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Outdoor Thermal Comfort Autonomy: Performance Metrics for Climate-Conscious Urban Design

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Abstract

Thermal comfort in the built environment is a crucial factor impacting health, well-being, and productivity of urban dwellers. Accordingly, comprehensive analyses are needed to ensure that acceptable criteria of thermal comfort are defined and met in urban environments. The main objective of this study is to define such performance metrics and quality measures of outdoor thermal comfort (OTC), aiming to inform climate-conscious urban design. This article first discusses the motivations for introducing comprehensive thermal comfort metrics, addressing the shortcomings of conventional OTC evaluations that neglect the temporal or spatial variability of OTC. It then introduces four performance metrics, which collectively inform urban planners and designers on the performance of outdoor space with regards to thermal comfort. These metrics build upon the concept of “autonomy” previously introduced for indoor spaces and are extended to include the unique characteristics of outdoor thermal comfort. Second, we discuss the capability of these metrics given the limitations of modeling tools available for urban microclimate analysis, and evaluate the critical factors for an accurate evaluation of Outdoor Thermal Comfort Autonomy (OTCA). We observe that the spatial distribution of airflow at the pedestrian height is critical for OTCA calculation, while the consideration of realistic surface heating depends on the urban density. Lastly, we present an example of employing weather clustering methods such that OTC performance metrics are achieved on an annual basis in a comprehensive yet efficient way. By discussing the capability and the limitations of these metrics we aim to promote climate-conscious design using metrics that are tangible and accessible to non-simulation experts.

Keywords– Outdoor thermal comfort, performance metrics, comfort autonomy, urban design, climate-conscious solutions

1 Introduction

Urban livability, a sum of elements that contribute to the quality of life in cities, is greatly impacted by environmental factors such as water quality, air quality, and climate. Among these, the consideration of

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32 thermal comfort is gaining top priority as it directly impacts productivity and cognitive performance [65],
33 well-being, and health of urban dwellers. Additionally, given the increased frequency and duration of extreme
34 heat events [42], such considerations move beyond the prevention of “discomfort” and shift into concerns
35 regarding “stress”. Heat stress during extreme weather events is a grave health concern in cities, as mortality
36 is strongly associated with temperature metrics during heatwaves [5, 26, 62], specifically targeting the aging
37 and vulnerable populations with health hazards that are hard to quantify. In summer 2015 alone, over 11,000
38 people were hospitalized due to hot weather in Japan, with greater concentrations in such urbanized regions
39 as the Greater Tokyo Area [61], while a heat wave in southern India led to over 1,500 deaths [49]. Such global
40 concerns regarding thermal comfort and heat stress call for comprehensive and accurate analyses, aiming to
41 predict and reduce the adverse effects of heat events in future cities and further enhancing city livability.

42 Although of high importance, Outdoor thermal comfort (OTC) is a notoriously difficult microclimate pa-
43 rameter to evaluate [20, 24, 50, 60], as it involves a combination of various environmental factors, the
44 physiological thermoregulation mechanisms of the human body, and subjective psychological perceptions
45 as well as cultural and climatic backgrounds [8, 20]. Therefore, although thermal comfort is regarded as
46 a critical factor in affecting human health in urban areas, our understanding of OTC compared to other
47 microclimate parameters (such as urban airflow and air temperature) is rather limited. The early studies
48 of thermal comfort involved evaluating indoor spaces [11, 12, 38] and widely assumed that indoor thermal
49 comfort theory generalizes to outdoor settings [55]. However, compared to indoor spaces, there is a lack
50 of thermal boundary in the outdoor environments, exposure to the direct radiation is intensified, and high
51 variability of wind speed is observed. These factors result in great deviations from the thermal comfort
52 neutrality, which further leads to heat stress and makes the thermal comfort analysis intricate. Additionally,
53 due to the predominantly transient behavior of pedestrians in outdoor environments and a vast range of use
54 for outdoor spaces, the physiological and psychological states of each individual become increasingly more
55 complex and important. To address such complexities, the detailed analyses in outdoor urban environments
56 from various perspectives have been proposed [2, 10, 29, 32, 55] and the body of knowledge has grown im-
57 mensely over the last two decades, contributing to our understanding of outdoor thermal comfort. Using
58 various methods ranging from experimental measurements, survey campaigns, and numerical evaluations,
59 we have learned that:

- 60 (a) urban form, size, and configuration have significant effects on outdoor thermal comfort [2, 3, 22, 23,
61 57, 59];
- 62 (b) urban vegetation and trees can mitigate thermal stress in hot climates through modifying radiative
63 and evaporative cooling, although the pedestrian-level wind speed is reduced [3, 31, 41, 52, 58];
- 64 (c) the microscale variation in urban heating is significantly important in determining the local effects of
65 comfort and health, and therefore the spatial distribution of thermal comfort, i.e. the location of cold
66 and hot spots, should not be neglected for evaluating thermal stress [22, 34];
- 67 (d) regulatory physiological processes of individuals can affect the relative importance of meteorological
68 parameters, which makes thermal comfort variable for different individuals [19, 60]; and lastly,
- 69 (e) purely physiological or environmental approaches are not fully equipped for characterizing comfort
70 conditions outdoors, and an understanding of the dynamic “human parameter” (including the psycho-

71 logical states, cultural and climatic backgrounds, activities, and expectations) is necessary in designing
72 spaces for public use [8, 39].

73 In addition to addressing the fundamental and pivotal research questions regarding OTC, there has been
74 a quest for defining the most suitable metric that describes the multi-faceted characteristics of thermal
75 comfort. Accordingly, several indices are defined and implemented. The most common indices used for
76 outdoor spaces include: the index of thermal stress (ITS), which represents the ratio between the rate of
77 sweat necessary to maintain the thermal equilibrium to the cooling efficiency of the body based on the
78 microclimate and clothing characteristics[16]; the predicted mean vote (PMV) based on the Fanger comfort
79 model [13], which is an empirical index applicable for field measurements of thermal comfort or indoor
80 analysis; physiologically equivalent temperature (PET), which is “the air temperature at which, in a typical
81 indoor setting (without wind and solar radiation), the heat budget of the human body is balanced with the
82 same core and skin temperature as under the complex outdoor conditions to be assessed” [19]; Standard
83 Effective Temperature (SET), which is an outdoor adaptation of an indoor index based on the effective
84 temperature [15] by considering the mean radiant temperature [45], and Universal Thermal Climate Index
85 (UTCI) based on the multi-node dynamic thermo-physiological UTCI-Fiala model [14] that defines thermal
86 effects on the whole human body.

87 While thermal comfort indices vary significantly based on the studied parameters and their level of detail,
88 they all aim to comprehensively describe thermal comfort in terms of the contributing factors, and have
89 been widely used to report OTC for various time of the day, different locations, and specific target groups.
90 However, regardless of the thermal comfort metric used, comprehensive “quality measures” for urban design
91 performance with respect to outdoor thermal comfort have not yet been discussed. What are the acceptable
92 or desirable OTC criteria for a given site or a proposed design? And how do people respond to an undesirable
93 OTC? The answer indeed depends on the specific characteristics of each site and requires vigorous research
94 investment to address the “human factor”.

95 In indoor building design, a range of performance metrics exists that can be very specific to a parameter
96 of interest (such as acoustics or daylighting) or general in evaluating the building performance (including
97 sustainability or green measures). For instance, the concept of “autonomy” has been used, which indicates
98 the ability of a space in using passive and available environmental or design resources as opposed to pro-
99 viding active measures for achieving desirable conditions. Specific examples include Daylight Autonomy,
100 which was introduced by Reinhart et al. [47] and has been widely used for assessing the illumination in an
101 indoor design on an annual basis, and Visual Comfort Autonomy [25] which relates the visual comfort of
102 occupants to daylight glare and light adequacy. For the assessment of thermal comfort, a few studies have
103 also discussed performance metrics for indoor environments. Thermal Autonomy was introduced by Levitt
104 et al. [30] such that thermal comfort and energy consumption of buildings are assessed from the architectural
105 perspectives and not the mechanical systems, and Zomorodian and Tahsildoost [66] assessed the effects of
106 window properties in classrooms by employing long-term spatial comfort metrics. Carlucci and Pagliano
107 [7] further reviewed the indices for the long-term evaluation of the general thermal comfort conditions in
108 buildings, and concluded that all the current indices are mainly “single values, i.e. representing one single
109 numerical value summarizing the variety of comfort conditions over certain period of time”, and therefore
110 neglecting the spatial variability of thermal comfort in the built environment that is needed for informing

111 urban design. For outdoor spaces, all together, such performance metrics are lacking. Regarding OTC, while
 112 there are detailed description of the strengths and shortcomings of each thermal comfort index at various
 113 times and locations, it appears that there are limited efforts on prescribing the collective information that
 114 should be delivered to the architects, planners, and decision makers, such that the performance of an outdoor
 115 space with regards to thermal comfort is fully assessed.

116 This gap in the literature motivates the present study. We aim to introduce and define performance metrics
 117 that capture the site-specific and dynamic interaction between buildings and the surrounding climate on
 118 an annual basis. To do so, we identify the following characteristics that, regardless of the index used for
 119 describing the OTC, should be included in any analysis before it can effectively assess and inform the urban
 120 design strategies:

- 121 (a) consideration of the **temporal variabilities**: yearly analysis of thermal comfort with (sub)hourly
 122 resolution for the occupied hours,
- 123 (b) consideration of the **spatial variabilities**: spatial distribution of thermal comfort that identifies the
 124 “hot/cold spots” and indicates zones of persistent thermal discomfort,
- 125 (c) determination of **performance**: percentage of time that an outdoor space meets the desired thermal
 126 comfort range, and
- 127 (d) determination of **heat stress**: extent of deviation from the desired thermal comfort range that specifies
 128 the thermal stress.

129 Here, we aim to define performance metrics for OTC that consider these characteristics in a comprehensive
 130 way, such that they can then be used for comparative studies to guide urban design or to deepen our
 131 understanding on OTC in various meteorological conditions.

132 Figure 1 graphically overviews the present study, identifying the following objectives: 1. defining performance
 133 metrics (such as Outdoor Thermal Comfort Autonomy) that cover the holistic characteristic of outdoor
 134 thermal comfort (Sec. 2), 2. demonstrating the calculation of performance metrics using a numerical
 135 three-dimensional model of OTC and discussing the critical factors contributing to the accuracy of these
 136 metrics (Sec. 3), and 3. demonstrating a methodology of utilizing such performance metrics for obtaining a
 137 comprehensive yet efficient evaluation of OTC using weather clustering methods (Sec. 4).

138 2 Performance Metrics for Climate-Conscious Urban Design

139 This section describes the performance metrics for evaluating OTC in urban design, such that a) they
 140 represent comprehensive information in terms of the consideration of temporal and spatial variation of OTC,
 141 b) are easily comprehensible and applicable (described in terms of temperature and percentage metrics), and
 142 c) represent such critical factors as thermal stress that are relevant to OTC.

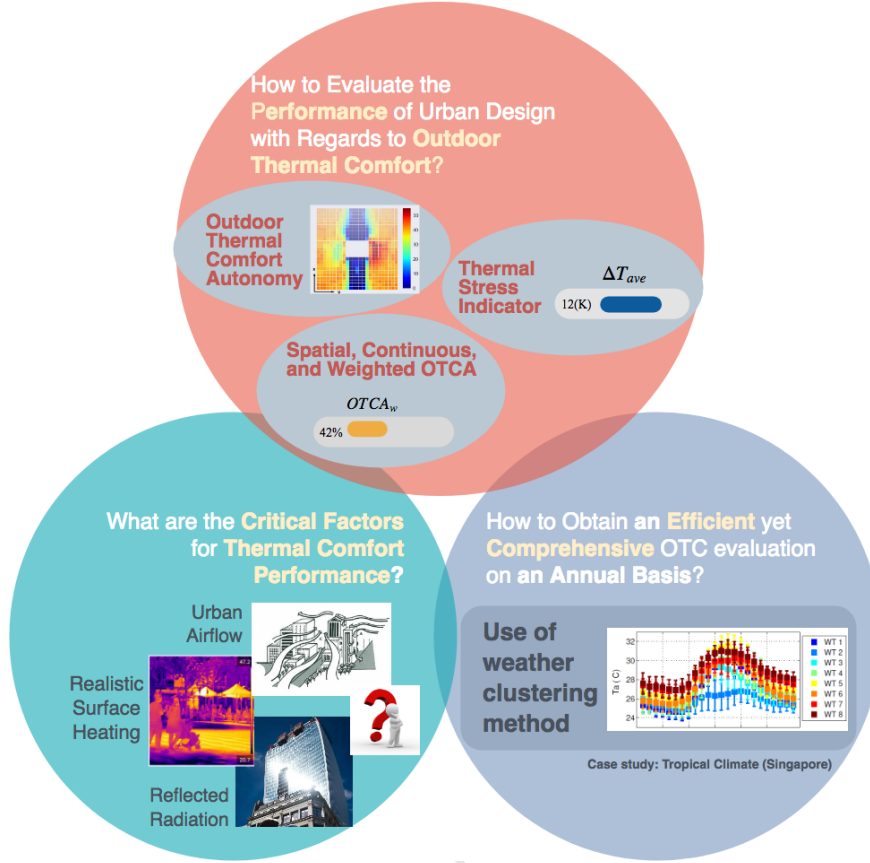


Figure 1: Graphical abstract of the present study indicating the objectives and research questions to be addressed.

2.1 Outdoor Thermal Comfort Autonomy (OTCA)

Outdoor thermal comfort autonomy is defined as the capability of keeping an outdoor space within a prescribed thermal comfort range, without additional cooling equipment or shading devices. Accordingly, *OTCA* is the percentage of occupied time over a year, or a prescribed period of use, where a designated area meets a given set of thermal comfort acceptability criteria.

The calculation of OTCA is based on a time series of the prescribed thermal comfort metric within the outdoor space. In the current study, Standard Effective Temperature (SET) by Gagge et al. [15] is considered as the evaluation metric, but the presented definition of OTCA can be similarly extended to other thermal comfort indices:

$$OTCA = \frac{1}{N} \frac{1}{n} \sum_{k=1}^N \sum_{hr=h_i}^{h_f} TC_{k,hr} \quad (1)$$

$$TC_{k,hr} = \begin{cases} 1 & \text{if SET} \in A \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

where $TC_{k,hr}$ is the thermal comfort index at a given day and hour, A is the “thermal comfort acceptability criteria,” i.e. the thermal comfort range that describes the desirable OTC conditions at a specific outdoor

150 space, N is the total number of occupied days, h_i and h_f denote the initial and final hours of occupation per
 151 day, and n is the total occupied hours ($n = h_f - h_i$). Here, $TC_{k,hr}$ is considered as either thermal comfort
 152 index calculated at hourly intervals or the time-averaged value over an hour of study.

153 An example of an OTCA map at the pedestrian height (1.5m) is demonstrated in Fig. 2 for an idealized array
 154 of buildings (a matrix of 3×3 equally spaced cubes with uniform height and plan area density, λ_p , of 0.0625).
 155 In this example, the operational hours are set to 0900 (h_i) to 1800 (h_f) local time while the acceptable OTC
 156 range (A) is set to $20\text{-}28^\circ\text{C}$. The large spatial variability seen in the OTCA map is attributed to the spatial
 157 distribution of wind speed (Fig. 2-b) as well as the cumulative effects of the shading pattern during the
 158 operational hours. Accordingly, the OTCA in adjacent grid cells may significantly differ, reflecting the
 159 combined impact of wind speed and shading on thermal comfort.

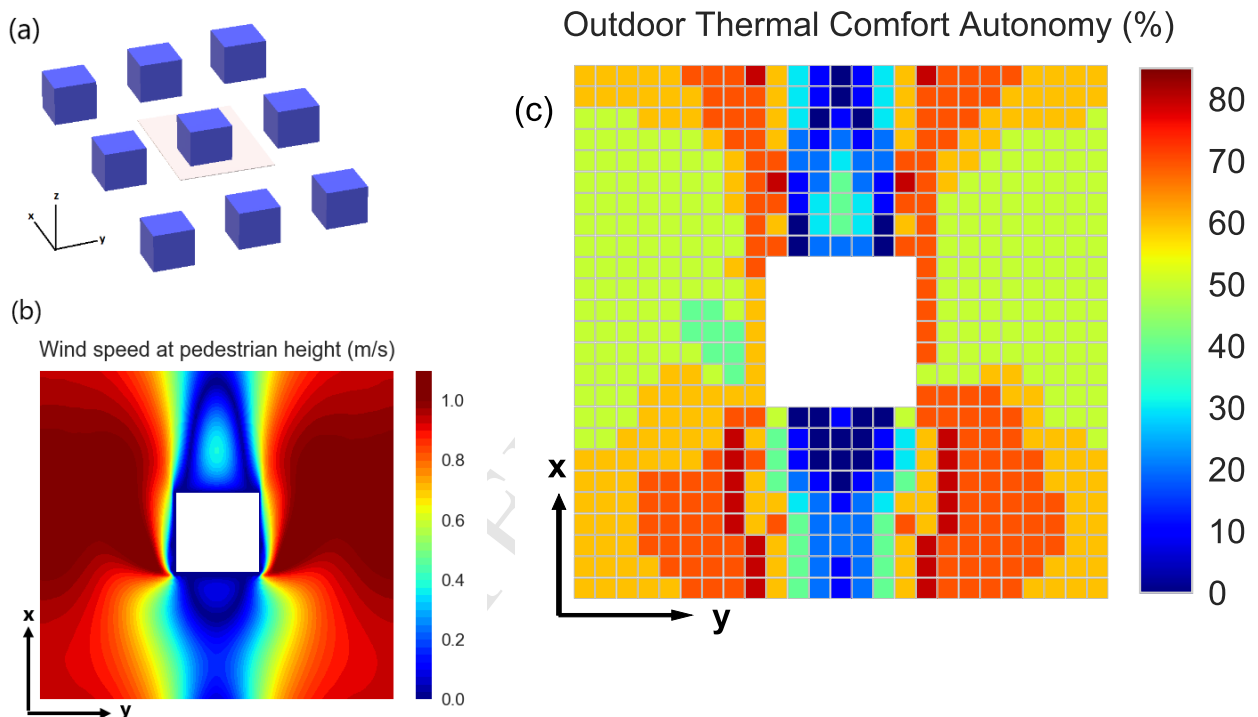


Figure 2: a) Schematic of a 3D array of idealized buildings with $\lambda_p = 0.0625$, b) spatial distribution of wind speed at the pedestrian height (1.5m) obtained from CFD [35], and c) an example of the spatial distribution of OTCA calculated at the pedestrian height (1.5m) for the configuration shown in (a). The example shown here is calculated for a typical dry-season day in Singapore during the month of March (meteorological data further discussed in Sec. 4.1.1 and Appendix B). The sun path during the studied day is from East to West at the equinox.

160 It is important to note that the calculation of OTCA requires the detailed consideration of human behaviors
 161 within the scope of the studied outdoor space as well as the expectation of the thermal environment. For
 162 example, the occupied hours, n , would be different based on the use of an outdoor space and should be
 163 factored in here for an accurate analysis of OTC. Additionally, the “acceptable” thermal comfort range in
 164 outdoor spaces is often larger than in indoor spaces, and varies based on the use of the outdoor space and the
 165 expectations of occupants. A recent study by Yang et al. [64] showed that the range of acceptable operative

166 temperature in outdoor urban spaces in Singapore can go as high as 31.7°C , which is significantly larger than
 167 the prescribed neutral range. Additionally, comparing the surveys carried out in semi-outdoor food-courts
 168 [54] with outdoor areas in Singapore [64], it can also be seen that the preferred temperature range can change
 169 up to 1.5°C in the same city, solely based on the functionality of a space. Such variations are more significant
 170 across different cities. Chow and Heng [9] has compared the neutral PET range for 10 major cities around
 171 the globe, and demonstrated that the reported range for “neutral comfort” can range from 18°C (Glasgow,
 172 UK [28]) to 29°C (Rome, Italy [51]), and the review of numerous studies by Potchter et al. [46] revealed
 173 that the range of the thermal comfort or dis-comfort varies strongly between hot and cold climates. Such
 174 variations are attributed to the acclimatization of the occupants to the local climate, their expectation of
 175 an outdoor space and climatic backgrounds, and physiological conditions of participants, which further call
 176 for the calibration of the thermal comfort acceptability criteria (A in Eq. 1) for the accurate calculation of
 177 OTCA.

178 2.2 Spatial and Continuous OTCA

179 *The **Spatial OTCA** is defined as the percentage of an outdoor space that is within the desired thermal*
 180 *comfort range at least 50% of the occupied time (over a year or a prescribed period of use).*

181 Additionally, partial credit can be attributed when thermal comfort lies below the threshold. Accordingly,
 182 ***Continuous OTCA** extends the definition of Spatial OTCA such that partial credit is given in an outdoor*
 183 *space where OTCA is lower than 50% threshold.*

184 For example, in the space where the OTCA is 40%, Continuous OTCA considers a partial credit of $40/50=0.8$.
 185 In the example shown in Fig 2, the Spatial OTCA is 7%, while Continuous OTCA is calculated as **13.4%**.
 186 The concepts of spatial and continuous OTCA are analogous to spatial and continuous daylight autonomy
 187 introduced by Reinhart et al. [47] as annual daylight metrics for indoor building design, and are defined to
 188 present and compare the performance of an outdoor space with regards to OTC in a tangible manner.

189 The spatial distribution of OTCA (shown in Fig. 2) is important in identifying the location of persistent
 190 “cold” or “hot” spots in urban areas, while Spatial and Continuous OTCA assess the overall performance
 191 of an outdoor space. There are valid arguments for considering both the spatial distribution of OTCA
 192 (Fig. 2) or the spatially-averaged quantities such as Spatial and Continuous OTCA as a design metric.
 193 As thermal comfort is highly variable in an outdoor space, the information provided in the spatial map of
 194 OTCA identifies the locations that are consistently outside of the thermal comfort acceptability criteria, and
 195 therefore urges designers to use passive design elements (such as shading devices) or active cooling methods
 196 (such as fans) for improving thermal comfort in these locations. However, pedestrians are often mobile in
 197 an outdoor urban space and at any time can move to a neighboring location with a desired thermal comfort
 198 range. This adaptive thermal comfort behavior should be considered in urban design, as it may not be
 199 needed nor feasible to design a space for 100% spatial autonomy. Therefore, Spatial and Continuous OTCA
 200 can be used as an adaptive and averaged thermal comfort evaluation.

201 Lastly, the threshold 50% here is considered analogous to the daylight autonomy, but more importantly, due
 202 to the fact that in outdoor urban spaces, people are often mobile and not bound to fixed position (contrary
 203 to the case indoor). However, we note that this threshold highly depends on the functionality of the outdoor

204 space. For instance, in case of alfresco outdoor dining, it is more suitable to pick a higher threshold such as
 205 80%, while in case of recreational outdoor space, park areas, or areas where people can move to chose their
 206 location in the urban area, the %50 is deemed acceptable.

207 **2.3 Thermal Stress Indicator: Deviation from the Thermal Comfort Accept-** 208 **ability Criteria**

209 *The **Thermal Stress Indicator** is defined as the average deviation of the thermal comfort index from the*
 210 *acceptable OTC range in an outdoor space, calculated during the occupied time over a year or a prescribed*
 211 *period of use.*

When calculating the outdoor thermal comfort autonomy, the OTC index is computed and discarded if not within the acceptability criteria. Accordingly, the computation of OTCA can be regarded as “binary” with no indication of the magnitude of deviation from the acceptable range, and therefore neglecting the extent of thermal stress. To give more information on OTC, the Thermal Stress Indicator can be computed as the average deviation of temperature from the desired range at each location:

$$\Delta T_{ave} = (K^{-1} - 1)\Delta T_{crit} \quad (3)$$

where K , the scaling factor between 0 to 1, is computed as

$$K = \frac{1}{N} \frac{1}{n} \sum_{k=1}^N \sum_{hr=h_i}^{h_f} m_{k,hr} \quad (4)$$

$$m_{k,hr} = \begin{cases} 1 & \text{if } |\Delta T| \leq \Delta T_{crit} \\ \frac{\Delta T_{crit}}{|\Delta T_{k,hr}|} & \text{otherwise} \end{cases} \quad (5)$$

Here, ΔT_{crit} is the acceptable temperature range from the midpoint, defined as

$$\Delta T_{crit} = (A_{max} - A_{min})/2. \quad (6)$$

For instance, if the thermal comfort acceptability range (A in Eq. 1) is set to 20 - 28°C, then $\Delta T_{crit} = 4^\circ C$. $\Delta T_{k,hr}$ is then defined as the difference of the thermal comfort index at any time and day ($TC_{k,hr}$) from the midpoint of the acceptable range A , calculated as

$$\Delta T_{k,hr} = TC_{k,hr} - (A_{max} + A_{min})/2. \quad (7)$$

212 Accordingly, ΔT_{ave} (Eq. 3) at every location indicates the (absolute) average deviation (in °C) of the
 213 thermal comfort index from the acceptable OTC range during the occupied time over a year, and therefore
 214 identifying the zones with critical thermal stress conditions throughout the occupied time (Fig. 3).

It is worth noting that the definition of scaling factor described in Eq. 4 a) neglects the distinction between “hot” and “cold” spots and solely considers the absolute value of temperature deviation, and b) does not indicate the frequency of occurrence of events within the thermal stress zone (i.e. 10 slightly uncomfortable days may result in a similar K factor than 1 extremely uncomfortable day out of 10 days). Therefore, for obtaining more information and presenting a comprehensive assessment, it is suggested to divide this metric

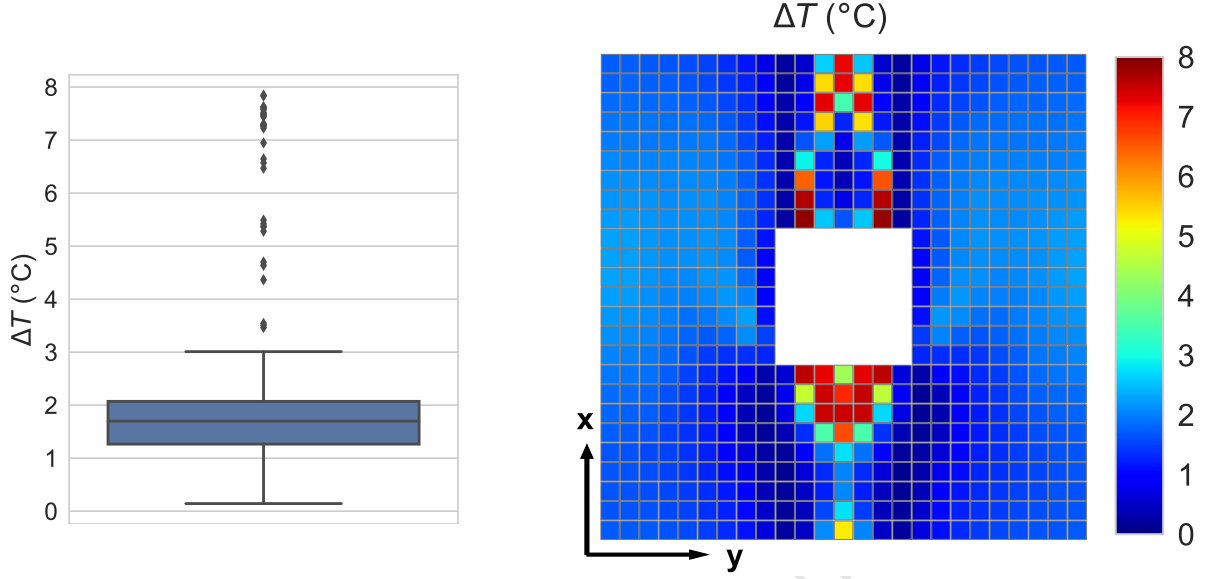


Figure 3: The spatial distribution (right) and box-and-whisker diagram (left) of ΔT_{ave} as the Thermal Stress Indicator (Eq. 3) calculated at the pedestrian level for an idealized array of building ($\lambda_p = 0.0625$). The example shown here is calculated for the same case and configuration discussed in Fig. 2 and Sec. 2.1.

into different bands (hot and cold) by considering K^+ and K^- based on the sign of $\Delta T_{k,hr}$. Additionally, the frequency of deviation in the cold and hot bands can be calculated in order to add more information regarding the occurrence of thermally uncomfortable conditions:

$$f_i = \frac{1}{N} \frac{1}{n} \sum_{k=1}^N \sum_{hr=h_i}^{h_f} F_i \quad \text{where } i = \{\text{cold, OK, hot}\} \quad (8)$$

$$\text{Cases} = \begin{cases} F_{cold} = 1 & \text{if } |\Delta T_{k,hr}| > \Delta T_{crit} \wedge \Delta T_{k,hr} < 0 \\ F_{OK} = 1 & \text{if } |\Delta T_{k,hr}| \leq \Delta T_{crit} \\ F_{hot} = 1 & \text{if } |\Delta T_{k,hr}| > \Delta T_{crit} \wedge \Delta T_{k,hr} > 0 \end{cases} \quad (9)$$

215 Following these calculations, the spatial map of ΔT_{ave} as a Thermal Stress Indicator (Fig. 3) together
 216 with the spatial map of frequency of occurrence (Eq. 8) can provide comprehensive information which
 217 distinguishes the persistent occurrence of “hot” and “cold” conditions from a potentially short-lived extreme
 218 event.

219 2.4 Weighted Outdoor Thermal Comfort Autonomy ($OTCA_w$)

220 Here, we introduce the **Weighted Outdoor Thermal Comfort Autonomy** ($OTCA_w$) to represent the
 221 average deviation from the acceptable OTC range together with the OTCA map, as opposed to considering
 222 the binary approach to comfort previously discussed in Eq. 1. Accordingly, $OTCA_w$ represents the percent
 223 of occupied time over a year, or a prescribed period of use, where a thermal zone meets a given set of thermal
 224 comfort acceptability criteria, while also accounting for the deviation (thermal stress) when the desired OTC
 225 range is not met.

Using the scaling factor K (Eq. 4), OTCA can further be weighted to include the deviation of the thermal comfort index from the acceptable OTC range during the occupied time over a year, such that

$$OTCA_w = K \times OTCA. \quad (10)$$

226 Figure 4 demonstrates the variability in OTCA compared with $OTCA_w$ and indicates the importance of
 227 including the deviation from the acceptability criteria.

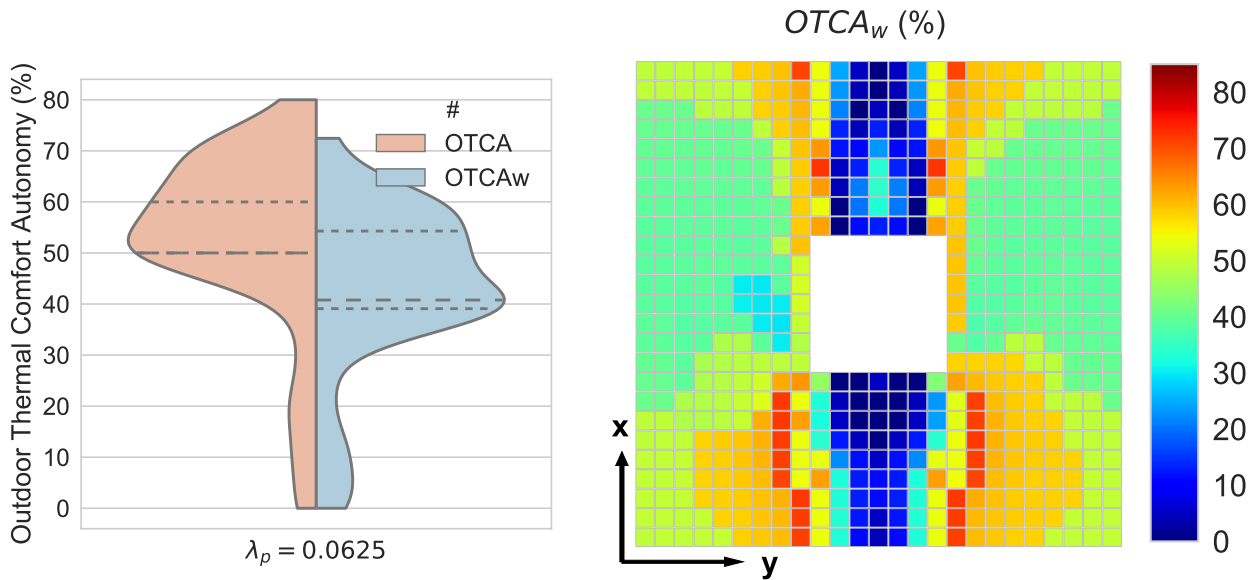


Figure 4: Spatial distribution of $OTCA_w$ (right) and violin plot (kernel density) distribution of OTCA and $OTCA_w$ (left) at the pedestrian height for an idealized array of building ($\lambda_p = 0.0625$). The example shown here is calculated for the same case and configuration discussed in Fig. 2 and Sec. 2.1. The inner lines in the violin plots demonstrate the quartiles of the distribution.

228 3 Critical Factors for Thermal Comfort Performance

229 Subsequent to defining the performance metrics for thermal comfort, it is paramount to discuss the means
 230 for their accurate estimation. Here, we present a series of sensitivity analyses which evaluate the role of
 231 various microclimate parameters in the OTC performance. This analysis is motivated by the state-of-the-
 232 art numerical models currently used for assessing OTC and the assumptions and limitations associated
 233 with them. The goal is to draw attention to the ways in which such assumptions can impact an accurate
 234 evaluation of thermal comfort in urban spaces, quantified by OTC performance metrics such as OTCA (Sec.
 235 2). Although it is out of the scope of the present study to conduct a comprehensive set of sensitivity analyses,
 236 the discussion given in this section is critical in presenting a comprehensive perspective regarding the OTC
 237 performance metrics and aim to emphasize on accurate assessments using numerical models. Overall, three
 238 critical parameters are examined:

- 239 (a) **Spatial distribution of urban airflow:** we consider the assumption of uniform wind speed at the
 240 pedestrian level as opposed to obtaining the detailed three-dimensional distribution of airflow (often

241 obtained from Computational Fluid Dynamics simulations).

242 (b) **Realistic distribution of surface heating:** the non-uniform three-dimensional distribution of sur-
 243 face temperature, and the subsequent role on the spatial distribution of OTCA, is examined compared
 244 to the assumption of uniform surface temperature for urban facades.

245 (c) **Reflected radiation from urban facades to pedestrians:** we evaluate the implications of neglect-
 246 ing the reflected radiation from urban facades on radiation exposure of pedestrians, and consequently,
 247 the performance of an outdoor space with regards to thermal comfort.

248 3.1 Case Studies

249 The sensitivity analysis presented here is conducted for Singapore (between $1^{\circ}09'N$ to $1^{\circ}29'N$, and $103^{\circ}36'E$
 250 to $104^{\circ}25'E$). More information on the climatic characteristics of Singapore is given in Sec. 4.1.1. The
 251 simulation days correspond to the month of April, which encompasses the highest air temperature and
 252 largest solar elevation angle. The test case presented here is an idealized array of buildings, while the plan
 253 area density (λ_p) is varied from 0.0625 to 0.44, representing Sparsely Built (LCZ 9) and Compact Mid-Rise
 254 (LCZ 2) Local Climate Zones, respectively [56]. Each building wall has a window with window-to-wall ratio
 255 of 0.4 and solar heat gain coefficient (SHGC) of 0.2. The albedo and emissivity of urban surfaces (walls and
 256 ground) are set to 0.3 and 0.9, respectively. The relative humidity is considered constant at the pedestrian
 257 level and set to 80%, which is the annual average of humidity in Singapore.

258 To obtain the most comprehensive analysis, a modular approach detailed by Nazarian et al. [37] is used
 259 such that existing microclimate tools of airflow and energy balance modeling contribute to the calculation
 260 of OTC. Accordingly, the surface temperatures and canopy air temperature is obtained from energy balance
 261 modeling using the Temperature of Urban Facets Indoor-Outdoor Building Energy Simulator (TUF-IOBES
 262 [63] and [27]), while the flow field is taken from large-eddy simulations (LES) of Nazarian et al. [35, 36]. For
 263 thermal comfort analysis, SET is taken as the OTC metric and calculated for a standing male pedestrian
 264 (metabolic rate = 1.2) who weighs 70 kg, is 150cm tall, and is wearing light summer clothing ($iclo=0.34$).
 265 The skin wetness, body emissivity, and body albedo are considered to be 0.088, 0.95, and 0.3, respectively.
 266 The OTC performance metrics are calculated for an outdoor space with operational hours of 0900 (h_i) to
 267 1800 (h_f) local time, while the acceptable OTC range, A in Eq. 1, is set to 20-28°C. This range covers the
 268 neutral zone prescribed in SET definition ($22.2 - 25.6^{\circ}C$ Auliciems and Szokolay 1997), as well as mid-range
 269 of slightly cold or slightly warm thermal zone, which is found to be acceptable in outdoor dining places in
 270 Singapore [64].

271 Table 1 represents the simulation cases that are studied here. The Base case represents the OTCA calculation
 272 with realistic 3D distributions of surface temperature and reflected radiation (taken from TUF-IOBES) and
 273 flow field (taken from LES simulations). The detailed description of other simulation cases are provided in
 274 the following sections.

Table 1: Proposed Case Studies for OTCA analysis

ID No.	Cases	Boundary Conditions		
		Surface Temperature	Airflow	Reflected Radiation
1	Base	Realistic (3D)	Realistic (3D)	Realistic (3D)
2	Wind-Test	Realistic (3D)	Constant	Realistic (3D)
3	Temp-Test	Constant	Realistic (3D)	Constant
4	Refl-Test	Realistic (3D)	Realistic (3D)	Neglected

3.2 On the Consideration of Urban Airflow in Thermal Comfort Autonomy

Here, we calculate the OTCA (Eq. 1) for an idealized array of building with plan area density (λ_p) of 0.0625 (shown in Fig. 5-a), and compare the following assumptions for wind conditions at the pedestrian level:

1. three-dimensional distribution of airflow for the representative urban configuration ($\lambda_p = 0.0625$) obtained using a CFD simulation [35] (Base in Table 1),
2. constant wind speed at all the pedestrian locations: value calculated based on the spatial mean of the airflow at the pedestrian height (Wind-Test in Table 1 with $u=0.7 \text{ m s}^{-2}$), and
3. constant wind speed at all the pedestrian locations: value based on the hourly-average of wind speed at the reference height above the canopy (Wind-Test in Table 1 with $u=2 \text{ m s}^{-2}$).

The realistic (3D) distribution of surface temperature and reflected radiation is considered in these cases. Figure 5 demonstrates the distribution of airflow at the pedestrian height (b) as well as the OTCA distribution for the wind conditions considered here (c-d): uniform and realistic distribution of wind speed at the pedestrian height. The spatial distribution of OTCA is significantly different in the two studied cases. When the wind is considered constant at all pedestrian locations, it can be seen that the spatial distribution of OTCA is dominated by the change in the shadow pattern throughout the occupied hours (0900 - 1800 local time). When the spatial distribution of the airflow is introduced, however, the spatial distribution of OTCA is modified to represent the flow field in addition to the shadow patterns, and consequently, the location of the "hot" and "cold" spots is modified.

Figure 6 further displays the violin plot distribution of OTCA in the three studied conditions, and it can be seen that not only the spatial distribution of the wind speed, but also the value assigned at the pedestrian height, has a significant importance in the OTCA outcome. In the case of using a higher above-canopy wind speed (2 m s^{-1}), the OTCA is generally larger than 50%, yielding a 100% spatial autonomy which is in contrast to the case with wind speed 0.7 m s^{-1} (taken as the average of the airflow at the pedestrian level) where the spatial OTCA is 0%. Similarly, when spatial distribution of wind speed is considered, the average deviation of the thermal comfort from the acceptable range (i.e. thermal stress indicator discussed in Sec. 2.3) can reach up to 12°C in some pedestrian locations (shown in the boxplot of ΔT_{ave} in Fig. 6) due to the formation of vortices before and after the building that significantly reduce the wind speed value. However, this extent of deviation from the acceptable thermal comfort range is not reflected in the cases with constant wind speed. Given these findings, it is evident that the consideration of the detailed flow field in urban environments is critical in evaluating the performance metrics for outdoor thermal comfort.

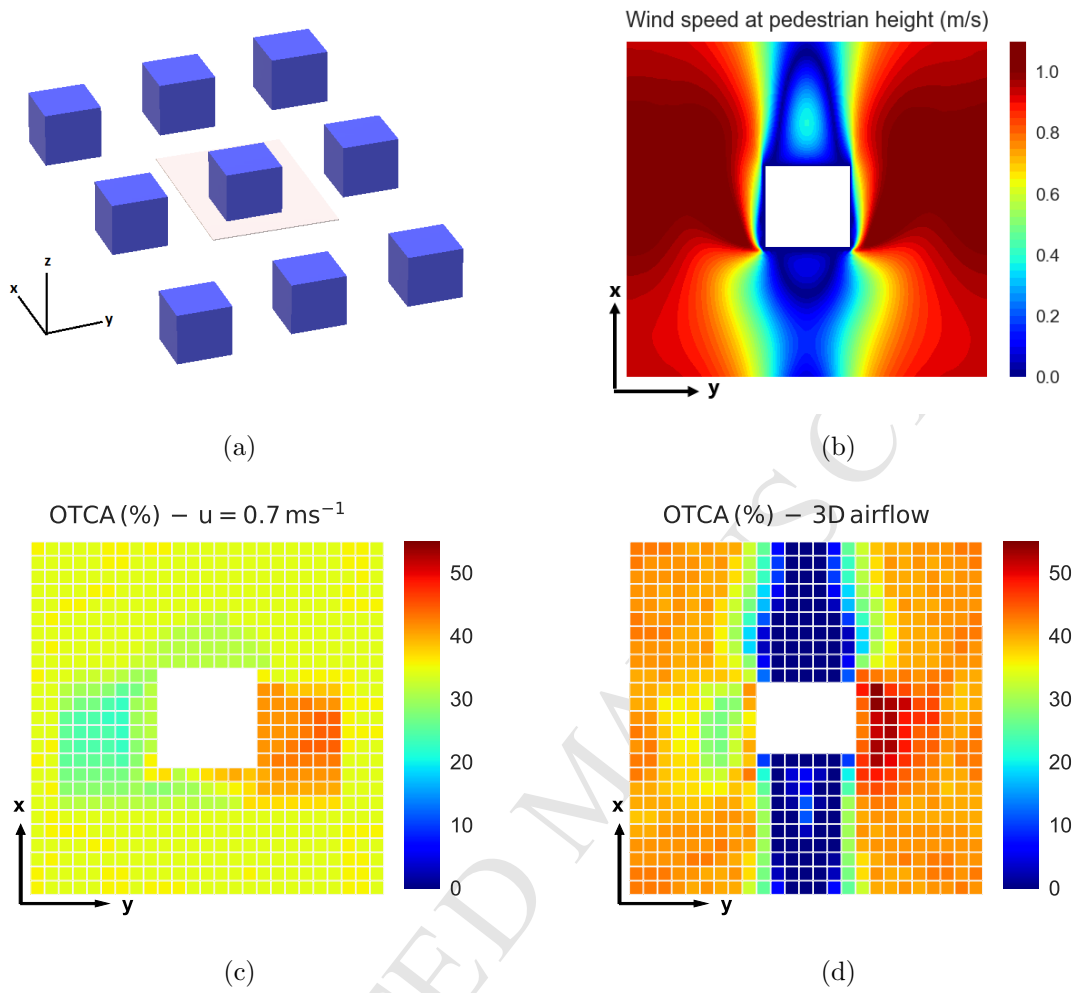


Figure 5: (a) Schematic of the computational domain as an idealized array of buildings, (b) spatial distribution of wind speed at the pedestrian height obtained from CFD [35], and the distribution of OTCA at the pedestrian height ($z=1.5\text{m}$) considering a uniform (0.7 m s^{-1}) and realistic wind speed, (c) and (d) respectively.

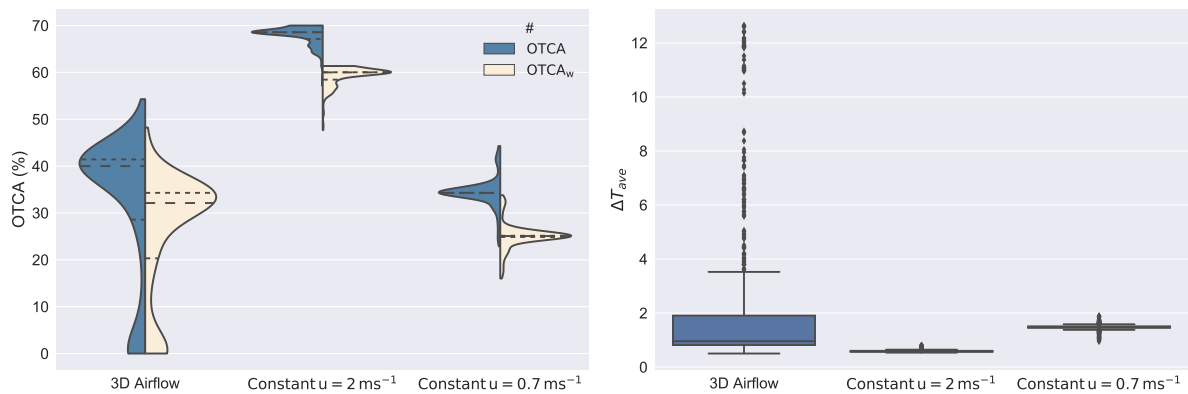


Figure 6: Left: violin plot distributions of OTCA and OTCA_w (Eqs. 1 and 10) and right: box plots of ΔT (Eq. 3) for $\lambda_p = 0.0625$ at the pedestrian level in 3 different wind conditions.

3.3 On the Consideration of Realistic Surface Heating in Thermal Comfort Autonomy

In this section, we evaluate OTCA calculation using two assumptions made for the temperature of urban facades:

1. non-uniform three-dimensional distribution of surface temperature obtained using a building-to-canopy energy balance model considered at urban facades (Base in Table 1), and
2. uniform (constant) temperatures considered at each surface, taken as the average value of surface temperature (Temp-Test in Table 1).

Figure 7 demonstrates an example of non-uniform surface heating at the ground level for $\lambda_p = 0.0625$ at 1000 local time, which is strongly dominated by the shading pattern. It is worth noting that the consideration of detailed shading on the pedestrian (and not surfaces) is kept intact here as it dramatically changes the analysis of thermal comfort, and only the distribution of surface temperature is of focus here. Additionally, the spatial (non-uniform) distribution of airflow at the pedestrian height is considered in these cases.

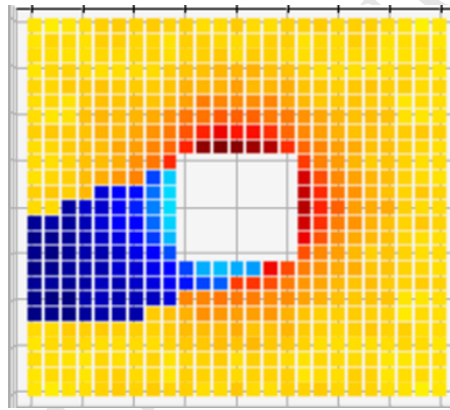


Figure 7: Spatial distribution of ground-level surface temperature at 1000 local time for $\lambda_p = 0.0625$.

We observe that the spatial distribution of OTCA at the pedestrian level is dominated by the spatial distribution of airflow and shading patterns (at pedestrian locations) during the occupied hours (similarly shown in Fig. 5), and therefore the assumption of uniform surface heating did not dramatically impact the OTCA map (not shown). However, the value of OTCA can be slightly impacted as shown in the violin plot in Fig. 8. When the 3D distribution of surface temperature is not considered, the OTCA values are slightly overestimated (up to 3% observed here). However, Nazarian et al. [37] demonstrated that the consideration of realistic surface heating affects the mean radiant temperature at the pedestrian height more significantly in the higher urban densities, which is expected to similarly affect the OTCA distribution. Accordingly, the accurate calculation of OTCA in high-density urban environments requires a careful attention to the surface heating distribution and further investigations are needed to evaluate the variation in OTCA based on urban density and surface properties.

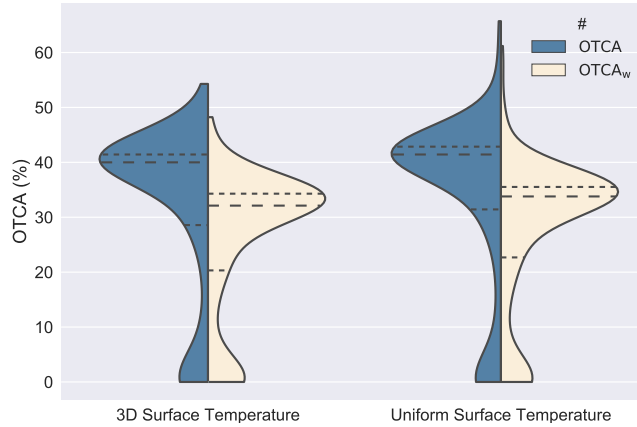


Figure 8: Violin plots of OTCA and OTCA_w (Eqs. 1 and 10) for $\lambda_p = 0.0625$ at the pedestrian level in two different surface heating conditions.

3.4 On the Consideration of Reflected Radiation in Thermal Comfort Autonomy

Lastly, we evaluate the OTCA calculation given the assumption of reflected radiation. In several existing thermal comfort models, the reflected radiation from surfaces that are visible to the pedestrians is neglected while it is expected to have a tangible impact, particularly when pedestrians are exposed to highly-reflective surfaces in densely-built urban areas. To assess this assumption, we evaluate the difference in OTCA distribution for two scenarios: with and without the consideration of reflected radiation in the calculation of OTC. The realistic distribution of wind speed at the pedestrian height and realistic surface heating is maintained for both cases. The analyses are done for two urban densities: 1) $\lambda_p = 0.0625$ representing “sparsely built” Local Climate Zone (LCZ 9) and 2) $\lambda_p = 0.44$ representing “compact mid-rise” Local Climate Zone (LCZ 2).

Figure 9 demonstrates the distribution of OTCA and OTCA_w for two urban configurations with and without reflected radiation from the visible urban surfaces. It can be seen that in both LCZs, neglecting the surface reflected radiation leads to the overestimation of both OTCA and OTCA_w. In the $\lambda_p = 0.44$ case, the median OTCA is changed up to 7%, which demonstrate the importance of surface reflected radiation in outdoor thermal comfort. It is worth noting that, here, only one value of surface albedo ($\alpha = 0.3$) is considered and therefore further investigations are needed to evaluate the importance of reflected radiation in OTCA given the variability of surface albedo and considering a full range of local climate zones.

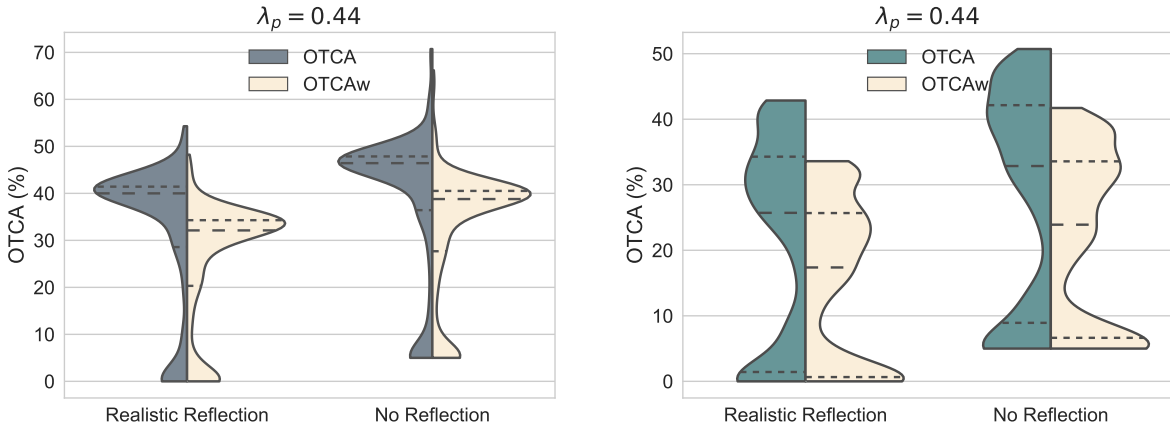


Figure 9: Violin plots of OTCA and OTCA_w (Eqs. 1 and 10) for $\lambda_p = 0.0625$ and $\lambda_p = 0.44$ at the pedestrian level with and without the consideration of reflected radiation.

4 Comprehensive Annual Evaluation of Thermal Comfort Metrics

After discussing the OTC performance metrics and drawing attention to the critical factors that should be scrutinized in their calculation, here we discuss a methodology to obtain a comprehensive yet efficient evaluation of OTC performance metrics. The aim is to minimize the computational costs of calculation while maintaining the variability in meteorological conditions, which is needed for detailed analyses on an annual basis.

In order to fully evaluate and describe the thermal comfort performance in urban design scenarios, it is essential that both spatial distributions (calculation of OTC at various pedestrian locations in urban areas) and temporal variabilities (consideration of hourly meteorological data) are represented. This calculation involves a coupling of several physical models at each hour of calculation, which can impose further limitations and simplifications of the processes. Here, as an alternative method for maintaining the spatial and temporal characteristics, we discuss a clustering method for the input meteorological data that can be utilized for effective calculation of OTC performance metrics.

4.1 Weather Clustering Method

The common method for implementing the meteorological forcing in urban climate simulations is to obtain the long-term databases of atmospheric parameters throughout at least one year, and directly use them in the numerical models. Such datasets are represented as locally recorded weather data or pre-selected “typical” years, which are available with a high temporal frequency (1-3 h). A comprehensive yearly energy and comfort analysis then needs to integrate the hourly representative meteorological forcing data. This approach is common for building or urban energy-balance analyses, where 8760 sets of forcing data (corresponding to yearly data with hourly resolution) are used, but poses several challenges for the comprehensive assessments of thermal comfort that depends on a range of microclimate parameters such as wind speed, air temperature, mean radiant temperature, and humidity. The main challenge arises when the variabilities in

370 the meteorological forcing are needed in the dynamic coupling of the underlying physical models, such as
371 urban flow field and energy balance models. Due to the complexities of such coupling methods, the hourly
372 variation of all parameters is not commonly considered. The second challenge is computational costs and
373 storage limitations. An annual analysis takes up a significantly large CPU and storage capacity. As a result,
374 the consideration of all hours for an annual analysis may not be feasible, and perhaps is unnecessary.

375 To address such challenges to the comprehensive annual analysis of thermal comfort, a method to cluster the
376 yearly meteorological data has been proposed. The goal of clustering is to obtain the representative weather
377 types that describe the typical daily patterns, and further produce synthetic long-term climatic forcing in an
378 efficient way. Previously, this approach was mostly implemented for the synoptic-scale circulation analysis
379 [21, 44], but a recent study by Acero et al. [1] has demonstrated that the application of weather clustering
380 can be extended to microscale climate simulations.

381 The process of weather clustering is as follows. Site observations are identified for a sufficiently long period
382 that represents the diversity of weather types throughout the year and a clustering method is applied to
383 classify the meteorological conditions of each day (a detailed description of the clustering method employed
384 here is explained in Appendix A and Acero et al. [1]). In each cluster, a diurnal cycle is then calculated for
385 each climate variable. As a result, sequences of weather data are reconstructed at an hourly frequency for
386 all forcing variables such that they represent the climatic variability of a location in terms of wind regimes,
387 precipitation, thermal range, and humidity amplitude for an entire year. Previous studies, such as Hidalgo
388 et al. [17], have shown that such reconstruction algorithms are able to produce diurnal cycles that compare
389 well within the hourly series from observations. Similarly, in order to achieve a comprehensive yet efficient
390 analysis of OTC performance metrics, we propose and evaluate a weather clustering method here. The
391 following sections describe an example of such analysis for a tropical climate of Singapore.

392 4.1.1 Example of Clustered Weather Data in a Tropical Climate of Singapore

393 This section details an example of clustered weather data for a case study of Singapore. Singapore is an
394 island state located in Southeast Asia (between $1^{\circ}09'N$ to $1^{\circ}29'N$, and $103^{\circ}36'E$ to $104^{\circ}25'E$) and its climate
395 is characterized by uniform air temperature and high humidity throughout the year with small diurnal and
396 seasonal variations. Accordingly, the minimum and maximum air temperature range between $23-25^{\circ}C$ and
397 $31-33^{\circ}C$, respectively, while the relative humidity (in the absence of rain) varies from 60% in the afternoon
398 to 90% in the morning (before sunrise). In the rainy periods, however, the RH reaches 100%, resulting in
399 an annual average of 84%. Further contrasts that prevent true all-year uniformity are the monsoon seasons
400 occurring twice a year. These monsoon seasons, labeled as Northeast (NE) and Southeast (SE) monsoons,
401 are characterized by increased precipitation and prevailing wind directions, and the highest precipitation
402 levels usually occur during the wet Northeast monsoon season [33, 48].

403 In order to obtain the clustered weather data for Singapore, the EnergyPlus Weather data (EPW file exten-
404 sion retrieved from <https://energyplus.net/weather>) was used, which includes an hourly dataset of a typical
405 year. This data represents compiled observations from multiple years collected at the Singapore Changi
406 Airport meteorological station. The following variables are then chosen to cluster the yearly meteorological
407 data into “typical” days using the statistical clustering K-Means method (Appendix A):

- 408 • Daily mean air temperature, T_a ($^{\circ}C$)
- 409 • Daily temperature amplitude, dT ($^{\circ}C$).
- 410 • Daily mean vapour pressure, e_v (Pa)
- 411 • Daily mean global horizontal irradiance, GHI ($W m^{-2}$)
- 412 • Daily mean wind speed and direction, WS and WD ($m s^{-1}$ and $^{\circ}$)

413 Table 2 summarizes the eight weather types (clusters) obtained for Singapore using the prescribed method.
 414 The clustered weather types were obtained from the entire year, as opposed to separating the meteorological
 415 data into various climatic periods (e.g. monsoons, and inter-monsoon seasons). This is acceptable due to
 416 the low inter-seasonal variability of climate in Singapore, but may not be recommended in the temperature
 climates and other locations with distinct seasonable variability [18].

Table 2: Summary of the typical weather types in Singapore obtained by the clustering method. The four possible **Seasons** for each clusters are 1) Northeast (NE) Monsoon season (December - early March), 2) Inter-Monsoon period (late March - May), 3) Southwest (SW) Monsoon season (June - September), and 4) Inter-Monsoon period (October - November). **WD** and **WS** stand for wind direction and wind speed, respectively, and **Rain** indicates the expected precipitation level. The columns **Months** and **Date** represent the months of occurrence for each cluster and the selected date of simulation corresponding to that period, respectively. f is then the frequency of occurrence for each weather type.

ID	Season	WD	WS	Rain	Months	Date	f
1	NE monsoon, Dry	NE	Medium-High	None-Low	Feb, Mar	1-Mar	11.8%
2	NE monsoon, Wet	NE	Low	High	Dec, Jan	1-Jan	10.4%
3	Inter-monsoon, Wet	-	Low	Medium	Oct, Nov	1-Nov	20.0%
4	SW monsoon	SW	Medium	Low	Aug, Sep	1-Sep	11.5%
5	NE monsoon, Dry	NE	Low-Medium	Low	Feb, Mar, Apr	15-Mar	16.7%
6	NE monsoon, Dry	NE	High	None-Low	Feb, Mar	1-Mar	8.0%
7	SW monsoon, Inter-monsoon	S-SE	Medium	None-Low	Apr - Sep	1-Jul	11.2%
8	SW monsoon	SW	Medium	low	May-Sep	15-Jul	10.4%

417
 418 Further description of the characteristics of each clustered weather type is presented in Appendix B. Over-
 419 all, the mean hourly values and the diurnal amplitude are well represented, especially for variables with
 420 pronounced diurnal variations such as incoming solar radiation, temperature, and humidity. The variabil-
 421 ity in wind flow is also represented reasonably well but with lower value of Pearson correlation coefficient
 422 than other parameters, which has been similarly reported in Hidalgo et al. [17]. Accordingly, although the
 423 clustering method represents the daily variability in some climatic variables better than others (Appendix B
 424 Table B.1), it can be concluded that the overall weather types obtained here are reliable for a yearly thermal
 425 comfort analysis. The forcing data in each weather type (including air temperature, relative humidity, wind
 426 speed and direction, short-wave radiation (DNI, GHI, DHI), cloud cover, and ceiling height) are then used
 427 for the calculation of OTC performance metrics detailed in the following section.

4.2 Calculation of OTC Performance Metrics using the Clustered Weather Data

Here, the clustered weather types obtained for Singapore (summarized in Table 2) are used to demonstrate the comprehensive calculation of OTC performance metrics for an entire year. Figure 10 displays the flowchart of the presented methodology. In order to obtain a more comprehensive analysis, we employ a modular approach such that existing microclimate tools for urban energy balance and airflow modeling provide the microclimate inputs needed for calculating thermal comfort [37]. First, instead of using the hourly values of meteorological data for an entire year, the clustered weather types (detailed in Sec. 4.1.1) are considered. Then, for each weather type, the energy balance simulations are run and the 3D distribution of surface temperature and radiation are obtained. Next, these results are combined with the airflow at the pedestrian level, simulated using Computational Fluid Dynamics (CFD) modeling, and the 3D distribution of the thermal comfort index is calculated. Lastly, the performance metrics are obtained for each weather type and weighted based on the frequency of each type (Table 2) to calculate the annual OTC performance metrics.

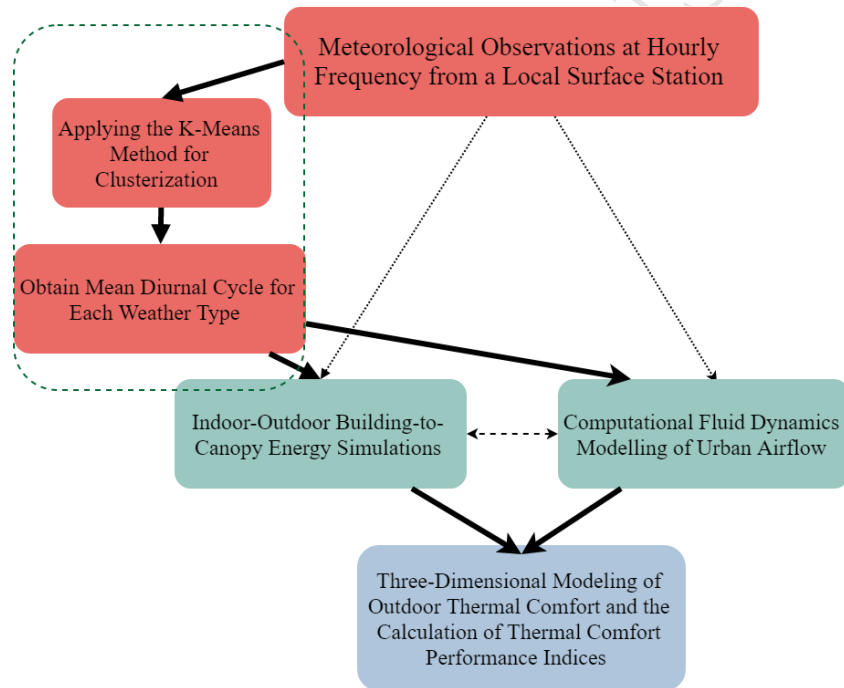


Figure 10: Flow chart of calculating the performance metrics for outdoor thermal comfort analysis. The solid black lines represent the path taken in this analysis, while the dashed/dotted lines represent the alternative or complementary modeling methods: the dotted lines indicate the use of representative weather data at each hour for an entire year (i.e. without clustering) and the dashed line indicates the dynamic coupling of urban energy balance and flow modeling. Here, the energy balance modeling is done using the Temperature of Urban Facets Indoor-Outdoor Building Energy Simulator (TUF-IOBES [63] and [27]), while the flow field is taken from large-eddy simulations (LES) of Nazarian et al. [35]. See Nazarian et al. [37] for more information on the OTC modeling in 3D.

440

The simulation test case presented here is an idealized array of buildings with plan area density (λ_p) of 0.0625 (demonstrated in Fig. 5) representing sparsely built local climate zones [56]. The energy balance model is run for 10 days encompassing the selected simulation date for each weather type (Table 2) and

443

444 the first three days are discarded to avoid the errors associated with the initial boundary conditions. The
 445 wind flow simulations are done for a neutral condition with a constant wind direction and wind speed at
 446 the forcing height, and then linearly scaled using the hourly wind speed values represented in each weather
 447 data. The assumptions are that 1) the effect of thermal forcing on the urban flow field is negligible and
 448 b) for the same urban flow regime (isolated buildings [40] here), the flow field at the pedestrian level is
 449 linearly correlated with the wind speed at a forcing height. These considerations are due to the limitations
 450 regarding the computational costs and acceptable as the present example is only meant for demonstrating
 451 the methodology. For a more accurate analysis, however, a one-way (static) or two-way (dynamic) coupling
 452 of thermal forcing with flow fields are recommended, which are more feasible to obtain using the weather
 453 clustering method presented here as the computational costs are significantly reduced.

454 For the calculation of the thermal comfort distribution at the pedestrian level, the Outdoor Thermal Comfort
 455 in 3D (OTC3D introduced by Nazarian et al. [34, 37]) is used with inputs from a) meteorological forcing
 456 data for each weather type (including hourly values of GHI, DNI, DHI, RH, CC, WS), b) 3D distribution
 457 of surface temperature from the energy balance model, and c) 3D distribution of wind flow obtained from
 458 CFD simulations. SET is taken as the OTC metric and calculated for a standing male pedestrian (metabolic
 459 rate = 1.2) who weighs 70 kg, is 150cm tall, and is wearing light summer clothing (iclo=0.34). The skin
 460 wetness, body emissivity, and body albedo are considered to be 0.088, 0.95, 0.3, respectively, and the OTC
 461 performance metrics are calculated for an outdoor space with operational hours of 0900 (h_i) to 1800 (h_f)
 462 local time while the acceptable OTC range (A) is set to 20-28°C.

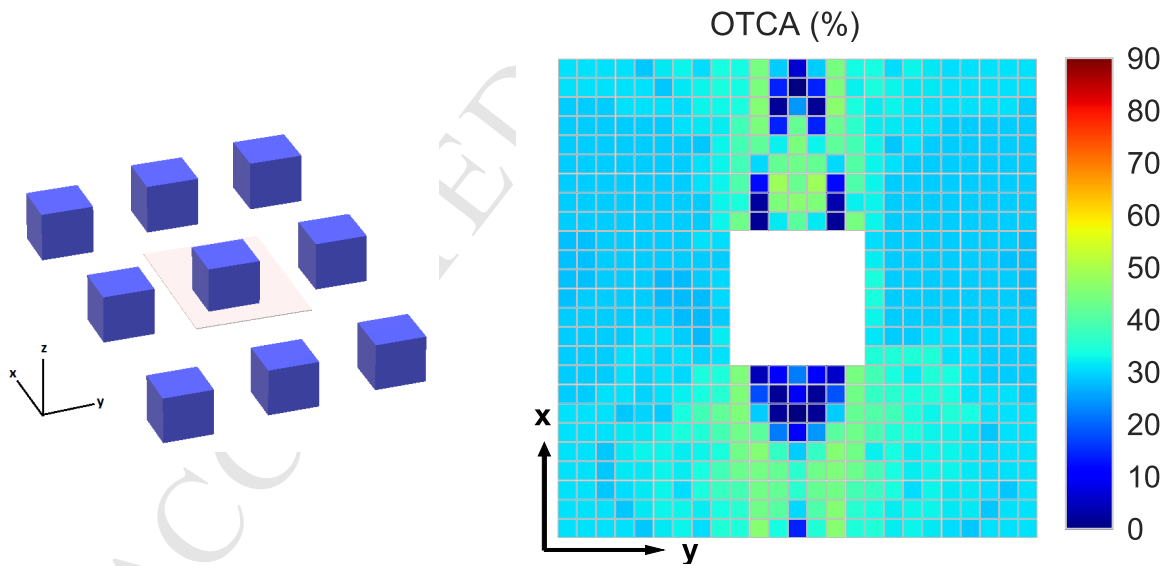


Figure 11: Left: Schematic of a 3D array of idealized buildings with $\lambda_p = 0.0625$. Right: Spatial distribution of OTCA calculated on an annual basis using the clustered weather types. OTCA is calculated at the pedestrian height (1.5m above ground level).

463 Figure 11 demonstrates the spatial distribution of OTCA (%) calculated for an idealized urban configuration,
 464 which is obtained by calculating the OTCA map for each clustered weather type (Fig. 12) and weighing
 465 the results based on the frequency of occurrence of weather types throughout the year (Table 2). The high

466 spatial variability of OTCA at the pedestrian height is seen for all cases in Fig. 12 and the OTCA range
467 is significantly different across various weather types. The spatial variability of OTCA is dominated by two
468 main factors: 1) airflow distribution, and 2) shading pattern at the pedestrian height. In these calculations,
469 the wind direction is aligned with the x-axis (Fig. 11), which is projected in the variability of OTCA around
470 the building for all weather types. The distribution of the shading pattern as well as the shade-to-sunlit
471 area, on the other hand, are dominated by the day of the year for which the simulations are conducted.

472 In order to better grasp the contributing factors to OTCA, the boxplot distribution of various parameters
473 is also presented in Fig. 13. The critical parameters contributing to thermal comfort (presented as SET
474 here) are a) air temperature, b) wind speed, c) relative humidity, and d) mean radiant temperature. In Fig.
475 13, these parameters are represented as the spatially-averaged values in each boxplot (i.e. each box plot
476 distribution represents 24 values corresponding to the spatially-averaged values at each hour). For OTCA,
477 however, the boxplot represents the spatial distribution at the pedestrian height, while the consideration of
478 the temporal variabilities is inherent to the OTCA calculations. We observe that the distribution of OTCA
479 is influenced by the combination of meteorological factors, which may have counteracting impacts on OTC
480 at certain hours. Additionally, the day of the simulation determines the sun path, and consequently shading
481 pattern and shade-to-sunlit ratio, which are critical in the spatial distribution of mean radiant temperature
482 as well as OTCA. These factors will further be altered by urban configuration and design elements (that
483 are kept constant here). This analysis further demonstrates that the comprehensive evaluation of OTC
484 performance in an outdoor space needs to consider both spatial and temporal variabilities in contributing
485 (meteorological and design) factors and represents the weather clustering method as an effective method of
486 achieving this objective.

487 Overall, such maps of OTC performance obtained on an annual basis can be employed for informing the
488 design decisions in the built environment. For example, the persistent zones of adverse thermal comfort
489 shown in this example can be ameliorated by using passive cooling systems such as shading devices, or in
490 the absence of such measures, the recommended use of the outdoor amenities can be limited. Nonetheless,
491 we note that the results presented here are meant as the demonstration of the prescribed methodology and
492 may not represent the final analysis for the case study of Singapore.

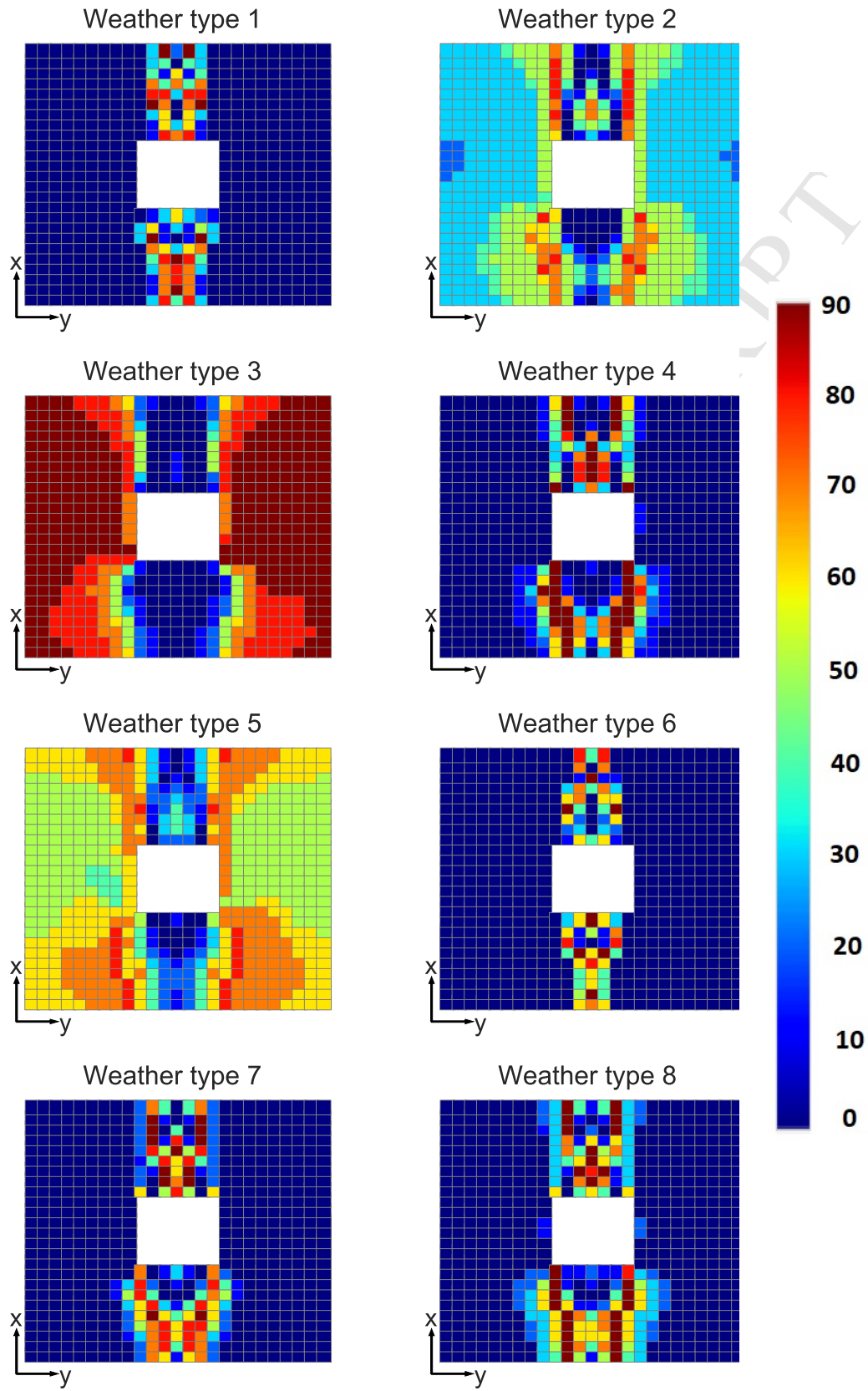


Figure 12: The spatial distribution of OTCA (%) at the pedestrian height ($\lambda_p = 0.0625$ shown in Fig. 11) for the different weather types represented in Table 2 and Appendix B. The color scale (shown in right) is kept consistent for all plots.

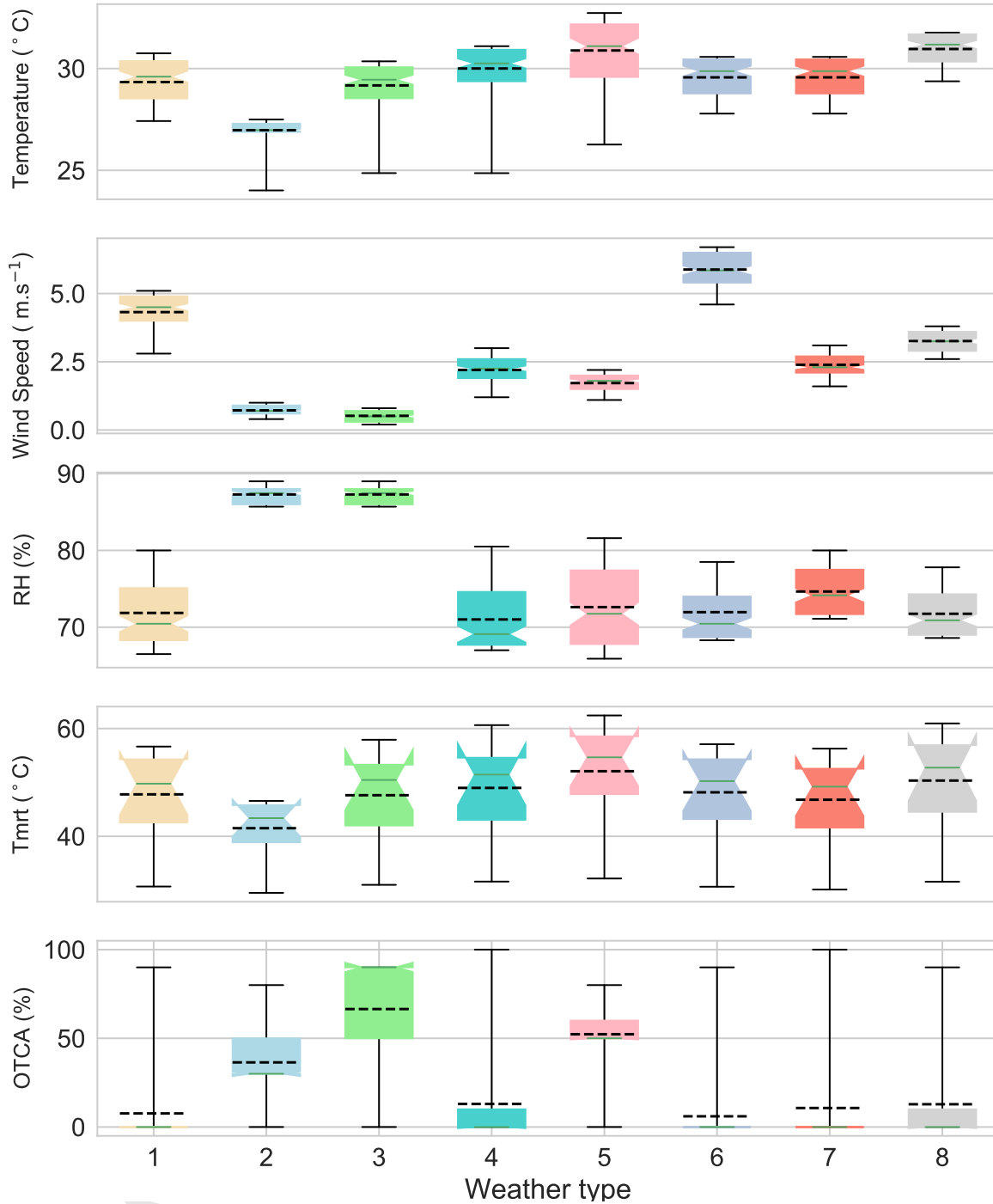


Figure 13: The notched boxplot distribution of hourly environmental parameters (such as air temperature, wind speed, and relative humidity - spatially averaged), hourly mean radiant temperature (T_{mrt} - spatially averaged), and the resulting spatial distribution of OTCA for each weather type (indicated in Table 2). The box shows the Inter-Quartile Range (IQR), that is the 25 to 75 percentile, that covers 50% of the data points. The whiskers are then extended to the minimum and maximum values. The horizontal green line and notch in the box plot indicate the median and the 95% confidence interval around the median, respectively, while the dashed black line is the arithmetic averaged. In the boxplot of T_{mrt} data, the distribution of data is skewed and the 95% confidence interval overlaps with the 75th percentile (3rd quartile), which explains the representation of the box.

5 Discussions regarding the use of comfort indices

In the present study, the performance metrics are calculated using the thermal comfort index SET. Here, we extend the discussion to consider other commonly-used comfort and heat stress indices. A recent comprehensive review of thermal comfort studies by Potchter et al. [46] reveals that out of 165 human thermal indices that have been developed, the most used indices for outdoor thermal perception studies are PET, PMV, UTCI, SET, and WGBT. Table 3 compares the range and descriptions of thermal sensation for these indices in addition to Wind Chill Temperature (WCT). For the indices that are based on the energy balance of human body, such as PET, SET, and UTCI, and described in temperature units, the calculation of OTCA and other performance metrics are as described before: First, the “thermal comfort acceptability criteria,” i.e. the thermal comfort range that describes the desirable OTC conditions at a specific outdoor space, is selected based on the thermal comfort index, and further calibrated based on the local climate as well as the desired use of the outdoor space. For example, in the case of Singapore, the acceptable thermal comfort range for a general-use outdoor space and based of SET calculations is found to be 20 to 28° [54, 64]. Using this range, the OTCA map as well as the spatial and continuous OTCA values can be calculated. Second, the critical temperature difference (Eq. 6) should be determined for the calculation of the Thermal Stress Indicator (i.e. the average deviation of comfort index from the acceptable criteria), weighted OTCA, and the frequency of the events outside of the acceptable criteria. The critical temperature difference is directly related to the acceptable range, but can further be modified to indicate the thermal stress zones. Accordingly, similar to the definition of WGBT, the deviation from the “comfortable” range prescribed by ΔT_{ave} can be classified in zones of low, moderate, high, and extreme stress. For the comfort indices differently prescribed, such as PMV, however, the calculation of critical temperature difference requires further investigation.

Table 3: Comparing thermal sensation based on various bioclimatic comfort/stress indices. The thermal sensation at each scale are taken from WGBT, WCT, and UTCI alert descriptions.

Thermal Sensation	Thermal Comfort Indices					
	PET	UTCI	SET	PMV	WGBT	WCT
Frosty (extreme hazard/Very strong cold stress)		-40 to -27				<-55
Very cold (very cold/Strong cold stress)	4	-27 to -30		-3		-54 to -40
Cold (cold/Moderate cold stress)	4 to 8	-13 to 0		-2		-39 to -28
Cool (moderate hazard/Slight cold stress)	8 to 18	0 to 9	<17	-1		-27 to -10
Comfortable (no danger/No thermal stress)	18 to 23	9 to 26	17 to 30	0	<18	>-10
Warm (caution/Moderate heat stress)	23 to 35	26 to 32	30 to 34	1	18 to 24	-
Hot (extreme caution/Strong heat stress)	35 to 41	32 to 38	34 to 37	2	24 to 28	-
Very hot (danger/Very strong heat stress)	>41	38 to 46	>37	3	28 to 30	-
Sweltering (extreme danger/Extreme heat stress)		>46			>30	-

6 Conclusions

For achieving climate-conscious urban design, comprehensive, accurate, and easily comprehensible evaluations of OTC are needed, such that the knowledge obtained from climatological assessments intersects the fields of architecture and urban planning. To respond to this need, we propose the first detailed description of metrics that quantify the performance of an outdoor space with regards to thermal comfort and heat stress. Analogous to “daylight autonomy”, widely used for indoor urban design [47], the concept of “Outdoor Thermal Comfort Autonomy” is introduced here, which evaluates if the available ambient and design resources are sufficient for an outdoor environment to be thermally comfortable or whether an adaptation strategy is needed. Additionally, the autonomy metrics are tailored to the unique characteristics of thermal comfort in an outdoor space, identifying the extent of deviation from the thermal comfort acceptability range as the Thermal Stress Indicator.

The proposed methodology for assessing the OTC performance through autonomy metrics does not intend to define a new thermal comfort index, but rather presents the means of translating the thermal comfort analyses using current indices into performance evaluations. The performance metrics discussed here introduce a comparative way of assessing design, identifying adaptation strategies, and facilitating climate-conscious decisions. We attempt to a) link human comfort to climate, urban fabric and design, and operation of an outdoor space, b) integrate the high spatial variability of thermal comfort with the diurnal and seasonal patterns in outdoor environments, and c) provide a rich visual feedback that can aid the decision-making process for urban design. Therefore, the methodology that is discussed here is representative of both performance metrics and design process as “the change in mental framework can inform a change in procedure” [30].

The use of performance metrics, such as OTCA, as design goals can enhance the communication of results and bridge the gap between scientific assessment and design decisions, and potentially aid the policy making in urban environments. Accordingly, the primary benefits of such urban design analysis include:

- Comprehensive metric for integrating spatial, temporal, and behavioral (such as occupancy hour and desirable comfort range) factors. The key advantage of dynamic performance metrics is that they consider the quantity and character of daily and seasonal variations of OTC for a given outdoor site together with irregular meteorological events.
- Comparative metric for assessing the adaptation and mitigation strategies. The use of a visual representation and simplified methods of communicating the results aids a holistic comparison of various adaptation and mitigation strategies proposed for enhancing thermal comfort in outdoor spaces.
- Quantitative metric for rethinking assumptions. While the final communication of results is simple and intuitive, the detailed consideration of various factors allows us to address various assumptions and complicated interactions in both urban design and assessment methodologies.

The contribution of this study goes beyond the definition of the performance metrics for OTC. In order to enable the scientists, designers, and architects to fully implement these metrics, we further discuss how to obtain comprehensive, accurate, yet efficient calculations. By discussing the limitation of the current microclimate models, we draw attention to critical factors, such as the 3D distribution of airflow in the

553 built environment and realistic shading patterns, which should be scrutinized for an accurate evaluation of
554 OTC performance. Additionally, we discuss weather clustering as an effective method for minimizing the
555 computational cost and complexities of calculating OCT performance, while not jeopardizing the important
556 variabilities in meteorological conditions throughout the year. In this way, we believe that the users not only
557 have the right tools for assessment, but would know how to use them efficiently and accurately.

558 The presented work describes the framework of evaluating the thermal comfort performance in outdoor spaces
559 that is first of its kind. However, certain limitations persist which are left for future works for enhancing the
560 analysis:

- 561 • There is a need for more comprehensive sensitivity analyses on the role of urban density, material
562 properties, and methodological assumptions on OTCA calculations. For instance, this methodology
563 can be applied in a range of different local climate zones [56] to demonstrate the intra-urban variability
564 in OTC performance, as well as assessing the impact of various mitigation strategies at various LCZs.
565 Additionally, the variability in OTC performance based on environmental parameters and various
566 climatic conditions can be assessed in future research.
- 567 • In the present discussion, transient behavior of pedestrians, and the subsequent effects on thermal
568 comfort, is not considered in the definition of performance metrics. Given that pedestrians are more
569 often moving through the outdoor spaces rather than staying for long periods, future research should
570 expand on the performance criteria that also includes a "temporal window" of comfort acceptability.
- 571 • The calculation of OTCA can further be extended for using not only "typical" but also "extreme"
572 meteorological condition for current and future scenarios. This methodology can be linked with the
573 measurement data, or the outcome of micro-/ and meso-scale (nested) modeling that predict extreme
574 heat events or future scenarios, and further translate the results into OTC performance metrics in the
575 face of such extreme events.
- 576 • In the present analysis, the measured data from the airport station in Singapore is used at the forcing
577 height above the urban canyon, while it is widely acknowledged that the recordings should be trans-
578 lated into forcing data at urban area. If such measurements are not available, it is recommended to
579 use numerical models such as Urban Weather Generator [6] or similar to obtain the meteorological
580 conditions at urban sites.

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APPENDICES

Appendix A - Specification of K-Means Method used for Clustering

The statistical k-means method has been applied to cluster weather types in Singapore. This method is based on the Squared Euclidean Distance (SED) between two data objects that can include one or more variables. The algorithm looks for the minimum value of the so-called “Within-cluster Sum of Squares (WSS)” defined as the sum of the squared differences between the observations and the corresponding centroid [43]:

$$WWS = \sum_{i=1}^k \sum_{x \in C_i} \|x - z_i\|^2 \quad (11)$$

where x denotes all the data belonging to the cluster C_i , z_i is the i th corresponding Cluster Centroid (CC) and k is the number of clusters. The minimum WWS is obtained in an interactive process that starts with the selection of CCs. The SED is calculated for each combination of CC and data objects. All data objects are assigned to their nearest CC to form the cluster. Data objects of each cluster are averaged to provide a new CC. This procedure of CC reassignment and calculation of SED ends when no data needs to be reassigned to another CC. The final CCs are unique for each cluster and represent all the data objects contained.

For the selection of the optimal number of clusters in which the yearly meteorological data should be divided, we have used the Dynamic Validity Index (*DVIndex*) developed by Shen et al. [53]. It is based on the assumption that clusters should be compact and well separated from each other. This is represented by the minimum value of *DVIndex*.

For each cluster k , the *DVIndex* is defined as

$$DVIndex(k) = IntraRatio(k) + \gamma InterRatio(k) \quad (12)$$

where

$$IntraRatio(k) = \frac{Intra(k)}{MaxIntra}, \quad (13)$$

$$InterRatio(k) = \frac{Inter(k)}{MaxInter}, \quad (14)$$

$$Intra(k) = \frac{1}{N} \sum_{i=1}^k \sum_{x \in C_i} \|x - z_i\|^2, \quad (15)$$

$$Inter(k) = \frac{Max_{i,j}(\|z_i - z_j\|^2)}{Min_{i \neq j}(\|z_i - z_j\|^2)} \sum_{i=1}^k \left(\frac{1}{\sum_{j=1}^k (\|z_i - z_j\|^2)} \right), \quad (16)$$

$$MaxIntra = \max_{i=1, \dots, K} (Intra(i)), \text{ and} \quad (17)$$

$$MaxInter = \max_{i=1, \dots, K} (Inter(i)). \quad (18)$$

Here, N is the number of data objects to be clustered, K is the pre-defined upper bound number of clusters (20 in our case), z_i is the CC of the cluster C_i , and γ is a tuning parameter (0.5) taken from Hoffmann and Schlünzen [18].

754 Appendix B - Clustered Weather Types Obtained for Singapore

755 The clusters have been defined using the following variables: daily mean temperature, daily mean temper-
 756 ature amplitude, daily mean vapour pressure, daily mean global incoming radiation, and mean u - v wind
 757 components. These daily values were obtained from the EnergyPlus Weather data (EPW file extension) that
 758 represents an hourly dataset of a typical meteorological year of Singapore. Fig. B.1 demonstrates the DVIn-
 759 dex for different numbers of clusters obtained using the k-means clustering procedure (detailed in Appendix
 760 A). The minimum DVIndex value corresponds to the eight clusters that were selected as the weather types.

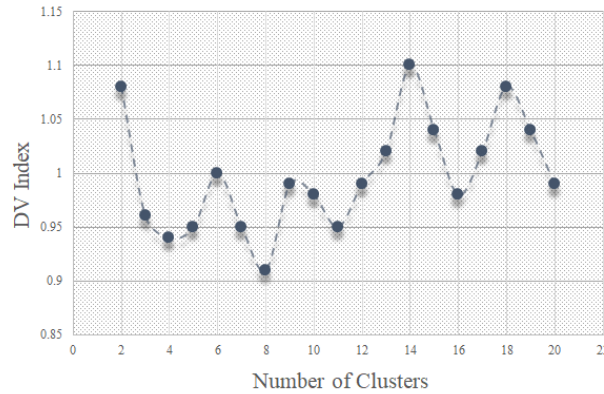


Figure B.1: DVIndex (Eq. 12) calculated for different number of clustered weather types.

761

762 Quantitative measures of the performance of the clustering procedure are presented in Table B.1. The best
 763 performance is for air temperature, relative humidity, and global incoming radiation. Although the Pearson
 764 correlation coefficient (R^2) is lower for the rest of the variables, the root mean square error (RMSE) presents
 acceptable values for a yearly thermal comfort analysis.

Table B.1: Quantitative measures of clustered hourly variables with respect to EPW file (on an hourly basis) for Singapore

Microclimate parameter	R^2	RMSE
Air Temperature (T_a)	0.706	1.2
Relative Humidity (RH)	0.686	5.7
Global Horizontal Irradiance (GHI)	0.930	68.8
Wind Speed (u-component)	0.565	1.5
Wind Speed (v-component)	0.422	1.2

765

766 Figure B.2 shows the diurnal variation in each of the clustered weather types for the variables that are
 767 relevant to the modelling of thermal comfort (see Sec. 4.1.1). The diurnal variations are well represented
 768 compared to the weather conditions in Singapore. For example, weather type 1 represents an overcast day
 769 with lowest daily maximum temperature (26.8 °C) and lowest global incoming radiation (negligible direct
 770 solar radiation) in Singapore. Wind speed is low (associated to calm conditions) and wind direction is from
 771 NE especially during the afternoon. Relative humidity values corresponds to the highest recorded value

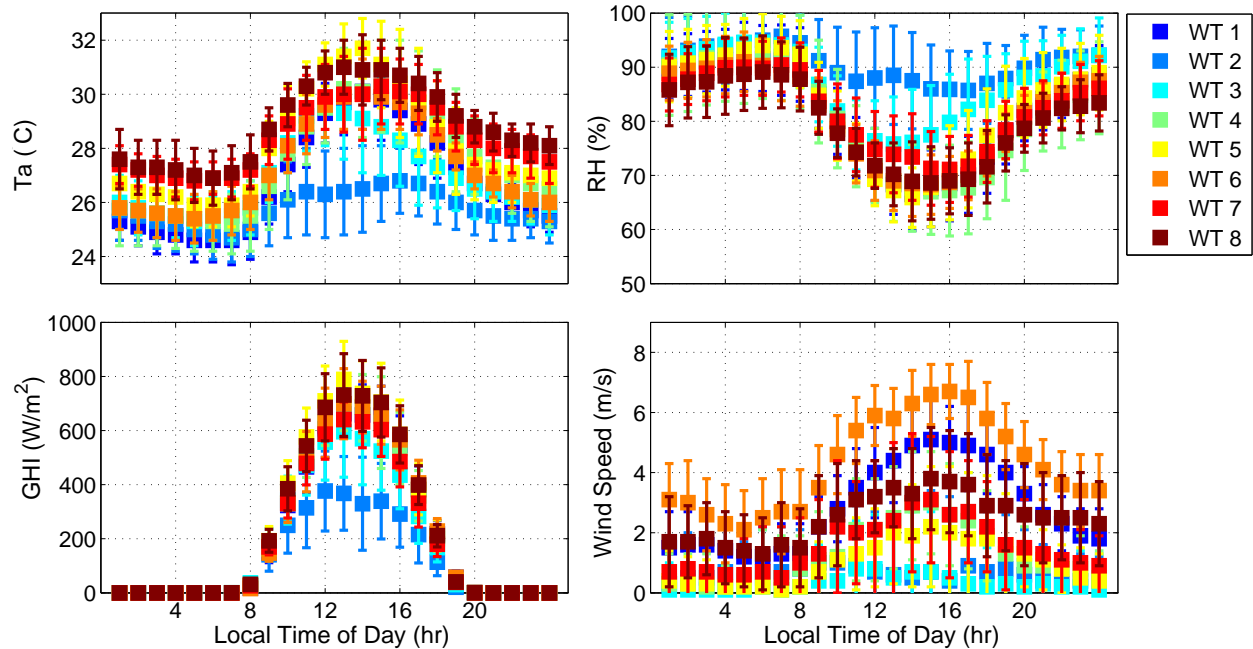


Figure B.2: Hourly evolution of air temperature (T_a), relative humidity (RH), global incoming radiation, (GHI), and wind speed for the 8 clustered weather types. The ID number for each weather type (WT) corresponds to Table 2.

772 in Singapore and precipitation is expected during these days. These climatic characteristics correspond
 773 to a typical day in the wet NE monsoon season but could also occur in other seasons. On the whole it
 774 represents 10.4% of the days of Singapore. On the contrary, weather type 4 represent a day with high
 775 maximum temperatures ($31.7\text{ }^{\circ}\text{C}$) and the highest global radiation (789 W m^{-2}) due to low cloud cover.
 776 Wind direction is constant from the NE and wind speed increases during daytime to more than 2 m s^{-1} .
 777 Daytime relative humidity values are low and no precipitation is expected during these days. This conditions
 778 are representative of the NE monsoon in the dry period that accounts for 16.7% of the days in Singapore.

Highlights

- Outdoor thermal comfort is critical for livability and should be considered in urban design
- We define 4 quantitative metrics to assess OTC performance in the built environment
- OTC metrics links comfort to urban climate, design, and the space operation
- Thermal Comfort Autonomy provides visual feedback to aid decision-making in urban design
- We observe the role of realistic microclimate representation on the OTC metrics
- We discuss weather clustering to reduce OTCA calculation cost and maintain accuracy