

MIT Open Access Articles

The intimate relationship between cavitation and fracture

The MIT Faculty has made this article openly available. *[Please](https://libraries.mit.edu/forms/dspace-oa-articles.html) share* how this access benefits you. Your story matters.

Citation: Raayai-Ardakani, Shabnam et al. "The intimate relationship between cavitation and fracture." Soft Matter 15, 25 (July 2019): 4991–5176 © 2019 Royal Society of Chemistry

As Published: http://dx.doi.org/10.1039/c9sm00570f

Publisher: Royal Society of Chemistry (RSC)

Persistent URL: <https://hdl.handle.net/1721.1/124396>

Version: Final published version: final published article, as it appeared in a journal, conference proceedings, or other formally published context

Terms of use: Creative Commons Attribution [Noncommercial](https://creativecommons.org/licenses/by-nc/3.0/) 3.0 unported license

Soft Matter

PAPER

Cite this:DOI: 10.1039/c9sm00570f

Received 20th March 2019, Accepted 27th April 2019 DOI: 10.1039/c9sm00570f

rsc.li/soft-matter-journal

The intimate relationship between cavitation and fracture†

Shabnam Raayai-Ardakani, D^a Darla Rachelle Earl^a and Tal Cohen D^{*ab}

Nearly three decades ago, the field of mechanics was cautioned of the obscure nature of cavitation processes in soft materials [A. Gent, Cavitation in rubber: a cautionary tale, Rubber Chem. Technol., 1990, 63, 49–53]. Since then, the debate on the mechanisms that drive this failure process is ongoing. Using a high precision volume controlled cavity expansion procedure, this paper reveals the intimate relationship between cavitation and fracture. Combining a Griffith inspired formulation for crack propagation, and a Gent inspired formulation for cavity expansion, we show that despite the apparent complexity of the fracture patterns, the pressure–volume response follows a predictable path. In contrast to available studies, both the model and our experiments are able to track the entire process including the unstable branch, by controlling the volume of the cavity. Moreover, this minimal theoretical framework is able to explain the ambiguity in previous experiments by revealing the presence of metastable states that can lead to first order transitions at onset of fracture. The agreement between the simple theory and all of the experimental results conducted in PDMS samples with shear moduli in the range of 25–246 [kPa] confirms that cavitation and fracture work together in driving the expansion process. Through this study we also determine the fracture energy of PDMS and show its significant dependence on strain stiffening. PAPER

The intimate relationship between cavitation

and that interactionship is the constant of the constant of the constrained and the spectra of the spectra o

When pushed to its extremes, a solid will usually fail by one of two mechanisms; cavitation or fracture. The former refers to the spontaneous growth of pre-existing defects within the body, while the latter is characterized by splitting the material to form new surface area. Fracture is something that we experience often, from the shattering of a window or a cellphone screen and to the splitting of a piece of fruit. Cavitation, on the other hand, is not as mundane, nonetheless it is ubiquitous. Theories of cavitation have been used to explain extreme phenomena that occur over various length scales; from the formation of craters by meteorite impact,^{1,2} volcanic eruptions,^{3,4} underground explosions,^{5–8} and penetration phenomena;^{9,10} to the exposure of seeds in ripening crop,‡ and to morphogenesis processes that occur in crucial stages of embryonic development.11,12 Moreover, cavitation is employed in medical applications to enhance drug delivery, and to treat cancer, $13-15$ it has been indicated as a primary mechanism of damage in traumatic brain injury, $16-18$ and has been shown to provide a

means for probing of local material properties in soft and biological materials.19–23

Although cavitation and fracture have been traditionally considered separately, it is well known that one can lead to the other. In ductile metals, growth and coalescence of voids is commonly accepted as the primary mechanism of fracture. $24-28$ In rubbers and highly deformable materials, however, there is no agreement as to which mechanism is activated at every instance²⁹ and the debate is ongoing.³⁰ On the one hand, an extensive body of literature has been devoted to investigation of cavitation as a purely elastic phenomenon.³¹⁻³⁵ On the other hand, the same phenomenon has been consistently considered in the literature as a fracture process.³⁶⁻⁴¹ In a recent study, Poulain et al.,³⁰ were able to observe the process at high spatial and temporal resolutions and conclude that ''internal damage in soft material should be viewed as a fracture phenomenon''.

While the general debate in the literature revolves around the question: Is it cavitation or fracture?, in this work we show that the two mechanisms are intimately coupled and inseparable. Additionally we show that the fully coupled behaviour can be captured analytically.

A major challenge in experimentally studying the formation of internal cavities/cracks is in controlling the process while clearly capturing the form of the cavity/crack in the bulk. Additionally, these processes are known to be highly sensitive to initial imperfections.⁴¹⁻⁴³ In available studies,^{30,40} neither

 a Department of Civil and Environmental Engineering, MIT,

⁷⁷ Massachusetts Avenue, Cambridge, MA, USA

 b Department of Mechanical Engineering, MIT, 77 Massachusetts Avenue,</sup> Cambridge, MA, USA. E-mail: talco@mit.edu

[†] Electronic supplementary information (ESI) available. See DOI: 10.1039/ c9sm00570f

[‡] See Fig. SI.2.1 in ESI.2.†

Fig. 1 Lateral and bottom views of the expanded cavities/cracks in transparent PDMS samples with various shear moduli. The cavities were filled with polyvinyl siloxane (PVS) to visualize the texture of the fracture surfaces. The background colour is for ease of visualization. A schematic of the experimental method is shown on the top left hand side.

the volume of the cavity nor the applied load have been controlled throughout the process. Hence, formation of the cavity/crack occurs abruptly and available models focus on determining the onset of fracture. Recent advances have been pushing the experimental capability into high speed fracture phenomena⁴⁴ and employing phase separation for identification of the crack initiation.⁴⁵

In the present work, by controlling the volume of the cavity/ crack as it expands within a transparent PDMS sample, we are able to obtain precise measurements of pressure (p) versus volume (V) throughout the process not only at the initiation of the crack but also throughout the crack propagation. This is achieved by our custom designed experimental setup, 22 which functions as a volume controlled syringe pump (see schematic illustration in Fig. 1). We fabricate cuboid PDMS samples of various shear moduli, in the range of 25–246 [kPa], as achieved by varying the base to cross-linking agent ratios, and we inflate a cavity/crack at the tip of the needle at a constant volumetric rate.§ The fabrication protocol and experimental procedure are detailed in ESI.1.† The shear moduli of the samples were measured using the method discussed in our previous work.²² For samples exhibiting strain stiffening, we fit our experimental results to a Gent model.⁴⁶

Even if viewed solely as a fracture process, the expansion behaviour observed in our experiments, is extremely complex. To demonstrate this, after performing the volume controlled experiment to a predefined volume, we drain the injected fluid and replace it with a fast curing polymeric material (polyvinyl siloxane) and 'freeze' the shape of our cavities/cracks as described in ESI.1.†

Images of representative cavities/cracks that have been 'frozen' using this method are shown in Fig. 1 for samples of

different shear moduli (μ) . It is apparent that the intricate patterns that form vary considerably between the specimens and even within the same cavity/crack, they can have several protrusions, and regions of different surface roughness. These differences may be attributed to the presence of initial imperfections created in the injection process. Nonetheless, if considering only the aspect ratio of the cavities/cracks, it is observed that stiffer specimens take forms of higher aspect ratio (additional images can be found in ESI.3,† Fig. SI.3.1–SI.3.5).

Despite the intricacy observed in Fig. 1, the pressure–volume response exhibits astonishing order. In Fig. 2 we show representative results for three different values of the shear moduli (additional curves can be found in ESI.4,† Fig. SI.4.1). The pressure is shown as a function of the effective stretch, $\lambda = (V/V_0)^{1/3} = a_0/A_0$, where V_0 is the volume of the initial defect, A_0 is the effective radius of the initial defect, and a_0 is the effective radius of the cavity/crack (see Fig. 3a for illustration, and the ESI.1,† for experimental details). This effective stretch provides a meaningful dimensionless measure for the cavity expansion that is independent of the initial volume. The response can be divided into three stages. At the initial stage of inflation, all of the experimental curves follow a similar path, then departure from that path is apparent at a peak value, but does not occur at the same point for each test. Nonetheless, as expansion progresses, the curves seem to resume a shared path. In this process the peak value of cavity pressure represents the stability limit. If the volume is not constrained, any pressure above this peak value would result in complete rupture of the specimen. As observed in Fig. 2, for stiffer samples the peak value increases and is followed by a steeper decline. Open Commons Articles. Published on 01 May 2019. This are not are not

Although the experimental observations indicate that this process is highly sensitive to initial imperfections, the conforming of the experimental curves to similar trends, in all but an intermediate range, suggests that a theoretical model can potentially aid in determining which mechanism drives this process (cavitation, fracture, or both).

Prediction of the expansion path

Complementary to the previous analyses of fracture initiation, $37,41,47$ here we assume that the deformation of the sample can be divided into two distinct zones that border at an effective radius that is denoted by A in the undeformed configuration and by a in the deformed configuration (Fig. 3a). The deformation in the external region is assumed to be purely elastic and spherically symmetric. Limiting our discussion to incompressible materials, the kinematics of the deformation in this region are fully defined as a function of the circumferential stretch at the boundary $\lambda_a = a/A$. Considering bodies of finite dimension we also write the circumferential stretch at the external boundary as $\lambda_b = b/B$ where the effective external radius of the body is B in the undeformed and b in the deformed configuration (it will be shown later that the dimension of the body does not effect the response). By integrating the elastic

[§] Note that the diameter of the needle is chosen to be sufficiently large so that surface tension effects can be neglected. The rate of inflation is sufficiently slow such that the process is quasi-static and no rate dependence is observed.

Fig. 2 Normalized pressure, measured inside cavities of PDMS samples with different shear moduli shown as a function of the effective stretch. Experimental curves are shown by the thin dotted lines. At least three tests were conducted for each material. The solid and dashed-dotted lines represent the predicted response using the present model, with the dashed-dotted lines representing metastable paths.

Fig. 3 (a) Illustration of theoretical spherically symmetric expansion field. The initial and current effective radius of the inflated cavity/crack is denoted by A_0 and a_0 , respectively. Similarly, the external radius is denoted by B and b and the boundary between the fractured region and the purely elastic region is denoted by A and a, respectively. (b) Phase diagram of the cavity expansion process shown for the different levels of material stiffening and calculated for $B/A₀$ = 15. The solid and dashed-dotted lines represent the predicted response using the present model, with the dashed-dotted lines representing metastable paths. (c) Fraction of fracture energy throughout the expansion process shown for different ratios $B/A₀$ and for different levels of material stiffening.

energy density over the volume of the body, the total elastic energy can be written, after some algebra, as in ref. 22

$$
U_{\rm E} = 4\pi\mu A^3 (1 - \lambda_{\rm a}^3) \int_{\lambda_{\rm a}}^{\lambda_{\rm b}} \frac{\bar{W}(\lambda_{\theta})}{(1 - \lambda_{\theta}^3)^2} \lambda_{\theta}^2 d\lambda_{\theta} \tag{1}
$$

where, for the considered deformation, the elastic energy density (per unit volume) of an arbitrary hyperelastic material $W = \mu \bar{W}(\lambda_{\theta})$ depends only on the shear modulus (μ) , and the local value of the circumferential stretch ($\lambda_{\theta} = r/R$), where r and R represent the radial coordinate in the current and reference configurations, respectively (Fig. 3a).

The internal region $R \in [A_0, A]$ is assumed to undergo a fracture process. While available theories^{37,38,48} consider cracks of specific shapes (for example penny shape), here by assuming an effective spherical region undergoing the fracture process, we eliminate the need for any assumption on the shape or number of protrusions present at the cavity surface. To estimate the energy invested in creating surface area within the fractured region, we employ an augmented Griffith⁴⁹ type approach to account for the spherical nature of the deformation and the effect of strain stiffening

$$
U_{\rm F} = 2\pi (A^2 - A_0^2) G_{\rm c} f(\lambda_{\rm a}). \tag{2}
$$

Here the geometric multiplier $2\pi(A^2 - A_0^2)$ provides a measure for the affected surface area, and G_c is an effective measure of the fracture energy per unit area. Note that G_c cannot be directly compared to the reported values in the literature; since the crack is free to take any form, it does not correspond to a predefined unit area. Here, we extend this energy based analysis not only to determine the point of fracture initiation but also to predict the pressure response during the propagation of the crack. This extends the approach used in ref. 37, 41 and 47, by controlling the cavity size to access the unstable branch. To account for the possible influence of strain stiffening on the energetic cost of advancing the crack (as it has also been previously discussed 41 , we include an additional (dimensionless) function $f(\lambda_a)$, which will be discussed later in further detail.

The total energy invested in the expansion process is the sum of the two energies $U = U_E + U_F$ and takes the dimensionless form

$$
\frac{U}{2\pi\mu A_0^3} = \left(\frac{A}{A_0}\right)^3 g(\lambda_a, \lambda_b) + \varphi \left(\left(\frac{A}{A_0}\right)^2 - 1\right) f(\lambda_a) \tag{3}
$$

where $\varphi = G_c/(\mu A_0)$ is a dimensionless measure of fracture energy, and

$$
g(\lambda_a, \lambda_b) = 2(1 - \lambda_a^3) \int_{\lambda_a}^{\lambda_b} \frac{\bar{W}(\lambda_\theta)}{(1 - \lambda_\theta^3)^2} \lambda_\theta^2 d\lambda_\theta \tag{4}
$$

Note that due to incompressibility, for a given imposed expansion a_0 , the stretches λ_a and λ_b depend on the initial dimensions of the body A_0 , B , and on the location of the boundary $A \in [A_0 \ B]$. It is expected that for a given imposed expansion a_0 , the equilibrium location of the boundary (A) will minimize the total energy, such that $\partial U/\partial A$ = 0 and $\partial^2 U/\partial A^2 > 0.$ Additional extrema may appear at the physical boundaries. An extramum at $A = A_0$ corresponds to the purely elastic solution, while an extramum at $A = B$ corresponds to complete failure.

Assuming that the fractured material is no longer capable of resisting the deformation, the cavity pressure can be estimated by considering only the elastic region and can be obtained by the derivative $p = -\partial U_{\rm E}/\partial V$, which can be simplified to the form

$$
\frac{p}{\mu} = \int_{\lambda_a}^{\lambda_b} \frac{\bar{W}'(\lambda_\theta)}{1 - \lambda_\theta^3} d\lambda_\theta \tag{5}
$$

where the prime denotes differentiation. An alternative derivation of the above formula can be achieved by integration of the radial equation of motion.²²

Note that in contrast to the above approach, earlier theoretical models have been limited to determining the onset of fracture.40,41,47,50 Here we solve for the entire process by controlling the volume of the cavity.

To obtain a prediction of the expansion process, it remains to choose a constitutive relation. A natural choice is the neo-Hookean response, for which $\bar{W} = (I_1 - 3)/2$ where for the present deformation, the first invariant of the left Cauchy– Green deformation tensor is $I_1 = 2\lambda_\theta^2 + \lambda_\theta^{-4}$. To account for strain stiffening that can appear due to limiting chain extensibility, this relation can be extended using the Gent model 46 to write $\bar{W} = (J_{\rm m}/2) \ln(1 - (I_1 - 3)/J_{\rm m})$. Locking of the polymer network appears as a singularity when $I_1 - 3 = J_m$. At the limit $J_m \rightarrow \infty$, the Gent model reduces to the neo-Hookean model.

With the above formulation, for a given elastic response, prediction of the expansion process depends only on φ . As a first step we consider the neo-Hookean response, which is commonly adopted to model PDMS. For simplicity we choose $f(\lambda_a) = 1$ in (3). In all figures (*i.e.* Fig. 2 and Fig. SI.4.1 in ESI.4†) the neo-Hookean prediction is represented by the black solid and dashed-dotted curves. Unless indicated otherwise, all of the results have been derived for samples with $B/A_0 = 15$, as in the experiments.

It is already worth noting that all of the theoretical predictions have been made with a single value of the dimensionless measure of surface energy $\varphi = 1$.

Comparing between the experimental curves and the neo-Hookean prediction for samples with $\mu \leq 48$ [kPa] (see Fig. 2 and Fig. SI.4.1 in ESI.4†) reveals a notable agreement. Recall that no fitting parameters are used (other than setting $\varphi = 1$). Focusing on the initial range of inflation (before the peak pressure) it is apparent that as the shear modulus increases, the experimental curves exhibit stiffening behaviour that is not captured by the neo-Hookean model, and that the increases in the peak pressures are followed by steeper gradients. The Gent model (as shown by the coloured curves) is able to capture the stiffening response within the elastic region and indicates that as the shear modulus increases (or equivalently the crosslinking increases) the elastic network can endure less stretching before locking (as indicated by the decreasing values of J_m). The good agreement between the experimental curves and the theoretical predictions in early stages of inflation before arriving at the peak pressure, confirms that within this range response is purely elastic. (Within this range the minimum energy solution is at the boundary $A = A_0$). Paper

The total energy invested in the expansion process is the

same of the three steps are the three steps are the common of the three steps are made with a single value of the dimensiones

In the three dimensiones ar

To account for the fact that stiffening increases the energetic cost of fracturing as previously discussed, $37,41$ we have included the function $f(\lambda_a)$ in (3). Based on the experimental results, at the neo-Hookean limit $J_m \rightarrow \infty$ this function should take the value $f(\lambda_a) = 1$, while at the other limit, if the locking stretch is approached $(J_m \rightarrow I_1 - 3)$ the energy required to fracture becomes singular. Although different functional forms can be employed, in view of the Gent model, a natural choice is

$$
\hat{f}(I_1) = \exp\left(\frac{J_m}{J_m - I_1 + 3} - 1\right)
$$
 (6)

which, for generality, is written here in terms of the first invariant.¶ For the present deformation pattern, (6) can be specialized in terms of the circumferential stretch at the boundary, to write $f(\lambda_a) = \hat{f}(2\lambda_a^2 + \lambda_a^{-4})$. Note that J_m in the above equation is found from the elastic portion of the experimental curves.

Now, without any additional fitting parameters, we apply the above formulation along with (6) to the entire range of expansion. As observed, this simple model is able to capture the response over the entire range of shear moduli (Fig. SI.4.1 in ESI.4†). Perhaps the most remarkable result is that it brings further insight into the physics of the problem by giving rise to first order transitions between metastable states (shown by the dashed-dotted coloured lines). Note that the metastable path for fracture corresponds to a local minimum in the energy U , that appears while the global minimum corresponds to the purely elastic path with $A = A_0$. At a critical expansion, the purely elastic solution is no longer a global minimum and fracture initiates $(A > A_0)$ (representative curves for the energy landscape are shown in ESI.5,† Fig. SI.5.1). As observed, these

[¶] This particular functional form has been found through a trial and error procedure and fits well to all of our experimental data.

transitions become more pronounced for stiffer materials and explain the sudden drops in pressure. Since a first order transition requires excess energy, the onset of fracture in stiffer materials varies significantly among the different tests. Nonetheless, the curves eventually unite and resume similar trends.

Cavitation or fracture?

With the new understanding of this phenomenon, we can now return to answer the original question: Is it cavitation or fracture? To do so, we first examine the propagation of the fracture front (A) throughout the expansion process on a phase diagram, as shown in Fig. 3b. In this plane, travelling in the horizontal direction corresponds to purely elastic expansion, while processes that involve only fracture without cavity expansion travel in the vertical direction. As observed, initially all curves travel along the horizontal line in a purely elastic process with $A = A_0$. At a critical expansion (λ_c) , departure from the horizontal path is observed and becomes more abrupt as stiffening increases. Eventually all curves follow a path that is driven by the simultaneous action of both mechanisms. For materials with J_m = 3.8 the metastable path departs earlier (*i.e.* $\lambda < \lambda_c$), a first order transition is then observed between the purely elastic expansion and a finitely fractured state. The transition corresponds to fracturing without any elastic effects, but then cavity expansion is resumed. Overall, throughout the process, expansion can abruptly switch between different mechanisms. Soft Matter Werelation account one pronounced for stiffer macerials and with experiments in all ones. Here, for the POMS samples used contain the substitute Walter and the substitute of the substitute of the substitute of

Now that it is clear that both mechanisms can be simultaneously activated, another means for determining which mechanism is more dominant, is by considering the fraction of energy invested in each. In Fig. 3c we plot the fraction of energy that has been invested in fracturing (for $J_m = 3.8$ and $J_{\rm m} \rightarrow \infty$). We find that within a large range of expansions $\lambda < 4$ the fraction of energy invested in fracture does not exceed 60%. It is only when the effective fracture radius approaches the external boundary of the body that fracture engulfs, as observed for the curves with $B/A_0 = 15$.

Often, the debate between cavitation and fracture revolves around the fact that fracture is associated with an initial length scale^{41,47} (*i.e.* the size of an initial defect or a notch), while cavitation theories exclude that information by considering the limit in which the initial defect is sufficiently small compared to the size of the body. In this case $B/A_0 \rightarrow \infty$, or equivalently $\lambda_{\rm b}$ = 1 (as seen from the incompressibility constraint). As shown in ESI.5,† Fig. SI5.2, the present model is practically insensitive to the ratio B/A_0 within a large range of expansion ratios. Hence, the formulation in eqn (1) – (5) can be recast in an even simpler form by substituting $\lambda_b = 1$.

Finally, we recall that all of the theoretical predictions have been calculated using $\varphi = 1$. This is a surprising result given the observed sensitivity to the shear modulus (μ) and that the value of φ directly determines both the point of departure from the purely elastic response and the trend of the curve at large strains. Nonetheless, $\varphi = 1$ is shown to provide good agreement with experiments in all cases. Hence, for the PDMS samples used in this work $G_c = \mu A_0$ is proportional to the shear modulus. With $A_0 \approx 1$ [mm] we find that G_c is in the range of 25–250 [J m⁻¹]. Since in the present formulation G_c is calculated per effective unit area $S = 2\pi(A^2 - A_0^2)$, which can be thought of as the minimal surface area needed to advance the fracture front from A_0 to A, a geometric correction should be included in comparing the present value of G_c with values measured *via* alternative methods.

The energy release rate (per effective unit area) is obtained by directly differentiating (1) with $\lambda_{\rm b} = 1$, which takes the simple form $\dot{U}_{\rm E} = -\partial U_{\rm E}/\partial S = \mu A \bar{W}(\lambda_{\rm a})$. To obtain the critical value at onset of fracture (when $A = A_0$), we substitute in this relation the critical stretch λ_c , as determined from the energy minimization. It is observed from our experiments (Fig. 2 and more in ESI.4,† Fig. SI.4.1), that at the neo-Hookean limit $\lambda_c \approx 1.55$ which leads to $U_E = \mu A_0 (= G_c)$. For increasing material stiffening, fracturing requires significantly higher levels of U_E , as shown in ESI.5, \dagger Fig. SI.5.3.

Several studies have considered the relationship between the critical fracture energy release rate (G_c) and the shear modulus (μ) . The classical model of Lake and Thomas⁵¹ considers chain scission as the dominant mechanism of fracture and predicts that critical energy release rate follows a scaling of the form $G_{\rm c}\varpropto\mu^{-1/2}.$ Recently, Mao and Anand 52 suggested that if fracture occurs by both cross-link stretching and scission, the scaling is $G_c \propto \mu^{1/2}$. Based on recent experiments and in accord with the classical models, Hutchens et $al.^{40}$ proposed a phenomenological power law model in the form $G_c \propto \mu^n$. They report a range of the powers $n \approx 0.08-3$ for a few representative polymer systems. Noting the variations in the power n in the previous literature, here, for PDMS samples we obtain a linear dependence $(n = 1)$. Another key point to highlight is that our experiments clearly demonstrate a strong dependence of the critical fracture energy release rate on the stiffening behaviour of the material (J_m) .

Conclusion

To summarize, we have shown that in soft materials cavitation and fracture co-operate to drive failure. This observation is facilitated by a controlled experimental procedure of cavity expansion, that allows us to both examine the cavity/crack patterns, and to measure the pressure–volume response with high precision. These tests are conducted on a family of PDMS samples with shear moduli in the range of 25–246 [kPa]. A simple theory based on energetic arguments is shown to agree with all of the experiments while revealing that occurrence of abrupt pressure drops is a manifestation of a first order transition between metastable states, which may arise when material stiffening is significant. In exposing the existence of metastable states, this study explains the source of the significant dependence on initial imperfections, even in the absence of surface tension effects. Additionally, an effective measure of the critical fracture energy release rate is directly found from these experiments and is shown to be linearly proportional to the shear modulus, while exhibiting significant sensitivity to strain stiffening, which appears in these materials due to locking of the polymer chains at large stretches.

Finally, while elucidating the basic mechanisms involved in formation of cavities/cracks in soft materials, the present work gives rise to a multitude of additional open questions. A natural next step is to extend this work to additional soft materials, to determine the microscopic mechanisms that lead to the dependence of fracture energy on stiffening of the polymer network, and to include surface tension effects that may become significant for smaller initial defects. It remains to be determined if similar interactions between cavitation and fracture appear in stiff materials, such as ductile metals. Reminiscent of viscous fingering phenomena, our fracture patterns are characterized by various length scales and surface roughness. Additional work is needed to explain and perhaps, control, the formation of these elusive patterns. Finally, it is worth noting that the theoretical framework presented here, applies equivalently to situations in which tension is applied remotely. Although we have not been able to confirm experimentally that remote tension will result in similar expansion processes, nature has provided us with some examples (see ESI.2,† Fig. SI.2.1). Paper

Open Karticles, which exhibiting significant sensitively 0 2 A Navis and C. M. Nebon, Sendo. Cell Dev. Biol. 2015

Occurs Articles. Which appears in these naturalis due to 2019. The subset are not the subset are als

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

The authors wish to acknowledge the support of the Army Research Office and Dr Ralph A. Anthenien, Program Manager.

References

- 1 J. N. Goodier, On the mechanics of indentation and cratering in solid targets of strain-hardening metal by impact of hard and soft spheres, Stanford Research Institute Menlo Park, CA, 1964.
- 2 H. Melosh and G. Collins, Nature, 2005, 434, 157.
- 3 R. Sulpizio and S. Massaro, Front. Earth Sci., 2017, 5, 18.
- 4 M. Davydov, V. Kedrinskii, A. Chernov and K. Takayama, J. Appl. Mech. Tech. Phys., 2005, 46, 208–215.
- 5 P. Chadwick, A. D. Cox and H. G. Hopkins, Phil. Trans. R. Soc. Lond. A, 1964, 256, 235–300.
- 6 C. F. Chyba, P. J. Thomas and K. J. Zahnle, Nature, 1993, 361, 40.
- 7 T. Cohen, R. Masri and D. Durban, J. Appl. Mech., 2010, 77, 041009.
- 8 T. Cohen and D. Durban, J. Appl. Mech., 2013, 80, 011017.
- 9 M. Forrestal and D. Tzou, Int. J. Solids Struct., 1997, 34, 4127–4146.
- 10 R. Sobeski and G. Urgessa, Int. J. Prot. Struct., 2015, 6, 43–64.
- 11 E. Hoijman, D. Rubbini, J. Colombelli and B. Alsina, Nat. Commun., 2015, 6, 7355.
- 12 A. Navis and C. M. Nelson, Semin. Cell Dev. Biol., 2016, 139–147.
- 13 C. C. Coussios and R. A. Roy, Annu. Rev. Fluid Mech., 2008, 40, 395–420.
- 14 A. K. Wood and C. M. Sehgal, Ultrasound Med. Biol., 2015, 41, 905–928.
- 15 E. P. Stride and C. C. Coussios, Proc. Inst. Mech. Eng., Part H, 2010, 224, 171–191.
- 16 T. El Sayed, A. Mota, F. Fraternali and M. Ortiz, Comput. Methods Appl. Mech. Eng., 2008, 197, 4692–4701.
- 17 R. S. Salzar, D. Treichler, A. Wardlaw, G. Weiss and J. Goeller, J. Neurotrauma, 2017, 34, 1589–1602.
- 18 J. Goeller, A. Wardlaw, D. Treichler, J. O'Bruba and G. Weiss, J. Neurotrauma, 2012, 29, 1970–1981.
- 19 J. A. Zimberlin, N. Sanabria-DeLong, G. N. Tew and A. J. Crosby, Soft Matter, 2007, 3, 763–767.
- 20 A. J. Crosby and J. J. McManus, Phys. Today, 2011, 64, 62–63.
- 21 T. Cohen and A. Molinari, Int. J. Solids Struct., 2015, 69, 544–552.
- 22 S. Raayai-Ardakani, Z. Chen, D. R. Earl and T. Cohen, Soft Matter, 2019, 15, 381–392.
- 23 J. B. Estrada, C. Barajas, D. L. Henann, E. Johnsen and C. Franck, J. Mech. Phys. Solids, 2018, 112, 291–317.
- 24 H. Rogers, Trans. Metall. Soc. AIME, 1960, 218, 498–506.
- 25 F. A. McClintock, J. Appl. Mech., 1968, 35, 363–371.
- 26 V. Tvergaard, J. Mech. Phys. Solids, 1982, 30, 265–286.
- 27 M. Ashby, F. Blunt and M. Bannister, Acta Metall., 1989, 37, 1847–1857.
- 28 V. Tvergaard and A. Needleman, Acta Metall., 1984, 32, 157–169.
- 29 A. Gent, Rubber Chem. Technol., 1990, 63, 49–53.
- 30 X. Poulain, V. Lefèvre, O. Lopez-Pamies and K. Ravi-Chandar, Int. J. Fract., 2017, 205, 1–21.
- 31 C. Horgan and D. Polignone, Appl. Mech. Rev., 1995, 48, 471–485.
- 32 J. M. Ball, Philos. Trans. R. Soc., A, 1982, 306, 557–611.
- 33 R. Stringfellow and R. Abeyaratne, Mater. Sci. Eng., A, 1989, 112, 127–131.
- 34 H. Hang-Sheng and R. Abeyaratne, J. Mech. Phys. Solids, 1992, 40, 571–592.
- 35 A. Gent and P. Lindley, Proc. R. Soc. London, Ser. A, 1959, 249, 195–205.
- 36 G. H. Lindsey, J. Appl. Phys., 1967, 38, 4843–4852.
- 37 Y.-Y. Lin and C.-Y. Hui, Int. J. Fract., 2004, 126, 205–221.
- 38 V. Lefèvre, K. Ravi-Chandar and O. Lopez-Pamies, Int. J. Fract., 2015, 192, 1–23.
- 39 S. Kundu and A. J. Crosby, Soft Matter, 2009, 5, 3963–3968.
- 40 S. B. Hutchens, S. Fakhouri and A. J. Crosby, Soft Matter, 2016, 12, 2557–2566.
- 41 A. Gent and C. Wang, J. Mater. Sci., 1991, 26, 3392–3395.
- 42 A. Gent and D. Tompkins, J. Polym. Sci., Part A-2, 1969, 7, 1483–1487.
- 43 O. Lopez-Pamies, M. I. Idiart and T. Nakamura, J. Mech. Phys. Solids, 2011, 59, 1464–1487.
- 44 M. P. Milner and S. B. Hutchens, Extreme Mech. Lett., 2019, 28, 69–75.
- 45 J. Y. Kim, Z. Liu, B. M. Weon, C.-Y. Hui, E. R. Dufresne and R. W. Style, 2018, arXiv preprint, arXiv:1811.00841.
- 46 A. Gent, Rubber Chem. Technol., 1996, 69, 59–61.
- 47 M. L. Williams and R. A. Schapery, Int. J. Fract. Mech., 1965, 1, 64–72.
- 48 J. Kang, C. Wang and S. Cai, Soft Matter, 2017, 13, 6372–6376.
- 49 A. A. Griffith and M. Eng, Philos. Trans. R. Soc., A, 1921, 221, 163–198.
- 50 M. Williams and R. Schapery, Int. J. Fract. Mech., 1965, 1, 64–72.
- 51 G. J. Lake and A. G. Thomas, Proc. R. Soc. London, Ser. A, 1967, 300, 108–119.
- 52 Y. Mao and L. Anand, J. Appl. Mech., 2018, 85, 081008.