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Gyrotropic response in the absence of a bias field

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Electromagnetic materials lacking local time-reversal symmetry, such as gyrotropic materials, are of keen interest and importance both scientifically and technologically. Scientifically, topologically nontrivial phenomena, such as photonic chiral edge states, allow for reflection-free transport even in the presence of large disorder. Technologically, nonreciprocal photonic devices, such as optical isolators and circulators, play critical roles in optical communication and computing technologies because of their ability to eliminate cross-talk and feedback. Nevertheless, most known natural materials that lack local time-reversal symmetry require strong external fields and function only in a limited range of the electromagnetic spectrum. By taking advantage of metamaterials capable of translating the property of unidirectional active electronic circuits into effective dielectric response, we introduce a microwave gyrotropic metamaterial that does not require an external magnetic bias. Strong bulk Faraday-like effects, observed in both simulations and experiments, confirm nonreciprocity of the effective medium. This approach is scalable to many other wavelengths, and it also illustrates an opportunity to synthesize exotic electromagnetic materials.

nonreciprocal systems | magneto-optics | effective media | time-reversal-symmetry breaking

Among natural mechanisms leading to gyrotropy, ferromagnetic resonance (1) is one of the strongest gyrotropic effects requiring a bias magnetic field at sub-Tesla levels, but is limited to the GHz frequency range. Magnetized plasma (2) and Zeeman splitting of optical dipole transitions do provide gyrotropy at optical frequencies, but at a very weak level even with a biasing field of several Tesla. These constraints, together with associated large absorption, have so far prevented large-scale application of nonreciprocal photonic systems. However, the recent advent of photonic crystals (3–6) and metamaterials enabled synthesis of artificial composite materials (7–14), possessing previously nonexistent electromagnetic properties, such as negative indices of refraction. Extending the concept of metamaterials to gyrotropic effects is thus an attractive venue to circumvent the limits of natural gyrotropic materials, especially if this could be done without using external magnetic fields. An important feature of gyrotropic materials is their nonreciprocal behavior, which cannot be created from dielectric or metallic structures alone even in the presence of loss or gain, according to the Rayleigh-Carson reciprocity theorem (15). Therefore, realizing gyrotropic metamaterials requires exploiting the inherent unidirectional property in the underlying electronic circuits, which has so far remained largely unexplored. In this paper, we intentionally combine unidirectional lumped electronic circuit elements with small subwavelength antennas oriented to change the polarization states: We introduce a bulk gyrotropic metamaterial with large Faraday-like rotation in the absence of an external magnetic bias; highly nonreciprocal propagation is observed in both simulations and experiments, where up to 14.4 degrees of Faraday-like rotation occurs over a 0.1 wavelength-thick metamaterial layer.

We start by reviewing the Faraday effect (1), which not only is a quintessential manifestation of both the broken local time-reversal symmetry and the nonreciprocity of a gyrotropic medi-

um, but also reveals important clues on the conditions necessary for construction of gyrotropic metamaterials. The Faraday rotation clearly differentiates gyrotropic materials from the closely related chiral materials (16–22), which, in contrast, are locally time-reversal symmetric and reciprocal. In a chiral medium, a linearly polarized traveling wave experiences a rotation of its polarization vector, with the direction of rotation determined by the wavevector k (23). Consequently, a backward-propagating wave unwinds the polarization vector (Fig. 1A) of a forward-propagating wave. The net change of the polarization angle of the reflected wave is zero, and the local time-reversal symmetry is preserved. On the other hand, an external dc magnetic field B dictates the rotation direction of the polarization in a gyrotropic medium (Fig. 1B). For instance, one can set up a magnetic field parallel to the optical axis such that a linearly polarized incident wave experiences a clockwise rotation for its polarization angle from φ_0 to $\varphi_0 + \Delta\varphi$. However, the backward wave, traveling along the direction antiparallel to the magnetic field, experiences a counterclockwise rotation, and the polarization angle of the exiting wave increases to $\varphi_0 + 2\Delta\varphi$. In other words, waves reflected in a gyrotropic medium do not revert to their initial incident polarization states; this implies broken local time-reversal symmetry and nonreciprocal propagation. In slightly more complicated geometries, Faraday rotation can also enable nonreciprocal amplitude and phase response (24), or even more exotic disorder-immune one-way waveguides (2, 25–27). Nevertheless, in this paper we focus on the essential feature of the Faraday rotation: the change in the polarization angle of the transmitted wave, which is conventionally determined by the external dc magnetic field in naturally occurring gyrotropic materials.

Although breaking local time-reversal symmetry in photonic systems is generally hard, in electronic systems it occurs quite commonly. Instead of employing an external magnetic field, our metamaterials take advantage of the directionality inherent in electronic amplifiers and transistors. By strongly coupling such electronic systems to incident electromagnetic radiation, we break the local time-reversal symmetry for E and M waves also. The input and output terminals are physically fixed by the circuit layouts and the underlying geometries of transistor channels (28). Signals travel only in one direction: Input voltages determine output voltages, but not the other way around. This circuit-level directionality is translated into a directional effective medium where, in each basis assembly, a unit-gain amplifier is driven by an input dipole antenna, and controls an output dipole antenna. The output polarization can be positioned along an arbitrary angle by the orientation of the antenna. To enable Faraday-like rotation, we implement four such assemblies per unit cell, as illustrated in Fig. 2A and explained in detail in *SI Text*.

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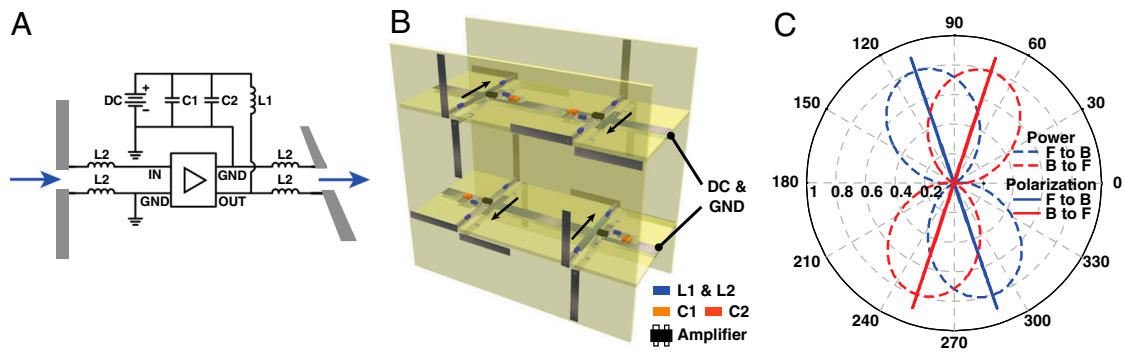


Fig. 3. Gyrotropic metamaterial for vertical polarization and its simulation results. (A) The circuit schematic of a basis assembly. (B) The structure schematic of a unit cell. (C) The simulated polarizations (solid) and power patterns (dashed) at the receiver when a vertically polarized wave at 885.45 MHz is incident in two opposite directions.

model remains 60 mm by 60 mm by 30 mm and the length of each dipole remains 29 mm with a 0.5-mm gap in the middle. The substrates for the front, back, and circuit boards are 1 mm-thick FR4 with relative permittivity 4.6 and loss tangent 0.02. The directions of the amplifier MGA53543 are marked by the black arrows. The lumped elements mounted on the circuit board are marked in different colors. $C1 = 100$ pF, $C2 = 10$ nF, and $L1 = L2 = 27$ nH. Simulation performed at 885.45 MHz for a vertically polarized incident wave is shown in Fig. 3C. Along the direction from the source to the receiver, the polarization angle rotates by $+16.75$ degrees and -16.75 degrees for front-side incidence and back-side incidence, respectively. The dc voltage of the amplifiers for these results is 0.533 V.

Finally, the Faraday-like rotation of the proposed gyrotropic metamaterial is confirmed in a transmission measurement experi-

ment. The photo of a metamaterial sample is shown in Fig. 4A, with the top-layer circuit board seen in Fig. 4B. Blue and red arrows indicate the directions of the amplifiers. A two-ridge horn antenna, serving as the source, is polarized along the vertical direction and driven with power at 10 dBm by a Hewlett-Packard 8350B Sweep Oscillator. A 133 mm-length printed dipole antenna on a 1 mm-thick FR4 substrate serves as a detector on the other side of the sample and is rotated to measure the polarization of the field through a Hewlett-Packard 8756A Scalar Network Analyzer. We first measured the polarization change with the wave incident from the front side to the back side of the sample, then flipped the sample horizontally and measured the polarization change with the wave incident from the back side to the front side. Along the direction from the source to the detector, we identify the change in the polarization angles, at a dc voltage of

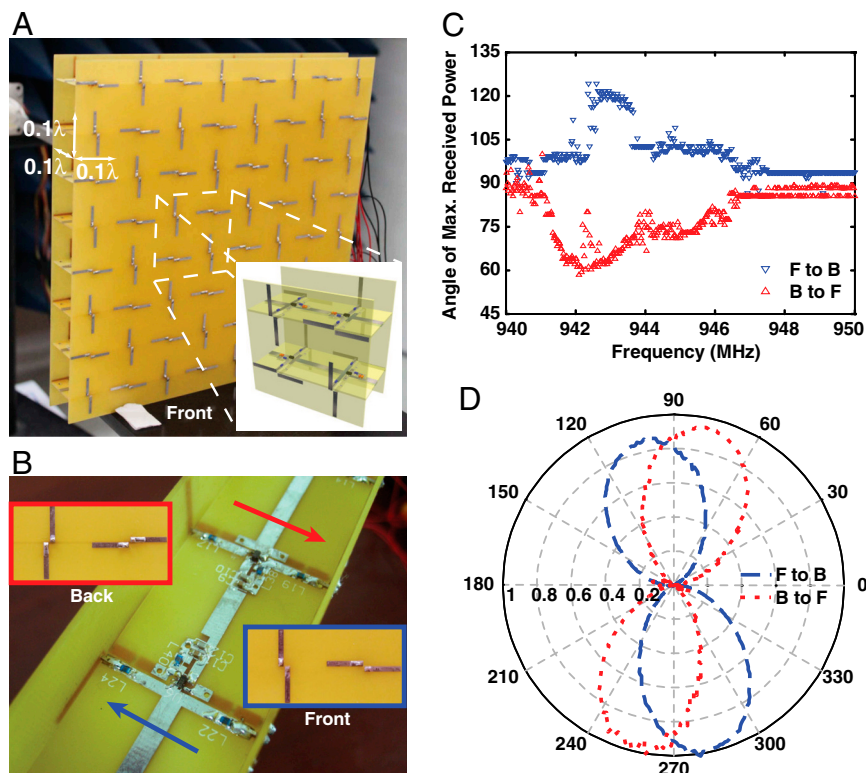


Fig. 4. Photos of the single-polarization gyrotropic metamaterial sample and its experimental results. (A) The photo of a single-layer gyrotropic metamaterial for vertical polarization. (B) The photo of the circuit board in the sample. (B, Inset) Photos of the metallic pattern on the front and the back board of the sample. (C) Angles at which the received power is maximized for a given incident frequency. (D) Measured power patterns calibrated from the free-space measurement with a vertically polarized wave incident at 946 MHz.

