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Calibrating genomic and allelic coverage bias in single-cell sequencing

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Abstract

1 Artifacts introduced in whole-genome amplification (WGA) make it difficult to derive
2 accurate genomic information from single-cell genomes and require different analytical
3 strategies from bulk genome analysis. Here we describe statistical methods to quantitatively
4 assess the amplification bias resulting from whole-genome amplification of single-cell genomic
5 DNA. Analysis of single-cell DNA libraries generated by different technologies revealed
6 universal features of the genome coverage bias predominantly generated at the amplicon level
7 (1-10 kb). The magnitude of coverage bias can be accurately calibrated from low-pass
8 sequencing ($\sim 0.1x$) to predict the depth-of-coverage yield of single-cell DNA libraries
9 sequenced at arbitrary depths. We further provide a benchmark comparison of single-cell
10 libraries generated by multi-strand displacement amplification (MDA) and multiple annealing
11 and looping-based amplification cycles (MALBAC). Finally we develop statistical models to
12 calibrate allelic bias in single-cell whole-genome amplification and demonstrate a census-based
13 strategy for efficient and accurate variant detection from low-input biopsy samples.

14 Introduction

15 Single-cell sequencing has provided unique insights into the genetic diversity of living
16 organisms and among different cells within the same individual¹⁻³. Recent single-cell analyses
17 have uncovered different clonal populations within a single tumor^{4,5}, revealed genomic diversity
18 in gametes^{6,7} and neurons^{8,9}, and resolved historical cellular lineages during development^{10,11}.
19 Single-cell sequencing also has many potential clinical applications, such as characterization of
20 circulating tumor cells^{12,13} or fine-needle aspirates for clinical diagnostics.

21 A major drawback of single-cell sequencing, however, is the need to amplify genomic
22 DNA prior to genomic characterizations¹⁴⁻¹⁷. Due to the limited processivity (<100 kb) and
23 strand extension rate (<100 nt/second) of DNA polymerases, the amplification of large genomes
24 requires priming and extension at millions of loci, each amplified 10,000 to 1,000,000 fold. Such
25 a large number of polymerase reactions inevitably generate amplification errors that confound
26 the detection of genetic variants (**Supplementary Fig. 1**). Furthermore, differential priming
27 efficiencies and extension rates result in uneven amplifications across the genome^{18,19} and
28 skewed representations of homologous chromosomes. These variations both compromise variant
29 detection sensitivity and may lead to incorrect genotypes^{5,12}. Although technological innovations
30 may improve the fidelity of whole-genome amplification (WGA)^{15-17,20-23}, statistical fluctuations
31 in the amplifications of millions of different DNA templates will persist.

32 As genetic variants are detected by the relative abundance of variant-containing DNA
33 templates in the library, non-uniformity in genome coverage directly impacts the sensitivity to
34 detect variants. For example, grossly non-uniform libraries emphasize only over-represented
35 regions of the genome, and contain little information on other regions. Current methods to assess
36 the uniformity of WGA rely on either direct visual inspection or various statistical measures of
37 the sequencing coverage at the base-level^{18,22} or the allele-level^{5,12}. These empirical methods and
38 metrics generally require substantial sequencing (10x or greater) and only gauge the deviation of
39 amplified DNA from the "uniform" bulk DNA at a particular sequencing depth. They fail,
40 however, to characterize the intrinsic non-uniformity resulting from WGA that is independent of
41 sequencing depth (**Fig. 1a,b**). Moreover, the nature of the main sources of bias remains poorly
42 characterized (**Fig. 1c**).

43 Here we report a systematic analysis of the coverage bias in single-cell whole-genome
44 amplification. We show that the structure of individual WGA amplicons imparts a dominant
45 amplification bias on length scales longer than the average size of sequencing fragments.
46 Sequencing at low depths (0.1-1x) can effectively reveal this variation in the amplicon-level
47 coverage, and enable accurate predictions of the depth-of-coverage yield when sequencing
48 single-cell libraries to arbitrary depths. We further characterized the amplification bias between
49 homologous chromosomes using analytically solvable models and validated these model
50 predictions of allelic coverage by experimentally observed coverage at heterozygous sites. These
51 results provide a framework for quality assurance of single-cell libraries and for estimating the
52 sensitivity to detect local variants—such as single-nucleotide variants or chromosomal
53 translocations—present in an individual cell at a given sequencing depth. Finally we demonstrate
54 that the amplification bias in multi-strand displacement amplification (MDA) is more random
55 than recurrent. Although such random bias cannot be corrected systematically, it suggests an
56 efficient census-based strategy to accurately determine somatic genetic variants in small biopsy
57 samples by sequencing multiple single cells from the same sample at modest depths.

58 **Results**

59 **Information yield from bulk and single-cell sequencing**

60 In bulk DNA libraries, each sequencing fragment represents genomic information from
61 an individual cell; therefore, the information content increases with the sequencing depth until
62 fragments are sequenced to exhaustion. The information content of a DNA library (“library
63 complexity”) is thus measured by the total number of distinct molecules (sequencing fragments)
64 in the library²⁴⁻²⁶. This measure is essentially determined by the total number of cells (or the total

65 amount of genomic DNA) used to prepare the library (**Fig. 1a**, left panel). In single-cell DNA
66 sequencing, whole-genome amplification (WGA) precedes the construction of a DNA library
67 and introduces non-uniformity across the genome: As sequencing depth increases, more genomic
68 regions are uncovered (**Fig. 1a**, right panel). Hence the fraction of the single-cell's genome
69 uncovered at a given sequencing depth determines the information content of single-cell
70 sequencing. This measure ultimately depends on the uniformity of genome coverage, or the
71 magnitude and spread of whole-genome amplification bias, and is conceptually equivalent to a
72 “single-cell DNA library complexity.”

73 **Amplicon-level bias dominates coverage variation**

74 Visual inspection of single-cell sequencing coverage suggests that the genome coverage
75 varies at many different length scales (**Fig. 1b**). To systematically evaluate the amplification bias
76 in single-cell libraries, we sequenced multi-strand displacement amplified (MDA) DNA libraries
77 of diploid RPE-1 cells (5-10x) and compared the sequencing coverage to a matched, unamplified
78 bulk DNA library (~12x). To eliminate the effects of sequencing depths, we computationally
79 down sampled the bulk and single-cell DNA libraries and calculated the auto-correlation of base-
80 level coverage in diploid chromosome 1 at various depths to examine coverage correlations at all
81 length scales (**Fig. 2a**, **Supplementary Fig. 2**). Both bulk and MDA libraries exhibited a
82 correlation at length scale $l_c \approx 100$ bp, reflecting the sequencing read length (101 bp). Looking
83 more closely we also identified a correlation at $l_c \approx 250$ bp, corresponding to the average size of
84 the paired-end fragments (**Supplementary Fig. 2**). As expected, the magnitude of such
85 correlations at the fragment scale decays with increasing sequencing depth.

86 Besides the fragment-level correlations, the bulk DNA sequencing coverage showed
87 minimal correlation between loci separated by more than 1 kb. In contrast, single-cell libraries

88 exhibited a prominent correlation in 1-100 kb that is independent of the sequencing depth.
89 Independent sequencing of the same single-cell library to 0.1x on the Illumina MiSeq platform
90 and to 9x on the HiSeq platform revealed the same correlation with a characteristic length $l_c \approx 33$
91 kb (**Fig. 2a**). The sequencing-depth-independent correlation reflects the intrinsic non-uniformity
92 in the DNA library and suggests a characteristic length scale of amplification bias.

93 The predominant correlation at l_c suggests adjacent loci within this distance have
94 comparable coverage. This observation implies the primary source of coverage variation (or
95 amplification bias) is at or above the distance l_c . Therefore, statistical variation of coverage at the
96 single-base level should reflect coverage variation at the amplicon level. To test this hypothesis,
97 we computed the cumulative distribution of bin-level coverage (bin size $\approx 17\text{Kb}$, half of l_c).
98 Normalizing the bin-level coverage by the mean depth-of-coverage, we found the cumulative
99 distribution of bin-level coverage to be nearly identical between independent sequencing at 9x or
100 at 0.1x (**Fig. 2b**), confirming that the amplicon-level coverage variation is intrinsic to the
101 amplified DNA but independent of the sequencing depth. Furthermore, the cumulative
102 distribution of single-base coverage at 9x sequencing depth aligned with the bin-level coverage
103 (**Fig. 2b, Supplementary Fig. 2**), suggesting that the amplicon-level variation was indeed the
104 dominant source of non-uniformity in single-cell libraries.

105 To further validate this conclusion, we computed the depth-of-coverage (DoC) curves
106 and the Lorenz curves for the bulk RPE-1 library and a single RPE-1 library by MDA at different
107 bin sizes (**Supplementary Fig. 3**). For the bulk library, the distribution of single-base level
108 coverage is indistinguishable from that evaluated at the bin level when the bin size is smaller
109 than the fragment size (~ 300 bp); above this scale the bin-level distribution is more uniform than
110 the single-base level distribution, reflecting smoothing of coverage non-uniformity.

111 By contrast, for the MDA generated library, the distribution of single-base level coverage
112 remains constant until the bin size exceeds the amplicon size ~ 10 kb. Characterization of
113 coverage non-uniformity by Lorenz curves²² also confirmed that the same bias was observed for
114 bin sizes less than or comparable to the amplicon size and was independent of the sequencing
115 depth. In particular, at sequencing depths $\ll 1x$, the majority of the genome is uncovered and
116 shows no variation in the single-base-level coverage; amplification bias, however, is manifested
117 in the correlation between covered loci and can be evaluated by low-pass sequencing. For typical
118 MDA-generated libraries, the amplicon size ($\sim l_c$) is on the order of 10 kb, hence at 0.1x
119 sequencing depth there are $0.1 \times 10^4 / 100 \approx 10$ reads (assuming 100 bp single-end reads) on
120 average for each amplicon. As long as the number of reads per amplicon is much larger than the
121 statistical variation due to random selection in sequencing (e.g., assuming poisson distribution,
122 the standard deviation of the observable is given by the square root of the expectation), the
123 percentage of such amplicons can be accurately calculated. At 0.1x sequencing, the amplicon-
124 level coverage can accurately predict the fractional genome coverage down to 0.1x mean depth,
125 when there is approximately one read for each of these under-represented amplicons; below this
126 depth, low-pass sequencing at 0.1x cannot distinguish between regions that are severely under-
127 amplified ($< 0.1x$ mean depth) and those that dropped out of amplification.

128 **Magnitude of amplicon-level variation determines coverage**

129 We tested the validity of the correlation analysis by analyzing DNA libraries generated
130 from different types of cells and by different amplification technologies. For this purpose, we
131 analyzed single-cell sequencing data of additional RPE-1 samples (**Supplementary Fig. 2**) and
132 data from multiple published studies, including frozen glioblastoma nuclei²⁷ (**Supplementary**
133 **Fig. 4**), single diploid lymphoblastoid cells⁵ (**Supplementary Fig. 5**), frozen single neuron

134 nuclei⁸ (**Supplementary Fig. 6**), single sperms⁶ (**Supplementary Fig. 7**), and SW480 tumor
135 cells²² (**Supplementary Fig. 8**); all samples were amplified by MDA. SW480 cells were also
136 amplified by quasi-linear multiple annealing and looping-based amplification cycles
137 (MALBAC). The amplicon size in MDA-generated libraries ranged from 5 to 50 kb, with the
138 sperm libraries having the lowest $l_c \approx 5$ kb (**Supplementary Fig. 7**). Interestingly, MDA of
139 hundreds or thousands of neurons exhibited similar amplicon sizes between 10-20 kb
140 (**Supplementary Fig. 6**), consistent with estimates by standard and alkaline gel electrophoresis⁸.
141 In contrast, MALBAC showed a much shorter correlation length ~ 600 bp (**Supplementary Fig.**
142 **8**), consistent with the reported average amplicon size (500-1500 bp)²². We also found
143 significant correlations at the fragment-size level in one single-cell library and the reference bulk
144 library⁵ that persisted at high sequencing depths (**Supplementary Fig. 5**); these correlations
145 reflected substantial GC bias at the fragment level absent in the other bulk libraries and likely
146 arose during library preparation due to PCR. Despite the vastly different correlation lengths
147 evident in MDA and MALBAC amplifications, our analysis accurately predicted the cumulative
148 coverage distribution in all libraries sequenced to above 10x from computationally down-
149 sampled sequencing data at 1x or less (**Supplementary Fig. 2, 4-8**).

150 To benchmark the performance of different single-cell libraries, we compared the fraction
151 of covered genome ($\geq 1x$) when each library was sequenced to 1x. This percentage was either
152 computed directly from down-sampled data (when the original data had higher depths) or
153 inferred from the depth-of-coverage curve when the original data had lower depths. The
154 coverage benchmark was plotted against the magnitude of amplicon-level variation as measured
155 by the plateau correlation strength at the amplicon scale (**Methods**) (**Fig. 2c**). As expected,
156 smaller amplification bias results in a larger fraction of covered genome. Out of the five

157 published single-cell DNA sequencing studies analyzed here, the single-neuron libraries had the
158 best overall uniformity, followed by the two single YH1 libraries; the MALBAC libraries overall
159 had less amplification bias than MDA, although optimized MDA libraries performed equally
160 well. The frozen glioblastoma libraries (59 total) exhibited a range of variations that can be fitted
161 by an empirical relationship

$$162 \quad y = \frac{0.86}{1.2 + \sqrt{x}} \quad (1)$$

163 where y is the percentage of covered genome and x is the (dimensionless) correlation magnitude.
164 Except for the single-sperm libraries that exhibited substantial bias, all other analyzed data
165 closely followed this relationship. This result suggested that the uniformity of genome coverage
166 is solely determined by the amplicon-level variation but not the amplicon size. Therefore, one
167 can directly employ this empirical relationship to benchmark the uniformity of single-cell
168 libraries by the correlation magnitude that can be accurately computed from low-pass sequencing
169 $\sim 0.1x$.

170 We further selected the best single-cell libraries from each study and compared the
171 fraction of genome covered at different depths as observed in the original high-depth sequencing
172 (**Fig. 2d**). Due to the different sequencing depths applied to these libraries, we plotted all
173 cumulative genome coverage against the normalized depth (by the mean depth). The benchmark
174 of amplification uniformity as measured by the depth-of-coverage curve agrees with the
175 computed correlation magnitude (**Fig. 2c** inset).

176 Finally we also analyzed the base-level coverage in single-cell libraries amplified by
177 degenerate oligonucleotide primed PCR (DOP-PCR)²⁸. The correlation was evident both at the
178 read length level (~ 50 bp) and on a longer scale ~ 200 bp (**Supplementary Fig. 9**) that is

179 consistent with the size of purified DOP-PCR product⁴. In comparison to MDA or MALBAC
180 generated libraries, the smaller overall correlation magnitude (at the amplicon level) explains the
181 better uniformity of DOP-PCR. Interestingly, even for the MDA generated libraries, shorter
182 amplicon size tends to result in better uniformity (**Supplementary Fig. 9**); the underlying
183 mechanism for this observation requires further characterization.

184 **Genome coverage variation reflects allele-level bias**

185 Coverage at the locus-level includes contributions from homologous chromosomes (the
186 allele-level coverage). The same non-uniformity in the genome coverage, however, may result
187 from different combinations of non-uniformity at the allelic level (**Fig. 3a**). Although allele
188 coverage determines the sensitivity to detect heterozygous variants, we rarely consider this
189 aspect in bulk sequencing due to the comparable contributions of all alleles and largely uniform
190 coverage of the genome. In single-cell libraries, however, we often observe disproportionately
191 represented alleles and numerous loci may exhibit “allelic dropout”^{5,12}. Consequently, the
192 detection sensitivity of hemizygous variants is measured by the allele coverage and needs to be
193 derived from the genome coverage.

194 To predict the allele coverage from the locus-level genome coverage, we considered two
195 limiting scenarios: a “segregated template model” (STM) assuming completely independent
196 amplification of homologous chromosomes, and a “mixed template model” (MTM) assuming
197 identical coverage of homologous chromosomes (as expected in bulk sequencing) (**Fig. 3a**). The
198 difference between the two models is most evident in highly amplified regions: STM implies
199 preferential amplification of one allele while MTM suggests that both alleles have been highly
200 amplified. Both models are analytically solvable and can be easily implemented computationally
201 (**Methods, Supplementary Fig. 10**).

202 We compared the model predictions for allele-level coverage to the observation at
203 germline heterozygous sites detected from bulk DNA sequencing (**Fig. 3b, Supplementary Figs.**
204 **5,11**). For glioblastoma libraries (**Fig. 3b**), both locus- and allele-level coverage was calculated
205 from disomic chromosome 12 at 1x sequencing depth. Coverage at heterozygous sites was
206 evaluated for different disomic chromosomes (5, 12, and 13) from higher-depth sequencing at 9-
207 10x. As expected, the total coverage (reference plus alternate bases) at these sites agreed well
208 with the prediction for locus-level coverage, reflecting similar amplification bias for different
209 chromosomes with the same copy number. Meanwhile, coverage of either reference or alternate
210 bases followed the same distribution as predicted by the STM model. These results suggested
211 homologous chromosomes are amplified almost independently during WGA and manifest the
212 same degree of amplification bias. This discovery was further underscored by the agreement
213 between the observed coverage of monosomic chromosome 10 and the STM allele-coverage
214 prediction (**Supplementary Fig. 11**).

215 We further verified that coverage of alternate or reference alleles was indeed independent
216 of each other in the glioblastoma samples by looking at the distribution of alternate and reference
217 reads at heterozygous sites in disomic chromosome 5 (**Supplementary Fig. 12**). Interestingly,
218 the two-cell RPE-1 libraries showed positive correlations between the counts of the reference
219 and of the alternate alleles (**Supplementary Fig. 12**), consistent with the MTM model
220 (**Supplementary Fig. 11**). Of the two published single YH1 libraries⁵, one agreed better with the
221 MTM model and the other agreed with the STM model (**Supplementary Fig. 5**). Whether this
222 difference resulted from the cell's initial condition (frozen vs. fresh), the stage of cell cycle, or
223 other factors requires further characterization.

224 **Census-based strategy enables efficient variant detection**

225 Our analytical prediction of the allele coverage measures the average probability of
226 capturing a single variant read in single-cell sequencing. In sequencing analysis, however, more
227 than one observation of the variant is necessary to mitigate sequencing errors. This requirement
228 substantially reduces the percentage of detectable variants at low sequencing depths. In one
229 example (GBM#4, correlation magnitude ≈ 4 for disomic chromosomes), the normalized allele
230 coverage implied that only 13.3% of clonal hemizygous variants could be confidently detected at
231 a mean sequencing depth of 1x when requiring at least two reads for each variant
232 (**Supplementary Fig. 11**). This percentage increased with sequencing depth to a limit of 79% at
233 100x. In contrast, the sensitivity to detect a sub-clonal mutation with allelic fraction of 0.4 in a
234 bulk library at 10x sequencing is $\sim 80\%$ and quickly reaches $> 95\%$ at a sequencing depth of
235 $20x^{29}$. The reduced dependence of detection sensitivity on sequencing depth for single-cell
236 libraries suggested that deep sequencing of an individual library is not an efficient approach to
237 increase power for detecting variants from libraries prepared by WGA.

238 To overcome this challenge, we devised an approach to sequence a large number of
239 single-cell genomes at only modest depths ($\sim 1x$). We simultaneously controlled for errors
240 resulting from random MDA artifacts or from sequencing by requiring true variants to appear in
241 multiple libraries (“census based”) (**Fig. 4a**). We expected this population-based approach to be
242 effective only when the amplification bias is random, but not recurrent (**Fig. 1c**). We thus
243 evaluated the correlation between the coverage of reference and alternate alleles in four
244 independent glioblastoma libraries. The small covariance (~ 0.01) between the coverage of each
245 given allele in different libraries is consistent with random MDA bias (**Table 1**). These data
246 contrasted with recurrent locus-specific amplification bias in degenerate-oligonucleotide-primed
247 PCR methods such as GenomePlex³⁰.

248 We next examined how many single cells sequenced to the same total depth would
249 maximize the total allele coverage by census-based variant detection using a representative
250 library with modest bias (GBM#4, correlation magnitude ≈ 4) (**Fig. 4b**). In all cases, our model
251 predicted maximum allele coverage when each individual cell was sequenced to a modest depth
252 ($\sim 1x$). We repeated this calculation using each of the other libraries as the representative, and
253 found that the optimal depth for detecting clonal and sub-clonal variants is always $\lesssim 1x$ (**Fig. 4c**).

254 To test this experimentally, we sequenced each of the following subsets of single
255 glioblastoma libraries to 20x total depth: 59 libraries ($\sim 0.33x$ per library), 22 libraries ($\sim 1x$ per
256 library), two libraries ($\sim 10x$ each, group A) with minimal bias (correlation magnitude ≈ 0.9 for
257 disomic chromosomes), and two libraries ($\sim 10x$ each, group B) with average bias (correlation
258 magnitude = 2~4). We genotyped germline heterozygous SNPs and detected somatic single
259 nucleotide variants (sSNVs) and small insertion/deletions (indels) by the census-based strategy
260 and compared the call sets with results from bulk DNA sequencing. For germline SNPs in
261 disomic chromosome 5, we observed that census-based detection in the two pools of single-cell
262 libraries (59 and 22 each) each uncovered more than 80% of all SNPs detected in bulk, while the
263 two sets of two libraries with minimal and average bias uncovered only $\sim 30\%$ and $\sim 5\%$ of the
264 heterozygous sites, respectively (**Fig. 4d**). A similar improvement in sensitivity was observed for
265 the detection of sSNVs and indels among the single cells sequenced to $\sim 0.33x$ and $\sim 1x$ per
266 library (as opposed to $\sim 10x$ per library), detecting more somatic variants found in bulk whole-
267 exome sequencing with fewer private or false positive calls (**Fig. 4e, Supplementary Data 1 -**
268 **5**). The false positive calls usually occur at low allele frequencies within each library and likely
269 reflect recurrent amplification errors and sequencing errors. Such errors are less frequent when
270 the library is sequenced to a low depth and can be suppressed by requiring more than one read

271 for each variant. Together, these data validate our statistical estimates of the variant detection
272 sensitivity from a population of single cell libraries and demonstrate that a census-based strategy
273 using only modest depths of sequencing for many single cells can substantially improve both
274 sensitivity and specificity for detecting variants compared to deep sequencing of individual
275 libraries.

276 **Discussion**

277 Here we have established a universal method to characterize the amplification bias in
278 single-cell DNA libraries at both locus and allele levels. Based on our discovery that intrinsic
279 amplification bias occurs predominantly at the amplicon level, we demonstrated that the
280 cumulative distribution of bin-level coverage (with bin size set to the length scale of dominant
281 amplification bias) directly predicts the depth-of-coverage at any sequencing depth. We further
282 derived a quantitative measure of amplification bias that can directly predict locus-level coverage
283 via an empirical relationship. Our analysis thus provides a statistical description of the
284 relationship between the genomic coverage of single-cell DNA libraries and the intrinsic
285 amplification bias. This metric provides a robust benchmark that enables a quantitative
286 prediction of the complexity of single-cell libraries from low-pass sequencing (0.01~0.1x).

287 We demonstrated that amplification of different chromosomes (including different
288 homologous chromosomes) in a single cell is often independent (“segregated template model”),
289 reflecting random priming and amplification. This biophysical feature is fundamentally different
290 from amplification from bulk DNA, where allele-level coverage is strongly
291 correlated^{31,32} (“mixed template model”). We proposed analytically solvable models that can
292 quantitatively predict the allele coverage of single-cell libraries at any sequencing depth. These

293 models provide the basic framework for estimating the detection sensitivity of hemizygous
294 genetic variants by single-cell sequencing.

295 The characteristic length in the coverage autocorrelation also determines the scale at
296 which the source of amplification bias should be characterized. In bulk DNA libraries, a
297 dominant bias at the fragment length level is shown to be associated with the sequence content
298 (GC%), but such bias quickly decays at longer length scales (**Supplementary Fig. 5 and 6**). In
299 MDA-generated libraries, however, we observed substantial variation even in regions with
300 similar GC content (**Supplementary Fig. 6**). This is in sharp contrast to MDAs from bulk
301 samples^{18,31-33}. Such a wide range of variation reflects random priming bias¹⁷ instead of recurrent
302 polymerase extension bias, and may also depend on the size of DNA templates after cell lysis,
303 which is known to affect displacement efficiency²¹. Our discoveries of the amplicon-level
304 correlation and independent allele amplifications are both consistent with the dominant bias
305 being generated in the early stage of amplification of single DNA templates and reflect the
306 discrete nature of single-molecule biochemical reaction. As early stage bias can be exponentially
307 amplified during subsequent cycles of amplification, limited amplification should result in better
308 uniformity^{27,34}.

309 The random nature of single-cell genome amplification further underscores the necessity
310 of single-cell specific bioinformatic tools and experimental design. Deep sequencing of single-
311 cell libraries to recover measures of variant alleles easily extends the sequencing cost and
312 becomes prohibitive for libraries with extreme bias. Our analyses suggest a more practical
313 approach by (1) preparing individual sequencing libraries from many independent samples, and
314 (2) ranking and selecting the best libraries based on the complexity and the allelic coverage

315 predicted based on low-pass whole-genome sequencing of each library (~0.1x) before extensive
316 sequencing.

317 For clinical samples with a limited number of cells, such as fine-needle aspirates or
318 circulating tumor cells, the most interesting genetic variants are shared among the cells,
319 including both sub-clonal and clonal variants. For this purpose it is most efficient to perform
320 “census-based variant detection” from multiplexed sequencing of independently amplified
321 single-cell DNA libraries each sequenced to modest depths (~ 1x). The census-based variant
322 detection strategy simultaneously controls random errors due to sequencing (0.1-1% per
323 sequenced base) or amplification (~ 1% loci with error reads exceeding 10% allele frequency,
324 **Supplementary Fig. 7**, Refs. 27 and 34) and maximizes the total allele coverage at a given
325 sequencing depth by sampling many independently amplified libraries, thus enabling accurate
326 detection of somatic variants and dissection of clonal heterogeneity.

327 One technical complication in single-cell sequencing is DNA contamination.
328 Contamination of non-human-genomic DNA before whole-genome amplification will result in a
329 large percentage of sequencing reads that are not mapped to the reference assembly, which can
330 be readily identified and excluded by low-pass sequencing. The census-based strategy also
331 effectively controls human genomic DNA contamination limited to one single-cell library.
332 Contaminations to multiple single-cell libraries are usually present at many more copies than a
333 single-cell genome at the affected loci and should be recognizable as they are substantially
334 amplified after whole-genome amplification.

335 At the current stage, errors introduced during WGA prohibit an accurate characterization
336 of individual genetic variants within a single cell. (This task can be accomplished through
337 independent amplifications of biological replicates after cell division.) It is however possible to

338 infer global features of mutagenesis, such as the mutation rates in tumor progenitor cells or
339 circulating tumor cells, by single-cell sequencing after correcting the total number of detected
340 genetic variants by the statistical power for detecting variants in a single-cell library sequenced
341 to a certain depth. Our analyses have laid the foundation for single-cell genetic variant detection
342 by calibrating the amplification bias at both genomic and allelic levels.

343

344 **Methods**

345 **Amplification and sequencing of RPE-1 cells**

346 The hTERT RPE-1 cell line stably expressing GFP-H2B was cultured and treated as
347 previously described³⁶. Briefly, cells were transfected with a pool of siRNAs (Smartpool,
348 Dharmacon) against p53 using RNAiMAX (Invitrogen) according to the manufacturer's
349 instructions. 18-hours later cells were treated with Nocodazole (100 ng/ml; Sigma) for 6 hours.
350 G2/M arrested cells were harvested by mitotic shake-off and replated after three washes with
351 medium. 4h after replating, G1- released cells were sorted into 384-well tissue culture plates and
352 cultured. Confirmed single cells were allowed to divide once, before being washed twice with
353 PBS and lysed and amplified within the 384-well tissue culture plate as outlined above.

354 Amplified DNA from two RPE-1 cells after one round of cell division was subject to
355 standard whole-genome DNA library preparation and assessed by low-pass sequencing ~ 0.1x
356 using the MiSeq platform (Illumina). DNA libraries of RPE cells (3 total) were then sequenced
357 to 4-9x on the HiSeq2500 platform (Illumina). Bulk RPE-1 DNA was sequenced to ~12x on the
358 HiSeq2500 platform (Illumina).

359 **Processing of single-cell sequencing data**

360 Sequencing reads from published studies were downloaded from the NCBI Short Read
361 Archive. For the diploid YH genome, we downloaded all sequencing runs of the bulk reference
362 (SRR294761) and two single-cell samples, “BGI_YH1” (SRR294759), and “BGI_YH2”
363 (SRR294760). For diploid neurons, we downloaded all the data from SRP014781, including
364 sequencing data for the bulk DNA, and for the whole-genome amplified products from single-
365 cell DNA, 100-cell DNA, and 50,000-cell DNA. For haploid sperms, we downloaded the deep
366 sequencing data of 8 single sperm libraries, “Sperm23” (SRS344176), “Sperm24” (SRS344190),
367 “Sperm 27” (SRS344191), “Sperm28” (SRS344192), “Sperm101” (SRS344222), “Sperm113”
368 (SRS344223), “Sperm135” (SRS344224), “Sperm136” (SRS344225). For SW480 tumor cells,
369 we obtained data corresponding to the bulk reference (SRS374235), a single-cell MDA library
370 (SRS375060), and five single-cell MALBAC libraries (SRS373654, SRS374233, SRS375671,
371 SRS375672, SRS375673). Data of the glioblastoma libraries were generated from a previous
372 study and can be accessible from SRP052627.

373 Reads were aligned to the human genome reference (hg19/GRCh37) using **bwa**
374 (<http://bio-bwa.sourceforge.net/>) in the paired-end mode. The RPE and glioblastoma libraries
375 were aligned by “bwa aln” followed by “bwa sampe” with default parameters. The
376 remaining data were aligned by “bwa mem”. PCR duplicates were removed by
377 **MarkDuplicates** from PICARD (<http://picard.sourceforge.net/>). Sequencing data of the
378 glioblastoma libraries and the matching blood were recalibrated and indel-realigned by GATK
379 (<http://www.broadinstitute.org/gatk/>) before variant detection.

380 Down-sampling of deep sequencing data to ~1x was done by **DownsampleSam** from
381 PICARD. Base-level sequencing coverage was enumerated by the **DepthOfCoverage** module
382 from GATK with minimum read mapping quality set to 5.

383 To evaluate the allele coverage in RPE-1 MDA libraries, we detected heterozygous SNPs
384 in Chr.1 of the RPE-1 cells from the sequencing of bulk RPE-1 DNA (~12x) and individual
385 MDA libraries by **UnifiedGenotyper** from GATK; only variants with Qual. ≥ 100 and at least
386 three reference and three alternate reads in the bulk sample were selected to evaluate the allele
387 coverage in MDA libraries. For other samples, we genotyped HapMap SNPs (v3.3) to
388 estimate the allelic coverage; only variants found to be heterozygous in the matching blood with
389 Qual. ≥ 500 were selected and genotyped in each set of glioblastoma libraries. Somatic single-
390 nucleotide variants and small insertions/deletions were detected by **HaplotypeCaller** from GATK
391 in each set of glioblastoma libraries and in the bulk library, and by **MuTect**²⁹ from bulk whole-
392 exome sequencing.

393 **Computation of auto-correlation function of sequence coverage**

394 The dimensionless auto-correlation function of coverage is defined as

$$395 \quad G(\Delta) = \frac{\langle C(x)C(x + \Delta) \rangle - \langle C(x) \rangle^2}{\langle C(x) \rangle^2} \quad (1)$$

396 The brackets denote average over all genomic loci x and Δ measures the spread of correlation. In
397 computing the auto-correlation functions we only include regions not adjacent to the assembly
398 gaps. (Adjacency is determined by the step Δ .)

399 The correlation function is fitted to an exponential form to estimate the correlation length
400 l_c :

$$401 \quad G(\Delta) = a + be^{-\Delta/l_c} \quad (2)$$

402 For MDA, the correlation length l_c is on the order of 10 kb and the correlation function $G(\Delta)$ is
403 roughly constant above the fragment length (~300 bp) and below the correlation length l_c . In this
404 regime, $G(\Delta)$ can be written as

$$G(\Delta) \approx \frac{\langle \bar{C}^2 \rangle - \langle \bar{C} \rangle^2}{\langle \bar{C} \rangle^2} . \quad (3)$$

405

406

407 Here \bar{C} is the average coverage within each bin $[x, x + \Delta)$. It becomes evident that $G(\Delta)$
 408 measures the standard deviation of bin-level coverage. For convenience, we choose to evaluate
 409 $G(\Delta)$ at $\Delta = 1$ kb as a quantitative metric of the magnitude of amplification bias (correlation
 410 strength).

411 **Statistical models for predicting allele coverage from genome coverage**

412 The power to detect a genetic variant is given by the probability that this variant locus
 413 (usually of one chromosome) is represented in the sequencing data, or the relative abundance of
 414 variant-supporting reads. But the direct observable in sequencing data is the total number of
 415 reads covering all possible alleles, i.e.,

$$416 \quad C = m_1 + m_2 + \dots + m_n, \quad (4)$$

417

418 where C is the total observed coverage at a given locus as a sum of contributions from each allele
 419 denoted by m_i .

420 In the presence of amplification bias both C and m_i 's vary across the genome. The
 421 distribution of C across different loci can be straightforwardly evaluated from the depth-of-
 422 coverage curve; here we want to infer the statistical distribution of m_i when the distribution of C
 423 is known. The segregated template model (STM) assumes that amplifications of homologous
 424 chromosomes are independent. As a consequence, the counts of reference and of alternate bases
 425 at heterozygous sites are independent, and one highly amplified allele may dominate over the
 426 remaining ones. In the mixed template model (MTM), different alleles are assumed to be

427 amplified to the same extent at every individual locus. As a result, the counts of reference and of
428 alternate bases at heterozygous sites follow a symmetric binomial distribution.

429 In mathematical terms, m_i 's are independent of each other but follow the same
430 distribution in STM. In this scenario, one can numerically compute the distribution of m_i from
431 the characteristic functions $C(k)$ and $m(k)$ (i.e, the Fourier transforms of the probability
432 distribution for C and m) which satisfy

$$433 \quad C(k) = m(k)^n. \quad (5)$$

434

435 Here we present an iterative method to calculate the distribution of m_i and illustrate this method
436 using a diploid genome (i.e., $n = 2$).

437 At a given sequencing depth, denote the total percentage of loci that are covered $\geq 1x$ by f ,

$$438 \quad P(C \geq 1) = f. \quad (6)$$

439

440 the percentage of loci that are covered in a particular allele is denoted by

$$441 \quad P(m_i \geq 1) = \lambda. \quad (7)$$

442

443 It is then straightforward to see that

$$444 \quad P(C \geq 1) = 1 - \prod_i (1 - P(m_i \geq 1)) \quad (8)$$

445

446 or

$$447 \quad f = 1 - (1 - \lambda)^n. \quad (9)$$

448

449 Hence in a region with n alleles, the probability that a given allele is covered is given by

450 $\lambda = 1 - (1 - f)^{1/n}$. (10)

451

452 For diploid genomes, this becomes

453 $\lambda = 1 - (1 - f)^{1/2}$. (11)

454

455 We can expand this further to compute the coverage at higher depths. For example,

456 $P(C \geq 2) = P(m_1 = 0)P(m_2 \geq 2) + P(m_1 = 1)P(m_2 \geq 1) + P(m_1 \geq 2)$ (12)

457 If we denote the percentage of loci where total coverage is at or above two as f_2 , and the

458 percentage of loci covered at or above two for each allele as λ_2 , then we have

459 $f_2 = (1 - \lambda)\lambda_2 + (\lambda - \lambda_2)\lambda + \lambda_2$, (13)

460 or

461 $\lambda_2 = \frac{f_2 - \lambda^2}{2(1 - \lambda)}$. (14)

462

463 The iteration can be continued to calculate the allele coverage at any depth,

464 $P(C \geq M) = \sum_{k=0}^{M-1} P(m_1 = k)P(m_2 \geq M - k) + P(m_1 \geq M)$ (15)

465 or (denoting $\lambda_0 = 1$, $\lambda_1 = \lambda$, etc.)

466
$$f_M = \sum_{k=0}^{M-1} (\lambda_k - \lambda_{k+1}) \lambda_{M-k} + \lambda_M$$

$$= \sum_{k=1}^{M-2} (\lambda_k - \lambda_{k+1}) \lambda_{M-k} + 2(1 - \lambda)\lambda_M + \lambda_{M-1}\lambda$$
, (16)

467 which gives

468 $\lambda_M = \frac{1}{2(1 - \lambda)} \left[f_M - \lambda\lambda_{M-1} - \sum_{k=1}^{M-2} (\lambda_k - \lambda_{k+1})\lambda_{M-k} \right]$ (17)

469 In the mixed template model, we assume that the local coverage C is a mixture of all
 470 alleles randomly sampled at the same frequency. In disomic regions, this implies that m follows a
 471 binomial distribution $B(C, 0.5)$ at any total coverage C . Under this model we have

$$\begin{aligned}
 \lambda = P(m \geq 1) &= \sum_{t=1}^M P(C = t) (1 - 0.5^t) \\
 &= \frac{1}{2} P(C \geq 1) + \frac{1}{2^2} P(C \geq 2) + \dots \\
 &= \frac{1}{2} f + \frac{1}{4} f_2 + \dots + \frac{1}{2^t} f_t + \dots
 \end{aligned} \tag{18}$$

472 where the sum runs over all observed local coverage ($t = 1, 2, \dots, M$). The series converges
 473 quickly as both f_t and the exponential prefactor decay quickly. Furthermore, one easily verifies
 474 that when f is small, this result is equal to the segregated template model to the leading order ($1/2$
 475 f).

476 It is also straightforward to calculate the allele coverage at higher depths.

$$\lambda_k = P(m \geq k) = \sum_{t=k}^M P(C = t) \left(1 - 2^{-t} \sum_{s=0}^{k-1} \frac{t!}{s!(t-s)!} \right) \tag{19}$$

479 **Census-based detection sensitivity from a pool of single-cell libraries**

480 As the percentage of genome that is covered at or above 1x at any sequencing depth can
 481 be estimated, we can also predict the census-based detection power for hemizygous variants in a
 482 pool of single-cell libraries. Consider a total number of Y libraries having similar amplification
 483 bias and the probability of observing a hemizygous variant in any of the Y libraries is given by λ ,
 484 then the probability for observing this variant in a subset of libraries (X out of Y) is given by

$$P(\text{Covered in } \geq X \text{ libraries}) = 1 - \sum_{m=0}^{X-1} \frac{Y!}{m!(Y-m)!} \lambda^m (1-\lambda)^{Y-m} \tag{20}$$

485 We can then compute this for a sub-clonal variant at clonal fraction y in a total of Z
 486 libraries from

$$P(\text{Covered in } \geq X \text{ libraries}) = 1 - \sum_{Y=0}^{X-1} \frac{Z!}{(Z-Y)!Y!} y^Y - \sum_{Y=X}^Z \frac{Z!}{(Z-Y)!Y!} y^Y \sum_{m=0}^{X-1} \frac{Y!}{m!(Y-m)!} \lambda^m (1-\lambda)^{Y-m}, \quad (21)$$

488

489 where random selection of cells containing the sub-clonal variant follows a binomial distribution

490 $B(Z, y)$.

491

492

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580 **Author contributions**

581 C.Z.Z. and V.A.A. initiated the project and carried out the analysis. C.Z.Z. performed analysis of
582 amplification bias; V.A.A. performed analysis of census-based detection sensitivity with help
583 from C.Z.Z. J.F., H.C., C.M., and K.L. prepared sequencing libraries for the RPE cell line and
584 glioblastoma samples. C.Z.Z., V.A.A., J.C.L., and M.M. wrote the manuscript with help from all
585 authors. M.M. and J.C.L. supervised the study.

586 **Competing interests**

587 M.M. is a founder and equity holder of Foundation Medicine, a for-profit company that provides
588 next-generation sequencing diagnostic services.

589 **Data access**

590 The sequence data have been deposited in the Short Read Archive from NCBI under the
591 following accession codes: RPE-1 bulk (SRX858057); two-cell RPE libraries (SRX858832,
592 SRR1779331 for RPE#1, SRR1779329 for RPE#2, SRR1779330 for RPE#3); single RPE
593 libraries (SRX858836, SRX858838, SRX858840, SRX858841); glioblastoma bulk whole-
594 genome sequencing (SRX848889); glioblastoma bulk whole-exome sequencing (SRX857666);
595 single-glioblastoma nuclei pool #1 (59 nuclei, SRX858332); single-glioblastoma nuclei pool #2
596 (22 nuclei, SRR1778915, SRR1779027, SRR1779078, SRR1779079, SRR1779080,
597 SRR1779083, SRR1779085, SRR1779088, SRR1779089, SRR1779091, SRR1779092,
598 SRR1779093, SRR1779095, SRR1779098, SRR1779157, SRR1779161, SRR1779163,
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601 #2; SRR1779348 for GBM #3; SRR1779350 for GBM #4); whole-genome sequencing of
602 blood reference for the glioblastoma patient (SRX851083); whole-exome sequencing of the
603 blood reference for the glioblastoma patient (SRX857684).

604 **Figure legends:**

605 **Figure 1 | Non-uniformity in genome coverage and its impact on the sequencing yield (a)**
606 Dependence of the information yield on the sequencing depth. Deeper sequencing of bulk
607 libraries yields information on a larger population of cells; deeper sequencing of whole-genome
608 amplified single-cell libraries reveals information on a larger fraction of the genome (thick lines).
609 **(b)** Genome coverage bias at different levels. “Amplification bias” (top): Whole-genome
610 amplification generates coverage bias at the amplicon level, which is around 10-50 kb for multi-
611 strand displacement amplification. “Sequencing bias” (bottom): Non-uniformity in the selection
612 of sequencing fragments can be caused by multiple sources of bias including whole-genome
613 amplification: the variation in sequencing coverage can be observed from 100 bp to multiple
614 megabases. **(c)** Schematic representations of recurrent and random amplification bias from
615 multiple independent amplifications of the same DNA material.

616

617 **Figure 2 | Statistical analysis of whole-genome amplification bias and coverage uniformity**
618 **(a)** Autocorrelation in the genome coverage of a two-cell RPE-1 DNA library (RPE#1) amplified
619 by multi-strand displacement amplification (MDA). The same library independently sequenced
620 to 0.1x (open triangles) and to 8x (solid triangles) exhibits a correlation above 1kb that is
621 invariant at intermediate depths (shaded triangles) from downsampling of the 9x sequencing
622 data. Black dashed curve represents exponential fitting of the autocorrelation in the 1-100 kb
623 range as $2 + 0.17e^{-\Delta/l_c}$ with a correlation length $l_c = 33$ kb. This correlation is absent in the bulk
624 library sequenced to different depths. Both the bulk and the MDA-generated libraries show a
625 sequencing-fragment-level correlation ($l_c = 100$ bp) that decays with the sequencing depth. **(b)**
626 The identical normalized cumulative coverage at bin size $1/2 l_c$ evaluated from the 9x (solid) and
627 from the 0.1x sequencing (dashed) reflects the same amplicon-level variation due to MDA. The
628 agreement between bin-level (dashed and solid lines) and base-level (red dots) depth-of-coverage
629 curves further suggests that the bin-level variation contributes the dominant amplification bias.
630 See **Supplementary Figs. 2,4-8** for more examples of the correlation **(a)** and coverage **(b)**
631 analysis of single-cell sequencing data from different studies. **(c)** Relationship between genome
632 coverage (% covered at 1x mean sequencing depth) and amplification bias (measured by the

633 amplitude of the amplicon-level correlation) of single-cell libraries from different studies.
634 Coverage is evaluated at Chr.1 for both haploid sperms and diploid cells, as well as the SW480
635 tumor cells (disomic in Chr.1), and at Chr.10 (monosomic), Chr.12 (disomic), and Chr.13
636 (disomic) for glioblastoma nuclei. The inverse dependence is fitted with an empirical formula, y
637 $= 0.86/(1.2+\sqrt{x})$. **(d)** Comparison of the cumulative coverage in the most uniform single-cell
638 library from each study. Data were directly evaluated from high-depth sequencing of all samples
639 except the neuron library for which the curve was interpolated from 0.5x sequencing as in **(b)**.

640

641 **Figure 3 | Amplification bias of homologous chromosomes.** **(a)** Schematic illustration of the
642 “mixed template model” and the “segregated template model” reflecting different allele-level
643 contributions to the same locus-level coverage. **(Methods, Supplementary Fig. 10).** **(b)**
644 Comparison of the allele coverage predictions (“Pre.”) from 1x sequencing depth with the
645 observed coverage at heterozygous sites (“Obs.”) at 9x sequencing depth in three single
646 glioblastoma libraries. The combined coverage of reference and alternate bases (red dots) at 9x
647 sequencing validates the prediction from 1x sequencing (dashed curve). The allele coverage
648 (reference or alternate) is then predicted from the combined coverage assuming mixed templates
649 (MTM, blue dotted lines) or segregated templates (STM, green dotted lines) and compared to the
650 coverage of reference (blue triangles) or alternate (green triangles) bases at heterozygous sites.
651 The predictions were made from the sequence coverage in disomic Chr. 12 but the agreement
652 with observations in different disomic chromosomes demonstrate that amplification bias is
653 consistent in all chromosomes.

654

655 **Figure 4 | Variant detection in single-cell genomes.** **(a)** Census-based variant calling requires
656 that acceptable variants be observed in at least two independent single-cell libraries. **(b)**
657 Estimates of the census-based detection sensitivity for a population of independently amplified
658 single-cell libraries all assumed to have similar amplification bias as GBM#4 **(Supplementary**
659 **Fig. 11)**. Optimal detection sensitivity is achieved at roughly 0.5x depth-per-library regardless of
660 the sub-clonal fraction or the total sequencing depth. **(c)** Optimal depth-per-library for census-
661 based variant detection in a population of independently amplified single-cell libraries assumed
662 to have similar coverage bias. The range of the optimal depths is calculated based on the

663 amplification bias observed in single glioblastoma libraries in **Fig. 2b**. For libraries with more
664 bias or for the detection of variants with lower clonal fractions it is optimal to sequence more
665 libraries at modest depths (0.1-0.5x). **(d)** Observed coverage of reference and alternate bases at
666 heterozygous SNP sites in disomic Chr.5 as an estimate of the census-based detection sensitivity
667 for clonal variants. A varying number of single glioblastoma nuclei (59, 22, and 2) were
668 sequenced to the same total depth (20x) and genotyped at germline heterozygous SNP sites.
669 Group (A) included two cells with the best uniformity and group (B) included two cells with
670 average uniformity. For either heterozygous coverage or the detection of alternate bases, the
671 larger pools offer better sensitivity than the two groups of two cells. **(e)** Comparison between
672 somatic non-synonymous variants detected in different sized pools of single cells sequenced to
673 the same total depths (20x). The truth set (48 variants in total) included 43 variants that were
674 detected in both 30x whole-genome and 120x whole-exome sequencing of bulk tumor DNA,
675 plus five additional variants detected in bulk whole-genome and single-cell sequencing. At the
676 same overall sequencing depth, census-based detection from a population of cells (59 and 22)
677 offers higher sensitivity and better specificity over deep sequencing of two libraries. A larger
678 number of private/false positive mutations are observed when individual samples are sequenced
679 to higher depths, and these private calls often arise from sporadic sequencing errors that coincide
680 with amplification errors.

681

682 **Tables:**

683 **Table 1** | Overlap and correlation between allele coverage in independent single-cell libraries by
684 multi-strand displacement amplification. Allele coverage in each library is evaluated by the
685 number of covered HapMap heterozygous SNP sites in disomic chromosome 5 detected in bulk
686 sequencing (combining blood and bulk tumor) by UnifiedGenotyper (Qual. ≥ 500). **(a)** In each
687 single-cell library, coverage of A and B alleles is almost equal and the expected overlap
688 assuming random A or B allele coverage—the estimated coverage of heterozygous sites—is
689 comparable to the observed number of heterozygous sites. **(b)** The overlap between different
690 single-cell libraries' coverage of each allele is also close to the expected overlap based on
691 random allele coverage.

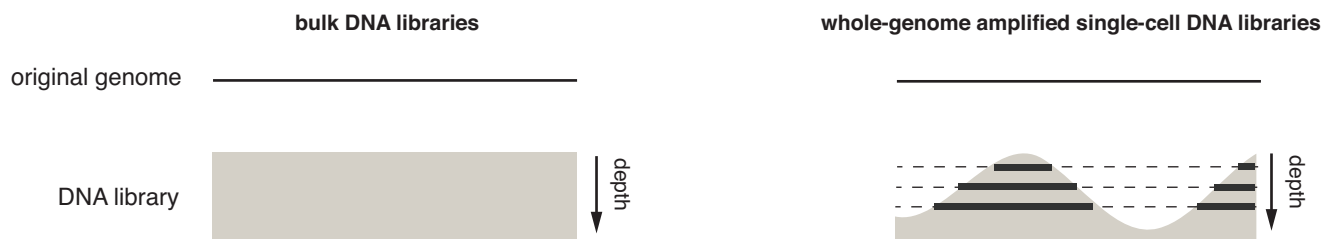
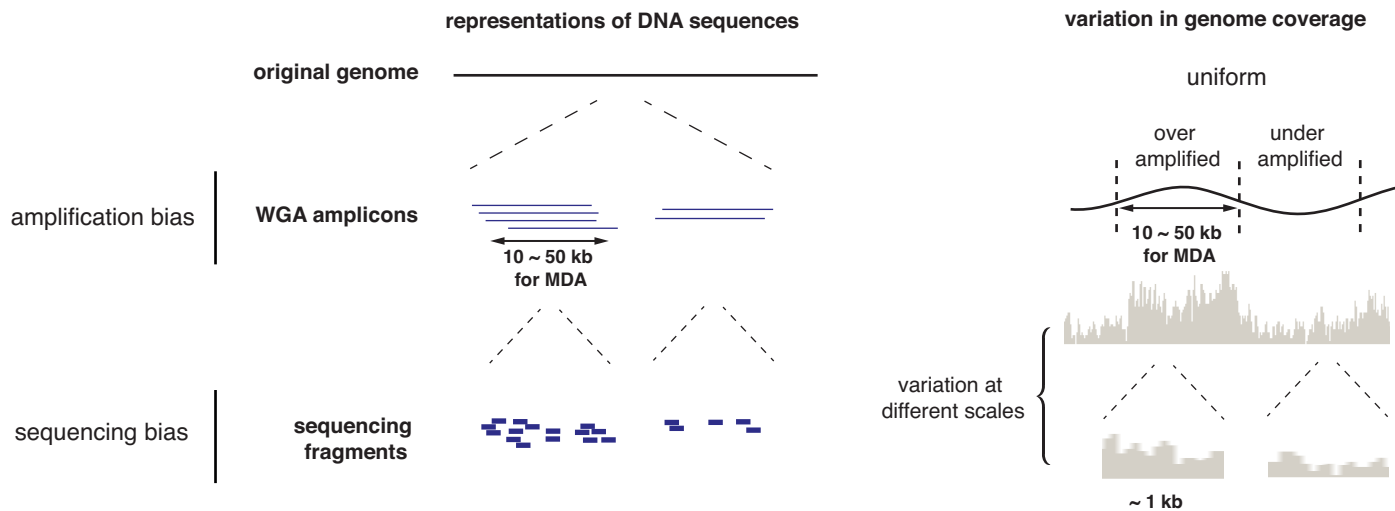
Fig. 1**a Library complexity and sequencing yield****b Coverage bias at different levels****c Recurrent and random amplification bias**

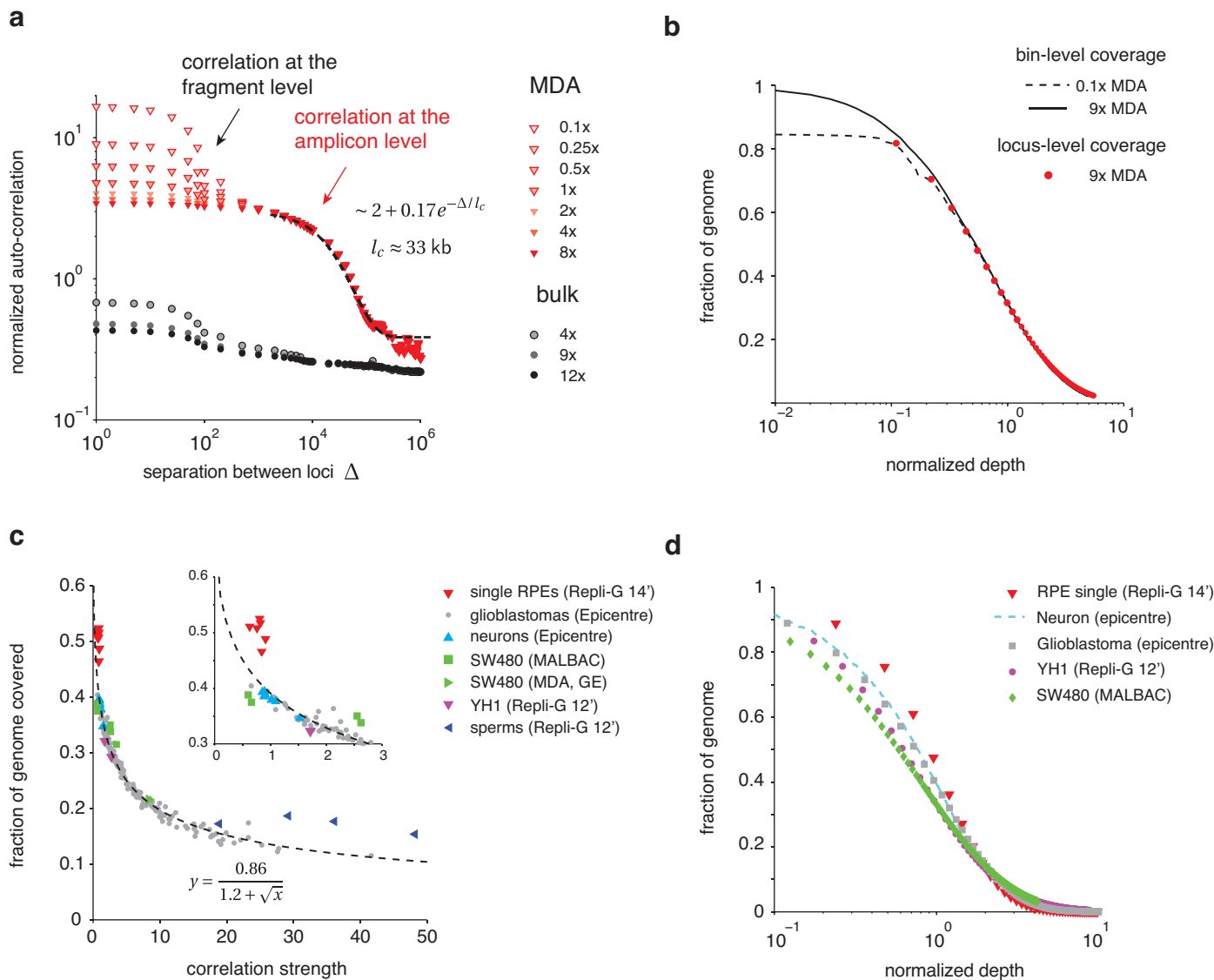
Fig. 2

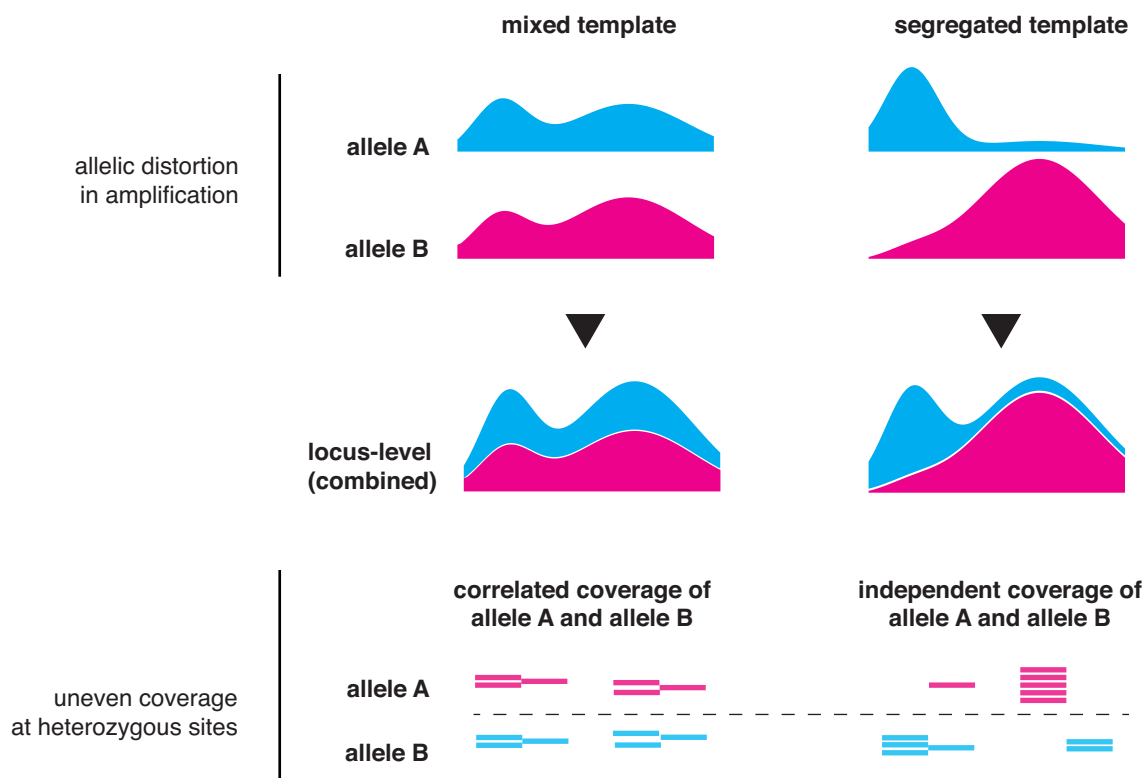
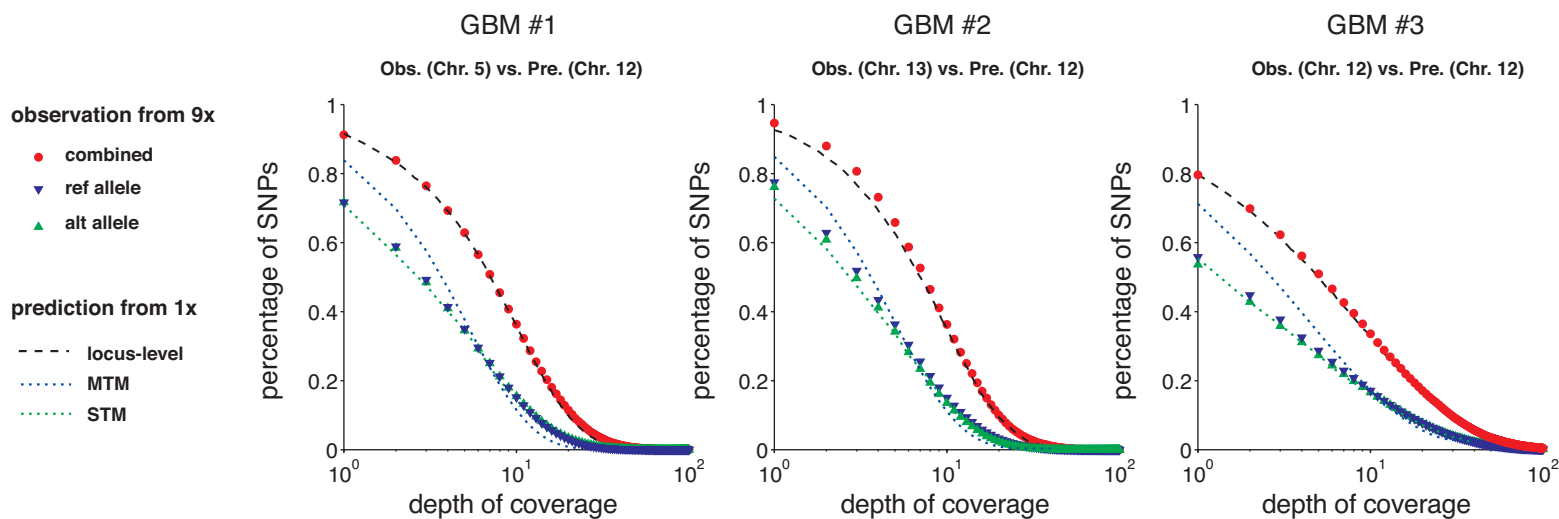
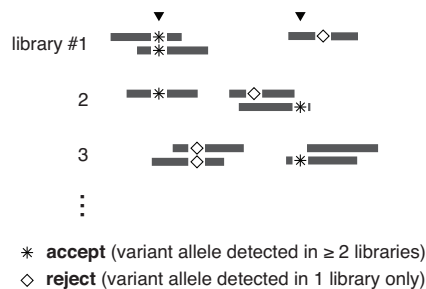
Fig. 3**a Amplification of homologous chromosomes****b Allele coverage predictions for single glioblastoma libraries**

Fig. 4**a census-based variant calling**

census-based sensitivity = % allele covered in ≥ 2 libraries

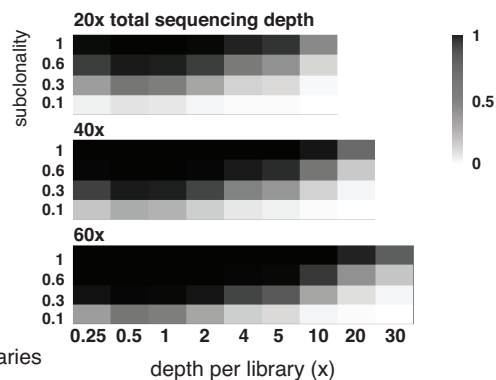
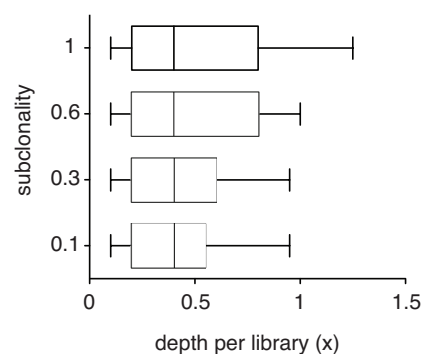
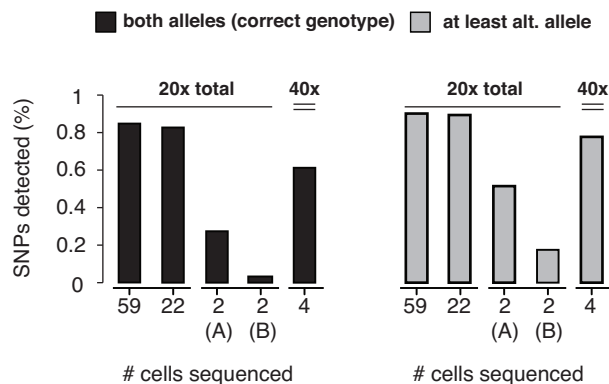
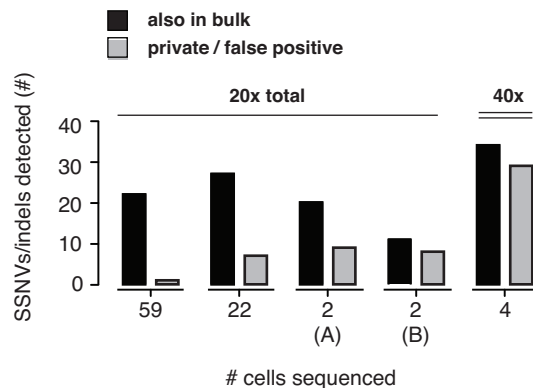
b predicted census-based sensitivity**c predicted optimal depth per library****d observed census-based sensitivity (germline/clonal)****e observed census-based sensitivity (somatic/subclonal)**

Table 1a | Coverage at heterozygous sites in single glioblastoma nuclei libraries

	Depth	Total	Reference	Alternate	Allelic %	Hets (est.)	Hets (obs.)
(i)	9.2x	49,457	40,345	40,356	72%	28,931	29,336
(ii)	8.1x	48,745	39,569	39,521	70%	27,787	28,149
(iii)	6.6x	35,765	22,163	21,549	39%	8,486	7,950
(iv)	9.0x	37,507	23,763	23,883	42%	10,084	10,144

Total germline heterozygous SNPs in Chr. 5: 56,278 (qual. \geq 500, HapMap) \square

Table 1b | Overlap between independent single-nuclei libraries (Covariance = $p_{AB} - p_A \cdot p_B$)

	Allele A	Allele B		Allele A	Allele B		Allele A	Allele B
Cell (i)	40,345	40,356	Cell (i)	39,569	39,521	Cell (i)	40,345	40,356
Cell (ii)	39,569	39,521	Cell (ii)	22,163	21,549	Cell (ii)	23,763	23,883
Overlap	28,912	28,953	Overlap	15,290	15,195	Overlap	17,420	17,521
Covariance	0.010	0.011	Covariance	0.006	0.001	Covariance	0.007	0.007