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## FORMATION OF CLOSE IN SUPER-EARTHS AND MINI-NEPTUNES: REQUIRED DISK MASSES AND THEIR IMPLICATIONS

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### ABSTRACT

Recent observations by the *Kepler* space telescope have led to the discovery of more than 4000 exoplanet candidates consisting of many systems with Earth- to Neptune-sized objects that reside well inside the orbit of Mercury around their respective host stars. How and where these close-in planets formed is one of the major unanswered questions in planet formation. Here, we calculate the required disk masses for in situ formation of the *Kepler* planets. We find that if close-in planets formed as *isolation masses*, then standard gas-to-dust ratios yield corresponding gas disks that are gravitationally unstable for a significant fraction of systems, ruling out such a scenario. We show that the maximum width of a planet's accretion region in the absence of any migration is  $2v_{\text{esc}}/\Omega$ , where  $v_{\text{esc}}$  is the escape velocity of the planet and  $\Omega$  is the Keplerian frequency, and we use it to calculate the required disk masses for in situ formation with giant impacts. Even with giant impacts, formation without migration requires disk surface densities in solids at semi-major axes of less than 0.1 AU of  $10^3\text{--}10^5\text{ g cm}^{-2}$ , implying typical enhancements above the minimum-mass solar nebular (MMSN) by at least a factor of 20. Corresponding gas disks are below but not far from the gravitational stability limit. In contrast, formation beyond a few AU is consistent with MMSN disk masses. This suggests that the migration of either solids or fully assembled planets is likely to have played a major role in the formation of close-in super-Earths and mini-Neptunes.

*Key words:* planets and satellites: dynamical evolution and stability – planets and satellites: formation – protoplanetary disks

*Online-only material:* color figures

### 1. INTRODUCTION

NASA's *Kepler* mission has been a great success. To date it has discovered over 4000 exoplanet candidates (Batalha et al. 2013). The results from the *Kepler* mission have provided us, for the first time, with a robust determination of the relative abundances of different-sized planets ranging from Earth-sized bodies all the way to Jupiter-sized planets with periods of less than 100 days. We now know that planets smaller than Neptune are ubiquitous and that about 50% of all Sun-like stars harbor an exoplanet smaller than Neptune with a period of less than 100 days (Howard et al. 2012; Fressin et al. 2013). The results from *Kepler* reveal a new population of planets that consists of Earth- to Neptune-sized bodies that reside well inside the orbit of Mercury around their respective host stars. This new class of planets is unlike anything found in our own solar system, raising fundamental questions concerning their nature and formation.

Planet formation is generally considered to consist of several distinct stages (e.g., Goldreich et al. 2004). In the first phase, dust settles into the mid-plane of the solar nebula and accumulates into planetesimals (Goldreich & Ward 1973; Youdin & Shu 2002). In the second stage, runaway growth leads to the rapid formation of a small number of large, roughly lunar-sized protoplanets (e.g., Safronov 1972; Wetherill & Stewart 1989; Schlichting & Sari 2011). In the third stage, the growth transitions to oligarchic growth once protoplanets become massive enough to dominate the gravitational stirring in their respective feeding zones (e.g., Kokubo & Ida 1998; Rafikov 2003). By the end of oligarchic growth, protoplanets have consumed most of the material in their respective feeding zones and thereby reached their *isolation masses*. In the outer parts of the disk, *isolation masses* are comparable to the masses of Uranus and Neptune. However, in the inner regions, *isolation masses*

are only a fraction of an Earth mass. The terrestrial planets are therefore thought to have undergone an additional stage in the planet formation process consisting of collisions of a few dozen protoplanets, called giant impacts (Chambers & Wetherill 1998; Agnor et al. 1999). Numerical modeling of this final stage of terrestrial planet formation (Chambers 2001) generally produces about the right masses and number of terrestrial planets. The typical eccentricities of those planets are significantly larger than those of the terrestrial planets in our solar system today, but dynamical friction provided by small, leftover planetesimals (Raymond et al. 2006; Schlichting et al. 2012) can dampen the eccentricities to observed values.

What makes the many planetary candidates discovered by *Kepler* so intriguing is that they have orbital distances well inside our terrestrial planet region, but their typical sizes, densities, and inferred compositions more closely resemble those of Uranus and Neptune (Lopez & Fortney 2014; Rogers 2014). Understanding how these close-in planets formed is one of the major unanswered questions in planet formation.

Bodenheimer & Lissauer (2014) performed detailed numerical simulations of gas accretion onto *isolation masses* at formation locations from 0.5 to 4 AU and concluded that the *Kepler*-11 systems likely formed further out in the disk with subsequent inward migration. Chiang & Laughlin (2013) recently proposed that close-in super-Earths could have formed in situ from typical disks that are enhanced by about a factor of five compared to the minimum mass solar nebula (Hayashi 1981) and find a radial disk mass surface density profile  $\Sigma \propto a^{-1.6}$ , which has a similar scaling to the minimum-mass solar nebular (MMSN). However, Raymond & Cossou (2014) used known *Kepler* systems that contained at least three planets to construct an MMSN. They find that it is inconsistent to assume a universal disk density profile and that many of the resulting disk profiles

cannot be explained by viscous gas disk models (Chiang & Goldreich 1997; Lynden-Bell & Pringle 1974). Hansen & Murray (2012) proposed that 50–100  $M_{\oplus}$  of rocky material was delivered to the inner regions of the protoplanetary disk and that the final assembly of planets occurred locally via giant impacts. Finally, Boley & Ford (2013) and Chatterjee & Tan (2014) suggested that inward drifting material is stopped and collected in a pressure maximum in the disk and that planet formation proceeds from there either by core accretion or by gravitational instability.

In this Letter, we examine the minimum disk masses required for in situ formation of close-in super-Earths and mini-Neptunes in the absence of the migration of solids and/or planets. We calculate the minimum disk masses needed to form these planets as *isolation masses* similar to Uranus and Neptune, as assumed by Rogers et al. (2011) and Bodenheimer & Lissauer (2014), and also determine the disk masses required if planets formed with a final stage of giant impacts analogous to the terrestrial planets in the solar system as suggested by Chiang & Laughlin (2013). Assuming standard dust-to-gas ratios, we examine the stability of the inferred gas disk against gravitational collapse.

This Letter is structured as follows. In Section 2.1, we first derive the maximum planet masses that a body can grow to in the absence of migration and use this to infer the local disk surface densities that would have been required for in situ formation. In Section 2.2, we show that for standard gas-to-dust ratios, a significant fraction of these gas disks are close to, or even beyond, the gravitational stability limit. We compare the required disk masses for in situ formation to the MMSN in Section 2.3. Our discussions and conclusions follow in Section 3.

## 2. FORMATION OF CLOSE-IN SUPER-EARTHS AND MINI-NEPTUNES

### 2.1. Maximum Planet Masses without Migration

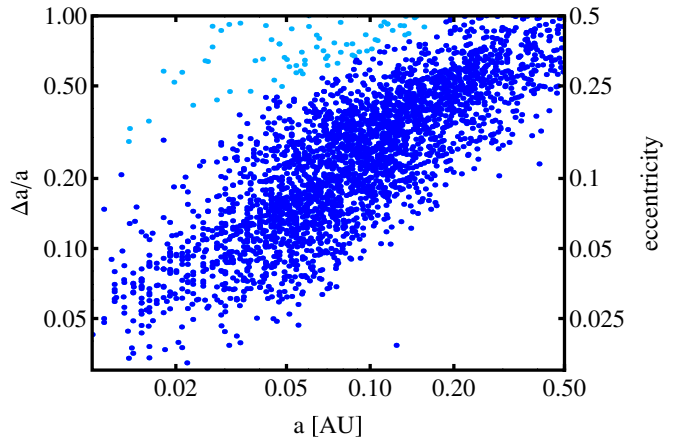
The largest mass a planet or protoplanet of radius  $R$  can grow to in the absence of any migration is its *isolation mass*,  $M$ , defined as the sum of all the material in its local feeding zone, and is given by

$$M = 2\pi a \Delta a \Sigma, \quad (1)$$

where  $a$  is the semi-major axis,  $\Delta a$  is the width of the feeding zone, and  $\Sigma$  is the mass surface density of solids in the disk. The width of the feeding zone is given by the radial extent over which the planet can accrete material and therefore depends on the planet's and planetesimals' velocity dispersions. It is usually assumed that both have random velocities less than the Hill velocity, such that their relative velocities are dominated by the Keplerian shear of the disk. In this case,  $\Delta a \sim 2v_H/\Omega$ , where  $\Omega$  is the Keplerian frequency,  $v_H = a\Omega(M/3M_{\odot})^{1/3}$  is the planet's Hill velocity,  $M_{\odot}$  is the mass of the host star, and the factor of two accounts for the contributions from planetesimals residing interior and exterior with respect to the planet. Numerical integrations find that the largest impact parameters leading to accretion are about a factor of 2.5 times larger than the above estimate for the width of the planet's feeding zone (Greenzweig & Lissauer 1990). This yields an *isolation mass* of

$$M = \frac{(10\pi\Sigma a^2)^{3/2}}{(3M_{\odot})^{1/2}}. \quad (2)$$

Evaluating the *isolation mass* assuming that  $\Sigma$  is given by the MMSN,  $\Sigma_{\text{MMSN}} = 7 \times (a/1 \text{ AU})^{-3/2} \text{ g cm}^{-2}$  (Hayashi 1981),



**Figure 1.** Maximum width of the accretion zone,  $\Delta a$ , divided by the semi-major axis,  $a$ , as a function of  $a$  for *Kepler* planetary candidates. The dark blue points correspond to systems with planetary radii of  $R \leq 5 R_{\oplus}$  and the light blue points to systems with planetary radii of  $R > 5 R_{\oplus}$ . A density of  $2 \text{ g cm}^{-3}$  was assumed when converting planetary radii into masses throughout this Letter. At small distances from the star, the accretion zones are only a small fraction of the planet's semi-major axis. The ratio  $\Delta a/a$  can also be thought of as the planet formation efficiency, because its inverse gives an estimate of the number of similarly sized planets that should have formed interior to the observed *Kepler* planet if the disk extended inward toward the central star. The y axis on the right side displays the corresponding eccentricities.

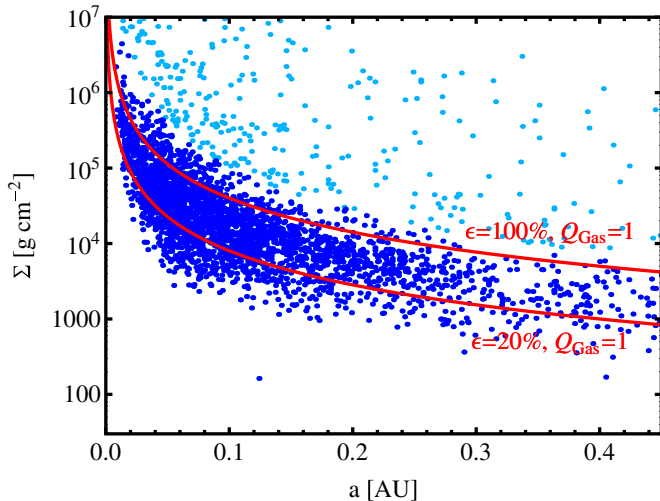
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yields  $M \simeq 0.03 M_{\oplus}$  at 1 AU. Due to these small *isolation masses*, the terrestrial planets are believed to have formed from a series of giant impacts of a few dozen protoplanets (e.g., Agnor et al. 1999; Chambers 2001).

Using Equation (1), we can also calculate the largest planetary masses that form as a result of giant impacts. Viscous stirring increases the velocity dispersion,  $v$ , of all the bodies in the disk by converting the energy associated with the Keplerian shear into the random kinetic energy of the protoplanets. In this way, protoplanets can mutually stir themselves to a velocity dispersion comparable to their own escape velocity,  $v_{\text{esc}}$ . Once velocity dispersions of  $v_{\text{esc}}$  are achieved, the collision rate,  $\mathcal{R}_{\text{coll}} \simeq n v \pi R^2 (1 + (v_{\text{esc}}/v)^2)$ , exceeds the rate for gravitational stirring,  $v^{-1} dv/dt \simeq n v \pi R^2 (v_{\text{esc}}/v)^4$ , where  $n$  is the number density of protoplanets (Safronov 1972; Goldreich et al. 2004) and  $v$  can only be increased significantly further in a single interaction by encounters with minimum encounter distances of less than the protoplanet's radius. Such encounters, however, result in a collision rather than a gravitational deflection. Therefore, the maximum distance from which planetesimals and comparably sized protoplanets can be accreted is given by  $\Delta a \simeq 2v_{\text{esc}}/\Omega$ , which yields

$$\Delta a \simeq 2^{3/2} a \left( \frac{a}{R} \frac{M}{M_{\odot}} \right)^{1/2}. \quad (3)$$

This corresponds to eccentricities of  $e \simeq \Delta a/2a \simeq (2aM/RM_{\odot})^{1/2}$ . Figure 1 shows the maximum width of the accretion zone,  $\Delta a$ , divided by the semi-major axis,  $a$ , as a function of  $a$  for *Kepler* planetary candidates. At small distances from the star, the accretion zones are only a small fraction of the planet's semi-major axis, which is very different from the assumption made by Chiang & Laughlin (2013), who used  $\Delta a \sim a$ , and requires eccentricities of the order of unity. The ratio  $\Delta a/a$  can also be thought of as the planet formation efficiency, because its inverse gives an estimate of the number of similarly sized planets that should have formed interior to the observed *Kepler*



**Figure 2.** Mass surface density in solids,  $\Sigma$ , needed to form the *Kepler* candidates as *isolation masses*, by accreting all the material in their respective feeding zones without migration of solids and/or planets. The dark blue points correspond to systems with planetary radii  $R \leq 5 R_{\oplus}$  and the light blue points to systems with planetary radii  $R > 5 R_{\oplus}$ . The upper and lower solid red lines corresponds to the Toomre  $Q$  stability parameter of 1 for the corresponding gas disk, assuming a gas-to-dust ratio of 200 and a planet formation efficiency of  $\epsilon = 100\%$  and  $\epsilon = 20\%$ , respectively. A significant fraction of systems fall above the  $\epsilon = 100\%$ ,  $Q_{\text{Gas}} = 1$  line, implying that these disks would be gravitationally unstable to collapse.

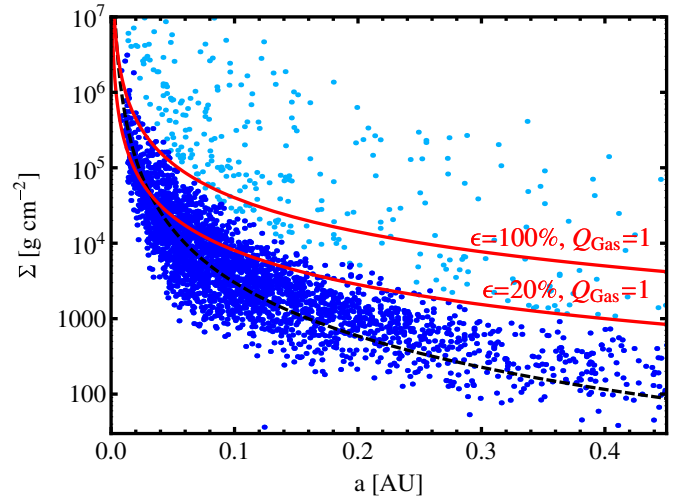
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planet if the disk extended inward toward the central star. Given the large number of single-planet systems discovered by *Kepler* (Batalha et al. 2013), Figure 1 therefore also shows that true in situ formation must have been very inefficient at small semi-major axis. If most *Kepler* candidates formed in situ at  $a < 0.1$  AU without migration, then less than 20% of all the solids present were converted into the planets observed today. Our results on the maximum accretion width and its implication for the number of planets formed by giant impacts are also the likely explanation for why numerical simulations of in situ assembly by giant impacts find much fewer single-planet systems (Hansen & Murray 2013) than have been discovered by *Kepler*.

Substituting for  $\Delta a$  from Equation (3) into Equation (1) yields a maximum planet mass of

$$M_{\text{max}} \simeq \frac{[2^{5/2} \pi a^2 \Sigma (\rho/\rho_{\odot})^{1/6} (a/R_{\odot})^{1/2}]^3}{M_{\odot}^{1/2}}. \quad (4)$$

The maximum mass in Equation (4) should be close to the absolute maximum mass that a planet can grow to due to giant impacts, because even if the velocity dispersion of the protoplanets could somehow be significantly excited above  $v_{\text{esc}}$ , mutual giant impacts of protoplanets with random velocities equal to  $v_{\text{esc}}$  and larger typically do not lead to accretion (Asphaug 2010). Evaluating Equation (4) for the MMSN at 1 AU yields  $M_{\text{max}} \simeq 1.4 M_{\oplus}$ . We somewhat overestimate the actual width of the accretion zone because we assume that all the random velocity is excited in the plane rather than distributed in comparable amounts between eccentricity and inclination (Ida & Makino 1992). The actual accretion width will therefore be, on average, smaller by up to a factor of two compared to Equation (3). This is also consistent with the typical eccentricities that are found in  $N$ -body simulations at the end of giant impacts, which have characteristic values of less than 0.2 (Chambers 2001).



**Figure 3.** Same as Figure 2, but for solid mass surface density,  $\Sigma$ , needed to form the *Kepler* candidates in situ with a phase of giant impacts. The mass surface densities displayed here are calculated assuming  $\Delta a \simeq 2v_{\text{esc}}/\Omega$ . This corresponds to the maximum accretion widths that can result in disks in which protoplanets stir themselves gravitationally. Furthermore, even if the velocity dispersion could be excited significantly above  $v_{\text{esc}}$ , the resulting giant impacts typically would not lead to accretion and may, in some cases, result in erosion instead (Asphaug 2010). The dashed black line is the best-fit disk surface density model and is given by  $\Sigma = 13 \times (a/1 \text{ AU})^{-2.35}$ .

(A color version of this figure is available in the online journal.)

Figures 2 and 3 show the mass surface density in solids needed to form the observed *Kepler* planets in situ as *isolation masses* (i.e., Equation (2)) and with a phase of giant impacts (i.e., Equation (4)), respectively. The mass surface densities that we find are higher than those calculated in previous works, since these works assumed that solids can be accreted over an annulus with a width of the order of  $a$  (Chiang & Laughlin 2013). The best-fit disk surface density model for the *Kepler* planets with  $R < 5 R_{\oplus}$  is  $\Sigma = 13 \times (a/1 \text{ AU})^{-2.35}$ . This scaling is steeper than that found by Chiang & Laughlin (2013) because of the additional  $a^{1/2}$  dependence on  $\Delta a$  in Equation (3).

## 2.2. Disk Stability

The Toomre instability criterion for a gas disk is

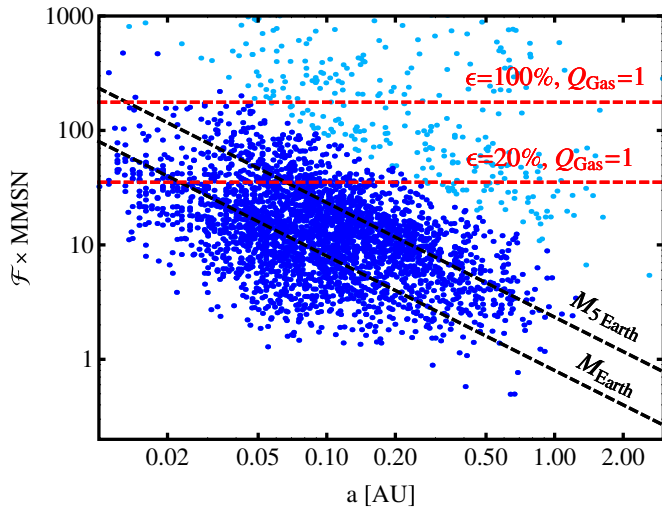
$$Q_{\text{Gas}} \equiv \frac{c_s \Omega}{\pi G \Sigma_{\text{gas}}} < 1 \quad (5)$$

(Toomre 1964; Goldreich & Lynden-Bell 1965). Assuming an isothermal disk with a temperature of  $10^3$  K and a gas-to-dust ratio of  $\Sigma_{\text{gas}}/\Sigma = 200$  (D'Alessio et al. 2001) yields

$$Q_{\text{Gas}} \simeq 4 \times \left( \frac{a}{0.1 \text{ AU}} \right)^{-3/2} \left( \frac{\Sigma}{10^4 \text{ g cm}^{-2}} \right)^{-1}. \quad (6)$$

The upper and lower solid red lines in Figures 2 and 3 show the Toomre  $Q_{\text{Gas}}$  stability parameter  $\sim 1$  for the corresponding gas disk with a gas-to-dust ratio of 200, assuming planet formation efficiencies of 100% and 20%, respectively. A planet formation efficiency of 100% means that all the solids in the accretion zone of width  $\Delta a$  are ultimately accreted onto the planet, whereas a planet formation efficiency of  $\epsilon = 20\%$  implies that only one-fifth of the solids end up as planets.

Figure 2 shows that even if we assume a 100% planet formation efficiency, a significant fraction of *Kepler* systems



**Figure 4.** Enhancement factor above the MMSN,  $\mathcal{F} = \Sigma/\Sigma_{\text{MMSN}}$ , needed for in situ formation as a function of semi-major axis. Planetary candidates discovered by *Kepler* are represented by blue points, where the dark blue points correspond to systems with planetary radii  $R \leq 5 R_{\oplus}$  and the light blue points to systems with planetary radii  $R > 5 R_{\oplus}$ . For comparison, the green points correspond, from right to left, to Earth, Venus, and Mercury. The lower and upper dashed black lines display the enhancement factors needed to form a  $1 M_{\oplus}$  planet and a  $5 M_{\oplus}$  planet, respectively. The red dashed lines give the Toomre  $Q$  parameter for the corresponding gas disk,  $Q_{\text{Gas}}$ , assuming a gas-to-dust ratio of 200 and planet formation efficiencies of 100% and 20%, respectively.

(A color version of this figure is available in the online journal.)

fall above the gravitational stability limit, implying that such gas disks are gravitationally unstable to collapse. From this, we conclude that these planets therefore cannot have formed as *isolation masses* at their current locations. Figure 3 shows that if most close-in *Kepler* planets were assembled by giant impacts with a planet formation efficiency of  $\epsilon = 100\%$ , then the corresponding gas disks of *Kepler* planets with  $R < 5 R_{\oplus}$  fall close to but typically below the gravitational instability limit. If the planet formation efficiency was somewhat less than 100%, then many of the corresponding gas disks would be unstable. Although our findings do not rule out in situ formation by giant impacts, the initial gas disks would have to have been close to the gravitational stability limit.

### 2.3. Comparison to the Minimum Mass Solar Nebular

It is instructive to compare our minimum disk masses for in situ formation with the MMSN. Normalizing Equation (4) to the MMSN yields

$$\frac{M_{\text{max}}}{M_{\oplus}} \simeq 1.4 \times \left( \frac{\mathcal{F}a}{1 \text{ AU}} \right)^{3/2}, \quad (7)$$

where  $\mathcal{F}$  is the enhancement factor in solids above the MMSN,  $\mathcal{F} \equiv \Sigma/\Sigma_{\text{MMSN}}$ . This implies that for an MMSN radial disk density profile, the maximum planet mass decreases as  $a^{3/2}$ . Forming close-in planets in situ therefore requires a significant enhancement in solids over the MMSN. For example,  $\mathcal{F} \sim 20$  and  $\mathcal{F} \sim 100$  are required to form a  $5 M_{\oplus}$  planet at 0.1 AU and 0.02 AU, respectively. Figure 4 shows the enhancement factor needed to form the *Kepler* candidates in situ. Most *Kepler* systems require disk masses that are significantly enhanced above the MMSN for in situ formation. In contrast, formation beyond a few AU is fully consistent with MMSN disk masses.

## 3. CONCLUSIONS

We have calculated the disk masses required to form close-in super-Earths and mini-Neptunes in situ from *isolation masses*. We find that the standard gas-to-dust ratios yield gas disks that are gravitationally unstable for a significant fraction of systems, ruling out such a scenario. In addition, we showed that the maximum width of a planet's accretion region in the absence of any migration is  $2v_{\text{esc}}/\Omega$ . This maximum width is due to the fact that planets can gravitationally excite their velocity dispersions to values comparable to their escape velocities, but not significantly beyond that. We used this maximum accretion width to calculate the required disk masses for in situ formation of the observed *Kepler* systems with giant impacts. Our results imply that even with giant impacts, formation without migration of solids or planets requires typical disk surface densities in solids at semi-major axes less than 0.1 AU of  $10^3$ – $10^5 \text{ g cm}^{-2}$ . This corresponds to typical enhancements above the MMSN by at least a factor of 20. For standard dust-to-gas ratios, this yields gas disk masses close to the gravitational stability limit. These findings are not sensitive to the exact form of the mass–radius relationship. Using published mass–radius relationships (Lissauer et al. 2011; Weiss & Marcy 2014), instead of simply assuming a density of  $2 \text{ g cm}^{-3}$  strengthens our results somewhat, since these relationships yield more massive planets for  $R < 3 R_{\oplus}$  compared to our mass–radius relationship, increasing the values of  $\Sigma$  that make up the lower envelopes in Figures 2 and 3, and hence increasing the number of systems that lie close to, or above, the gravitational stability limit. Furthermore, we find that the best-fit mass surface density profile for the solids in the disk inferred from the population of *Kepler* planets is  $\Sigma = 13 \times (a/1 \text{ AU})^{-2.35}$ . However, such disk density profiles are much steeper than those inferred from sub-millimeter observations of cold dust in the outer parts of protoplanetary disks, which typically find surface density profiles of  $\propto a^{-1.0}$  (e.g., Andrews et al. 2009). This leads us to conclude that in stark contrast to the terrestrial planets in our solar system, which likely formed close to their current locations from the material locally available in the disk, the formation of close-in super-Earths and mini-Neptunes requires either the transport of large quantities of solids to the inner disk (Hansen & Murray 2012; Chatterjee & Tan 2014), significantly decreasing the local dust-to-gas ratio, or formation at larger semi-major axes and subsequent migration to their current locations.

Recent sub-millimeter observations (Andrews et al. 2012) and theoretical modeling (Birnstiel & Andrews 2014) suggest that drift in viscous disks rapidly modifies the radial distribution of dust-to-gas ratios in the outer parts of protoplanetary disks such that the standard assumption that  $\Sigma_{\text{Gas}} \sim 200\Sigma$  is no longer valid (Williams & Best 2014). No such observations exist for the inner most parts of the disk, but it is possible that radial drift gives rise to a significant increase in the amount of solids locally available. Since migration of solids increase the fraction of solids available relative to the gas, it offers a way to locally increase the solid disk surface densities without making the gas disks so massive that they become gravitational unstable. True in situ formation is very inefficient at small semi-major axes (see Figure 1) and it should have produced a larger fraction of multiple-planet systems than observed. Even with migration of solids, planet formation efficiencies will remain low, unless material can be trapped locally or unless most of the solids are accreted by a single growing planet, requiring almost complete accretion as the solids drift through the planet's feeding zone.

Planet formation at larger semi-major axes and subsequent migration offers the other solution for the formation of the observed close-in *Kepler* planets. Formation of super-Earths and mini-Neptunes at distances of 1 AU or larger requires no significant enhancement above the MMSN (see Figure 4). For example, an MMSN type disk would be sufficient for the formation of a  $5 M_{\oplus}$  planet at 2 AU. The outcome of type I migration, when both migration and eccentricity damping due to the planet's interaction with the gas disk are considered, is consistent with the observation that most ( $\gtrsim 90\%$ ) *Kepler* planets are currently not in or near mean-motion resonances (Goldreich & Schlichting 2014). Furthermore, a significant fraction of close-in super-Earths and mini-Neptunes are thought to have large gaseous envelopes containing up to 1%–10% of their total mass. Models examining the accretion and subsequent photo-evaporation of such gaseous envelopes favor formation at a few AU and subsequent inward migration over in situ formation (Lopez et al. 2012; Bodenheimer & Lissauer 2014).

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