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## Why Does Misallocation Persist?†

By ABHIJIT V. BANERJEE AND BENJAMIN MOLL\*

*Recent papers argue that the misallocation of resources can explain large cross-country TFP differences. This argument is underpinned by empirical evidence documenting substantial dispersion in the marginal products of resources, particularly capital, in developing countries. But why does misallocation persist? That is, why don't distortions disappear on their own? This is particularly true for capital misallocation, a point we illustrate in a simple model of capital accumulation with credit constraints. We distinguish between misallocation on the intensive and the extensive margin, and show that the former should disappear asymptotically under general conditions, while the latter may persist. We conclude by discussing possible theories of persistent misallocation. (JEL D24, E22, G31, G32, L26)*

There is growing interest in the view that underdevelopment may not be just a matter of lack of resources, such as capital, skilled labor, entrepreneurship, or ideas, but also a consequence of the misallocation or misuse of available resources. In particular Banerjee and Esther Duflo (2005); Hyeok Jeong and Robert M. Townsend (2007); Diego Restuccia and Richard Rogerson (2008); Chang-Tai Hsieh and Peter Klenow (2009); Eric Bartelsman, John Haltiwanger, and Stefano Scarpetta (2008); Laura Alfaro, Andrew Charlton, and Fabio Kanczuk (2008); and Francisco J. Buera, Joseph P. Kaboski, and Yongseok Shin (2008) all argue that the extent of misallocation of resources in poor countries is large enough to explain a large part of the total factor productivity (TFP) gap between rich and poor countries.

Evidence on the misallocation of resources takes many forms. There is evidence on interest rates suggesting that many smaller firms in developing countries borrow at interest rates of 50 percent, 80 percent, or even higher.<sup>1</sup> This suggests that these firms must have marginal returns on capital that are even higher. These high estimates of the marginal returns are consistent with the direct evidence on the return on capital in small- to medium-sized firms in developing countries that we get from randomized experiments, natural experiments, and other sources.<sup>2</sup>

\* Banerjee: Massachusetts Institute of Technology, 50 Memorial Drive, Cambridge, MA 02142 (e-mail: banerjee@mit.edu); Moll: University of Chicago, 1126 E. 59th St., Chicago, IL 60637 (e-mail: bmoll@uchicago.edu). We thank Daron Acemoglu, Esther Duflo, Chang-Tai Hsieh, Pete Klenow, and an anonymous referee for helpful comments and encouragement.

† To comment on this article in the online discussion forum, or to view additional materials, visit the articles page at: <http://www.aeaweb.org/articles.php?doi=10.1257/mac.2.1.189>.

<sup>1</sup> Banerjee (2003) describes the evidence on this point and emphasizes that default is rare, so that these interest rates should be thought of as the rates that firms actually pay.

<sup>2</sup> See, for example, Suresh de Mel, David McKenzie, and Christopher Woodruff (2008); Banerjee and Duflo (2008); and Christopher Udry and Santosh Anagol (2006).

We see a very different picture when we look at the evidence on the aggregate marginal product of capital for various developing countries, however. Francesco Caselli and James Feyrer (2007) find that the marginal product of capital is the same in poor and rich countries, and is, in fact, below 10 percent everywhere. Anthony Swan (2008), using a different series for the prices of capital goods, finds substantially higher estimates for developing countries, but even his estimates are much lower than many of the firm level estimates for the marginal product of capital. Chong-En Bai, Hsieh, and Yingyi Qian (2006) come up with 20 percent as the aggregate marginal product of capital in China, down from 25 percent in the earlier period.

The obvious way to reconcile these two sets of facts is to assume that marginal products, contrary to what efficiency would require, are not equalized across firms. Some firms have very high marginal products, but many other firms do not.

A second source of evidence involves fitting a production function to firm level data and directly estimating the distribution of marginal products, or something related, within an industry. Hsieh and Klenow (2009) estimate the distribution of TFPR, which turns out to be a geometric average of the marginal products of capital and labor, and calculate that the ratios of ninetieth to tenth percentiles of TFPR are 5.0 in India, 4.9 in China, and 3.3 in the United States. Moreover, the most productive firms (firms in which the conventional measure of TFP is the highest) tend to be the most distorted in the direction of being too small in both countries, which amplifies the effect of the TFPR not being equalized.

A less structural version of the same exercise involves comparing the distribution of firm sizes across countries to argue that the distribution of firm sizes in most developing countries looks different from the presumed efficient US distribution (Alfaro, Charlton, and Kanczuk 2008). An alternative approach uses the correlation between firm size and the average product of labor as a measure of allocative efficiency, under the theory that the most productive firms should be the biggest (Bartelsman, Haltiwanger, and Scarpetta 2008). Both of these exercises yield some evidence that less developed countries have a joint distribution of firm size and productivity unlike the United States.

Finally, one could do a pure calibration exercise using some plausible parameter values and a model, to put some magnitudes on the potential extent of output loss due to misallocation (as in Jeong and Townsend 2007; Restuccia and Rogerson 2008; Buera, Kaboski, and Shin 2008; and Banerjee and Duflo 2005). All of these papers find that 50 percent or more of the difference between rich and poor countries (or, in the case of Jeong and Townsend (2007), 73 percent of the increase in TFP in Thailand) can be explained by the effects of misallocation under reasonable assumptions about parameter values.

While each of these pieces of evidence has its limitations, taken together, they strongly suggest that misallocation is quantitatively important as an empirical phenomenon.

### I. Theorizing Misallocation

One very natural explanation of why there is so much misallocation, especially given the evidence presented above about the high rates of interest, is to blame asset

markets. The inefficiency in the functioning of asset markets makes it harder for successful firms to acquire the assets they need to expand, and simultaneously allows failed firms to survive (because the alternative of downsizing and putting the rest of the money in asset markets is unattractive). As a result high productivity firms underinvest in what they need—be it management ideas, new technology, marketing advice, reputation building, or new plants or machinery.

Focusing on asset markets would also be consistent with Hsieh and Klenow's (forthcoming) result that most of the gains in India and China would come from reallocating capital across firms. From the point of view of reallocating resources, the key asset markets are the markets for land, financing, and opportunities for risk diversification (which we will call risk capital). Of the primary assets of a firm, land (and what gets built on it) is the one for which the physical adjustment costs are high everywhere in world. However, while the acquisition of land has been a major issue in India and China, this is less of a problem at the firm level (unless it is a very large firm) than it is at the regional level, whereas the reallocation that Hsieh and Klenow (forthcoming) are emphasizing is mostly between firms within the same region. On the other hand, there may be constraints on selling land (though this seems unlikely since India and China had a boom in residential real estate in this period, which made it extremely lucrative to sell existing land holdings that were often in prime locations), and getting building permits and infrastructure connections are quite likely to have been a problem. At this stage, we know too little, descriptively, about the workings of the urban "land" market in developing countries to say anything useful about this.

Finance and risk capital are, of course, the other two key assets that any firm needs (and the availability of which constrains its ability to acquire machines, ideas, consulting, etc.), and, in those areas, we know that the US financial infrastructure is much better. The banking sector in India and China continues to be dominated by slow moving and badly managed public sector banks, and the system as a whole is notoriously ineffective in the enforcement of credit contracts, so that even the private sector is often unwilling to lend. The stock markets in India and China are not known for their effective regulations (in India things are said to have improved, but only after 2000, while the data ends in 1995). And venture capital, as an institutional form, is more or less in its infancy in both countries.

However an alternative to acquiring these assets on the market is to accumulate them. The high rates of return faced by firms that are underinvesting create a strong pressure for accumulation. Similarly, the lack of risk capital generates a precautionary savings motive that may drive firms to accumulate so much capital that they can self-insure. Both of these forces generate forces toward eliminating the distortions across firms.

This does not mean, as we will emphasize later in this paper, that these asset market failures do not have aggregate consequences. But it does pose a challenge for explaining why distortions would not go away on their own. Since underdevelopment is a persistent phenomenon, we need a theory that explains the persistence of misallocation.<sup>3</sup>

<sup>3</sup> There is some evidence on the rate of change in the extent of misallocation. Hsieh and Klenow (2009) report that for China, hypothetically moving to "US efficiency" might have boosted TFP by 50 percent in 1998 and

The next section sets up a simple model that helps us understand this challenge. We focus on the role of credit constraints, for simplicity, suppressing the issue of risk capital by assuming away all risk.

## II. A Simple Model of Capital Accumulation with Credit Constraints

### A. Preferences and Technology

Time is discrete. There is a continuum of households that are indexed by their ability  $z$  and their wealth  $a$ . At each point in time  $t$ , the state of the economy is some joint distribution  $G_t(a, z)$ . The marginal distribution of ability is denoted by  $\mu(z)$ , and it is supported by  $[\underline{z}, \bar{z}]$ .

Agents have preferences

$$(1) \quad \sum_{t=0}^{\infty} \beta^t u(c_t),$$

where  $u$  is strictly increasing, strictly concave, and satisfies standard Inada conditions. Each household owns a private firm that uses  $k_t$  units of capital to produce  $f(k_t, z)$  units of output. We assume that the function  $f$  is strictly increasing, but not necessarily concave. Capital depreciates at the rate  $\delta$ .

### B. Market Structure and Equilibrium

Denote by  $a_t$ , an agent's wealth, and by  $r_t$ , the (endogenous) interest rate. Agents can rent capital  $k_t$  in a rental market at a rental rate  $R_t = r_t + \delta$ .<sup>4</sup> Then an agent's wealth evolves according to

$$(2) \quad a_{t+1} = f(k_t, z) - (r_t + \delta)k_t + (1 + r_t)a_t - c_t.$$

Agents face borrowing constraints

$$(3) \quad k_t \leq \lambda(z, r_t) a_t,$$

where  $\lambda$  is continuous, and nonincreasing in its second argument.<sup>5</sup> A collateral constraint, as in equation (3), is a particularly simple form of credit constraint. As will become clear later, our main result (Proposition 1) does not depend on the particular

30 percent in 2005. But, for India, hypothetically moving to US efficiency might have raised TFP about 40 percent in 1987 or 1991, and 59 percent in 1994, notwithstanding the fact that in this period India liberalized substantially. However there is some danger of overinterpreting this evidence, since taking short-term changes seriously asks a lot of the data.

<sup>4</sup> Here, the capital is accumulated by some intermediary, who then rents it out to entrepreneurs. That the rental rate equals  $r_t + \delta$  can be shown by a standard arbitrage argument. This way of stating the problem avoids carrying  $k_t$  as a state variable in the agent's problem.

<sup>5</sup> For example, suppose that agents can avoid the payment for rented capital  $(r + \delta)k$  by incurring a cost proportional to capital usage,  $\phi k$ , where we assume  $\phi < r + \delta$ . If they default, they also lose their savings  $(1 + r)a$ . The enforcement constraint is  $f(k, z) - (r + \delta)k + (1 + r)a \geq f(k, z) - \phi k$ , so that  $\lambda(z, r) = (1 + r)/(r + \delta - \phi)$ . More generally,  $\lambda$  also depends on ability  $z$ .

form of credit constraints we assume. The underlying logic is very simple and robust, so that the particular form of credit constraint is not likely to matter. Moreover, specification (3) nests the extreme case of no borrowing,  $\lambda(z, r_t) = 1$  for all  $z, r_t$ . This is a useful benchmark delivering an upper bound on the effects of credit constraints. In our model, there are also no intermediation costs so that the borrowing rate equals the deposit rate. We could incorporate a spread between the two rates, as in Andres Erosa (2001), at the expense of some extra notation. All of our results still hold in the presence of intermediation costs.

The production and savings/consumption decisions separate in a convenient way. Define the profit function:

$$(4) \quad \pi_t(a, z) = \max_k \{f(k, z) - (r_t + \delta)k + (1 + r_t)a \quad \text{s.t.} \quad k \leq \lambda(z, r_t)a\}.$$

It is easy to see that this profit function is increasing in both of its arguments. Also, denote the optimal capital choice from this profit maximization problem by

$$k_t(a, z) = \min \{\lambda(z, r_t)a, k^u(z, r_t)\},$$

where

$$(5) \quad k^u(z, r_t) \equiv \arg \max_k \{f(k, z) - (r_t + \delta)k\}$$

is unconstrained capital demand.

Summarizing, at each point in time  $t$ , each household solves

$$(6) \quad v_t(a, z) = \max_{\{c_s, a_s\}_{s=t}^{\infty}} \sum_{s=t}^{\infty} \beta^{s-t} u(c_s) \quad \text{s.t.}$$

$$a_{s+1} = \pi_s(a_s, z) - c_s, \quad \forall s \geq t, \quad a_t = a.$$

The problem for each household can be written in recursive form:

$$(7) \quad v_t(a, z) = \max_{a'} u[\pi_t(a, z) - a'] + \beta v_{t+1}(a', z).$$

Note that the value function is indexed by  $t$ . This is because  $r_t$  varies over time, albeit exogenously from the point of view of the household. Denote the optimal choice of savings  $a'$  by  $s_t(a, z)$ . This is the policy function of a household with assets  $a$  and productivity  $z$ .

This paper studies capital misallocation. We find it useful to distinguish between two forms of misallocation.

#### DEFINITION 1:

- (i) We say there is capital misallocation on the intensive margin at time  $t$  if marginal products of capital  $f_k(k_t(a, z), z)$  are not equalized across all agents who have positive levels of capital usage,  $k_t(a, z) > 0$ .

- (ii) We say there is capital misallocation on the extensive margin if it is possible to redistribute capital from one agent to another individual with either an equal marginal product or zero capital, and raise the sum of their outputs.

Misallocation on the intensive margin is misallocation in the conventional sense, and it is what the empirical evidence has been principally about (Hsieh and Klenow forthcoming; Restuccia and Rogerson 2008). On the other hand, misallocation at the extensive margin exists only if there are nonconvexities in production, or if some individuals have zero capital, and are not being picked up by the current methodologies for measuring misallocation that focus on the equalization of the marginal products. Therefore, there may be much more misallocation than the data on marginal products suggests—in particular, because there are talented people who never have enough money to set up a business—and, therefore, we do not see them in the data. Jeong and Townsend (2007) and Buera, Kaboski, and Shin (2008) attempt to get at this by making assumptions about the underlying distribution of talent.

A *competitive equilibrium* in this economy is defined in the usual way. That is, individuals solve (6), taking, as given, the equilibrium time path for the interest rate  $\{r_t\}_{t=0}^{\infty}$ ; and the capital market (which is the only market in this economy) clears at every point in time:

$$(8) \quad \int k_t(a, z) dG_t(a, z) = \int a dG_t(a, z), \quad \text{all } t \geq 0.$$

The main question we are interested in is whether misallocation disappears over time. The answer turns out to depend on the shape of the production function (in particular, whether it exhibits diminishing returns or not), and on whether we are looking for misallocation at the intensive or the extensive margin. In particular, misallocation at the intensive margin tends to disappear in the long run, even when the misallocation at the extensive margin does not. This is what we now turn to.

### C. Diminishing Returns

Here, we make the following assumption.

**ASSUMPTION 1:** *The function  $f(k, z)$  is concave in  $k$  for any  $z$ , and satisfies standard Inada conditions.*

As already noted, with diminishing returns, there is no role for misallocation on the extensive margin, except in the case where some individuals start out with zero wealth. The Euler equation corresponding to (6) is

$$(9) \quad u'(c_t) = \beta u'(c_{t+1})[1 + r_{t+1} + \lambda(z, r_{t+1})\psi_{t+1}],$$

where

$$\psi_t = \max \{f_k(\lambda(z, r_t)a_t, z) - (r_t + \delta), 0\}$$

is the Lagrange multiplier on the borrowing constraint (2). If there is no misallocation on the intensive margin at time  $t$ , marginal products are equalized across individuals, and all multipliers are zero. In this case, the unconstrained Euler equation

$$(10) \quad u'(c_t) = \beta u'(c_{t+1})(1 + r_{t+1})$$

holds for all agents.

The following Lemma about the optimal savings policy function  $s_t(a, z)$  is an adaptation of a result by W. Davis Dechert and Kazuo Nishimura (1983), and will be useful below. Note that it applies regardless of the assumptions on technologies  $f$ , for instance, and also for the case of (local) increasing returns.

LEMMA 1: *The policy function  $s_t(\cdot, z)$  is strictly increasing for all  $z$ .*

(All proofs appear in the Appendix.) This Lemma implies

COROLLARY 1: *Consider individuals with the same ability  $z$ . Their wealth trajectories never intersect, that is, if  $a_0 > \hat{a}_0$ , then  $a_t > \hat{a}_t$  for all  $t$ .*

We are now in the position to prove our main result about the asymptotic behavior of misallocation with diminishing returns.

PROPOSITION 1: *Under Assumption 1, there is no misallocation on the intensive margin asymptotically. That is, (10) holds for all agents, as  $t \rightarrow \infty$ .*

While there is no misallocation on the intensive margin, there may be misallocation on the extensive margin. If there are some individuals that have zero wealth at  $t = 0$ , they produce zero output, and will never accumulate any wealth which, according to our definition, is extensive margin misallocation. This knife-edge case can be ruled out by

ASSUMPTION 2: *The initial distribution of wealth  $G_0(a, z)$  places no mass at  $a = 0$ .*

Adding this assumption gives the following corollary to Proposition 1.

COROLLARY 2: *Under Assumptions 2 and 6, there is no misallocation (either on the intensive or extensive margins) asymptotically.*

Informal versions of this claim have appeared in the literature in the past (for example, in Banerjee and Duflo 2005), and it is entirely intuitive. Indeed, this result is general in many ways. We allowed for arbitrary correlations between productivity and access to credit. Moreover, while we do not formally deal with that case, the result holds in the presence of intermediation costs. The result does not depend on the particular form of credit constraints in equation (3) either. It would hold in models of credit constraints in which access to credit depends on the present, as



well as the future, profitability of the firm. For example, Moll (2009a) analyzes a similar environment with the main exception that credit constraints take the form of endogenous and forward-looking limited enforcement constraints. Misallocation also disappears with this form of credit constraint. This makes clear that the logic behind the proof of Proposition 5 is general.<sup>6</sup>

The one assumption that is critical for this result is the assumption that all agents are equally patient. If we drop this assumption, and allow for heterogeneity in discount rates, the result does not hold. Below, we demonstrate the existence of a steady state in which there are two types of agents with differing levels of patience, where the less patient agent is permanently credit constrained. This is a counterexample to Proposition 1 because the proposition ought to hold for any initial distribution of wealth and ability.<sup>7</sup>

More can be said about steady states of this economy.

**DEFINITION 2:** *A steady state is a competitive equilibrium with a constant interest rate  $r_t = r^*$ , and a constant aggregate capital stock  $K_t = K^*$  for all  $t$ .<sup>8</sup>*

In line with Proposition 1, we can show that there will be no capital misallocation in steady state. Furthermore, the interest rate equals the rate of time preference,  $r^* = \rho$ , where  $\rho$  is defined by  $\beta \equiv (1 + \rho)^{-1}$ . To see this, first note that an interest rate greater than the rate of time preference,  $r^* > \rho$ , is inconsistent with a steady state. From the Euler equation, this would imply positive consumption growth  $c_{t+1} > c_t$  for all agents, which can only be true if the aggregate capital stock grows. We can also rule out an interest rate  $r^* < \rho$ . In the absence of credit constraints, agents would dissave until they reach zero wealth. With credit constraints, this is not true anymore. Instead, individuals dissave until their wealth reaches a level satisfying

$$(11) \quad \begin{aligned} 1 + \rho &= 1 + r^* + \lambda(z, r^*)\psi^*(a, z) \\ &= 1 + r^* + \lambda(z, r^*)[f_k(\lambda(z, r^*)a, z) - r^* - \delta]. \end{aligned}$$

That is, unconstrained agents only stop dissaving once they become constrained. But there cannot be only constrained agents in equilibrium. There have to be some lenders as well. This tells us that the interest rate must equal the rate of time preference.

Given this, no one is decumulating capital in the steady state. Now, if some individuals were credit constrained in steady state, they would have an incentive to accumulate wealth because the right-hand side of (11) would be greater than the left-hand side. Therefore, the capital stock must be going up, contradicting the definition of a steady state. Summarizing, in any steady state of the economy with diminishing

<sup>6</sup> Note, also, what this proposition does and does not say. It says that misallocation disappears asymptotically as time  $t \rightarrow \infty$ . It does not say that this will happen in finite time. In fact, Moll (2009a) finds that credit constraints always bind in finite time with slightly different modeling of credit constraints.

<sup>7</sup> Moll (2009a) shows that if the discount factor of agents differs, misallocation also persists asymptotically with endogenous and forward-looking limited enforcement constraints.

<sup>8</sup> The definition of the aggregate capital stock is the obvious one,  $K_t \equiv \int adG_t(a, z)$ .

returns, all agents must be unconstrained, and the interest rate equals the rate of time preference.

The allocation of capital is then first-best and can be described by an aggregate production function. Individual capital usage  $k^*(a, z)$  is, therefore, simply the same as in the standard neoclassical growth model:

$$f_k(k^*(a, z), z) = \rho + \delta, \quad \text{all } (a, z).$$

Recalling the definition of unconstrained capital demand  $k^u(z, r)$  in (5), this implies that individual steady state capital stocks  $k^*(a, z)$  are equal to the unconstrained capital demands  $k^u(z, \rho)$ . The unique aggregate steady state capital stock is first-best and equals

$$K^* = \int k^u(z, \rho) \mu(z) dz.$$

Once again, this is something that holds with some generality. The nature of the credit constraint does not matter, nor does the presence of intermediation costs. Since, in steady state, relative prices are constant, the argument that no firm can be credit constrained also immediately extends to the case where there are multiple goods. The one assumption that is essential for the claim that the steady state capital stock is first-best efficient is the assumption of identical discount factors. To see how there can be a steady state where agents are credit constrained and output is less than first-best efficient, suppose that there are two types of agents with the same ability  $z$  (so that we can drop  $z$  from the  $f$  and  $\lambda$  functions), but different discount factors  $\beta_2 < \beta_1$ . We show, now, that it is possible to construct a steady state in which type 2 agents are credit constrained. If type 2 agents are constrained, it must be that type 1 agents are lending, and, therefore, from their Euler equation, the interest rate is given by  $r^* = \rho_1$ . Similarly, from type 2 agents' Euler equation, it must be that

$$1 + \rho_2 = 1 + \rho_1 + \lambda(\rho_1)[f'(\lambda(\rho_1)a_2^*) - \rho_1 - \delta].$$

This determines the steady state wealth of a type 2 agent. Since  $f$  satisfies an Inada condition, this only has a solution if  $a_2^* > 0$ . Therefore, the constrained type must own positive wealth. To complete the construction, note that the steady state wealth of a type 1 agent must be such that he is able and willing to meet the demand for loans from type 1 agents. Assuming that there are equal numbers of type 1 and type 2 agents, this requires that

$$a_1^* - k^u(\rho_1) = (\lambda(\rho_1) - 1)a_2^*.$$

Finally, observe that

$$\lambda(\rho_1)[f'(\lambda(\rho_1)a_2^*) - f'(k^u(\rho_1))] = \rho_2 - \rho_1 > 0.$$

Interestingly, the wedge in the marginal products of capital of the two agents equals the difference in their discount rates.

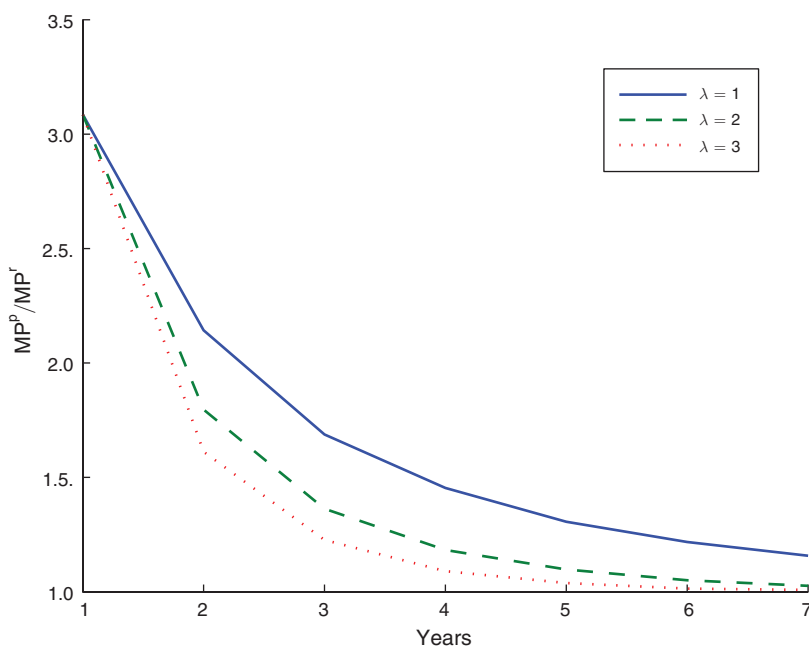


FIGURE 1. CONVERGENCE OF MARGINAL PRODUCTS

Given that misallocation disappears asymptotically as  $t \rightarrow \infty$ , and the steady state is first-best efficient, a natural question is: how long does this convergence of marginal products take? To get a feel for the length of time involved, we have conducted some numerical experiments.<sup>9</sup> We compare two individuals, one rich and one poor, with the same  $z$ . The borrowing constraint of the poor agent binds at time zero, so much so that the poor agent has a three times higher marginal product than the rich agent,  $f_k(k^p, z)/f_k(k^r, z) = 3$ . Figure 1 plots the ratio of the marginal products over time, under the assumption that  $r$  remains fixed over time, for different values of  $\lambda(z, r) = \lambda$ . The speed at which the gap between the two marginal products narrows is quite striking. Even if credit markets are completely shut down,  $\lambda = 1$ , the gap has almost disappeared after seven years. For better functioning credit markets, convergence is even faster. With  $\lambda = 3$ , for example, the gap has essentially disappeared after five years. From a theoretical perspective, the result becomes less surprising if one keeps in mind that the model is a variant of the standard neoclassical growth model. With no credit markets,  $\lambda = 1$ , the models are in fact identical. It is well known that the speed of convergence of the neoclassical growth model is relatively high (Robert G. King and Sergio T. Rebelo 1993). With better working credit markets, this speed is only increased.

<sup>9</sup> Production takes the Cobb-Douglas form  $f(k, z) = k^\alpha$ . Utility is of the constant relative risk aversion (CRRA) form with parameter  $\sigma$ . Borrowing constraints take the simple form  $k_t \leq \lambda a_t$ , where  $\lambda \geq 1$  is a constant. We choose the following very conventional parameter values:  $\alpha = 0.3$ ,  $\delta = 0.05$ ,  $\beta = 0.95$ ,  $\sigma = 2$ .

### D. Local Increasing Returns

The assumption of global diminishing returns is not always a great description of how real firms function. There is often a set-up cost involved in starting a business and, more generally, nonconvexities arise naturally from the fact that machines come in fixed sizes and ideas tend to be indivisible. Following A. K. Skiba (1978) and Dechert and Nishimura (1983), we now allow for increasing returns over some range.

ASSUMPTION 3:  $f(k, z)$  is convex over some range of  $k$ , but there is a  $\hat{k} < \infty$ , such that  $f(k, z)$  is concave for  $k > \hat{k}$ .

An example of this kind of production function is  $f(k, z) = z(k - \underline{k})^\alpha$  for  $k > \underline{k}$ , and zero otherwise.

In this section, we look at steady states (as in Definition 2). We are not able to guarantee that the economy converges to a steady state, though in our simulations it always does. As a result of the steady state assumption, in contrast with the earlier analysis, the problem of an agent is now stationary. Nevertheless, because the production function is nonconvex, so is the agent's maximization problem. The result is that people at different wealth levels may exhibit radically different behaviors. Those who are not too far below a particular nonconvexity will save up and "cross" the nonconvex region to get to the high returns available at high levels of investment, while those with only slightly less assets will prefer to dissave because the climb to get to the high returns is too far for them. Therefore, where you converge to depends on where you started, and there are multiple individual steady state wealth levels with different levels of output associated with them (these results are not formally demonstrated here, but follow directly from the logic of such problems spelled out in Skiba (1978) and Dechert and Nishimura (1983)).

Note, however, that regardless of any nonconvexities, it is still true that credit constrained agents have a higher intertemporal marginal rate of substitution than unconstrained agents. This allows us to prove

PROPOSITION 2: Consider a steady state with constant interest rate  $r$  and constant aggregate capital stock  $K^*$  (definition 2). As  $t \rightarrow \infty$ , each agent converges to his individual steady state, there is no capital misallocation on the intensive margin, and  $r = \rho$ .

This result extends Proposition 1 to the case of local increasing returns. Misallocation on the extensive margin is now a "robust" phenomenon. For instance, suppose the nonconvexity takes the form of a fixed cost. Then individuals starting off below some threshold wealth level will never produce any output because they cannot cover the fixed cost. Extensive margin misallocation is "robust" in the sense that this outcome is not a knife-edge result that depends on the initial distribution of wealth  $G_0(a, z)$ , as in Corollary 2.

While not reported here, we also carried out numerical exercises parallel to the ones previously reported for the diminishing returns case, under the current

assumption about the production function. Once again, except for those who are trying to “cross the nonconvex region,” convergence to an unconstrained state is relatively quick, which should not surprise us since they essentially operate in a diminishing returns environment.<sup>10</sup>

### *E. Implications of These Results*

These results tell us that unless convergence to an aggregate steady state fails (which we have not ruled out for the local returns increasing case), and the interest rate continues to fluctuate substantially even in the long run, we would expect to see misallocation at the intensive margin to disappear relatively quickly in the world of this model. That does not have to mean that there is no misallocation in this economy. Indeed, with local increasing returns, we can construct examples in which the extensive margin misallocation is so large that steady state output as a ratio of first-best steady state output is arbitrarily close to zero.<sup>11</sup> It does raise the question: why do we see so much intensive margin misallocation in the data (remember all the misallocation that Hsieh and Klenow (forthcoming) find is at the intensive margin)?

### **III. Conclusion: Toward an Understanding of Persistent Misallocation**

Persistence of misallocation is easy to explain if we are prepared to assume, as Restuccia and Rogerson (2008) do (for illustrative purposes), that there are “taxes” on the firms that are permanently fixed. However, since Hsieh and Klenow (forthcoming), in particular, only compare firms within an industry (and, indeed, get very similar results from comparing firms within the same industry within the same region), we need to explain why these taxes vary at the firm level. Moreover, as Restuccia and Rogerson (2008) point out, to get large effects, the taxes need to be strongly, positively correlated with firm level TFP.

The problem is explaining why there would be such large firm specific taxes.

In a recent paper, Roger Gordon and Wei Li (2005) suggest an argument for why “taxes” will systematically vary across firms even within the same industry. Their argument is that firms face a choice between joining a formal sector in which they have to pay taxes but can grow to their appropriate size (firms in the formal sector have access to efficient intermediation through the banking system), or operating in the informal sector by staying small enough to avoid detection by the tax system. What does such a choice imply for the correlation between productivity and firm size? We believe that it is likely that *less* productive firms have a bigger incentive to stay small. This will, for example, be the case if joining the formal, intermediated sector requires paying a tax on profits. Since a profit tax works like a “fixed cost,”

<sup>10</sup> Such nonconvex problems are not much harder to solve computationally than their convex counterparts. This is because standard dynamic programming does not require the assumption of a concave period return function. This fact is, for example, used extensively in Dechert and Nishimura (1983).

<sup>11</sup> There is a long tradition of research on the effects of fixed costs combined with credit constraints on the long-run performance of the economy (Oded Galor and Joseph Zeira 1993; Banerjee and Andrew F. Newman 1993; Philippe Aghion and Patrick Bolton 1997; Thomas Piketty 1997). More recently, Buera, Kaboski and Shin (2008) find that introducing fixed costs leads to larger TFP losses.

only the most productive firms will find it worth paying the profit tax, while the least productive firms will stay under the tax net. Note that this says that the factor that distorts firm size (i.e., Restuccia and Rogerson's "taxes") should be negatively correlated with firm level TFP. This is the opposite of what, according to Restuccia and Rogerson (2008), we should be looking for. Moreover as Hsieh and Klenow (forthcoming) point out, the potential productivity gains remain almost unchanged when they only equalize TFPR between firms within the same size quartile. In other words, misallocation within the category of firms that are all large enough to be in the tax net is very sizeable.

One scenario in which high TFP firms may face high "taxes" is when some people set up firms because they have high TFP, while others do so despite having low TFP, because they are politically connected and, therefore, are in less danger of being expropriated. Then, high TFP firms would underinvest because they fear expropriation. However, while expropriation risk in today's India and China is not entirely absent, it is hard to believe that it is a serious issue for the average firm (as against the largest and most visible firms). But, most firms that are in the Hsieh and Klenow (forthcoming) study are neither large enough (the median firm in the top quartile of the distribution has around 200 employees) nor, in another way, so special (there are thousands of such firms) to attract special attention, one way or the other, from the political system in either of the two enormous countries. And, while one could imagine firms getting into an especially friendly or unfriendly relationship with the local political bosses, it is not clear why the firms that are suffering could not move to a different area, or why someone without the political baggage could not buy out the firm.

A third potential source of "taxes" that could be causing misallocation is an explicit policy that discriminates against large firms. It is true that India (but as far as we know, not China) has some policies, labor laws, in particular, that specifically discriminate against larger firms. However Hsieh and Klenow (forthcoming) report that their estimates of the potential productivity gain change very little when they only equalize TFPR between firms within the same size quartile, and, moreover, states in India with better labor laws do not do better in terms of TFPR dispersion.<sup>12</sup>

The alternative approach to persistence relies on shocks. Within our framework, there can be shocks to both assets ( $a$ ) and ability ( $z$ ). It should be clear that any temporary shock to the profitability of the firm that occurs after investment has been chosen is isomorphic to an  $a$  shock, while any shock that affects the marginal product of investment that is yet to be carried out is like a  $z$  shock.

From the point of view of explaining the persistence of misallocation, shocks are important because they move people away from their steady states. Thus, someone who used to have low  $z$ , but now discovers that she has a high  $z$ , will be massively underinvested, and will show a high marginal product. The same will be true if a firm loses a large part of its capital stock.

<sup>12</sup> A comment regarding the discussion of "taxes" in the preceding three paragraphs seems in order. We are not arguing against the importance of "taxes," per se. Instead, we are arguing against "taxes" as an explanation for persistent and large differences in marginal products between firms in both the same size category and the same four-digit industry.

Clearly, the extent to which shocks can explain the persistence of misallocation (in combination with financial constraints) depends on the frequency of the shocks. A low frequency gives firms a long time to adjust to a shock before the next shock hits, and we would not expect to find very much misallocation in the stationary state.

Caselli and Nicola Gennaioli (2005) take a clear a priori position on the frequency of shocks. They look at a model in which there are only  $z$  shocks, and these occur once in every generation, because the current owner of the business dies and is replaced by his child (because capital markets are imperfect, it does not make sense to sell the firm unless the child is especially untalented). With this, they are able to explain a surprisingly large (up to 50 percent) fraction of the TFP gap across countries. However, agents in their model have one period lives and follow a fixed bequest rule, so the possibility of undoing misallocation by accumulating resources does not arise. Buera and Moll (2009) consider a similar environment, but add the possibility for individuals to accumulate wealth during their own lifetime, which implies smaller effects.

On the other hand, there is no reason to take the idea that  $z$  is ability too literally. When a firm loses a contract because its contact in the buying firm has moved on, this is also a  $z$  shock, as is the introduction of a new product into the market. Interpreted in this way, the hypothesis of frequent and large  $z$  shocks does not seem *prima facie* implausible.

Unfortunately, at this point, there is relatively little empirical evidence on this point. Buera and Shin (2008) use US data on the distribution of income and firm sizes, and conclude that an estimate of 0.87 for the autocorrelation of  $z$  fits the data best.<sup>13</sup> Even more recently, Virgiliu Midrigan and Daniel Yi Xu (2009) calibrate a model of firm dynamics with financing frictions to plant-level panel data from Korea with their benchmark calibration implying an autocorrelation of 0.94. Based on this correlation, they conclude that financial constraints cannot explain very much of the misallocation that they observe in the Korean data. However, while 0.87 and 0.94 might seem relatively close, Moll (2009b) provides a closed-form example in which the extent of misallocation is highly sensitive to the autocorrelation of  $z$ , even in this range.<sup>14</sup>

However, as Buera and Shin (2008) point out, we might be missing the most important reason for the observed misallocation by focusing on stationary states. After all, even if it is true that highly autocorrelated  $z$  shocks tend to generate a stationary state with limited misallocation, the transition to the stationary state from a highly distorted initial allocation (think of India or China before liberalization) can be quite slow in the presence of financial constraints, and, therefore, in the short to medium run, we will continue to observe a lot of misallocation.

<sup>13</sup> They set this up using slightly different language, namely that each period, individuals draw a new  $z$  with probability 0.13, implying an autocorrelation of  $1 - 0.13 = 0.87$ .

<sup>14</sup> The extent of misallocation also depends on the concavity of the production function, which determines the speed at which firms adjust their capital to shifts in productivity. The more concave the technology, the higher the payoff from a small adjustment, and the faster this adjustment. Midrigan and Xu (2009) assume strong diminishing returns to scale (an elasticity of output with respect to scale of 0.45), so, within their framework, it is possible that results are less sensitive to variations in the autocorrelation of shocks than it is in Moll's example which assumes constant returns to scale. A proper assessment of firm-level returns to scale also has to be an important part of this research agenda.

Finally, is it possible that the reason why there is persistent misallocation is that there are large differences in the level of patience of different entrepreneurs? Banerjee and Sendhil Mullainathan (2009), for one, argue that discount factors may be endogenous.

It is clear that what is needed at this point is empirical evidence that will help us decide between these alternative views of what lies behind the growing number of observations of large-scale misallocation. Is it financial constraints, some other form of market or government failure, some failure of patience or rationality, or are we simply reading the data wrong and there is less misallocation than we think? Answering these questions will require, in part, more detailed data about firms. What borrowing opportunities do they have available? What are the sources of change in their TFP? What regulations do they face? How much extortion and expropriation do small to medium firms on the ground face, etc.? In part, it would require following firms over time (i.e., panel data) to see how they make adjustments. And, in part, there needs to be a better understanding of how to model firm decision making in imperfect market conditions.

#### APPENDIX

##### PROOF OF LEMMA 1:

The proof follows the same steps as Theorem 1 in Dechert and Nishimura (1983). By way of contradiction, let  $a > \hat{a}$ , but  $s_t(a, z) \leq s_t(\hat{a}, z)$ . By utility maximization,

$$\begin{aligned} v_t(a, z) &= u[\pi_t(a, z) - s_t(a, z)] + \beta v_{t+1}[s_t(a, z), z] \\ &\geq u[\pi_t(a, z) - s_t(\hat{a}, z)] + \beta v_{t+1}[s_t(\hat{a}, z), z]. \end{aligned}$$

Likewise,

$$\begin{aligned} v_t(\hat{a}, z) &= u[\pi_t(\hat{a}, z) - s_t(\hat{a}, z)] + \beta v_{t+1}[s_t(\hat{a}, z), z] \\ &\geq u[\pi_t(\hat{a}, z) - s_t(a, z)] + \beta v_{t+1}[s_t(a, z), z]. \end{aligned}$$

Differencing the above two inequalities, we have

$$\begin{aligned} u[\pi_t(a, z) - s_t(a, z)] - u[\pi_t(\hat{a}, z) - s_t(a, z)] \\ \geq u[\pi_t(a, z) - s_t(\hat{a}, z)] - u[\pi_t(\hat{a}, z) - s_t(\hat{a}, z)]. \end{aligned}$$

Note that

$$\begin{aligned} [\pi_t(a, z) - s_t(a, z)] - [\pi_t(\hat{a}, z) - s_t(a, z)] \\ = [\pi_t(a, z) - s_t(\hat{a}, z)] - [\pi_t(\hat{a}, z) - s_t(\hat{a}, z)]. \end{aligned}$$

But, then the inequality in (12) contradicts the strict concavity of  $u$  (strictly decreasing differences).



PROOF OF PROPOSITION 1:

Fix a  $z$ . Consider an agent with initial wealth  $a_0$ . Denote his wealth and consumption by  $\{a_t\}$  and  $\{c_t\}$ . Consider another agent with the same ability, but initial wealth  $\hat{a}_0 < a_0$ . Denote his wealth and consumption by  $\{\hat{a}_t\}$  and  $\{\hat{c}_t\}$ . Denote the ratio of their marginal utilities by

$$\alpha_t \equiv \frac{u'(c_t)}{u'(\hat{c}_t)}.$$

Combining the Euler equations (9), we have that

$$\alpha_t = \alpha_{t+1} \frac{1 + r_{t+1} + \lambda(z, r_{t+1}) \psi_{t+1}}{1 + r_{t+1} + \lambda(z, r_{t+1}) \hat{\psi}_{t+1}} \leq \alpha_{t+1}.$$

The inequality follows because, by Lemma 4,  $a_t > \hat{a}_t$ , all  $t$  so that either  $\psi_t = \hat{\psi}_t = 0$  or  $\psi_t < \hat{\psi}_t$ . The sequence  $\{\alpha_t\}_{t=0}^{\infty}$  is nondecreasing and, therefore, converges on the extended real line. There are only two possible cases.

CASE 1:  $\{\alpha_t\}_{t=0}^{\infty}$  converges to some  $\alpha^* < \infty$ . This is only possible if the sequence of multipliers  $\{\hat{\psi}_t\}_{t=0}^{\infty}$  converges to zero, implying the desired result.

CASE 2:  $\{\alpha_t\}_{t=0}^{\infty} \rightarrow \infty$ . This is only possible if  $\hat{c}_t \rightarrow \infty$  or  $c_t \rightarrow 0$ . But, this would imply that

$$\lim_{t \rightarrow \infty} v_t(a_t, z) < \lim_{t \rightarrow \infty} v_t(\hat{a}_t, z).$$

Since wealth trajectories do not cross, and the value function  $v_t(\cdot, z)$  is weakly increasing, this is a contradiction.

PROOF OF PROPOSITION 2:

Consider a steady state with some interest rate  $r$  (not necessarily equal to  $\rho$ ). Consider, first, the case where every individual is in steady state. Then, from the Euler equation, a steady state with positive wealth has to satisfy

$$1 + \rho = 1 + r + \lambda(z, r) \psi(a, z).$$

Next, we want to argue that (given that the interest rate is constant) this steady state is stable from the perspective of an individual. This can be done using the apparatus of Skiba (1978), Dechert and Nishimura (1983), and Buera (2008). We do not include the detailed argument due to space restrictions. Suffice it to say that individual wealth sequences are monotonic because policy functions are strictly increasing (Lemma 3), and that individuals either converge to a positive steady state satisfying (13) or decumulate wealth until it reaches zero. By a similar argument,

as in the diminishing returns case, we can rule out the case  $r \neq \rho$ : with  $r > \rho$  the aggregate capital stock would grow; with  $r < \rho$  everyone would be constrained and there would be no lenders. Again, as above, all multipliers  $\psi(a, z)$  must equal zero; otherwise constrained agents would be accumulating wealth. Therefore, there is no misallocation on the intensive margin.

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