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A Methodology for Robust Comparative Life Cycle Assessments Incorporating Uncertainty

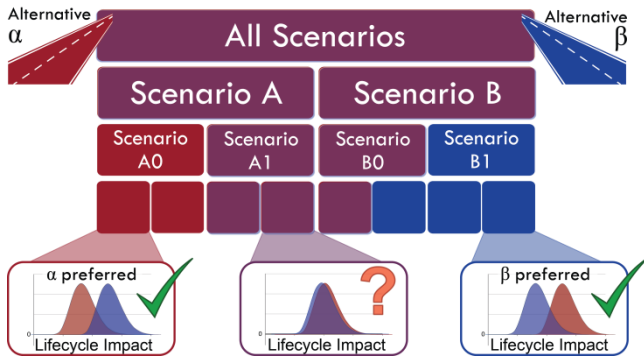
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ABSTRACT.

We propose a methodology for conducting robust comparative life cycle assessments (LCA) by leveraging uncertainty. The method evaluates a broad range of the possible scenario space in a probabilistic fashion while simultaneously considering uncertainty in input data. The method is intended to ascertain which scenarios have a definitive environmentally preferable choice among the alternatives being compared and the significance of the differences given uncertainty in the parameters, which parameters have the most influence on this difference, and how we can identify the resolvable scenarios (where one alternative in the comparison has a clearly lower environmental impact). This is accomplished via an aggregated probabilistic scenario-aware analysis, followed by an assessment of which scenarios have resolvable alternatives. Decision-tree partitioning algorithms are used to isolate meaningful scenario groups. In instances where the alternatives cannot be resolved for scenarios of interest, influential parameters are identified using sensitivity analysis. If those parameters can be refined, the process can be iterated using the refined parameters. We also present definitions of uncertainty quantities that have not been applied in the field of LCA and approaches for characterizing uncertainty in those quantities. We then demonstrate the methodology through a case study of pavements.



23

24 INTRODUCTION

25 As the application of life cycle assessment (LCA) expands, the importance of achieving meaningful and
26 robust comparisons of the environmental performance of alternatives has increased. Indeed, the stakes are
27 high for firms selling products and executing processes under consideration in LCAs. For instance, a
28 European Union biofuels policy requires biofuels producers to demonstrate that the life cycle greenhouse
29 gas emissions of a fuel are 35% below the baseline footprint of a fossil-derived fuel (this will increase to
30 50% in 2017 and starting in 2018 new installations will be subject to a 60% reduction).¹

31 LCAs have often included the comparison of products or processes because relative impacts bring
32 meaning to what is otherwise an abstract concept (e.g., mass of carbon dioxide in the air or disability
33 adjusted life years). Practitioners have long understood the importance of standards to enable meaningful
34 comparison including the broad ISO 14040/14044 standards² and product-focused standards such as the
35 Publicly Available Specification (PAS) 2050 from the British Standards Institute,³ the Product Life Cycle
36 Accounting and Reporting Standard from the Greenhouse Gas (GHG) Protocol,⁴ and the ISO 14067
37 standard.⁵ However, to date, there is limited attention paid in the standards on how to investigate and
38 comment on the significance of the difference between products' environmental impacts.

39 Analyzing uncertainty in LCA calculations is one way to evaluate the significance of calculated
40 differences and this is recognized in the ISO 14044 standard: “An analysis of results for sensitivity and
41 uncertainty shall be conducted for studies intended to be used in comparative assertions intended to be
42 disclosed to the public.”² While this statement is important, there is no guidance in the ISO 14044 standard

43 on how to conduct uncertainty analyses to support assertions of the difference of impact between products.
44 Indeed, there have been calls for such guidance in standards from the literature⁶ and encouragingly the
45 PAS 2050 and the Product Life Cycle Accounting and Reporting Standard from the GHG Protocol each
46 have sections discussing uncertainty. However, the guidance is limited in that the focus is solely on
47 qualitative characterizations of data quality and quantitative calculations of uncertainty in input data (often
48 referred to as *parameter uncertainty*).

49 We note four challenges that are endemic to the assessment of uncertainty in comparative LCA and
50 which deserve further guidance. The first challenge is that LCA uncertainty does *not* solely derive from
51 conventional sources of data variation; instead it derives from the choices available for the framing of an
52 LCA and the unique characteristics of individual decision-makers. Collectively these are often referred to
53 as *scenario uncertainty*. Second, at present, there is little published guidance on how to combine analyses
54 of scenario uncertainty with more conventional parameter uncertainty, particularly within comparative
55 assessments. Third, while parameter and scenario uncertainty are typically analyzed together, their
56 implications must be assessed distinctly. When scenario uncertainty is analyzed in a manner like
57 conventional empirical parameters, information about the decision can be lost and the robustness of a
58 given comparison becomes more ambiguous. Because the scenario/uncertainty space is large, analytical
59 methods are important to efficiently synthesize the implications of scenarios. Finally, we note that life
60 cycle (LC) data, especially data on uncertainty and variation, are costly to collect. Methods to assess
61 comparative performance should accommodate efforts to reduce this cost through informed triage.

62 Given these challenges, we build upon previous work reported in the literature to address aspects of the
63 gap in current LCA literature and practice by describing (and executing) a methodology for conducting
64 comparative LCAs that 1) improves the definition and characterization of uncertain quantities in LCAs
65 analyzed in both parameter and scenario analysis, 2) evaluates a broad range of the possible scenario space
66 while simultaneously considering uncertainty in input data, and 3) efficiently synthesizes the implications
67 of those results across the scenario space through the use of a categorization and regression tree analysis.
68 The objective is to comment on the robustness of an assertion of difference among multiple products or

69 processes. In particular, we ascertain 1) which scenarios have a statistically definitive environmentally
70 preferable choice, 2) which parameters have the most influence on this difference, and 3) how we can
71 identify the resolvable scenarios.

72 Our work represents a methodological contribution for uncertainty analyses in comparative LCAs and
73 highlights the importance of analyzing scenario-related uncertainties in a proper manner. Specifically,
74 we demonstrate that results are obscured when these scenario-related uncertainties are evaluated in a
75 strictly probabilistic fashion. We use a case study of pavements throughout the document to illustrate
76 concepts and demonstrate the methodology. Details on the models and data used in the case study are
77 presented first, followed by definitions of quantities used in LCAs and approaches for characterizing
78 uncertainty in those quantities. The comparative assessment methodology is then described and
79 demonstrated using the pavements case study.

80 PAVEMENT LIFE CYCLE ASSESSMENT MODELS AND DATA

81 We consider two alternative pavements for an urban interstate highway in Missouri in a comparative
82 LCA. The two alternatives are a hot-mix asphalt concrete (AC) pavement, representing a flexible
83 pavement, and a jointed plain portland cement concrete (PCC) pavement, representing a rigid pavement.
84 More technical details about the designs specifications are presented in Section 3 of the supporting
85 information (SI).

86 Pavement LCAs usually comprise five phases: material extraction, construction of the pavement, use
87 phase, maintenance and rehabilitation, and end-of-life.^{7,8} Figure S1 in the SI depicts the five phases and
88 the major subcomponents associated with these phases. A detailed description of the life cycle model is
89 presented in Noshadravan, et al⁹; here we focus on defining the terms and concepts that are of particular
90 importance to the comparative assessment: analysis period, design life, and particularly the elements that
91 contribute to the use phase of the pavement.

92 The first noteworthy elements in pavement LCA are the analysis period and design life of the pavement.
93 The analysis period is the time boundary of the study and the design life is the life time of the pavement.
94 The design life defines how frequently maintenance will be considered within the analysis period for the

95 LCA. Details on the models used in the use phase portion of the LCA are provided in Section S4 of the
96 SI, but key elements are summarized here. The use phase could be significant in a comparative life cycle
97 assessment, especially for high-volume roads, due to the effect of pavement-vehicle interaction (PVI).⁹
98 ¹⁰ Two major sources of PVI include fuel losses due to changes in roughness and fuel losses due to
99 deflection of pavements. The LCA model applied in this study accounts for both roughness and deflection
100 components. The deflection losses are calculated based on the model developed by Akbarian et al.¹⁰
101 Roughness is characterized by the international roughness index (IRI). The prediction of roughness over
102 time is extracted from output of a pavement design software tool (Pavement-ME), which implements the
103 calculations specified by the industry design guide. There is an underlying probabilistic model associated
104 with the prediction of roughness over time using this model. Although the pavement is designed for a
105 prescribed level of reliability, the uncertainty in the roughness evolution over time can be significant. We
106 account for this uncertainty in our LCA and propagate it into the estimation of roughness-induced
107 emissions in pavement LCA.^{11, 12} The progressive change in the roughness over time relative to its value
108 at initial construction is calculated and translated to the excess fuel consumption (i.e., fuel consumption
109 due to pavement roughness beyond the fuel required to move the vehicle) using the empirical model
110 presented by Zaabar and Chatti.¹³

111 Other parameters related to the use phase burden include the fuel economy and traffic growth of both
112 cars and trucks on pavement, the albedo and carbonation resulting from the pavement material, and the
113 lighting used to illuminate the pavement. Further details on the data sources for the remainder of the life
114 cycle inventory are included in the Section S5 of the SI.

115 We use global warming potential (GWP) as the impact assessment metric in this case study and
116 calculate it based on the guidelines put forward by the Intergovernmental Panel on Climate Change.¹⁴ It
117 should be emphasized that GWP is only one of many measures of environmental burden and a complete
118 LCA would calculate multiple measures. Furthermore, our analysis focuses on uncertainty in life cycle
119 inventory parameters and thus, we do not include uncertainty in the GWP factors, as has been done
120 elsewhere.¹⁵

121 DEFINITIONS OF QUANTITIES IN LIFE CYCLE ASSESSMENTS

122 There is an extensive literature characterizing sources and types of uncertainty in life cycle assessment
123 and methods for analyzing the impact of uncertainty on life cycle impact assessment. Huijbregts¹⁶
124 conducted early work on the topic of uncertainty in LCA and since then Lloyd and Ries¹⁷ and Williams
125 et al.¹⁸ have published thorough summaries of previous work in the field and a recent contribution also
126 provides a review of LCA uncertainty methods.¹⁵ (We refer readers to the latter three references for a
127 comprehensive literature review on uncertainty in LCA.) Major life cycle inventories including
128 developers of ecoinvent¹⁹ and the United States Life Cycle Inventory Database²⁰ have built upon and
129 refined the frameworks outlined in the literature.

130 The literature and footprinting standards have coalesced around the terminology for types of uncertainty
131 in LCA proposed by Huijbregts¹⁶ and summarized in Lloyd and Ries¹⁷ for both life cycle inventories (LCI)
132 and life cycle impact assessment (LCIA) methods: parameter, scenario, and model uncertainty (parameter
133 and scenario uncertainty were defined in the introduction; model uncertainty refers to uncertainty in the
134 mathematical relationships used to develop LCIs and LCIA).

135 Although the delineation of the three types of uncertainty appears straightforward, in practice
136 differentiating the three types in an analysis can prove difficult because there is overlap among them. For
137 example, parameters may be used in scenarios or choices may be made in models. de Koning et al.²¹ have
138 noted that these three types of uncertainty manifest themselves by contributing to the uncertainty of the
139 final result of an aggregated cradle-to-gate LCA. They correctly point out that all forms of uncertainty are
140 expressed as uncertainty in a parameter value, even though it is actually an aggregate of parameter, model,
141 and scenario uncertainty. This overlap can make it challenging for practitioners to characterize uncertainty
142 and select appropriate uncertainty analysis methods.

143 We attempt to clarify this matter by describing how literature in the field of risk and policy analysis has
144 defined uncertainty for different types of quantities that are also used in LCAs. Morgan and Henrion²²
145 define eight types of quantities related to uncertainty and we will discuss the five quantities that are of
146 most importance for uncertainty analysis in LCA. These five quantities are summarized in Table S1 of

147 the SI and described here. Each analysis is framed by *decision variables* (subjectively selected by the
148 analyst to frame the decision – a way to answer the question, “what is the best outcome?”, or more
149 specifically, “which product has the lowest environmental impact?”) and *outcome criterion* (the metric
150 from the life cycle impact assessment method used to measure the desirability of possible outcomes).
151 *Empirical parameters* represent properties that are measurable, at least in principle, because they can be
152 said to have a *true* value (such as electricity consumption by a laptop or particulate emissions from a
153 diesel engine). By contrast, *model domain parameters* define the scope of the system being analyzed (e.g.,
154 temporal or geographic boundaries) and there is no true value. Rather, there is an *appropriate* value that
155 is selected by the analyst (the interpretation of appropriateness may vary depending on the analyst).
156 Similarly, *value parameters* represent aspects of the preferences of the analyst or decision-maker and an
157 appropriate value is selected by the analyst. Examples include the discount rate applied in cost analyses
158 (there is no true value), or the allocation method used for the life cycle burden of materials depending on
159 end-of-life assumptions (such as 50/50 or cut-off methods).

160 All of the parameters used in the pavement LCA, their quantity type, and their associated uncertainty
161 are included in Section S6 of the SI; a sampling is included in Table 1 **Error! Reference source not**
162 **found.** It is worth noting that nearly all of the model inputs are empirical quantities, with the exception
163 of five model domain parameters and two value parameters. Uncertainty characterization for the
164 parameters will be discussed in the following section.

165
166
167

Table 1. A sample of the parameters used in pavement LCA model parametric analysis and their associated uncertainty values (see Section S6 of SI for a comprehensive list, including data sources for baseline and standard deviation values). M&R = maintenance and rehabilitation; SD = standard deviation. *Scope* refers to whether or not the phenomenon is included in the analysis.

Model input	Quantity Type	Mean	SD	Distribution
Scope: Albedo	Model domain	-	-	Binary
Scope: Deflection	Model domain	-	-	Binary
Scope: Roughness	Model domain	-	-	Binary
Analysis period	Model domain	-	-	uniform discrete
Design life	Model domain	-	-	uniform discrete
Salvage life allocation	Value	-	-	Binary
M&R strategy	Value	-	-	Binary
Roughness evolution	Empirical	-	-	uniform discrete
Traffic growth factor	Empirical	0.030	0.003	lognormal
Fuel efficiency-cars (mpg)	Empirical	23.70	2.152	lognormal
Fuel efficiency increase (%)	Empirical	0.005	0.0006	lognormal
Fuel loss prediction due to roughness, car (gal/in-mile)	Empirical	0.00017	0.00002	lognormal
Albedo: coefficient-Asphalt	Empirical	0.125	0.011	lognormal
Albedo: coefficient-Concrete	Empirical	0.325	0.030	lognormal
PCC thickness (in)	Empirical	8.000	0.154	lognormal
Cement content (lb/yd ³)	Empirical	564.0	10.830	lognormal
AC thickness, layer 1 (in)	Empirical	2.000	0.038	lognormal
Binder percentage (%)	Empirical	0.087	0.002	lognormal
impact factor: cement impact	Empirical	1.00	0.230	lognormal
impact factor: kg of bitumen	Empirical	0.403	0.075	lognormal

168

169 **UNCERTAINTY CHARACTERIZATION FOR PARAMETERS**

170 Morgan and Henrion²² argue that empirical quantities are the only types of quantities whose uncertainty
 171 may be represented by a weighted probability distribution because they have a true value. Thus, their
 172 implication may be evaluated using probabilistic methodologies, such as a Monte Carlo analysis.
 173 Conversely, Morgan and Henrion contend that model domain and value parameters should not be treated
 174 probabilistically because there are no true values and, hence, the frequency of values cannot be
 175 meaningfully defined within the context of the decision. Consequently, they argue it would be
 176 inappropriate to represent uncertainty for these parameters with a subjective weighting or probability,
 177 although it is technically feasible and certainly has been done.^{21, 23} When the influence of these is
 178 convolved through weighting, important information about their impact is masked and lost.

179 We agree with this philosophy but depart from it in part of our approach simply to avoid unnecessary
180 computation, but adhere to it otherwise. Specifically, we formulate model domain and value parameters
181 probabilistically only to test for the extreme case of a wholly dominating alternative, and in the context
182 of a sensitivity analysis to characterize their overall influence on model results. Furthermore, even in such
183 a context they should be defined as a range of continuous or discrete values with equal likelihood (i.e., an
184 unweighted or uniform distribution). This enables one to analyze a wide range of systematically or
185 randomly-generated combinations of model domain and value parameters (each combination of these
186 framing parameters is a scenario) without specifying that one scenario is more likely than another.

187 Empirical parameters are generally uncertain in nature. For those parameters for which there is no clear
188 representative value and/or distribution, a rough distribution should be defined using any number of
189 methods (e.g., the ecoinvent pedigree matrix¹⁹ or underspecification²⁴). In such cases, the analyst should
190 err toward overestimating uncertainty and if these parameters are identified as influential, using a range
191 of values. Value and model domain parameters should be characterized using a broad range of discrete or
192 continuous values with equal likelihood (i.e., unweighted or uniform distribution). (A “broad” range
193 clearly cannot be defined precisely, but in general one should err on the side of being conservative in this
194 first step.)

195 A final complicating factor in characterizing uncertainty in parameters used in LCA, particularly
196 empirical quantities with probabilistic distributions, is that multiple sources of uncertainty are addressed
197 in different ways. Section S1 of the SI details our framework for types, sources, and methods for
198 characterizing uncertainty in parameters, which builds upon the work of others. Section S2 provides
199 details about how uncertainty characterizations for multiple uncertainty types can be combined into one
200 probability distribution for a parameter, using the ecoinvent pedigree matrix methodology.

201 The uncertainty distributions and values for a selection of the parameters in the pavement LCA are
202 included in Table 1 the complete list is in Section S6 of the SI. All empirical quantities have lognormal
203 distributions, whereas model domain and value parameters have either binary or uniform discrete
204 distributions, depending on the parameter type. Lognormal distributions were selected because a) all of

205 the parameters were exclusively positive, b) it is a commonly used distribution throughout the LCA
206 literature, and c) it is conveniently compatible with pedigree based approaches to estimate uncertainty.
207 To maintain consistency, we use lognormal distributions even for values that are percentages because the
208 mean and standard deviation values are significantly smaller than one, so the likelihood of sampling
209 values close to one is essentially zero.

210 The approach outlined in Sections S1 and S2 of the SI was used to calculate standard deviations for the
211 parameters in Table 1 (and Section S6 of the SI), including using theecoinvent pedigree matrix to estimate
212 quantities due to several types of uncertainty. Furthermore, all parameters are uncorrelated for calculations
213 of one alternative, but common parameters in the comparative assessment of two alternatives are
214 correlated across the two alternatives.

215 METHODOLOGY FOR EVALUATING UNCERTAINTY IN COMPARATIVE LIFE CYCLE 216 ASSESSMENTS

217 Some studies exploring the incorporation of uncertainty in comparative life cycle assessments have
218 focused on evaluating the impact of parameter uncertainty on outcomes.^{25,26} Methods typically involve
219 evaluating the ratios of or differences between the impacts of products being compared. These metrics are
220 usually referred to as comparison indicators and guidance to this effect is given in product carbon footprint
221 standards.⁴ In most LCAs, alternatives should be compared assuming some amount of correlation in input
222 parameters across the alternatives. This means that meaningful tests of significance should accommodate
223 that correlation. When Monte Carlo methods are used, statistical characteristics of a comparison indicator
224 are usually the simplest option which meets this criterion.

225 While comparison indicator approaches and careful treatment of correlation are critical for the accurate
226 evaluation of parameter uncertainty, they are only applicable for a given scenario. Comparative
227 performance of alternatives should be evaluated through a probabilistic analysis which also attempts to
228 explore the scenario space (i.e., all possible combinations of model domain and value parameters)
229 comprehensively.

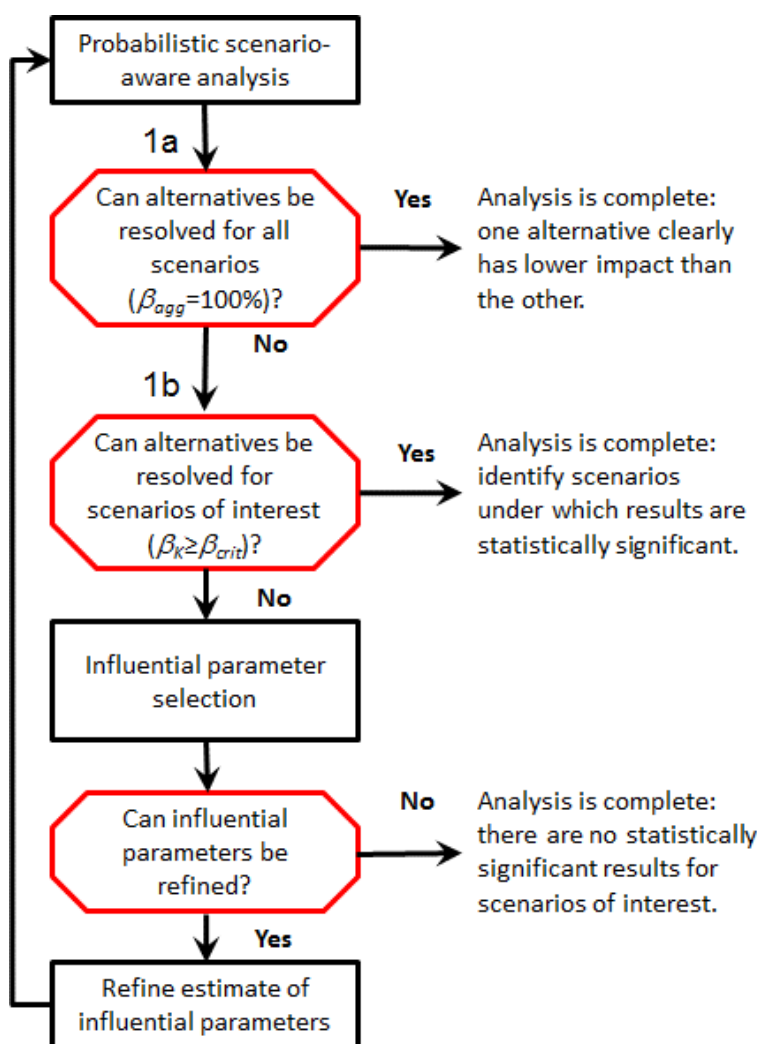
230 More expansive comparative LCAs that include both parameter and scenario uncertainty have been
231 conducted by a few researchers, including Huijbregts et al.,²³ de Koning et al.,²¹ Mattila et al.,²⁷ and
232 Gregory et al.²⁸ Huijbregts et al. combined parameter, scenario, and model uncertainty in a single
233 probabilistic assessment.²³ Notably, in doing so they characterized uncertainty in choices (i.e., model
234 domain and value parameters) using weighted probability functions. Similarly, de Koning et al. explored
235 parameter, scenario, and model uncertainty by using subjective probabilities for scenarios that reflect the
236 preferences of a decision-maker.²¹ Weighting of this form raises some abstract conceptual concerns, but
237 more importantly also a real practical concern – convolving scenario outcomes through weighting
238 potentially masks distinct outcomes among the different scenarios. For example, under scenario one,
239 option A may be preferred; under scenario two, option B may be preferred. A weighted combination of
240 the outcomes of one and two may suggest that either or no alternative is preferred. Whatever the specific
241 outcome, details about the nature of comparison are lost.

242 Before describing our proposed methodology, some contextual comments must be made. As noted in
243 the introduction, our objective is to be able to comment on the robustness of an assertion of difference
244 among multiple products or processes. This objective recognizes that a) for any nominal comparison there
245 are in fact numerous versions of that comparison each situated within distinct scenarios defined by specific
246 combinations of model domain and value parameters; b) the significance of difference between
247 alternatives can be evaluated within a given scenario, but that result may not hold (and may, in fact, be
248 inverted) under other scenarios; and c) the goal of a comparative analysis is to identify the briefest
249 description of the scenario space within which statistically significant results are observed and conversely
250 where they are not. We believe that these points have not been specifically called out in previous work.

251 Although a scenario could technically be defined as a collection of parameters for a single analysis, this
252 would include every simulation conducted in a probabilistic sampling method (such as a Monte Carlo
253 analysis), which is not the way the term is typically used. Instead, we are defining a scenario to be a
254 collection of framing assumptions; that is, the combined set of value and model domain parameters
255 (represented by F). Any analyses which share a common set of F represent the same scenario. Scenario

256 populations are a collection of scenarios with some common framing assumptions, (i.e., for two scenarios
 257 1 and 2 to be in the same population then $F_1 \cap F_2 \neq \emptyset$). This terminology will be demonstrated in the case
 258 study in order to clarify its application.

259 Our proposed methodology for evaluating uncertainty in comparative life cycle assessments of
 260 alternatives (e.g., processes or products) is outlined in Figure 1. The process is for a single set of decision
 261 variables and outcome criteria (e.g., impact assessment methods) and therefore must be repeated for
 262 different sets of decisions or criteria. It may be necessary to iterate the process several times before
 263 drawing final conclusions.



264

265 **Figure 1. Methodology for evaluating uncertainty in comparative life cycle assessments.** β is the frequency that one alternative has
 266 lower impact than the other across a set of simulations (β_{crit} is a minimum threshold for statistical significance, β_{agg} is the frequency
 267 for the aggregated analysis, or the combination of empirical, model domain, and value parameters in an analysis, and β_k is the
 268 frequency for each set of framing assumptions).

269 The methodology begins with an *aggregated probabilistic scenario-aware analysis* as shown at the top
 270 of Figure 1. This is a simultaneous analysis of uncertainty in empirical, model domain, and value
 271 parameters using a probabilistic analysis of the relative performance of the alternatives. (Using the
 272 conventional terminology found in the literature, this could be referred to as combined analysis of
 273 parameter, scenario, and model uncertainty across a wide scenario space.) The probabilistic analysis can
 274 be accomplished using any sampling-based method (such as a Monte Carlo or structured sampling) or in
 275 some cases analytical approaches.²⁵ Care must be taken in the analysis to correlate parameters that are
 276 common between the two alternatives.²¹ (Indeed, one value parameter may involve the use of different
 277 correlation assumptions.) In subsequent mathematical expressions, we will assume that K samples of each
 278 set of value and model domain parameters (F) are generated and the index k represents the k^{th} instance of
 279 those samples. And for each of these K sets of value parameters, M samples of the empirical parameters
 280 are generated (indexed on m). In total, KM samples are generated.

281 The next step (Step 1a in Figure 1) is to calculate the probability that one alternative has a lower impact
 282 than another across all of the simulations. This is accomplished by calculating a comparison indicator for
 283 each simulation (k,m) , $CI_{L,(k,m)}$,²³ which is defined as the ratio between the impacts of two alternatives as
 284 follows:

$$285 \quad CI_{L,(k,m)} = \frac{Z_{L,B,(k,m)}}{Z_{L,A,(k,m)}} \quad \text{Equation 1}$$

286 where $Z_{L,B,(k,m)}$ is the environmental impact for alternative B using the life cycle environmental impact
 287 assessment metric L for the specific realization of parameters k and m , and $Z_{L,A,(k,m)}$ is the environmental
 288 impact for alternative A using the same metric and same sampled sets of parameters. We define β as the
 289 frequency that alternative B has a lower impact than A across some set of scenarios. That is, as:

$$290 \quad \beta = P(CI_L < 1) \quad \text{Equation 2}$$

291 In practice, we estimate β through the use of Monte Carlo simulation trials. More specifically, we initially
 292 evaluate an aggregated measure β_{agg} which is the fraction of all results $\{CI_{L,(1,1)}, CI_{L,(1,2)}, \dots$
 293 $CI_{L,(2,1)}, CI_{L,(2,2)}, \dots CI_{L,(k,m)}\}$ that are less than one. Expressed symbolically, that is:

$$294 \quad \beta_{agg} = \frac{\sum_{k=1}^K \sum_{m=1}^M [CI_{L,(k,m)} < 1]}{KM} \text{ where } [\xi] = \begin{cases} 1 & \text{if } \xi \text{ is true} \\ 0 & \text{otherwise} \end{cases} \quad \text{Equation 3}$$

295 If β_{agg} (or $(1 - \beta_{agg})$) = 100% (outcome 1a-yes in Figure 1), then one alternative clearly has lower impact
 296 than the other and the analysis is complete. However, this would be extremely unlikely for an aggregated
 297 analysis and thus, the next step (1b) would be to evaluate β_k for each scenario, where β_k is defined as:

$$298 \quad \beta_k = \frac{\sum_{m=1}^M [CI_{L,(k,m)} < 1]}{M} \quad \text{Equation 4}$$

299 The difference in impact of the two alternatives in a given scenario is considered to be statistically
 300 significant if β_k or $(1 - \beta_k)$ is greater than a threshold value, β_{crit} . In the interest of brevity, we will refer
 301 to such cases as resolvable (i.e., we can resolve the difference in the impact of A from the impact of B).
 302 This threshold, β_{crit} , is a decision parameter that controls the level of confidence in the decision and
 303 should be set by the analyst for a given context. As noted previously, it is unlikely that the two alternatives
 304 will be resolvable for all scenarios. By contrast, is likely that some scenarios are of more interest to a
 305 particular set of decision makers (e.g., because their convictions are more likely to be aligned to those
 306 scenarios or because they feel that particular set of framing conditions are likely to be considered valid).
 307 If the alternatives can be resolved for the scenarios of interest (outcome 1b-yes), then the analysis is
 308 complete and the scenarios under which one alternative has a lower impact than another can be identified
 309 as statistically significant.

310 In the case presented here, the β_k results were analyzed using a categorization and regression tree
 311 (CART) algorithm implemented in the software JMP. CART identifies a succinct description of the
 312 statistically differentiable subpopulations within the scenario populations by recursively partitioning the
 313 space of input data and fitting a simple regression model within each partition. Comprehensive structured

314 sampling was performed for the value and model domain parameters to assess the combination of
315 scenarios.

316 If the alternatives cannot be resolved for the scenarios of interest, then the *influential parameters* for all
317 scenarios need to be identified in order to determine the parameters that are worthy of further refinement
318 because of their influence on the result. Influence can be assessed using different methods of sensitivity
319 analysis.²⁹ These methods include regression-based methods (such as Spearman rank correlation),
320 variance-based methods (such as Sobol indices), and analytical approaches when uncertainty is
321 propagated thusly.^{30, 31}

322 Once influential parameters are identified, an assessment needs to be made as to whether resources are
323 available to improve the fidelity of the analysis. This would manifest in the *refinement of uncertainty*
324 *characterization* for influential parameters (e.g., more data collection). If the influential parameters cannot
325 be refined then the analysis is complete and the outcome is that there are insufficient statistically
326 significant results for the scenarios of interest. If they can be refined, then the entire process should be
327 repeated using the refined uncertainty characterizations. An analogous, iterative approach to LCA
328 parameter refinement was previously proposed by Huijbregts.²³

329 PAVEMENT LCA RESULTS

330 For the pavement LCA seven value and model domain parameters were identified that define the
331 scenario space and are members of the framing parameters vector (F). Five of these parameters are binary
332 in nature; for the other two, two representative levels were selected to manage the computational expense
333 of the analysis. The full factorial combination of these parameters represents 128 scenarios. For each k^{th}
334 sample of F , 1,000 samples were taken of the empirical parameters comprising E ($M=1,000$). The number
335 of samples has a significant influence on computational intensity because the samples must be run in each
336 of the 128 scenarios. We conducted a convergence analysis and determined that 1,000 samples was
337 sufficient to approximate the statistics of the scenarios. The probabilistic scenario-aware analysis results
338 in an aggregate pool of results that can be disaggregated into 128 probability density functions (PDF)
339 characterizing the comparison indicator for each scenario.

340 1. Probabilistic Scenario-Aware Analysis

341 The first results of this analysis are aggregate measures of the individual designs and their
 342 resolvability. Figure 2a plots the two aggregate probability density functions (PDF) of GWP for the two
 343 designs across the scenario populations. Figure 2b shows the corresponding PDF of CI_{GWP} and a graphical
 344 representation of the fraction of results that fall below one (shaded region). For these results, $\beta_{agg} = 0.75$
 345 well below the 1.0 needed to draw a conclusion (c.f. Figure 1, outcome 1a-no). Based on the β_{agg} it would
 346 be tempting to conclude that this comparison is statistically irresolvable. However, that conclusion is
 347 misleading because the aggregate result does not differentiate the numerous underlying decision scenarios
 348 defined by combinations of model domain and value parameters (F).

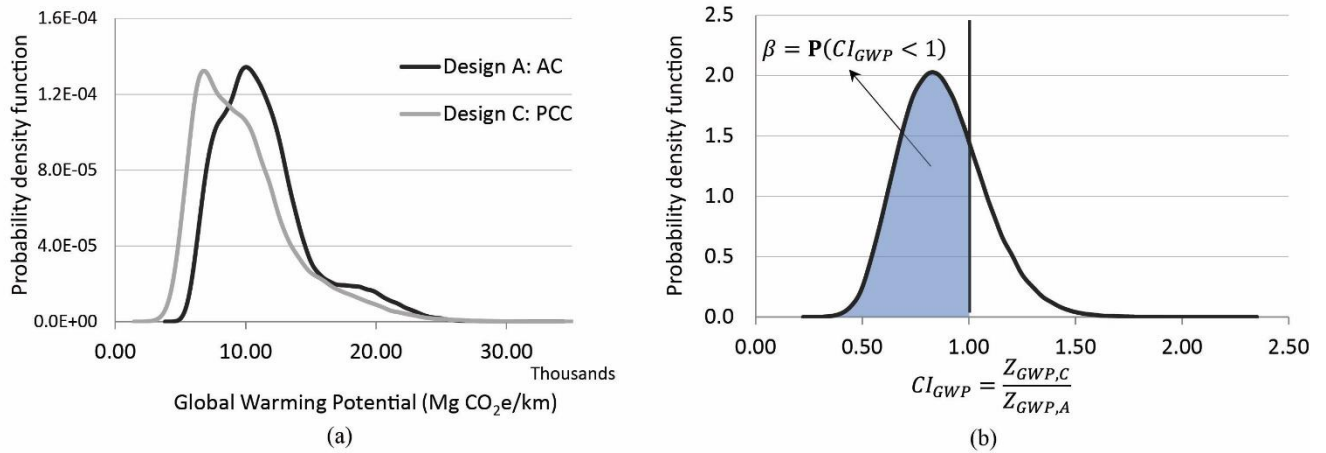


Figure 2. The probabilistic description of aggregated results from combining 128 sets of Monte Carlo realizations. (a) the comparison of PDFs of GWP for design A (asphalt) and C (concrete). (b) the PDF of CI_{GWP} . The shaded region corresponds to the likelihood that the design A has lower impact than design C.

349 We computed β_k (see Equation 4) for each of the underlying 128 scenarios as part of the next step in
 350 the methodology. For this case, 41 scenarios are statistically resolved for $\beta_{crit} = 0.9$ (highlighted in
 351 green in Figure 3). Using a CART algorithm it is possible to create a hierarchical categorization of the
 352 various scenarios in terms of their respective beta values to identify the characteristics of resolvable and
 353 irresolvable subpopulations. As such, we can say not only that scenario k produces a statistically
 354 significant result, but also what characteristics it shares with a larger subpopulation.

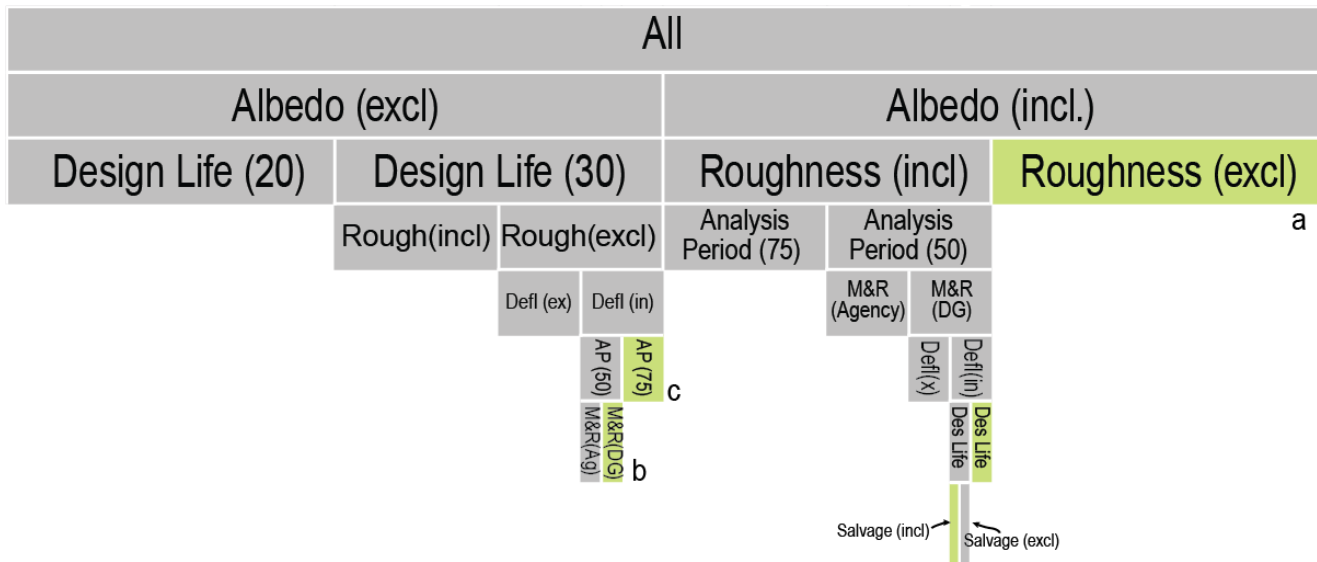


Figure 3. Categorization analysis of resolvable scenarios when all empirical quantities are at full range of values (iteration 1). Green bars differentiate scenarios that are statistically resolved for $\beta_{crit} = 0.9$ (design C has lower impact than design A). For binary model domain parameters (c.f. Figure 2) the scope is either included (incl) or excluded (excl). Parenthetical numbers indicate the value of the parameter. Letters a, b, and c denote scenarios discussed in the text. Rough = roughness; AP = Analysis period; Defl = deflection; M&R = maintenance and rehabilitation; Des Life = design life.

355 This partitioning analysis (shown in Figure 3) reveals that 32 of these resolved scenarios (labelled a in
 356 the figure) share the common features of including the impact of surface albedo (Albedo(incl.)) and
 357 excluding the impact of surface roughness (Rough(excl)). In fact, specifying only these two aspects of a
 358 scenario is sufficient to diagnose that these scenarios can be resolved (irrespective of the state of the other
 359 five scenario variables). The other 10 resolved scenarios are distributed among the states examined, but
 360 all share the common feature of including the impact of pavement deflection (Defl(Incl.)). The
 361 subpopulation of scenarios which exclude albedo effects (Albedo(Excl.) – the left half of tree), serves as
 362 an object lesson on the importance of considering and isolating individual scenarios and scenario
 363 populations. With a β_{agg} of 0.6, this subpopulation seems thoroughly irresolvable. Within this group,
 364 however, one can isolate six specific scenarios (labelled groups b and c in Figure 3) that are, in fact,
 365 resolvable.

366 For the purposes of exercising the method, we will presume that these initial results were deemed too
 367 ambiguous (i.e., there were too many unresolved scenario states which were deemed of interest). As such,
 368 it would be necessary to refine the influential data to improve the fidelity of the result and expand the

369 scenarios under which alternatives are resolvable. To guide that refinement process, we first evaluate the
370 influence of the various parameters.

371 *2. Influential Parameter Selection*

372 As noted earlier, there are several approaches to identify those parameters with the most influence on
373 the results. Here we identify the influential parameters through the use of normalized squared Spearman
374 rank correlation coefficients (SRCC) derived from the simulations run for step 1.³²

375 Figure S3 in the SI shows the results of this global sensitivity analysis. The correlation coefficients are
376 normalized and represented as a percentage characterizing the relative contribution to the variance of
377 GWP for different input parameters. The results show that the model domain decision regarding including
378 or excluding the impact of surface albedo in the scope of analysis has the largest effect (Scope: Albedo)
379 on the result. Other model domain parameters such as the inclusion of roughness-derived impacts (Scope:
380 Roughness), maintenance and rehabilitation schedule (M&R), and design life are also important. Among
381 the empirical quantities, the rate of evolution of roughness (Roughness evolution) and the impact factor
382 of bitumen (IF Bitumen) are among other top influential parameters.

383 *3. Refine estimate of influential parameters*

384 In this particular pavement analysis it was not possible to collect more refined data. In order to
385 demonstrate the full, proposed methodology, we approximate that refinement by arbitrarily bounding the
386 two most influential empirical parameters, the rate of roughness evolution and the impact factor for
387 bitumen, to narrow ranges. Specifically, we will explore a case where the rate of roughness degradation
388 is typical (around the median) and where the production of bitumen has high burden (the mean impact
389 factor for bitumen is around 0.40 kg CO₂-eq/kg). The artificial refinement is useful both to demonstrate
390 the method and to explore the explanatory power of these quantities. If this analysis proves that resolution
391 of these empirical quantities enables sufficient resolution among the alternatives, it should be easier to
392 acquire the resources to collect more data and refine our uncertainty estimates.

393 The same analysis described in step 1 is repeated, but with the newly refined values for the two most
 394 influential empirical quantities. The β_{agg} for this analysis is improved (0.80), but is still far from 1.0
 395 (outcome 1a-no). As such, we proceed to the disaggregated β_k analysis.

396 For this analysis, 83 of the 128 scenarios are significant using the criterion $\beta_{crit} = 0.9$. Figure 4 shows
 397 the CART analysis pruned to descriptions of resolvable or irresolvable subpopulations. For this round of
 398 analysis, all scenarios where the impact of albedo is included are resolvable irrespective of the state of
 399 any of the other model domain or value parameters (labeled a in Figure 4). Similarly, the subpopulation
 400 of scenarios labeled b (i.e. scenarios defined by excluding the impact of albedo, with long design lives
 401 (30) and analysis periods (75), and which exclude the impact of roughness (Roughness (ex)), produce
 402 significant results, irrespective of the state of the three remaining parameters: inclusion of deflection
 403 effect, maintenance strategy, and salvage allocation.

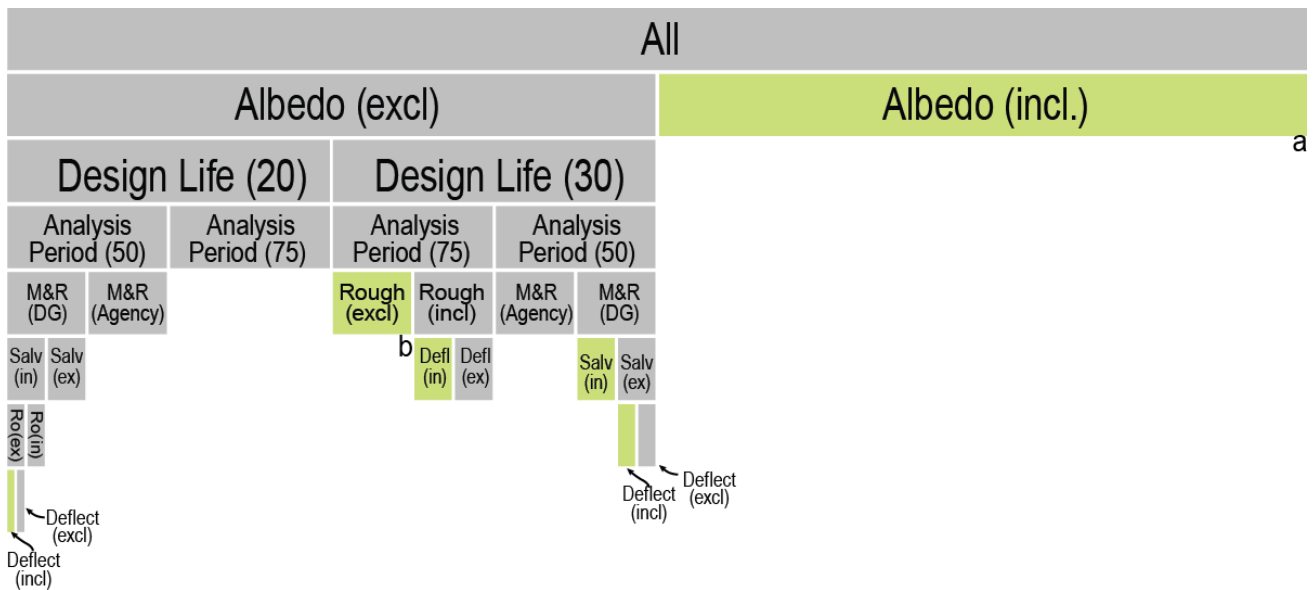


Figure 4. Categorization analysis for refined data analysis (iteration 2). Green bars differentiate scenarios that are statistically resolved for $\beta_{crit} = 0.9$. For binary model domain parameters (c.f. Figure 2) the scope is either included (incl) or excluded (excl). Parenthetical numbers indicate the value of the parameter. Letters a, and b denote scenarios discussed in the text. Salv = salvage allocation; Defl = deflection; M&R = maintenance and rehabilitation; Rough or Ro = roughness.

404 Although the data refinement step successfully produced significant resolution in about 65% (83 of 128)
 405 of scenarios, much of the scenario space remains unresolved. If those scenarios are possibly germane,
 406 then the analyst should iterate through the process again, identifying influential parameters and exploring
 407 whether resources are available to improve the fidelity of parameter estimates. Although an initial

408 sensitivity, as presented in Figure S3, provides useful guidance for those iterations, that analysis should
409 be repeated each time more refined information is introduced.

410 DISCUSSION

411 A promising result of this example is that resolution is most strongly driven by model domain
412 parameters (the inclusion of albedo effects, the manner in which maintenance is modeled, and the design
413 life – which together represent more than 90% of the variance of the β values), rather than value
414 parameters such as the analysis period and allocation. Model domain parameters can be resolved through
415 better information and science about a particular system and through consensus development processes
416 within the decision-making community (e.g., product category rules). Many value parameters are inherent
417 to the preferences of the stakeholder and often represent an irreducible form of uncertainty.

418 Uncertainty is a pervasive challenge in life cycle assessment. Conventional forms of uncertainty in
419 empirical quantities are clearly important drivers of that uncertainty. It is critical to recognize, however,
420 that uncertainty in framing (model domain parameters) and decision maker values (value parameters) can
421 represent even larger sources of uncertainty in LCA results. As a consequence, it is equally critical for
422 LCA studies to explore a broad range of the scenario space.

423 It is also important to recognize that these kinds of scenario parameters define specific decision contexts
424 and as such are not appropriately described by frequency or probability distributions. More pointedly, any
425 given combination of scenario parameters can represent the perspective of a specific decision-maker.
426 Because of this, probabilistic comparative analyses should only be framed within the context of a given
427 scenario.

428 Here we propose that the appropriate analysis around scenario uncertainty is to identify the classes of
429 scenarios where statistically defensible decisions can be made (or cannot). The most effective descriptions
430 are the most terse and, therefore, broad. This final goal has been facilitated through the use of decision-
431 tree partitioning algorithms which appear to offer an efficient means to isolate meaningful scenario
432 groups.

433 Finally, it is important to emphasize that this analysis was done for a single outcome criterion (global
434 warming potential). A more complete LCA would include similar analyses for multiple outcome criteria
435 (other LCIA metrics), which would add a multicriteria component to the decision. Results from all the
436 comparative uncertainty assessments would need to be included in a multicriteria decision analysis, as is
437 the case for deterministic LCAs. The result space in such a situation is even larger than that of a single
438 outcome criterion situation. As such, methods like CART will be even more important to systematically
439 evaluate the space. Future research will explore this topic.

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446 SUPPORTING INFORMATION AVAILABLE

447 Details on uncertainty characterization of parameters, the pavement LCA model and data, and
448 sensitivity analysis results are in the SI. This information is available free of charge via the internet at
449 <http://pubs.acs.org/>.

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