Missing transverse energy performance of the CMS detector

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Missing transverse energy performance of the CMS detector

The CMS collaboration

ABSTRACT: During 2010 the LHC delivered pp collisions with a centre-of-mass energy of 7 TeV. In this paper, the results of comprehensive studies of missing transverse energy as measured by the CMS detector are presented. The results cover the measurements of the scale and resolution for missing transverse energy, and the effects of multiple pp interactions within the same bunch crossings on the scale and resolution. Anomalous measurements of missing transverse energy are studied, and algorithms for their identification are described. The performance of several reconstruction algorithms for calculating missing transverse energy are compared. An algorithm, called missing-transverse-energy significance, which estimates the compatibility of the reconstructed missing transverse energy with zero, is described, and its performance is demonstrated.

KEYWORDS: Performance of High Energy Physics detectors; Missing Transverse Energy studies; Calorimeter methods; Detector modelling and simulations (interaction of radiation with matter, interaction of photons with matter, interaction of hadrons with matter, etc)
Contents

1 Introduction 2

2 The CMS detector 2

3 Data sample selection and particle reconstruction 3

4 Reconstruction of $E_T$ 5

5 Large $E_T$ due to misreconstruction 6
  5.1 Contributions to $E_T$ from anomalous signals in the calorimeters 6
  5.2 Removal of beam-induced contributions to $E_T$ 8
  5.3 Contributions of noninstrumented or nonfunctioning detector regions 10

6 Missing transverse energy scale and resolution 12
  6.1 Direct photon sample 13
  6.2 Z samples 14
  6.3 Scale and resolution for events with one primary vertex 15
  6.4 Resolution in multijet events 18
  6.5 Effect of multiple interactions 19
    6.5.1 Studies of pile-up effects using photon and Z events 20
    6.5.2 Studies of pile-up effects in jet data 21

7 Studies of physics processes containing genuine $E_T$ 22
  7.1 W events 23
  7.2 Heavy flavour production and $E_T$ 24

8 $E_T$ significance 25
  8.1 Definition 26
  8.2 Performance of $S_{PF}$ in dijet events 28
  8.3 Application to $W \rightarrow e\nu$ events 29

9 Conclusions 31

A Appendix: optimization of $E_T$ corrections 34

The CMS collaboration 39
1 Introduction

Neutral weakly interacting particles, such as neutrinos, escape from typical collider detectors without producing any direct response in the detector elements. The presence of such particles must be inferred from the imbalance of total momentum. The vector momentum imbalance in the plane perpendicular to the beam direction is particularly useful in pp and p̅p colliders, and is known as missing transverse momentum, here denoted $\vec{E}_T$. Its magnitude is called missing transverse energy, and is denoted $E_T$.

Missing transverse energy is one of the most important observables for discriminating leptonic decays of W bosons and top quarks from background events which do not contain neutrinos, such as multijet and Drell-Yan events. It is also an important variable in searches for new weakly interacting, long-lived particles. Many beyond-the-standard-model scenarios, including supersymmetry, predict events with large $E_T$. The reconstruction of $\vec{E}_T$ is very sensitive to particle momentum mismeasurements, particle misidentification, detector malfunctions, particles impinging on poorly instrumented regions of the detector, cosmic-ray particles, and beam-halo particles, which may result in artificial $E_T$.

In this paper, we present studies of $\vec{E}_T$ as measured using the Compact Muon Solenoid (CMS) detector at the Large Hadron Collider (LHC), based on a data sample corresponding to an integrated luminosity of 36 pb$^{-1}$. In section 2, the CMS detector is briefly described. In section 3, particle reconstruction algorithms and identification requirements, together with the basic sample selection requirements, are given. In section 4, the different algorithms for evaluating $\vec{E}_T$ are presented. In section 5, methods for identifying anomalous $\vec{E}_T$ measurements from known detector artifacts are described. In section 6, the scale and resolution are measured using events containing photons or Z bosons. The degradation of the resolution due to the presence of additional soft pp collisions in the same crossing as the hard scatter (“pile-up”) is presented. In section 7 we present distributions from physics processes containing genuine $E_T$. In section 8, an algorithm, called “$\vec{E}_T$ significance”, which assesses the likelihood that the observed $\vec{E}_T$ is due to resolution effects, is described, its performance in jet events is demonstrated, and its efficacy for separating events containing a W boson decaying to either an electron and a neutrino or a muon and a neutrino from multijet backgrounds is shown. Conclusions are given in section 9. Finally, in the appendix, the optimization of the parameters used in the correction for the detector response is described.

2 The CMS detector

The central feature of the CMS apparatus is a superconducting solenoid, of 6 m internal diameter, providing a field of 3.8 T. Within the field volume are the silicon pixel and strip tracker, the crystal electromagnetic calorimeter (ECAL), and the brass/scintillator hadron calorimeter (HCAL). Muons are measured in gas-ionization detectors embedded in the steel return yoke. In addition to the barrel and endcap detectors, CMS has extensive forward calorimetry.

CMS uses a right-handed coordinate system, with the origin at the nominal interaction point, the x-axis pointing to the centre of the LHC, the y-axis pointing up (perpendicular to the LHC plane), and the z-axis along the anticlockwise-beam direction. The polar angle, $\theta$, is measured from the positive z-axis and the azimuthal angle, $\phi$, is measured in the x-y plane relative to the
Transverse quantities, such as “transverse momentum” ($\vec{p}_T$), refer to the components in the $x$-$y$ plane. The magnitude of $\vec{p}_T$ is $p_T$. Transverse energy, $E_T$, is defined as $E \sin \theta$.

The electromagnetic calorimeter (ECAL) consists of nearly 76,000 lead tungstate crystals, which provide coverage in pseudorapidity $|\eta| < 1.479$ in a barrel region (EB) and $1.479 < |\eta| < 3.0$ in two endcap regions (EE). A preshower detector consisting of two planes of silicon sensors interleaved with a total of $3X_0$ of lead is located in front of the EE. The ECAL has an energy resolution of better than 0.5% for unconverted photons with $E_T > 100\text{GeV}$.

The HCAL is comprised of four subdetectors, a barrel detector (HB) covering $|\eta| < 1.3$, two endcap detectors (HE) covering $1.3 < |\eta| < 3.0$, two forward detectors (HF) covering $2.8 < |\eta| < 5.0$, and a detector outside of the solenoid (HO) covering $|\eta| < 1.3$. The HCAL, when combined with the ECAL, measures hadrons with a resolution $\Delta E/E \approx 100\% \sqrt{E [\text{GeV}]} + 5\%$. In the region $|\eta| < 1.74$, the HCAL cells have widths of 0.087 in pseudorapidity and 0.087 rad in azimuth. In the ($\eta, \phi$) plane, and for $|\eta| < 1.48$, the HCAL cells map onto $5 \times 5$ ECAL crystal arrays to form calorimeter towers projecting radially outwards from close to the nominal interaction point. At larger values of $|\eta|$, the size of the towers increases and the matching ECAL arrays contain fewer crystals.

The muons are measured in the pseudorapidity window $|\eta| < 2.4$, with detection planes made of three technologies: Drift Tubes, Cathode Strip Chambers, and Resistive Plate Chambers. A global fit of the measurements from the muon system and the central tracker results in a $p_T$ resolution between 1 and 5%, for $p_T$ values up to 1 TeV.

The inner tracker measures charged particles within the $|\eta| < 2.5$ pseudorapidity range. It consists of 1440 silicon pixel and 15,148 silicon strip detector modules and is located in the 3.8 T field of the superconducting solenoid. It provides an impact parameter resolution of $\sim 15 \mu m$ and a $p_T$ resolution of about 1.5% for 100 GeV particles.

The first level (L1) of the CMS trigger system, composed of custom hardware processors, uses information from the calorimeters and muon detectors to select, in less than 1 $\mu$s, the most interesting events. The High Level Trigger (HLT) processor farm further decreases the event rate from around 100 kHz to $\sim 300$ Hz, before data storage.

The calibrations used in this analysis were those available at the beginning of the fall of 2010, which are not the final calibrations for this data sample. Improvements and updates to the calibrations can lead to small improvements in resolution.

A much more detailed description of CMS can be found elsewhere [1].

3 Data sample selection and particle reconstruction

The data sets used for the studies presented in this paper were collected from March through November, 2010, and consist of pp collisions at a centre-of-mass energy $\sqrt{s} = 7\text{TeV}$. An integrated luminosity of 36 $\text{pb}^{-1}$ was available with all subdetectors certified as fully functional. The detailed selection criteria for the individual data samples used for each study are given throughout the text. However, all require at least one well-identified primary vertex (PV) whose $z$ position is less than 24 cm away from the nominal centre of the detector and whose transverse distance from the $z$-axis is less than 2 cm, ensuring that particles coming from collisions are well contained in the CMS detector.
The samples used for the studies in this paper are defined through selection requirements on reconstructed jets, electrons, photons, muons, and b jets. We describe the basic identification requirements used for these particles here.

Jet reconstruction and its performance in CMS are discussed in detail elsewhere [2]. For the analyses described in this paper, jets are reconstructed using an anti-$k_T$ algorithm [3] with a jet radius parameter $R$ of 0.5. The energy of a jet is corrected, on average, to that which would have been obtained if all particles inside the jet cone at the vertex were measured perfectly (particle-level). Calorimeter jets (Calo Jets) are clusters of calorimeter tower energies. Jet-plus-track jets (JPT Jets) achieve improved response by supplementing the calorimeter information with tracking information. Tracks are associated with Calo Jets if they are within the jet cone at the PV. The measured momentum of these tracks is added to the jet. To avoid double-counting energies, the expected response in the calorimeter is subtracted from the Calo Jet if the particle is still within the cone when it impacts the calorimeter.

Photon candidates are selected from clusters of energy in the ECAL. They are required to be isolated. The ECAL energy in an annular region in the $\eta$-$\phi$ plane with inner radius 0.06 and outer radius 0.4, excluding a three-crystal-wide strip along $\phi$ from the candidate, is required to be less than $4.2 + 0.006 p_T^2$ GeV, where $p_T^2$ is the transverse momentum in GeV of the photon candidate. The sum of the $p_T$s of the tracks in the same region must be less than $2.2 + 0.0025 p_T^2$ GeV. The ratio of the HCAL energy in an annular region with inner radius 0.15 and outer radius 0.4 to the ECAL cluster energy is required to be less than 0.05. The shape of the cluster of calorimeter energies must be consistent with that of an electromagnetic shower. The agreement is quantified by the variable $\sigma_{\eta\eta}$, which uses the following definitions:

$$\sigma_{\eta\eta}^2 = \frac{\sum (\eta_i - \bar{\eta})^2 w_i}{\sum w_i}, \quad \bar{\eta} = \frac{\sum \eta_i w_i}{\sum w_i}, \quad w_i = \max(0, 4.7 + \log(E_i/E_{5\times5}))$$

and where the sums run over the $5 \times 5$ crystal matrix around the most energetic crystal. $E_i$ and $\eta_i$ are the energy and pseudorapidity of the $i$th crystal within the $5 \times 5$ electromagnetic cluster. $E_{5\times5}$ and $\bar{\eta}$ are the energy and $\eta$ of the entire $5 \times 5$ cluster. Photon candidates with $0.002 < \sigma_{\eta\eta} < 0.013$ are selected. In addition, to provide strong rejection against misidentification of electrons as photons, the cluster must not match any track reconstructed in the pixel detector that is consistent with coming from the primary vertex. Photon reconstruction and identification are described in detail in [4].

Electrons are identified using similar criteria. In addition to similar shower shape and isolation requirements, the candidate must match well in both $\phi$ and $\eta$ to a charged track, but be isolated from additional tracks. Electron candidates are also required to be in the fiducial portion of the calorimeter ($|\eta| < 1.4442$ or $1.5660 < |\eta| < 2.5$). More details are given in [5]. In addition, photon-conversion rejection is used in some of the analyses presented in this paper.

Muon candidates consist of a track in the tracker which can be linked to one reconstructed in the muon system. The candidate must be isolated from deposits of energy in the ECAL and HCAL that are not consistent with having been deposited by the muon. The sum of the $p_T$s of other tracks within an isolation cone centred on the candidate must also be small.

Several algorithms for the identification of b jets have been developed [6, 7]. Two of them are used in an analysis described in this paper. The SimpleSecondaryVertex (SSV) tagging
algorithm exploits the significance of the three-dimensional flight distance between the PV and a reconstructed secondary vertex. The SoftMuonByPt (SMbyPt) tagger uses the transverse momentum of the muon with respect to the jet axis to construct a discriminant.

CMS also has a global particle-flow reconstruction. Details on the CMS particle-flow algorithm and performance can be found in [8]. The particle-flow technique reconstructs a complete, unique list of particles (PF particles) in each event using an optimized combination of information from all CMS subdetector systems. Reconstructed and identified particles include muons, electrons (with associated bremsstrahlung photons), photons (including conversions in the tracker volume), and charged and neutral hadrons. These particles are not necessarily the same as those found in the other reconstruction, and all detector information is used in the construction of the PF particles. For the analyses described in this paper, PF particles are used to construct a third type of jets (PF Jets). They are also used in one type of $\sum E_T$ reconstruction, as discussed in section 4.

The collision data are compared to samples of simulated events that were generated either using PYTHIA 6 [9], with a parameter setting referred to as tune Z2, or with MADGRAPH interfaced with PYTHIA [10]. The generated events are passed through the CMS detector simulation based on GEANT4 [11]. The detector geometry description includes realistic subsystem conditions such as simulation of nonfunctioning channels. The samples used in section 6.5 include pile-up. The offline event selection for collision data is also applied to simulated events.

4 Reconstruction of $\sum E_T$

In general, $\sum E_T$ is the negative of the vector sum of the transverse momenta of all final-state particles reconstructed in the detector. CMS has developed three distinct algorithms to reconstruct $\sum E_T$: (a) PF $\sum E_T$, which is calculated using a complete particle-flow technique [8]; (b) Calo $\sum E_T$, which is based on calorimeter energies and the calorimeter tower geometry [12]; and (c) TC $\sum E_T$, which corrects Calo $\sum E_T$ by including tracks reconstructed in the inner tracker after correcting for the tracks’ expected energy depositions in the calorimeter [13].

As discussed in section 3, the CMS particle flow reconstruction uses all detector information to create a complete list of identified and reconstructed PF particles. Since all detector information is included, it is simple to use the PF particles to calculate a $\sum E_T$: $\sum E_T$ is the negative of the vector sum over all PF particles of their transverse momentum. $\sum E_T$ is the associated scalar sum of the transverse energies of the PF particles.

Calo $\sum E_T$ is calculated using the energies contained in calorimeter towers and their directions, relative to the centre of the detector, to define pseudo-particles. The sum excludes energy deposits below noise thresholds. Since a muon deposits only a few GeV on average in the calorimeter, independent of its momentum, the muon $p_T$ is included in the Calo $\sum E_T$ calculation while the small calorimetric energy deposit associated with the muon track is excluded. Calo $\sum E_T$ is the associated scalar sum of the transverse energies of the calorimeter towers and muons.

TC $\sum E_T$ is based on Calo $\sum E_T$, but also includes the $p_T$S of tracks that have been reconstructed in the inner tracker, while removing the expected calorimetric energy deposit of each track. The predicted energy deposition for charged pions is used for all tracks not identified as electrons or muons. The calorimetric energy deposit is estimated from simulations of single pions, in intervals of $p_T$ and $\eta$, and an extrapolation of the track in the CMS magnetic field is used to determine
its expected position. No correction is applied for very high $p_T$ tracks ($p_T > 100\text{GeV}$), whose energy is already well measured by the calorimeters. For low-$p_T$ tracks ($p_T < 2\text{GeV}$), the measured momentum is taken into account assuming no response from the calorimeter.

The magnitude of the $\not E_T$ can be underestimated for a variety of reasons, including the non-linearity of the response of the calorimeter for neutral and charged hadrons due to its noncompensating nature, neutrinos from semileptonic decays of particles, minimum energy thresholds in the calorimeters, $p_T$ thresholds and inefficiencies in the tracker, and, for Calo $\not E_T$, charged particles that are bent by the strong magnetic field of the CMS solenoid and whose calorimetric energies are therefore in a calorimeter cell whose associated angle is very different from the angle of the track at the vertex. The displacement of charged particles with small $p_T$ due to the magnetic field and the calorimeter nonlinearity are the largest of these biases, and thus Calo $\not E_T$ is affected most. A two-step correction has been devised in order to remove the bias in the $\not E_T$ scale. The correction procedure relies on the fact that $\not E_T$ can be factorized into contributions from jets, isolated high $p_T$ photons, isolated high $p_T$ electrons, muons, and unclustered energies. The contribution due to unclustered energies is the difference between the $\not E_T$ and the negative of the vector sum of the $p_T$s of the other objects. Isolated photons, electrons, and muons are assumed to require no scale corrections.

Jets can be corrected to the particle level using the jet energy correction [2]. The “type-I corrections” for $\not E_T$ use these jet energy scale corrections for all jets that have less than 90% of their energy in the ECAL and corrected $p_T > 20\text{GeV}$ for Calo $\not E_T$, and for a user-defined selection of jets with $p_T > 10\text{GeV}$ for PF $\not E_T$. These corrections can be up to a factor of two for Calo $\not E_T$ but are less than 1.4 for PF $\not E_T$ [14]. In order to correct the remaining soft jets below this threshold, and energy deposits not clustered in any jet, a second correction can be applied to the unclustered energy, which is referred to as the “type-II correction”. This correction is obtained from $Z \rightarrow ee$ events, as discussed in the appendix.

In this paper, distributions involving Calo $\not E_T$ include both type-I and type-II corrections, those involving PF $\not E_T$ include type-I corrections, and those involving TC $\not E_T$ are uncorrected, as these were the corrections that were available at the time the analyses presented in this paper were performed and are the versions used most typically in 2010 physics analyses. As discussed in the appendix, type-II corrections have been developed for PF $\not E_T$ and can be used in future analyses. The optimization of both corrections is also discussed in the appendix.

5 Large $\not E_T$ due to misreconstruction

This section describes various instrumental causes of anomalous $\not E_T$ measurements, and the methods used to identify, and sometimes to correct, $\not E_T$ for these effects. We also examine the contributions to the tails of the $\not E_T$ distribution from nonfunctioning channels, uninstrumented regions of the detector, and particles from sources other than pp interactions.

5.1 Contributions to $\not E_T$ from anomalous signals in the calorimeters

The CMS ECAL and HCAL occasionally record anomalous signals that correspond to particles hitting the transducers. Anomalous signals in HCAL can also be produced by rare random discharges of the readout detectors. Some of these effects had already been observed during past test
beam and cosmic data taking [15]. Detailed studies of these effects have continued with the 7 TeV data taking, and are documented in detail in [16] for the HCAL and in [17] for the ECAL. For some types of anomalous energies, the number of affected channels is small and the event can still be used in physics analysis after the removal of the anomaly. We refer to the removal process as “cleaning” the event. If a large number of channels are affected, “filters” instead tag the event as not suitable for use in physics analysis.

Anomalous energy deposits in EB are associated with particles striking the sensors and very occasionally interacting to produce secondaries that cause large anomalous signals through direct ionization of the silicon. Three main types of noise have been identified in HF: scintillation light produced in the light guides that carry the light from the quartz fibres to the photomultipliers, Cherenkov light in the photomultiplier tube (PMT) windows, and punch-through particles hitting the PMTs. While the EB, HF scintillation, and HF Cherenkov sources typically affect only a single channel, signals generated in the HF by particles that exit the back of the calorimeter can affect clusters of channels per event. In the HB and HE, electronics noise from the Hybrid Photo Diode (HPD) and Readout BoX (RBX) occurs, and can affect from one up to all 72 channels in an RBX. This noise is not related to interactions with particles from pp interactions but instead occurs at a low rate and at random times, so the overlap with pp interactions is very low at the bunch spacings of the 2010 run.

The basic strategy for the identification and removal of anomalous signals (cleaning) is based on information such as unphysical charge sharing between neighbouring channels in $\eta$-$\phi$ and/or depth, and timing and pulse shape information. Each of the calorimeters in CMS measures and samples signals every 25 ns and several samples are saved with the event record. The shapes of the pulses for signals that develop from energy deposits in the calorimeters are different than those from anomalous noise signals.

Once a “hit” in an HCAL tower or ECAL crystal is determined to be unphysical, we exclude it from the reconstruction of higher-level objects such as jets or $E_T$. We thus arrive at a reconstruction of jets and $E_T$ that is consistently “cleaned” of anomalous detector effects. Studies using simulations of a variety of different physics processes indicate that the amount of energy that is removed that comes from particles produced in a pp scattering is negligible.

Some features of anomalous signals can be used most effectively to identify events contaminated by them after higher level objects such as jets have been reconstructed. Usually we reject events containing these types of anomalies using filters instead of trying to clean them, although some cleaning is available for PF $E_T$. For example, we usually exclude events with HPD or RBX noise affecting many channels by imposing the requirements described in [15]. We find that these requirements exclude 0.003% of an otherwise good inclusive sample of pp interactions (minimum-bias events).

The Calo $E_T$ distribution from a data sample that was collected with a trigger that requires a coincidence in the beam pickup monitors and scintillators in front of the HF calorimeter (minimum-bias data) are shown before and after removal of the anomalous signals in figure 1, demonstrating the effect of the cleaning and filters. The fraction of events in this sample that had energies recorded in the HF cleaned was $1 \times 10^{-2}$. The fraction for the EB was $3 \times 10^{-3}$. These are the dominant sources of anomalous signals for the bunch spacings of the 2010 run. A comparison with simulation, which does not include anomalous energies, shows good agreement. The effect of the cleaning on the other $E_T$ algorithms is similar.
The minimum-bias triggers used to collect the data shown in figure 1 were prescaled for most of the data-taking period. Triggers that require large amounts of energy in the detector, such as $E_T$ triggers and single-jet triggers, are enriched in events with anomalous energies. Filters to remove cosmic rays, other non-collision-related sources of high $E_T$, and other types of anomalies have been developed in the context of specific searches for new particle production [18]. An example of a filter for beam-halo muons, which can produce high energy bremsstrahlung photons in the detector, is given in the next section.

Hardware modifications to mitigate one of the largest sources of anomalous energies during the 2010 run, scintillation light produced in part of the light guide reflective sleeves in the HF, were implemented during the winter 2010–2011 shutdown period. During this period, the material that was producing the scintillation light was replaced with Tyvek. These modifications reduce the rate of noise events in HF by an order of magnitude. The HF PMTs will be replaced with multi-anode PMTs with flat, thinner front glass during the winter 2013–2014 shutdown, reducing the noise from Cherenkov light and punch-through particles. To reduce the noise observed in HB and HE, the HPDs will be replaced by silicon photomultipliers that do not produce this type of noise.

5.2 Removal of beam-induced contributions to $E_T$

Machine-induced backgrounds, especially the production of muons when beam protons suffer collisions upstream of the detector (“beam halo”), can cause anomalous, large $E_T$. The CMS beam-halo event filter uses trigger and reconstruction-level information obtained from the Cathode Strip Chambers (CSCs), a subdetector with good reconstruction performance for both collision and non-collision muons [19], and can be used to tag events for removal. The geometry of the CSCs makes
it difficult for beam-halo particles, with mostly parallel-to-beam trajectories, to traverse the barrel calorimetry without traversing one or both CSC endcaps.

The filter can operate in either a “loose” or “tight” mode. The former is designed for high tagging efficiency at the cost of a modest misidentification probability, while the latter tags only well-identified halo candidates and has a smaller misidentification probability. The tagging efficiencies and misidentification probabilities have been assessed using simulation. For simulated beam-halo particles which impact the calorimeters and produce Calo $E_T > 15\text{GeV}$, the loose (tight) filter is roughly 92% (65%) efficient. The per-event mistag probability determined from a simulation of inclusive pp interactions (minimum-bias events) for the loose (tight) filter is $\sim 10^{-5}$ ($10^{-7}$).

The tagging inefficiency is due in part to halo muons that do not traverse enough active layers of the CSCs for a well-measured track to be reconstructed and in part to muons that do not meet the coincidence requirements of the L1 beam-halo trigger. Many of the mistagged events are from extremely soft and forward muons (i.e. $p_T < 2\text{GeV}$ and $|\eta| > 1.7$), from pion decay or from hadron punch-through.

The CSC-based beam-halo filter was applied to events passing muon triggers which had $p_T$ thresholds of 9, 11, or $15\text{GeV}$, depending on the running period. Beam-halo muons, because their tracks do not point towards the nominal interaction point in the centre of the detector, in general do not fire the triggers for muons from pp interactions. The beam halo muons in this sample are therefore overlaid on events triggered otherwise, providing an unbiased comparison of $E_T$ in events with and without a beam-halo muon in coincidence. Minimum-bias events could have been used as well, but, because the minimum-bias trigger was prescaled, the number of available events was small. The fraction of halo-tagged events for each running period is shown versus the average beam intensity, with an uncertainty of approximately 10%, in figure 2 (left). The fraction of tagged events increases with the beam intensity, as might be expected.

Figure 2 (right) shows the PF $E_T$ distribution for two trigger streams. The distribution from events recorded by collision muon triggers is shown by the dashed curve while that from the sub-

Figure 2. (left) Probability of finding a beam-halo tagged event in muon-triggered events. Results are shown as a function of the beam intensity. (right) PF $E_T$ distribution for all the events from muon and Calo $E_T$ triggers that were analyzed, and for the subset of these events that were identified as beam halo.
set of these events satisfying the requirements of the tight halo filter is shown by the red inverted triangles. As can be seen, the halo muons that overlapped with these events did not disproportionate produce events with large PF $E_T$, indicating that the probability of a halo muon producing large $E_T$ in events taken from triggers that are uncorrelated with $E_T$ is small. Also shown are the PF $E_T$ distributions for events taken on a trigger with a minimum trigger threshold of 100 GeV (solid curve). The structure seen in this plot at 100 GeV is due to the trigger threshold. No cleaning of anomalous energies is done for the $E_T$ used in the trigger decision. The peak at low values of the $E_T$ is due to events that had large trigger $E_T$ but were cleaned during the reconstruction used for physics analysis. A substantial fraction of events collected on this trigger are identified as halo (blue triangles), since the trigger preferentially selects events in which the beam-halo muon has deposited large amounts of energy in the calorimeter. A beam-halo filter is therefore necessary for analyses that make use of samples based on this trigger.

5.3 Contributions of noninstrumented or nonfunctioning detector regions

Particles traversing poorly instrumented regions of the detector can be a cause of apparent $\vec{E}_T$. While generally hermetic, the CMS calorimeter does have uninstrumented areas (cracks) at the boundary between the barrel and endcap sections, and between the endcap and the forward calorimeters. The gap between the barrel and endcap sections is about 5 cm and contains various services, including cooling, power cables, and silicon detector readout. The crack is not projective to the interaction point. In addition, about 1% of the ECAL crystals are either not operational or have a high level of electronic noise [17], and they are “masked” (ignored) during reconstruction. The $\eta$-$\phi$ distribution of these crystals for the barrel and $x$-$y$ distribution for the endcaps are shown in figure 3.

In this section, we illustrate the effect of these features on the $E_T$ distribution and test the reliability of the simulation for events with jets pointing towards masked ECAL channels or cracks.

Figure 4 shows the $E_T$ distributions from simulated samples of events containing at least 2 jets, with the leading jet satisfying $p_T > 50$ GeV and the second jet satisfying $p_T > 25$ GeV, for Calo $E_T$, TC $E_T$, and PF $E_T$. For events with $100 < E_T < 200$ GeV, the contribution from QCD multijet production is 24–42%, depending on the $E_T$ reconstruction algorithm; the rest is from W/Z/t\bar{t} production. In order to illustrate the effect of the cracks, distributions are also shown for those subsets of these samples that have at least one jet that is aligned with the $E_T$ to within $\Delta \phi (E_T, \text{jet}) < 0.2$ and that is pointing towards masked ECAL channels, the barrel-endcap boundary ($1.3 < |\eta| < 1.7$), or the endcap-forward boundary ($2.8 < |\eta| < 3.2$). The masked ECAL channels considered here are those that are part of a group of $5 \times 5$ or $5 \times 1$ masked channels that are adjacent in $\eta$-$\phi$, as they have larger impact on the $E_T$ distributions than isolated masked channels. A jet is considered to be pointing to one of the masked ECAL channels when its jet centroid is within $\Delta R < 0.2$ of a masked ECAL channel, where $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}$. We can see effects on the $E_T$ distribution from masked ECAL channels, while the calorimeter boundaries do not appear to have an enhanced contribution to the events with large $E_T$.

Figure 5 shows the fraction of dijet events with at least one jet aligned with the $E_T$ and also pointing towards the masked ECAL channels, the barrel-endcap boundary, or endcap-forward boundary for data and for simulation. Figure 5(left) shows that the masked ECAL channels enhance the rate of events with large $E_T$ in both data and Monte Carlo simulation. Approximately
20% of the events with $\vec{E}_T > 80$ GeV have contributions to the measured $\vec{E}_T$ from mismeasurements due to masked ECAL channels. Results from simulations indicate that the fraction of events with large $\vec{E}_T$ due to mismeasurements (excluding the predicted contributions from sources of genuine $\vec{E}_T$, such as W/Z/\(t\bar{t}\)) is 30%. As shown in figures 5 (middle) and 5 (right), the fraction of events which contain a jet that is both aligned with the $\vec{E}_T$ and pointing towards a calorimeter boundary does not have a strong dependence on $\vec{E}_T$, indicating that the calorimeter boundaries are not major contributors to events that have large apparent $\vec{E}_T$ due to mismeasurements. Unlike the masked ECAL channels, the cracks are not projective to the interaction point, and therefore energies of particles traversing these cracks are still measured, albeit with degraded resolution.

While the impact of the cracks is small, analyses sensitive to events with large $\vec{E}_T$ need to take the ECAL masked channels into account. About 70% of the ECAL channels that are masked
during offline reconstruction have a useful measurement of their energy from the separate readout of the L1 trigger. Although the trigger readout saturates at $\ET = 64\text{ GeV}$, it can be used to recover energies smaller than this and to identify events that had more than this amount of energy in a masked channel. The saturation level was increased to 128 GeV in 2011. Analysts can veto events with a jet pointing towards an ECAL masked channel that does not have trigger information or that has trigger-readout energy at the saturation threshold.

6 Missing transverse energy scale and resolution

In this section, we study the performance of $\MET$ using events where an identified $Z$ boson or isolated $\gamma$ is present. Events containing vector bosons may be produced in hard parton-parton collisions such as $qg \rightarrow q\gamma$, $q\bar{q} \rightarrow Z$, $qg \rightarrow qZ$, and $q\bar{q} \rightarrow gZ$. While there is no genuine $\MET$ in these events, we can induce it by removing the vector boson. By comparing the momenta of the well-measured and well-understood vector boson to the $\MET$ induced this way, we probe the detector response to the global hadronic system and measure the scale and resolution of $\MET$. While the lowest order under-
lying processes may be simple, many physics and experimental issues contribute to the measured, induced $\vec{E}_T$ in these events. Effects due to jet energy scale corrections and fluctuating jet composition directly impact the measurement of the hadronic products of the hard collision. Underlying event activity, pile-up, detector noise, and detector acceptance contribute as well.

The following notation is used: the vector boson momentum in the transverse plane is $q_T$, and the hadronic recoil, defined as the vector sum of the transverse momenta of all particles except the vector boson (or its decay products, in the case of $Z$ candidates), is $\vec{u}_T$. Momentum conservation in the transverse plane requires $\vec{q}_T + \vec{u}_T = 0$. The recoil is the negative of the induced $\vec{E}_T$.

The presence of a well-measured $Z$ or $\gamma$ provides both a momentum scale, $q_T \equiv |\vec{q}_T|$, and a unique event axis, $\hat{q}_T$. The hadronic recoil can be projected onto this axis, yielding two signed components, parallel ($u_{\parallel}$) and perpendicular ($u_{\perp}$) to the event axis. Since $u_{\parallel} \equiv \vec{u}_T \cdot \hat{q}_T$, and the observed hadronic system is usually in the opposite hemisphere from the boson, $u_{\parallel}$ is typically negative.

The absolute value of the mean of the scalar quantity $u_{\parallel}/q_T$ is the scale factor correction required for $\vec{E}_T$ measurements in the classes of events considered here, and is closely related to jet energy scale corrections and jet parton flavour. We refer to $|\langle u_{\parallel} \rangle|/q_T$ as the “response” and denote distributions of this quantity versus $q_T$ as “response curves”. Deviations of the response curve from unity probe the $\vec{E}_T$ response as a function of $q_T$.

Resolution is assessed by measuring the RMS spread of $u_{\parallel}$ and $u_{\perp}$ about their mean values, after correcting for the response, and is denoted $\text{RMS}(u_{\parallel})$ and $\text{RMS}(u_{\perp})$. As with the response, we examine the resolutions as functions of $q_T$.

The uncertainty on the $\vec{E}_T$ scale and resolution for a generic physics analysis has a strong dependence on the final state being studied: events where the transverse momenta of the jets in the final state are small compared to the $p_T$ of a lepton (often true, for example, for leptonic W decays) will have very different uncertainties than those dominated by several high $p_T$ jets. Each physics analysis must have its $\vec{E}_T$ uncertainty evaluated carefully for its particular final state. The error bars shown on the plots in these figures, however, can give an order of magnitude estimate of the resulting uncertainty for similar final states.

### 6.1 Direct photon sample

Candidate photon events are selected by requiring each event to contain exactly one reconstructed photon in the barrel portion of the ECAL ($|\eta| < 1.479$), with $q_T > 20$ GeV, and which passes the identification and isolation selection described in section 3. The total number of events passing all requirements is 157,567, of which 67,621 have only one reconstructed primary vertex. The prescale factors for the HLT triggers used to collect this sample varied over the course of the 2010 LHC running period. As a result, this sample is dominated by events recorded during the earlier period of the data taking, when the fraction of crossings containing pile-up interactions was smaller.

Figure 6 shows the photon $q_T$ spectrum for data and for simulation. About half of the observed rate arises from QCD dijet production where one jet passes all photon identification requirements. Such jets are typically highly enriched in $\pi^0 \rightarrow \gamma \gamma$ and contain little hadronic activity. The detector response to these jets is similar to that of single photons, and studies indicate that response curves extracted from these QCD background events match the response of true photon-jet events to within a percent. We therefore make no further attempt to filter them out. The detector response to the jet depends on the type of parton from which it originated. The leading jet in photon events is
predicted to predominantly be a quark jet. A prediction for the difference in response for the CMS
detector between quark and gluon jets can be found in [20]. The difference is largest for Calo Jets
(≈ 20% for jets with $p_T$ of 20GeV), and decreases with $p_T$. The primary reason that the response
is lower for gluon jets is that their particles tend to have lower $p_T$s, and the calorimeter response
is lower at low $p_T$. For PF jets and PF $E_T$, which use tracker instead of calorimeter momenta for
most charged hadrons, the difference in response is reduced, and varies from about 5% at 20GeV
to a percent a high $p_T$.

### 6.2 Z samples

For the $Z \rightarrow e^+e^-$ selection (electron channel), we require two well-identified and isolated electrons
with $p_T > 20$ GeV, within the fiducial region of the ECAL. The invariant mass ($M_{\ell\ell}$) of the electron
pair is required to be in the range $70 < M_{\ell\ell} < 120$ GeV.

For the $Z \rightarrow \mu^+\mu^-$ selection (muon channel), we require two isolated muons with opposite
electric charges, that have $p_T > 20$ GeV, and are within the $|\eta| < 2.1$ region. The invariant mass
$M_{\ell\ell}$ of the muon pair is required to be at least 60GeV and no more than 120GeV.

We obtain a total of 12 635 (12 383) $Z \rightarrow e^+e^- (Z \rightarrow \mu^+\mu^-)$ candidates. The relative contributions of signal and background are estimated from simulation. By normalizing the signal plus background invariant mass distribution from simulation so that it has the same number of events as observed in the data, a total background of around 143 (35) events is estimated, with contributions of 97 (2) events from QCD, 28 (9) events from electroweak, and 18 (24) from final states containing top quarks.

Figure 7 shows the $M_{\ell\ell}$ distributions for the electron and muon samples. Figure 8 shows their
$q_T$ spectra. Except at very low $q_T$, the leading jet in $Z$ events, as with the $\gamma$ events, should usually
be a quark jet.
Figure 7. (left) Invariant mass distribution of the two leading electrons and (right) invariant mass distribution of the two leading muons, for the Z boson candidates, along with the predicted distributions from simulation. QCD refers to multijet events.

Figure 8. The $q_T$ distribution for Z boson candidates in (left) the electron channel and (right) the muon channel, along with the prediction from simulation. Systematic uncertainties are shown as grey bands.

6.3 Scale and resolution for events with one primary vertex

To study the $E_T$ scale and resolution, we decompose the recoil with respect to the boson ($\gamma$ or $Z$) direction in the transverse plane. We restrict ourselves to events containing one reconstructed primary vertex. Z yields are thus reduced to 2611 $Z \rightarrow e^+e^-$ candidates and 2438 $Z \rightarrow \mu^+\mu^-$ candidates. The effect of pile-up on the scale and the resolution is studied in section 6.5.1. Distributions of the components of the recoil calculated from PF $E_T$ that are parallel and perpendicular to the boson axis, $u_\parallel$ and $u_\perp$, are shown in figure 9 for direct photon candidates, $Z \rightarrow e^+e^-$ candidates, and $Z \rightarrow \mu^+\mu^-$ candidates. As expected, the parallel component is mainly negative, consistent with the back-to-back nature of the events, while the perpendicular component is symmetric.

The distributions are corrected for the residual contamination ($5 \pm 1\%$) from events with more
than one interaction. The number of events with more than one scattering that are reconstructed as a single PV is estimated by convolving the efficiency for reconstructing two vertices as a function of the vertex separation with the \( z \) distribution of vertices. The distributions are corrected for this contamination by subtracting multi-vertex-event shapes obtained from data, rescaled to the estimated contamination, from the distribution from events with one PV. The systematic uncertainty on the residual contamination is obtained by varying the normalization within its uncertainties.

Events generated with \textsc{pythia} are reweighted so that the \( q_T \) spectrum matches that predicted by the \textsc{resbos} Monte Carlo program [21], in order to take advantage of its resummed calculation of the boson \( q_T \) spectrum. The systematic uncertainties due to our imperfect knowledge of the true \( q_T \) distributions for Z bosons are estimated from the difference between the \( q_T \) distributions predicted by \textsc{pythia} and \textsc{resbos}. We set the systematic uncertainty, bin-by-bin in \( q_T \), equal to this difference.

In addition, there is a systematic uncertainty on the prediction from the simulation due to the size of the simulation samples. The dominant uncertainty on the \( u_j \) distribution from the electron channel below \(-100\,\text{GeV}\) is from this source and from uncertainties on the removal of the multi-PV contamination.

Figure 10 shows the response curves, \(|\langle u_j \rangle|/q_T\) versus \( q_T \), extracted from data, for the three \( \slashed{E}_T \) reconstruction algorithms, \textsc{calo} \( \slashed{E}_T \), \textsc{tc} \( \slashed{E}_T \), and \textsc{pf} \( \slashed{E}_T \), for \( \gamma, Z \rightarrow e^+ e^- \), and \( Z \rightarrow \mu^+ \mu^- \) samples.
Figure 10. Response curves for events with one primary vertex, for (left) Calo $E_T$, (middle) TC $E_T$, and (right) PF $E_T$. Results are shown for photon events (full blue circles), $Z \rightarrow e^+e^-$ events (open red circles) and $Z \rightarrow \mu^+\mu^-$ events (open green squares). The upper frame of each figure shows the response in data; the lower frame shows the ratio of data to simulation. The vertical axis labels at the far left apply to all three subfigures.

Figure 11. Resolution curves for components of hadronic recoil measured in direct photon candidate events with one primary vertex, (left) parallel to the boson direction, and (right) perpendicular to the boson direction. Data and simulation are indicated by points and histograms, respectively. Black circles denote Calo $E_T$, pink squares TC $E_T$, and blue triangles PF $E_T$. Shaded regions indicate statistical uncertainties on the simulation.

The agreement in response between the different samples is good. The agreement between data and simulation is good, and the results indicate that the three reconstruction algorithms are distinct in their capabilities, performing differently in the recovery of hadronic activity in the detector. The response for Calo $E_T$ is slightly larger than one because the jet energy scale used in the type-I corrections was determined from a sample with a mixture of quark and gluon jets, while in these samples the leading jet is primarily a quark jet. The TC $E_T$ response is lower because it has neither
Figure 12. Resolution curves for components of hadronic recoil calculated using PF $\not{E}_T$, measured in events with one primary vertex, (left) parallel to the boson direction, and (right) perpendicular to the boson direction. $Z \to \mu^+\mu^-$, $Z \to e^+e^-$ and $\gamma$ events are indicated by open green squares, open red circles, and full blue circles, respectively. The lower frame indicates the ratio of data to simulation. The vertical axis labels at the far left apply to both subfigures.

Figure 11 shows the resolution curves from photon candidate events for $u_\parallel$ and $u_\perp$ for data and simulation, for all three reconstruction algorithms. Figure 12 shows the resolution as measured in $\gamma$, $Z \to e^+e^-$, and $Z \to \mu^+\mu^-$ events for PF $\not{E}_T$. The measured resolution must be corrected for the scale to avoid a misleading result; e.g., the apparent resolution on $u_\perp$ is proportional to the scale and therefore an algorithm with a scale that is smaller than unity could appear to have a better resolution than one with a scale of unity without such a correction. Since only Calo $\not{E}_T$ has been corrected fully for the detector response with both type-I and type-II corrections, the resolution measurements are rescaled, bin by bin, using the corresponding response curves of figure 10. The data confirm the prediction from simulation that tracking information significantly enhances the $\not{E}_T$ resolution. The resolutions measured in the different samples are in good agreement, but are $\approx 10\%$ worse than expected from the simulation. A similar difference in resolution for jets in the 2010 run is documented in [14]. The small discrepancies between data and simulation shown in figure 9 are due to this difference.

6.4 Resolution in multijet events

The $\not{E}_T$ resolution can also be evaluated in events with a purely hadronic final state, where the observed $\not{E}_T$ arises solely from resolution effects. Because the $\not{E}_T$ resolution has a strong dependence on the associated $\sum E_T$, it is presented as a function of $\sum E_T$. We characterize the $\not{E}_T$ resolution using the $\sigma$ of a Gaussian fit to the distribution of the $x$ and $y$ components of $\not{E}_T (\not{E}_{x,y})$. In order
to make a meaningful comparison, we calibrate the measured $E_T$ for the different algorithms to the same scale using the response from figure 10. These corrections would not be needed if all $E_T$ algorithms had both type-I and type-II corrections.

We use the PF $\Sigma E_T$ in plotting the $E_T$ resolutions for all three algorithms, as it gives the best estimate of the true $\Sigma E_T$, and hence is an accurate evaluation of the event activity. We calibrate PF $\Sigma E_T$ to the particle-level $\Sigma E_T$, on average, using the predicted average mean value as a function of the particle-level $\Sigma E_T$ from a simulation of events from the PYTHIA 8 event generator [22].

Figure 13 shows the calibrated $E_{x,y}$ Gaussian core resolution versus the calibrated PF $\Sigma E_T$ for different $E_T$ reconstruction algorithms in events containing at least two jets with $p_T > 25$ GeV. Both TC $E_T$ and PF $E_T$ show improvements in the $E_T$ resolution compared to the Calo $E_T$, with the PF $E_T$ yielding the smallest $E_T$ resolution.

Figure 14 shows the PF $E_T$ distributions for different intervals of Calo $\Sigma E_T$ and for jet multiplicities varying from two to four, normalized to the same area. The jets are required to be above a $p_T$ threshold of 20 GeV. The good agreement of the normalized shapes in figure 14 indicates that PF $E_T$-performance in events without genuine $E_T$ is driven by the total amount of calorimetric activity (parametrized by Calo $\Sigma E_T$) and no residual nonlinear contribution from jets to PF $E_T$ is visible. Similar behaviour is also observed for Calo $E_T$ and TC $E_T$.

6.5 Effect of multiple interactions

Pile-up, namely multiple proton collisions within the same bunch crossing, occurs because of high LHC bunch currents and can play an important role in $E_T$ performance.

Because there is no true $\vec{E}_T$ in minimum-bias events and because the average value for a component of $\vec{E}_T$ in these events is zero (e.g., the $x$ or $y$ component), pile-up should have only a small effect on the scale of the component of the measured $\vec{E}_T$ projected along the true $\vec{E}_T$ direction. Pile-up, however, will have a considerable effect on the resolution of the parallel and perpendicular components.

We investigate the effect of pile-up using multijet samples, $\gamma$, and Z data.
Figure 14. PF $E_T$ distributions in 2-, 3-, and 4-jet events, in selected Calo $\Sigma E_T$ bins.

Figure 15. The ratio of the responses for the component of the induced $\vec{E}_T$ along the boson direction, measured in $\gamma$ events containing 1 PV and at least 2 PVs, for (left) Calo $E_T$, (middle) TC $E_T$, and (right) PF $E_T$. Also given is the best fit value for the average ratio, which corresponds to the solid, red line.

6.5.1 Studies of pile-up effects using photon and $Z$ events

In this section, we use samples containing a vector boson to measure the effect of pile-up on the scale and resolution of a component of $\vec{E}_T$. Figure 15 shows the ratio of the responses measured in $\gamma$ events containing 1 PV and at least 2 PVs. The ratio of the responses of the component of the induced $\vec{E}_T$ along the boson direction is close to one, as expected. It is slightly larger at low $q_T$ when pile-up is present. This is expected, as pile-up can reduce energy lost due to zero suppression in the readout of the calorimeter if energy from a pile-up interaction and from the hard scattering are both in the same readout channel. If the sum is larger than the zero suppression thresholds, more of the energy from the hard scattering is recorded.

Figure 16 shows the resolution versus the $q_T$ of the $\gamma$ for the components of the hadronic recoil parallel and perpendicular to the boson direction for 1, 2, and 3 reconstructed PVs. Also shown is the prediction from simulated $\gamma$ events without pile-up. Figure 17 shows the resolution versus the $q_T$ of the $Z$ for the parallel and perpendicular components of the hadronic recoil. The
parametrization of $E_T$ resolution used in figures 16 and 17 is given by
\[
\sigma_{\text{total}}^2 = (a \sqrt{q_T} + b)^2 + (\sigma_{\text{noise}} f_{\text{ES}}(q_T))^2 + (N - 1) (\sigma_{\text{PU}} f_{\text{ES}}(q_T))^2,
\]
where $a$ and $b$ characterize the hard process, $\sigma_{\text{noise}}$ is the intrinsic noise resolution, $N$ is the number of reconstructed vertices in the event, $\sigma_{\text{PU}}$ is the intrinsic pile-up resolution, and $f_{\text{ES}}(q_T)$ is the energy scale correction applied on each event. At low $q_T$, the resolution is dominated by contributions from the underlying event and detector noise ($\sigma_{\text{noise}}$). Since these contributions cannot be distinguished from those due to the particles from the recoil, and since the recoil measurement needs to be corrected for the detector response, these contributions are magnified and have a larger effect at low boson $q_T$ when energy scale corrections are applied. As expected, the resolution is degraded with increasing pile-up interactions. Results from the $Z$ and $\gamma$ channels are in agreement and are similar to the values obtained in section 6.5.2 from jet data.

6.5.2 Studies of pile-up effects in jet data

In this section, we study the behaviour of the PF $E_T$ distributions in samples containing high $p_T$ jets when pile-up is present. The data are selected using a prescaled $H_T$ trigger with a threshold of 100GeV, where $H_T$ is defined as the scalar sum of the transverse momenta of PF jets ($p_T > 20\text{GeV}$, $|\eta| < 3$). Additionally, in the offline analysis, each event is required to have $H_T$ (calculated using PF jets) $>$ 200GeV to avoid bias from the trigger. Figure 18 shows that the widening of the PF $E_T$ distribution with increasing number of vertices can be modeled by convolving the $x$ and $y$
components of the one-vertex $E_T$ shape with a Gaussian function $G$ whose mean is $(n - 1) \cdot \Delta \mu_z$ and whose standard deviation is $\sqrt{n - 1} \cdot \Delta \sigma_z$:

$$E_{T,n} = \sqrt{(E_{x1} \otimes G[(n - 1) \cdot \Delta \mu_z, \sqrt{n - 1} \cdot \Delta \sigma_z])^2 + (E_{y1} \otimes G[(n - 1) \cdot \Delta \mu_y, \sqrt{n - 1} \cdot \Delta \sigma_y])^2}, \quad (6.2)$$

where $E_{x,y}$ are the $x$ and $y$ components of $E_T$. Here we assume that each additional vertex contributes with a constant $\Delta \mu_z$ ($\Delta \sigma_z$) to the $E_T$ resolution such that the resolution with $n$ pile-up interactions is related to that with one primary vertex via $\sigma_{n1}^2 = \sigma_{11}^2 + (n - 1) \Delta \sigma_z^2$. In addition we also allow for a linear shift of $E_x$ and $E_y$ by $\Delta \mu_x$ ($\Delta \mu_y$) such that $\mu_{zn} = \mu_{z1} + (n - 1) \Delta \mu_z$. A fit of eq. (6.2) to data results in $\Delta \sigma_x = \Delta \sigma_y = 3.7 \text{ GeV}$, consistent with the results from section 6.5.1. This fit is performed simultaneously on the $E_T$ distributions of events containing two to seven vertices. The shifts of the $x$ and $y$ $E_T$ components are estimated to be $\Delta \mu_x = 0.5 \text{ GeV}$ and $\Delta \mu_y = -0.3 \text{ GeV}$, respectively, which are small compared to $\Delta \sigma$ and are consistent with the expected shift seen in simulation due to nonfunctioning channels.

7 Studies of physics processes containing genuine $E_T$

In this section, we examine distributions relevant to $E_T$ in events containing neutrinos. Events containing W bosons and b quarks are studied.
Figure 18. PF $\slashed{E}_T$ distributions in pile-up events. The figures show a comparison between the one- and $n$-vertex shapes ($n = 2, \ldots, 7$) and the results of a simultaneous fit of eq. (6.2) to the $n$-vertex shapes. The one-vertex distribution is normalized to the $n$-vertex distribution for each plot.

7.1 W events

The performance of $\slashed{E}_T$ is studied in events that contain large, genuine $\slashed{E}_T$: W → ℓν events, where ℓ is a muon or electron. For most W events, the magnitude of $\slashed{E}_T$ is approximately equal to the $p_T$ of the charged lepton, but its resolution is dominated by the hadronic recoil. When the W $q_T$ is small compared to the W mass, the $\slashed{E}_T$ is approximately

$$\slashed{E}_T \approx p_T(\ell) - u_\ell,$$

where $u_\ell$ is the component of the recoil parallel to the lepton transverse direction.
In the $W \rightarrow \mu \nu$ decay channel, events are required to have been collected by a single-muon high-level trigger. In addition, candidates are selected by requiring a muon with $|\eta| < 2.1$ and $p_T > 25 \text{GeV}$. Events with a second muon with $p_T > 25 \text{GeV}$ are rejected to suppress $Z$ and $t\bar{t}$ contamination. $W \rightarrow e\nu$ decays are identified using similar selection criteria. A single-electron high-level trigger requirement with a $p_T$ threshold of $15 \text{GeV}$ is applied. Events are also required to contain an electron with $p_T > 25 \text{GeV}$. Events with a second electron with $p_T > 20 \text{GeV}$ are rejected, and rejection against $\gamma$ conversions is applied. A total of 24,628 (29,200) $W \rightarrow \mu\nu$ ($W \rightarrow e\nu$) events with only one primary vertex are selected.

The main sources of background to the $W \rightarrow \ell\nu$ signal are multijet events with one jet misidentified as a high-$p_T$ muon or electron and $Z \rightarrow \ell\ell$ events with one lepton escaping detection. The multijet events usually have low values of $\slashed{E}_T$. The apparent $\slashed{E}_T$ in these events (which have no genuine $\slashed{E}_T$) tends to be amplified by scale corrections to the $\slashed{E}_T$ (type-I and type-II). Other backgrounds include $W$ and $Z$ bosons decaying into $\tau$, followed by $\tau \rightarrow \ell\nu\bar{\nu}$, and $t\bar{t}$ events with one top quark decaying semileptonically. The relative normalization of the different simulated electroweak (EWK) signal event ensembles, and simulations of those backgrounds that contain an electroweak boson ($W \rightarrow \ell\nu$, $Z \rightarrow \ell\ell$, $t\bar{t}$), are set by the ratios of their theoretical cross sections computed at next-to-leading order [23]. The normalization of the composite EWK and the QCD contributions are established through a one-parameter binned fit to the $\slashed{E}_T$ distribution from data.

Figure 19 shows the $\slashed{E}_T$ distribution for the $W \rightarrow e\nu$ and $W \rightarrow \mu\nu$ candidate samples, along with the expectation from simulation. As for the analyses using $Z$ events, the background distributions include a grey-shaded band indicating the estimated uncertainty due to the size of the simulation samples, modeling of the $W q_T$ spectrum, and the pile-up correction procedure. In most cases this uncertainty is too small to be visible. Data and simulation agree well, and the $W$ shows up prominently as expected.

Figure 19 also shows the distribution of $u_T$, the magnitude of $\vec{u}_T$. To suppress QCD background, for the $u_T$ studies only, we further require that the $W$ candidate pass a requirement on the transverse mass, defined as $M_T = \sqrt{p_T(\ell)\slashed{E}_T\,(1 - \cos\Delta\phi)}$, where $\Delta\phi$ is the opening angle in the transverse plane between the lepton candidate and the $\slashed{E}_T$. We require $M_T > 50 \text{GeV}$ and $\slashed{E}_T > 25 \text{GeV}$. The $\slashed{E}_T$ resolution has substantial contributions from the mismeasurement of the many particles in the underlying event. These contributions can be more clearly seen in the $u_T$ distribution, since they are not obscured by the contributions from the charged lepton. Again we see reasonable agreement between data and simulation.

7.2 Heavy flavour production and $\slashed{E}_T$

The $\slashed{E}_T$ distributions from jet samples containing $b$ quarks can differ from those of inclusive jet samples because the $B$ hadrons have unique fragmentation properties, and sometimes their final states contain neutrinos. Neutrinos from $b$ jets are one of the main sources of severe underestimations of jet energies (the other main source being the ECAL masked channels discussed in section 5.3). In this section, we study the induced $\slashed{E}_T$ in an inclusive $b$-tagged jet sample.

We compare the $\slashed{E}_T$ distributions in dijet events with and without a secondary vertex, i.e., events where the leading jet has a positive SSV (displaced vertex) tag or a SMbyPt (lepton) tag [6, 7]. (Section 3 includes a description of these algorithms.) Since these taggers rely on tracking information, we require the leading jet to have $|\eta| < 2.1$. Also, we require the leading two jets
Figure 19. The PF $E_T$ (left) and $\eta_T$ (right) distributions in $W \rightarrow e\nu$ (top) and $W \rightarrow \mu\nu$ (bottom) candidate events. Both data (points) and simulation (solid lines) are shown. The plots on the right include selection requirements on $E_T$ and $M_T$, while those on the left do not.

to have $p_T > 40\text{GeV}$. Below this value, the b-quark tagging purity is significantly reduced. A prescaled jet trigger with a $p_T$ threshold of 15 GeV was used; the resulting sample corresponds to an integrated luminosity of $0.025 \text{ pb}^{-1}$. Figure 20 shows the fraction of events from this sample with a b-tagged jet as a function of $E_T$ for the two tagging algorithms. The larger increase in the fraction of b-tagged events at large $E_T$ for SMbyPt than for SSV is due, in part, to the higher probability of neutrinos in leptonically tagged events.

8 $E_T$ significance

A spurious nonzero $E_T$ in an event can have contributions from many sources, including measurement resolution, reconstruction inefficiencies, instrumental defects, and improper pattern recognition. Events in which the reconstructed $E_T$ is consistent with contributions solely from particle-measurement resolutions and efficiencies can be identified by evaluating the $E_T$ significance, $S$. The significance offers an event-by-event assessment of the likelihood that the observed $E_T$ is consistent with zero given the reconstructed content of the event and known measurement resolutions. A similar variable used by the CDF collaboration is described in [24].
SSV-Tag MC
SSV-Tag MC
SSV-Tag Data
SSV-Tag Data
Figure 20. Fraction of events in a multijet sample that contain a jet tagged as a b jet by the SSV and SMbyPt taggers for (left) Calo $E_T$ and (right) PF $E_T$.

8.1 Definition

The significance requires evaluation of the uncertainty in the total measured transverse momentum, which is given by

$$\vec{E}_T^\text{total} = \sum_{i \in X} \vec{E}_T = -\vec{E}_T,$$  \hspace{1cm} (8.1)

where $\vec{E}_T = (E_x, E_y)$ is the measured transverse momentum of the $i$th reconstructed object. $X$ is the set of reconstructed objects, such as calorimeter towers (for Calo $E_T$) or PF particles (for PF $E_T$), used to calculate $\vec{E}_T$. In the derivation of the significance, three quantities are relevant for each object in the sum. The first of these is $\vec{e}_T$, the true transverse momentum of the object. Under the null hypothesis of zero genuine total transverse momentum, $\sum_{i \in X} \vec{e}_T = 0$. The second is $\vec{E}_T$, the measured transverse momentum of the object, which is distributed according to $P_1(\vec{E}_T | \vec{e}_T)$, the probability density function (pdf) for observing the measured transverse momentum given the true transverse momentum of the object. The third is $\vec{e}_T = \vec{E}_T - \vec{e}_T$. For convenience, we define an equivalent pdf in terms of this difference: $P_1(\vec{e}_T | \vec{e}_T) \equiv P_1(\vec{e}_T | \vec{e}_T)$. Given the null hypothesis, $\sum \vec{E}_T = \sum \vec{e}_T$, so that the $i$th reconstructed object contributes $\vec{e}_T$ to the measured total transverse momentum.

We first introduce the likelihood that we would observe a total transverse momentum $\vec{e}$ under our null hypothesis. For the two-object case, the likelihood function is given by

$$L(\vec{e}) = \int P_1(\vec{E}_T_1 | \vec{e}_T_1) P_2(\vec{E}_T_2 | \vec{e}_T_2) \delta(\vec{e} - (\vec{E}_T_1 + \vec{E}_T_2)) d\vec{E}_T_1 d\vec{E}_T_2$$

$$= \int P_1(\vec{e}_T_1 | \vec{e}_T_1) P_2(\vec{e}_T_2 | \vec{e}_T_2) \delta(\vec{e} - (\vec{e}_T_1 + \vec{e}_T_2)) d\vec{e}_T_1 d\vec{e}_T_2$$

$$= \int P_1(\vec{e}_T_1 | \vec{e}_T_1) P_2(\vec{e}_T_2 | \vec{e}_T_2) \delta(\vec{e} - (\vec{e}_T_1 + \vec{e}_T_2)) d\vec{e}_T_1 d\vec{e}_T_2,$$  \hspace{1cm} (8.2)

since $0 = \sum \vec{e}_T = \vec{e}_T_1 + \vec{e}_T_2$. For an arbitrary number of input objects, the full likelihood function can be generated by a recursive application of eq. (8.2). The significance is defined as the log-
likelihood ratio

$$S \equiv 2 \ln \left( \frac{\mathcal{L}(\bar{\epsilon} = \sum \bar{\epsilon}_i)}{\mathcal{L}(\bar{\epsilon} = 0)} \right), \quad (8.3)$$

which compares the likelihood of measuring the total observed $\bar{E}_T^{\text{total}} = \sum \bar{E}_T = \sum \bar{\epsilon}_i$ to the likelihood of the null hypothesis, $\bar{E}_T^{\text{total}} = 0$.

This formulation is completely general and accommodates any probability distribution function. In practice, however, we often employ Gaussian uncertainties for measured quantities, for which the integrals of eq. (8.2) can be done analytically. The Gaussian probability density function is given by

$$p_i(\bar{\epsilon}_i|\bar{E}_T) \sim \exp \left( -\frac{1}{2} (\bar{\epsilon}_i)^\dagger V_i^{-1} (\bar{\epsilon}_i) \right),$$

where $V_i$ is the $2 \times 2$ covariance matrix associated with the $i$th measurement. The integration of eq. (8.2) yields

$$\mathcal{L}(\bar{\epsilon}) \sim \exp \left( -\frac{1}{2} (\bar{\epsilon})^\dagger \left( \sum_i V_i \right)^{-1} (\bar{\epsilon}) \right). \quad (8.4)$$

The covariance matrix $U_i$ for each reconstructed object in the $\bar{E}_T$ sum is initially specified in a natural coordinate system having one axis aligned with the measured $\bar{E}_T$ vector, $\bar{E}_T \equiv (E_T \cos \phi, E_T \sin \phi)$:

$$U_i = \begin{pmatrix} \sigma_{\bar{E}_T}^2 & 0 \\ 0 & \sigma_{\phi}^2 \end{pmatrix}. \quad (8.5)$$

(We adopt the simplifying assumption that $E_T$ and $\phi$ measurements are uncorrelated.) This matrix is rotated into the standard CMS $x$-$y$ reference frame to give the error matrix

$$V_i = R(\phi_i) U_i R^{-1}(\phi_i), \quad (8.6)$$

where $R(\phi_i)$ is the rotation matrix. The matrix summation is then performed in this common reference frame. Combining eqs. (8.3), (8.4), and (8.6) yields

$$S = \left( \sum_{i \in X} \bar{E}_T_i \right)^\dagger \left( \sum_{i \in X} R(\phi_i) U_i R^{-1}(\phi_i) \right)^{-1} \left( \sum_{i \in X} \bar{E}_T_i \right). \quad (8.7)$$

Equation (8.7) makes explicit the dependence of $S$ and $\bar{E}_T$ on the set of objects $X$ over which the vectors and matrices are summed. In general $S$ is small when the $\bar{E}_T$ can be attributed to measurement resolution, and large otherwise.

In the Gaussian case, $S$ is simply a $\chi^2$ with two degrees of freedom. If we rotate into a coordinate system with the $x$ axis parallel to the $\bar{E}_T$ axis, instead of the CMS horizontal axis, then eq. (8.7) is simplified to

$$S = E_T^2 / (\sigma_{\bar{E}_T}^2 (1 - \rho^2)), \quad \text{where } \sigma_{\bar{E}_T}^2 \text{ is the variance of the magnitude of } \bar{E}_T, \text{ and } \rho \text{ is the correlation coefficient between the variances parallel to and perpendicular to the}$
measured $\vec{E}_T$. This form emphasizes the essential meaning of $S$, but obscures the important feature that, through its denominator, $S$ embodies the full topological information in the event. Essential features such as the angles between the measured $\vec{E}_T$ and the reconstructed objects in the event are embedded in the definition of the denominator. This form also makes apparent the relationship between the true significance (in the Gaussian limit) and the more naive measure $\Sigma = \vec{E}_T / \sqrt{\sum \vec{E}_T}$.

The specialization to a Gaussian probability density function is less restrictive than it may appear, as any probability density function expressible as a linear combination of Gaussians is accommodated by the formalism presented here.

To apply eq. (8.7) to PF $\vec{E}_T$ significance, we note that the Gaussian pdf only accommodates measurement resolution. Using only reconstructed PF particles to determine the covariance matrix would neglect fluctuations in the measured PF particle content itself. These fluctuations arise from detection and reconstruction efficiencies, and provide a nonnegligible contribution to the PF $\vec{E}_T$ resolution. These fluctuations, however, also affect the PF jet resolutions. We can therefore substitute the PF jet resolutions for the combined measurement resolutions of the PF particles that have been clustered into jets. The sum of covariance matrices in eq. (8.7) thus includes contributions from PF jets, PF particles that were not considered during jet finding (e.g. isolated leptons), and PF particles that are not clustered into any jet. This approach inherently takes into account the contributions both from measurement resolution and from fluctuations in the reconstructed particle content.

The covariance matrices $U_i$ of eq. (8.5) are obtained from the known response of each type of PF particle or jet as a function of $p_T$ and $\eta$. The charged hadron and muon resolutions are obtained on a particle-by-particle basis from the error matrix from the final track fit, and the resolutions for electrons are those obtained from studies of data samples of known resonances such as neutral pions, $Z$ bosons, etc. The jet and photon resolutions are from simulation. No input resolutions were tuned based on the behaviour of the significance distribution itself.

### 8.2 Performance of $S_{PF}$ in dijet events

Because $S$ is $\chi^2$ distributed, it should exhibit a flat probability of $\chi^2$, $P(\chi^2)$, for two degrees of freedom in an event sample that nominally has no genuine $\vec{E}_T$. (That is, $1 - P(\chi^2)$ is the standard cumulative distribution function of the $\chi^2$ statistic for two degrees of freedom.) Dijet samples from pp collisions are dominated by such events.

We select dijet events by requiring at least two jets satisfying $|\eta| < 2.3$ and $p_T > p_T^{\min}$, with thresholds $p_T^{\min}$ of 30 or 60 GeV. One of the jets above threshold must have been responsible for the event passing an HLT single-jet trigger. We use data collected with a 15 GeV trigger threshold for our 30 GeV dijet sample, and a 30 GeV trigger threshold for the 60 GeV dijet sample. (Because of different prescale factors applied to the two trigger streams, the 60 GeV dijet sample is not a direct subset of the 30 GeV sample.)

We compare the distributions of the PF significance, $S_{PF}$, as well as the corresponding $P(\chi^2)$ distributions, in data and simulation in figure 21 for both values of the $p_T^{\min}$ threshold. The significance distribution very closely follows a pure exponential, and the $P(\chi^2)$ distribution is populated quite uniformly between zero and unity in both data and simulation. There is a small peak at zero in $P(\chi^2)$; simulation (figure 21) indicates that about half of this peak results from genuine $\vec{E}_T$ in the event sample. This $\vec{E}_T$ arises from a combination of sources such as the semileptonic decays of heavy quarks and the $\eta$ acceptance of the detector. The data and simulation distributions match...
well in the 30GeV threshold sample. MC studies show that the remainder of the excess of low probability events after accounting for genuine $E_T$ typically have at least one high-$p_T$ jet whose response is in the non-Gaussian tail of the response function.

To probe the stability of the $S_{PF}$ behaviour, we have studied dijet samples with different $p_T^{\text{min}}$ thresholds, which changes the relative contributions of different detector regions in the covariance matrix calculations. We find that, overall, the $S_{PF}$ distributions for the bulk of the data continue to exhibit near-ideal behaviour independent of threshold. As the 60GeV sample shown here demonstrates, though, the higher threshold data does begin to develop a larger tail in the significance, and a correspondingly larger peak at zero in $P(\chi^2)$, than we find in the simulation. The discrepancy between data and MC is below the 0.2% level. Visual examination of the events with low probability reveal that the discrepancy arises from a combination of events with a residual anomalous energy contamination and other events with a high-$p_T$ jet with activity straddling the endcap (HE) and forward (HF) calorimetry, for which the non-Gaussian tails are not yet perfectly modeled.

For the $S_{PF}$ distributions shown here, the transition point for use of resolutions based on PF jets rather than resolutions from unclustered PF particles in the $S_{PF}$ calculation (eq. (8.7)) occurs at a jet $p_T$ of 3GeV. The $S_{PF}$ distributions are insensitive to the variation of this transition point between jets and individual particles over the range of 1 to approximately 6GeV. By 10GeV, a slope in the $P(\chi^2)$ distribution clearly appears, indicating that we no longer account sufficiently for contributions to the $E_T$ resolution from fluctuations in the reconstructed particle content.

A powerful feature of the $E_T$ significance is that its distribution is insensitive to pile-up (for events with no genuine $E_T$). As long as the correct resolutions are input, the significance should still have a purely exponential behaviour with a uniformly distributed $P(\chi^2)$. In figure 21, no restrictions were made on the number of interaction vertices in the data, while the simulation has no pile-up. In figure 22, we compare the shapes of the single-vertex and multiple-vertex significance and $P(\chi^2)$ distributions in data. The shapes are very similar, as expected. The main difference arises in the low probability region, where the multiple interaction data exhibits behaviour closer to the ideal — an example of the central limit theorem. With the additional contributions to the $E_T$ resolution, the roles of the non-Gaussian response tails and genuine $E_T$ are diminished. The overall insensitivity can be useful, for example, when extrapolating backgrounds dominated by samples with nominally zero genuine $E_T$.

### 8.3 Application to $W \to e\nu$ events

As a case study, we examine the potential gain of introducing the significance variable into the selection criteria for $W \to e\nu$ analyses. The set of criteria employed is that of the recent measurement by the CMS Collaboration of the W cross section [25], for which backgrounds were reduced by means of a stringent, 80% efficient, electron isolation criterion. Signal and background yields in that analysis were determined by a fit to the reconstructed $E_T$ distribution, though because of the large backgrounds at small values of $E_T$, the signal level is largely determined from the $E_T > 20\text{GeV}$ region.

One analysis option would be to relax the electron isolation from an 80% to a 95% efficient criterion and introduce $E_T$ significance to help reduce backgrounds. Figure 23 compares the efficiency for signal versus background in simulation for increasing minimum thresholds on $E_T$, with both the 80% and 95% electron isolation criteria applied; $S_{PF}$, again with both isolation criteria;
Figure 21. Distributions of the $E_T$ significance $S_{PF}$ (left) and the corresponding probability of $\chi^2$, $P(\chi^2)$ (right), for dijet event samples in data (points) and simulation (solid histograms) with 30GeV (top) and 60GeV (bottom) jet $p_T$ thresholds. The dashed histograms show the simulation distributions with true $E_T$ contributions, from physics and acceptance effects, subtracted event-by-event. The dotted line overlaid on the $S_{PF}$ distributions shows a reference pure exponential function. Each inset expands the small $P(\chi^2)$ region.

and $E_T/\sqrt{\sum E_T}$ with the 95% isolation criterion. All efficiencies are measured relative to the signal or background yield obtained with the looser 95% electron isolation criterion applied. (As a result, the tighter 80% criterion has an asymptotic efficiency value of approximately 84%.) Application of the tighter criterion changes the relative signal and background distributions for $E_T$ and $E_T$ significance compared to the looser criterion. When a minimum $E_T$ threshold is applied, the tighter isolation criterion provides a better signal to background ratio at low background levels than the looser criterion. Application of a minimum $S_{PF}$ threshold with the looser criterion, however, outperforms all the other combinations for background rejection at a given signal efficiency.
Figures 22 and 23 also show that the $S_{PF}$ distributions for $W \rightarrow e \nu$ in data and simulation agree well. As expected, the backgrounds without genuine $E_T$ are compressed towards low values of $S_{PF}$ while signal events having real $E_T$ extend to high values of $S_{PF}$.

Figures 24 and 25 contrast the behaviour of signal and total background efficiencies for minimum $E_T$ or $S_{PF}$ thresholds for different numbers of interaction vertices (pile-up) in simulation. The jets and $\gamma$+jets backgrounds, which have no genuine $E_T$, dominate. As pile-up increases, the background contribution at higher $E_T$ grows, while that at high $S_{PF}$ remains quite stable. As a result, a background subtraction based on extrapolation of $E_T$ will be sensitive to the modeling of pile-up, while one based on extrapolation of $S_{PF}$ would not. As one can see from the signal versus background efficiency curves shown in figure 25, differentiation of signal from background degrades for both $E_T$ and $S_{PF}$ as pile-up increases. Regardless of the amount of pile-up, however, $S_{PF}$ always provides a superior signal to background ratio compared to $E_T$.

9 Conclusions

In conclusion, we studied $E_T$ as measured by the CMS detector in pp collisions at $\sqrt{s} = 7$ TeV during the 2010 run of the LHC. We have determined the $E_T$ scale, resolution, and tails, as well as the degradation of the $E_T$ performance due to pile-up. We find that we are able to remove most sources of anomalous energies that produce artificial, large $E_T$. The measured $E_T$ scale agrees with the expectations of the detector simulation, but the resolution is degraded by 10% in data. CMS has three different algorithms for calculating $E_T$. Algorithms using tracker information have
Figure 23. (left) Efficiency curves for $W \to e\nu$ signal versus backgrounds varying the minimum value of $E_T$ (solid lines), of $S_{PF}$ (dotted lines), and of $E_T/\sqrt{\sum E_T}$ (dot-dash line), with the 95% efficient (blue) or 80% efficient (red) electron isolation criterion applied. (right) Distributions of $S_{PF}$ in candidate $W \to e\nu$ events from data (points) and simulation (stacked histograms). The simulation components, from top to bottom, are signal (mustard) and backgrounds from jets (purple), $\gamma$+jets (black), $Z \to e^+e^-$ (yellow), and $W^{\pm} \to \tau^{\pm}\nu_{\tau}$ (orange). The simulation is scaled by a fit to the data with floating normalizations for the signal and the total background.

Figure 24. Efficiency versus minimum threshold curves for $W \to e\nu$ signal and for total background for different numbers of interaction vertices with a minimum applied $E_T$ threshold (left) and a minimum applied $S_{PF}$ threshold (right).
an improved resolution, and the use of a global particle-flow event reconstruction gives the best resolution. We find that pile-up interactions contribute to the degradation of the $E_T$ resolution but have little effect on the scale of the components of $E_T$. We also find that we can model its effects with a simple parametrization.

One of the most important uses of $E_T$ is to distinguish between genuine $E_T$ produced by weakly interacting particles and artificial $E_T$ from detector resolution. An algorithm, called $E_T$ significance, for separating genuine $E_T$ from artificial $E_T$, is shown to perform better than traditional variables such as $E_T$ alone or $E_T$ divided by the square root of the $\sum E_T$.

Because of the demonstrated good measurement of $E_T$, the CMS detector is ready to be used for a variety of precision physics measurements, such as studies of the W boson and the top quark, and searches for new neutral, weakly interacting particles.

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Appendix: optimization of $\mathbf{E}_\mathbf{T}$ corrections

In this section, we describe the optimization of the parameters used in the type-I and type-II corrections to $\mathbf{E}_\mathbf{T}$.

The $p_T$ threshold used to select the jets that receive the type-I corrections was optimized by examining its effect on the $\mathbf{E}_\mathbf{T}$ resolution and scale, and led to our choice of 10 GeV for PF $\mathbf{E}_\mathbf{T}$. We optimize the $p_T$ threshold to simultaneously obtain the best $\mathbf{E}_\mathbf{T}$ scale and $\mathbf{E}_\mathbf{T}$ resolution, under the constraint that very low-$p_T$ jets not be included in the calculation because their energy corrections have large uncertainties and can degrade the $\mathbf{E}_\mathbf{T}$ performance. The use of low-$p_T$ jets also makes the measurement more sensitive to pile-up.

Figure 26 shows the PF $\mathbf{E}_\mathbf{T}$ response versus $q_T$ for $\gamma$ candidate events for various jet thresholds for events with and without pile-up. As can be seen from these distributions, the type-I corrections substantially improve the $\mathbf{E}_\mathbf{T}$ scale, the dependence on the threshold is small for thresholds $\leq 10$ GeV, and the response is independent of the number of additional pile-up interactions.

Figure 27 shows the ratio of the PF $\mathbf{E}_\mathbf{T}$ resolution with type-I corrections to the PF $\mathbf{E}_\mathbf{T}$ resolution without type-I corrections for the parallel and perpendicular components of PF $\mathbf{E}_\mathbf{T}$ versus $q_T$ for $\gamma$ candidate events, for various jet thresholds and for events with and without pile-up. The op-
timal resolution for 1-vertex events is obtained for the chosen 10 GeV threshold; for this threshold, the degradation with pile-up is not large.

The same study was performed in $Z \rightarrow \mu^+\mu^-$ candidate events. The 10 GeV threshold is also found to optimize the $E_T$ scale and $E_T$ resolution in these events.

Type-II corrections were not used for analyses done using the 2010 data. However, studies were done to optimize the parameters for future use. The type-II correction is obtained using a $Z \rightarrow e^+e^-$ data sample. $Z$ events constitute an ideal sample for determining the type-II correction, as $Z$ bosons are generally produced with low $q_T$ and the recoil is often dominated by unclustered energy. We take the vector sum of the momenta from all calorimeter towers and PF particles not corrected by the type-I corrections as a single object denoted $\vec{U}$. The measured value of $\vec{U}$ is defined as

$$\vec{U}_{\text{meas}} = \vec{E}_{T,\text{uncorr}} - \sum p_{T,\text{jet,uncorr}} - \sum p_{T,e,\text{meas}},$$

(A.1)

where $\vec{E}_{T,\text{uncorr}}$ is the uncorrected $E_T$, $\sum p_{T,\text{jet,uncorr}}$ is the total momentum of uncorrected jets, and $\sum p_{T,e,\text{meas}}$ is the total momentum of the measured electrons. The sum is over all jets with corrected $p_T > 20$ GeV for Calo $E_T$ or $p_T > 10$ GeV for PF $E_T$.

The type-II correction for the unclustered energy $U_{\text{meas}}$ is obtained from events without any reconstructed jets, using the correlation between $U_{\text{meas}}$ and the $\vec{q}_T$ of the $Z$ boson measured from the electrons.

As the direction of $\vec{U}_{\text{meas}}$ may differ from the direction of $\vec{q}_T$ due to noise, the underlying event, etc., the parallel component of $\vec{U}_{\text{meas}}$ projected onto the direction of $\vec{q}_T$, $U_{T,\text{meas},||}$, is used for the derivation of the correction. The response of the unclustered energy is then defined as $\langle |U_{T,\text{meas},||}|/q_T \rangle$. The correction factor $U_{\text{scale}}$ so obtained is parametrized as $2.3 + 1.9 \exp(-0.2 U_{T,\text{meas}})$ for Calo $E_T$. For PF $E_T$, $U_{\text{scale}}$ equals 1.4. These values obtained from data correspond well to the MC expectations.

The performance of the type-II corrected $E_T$ is verified by decomposing $\vec{E}_T$ into two components in dijet events. The decomposition is based on the dijet bisector axis, which divides the azimuthal opening angle between the two leading jets in half as illustrated in figure 28. Positive

![Figure 26](image-url). Response for PF $E_T$ versus $\gamma q_T$ for various jet correction thresholds for $\gamma$ candidate events with 1 primary vertex (left) and more than 1 vertex (right).
\( E_{T\parallel} \) points toward the smaller opening angle of the two leading jets, and positive \( E_{T\perp} \) points towards the more central jet (smaller \(|\eta|\)). The distribution of \( E_{T\perp} \) is symmetric for all correction levels, while by definition there is a slight asymmetry in \( E_{T\parallel} \). This is due to the fact that the bisector axis always points towards the opening angle of the leading two jets, while the \( E_T \) tends to point in the opposite direction. The type-I correction introduces a more significant asymmetry in the \( E_{T\parallel} \) distribution, because it produces artificial \( E_T \) in the direction opposite to the dijet opening angle. The type-II correction, however, calibrates the rest of the calorimeter energies, and makes the \( E_{T\parallel} \) distribution nearly symmetric again. This trend may be seen in figure 29, which shows the mean values of \( E_{T\parallel} \) as a function of \( p_T^{\text{avg}} = (p_{T1} + p_{T2})/2 \) for uncorrected, type-I corrected, and type-II corrected Calo \( E_T \) and PF \( E_T \) in events containing at least two jets with \( p_T > 40 \text{GeV} \) and \(|\eta| < 3\).
Figure 28. Kinematic definitions for dijet events.

Figure 29. Mean values of $E_T$ as a function of average $p_T$ of the two leading jets ($p_T^{av}$) in dijet events compared with Monte Carlo simulation (dashed lines) for uncorrected, type-I corrected, and type-II corrected (left) Calo $E_T$ and (right) PF $E_T$. The blue band on the distribution with type-I corrections reflects the uncertainty on the jet energy scale. The red band on the distribution with type-II corrections corresponds to the uncertainties on the jet energy scale and statistical uncertainties due to the size of the $Z \rightarrow e^+ e^-$ sample from which the correction for unclustered energies was derived.

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