ground station. In contrast
344 to the artificial bacteria behaviour in BFO, robots have continuous dynamics
345 and traverse all the paths between its current position towards a different
346 location. Therefore, the adapted BFO algorithm generates high-level path
347 planning and waypoints, which are used iteratively to compare chemical con-
348 centrations. The data received are then combined, interpolated, and filtered
349 to form a real-time map of chemical gas concentrations in an environment.
350 The performance of the implemented BFO was later evaluated against other
351 bio-inspired implementations (ACO and decentralised asynchronous particle
352 swarm optimisation), sweeping, and canonical particle swarm optimisation
353 [54]. The findings demonstrate the superior performance of the bio-inspired
354 implementation for concentration map building, where BFO and ACO were
355 able to complete their search.

356 A multi-robot path planning algorithm inspired by the original BFO for
357 known and unknown targets was developed [55]. A clustering-based method
358 was used to divide the area virtually, and bacteria-inspired direction-based
359 movement was utilised. The algorithm was tested for simple and complex
360 environments, where the results showed that the proposed algorithm was
361 able to efficiently perform path planning to the classified targets. Similarly,
362 the BFO algorithm was applied to the problem of mobile robot navigation
363 to determine the shortest path to a target position in an unknown environ-
364 ment with moving obstacles [56]. Particles are randomly distributed around
365 a robot, by which the best particle is selected based on the distance to the
366 target and a cost function. The selection of the best particle is generated
367 using a high-level decision strategy, and the robot proceeds to its target.

368 The efficiency of the proposed approach was assessed against the standard
369 BFO and particle swarm optimisation. The findings showed that the pro-
370 posed bacteria- and particle-inspired algorithm produces better solutions and
371 optimal paths.

372 A self-organisation algorithm inspired by the behaviour of bacteria was
373 proposed for multi-robot target search and trapping [57]. Target search and
374 trapping tasks were achieved by the robots using bacteria chemotaxis guided
375 by the gradient information obtained from the target until the target was
376 located. Simulations were conducted to assess the performance, robustness,
377 and complexity of the proposed algorithm. The findings demonstrated the
378 effectiveness of the algorithm and robustness under unanticipated failures.
379 The results also proved the algorithms ability to avoid being trapped in lo-
380 cal optima and its computational efficiency. The BFO algorithm was also
381 the source of inspiration and improvement for multi-robot cooperation for
382 nanarobotics and nanomedicine [58]. Referred to as the improved BFO al-
383 gorithm (IBFOA), the proposed methods utilised cooperative learning for
384 multiple nanorobots to reach and eradicate cancer cells in a blood vessel.
385 The performance of the proposed IBFOA algorithm was compared against
386 the standard BFO algorithm. The findings demonstrated the superior perfor-
387 mance of IBFOA, as it reduced time complexity and improved global search.

388 Previous work, be it based on conventional approaches (e.g., auction and
389 max-sum) or swarm intelligence, would often introduce general optimisation
390 solutions for the MUTA problem (i.e., problem-independent heuristics and
391 metaheuristics) rather than tailored algorithms that consider the particulari-
392 ties of the mission or task (i.e., problem-dependent heuristics). Moreover,
393 to the best of our knowledge, the behaviour of bacteria has not been previously
394 adapted for non-clairvoyant MUTA tasks where job information is unknown
395 a priori.

396 **3. Bacteria Inspiration**

397 Natural systems consist of simple agents that interact with each other by
398 abiding to simple rules. These agents are self-organised and are capable of
399 adapting to changing requirements and environments. These properties en-
400 able natural systems to solve complex problems that are beyond the abilities
401 of current computer systems [59, 60, 61]. The simple agents and rules of natu-
402 ral systems of many organisms have been simulated to govern task allocation
403 (e.g., [17, 52]), resource management (e.g., [62, 63]), synchronisation (e.g.,

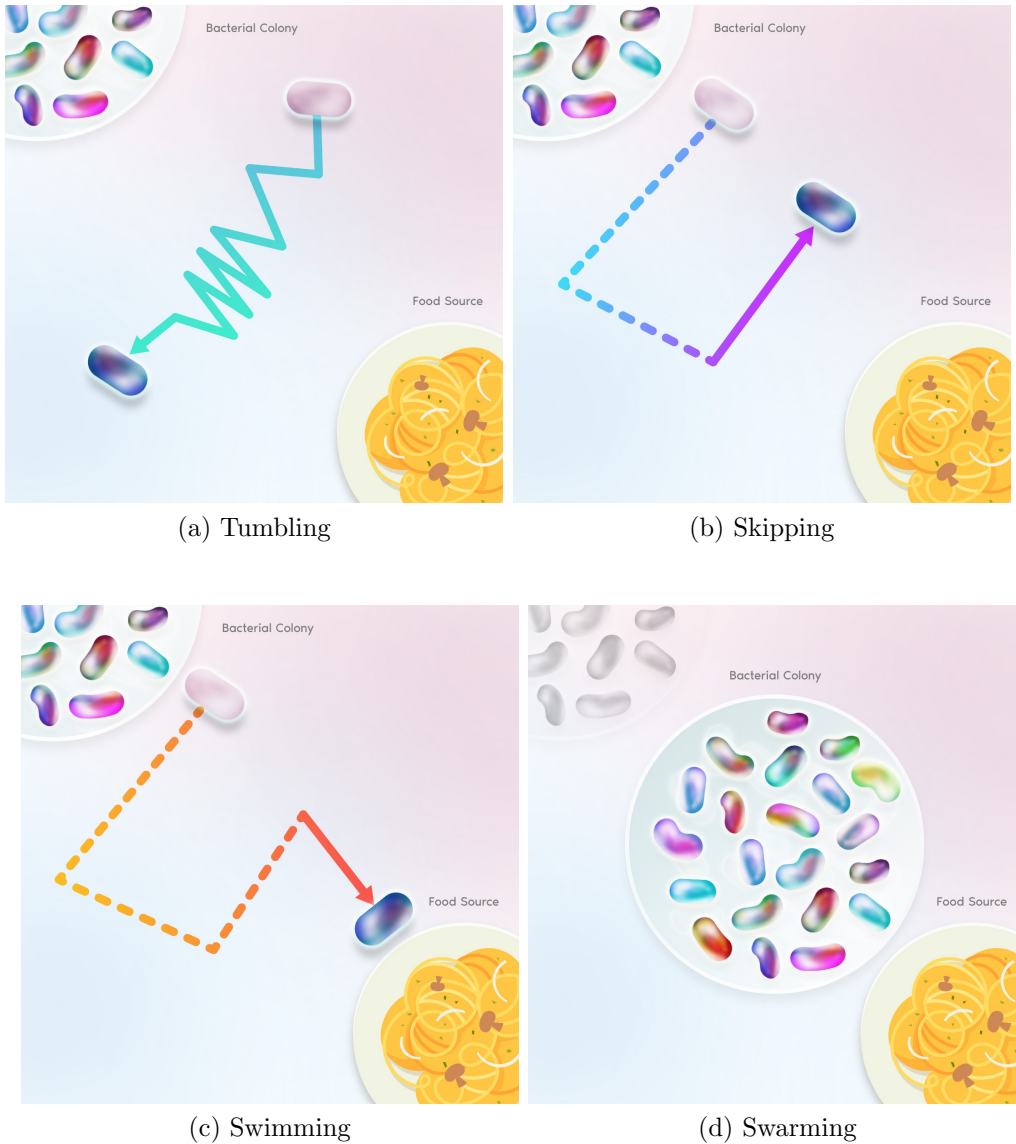


Figure 1: Bacteria foraging behaviour as a bacterium moves from a starting to an end position with lines depicting its movement.

404 [64, 65]), and social differentiation (e.g., [66, 67]). For many swarm organ-
 405 isms, the foraging process involves the aggregation of organisms into groups
 406 to search for sustenance by maximising the energy obtained per unit time

407 spent foraging [68]. The aggregation of organisms into social foraging groups
408 is also a key element for avoiding predators and increasing their chances of
409 finding profitable food sources [69]. Bacterial colonies exhibiting movement
410 during foraging show some intelligence that cannot be simply regarded as
411 random or arbitrary [60, 70, 30, 68].

412 The mobility of bacteria can be divided into four types, as shown in
413 Figure 1: tumbling, skipping, swimming, and swarming. In the absence of
414 stimuli, a bacteria cell forages for nutrients in random directions; it moves in
415 a straight line for some time, then changes its angle and repeatedly moves in a
416 certain pattern for an arbitrary amount of time and as long as no stimulus
417 is experienced. This tumbling behaviour serves to randomly reorient the
418 bacteria. Bacteria typically alternate periods of tumbling and swimming.
419 In the latter instance, the bacteria is in the presence of a stimulus and thus
420 moves directly towards it. Tumbling and swimming are collectively known as
421 chemotaxis, where bacteria direct their movement based on the presence of
422 chemical gradients, i.e., stimuli [69, 71]. As a bacteria cell tumbles for a long
423 period of time without encountering a stimulus, it significantly changes its
424 direction by skipping towards a new course. Bacteria secrete attracting and
425 repelling chemicals into the environment to communicate. If a food source
426 is found, a bacterial cell releases attractants for other bacteria to sense and
427 swarm around the source. If a stimulus is found to be revolting, the bacteria
428 cell releases repellents for others to keep away from the stimulus [72, 60].
429 This continuously changing strategy for selecting a search point based on the
430 current situation is the source of inspiration for this work.

431 4. System Model

432 When building a system model, the system is simplified to its main prop-
433 erties and functions. Nominally, system models are classified as: (1) mathe-
434 matical or analytical models, and (2) simulation models. Mathematical mod-
435 els provide an abstraction of the system, which are represented as equations
436 that summarise the system performance. Simulation models, on the other
437 hand, experimentally mimic events that occur in the real system. Thus,
438 allowing experimentation with different parameters and control logic [73].

439 Several works that mathematically model the foraging behaviour of bac-
440 teria have already been published and reviewed in Section 2. These models
441 quantify the features of the foraging behaviour of bacteria colonies based on a
442 set of predefined assumptions. The rigidity of these mathematical approaches

443 are built upon assumptions that are different from the unique characteristics
444 of biological systems. For instance, analytical models measure the system
445 behaviour using expected values for a predefined set of performance metrics,
446 which ignore any changes in the system behaviour over time [74]. This dis-
447 regards the flexibility of natural systems that typically employ an adaptive
448 control strategy to persevere in a changing world.

449 This paper presents a generic model for UTARB that is simulated in
450 several representative scenarios. The proposed system is comprised of a finite
451 number of UAVs in a multi-UAV fleet and a finite number of infested palms
452 in a plantation area. Each UAV is capable of executing one task at a time.
453 The goal of UTARB is to assign detect-and-treat tasks to UAVs to maximise
454 the overall number of detected and treated infested palms, considering the
455 urgency of the infested case and efficiency of the UAVs in conducting the
456 task.

457 The proposed system is comprised of three main components:

- 458 • The *palm plantation* is a physical agricultural field that consists of palm
459 trees that are to be investigated for RPW infestations.
- 460 • In almost all multi-UAV missions, a *ground station* is required to con-
461 trol and manage the running of the mission. In the case of UTARB,
462 the role of the ground station is limited to sending the mission require-
463 ments and the variables necessary for initialising the mission. Upon
464 mission completion, a mission report detailing the outcome is sent to
465 the ground station.
- 466 • The *UAVs* are a group of agricultural systems with built-in capabilities
467 for flying and collision avoidance. The agents are equipped with various
468 sensors such as piezo electric microphones, pesticide containers and
469 injectors. UAVs are programmed offline and autonomously fly to detect
470 infestation and treat palms as needed.

471 The simulation environment considers a DAT mission with the number,
472 severity level, and locations of infested palms unknown a priori. Each in-
473 fested palm is randomly assigned a severity level, which deteriorates as the
474 mission time passes. Infested palms are scattered across the plantation area
475 arbitrarily, with some hotspots representing areas with a potentially greater
476 concentration of infested palms. An infested palm can be in one of two states:

- 477 • A palm with a *mild* infestation that can be remedied using the UAV's
478 built-in pesticide injectors. A mild infestation deteriorates to severe if
479 not detected within a certain time period.
- 480 • An infested palm with a *severe* infestation which requires contact with
481 the ground station to call for help.

482 The plantation area is divided into logical blocks. Each set of blocks in a
483 row is referred to as a *region*. Each block has a size of $a \times b$, where a and b
484 are positive integers. The size of the block is determined during initialisation
485 and assumes one palm per block. Each block can be in one of the following
486 states:

- 487 • An *unchecked* block has yet to be checked for infestation by a UAV.
488 This is the initial state for all blocks.
- 489 • A *healthy* block contains a palm that is free of infestation.
- 490 • A *treated* block is comprised of a mildly infested palms that has since
491 been treated by a UAV.
- 492 • A *severe* blocks has a severely infested palm that has been detected by
493 a UAV and the ground station has been contacted for help.
- 494 • A *skipped* block refers to a block that has been temporarily bypassed
495 since a UAV assigned to the region has scanned a certain percentage of
496 the region ($P\%$) and no infestations were detected in the other blocks.

497 Blocks that are labelled as *unchecked* or *skipped* can further be categorised
498 based on their level of urgency. The urgency of a block is set by the UAV after
499 discovering an infested palm in a neighbouring block. The level of urgency
500 for *unchecked* and *skipped* blocks are set as follows:

- 501 • An *unchecked* or *skipped* block urgency is set to *very urgent* when a
502 severely infested palm is discovered in its vicinity. In other words, if a
503 palm is discovered to be severely infested, the the urgency level of its
504 direct neighbours (i.e., the eight blocks surrounding the infested block)
505 are set to *very urgent*.
- 506 • An *unchecked* or *skipped* block urgency is set to *urgent* when a mildly
507 infested palm is discovered in its vicinity.

508 Urgency levels are useful, as they allow the UAVs to target the infested region
509 mimicking the behaviour of bacterial swarming.

510 A region is comprised of a row of blocks and the status of a region is
511 dependent on the status of its blocks. The state changes as the UAVs explore
512 blocks and regions and act accordingly. A region can be in one of the following
513 states:

- 514 • A region's state is *unchecked* when all of its blocks are similarly *unchecked*.
515 This is the initial state for all blocks and regions.
- 516 • A region is *pending* when at least one block in the region is *skipped* or
517 *unchecked*.
- 518 • A region's state is *checked* once all of its blocks have been checked for
519 infestation.

520 Figure 2 illustrates UTARB's abstract system architecture. The figure shows
521 a plantation area with a number of healthy and infested palms. Region A
522 is marked as *pending* as it contains one *skipped* block that was skipped by
523 the UAV since a consecutive percentage of blocks were labelled as *healthy*,
524 i.e. the palms were not infested. In Region B, a UAV treated three mildly
525 infested palms (B1, B3, B4) and one block was labelled as *severe* and await-
526 ing elimination, thus, the region is marked as *checked*. Since block B2 was
527 labelled as *severe*, all *skipped* and *unchecked* neighbouring blocks were tagged
528 as *very urgent*, such as blocks C1 and C2. This indicates that priority should
529 be given to blocks marked as *very urgent*. An *unchecked* block, C3, in Region
530 C contains a mildly infested palm that is about to be treated by the UAV.
531 Once the palm is injected with the pesticide, block C3 will be labelled as
532 *treated*. Subsequently, all *skipped* and *unchecked* neighbouring blocks to C3
533 were tagged as *urgent* (i.e. D3 and D4 in Region D).

534 The wide objective of UTARB is to maximise the net throughput with
535 minimal cost to the running time of the algorithm, which ensures the proba-
536 bility of halting the spread of RPW infestation. For simplicity, it is assumed
537 that several charging and pesticide filling stations are available throughout
538 the plantation to ensure infinite battery lifetime and immediate pesticide re-
539 fills. These are valid assumptions, as RPW DAT missions are not time critical
540 and resources are usually easy to deploy and reach compared to search-and-
541 rescue and military missions.



Figure 2: The UTARB system abstract architecture.

542 **5. Proposed Method**

543 The task allocation algorithm is the core component of the UTARB sys-
 544 tem. A task allocator component runs in each UAV to allow for autonomous
 545 distributed decision making when allocating tasks, i.e., which block should
 546 be assigned to which UAV and when. To achieve this, the mission time is
 547 divided into two phases: exploratory search and extensive search. The DAT
 548 mission begins by receiving specifications from the ground station so that
 549 each UAV can be initialised according to the mission requirements.

550 *5.1. Exploratory Search Algorithm*

551 Exploratory search is the first phase in the DAT mission. This phase
 552 implements the four main procedures that mimic the behaviour of mobile
 553 bacterial cells as they forage for food (see Section 3). These behaviours can
 554 be summarised in the exploratory search phase as follows:

- 555 • **Tumbling (random selection):** The tumbling behaviour of bacteria is

556 mimicked by UAVs at the start of the mission. In this case, UAVs
557 select unchecked regions randomly.

558 • **Skipping:** The skipping bacteria behaviour is mimicked in the algorithm
559 by skipping *unchecked* blocks when a certain consecutive percentage
560 ($P\%$) of the blocks was healthy.

561 • **Swimming:** After a region is selected by a UAV, the UAV scans the
562 region's block consecutively from left to right or right to left (depending
563 on the block's location). This procedure is similar to that of the
564 swimming behaviour of bacteria as they respond to a stimulus.

565 • **Swarming:** In the exploratory search algorithm, swarming is performed
566 implicitly by UAVs without team communication. This is possible with
567 the urgency labels attached to blocks. In this case, blocks in close
568 vicinity to infested blocks attract UAVs due to the higher probability
569 of infestation. This procedure closely mimics the swarming behaviour
570 of foraging bacteria.

571 These procedures are illustrated in the exploratory search flowchart in Figure
572 3 and presented as pseudocode in Algorithm 1.

573 As depicted in Figure 3 and Algorithm 1, the exploratory phases of the
574 DAT mission commences with each UAV randomly selecting a block to ex-
575 plore. The selection is typically based on the urgency level of a block, which
576 is not the case when the mission first starts and the urgency is not yet de-
577 termined. The UAVs check the infestation level of each block and respond
578 accordingly. If a palm is infestation free, then the block is tagged as *healthy*.
579 A mildly infested palm is treated by the UAV and tagged as such. Addi-
580 tionally, the urgency level of the neighbouring blocks of the mildly infested
581 palm is set to *urgent*. If a palm seems to be severely infested, then the UAV
582 calls the ground station for help, and the block's state is set to *severe*. The
583 urgency level of all neighbouring blocks is also updated to *very urgent*.

584 The skipping behaviour of bacteria is mirrored early on to determine if a
585 certain consecutive percentage ($P\%$) of the region has been scanned without
586 infestation. This is because the likelihood of the remainder of the region being
587 infestation free is relatively high, and thus, the remainder of the blocks in the
588 region are skipped. If this is not the case, the bacterial swimming behaviour
589 is adopted to move to the next *unchecked* block in the region. Once all blocks
590 are checked in the region, the UAV will scan an *unchecked* region if available

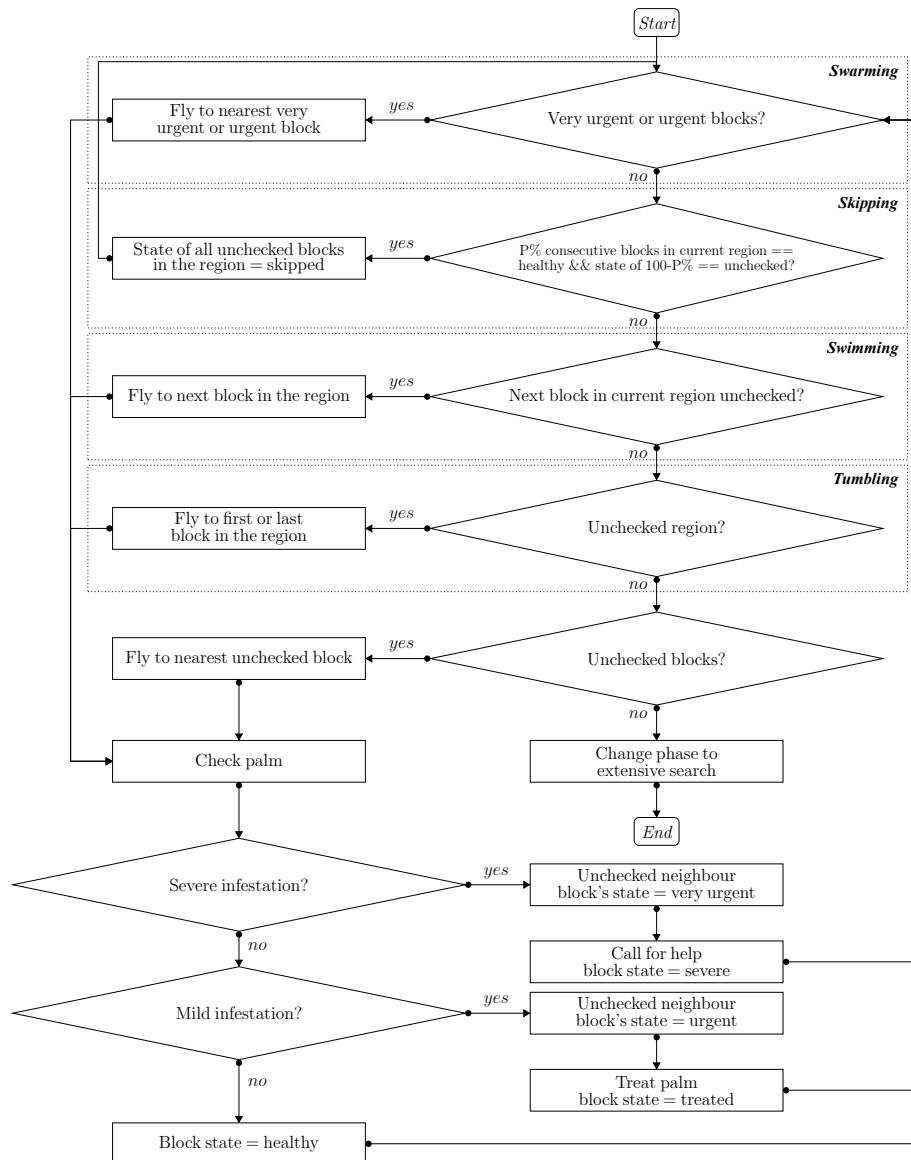


Figure 3: The UTARB system exploratory search flowchart.

Algorithm 1: The proposed algorithm’s exploratory search.

```
1 repeat
2   if there are any very urgent or urgent blocks then
3     | Fly to nearest very urgent or urgent block           //Swarming
4   else if state of  $P\%$  consecutive block in current region is healthy and state of  $100 - P\%$  of
      block is unchecked then
5     | State of all unchecked blocks in the region = skipped           //Skipping
6   else if there is an unchecked block in current region then
7     | Fly to the next block in the region                       //Swimming
8   else if there is an unchecked region then
9     | Fly to first or last block in the region                 //Tumbling
10  else if there are unchecked blocks then
11  | Fly to nearest unchecked block
12  else if there are no unchecked blocks then
13  | Change phase to extensive search
14  After selecting a block to detect, check palm
15  if palm is severely infested then
16  | Unchecked neighbors’ blocks state = very urgent
17  | Call for help
18  | Block state = severe
19  else if the palm is mildly infested then
20  | Unchecked neighbors’ blocks state = urgent
21  | Treat palm
22  | Block state = treated
23  else
24  | Block state = healthy
25 until no unchecked blocks remain
```

591 (i.e., tumbling behaviour), or it randomly selects an *unchecked* block in other
592 regions. This process continues until all blocks have been checked.

593 Once a palm is reached via the swarming, skipping, swimming or tum-
594 bling behaviour, it is then checked for infestation. This, in turn, determines
595 the state of the palms and urgency levels for neighbouring palms. The ex-
596 ploratory phase concludes with at least one skipped block. At this time, the
597 UAVs switch to the extensive search phase.

598 5.2. Extensive Search Algorithm

599 In the extensive search cycle, skipped blocks are checked for infestation.
600 The task allocation in the extensive search phase is significantly simpler (see
601 Figure 4 and Algorithm 2). A greedy approach is utilised, where each UAV
602 selects the nearest skipped block to check and tag according to the palm’s
603 state.

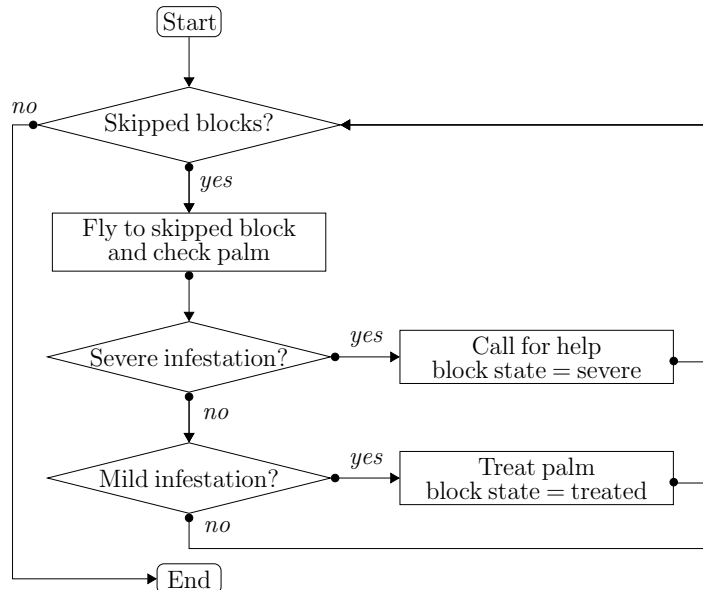


Figure 4: The UTARB system extensive search flowchart.

604 6. Evaluation

605 The paper aims to introduce UTARB as a bio-inspired algorithms for DAT
 606 missions. The primary hypothesis is that relative to the benchmark algo-
 607 rithms, utilising UTARB in DAT missions will maximise the net throughput
 608 without cost to the running time of the algorithm at various problem scales
 609 in terms of the number of UAVs and infestations with a set mission time. A
 610 well controlled empirical evaluation framework was developed to evaluate the
 611 performance of the proposed algorithm and test the hypothesis. A flexible
 612 Java simulator (MASPlanes++) was built based on MASPlanes multi-UAV
 613 simulator [75] using Java SDK 1.6 and Maven 2.0. MASPlanes++ allows
 614 for dynamic illustrations of multi-agent missions that are composed of two
 615 groups of tasks, such as is the case for DAT missions. The simulations were
 616 conducted on a computer with an Intel Core i7 processor at 2.8 GHZ and
 617 paired with 16 GB of RAM operating at 1866 MHz.

618 The evaluation framework considers the scalability of the proposed and
 619 benchmark algorithms to a larger number of UAVs, and the algorithms sus-
 620 tainability under larger number of infestations. For this purpose, two context
 621 parameters are controlled in the simulations to represent samples of DAT

Algorithm 2: The proposed algorithm’s extensive search.

```
1 repeat
2   if there is a skipped block then
3     Fly to this block
4     Check palm
5     if palm is severely infested then
6       Call for help
7       Block state = severe
8     else if the palm is mildly infested then
9       Treat palm
10      Block state = treated
11 until all skipped blocks are detected
```

622 missions:

- 623 • The number of UAVs was logarithmically increased to the power of 2 to
624 illustrate the performance of the algorithms in six different fleet scales:
625 $2^{\hat{k}}$, $k = 2, \dots, 7$ UAVs.
- 626 • The number of infested palms was similarly logarithmically increased
627 to the power of 2 at a larger scales, where 12 values for the number of
628 infested palms was considered: $2^{\hat{k}}$, $k = 1, \dots, 12$ infested palms.

629 The performance of UTARB was evaluated against a total of three bench-
630 mark algorithms (auction-based, max-sum, and LIAM), as well as OTA which
631 was used as a baseline. The total number of developed scenarios was 288:
632 number of heuristics (4) \times number of values for the number of infestations
633 (12) \times number of values for the number of UAVs (6). Further simulations
634 were carried out with the proposed algorithm at a larger plantation scale
635 to include 72 additional simulations, with a total of 360 scenarios. Each
636 scenario was executed 10 times to reduce the variability of the performance
637 metrics.

638 The OTA scheme is used as a baseline performance measure, which simply
639 allocates UAVs to search the nearest block in the plantation area that has yet
640 to be explored. If an infested palm is discovered, the UAV treats the palm
641 and then resume its search for more infestations using the same strategy [27].

642 A typical auction-based coordination strategy commands all UAVs to
643 search the plantation area and report a list of infestations found and their
644 locations at the earliest upcoming auction event. A cost function for each
645 infested palm, as well as the UAV’s own ongoing tasks, is evaluated to place

646 a bid. Infested palms are then assigned to the winning bidder by the auc-
647 tioneer UAV. Once all infested palms are assigned to bid winners, the UAVs
648 commence treating the infested palms and continue to do so until the next
649 upcoming auction event occurs or the assigned treat tasks are completed.
650 Once the tasks are completed and unchecked blocks still remain in the plan-
651 tation area, the UAV will return to detect infestations until the next auction
652 event occurs [76, 77].

653 The third benchmark algorithm, max-sum coordination, is an alternative
654 form of the auction-based strategy. The algorithm performs a detect cycle
655 similar to that of the auction algorithm. For the treat cycle, the agents
656 perform a specific repetition of a non-greedy distribution algorithm. This
657 algorithm uses factoring to allocate all the infested palms between the agents
658 in an optimal distribution. The algorithm also depends on specific costs
659 such as those associated with the battery, capacity, and infestation level
660 factors. After repeating the max-sum algorithm, each infested palm is re-
661 assigned if new optimal agents are available to treat these infested palms. As
662 with the auction algorithm, the agents then continue to conduct their new
663 assignments until the next round of max-sum repetitions, or if no infested
664 palm assignments remain, each agent is restored as a detect agent if the
665 search area has not been completely explored.

666 The last benchmark algorithm is LIAM, a recently proposed heuristic
667 that is inspired by the behaviour of locusts. The swarm behaviour of locusts
668 is well-known as millions can gather to form huge swarms, while also being
669 able to exist in solitary. This role-changing behaviour presents a biological
670 example of adaptive control in response to internal and external stimuli [27].
671 LIAM was developed to mimic this behaviour and exploit the role changing
672 property of locusts [17]. This is similar to the behaviour of agents in UTARB,
673 where roles adapt to the environment. In the original paper, searcher UAVs
674 start off as scout UAVs that follow a random search strategy at low speed and
675 short distances. As all search areas are assigned, scouts change their roles
676 to eagle UAVs where a guided search strategy is adopted at a medium speed
677 for medium distances. Standby UAVs are not involved in the search process,
678 however they are available for on-demand rescue with intermittent flights at
679 high speed for long distances. The original LIAM was proposed for search and
680 rescue mission and was thus adapted to DAT missions to comparatively assess
681 the performance of UTARB. This is possible since LIAM is not limited to
682 search and rescue missions and can be applied to other missions that involve
683 dynamic allocation of two groups of task in multi-agent systems.

Table 1: Parameter settings of the evaluation environment.

Parameters	Settings
	100 × 100 regions
Plantation area size	100 blocks per region
	8 × 8 meters block size
Hotspots	10; radius: 200 meters, DOF: 2.5
Plane maximum speed	40 miles/hour
Block detect power consumption penalty	5 units of power
Block detect time penalty	10 seconds
Palm treatment power consumption penalty	10 units of power
Palm treatment time penalty	60 seconds
Idle power consumption	1 unit of power/300 millise- conds
Standard power consumption	1 unit of power/100 millise- conds

684 Two performance metrics were measured for each scenarios: net through-
685 put and algorithm running time. The net throughput is used to measure the
686 total number of detected and treated palms in the simulations. The second
687 metric, algorithm running time, measures the time from when the simulation
688 starts until its end. The latter measure is used to indicate the algorithm’s
689 complexity. The standard deviation for both metrics was also calculated to
690 indicate the extent of the deviation across the ten trials for each of the 360
691 scenarios.

692 The simulated plantation area is comprised of a number of infested palms,
693 where the locations, infestations level, and scattering were randomised to
694 best simulate representative samples in all the experiments. The location
695 of the infested palms were randomly generated using multivariate normal
696 distributions that simulate hotspots of a specified radius. These hotspots
697 showcase infested palms that are clustered together and are more likely to
698 support the spread of RPW infestation. Several variables were generated
699 and stored as test scenarios to ensure the repeatability of the testing process.
700 This includes: number of infested palms, infestations level, palm locations,
701 and the number of UAVs. At the start of each simulation, the initial locations
702 of the UAVs is randomly generated to introduce variability and imitate real-
703 world scenarios.

704 In the simulation, the plantation area was modelled as an area of size 100
705 \times 100 regions (with 8×8 meter blocks). The maximum UAV speed was
706 40 miles/hour. The power consumption was uniform across all UAVs and
707 power is assumed infinite for all. However, penalties were applied every time
708 a block was explored (5 units of power) and a palm was treated (10 units
709 of power). Time penalties of 10 and 60 seconds were also assumed when
710 exploring a block and treating an infested palm, respectively. The power
711 consumption during idle time and standard operational time was 1 unit of
712 power/300 milliseconds and 1 unit of power/100 milliseconds. Hotspots are
713 randomised locations simulated with a specific radius using a multivariate
714 normal distribution, with a total of ten 200-meter-radius hotspots. Table
715 1 displays the parameter settings of the simulation environment that are
716 utilised by UTARB and the benchmark algorithms (OTA, auction-based,
717 max-sum, and LIAM). Further simulations were carried out for UTARB in
718 a plantation area that was modelled as an area of size 1000×1000 regions
719 with 8×8 meter blocks. The rest of the environment’s parameters were
720 maintained as presented in Table 1.

721 The MASPlanes multi-UAV simulator sustains defaults values for the
722 auction-based and max-sum algorithms which were suited to the scenarios
723 simulated in this paper. In the auction-based algorithm, auctions were con-
724 ducted every 0.5 seconds and bids placed by UAVs are dependent on the
725 auctioned task’s cost. For the max-sum algorithms, the number of max-sum
726 iterations to the point of reaching a decision was set at 9 iterations. The
727 number of iterations between max-sum cycles was set at 10 iterations. Co-
728 ordinations between the UAVs in the max-sum algorithm was via workload
729 auctions. LIAM maintains several roles to mimic the behaviour of locusts:
730 Scouts, Eagles, and Standby UAVs. LIAM introduces penalties for conver-
731 sion from one to another, primarily a loss of approximately 44% of the battery
732 capacity to convert a Scout UAV to Eagle UAV and approximately 8% to
733 convert an Eagle UAV to Standby UAV. These roles and their parameters
734 are described in the original paper and were utilised for the simulations [17].

735 For each scenario, the experiment was repeated ten times. The results
736 were then averaged and presented in lin-log graphs defined by a logarithmic
737 base-2 scale, with the number of UAVs on the x-axis, and with a linear scale
738 for the performance measures on the y-axis (net throughput and algorithm’s
739 running time). Lin-log graphs employing a logarithmic axis allow for simulta-
740 neous comparisons of data points drawn from a wide range of UAVs (4-128).
741 The standard deviations was also collected for the ten trials to present the

742 spread out from the computed average.

743 **7. Results and Discussion**

744 The performance of UTARB is analysed in this section on DAT mis-
745 sions against four benchmark algorithms: OTA strategy, auction algorithm,
746 max-sum coordination, and LIAM. The following subsections examine the
747 performance of the four algorithms considering the two performance met-
748 rics: net throughput and algorithm running time. The analysis is conducted
749 separately for each of the metrics.

750 *7.1. Net Throughput*

751 The net throughput of the system was computed by collecting the total
752 number of detected and treated palms in each scenario. The percentage of
753 detected and treated palms is plotted against the number of UAVs as the
754 number of infestations is increased exponentially from 2 to 4,096 infestations
755 (see Figure 5). The different scenarios are presented using radar graphs,
756 where the axis and scale of 0 to 100% represent the net throughput, and
757 the UAV fleet size (4-128) is shown on a separate axis. Figure 5 shows 12
758 subfigures, each of which displaying the net throughput for the UTARB,
759 OTA, auction, max-sum, and LIAM algorithms. Because of the steep in-
760 crease in the runtime performance of the auction and max-sum strategies,
761 the algorithms halted at an early stage (see subfigures 5i -5l). The standard
762 deviation for the 10 trials collected for each algorithm was also computed
763 and presented in Table 2.

764 With only two infested palms in the first scenario (see subfigures 5a), all
765 five algorithms achieved a net throughput of 100% as different UAV fleet
766 sizes were deployed (i.e., all infested palms were detected and treated for
767 infestation). A similar performance can be observed with only four infesta-
768 tions (see subfigure 5a); however, max-sum begins to lag behind, as it was
769 only able to discover three of the four infested palms. As more infestations
770 are spread throughout the plantation, the superior performance of the pro-
771 posed UTARB algorithm becomes apparent. In all scenarios, UTARB was
772 able to detect and treat all infested palms within the mission parameters at
773 increasing fleet sizes and number of infested palms. Of the four benchmarks,
774 the performance of LIAM was closest to that of UTARB with infestations
775 spreading to no more than 512 palms (see subfigure 5i). As the number of
776 infested palms increases to 1,024 the performance of LIAM falters with only

777 4 UAVs in its fleet (see subfigure 5j). The performance continues to decline
778 with 2,048 and 4,096 UAVs and more UAVs (see subfigures 5k and 5l).

779 Although the two benchmark algorithms, auction and max-sum, achieved
780 almost identical performances, max-sum proved to be less robust to increas-
781 ing number of UAVs in a fleet and number of infestations (see subfigures 5i
782 -5l). At 1,024 infestations, the performance of the auction-based algorithm
783 begins to deteriorate as the fleet size increase to 128 UAVs. The algorithm
784 progressively worsens as the number of infestations increases to 2,048 and
785 4,096 and halts with even fewer agents: 32 UAVs. The performance of max-
786 sum coordination proved to be even poorer, as it halted earlier than the
787 auction algorithm at only 512 infested palms in the plantation area and 32
788 UAVs. The algorithm failed to produce more results in subsequent scenarios
789 as well, with fewer UAVs in the fleet. The deterioration of the algorithms'
790 performances is likely because of the large number of iterations that are per-
791 formed by the auction and max-sum algorithms. This, of course, left the
792 system unable to handle the increasing number of tasks.

793 At only a few infestations, the OTA strategy and LIAM perform well
794 compared to the other two benchmark algorithms. Whereas the auction-
795 based and max-sum coordinations halted as infestations grew in number,
796 OTA and LIAM were able to progress and detect infestations. However, the
797 percentage of treated palms clearly diminishes when only a few UAVs are
798 deployed for most scenarios for OTA (see subfigures 5d-5l). This was also the
799 case for the auction and max-sum algorithms, but to a relatively lower extent,
800 as the two algorithms produced better net throughput than OTA. LIAM, on
801 the other hand, produced significantly higher net throughput compared to
802 the other benchmarks with reasonable runtime performance. At 2,048 and
803 4,096 infestations the runtime performance of LIAM lies in contrast to that of
804 OTA, where the increasing number of UAVs improved LIAM's performance.
805 Nevertheless, unlike the four benchmark strategies, the proposed UTARB
806 algorithm's net throughput was not affected by the increase in the number
807 of UAVs. This demonstrates its ability to conduct the mission efficiently and
808 economically with fewer UAVs.

809 Additional simulations were carried out with UTARB to inspect its per-
810 formance in a larger plantation area (1000×1000 regions) with logarithmi-
811 cally increasing UAV fleets and infestations. Similar to what was observed
812 in the smaller area, the UTARB algorithm was able to detect and treat all
813 infestations in this larger plantation. This shows that the performance of
814 UTARB is scalable to larger plantations, while still maintaining its economic

815 advantage.

816 *7.2. Runtime Performance*

817 The runtime performances of the UTARB, OTA, auction, max-sum, and
818 LIAM algorithms were recorded for each of the simulated scenarios. The re-
819 sults of the average runtime performances and standard deviation are shown
820 in Table 3 and illustrated in Figure 6 as lin-log graphs as the number of infes-
821 tations grew from 2 to 4,096 infested palms against the number of UAVs. The
822 dashed lines in the figures represent values and lines that extend sharply be-
823 yond the values displayed in the vertical axis. Therefore, Table 3 is included
824 to report these values. As previously indicated in the previous section and
825 Figure 5, the auction-based and max-sum algorithms halted in scenarios with
826 a large number of infested palms because of the large computational over-
827 head.

828 The results show that UTARB outperformed the other benchmark algo-
829 rithms in this performance measure as well. This is especially the case with
830 larger infestations and a larger number of UAVs (see subfigures 6j-6l). It is
831 important to note that the performance of the proposed algorithm and OTA
832 was similar in this metric when only a few UAVs were deployed at lower in-
833 festation levels (up to 16 infested palms). However, the runtime performance
834 of the OTA algorithm steadily increased with the number of UAVs in the
835 fleet and number of infested palms. The number of deployed UAVs in the
836 scenarios had minimal impact on the runtime performance of UTARB, where
837 only slight variations occurred across the scenarios. This marginal impact
838 on the performance of UTARB at the different levels of infestation and fleet
839 size demonstrates the algorithm’s capability of economically completing the
840 DAT mission with fewer UAVs.

841 LIAM’s running time was relatively close to that of UTARB and OTA
842 at lower levels of infestations. Similar to what was observed for the OTA
843 algorithm, the running time of LIAM steadily grows as the number of in-
844 festations was increased from 2 to 4,096 infested palms. At lower levels of
845 infestations (2-8 infested palms), the running time of OTA is almost twice as
846 fast as that of LIAM. However, this number starts to significantly decrease
847 as the number of infestations grow with LIAM outperforming the OTA algo-
848 rithm. Similar to UTARB, the variations in running time for LIAM as the
849 number of UAVs was increased was relatively small. However, as the running
850 time of the UTARB algorithm increased those for LIAM begin to decrease
851 as the fleet size grows for higher levels of infestations. This shows that while

852 UTARB is able to sustain its running time with smaller and larger fleets,
853 LIAM’s performance is significantly better with larger fleets of UAVs.

854 The auction and max-sum strategy required considerably more time to de-
855 tect infestation in the DAT mission than did the proposed algorithm and the
856 baseline. The runtime of the auction and max-sum algorithms significantly
857 increased, taking up to 16 and 20 hours for 4,096 infestations, respectively.
858 For both strategies, the system halted before showing meaningful results
859 starting at 512 infestations and above (see subfigures 6i-6l). In subfigure 6g-
860 6l, the lines representing the runtime performance of the max-sum algorithm
861 extend far beyond the x-axis because of the large disparity between its values
862 and those of the other algorithms as the number of infestations increased.
863 This was also the case for the auction algorithm as the number of UAVs was
864 increased in the scenarios. These large variations for both algorithms are
865 likely because of the amplified complexity as more UAVs were introduced.

866 The running time of the UTARB algorithm was further examined in a
867 larger plantation area of 1000×1000 regions (with 8×8 meter blocks) as
868 the number of UAVs were increased along with the number of infested palms
869 (see Figure 7). Table 4 shows UTARB’s running time for a small and a
870 large plantation area. The findings show that UTARB’s running time in the
871 bigger area is understandably larger than that of the smaller area. UTARB’s
872 running time as the number of UAVs increases almost doubles for the larger
873 area and variations are slightly bigger than those observed in the smaller
874 area. In fact, in a larger area, UTARB appears to perform better with fewer
875 UAVs. This finding continues to demonstrate the economic value of UTARB
876 as it is able to complete the DAT mission with fewer UAVs.

877 8. Conclusions

878 In DAT missions, the deployment of multiple UAVs requires the proper al-
879 location of tasks to efficiently detect and treat pest infestations. The MUTA
880 problem is addressed in this paper with UTARB, a bacteria-inspired problem-
881 based heuristic. UTARB’s computational parameters are simple and are mea-
882 sured by each UAV locally. This gives each UAV the capability of making
883 independent task allocation decisions to ensure autonomy and low running
884 times. A simulator was built to thoroughly assess the performance of the
885 proposed bio-inspired heuristic against three well-established benchmark al-
886 gorithms and a recently proposed problem-dependent bio-inspired algorithm.
887 The experimental findings demonstrate that using UTARB for task alloca-

888 tion in DAT missions considerably increased the percentage of detected and
889 treated RPW infested palms and reduced the overall runtime complexity un-
890 der different scales of fleet size and number of infestations. The results also
891 highlighted the economic value of UTARB, as fewer UAVs were required to
892 quickly detect and treat infestations and halt their spread.

893 Although UTARB was introduced within the context of DAT missions, it
894 is by no means limited to this application domain. The algorithm can poten-
895 tially be applied in missions such as search-and-monitor missions for goods
896 and items in factories and warehouse and survey-and-treatment missions for
897 livestock, crops, and forest protection. The work in this paper opens up
898 several interesting research directions. The proposed UTARB algorithm out-
899 performed conventional algorithms, and we plan to assess its behaviours when
900 compared to well-established bio-inspired algorithms. Additionally, only in-
901 dependent tasks were considered; we intend to explore the task allocation
902 problem with dependent tasks and workflows. Furthermore, this work was
903 done as a part of a national project aimed at combating RPW infestation
904 in Saudi Arabia and thus will be deployed in a field setting to assess the
905 performance of the algorithm.

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911 **Declarations of interest**

912 The authors declare no competing interest.

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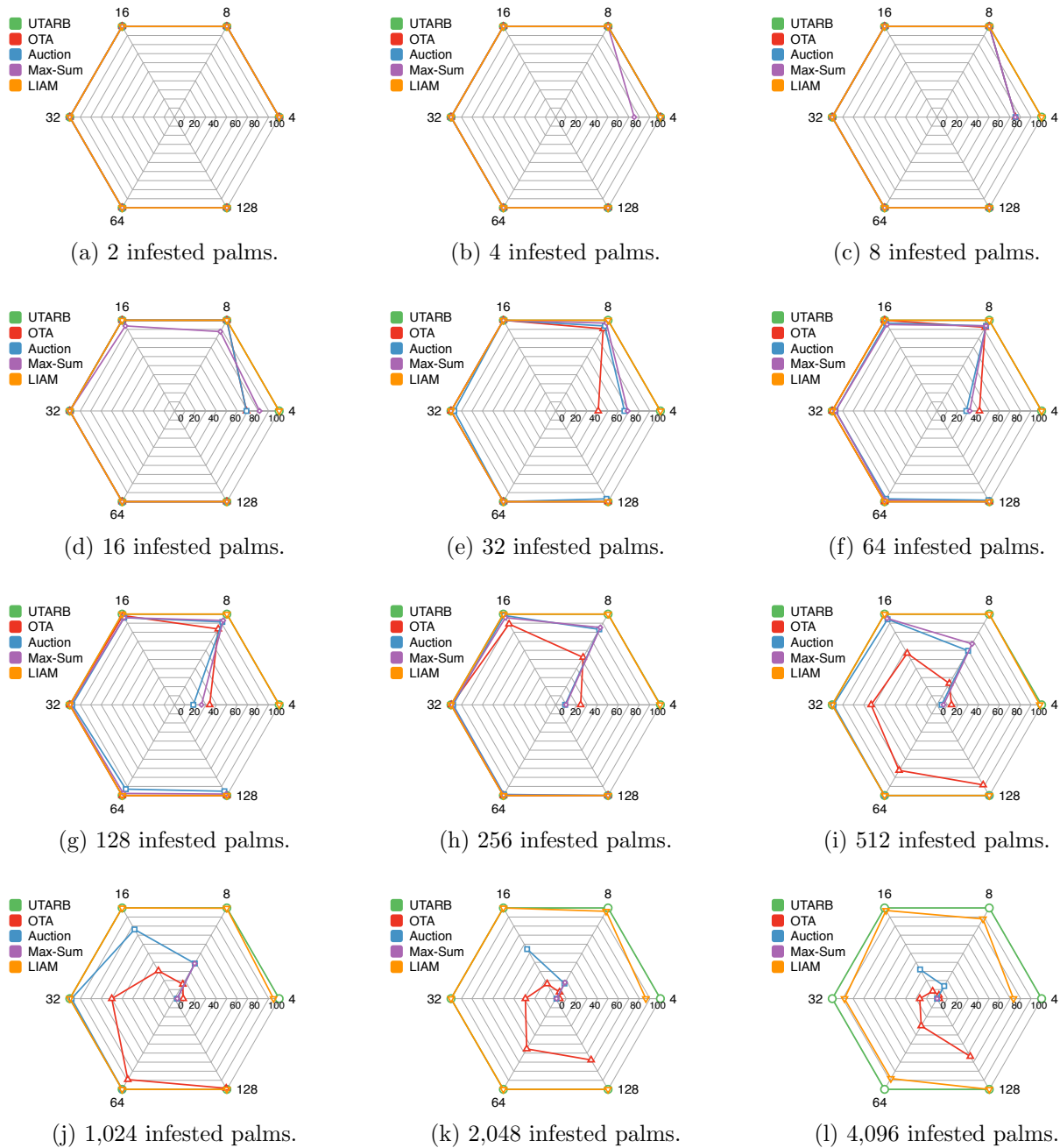


Figure 5: Net throughput as the number of infested palms increases from 2 to 4,096 in the plantation area.

Table 2: Net throughput standard deviation for total number of detected and treated palms (presented as a percentage %) trials as the number of infestations increases from 2 to 4,096 in the plantation area.

Infestations	UAVs	UTARB	OTA	Auction	Max-Sum	LIAM
2	4	0.00	0.00	0.00	0.00	0.00
	8	0.00	0.00	0.00	0.00	0.00
	16	0.00	0.00	0.00	0.00	0.00
	32	0.00	0.00	0.00	0.00	0.00
	64	0.00	0.00	0.00	0.00	0.00
	128	0.00	0.00	0.00	0.00	0.00
4	4	0.00	0.00	0.00	3.14	0.00
	8	0.00	0.00	0.00	0.00	0.00
	16	0.00	0.00	0.00	0.00	0.00
	32	0.00	0.00	0.00	0.00	0.00
	64	0.00	0.00	0.00	0.00	0.00
	128	0.00	0.00	0.00	0.00	0.00
8	4	0.00	3.70	0.00	0.00	0.00
	8	0.00	0.00	0.00	0.00	0.00
	16	0.00	0.00	0.00	0.00	0.00
	32	0.00	0.00	0.00	0.00	0.00
	64	0.00	0.00	0.00	0.00	0.00
	128	0.00	0.00	0.00	0.00	0.00
16	4	0.00	3.21	4.85	5.43	0.00
	8	0.00	0.00	0.00	0.00	0.00
	16	0.00	0.00	0.00	0.00	0.00
	32	0.00	0.00	0.00	0.00	0.00
	64	0.00	0.00	0.00	0.00	0.00
	128	0.00	0.00	0.00	0.00	0.00
32	4	0.00	4.10	1.81	3.89	0.00
	8	0.00	1.21	2.99	2.29	0.00
	16	0.00	0.00	0.00	0.00	0.00
	32	0.00	0.00	0.98	0.00	0.00
	64	0.00	0.00	0.00	0.00	0.00
	128	0.00	0.00	2.41	0.00	0.00
64	4	0.00	5.66	4.34	5.96	0.00
	8	0.00	0.96	4.71	5.57	0.00
	16	0.00	0.00	2.05	2.21	0.00
	32	0.00	0.00	5.82	1.83	0.00
	64	0.00	0.00	3.32	5.61	0.00
	128	0.00	0.00	2.57	0.00	0.00
128	4	0.00	5.92	3.09	0.58	0.00
	8	0.00	1.15	3.27	1.99	0.00
	16	0.00	5.70	5.48	4.46	0.00
	32	0.00	0.00	0.96	4.04	0.00
	64	0.00	0.00	3.39	1.72	0.00
	128	0.00	0.00	1.73	2.26	0.00
256	4	0.00	3.20	2.18	2.35	1.00
	8	0.00	0.31	3.10	2.35	0.00
	16	0.00	1.60	1.97	4.94	0.00
	32	0.00	4.48	5.71	1.83	0.00
	64	0.00	3.03	2.16	0.38	0.00
	128	0.00	1.63	0.00	0.00	0.00
512	4	0.00	2.03	0.17	2.16	1.60
	8	0.00	4.84	3.48	0.60	0.00
	16	0.00	5.69	4.92	2.29	0.00
	32	0.00	4.96	2.14	/	0.00
	64	0.00	5.67	0.00	/	0.00
	128	0.00	4.70	0.00	/	0.50
1,024	4	0.00	2.89	4.67	1.92	2.10
	8	0.00	2.05	2.16	3.33	1.10
	16	0.00	2.38	5.47	/	0.00
	32	0.00	1.66	0.77	/	0.00
	64	0.00	5.89	0.00	/	0.00
	128	0.00	2.07	/	/	0.00
2,048	4	0.00	3.55	0.33	3.72	2.31
	8	0.00	2.61	1.47	2.19	1.20
	16	0.00	2.19	0.67	/	0.00
	32	0.00	3.34	/	/	0.00
	64	0.00	2.92	/	/	0.00
	128	0.00	3.18	/	/	0.00
4,096	4	0.00	2.29	3.22	0.72	2.80
	8	0.00	1.61	3.62	/	3.11
	16	0.00	2.21	2.25	/	0.90
	32	0.00	5.23	/	/	1.20
	64	0.00	1.42	/	/	1.31
	128	0.00	0.35	/	/	0.00

Table 3: Average runtime performance and standard deviation (h:mm:ss) as the number of infestations increases from 2 to 4,096 in the plantation area.

Infestations	UAVs	UTARB	OTA	Auction	Max-Sum	LIAM
2	4	0:00:15 (0:00:03)	0:00:26 (0:00:11)	0:02:07 (0:00:47)	0:02:58 (0:00:09)	0:01:01 (0:00:17)
	8	0:00:16 (0:00:02)	0:00:42 (0:00:15)	0:08:18 (0:01:43)	0:11:27 (0:01:43)	0:01:17 (0:00:17)
	16	0:00:15 (0:00:04)	0:00:50 (0:00:08)	0:12:36 (0:07:21)	0:13:40 (0:00:54)	0:00:50 (0:00:08)
	32	0:00:16 (0:00:13)	0:00:53 (0:00:12)	0:30:11 (0:10:34)	0:47:29 (0:03:40)	0:00:56 (0:00:19)
	64	0:00:17 (0:00:05)	0:00:56 (0:00:04)	1:06:08 (0:21:50)	1:29:06 (0:04:29)	0:00:59 (0:00:20)
	128	0:00:18 (0:00:08)	0:01:00 (0:00:05)	1:33:06 (0:11:40)	2:10:43 (0:17:17)	0:01:07 (0:00:17)
4	4	0:00:15 (0:00:03)	0:00:47 (0:00:10)	0:06:52 (0:02:09)	0:10:31 (0:01:21)	0:01:15 (0:00:17)
	8	0:00:15 (0:00:04)	0:00:56 (0:00:12)	0:09:05 (0:00:37)	0:17:53 (0:01:06)	0:01:19 (0:00:05)
	16	0:00:19 (0:00:03)	0:01:00 (0:00:05)	0:15:34 (0:06:27)	0:24:19 (0:02:53)	0:01:15 (0:00:11)
	32	0:00:20 (0:00:09)	0:01:07 (0:00:06)	0:41:16 (0:11:08)	0:54:39 (0:02:26)	0:01:02 (0:00:06)
	64	0:00:27 (0:00:07)	0:01:16 (0:00:08)	0:56:27 (0:11:52)	2:53:41 (0:09:27)	0:01:11 (0:00:16)
	128	0:00:31 (0:00:05)	0:01:17 (0:00:12)	2:32:58 (0:23:58)	4:06:43 (0:12:20)	0:01:18 (0:00:16)
8	4	0:00:18 (0:00:04)	0:00:36 (0:00:09)	0:07:50 (0:01:45)	0:07:25 (0:01:17)	0:01:14 (0:00:03)
	8	0:00:19 (0:00:06)	0:00:44 (0:00:06)	0:11:33 (0:03:46)	0:16:55 (0:00:41)	0:01:25 (0:00:12)
	16	0:00:20 (0:00:03)	0:00:57 (0:00:08)	0:15:27 (0:02:49)	0:36:22 (0:03:23)	0:01:19 (0:00:06)
	32	0:00:21 (0:00:02)	0:01:04 (0:00:10)	0:41:33 (0:06:54)	1:16:31 (0:05:40)	0:01:25 (0:00:16)
	64	0:00:22 (0:00:08)	0:01:19 (0:00:11)	1:14:47 (0:10:44)	2:29:53 (0:10:33)	0:01:17 (0:00:20)
	128	0:00:23 (0:00:04)	0:01:21 (0:00:19)	3:14:08 (0:11:06)	5:22:56 (0:22:23)	0:01:23 (0:00:10)
16	4	0:00:19 (0:00:05)	0:01:37 (0:00:11)	0:10:23 (0:01:13)	0:13:34 (0:02:48)	0:01:28 (0:00:08)
	8	0:00:19 (0:00:05)	0:01:39 (0:00:07)	0:25:20 (0:07:34)	0:23:07 (0:05:27)	0:01:22 (0:00:17)
	16	0:00:22 (0:00:02)	0:01:43 (0:00:04)	0:56:11 (0:10:09)	0:52:39 (0:04:19)	0:01:25 (0:00:11)
	32	0:00:29 (0:00:08)	0:01:58 (0:00:14)	1:06:20 (0:06:45)	1:38:41 (0:11:35)	0:01:24 (0:00:09)
	64	0:00:31 (0:00:03)	0:03:02 (0:00:14)	1:15:16 (0:20:27)	3:51:22 (0:28:46)	0:01:27 (0:00:06)
	128	0:00:46 (0:00:06)	0:02:30 (0:00:19)	2:35:49 (0:13:50)	6:37:45 (1:02:23)	0:01:32 (0:00:05)
32	4	0:00:21 (0:00:03)	0:01:01 (0:00:03)	0:16:44 (0:02:07)	0:21:41 (0:01:30)	0:01:31 (0:00:08)
	8	0:00:18 (0:00:03)	0:01:05 (0:00:10)	0:27:39 (0:02:41)	0:43:48 (0:03:35)	0:01:32 (0:00:14)
	16	0:00:25 (0:00:06)	0:01:13 (0:00:11)	0:29:41 (0:06:27)	1:30:38 (0:05:20)	0:01:36 (0:00:12)
	32	0:00:31 (0:00:05)	0:01:19 (0:00:13)	1:10:33 (0:10:50)	3:07:49 (0:07:46)	0:01:30 (0:00:17)
	64	0:00:47 (0:00:04)	0:01:26 (0:00:04)	1:49:08 (0:10:44)	6:46:00 (0:10:42)	0:01:32 (0:00:15)
	128	0:00:48 (0:00:03)	0:01:32 (0:00:11)	3:37:57 (0:14:21)	10:43:39 (0:12:47)	0:01:43 (0:00:09)
64	4	0:00:28 (0:00:02)	0:01:15 (0:00:11)	0:18:07 (0:02:21)	0:32:00 (0:03:45)	0:01:28 (0:00:17)
	8	0:00:31 (0:00:04)	0:01:24 (0:00:12)	0:30:35 (0:01:34)	1:31:25 (0:08:16)	0:01:40 (0:00:08)
	16	0:00:32 (0:00:05)	0:01:36 (0:00:03)	0:38:13 (0:01:08)	2:48:14 (0:10:32)	0:01:36 (0:00:06)
	32	0:00:32 (0:00:06)	0:01:43 (0:00:13)	1:25:04 (0:10:33)	5:38:01 (0:13:48)	0:01:34 (0:00:10)
	64	0:00:30 (0:00:06)	0:01:56 (0:00:13)	3:17:19 (0:12:51)	10:44:42 (0:07:52)	0:01:53 (0:00:09)
	128	0:00:38 (0:00:04)	0:01:59 (0:00:06)	5:24:07 (0:11:36)	15:14:11 (0:20:06)	0:01:58 (0:00:16)
128	4	0:00:40 (0:00:04)	0:02:31 (0:00:11)	0:19:56 (0:01:40)	1:37:42 (0:10:25)	0:03:47 (0:00:12)
	8	0:00:40 (0:00:03)	0:02:57 (0:00:19)	0:42:24 (0:04:19)	3:24:23 (0:12:10)	0:03:37 (0:00:13)
	16	0:00:40 (0:00:03)	0:03:00 (0:00:09)	1:20:40 (0:10:27)	6:22:08 (0:12:44)	0:03:36 (0:00:16)
	32	0:00:42 (0:00:05)	0:03:07 (0:00:03)	2:16:51 (0:10:08)	10:53:39 (0:20:22)	0:03:44 (0:00:11)
	64	0:00:49 (0:00:03)	0:03:11 (0:00:14)	4:50:09 (0:20:10)	11:52:16 (0:15:53)	0:04:13 (0:00:19)
	128	0:01:06 (0:00:06)	0:03:05 (0:00:21)	9:00:00 (0:15:15)	16:09:45 (0:14:38)	0:04:41 (0:00:20)
256	4	0:00:35 (0:00:07)	0:03:48 (0:00:04)	0:25:56 (0:00:10)	1:53:39 (0:09:50)	0:02:16 (0:00:16)
	8	0:00:31 (0:00:04)	0:03:57 (0:00:14)	0:52:37 (0:04:14)	4:43:37 (0:10:27)	0:02:14 (0:00:15)
	16	0:00:30 (0:00:03)	0:04:59 (0:00:12)	2:44:45 (0:09:22)	5:37:14 (0:12:18)	0:02:06 (0:00:14)
	32	0:00:41 (0:00:07)	0:04:57 (0:00:17)	4:05:03 (0:10:26)	9:24:15 (0:20:27)	0:02:07 (0:00:06)
	64	0:00:50 (0:00:04)	0:04:41 (0:00:21)	9:28:56 (0:14:12)	12:55:11 (0:19:12)	0:02:31 (0:00:13)
	128	0:01:07 (0:00:04)	0:04:36 (0:00:15)	12:50:44 (0:21:14)	18:17:59 (0:22:47)	0:02:45 (0:00:16)
512	4	0:00:46 (0:00:02)	0:05:20 (0:00:23)	0:34:24 (0:07:17)	2:20:52 (0:09:08)	0:04:16 (0:00:08)
	8	0:00:46 (0:00:12)	0:04:56 (0:00:18)	1:28:01 (0:05:29)	10:55:35 (0:10:32)	0:03:11 (0:00:16)
	16	0:00:53 (0:00:08)	0:06:41 (0:01:13)	6:15:58 (0:11:42)	19:27:41 (0:30:33)	0:02:39 (0:00:19)
	32	0:00:57 (0:00:03)	0:06:58 (0:00:56)	7:50:30 (0:20:18)	/	0:02:38 (0:00:12)
	64	0:01:06 (0:00:10)	0:08:19 (0:02:14)	10:51:19 (0:31:23)	/	0:03:05 (0:00:16)
	128	0:01:10 (0:00:04)	0:10:29 (0:01:03)	13:50:45 (0:24:49)	/	0:03:19 (0:00:16)
1,024	4	0:01:07 (0:00:03)	0:07:34 (0:01:07)	0:32:54 (0:03:22)	3:40:49 (0:11:48)	0:07:27 (0:01:04)
	8	0:01:06 (0:00:10)	0:08:35 (0:00:03)	2:43:18 (0:09:22)	19:37:23 (0:31:06)	0:05:18 (0:00:18)
	16	0:00:56 (0:00:08)	0:09:58 (0:01:11)	6:35:20 (0:13:48)	/	0:04:16 (0:00:14)
	32	0:00:51 (0:00:09)	0:11:23 (0:01:05)	10:15:06 (0:22:22)	/	0:03:54 (0:00:14)
	64	0:01:07 (0:00:04)	0:19:48 (0:03:13)	14:26:26 (0:31:40)	/	0:03:55 (0:00:13)
	128	0:01:33 (0:00:08)	0:21:16 (0:02:14)	/	/	0:04:04 (0:00:16)
2,048	4	0:01:51 (0:00:11)	0:12:48 (0:00:34)	0:36:33 (0:06:20)	11:06:41 (0:19:32)	0:14:32 (0:02:16)
	8	0:01:56 (0:00:08)	0:14:55 (0:02:04)	3:05:18 (0:10:07)	19:24:39 (0:42:49)	0:10:57 (0:00:28)
	16	0:01:37 (0:00:12)	0:15:19 (0:01:06)	10:53:13 (0:13:24)	/	0:07:28 (0:00:15)
	32	0:01:15 (0:00:05)	0:17:42 (0:03:07)	/	/	0:06:46 (0:00:04)
	64	0:01:42 (0:00:06)	0:24:30 (0:02:13)	/	/	0:05:50 (0:00:13)
	128	0:01:56 (0:00:05)	0:27:18 (0:03:09)	/	/	0:06:03 (0:00:15)
4,096	4	0:02:43 (0:00:09)	0:26:37 (0:02:04)	0:46:35 (0:09:46)	20:00:14 (0:19:52)	0:42:32 (0:02:11)
	8	0:02:25 (0:00:03)	0:27:41 (0:02:14)	4:27:07 (0:14:06)	/	0:33:27 (0:04:09)
	16	0:02:24 (0:00:04)	0:36:05 (0:03:09)	16:49:03 (0:28:27)	/	0:22:24 (0:01:15)
	32	0:02:18 (0:00:13)	0:37:51 (0:02:03)	/	/	0:22:00 (0:02:13)
	64	0:02:30 (0:00:08)	0:41:14 (0:02:04)	/	/	0:21:36 (0:01:51)
	128	0:02:44 (0:00:09)	0:52:39 (0:04:09)	/	/	0:10:54 (0:01:03)

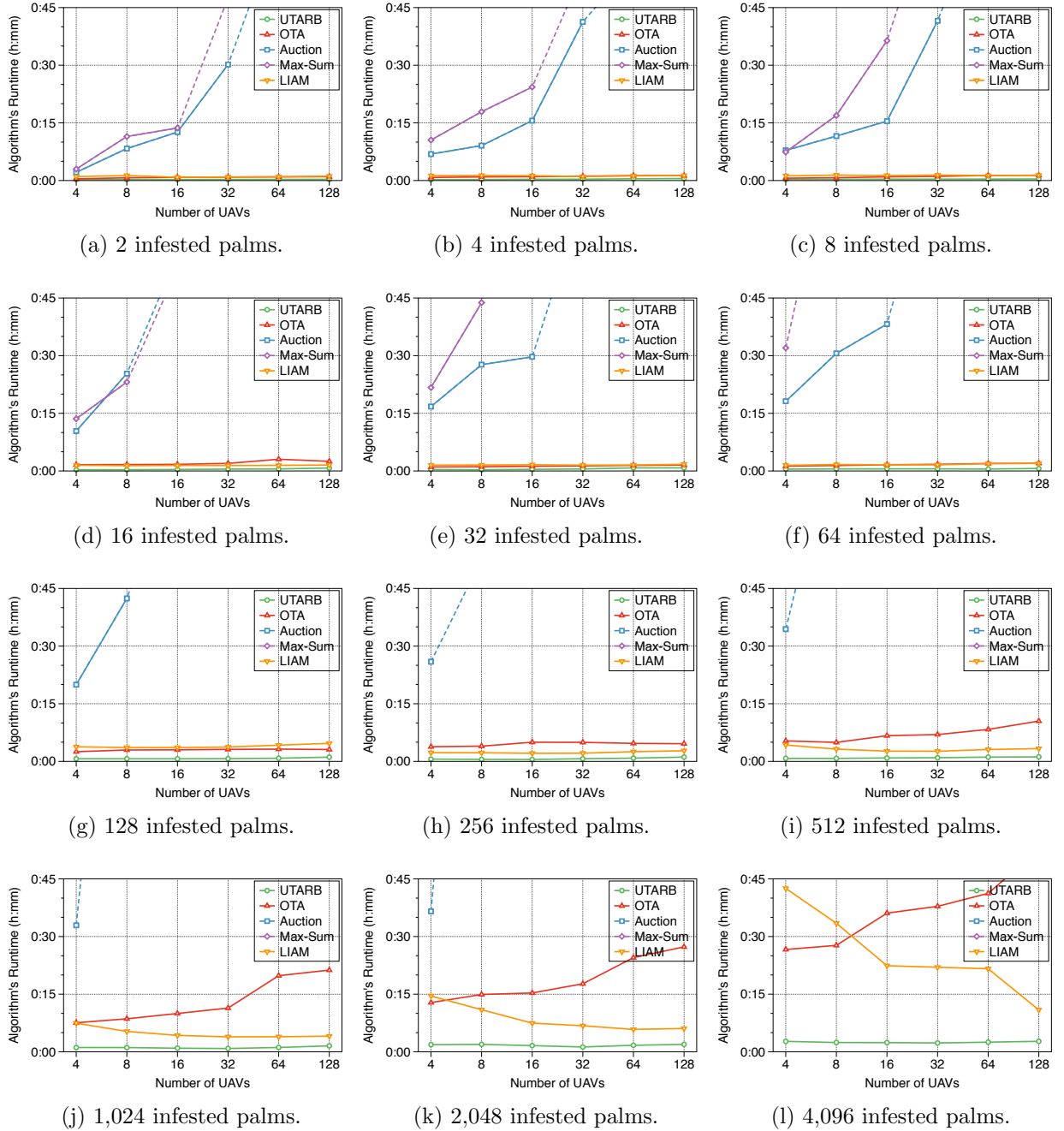


Figure 6: Runtime performance as the number of infested palms increases from 2 to 4,096 in the plantation area.

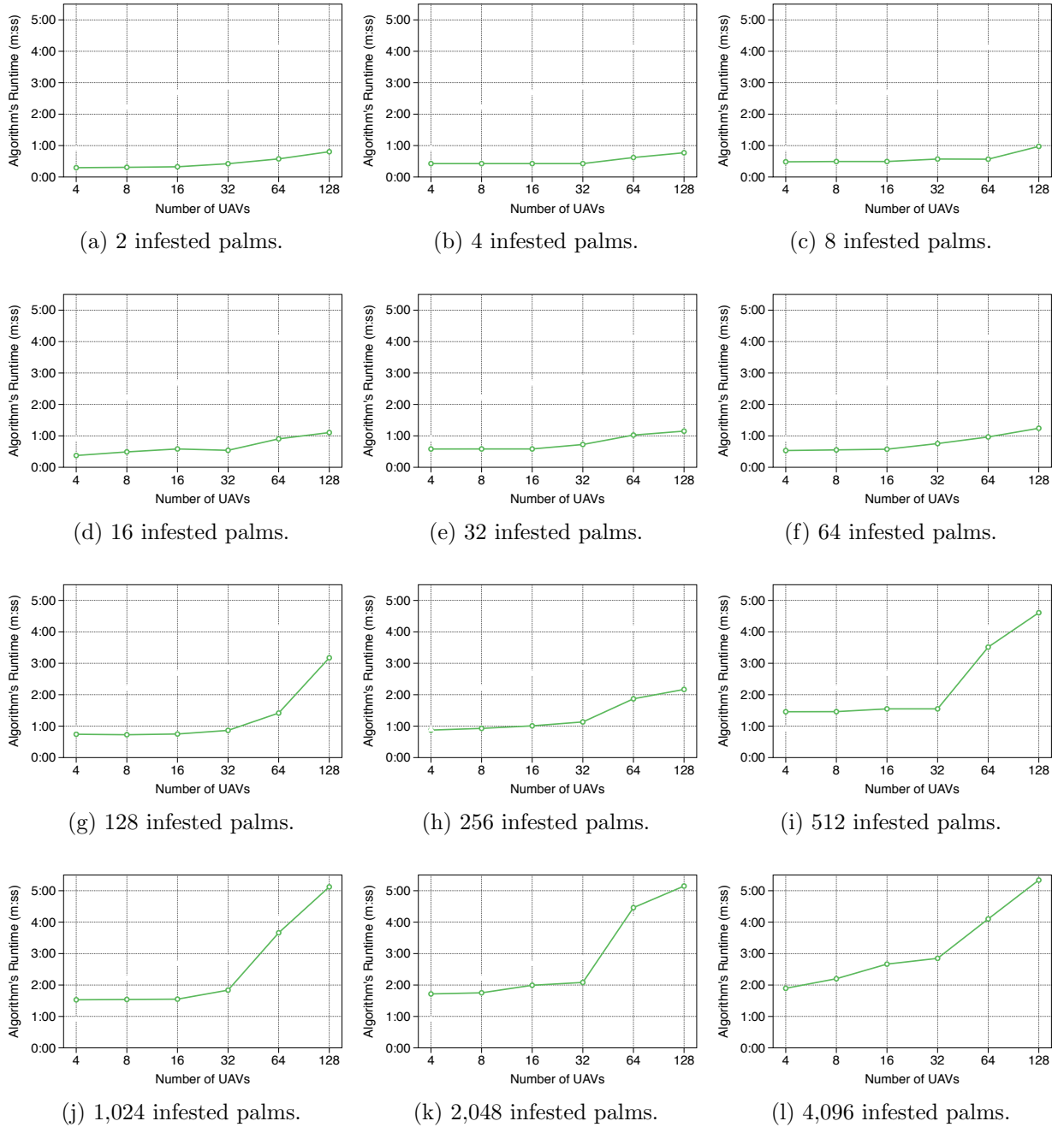


Figure 7: Runtime performance of UTARB as the number of infested palms increases from 2 to 4,096 in a large plantation area.

Table 4: Average runtime performance and standard deviation (h:mm:ss) of UTARB in a small and a large area as the number of infestations increases from 2 to 4,096 infested palms.

Infestations	UAVs	UTARB (small area)	UTARB (large area)
2	4	0:00:15 (0:00:03)	0:00:17 (0:00:08)
	8	0:00:16 (0:00:02)	0:00:18 (0:00:13)
	16	0:00:15 (0:00:04)	0:00:19 (0:00:12)
	32	0:00:16 (0:00:13)	0:00:25 (0:00:09)
	64	0:00:17 (0:00:05)	0:00:34 (0:00:13)
	128	0:00:18 (0:00:08)	0:00:48 (0:00:15)
4	4	0:00:15 (0:00:03)	0:00:25 (0:00:09)
	8	0:00:15 (0:00:04)	0:00:25 (0:00:03)
	16	0:00:19 (0:00:03)	0:00:25 (0:00:04)
	32	0:00:20 (0:00:09)	0:00:25 (0:00:03)
	64	0:00:27 (0:00:07)	0:00:37 (0:00:12)
	128	0:00:31 (0:00:05)	0:00:46 (0:00:15)
8	4	0:00:18 (0:00:04)	0:00:29 (0:00:10)
	8	0:00:19 (0:00:06)	0:00:29 (0:00:09)
	16	0:00:20 (0:00:03)	0:00:29 (0:00:14)
	32	0:00:21 (0:00:02)	0:00:34 (0:00:05)
	64	0:00:22 (0:00:08)	0:00:34 (0:00:14)
	128	0:00:23 (0:00:04)	0:00:58 (0:00:25)
16	4	0:00:19 (0:00:05)	0:00:22 (0:00:03)
	8	0:00:19 (0:00:05)	0:00:29 (0:00:08)
	16	0:00:22 (0:00:02)	0:00:35 (0:00:04)
	32	0:00:29 (0:00:08)	0:00:32 (0:00:12)
	64	0:00:31 (0:00:03)	0:00:54 (0:00:11)
	128	0:00:46 (0:00:06)	0:01:06 (0:00:05)
32	4	0:00:21 (0:00:03)	0:00:34 (0:00:06)
	8	0:00:18 (0:00:03)	0:00:35 (0:00:09)
	16	0:00:25 (0:00:06)	0:00:35 (0:00:07)
	32	0:00:31 (0:00:05)	0:00:43 (0:00:14)
	64	0:00:47 (0:00:04)	0:01:01 (0:00:16)
	128	0:00:48 (0:00:03)	0:01:09 (0:00:15)
64	4	0:00:28 (0:00:02)	0:00:32 (0:00:04)
	8	0:00:31 (0:00:04)	0:00:33 (0:00:04)
	16	0:00:32 (0:00:05)	0:00:34 (0:00:07)
	32	0:00:32 (0:00:06)	0:00:45 (0:00:05)
	64	0:00:30 (0:00:06)	0:00:57 (0:00:08)
	128	0:00:38 (0:00:04)	0:01:14 (0:00:15)
128	4	0:00:40 (0:00:04)	0:00:52 (0:00:02)
	8	0:00:40 (0:00:03)	0:00:55 (0:00:15)
	16	0:00:40 (0:00:03)	0:01:06 (0:00:11)
	32	0:00:42 (0:00:05)	0:01:08 (0:00:12)
	64	0:00:49 (0:00:03)	0:01:52 (0:00:06)
	128	0:01:06 (0:00:06)	0:02:10 (0:00:12)
256	4	0:00:35 (0:00:07)	0:00:52 (0:00:10)
	8	0:00:31 (0:00:04)	0:00:55 (0:00:11)
	16	0:00:30 (0:00:03)	0:01:00 (0:00:08)
	32	0:00:41 (0:00:07)	0:01:08 (0:00:06)
	64	0:00:50 (0:00:04)	0:01:52 (0:00:17)
	128	0:01:07 (0:00:04)	0:02:10 (0:00:08)
512	4	0:00:46 (0:00:02)	0:01:27 (0:00:08)
	8	0:00:46 (0:00:12)	0:01:27 (0:00:12)
	16	0:00:53 (0:00:08)	0:01:33 (0:00:09)
	32	0:00:57 (0:00:03)	0:01:33 (0:00:07)
	64	0:01:06 (0:00:10)	0:03:30 (0:00:18)
	128	0:01:10 (0:00:04)	0:04:36 (0:00:21)
1,024	4	0:01:07 (0:00:03)	0:01:31 (0:00:15)
	8	0:01:06 (0:00:10)	0:01:32 (0:00:16)
	16	0:00:56 (0:00:08)	0:01:33 (0:00:16)
	32	0:00:51 (0:00:09)	0:01:50 (0:00:17)
	64	0:01:07 (0:00:04)	0:03:39 (0:00:12)
	128	0:01:33 (0:00:08)	0:05:07 (0:00:20)
2,048	4	0:01:51 (0:00:11)	0:01:43 (0:00:17)
	8	0:01:56 (0:00:08)	0:01:45 (0:00:09)
	16	0:01:37 (0:00:12)	0:01:59 (0:00:18)
	32	0:01:15 (0:00:05)	0:02:04 (0:00:11)
	64	0:01:42 (0:00:06)	0:04:27 (0:00:21)
	128	0:01:56 (0:00:05)	0:05:08 (0:00:26)
4,096	4	0:02:43 (0:00:09)	0:01:53 (0:00:14)
	8	0:02:25 (0:00:03)	0:02:12 (0:00:16)
	16	0:02:24 (0:00:04)	0:02:39 (0:00:11)
	32	0:02:18 (0:00:13)	0:02:50 (0:00:18)
	64	0:02:30 (0:00:08)	0:04:06 (0:00:23)
	128	0:02:44 (0:00:09)	0:05:20 (0:00:18)