

Optimizing Inbound Freight Mode Decisions

by

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B.A., Middlebury College (2015)

Submitted to the Operations Research Center and Sloan School of
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and

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Abstract

Retail manufacturers often expedite inbound freight shipments from contract manufacturing bases to their distribution centers in destination markets at high cost to improve service levels to their wholesale partners and retail arm. The current process around these decisions has yielded lower than anticipated improvements to service level. This thesis (1) re-frames the goal of expediting inbound freight in quantitative, measurable terms that more directly impact the business outcomes, (2) develops an optimization model to select a set of freight shipments to expedite and best improve service, and (3) uses the optimization model to estimate potential improvement magnitudes with strategic changes.

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Note on Nike Proprietary Information

To protect information that is proprietary to Nike, Inc., the data presented throughout this thesis has been modified and does not represent actual values. Data labels have been altered, converted or removed to protect competitive information, while still conveying the findings of this project.

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Chapter 1

Introduction

This thesis proposes and outlines a solution for improving decisions around inbound freight mode selection. Many large companies rely on international shipping lanes to bring products from their origin to customers around the world. Shipping lines, air freight forwarders, rail companies, and trucking networks are some of the major players all competing for this freight business, each providing a unique mode of transport and value proposition to its segment of customers. This thesis details one way of determining how to most efficiently send product through these various modes to provide value for the large companies responsible for procuring and distributing products.

1.1 Introduction to the Footwear and Apparel Industry

The current landscape of footwear is dominated by athletics companies—Nike, Adidas, Puma, New Balance, Asics and others all earn billions of dollars of footwear revenue each year. For some footwear companies, apparel has evolved to become a co-equal pillar of the business. A simplified value stream for these four brands and for Nike’s competitors in general (adidas, Puma, lululemon, VF, etc.) is a system where products are produced by contract manufacturers around the world, sold to

these multinational brands (also called the ‘manufacturer’ throughout this thesis, as opposed to ‘contract manufacturer’), shipped to higher-income countries, then distributed and sold through a combination of wholesale and internal direct-to-consumer channels. As Phil Knight documented in his recent memoir, Nike was the first company to begin importing shoes from Asia to the US via a partnership with Onitsuka Tiger in the 1960s, and for the most part, the industry followed suit.¹ As it stands now, the vast majority of product is made in low-cost countries around the world like China, Vietnam, and Indonesia and transported to markets around the world. [9] [1].

The basic business model for manufacturers has shifted dramatically in the last 20 years. During the dot-com boom, Zappos, Amazon, and other direct-to-consumer e-commerce platforms began to challenge the basic wholesaler business model of the largest footwear and apparel brands [10]. Since the external innovations at the turn of the millennium, the largest brands now operate their own physical and digital direct-to-consumer platforms in addition to selling via dedicated e-commerce platforms like Zappos, and through the e-commerce and brick-and-mortar channels of their wholesale partners. These changes have impacted the way consumers interact with brands, with these large companies among the most eager to introduce omni-channel corporate strategy across supply chain, marketing, and endorsements. Where Nike and Adidas once relied purely on athletes like Franz Beckenbauer, Michael Jordan, or Billie Jean King to market their products, customers now interact with these brands via influencers like Kanye West and high-profile Instagram users as well as Serena Williams.

The flexibility and performance demanded from supply chains has increased dramatically due in part to the digital revolution reshaping consumer mindsets and expectations. One social media post advertising a new shoe will drive demand all across the world; different customers walking into a Nike store in Paris, a Foot Locker in Kansas or opening their phone to the Nike app will all expect to be able to buy the shoe that day. These demands require a fast, flexible, coordinated, and highly reliable

¹Textile manufacturing takes place around the world with New Balance notably still maintaining a major US manufacturing base.

supply chain that is being created within these companies. Asking the supply chains of twenty or even five years ago to fulfill that distributed demand in a coordinated way would be impossible or astronomically expensive.

1.2 Company Overview

Nike, Inc. is the world's largest footwear and apparel company with over \$39 Billion in revenue during the fiscal year ending May 2019. Nike, Inc. sells and distributes its products under four brands—Nike, Jordan, Converse, and Hurley, the latter two which operate as wholly-owned subsidiaries².

Nike has expanded dramatically since its beginnings in the Pacific Northwest. Today only 43% of its revenues come from North America, with the balance split approximately equally across Europe, the Middle East, and Africa (EMEA); China, Hong Kong, Macau, and Taiwan (Greater China); and Asia-Pacific and Latin America (APLA) [12].

1.2.1 Nike's Supply Chain Operations

Nike designers and researchers spend years developing technology and styles for future apparel and footwear products, but Nike's supply chain operations start months in advance of a sale and (returns notwithstanding) often end weeks prior to the end sale. In the months leading up to a season, Nike solicits orders from wholesale customers and develops internal predictions of demand. It orders product from contract manufacturers as Purchase Orders (POs), and as firm orders from its customers materialize, commits to delivering a Sales Order (SO) to its customers. In Nike's operations, and in this thesis 'customers' refers to external wholesale partners (Dick's Sporting Goods, Nordstrom's, Kohl's, etc.) and to internal customers responsible for direct-to-consumer channels, while 'consumers' refer to the individual actually purchasing product in stores or online.

²Hurley was spun off from Nike in October 2019

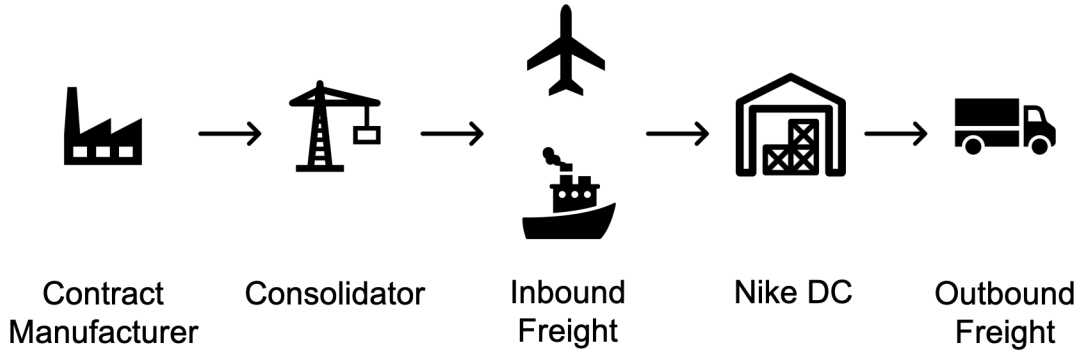


Figure 1-1: Simplified Sequence of Nike Supply Chain

In this thesis, we model the flow of inventory from the PO through the SO for North America. This flow generally takes one of two forms: the product is shipped directly to the customer’s distribution center, or the product is routed to one of Nike’s 6+ distribution centers in the US, then on to the customer. The product flows are split approximately 50/50 between these two channels for the North American market. The thesis focuses primarily on product that flows through Nike’s DC for reasons explained in Sec. 1.3.

In the vast majority of cases, the product will arrive at the departure port (in the country where the product was manufactured, most often Asia) and be placed on a ship to the US, arrive at port in the US where it clears customs and is placed on a truck to Nike’s or to a customer’s DC. In some cases, Nike will elect to divert a PO from the ship and instead fly product into the US, then truck it to the relevant distribution center. If that PO flows through Nike’s DC, the product will be allocated to a SO once it arrives at the distribution center. Once that SO is filled, all the product will ship out to the customer. See Fig. 1-1 for an overview of the supply chain for product routed via Nike’s DC.

1.2.2 Current Nike Strategy

Nike has always operated on the forefront of sport; to maintain that advantage, Nike announced the Consumer Direct Offense in 2017. The Consumer Direct Offense sets three ambitious goals known as the Triple Double: 2x Innovation, 2x Speed, and 2x

Direct to focus on innovative products; a fast and flexible supply chain; and emotional, personal connections with consumers, respectively.[11] As discussed in Sec. 1.1, the consumer landscape has changed to require the implementation of these ambitious goals in order to reach these consumers wherever they are—online, in Nike’s brick-and-mortar stores, or via wholesale partners. Nike’s biggest customers are facing similar issues and demanding high levels of service from Nike in order to meet these changing trends.

One lever to increase speed and flexibility is air freight. As diagrammed in Fig. 1-1, there is a choice of mode when product moves from consolidators in foreign ports like Hanoi to domestic ports such as New York. Sea freight is preferable for its low cost, and generally Nike’s supply chain can accommodate the long duration of trans-Pacific sailings. The choice to switch a PO to air freight can be made to react to outside factors, or to provide flexibility to Nike’s strategy. Outside factors include demand fluctuations, factory delays, and material constraints generally outside Nike’s direct control. Air freight may also be a strategic decision to better utilize factory capacity or allow for longer design windows while still meeting agreed delivery dates.

Nike relies heavily on its largest customers to plan and execute its strategies and to deliver its product to consumers. As such, Nike enters into agreements with its customers to ship product only when Nike can fulfill all or almost all of the order at once. For example, if a customer orders 10 units of product A and 20 units of product B, Nike will not ship product A in one shipment and product B several weeks later. The exact nature of these contracts are varied, time-dependent, and complex, especially when paired with allocation logic discussed in previous theses [8]. As such, it is difficult for a small group of people to manually make a decision about expediting (for example) 1000 units of product A. Coordinating arrival several weeks early to be able to say with confidence that more orders will be shipped to customers due to that earlier arrival is difficult as delays to companion products may delay outbound shipments.

1.3 Problem Statement and Motivation

The fundamental problem that this thesis addresses is the efficient utilization of resources for inbound freight for product that flows through Nike’s North America distribution centers. In order to activate the Consumer Direct Offense and increase the speed of its supply chain, Nike needs to know that a dollar spent moving product faster across the ocean will actually result in a customer getting that product sooner than they would have otherwise. This responsiveness to customer demands and efficient use of resources is crucial in a highly competitive retail market.

Shorter lead times throughout the supply chain can enable Nike to be closer to its consumers by changing supply levels to meet uncertain demand, to better capitalize on ethereal sports moments or brand heat events, and to bring new product innovations to consumers more regularly. Some work in this space will more fundamentally alter the supply chain, but there is an opportunity to make better decisions with the same infrastructure by quantifying value and using analytic frameworks to better understand the overall impact to the supply chain of individual decisions and drive more holistically beneficial decisions.

This problem also presents an opportunity for Nike to better understand more prescriptive analytics and its impact on internal company processes and supply chain outcomes. As such, this work focuses on the subset of Nike orders that flow through internal distribution centers. By focusing internally, Nike can have more control over implementation and performance measurement in the short term. In the long term, Nike views engagement with wholesale partners and smaller customers as crucial to its long term success, and performance improvement across its network of suppliers, internal business units, and customers will require spreading mechanisms for making better, more consistent decisions. This means that a natural extension of this work is understanding the relevant changes required to adapt these decisions to benefit the entire network.

1.4 Project Goals

The major contribution to Nike’s business process is a new model which evaluates the current state of the supply chain and order book and recommends decisions about the right set of products to expedite via air freight to improve customer outcomes. The model will take as inputs the current state of Nike’s orders and quantified values representing the priorities Nike places on certain products; the development of these inputs is discussed further. The model will then solve for efficient outcomes which are possible subject to supply chain parameters like travel and processing times and Nike’s constraints like available budget and procured air freight capacity. The goal of this model is not to recommend one scenario that produces the best outcome, but instead several different possibilities with tradeoffs between cost of service and quality of results. Understanding these tradeoffs will allow for a strategic decision about improving service levels or reducing costs.

Producing this new model will also require establishing a quantitative way to evaluate the outcomes of air freighting. This thesis also explores the quantification of the current business practices surrounding the air freight decisions and the establishment of a measurement of the benefits of air freight in addition to the costs. We measure the benefits of the current state and show how the model can be used to provide higher outcomes at lower cost.

1.4.1 Introduction to Approach

To provide relevant context to the methods, a summary of the approach is presented here, with more detailed discussion throughout the thesis.

We created a mixed integer network optimization problem, a simplified version is shown in Fig.1-2. This network flow approximation of the supply chain allows product to flow into the network as POs at the left, through nodes representing mode decisions and lateness choices before flowing out as SOs on the right. The model is formulated to maximize the value of the service provided—as determined both by the relative value of more on-time delivery vs. later delivery, but also the value of more

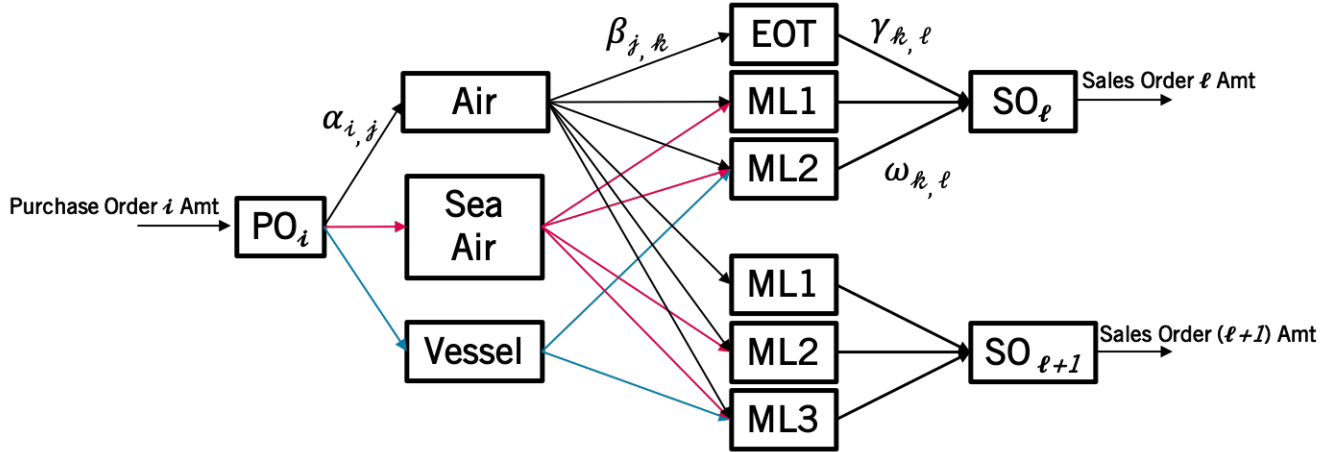


Figure 1-2: Simplified Network Model

important products. Key constraints assessed on the model include:

- **Budget:** as determined by the volume of product using a specific node
- **Lane Capacity:** certain transportation lanes have volume limits
- **Timing:** linking only the nodes corresponding to a feasible arrival date given the inbound mode and the shipment date required by the SO
- **Allocation:** linking product from a certain PO to a certain SO given the most recently available allocation forecast.

To determine the best possible options, we run the model with different budgets and maximize service in each case to see the tradeoffs between cost and service, and run useful sensitivity analyses to model the impact on these transportation decisions.

The rest of this thesis walks through the achievement of these goals with the following structure

1. Chapter 2 describes relevant optimization, supply chain, and transportation modeling, and how this work contributes to the literature
2. Chapter 3 evaluates the current business processes and a new proposal for evaluative metrics to improve the inbound freight process

3. Chapter 4 lays out the mathematical framework of the network optimization problem and how the modeling choices I made best represent business realities
4. Chapter 5 presents the results of the optimization model and several different scenarios for improving performance with specific customer classes
5. Chapter 6 discusses the recommendations and implementation strategies relevant to the model and its results

Chapter 2

Literature Review

Supply chain management has leveraged optimization for decades, especially over the last several years as optimizations algorithms and computing power have caught up with the scale and complexity of global supply networks. In my review of the relevant literature, I find that the basic principles leveraged in this thesis have been used time and again in adjacent questions, but low-level decision making such as freight mode choice for each order has not leveraged these tools. Due to the market dynamics and impact of the air freight decisions, it will be important to make good decisions about the use of air freight in the future. This section explores the industry, its dynamics, and the importance of air freight decisions in the near future.

2.1 The Air Freight Logistics Industry

The state of the global air freight market suggests that this is a key area to invest in better decision making. While the total cost of logistics in the United States has hovered around 8% consistently for the last decade [13], the air freight industry is forecasted to continue to grow approximately 4% annually over the next 20 years, growing 10% year-over-year as recently as 2017 [5]. Air cargo transportation accounts for less than 1% of total trade by volume while transporting over 35% of global trade by value. In order to compete with such high-value goods in the transportation network, retailers with lower input costs and value-to-volume ratios will need to be

exacting in their use of air freight or else risk paying premiums to compete with high value products. The air cargo industry's frequent fliers: consumer electronics, flowers, fresh fish, and specialized equipment can all justify air freight premiums due to infeasible alternatives or inventory holding costs, while traditional textile retailers look at this premium as a potential saving if slower, cheaper modes are suitable for market needs.

Despite the premium on air freight and the explosive growth of the industry, textiles have actually been increasing their market share in the key lane from East Asia in to North America [5]. Between 2016 and 2017, apparel's market share grew 14% over the year to represent 15% of the total tonnage between the two regions. The air freight industry between East Asia and North America has been dominated by China-US trading of late. Chinese exports now represent approximately half of all East Asian air freight exports by weight, up from 14% twenty years ago. The Chinese growth corresponded to a shirking of Japanese exports over the same time frame, and now seems to be threatened by a booming Vietnamese economy as textile, footwear, electronics, and machinery manufacturers look for cheaper labor outside China and seek political stability and supply base diversification.

This theme is replicated across other regions as well. In both East Asia-Europe and intra-East Asian air freight trade, China has grown to become the dominant power in the region while the growth in peripheral economies threatens to reduce Chinese market share, if not their gross freight value or volume.

2.2 Carbon Emissions and Business Context

Climate change is the single most impactful issue for humanity today and likely will be for the foreseeable future. A recent UN report forecasted mass extinctions, rising sea levels, and widespread famine, droughts, and poverty within in the next 20 years if humanity continues to pollute the atmosphere with greenhouse gasses [14]. A 2014 report by the UN attributed 15% of global greenhouse gas emissions to the transportation sector, the fourth largest group behind electricity and heating, farming

and agriculture, and industrials.

With nonexistent political leadership on climate change in the United States, corporations have begun to impose goals on themselves above and beyond standards imposed by the government in areas like emissions, labor sustainability, and overall environmental impact. This change is a notable departure from policies of just 20 years ago and is due to many factors. In 1998, a group of petroleum majors spent millions of dollars lobbying against US ratification of the Kyoto Protocol as part of a general strategy to make regulations favorable to major emitters of carbon [6]. Now, Chevron publically advertises its climate change initiatives—though its core business model has not materially changed [4]. Experts cite many reasons for these shifts, not least of which being the mountain of scientific evidence, but consumer perceptions of brands, customer choice in the market, and a dearth of political will are all cited as factors [17].

As companies look to reduce their environmental impact and improve the public perception of their sustainability, the supply chain is a natural first place to look. As mentioned, transportation is a major source of carbon emissions. The transportation mode as well as the distance travelled are the two main factors impacting the scale of carbon emissions for moving a given product from source to consumer. The World Shipping Council estimates that the carbon impact per weight and distance travelled is over 100x higher for air freight than ocean freighter and over 5x higher than heavy-duty truck [15]. In comparing ocean freight to air freight in intercontinental shipping, ancillary over-land routes taken by rail, inland waterway, or truck may change the exact factor by which air freight generates more carbon, but the order of magnitude of air freight emissions means that any air-based route will substantially out-emit any sea-based route.

Despite the outsize per-unit air freight carbon impact, ocean freight is estimated to be responsible for some 2% of global carbon emissions [15]. In the early 2010s large ocean freight vessels began ‘slow-steaming’ in an effort to curb rising fuel costs and save fuel over the course of the journey by reducing speed [19]. This has the added benefit of reducing emissions from ocean freight, but causes capacity constraints,

longer lead times, and increased inventory costs due to the increase in time ships take to sail across the ocean. This practice has mostly reversed in the years since oil prices spiked, and environmental groups have advocated a regulatory approach to reducing speed. The current climbing oil prices may bring back the practice on fuel economics alone [18].

2.3 Supply Chain Freight Optimization

Bravo and Vidal establish a review of freight transportation modeling in supply chain optimization models and find several trends both in the last few years and over the last decades [2]. First, they find that researchers favor an integrated optimization approach over a hierarchical one. Much of the literature around freight optimization also takes the size, location, and function of supply chain network nodes as variables. In cases where these factors are co-optimized with freight considerations, results are superior to a staged approach where the network is set then freight decisions are made.

Combining both the network design and operational decisions is not entirely straightforward. Cardona-Valdes et.al. formulates a bi-objective problem where the network design problem is formulated as a combinatorial assignment of plants I to locations J and serving customers K via those paths at some location and mode-dependent cost [3]. The use of a bi-objective framework has the feature of not identifying one particular optimal solution but instead outlining a pareto frontier of optimal solutions given different weights to the two objective functions—in this case cost of the network and time required to deliver to customers. A drawback of the pareto frontier is that the methods do not provide direction on where on the frontier would be best to operate—that comes from the business realities surrounding the problem. In practice, a sharp transition in the shape of the pareto frontier may suggest a highly sensible operation point.

While this bi-objective approach was preferred to a purely sequential optimization, there was a trend in the papers reviewed by Bravo and Vidal of using cost

minimization as the objective function for the vast majority of problems. In implementing optimization, cost minimization has the obvious advantage that the solution provided will cost less than any other feasible set and is therefore palatable to business users. It is also the most easily quantified parameter of the supply chain. It is perhaps no surprise that the business function often viewed as a cost center is ubiquitously modeled as a cost to minimize in the academic literature.

One work that attempted to move away from a purely cost based view of supply chain optimization was Paksoy et. al. [16]. The paper is in some way a prototypical supply chain cost optimization to minimize costs by directing product from manufacturers through distributors to retailers given different costs of each path. They introduced a layer of complexity by making the quality of the products a decision variable and introducing a probability of rework to penalize low quality. This approach struggles to correspond to a complex evaluation of the tradeoffs of just-in-time, e-commerce, or large retail supply chains, but instead is an interesting extension of Juran's optimal quality tradeoff as applied to network optimization. The concept is feasible if cost and quality are as inexorably linked as to provide an exhaustive explanation of the value of the supply chain. However, other factors like timeliness, completeness of order, and historical service levels will impact the value customers receive from a high-functioning supply chain and are difficult to capture in one metric of quality, and the average rework required given a level of quality.

The framework that this thesis follows can be seen in Diabat and Simchi-Levi's paper exploring shipping choice in a carbon-constrained world [7]. The problem is a supply chain network optimization involving the choice of distribution center locations and customers to serve from each location, subject to a constraint on the amount of carbon that can be emitted transporting the goods from each DC to all customers. The objective function used to position the DCs and allocate shipping lanes minimized the cost of the total network subject to a total carbon emissions constraint. Various scenarios with different carbon constraints then sketched out a pareto frontier showing the tradeoffs between minimal supply chain cost and the carbon emissions of the network. Assuming that there is generally some cost benefit

to increasing carbon emissions, this pareto frontier shows the tradeoff of reducing carbon emissions and reducing costs through the supply chain.

Chapter 3

Objective Function Determination

Key to developing and communicating an optimization framework for decision making is understanding the business goal the model will improve and translating it to a mathematical formulation. Related analyses have shown that a high proportion of the goods air freighted to market were not shipped out of distribution centers quickly and the outbound shipment dates could likely have been met by using slower inbound modes. The analyses also found that an important factor in these goods remaining stagnant in the DCs was due to incomplete orders: high importance goods were ordered on the same order as lower importance goods, and all units need to be available in order for the order to ship out.

Below, I lay out the current metrics used to track inbound freight results, their shortcomings, and the business processes surrounding the air freight decision. I then propose a service-level maximization objective function subject to budget constraints and motivation for that decision.

3.1 Current State

3.1.1 Purchase Orders

Purchase Orders (POs) are the unit of supply to the manufacturer and the unit of communication between the manufacturer (brand) and a given contract manufacturer.

Purchase Order	Item	Size	Quantity
A1	1	S	50
		M	100
		L	50
	2	S	20
		M	40
		L	20

Figure 3-1: Example Purchase Order

See Fig. 3-1 for an example of how a PO is structured. In this figure, the brand places an order with one supplier to produce all 280 units of product and deliver it to the manufacturer. This delivery happens at a consolidator at the port of departure in the country of the contract manufacturer (e.g. Hong Kong). Only once this product has been delivered does the manufacturer take control of the inventory financially and operationally. To not waste time, the decision about which mode to ship the PO from the departure port to the DC is made prior to the PO's scheduled arrival at the departure port.

As shown in Fig. 3-1, the POs are often written to have standard size curves, or proportions of each size of a given product. As these are relatively similar across each product category (e.g. shirts, pants, shoes), we model all sizes of each item as a single SKU (e.g. a red t-shirt) as opposed to disaggregated by size (e.g. a medium red t-shirt). Customers also order in similar size curves as shown in the next section so the assumption is consistent throughout. This will lower the number of items by an order of magnitude.

Finally, while in reality a PO has several different items on it (red t-shirts, white t-shirts, etc.), each PO line has only one item (e.g PO A1, Item 1 is one 'line') as shown in Fig. 3-1. The decisions about shipment mode are made independently for each PO line (i.e. each item). Therefore, for the definition of the model, a 'PO' is actually a PO line. This allows for modeling the unit of measure at which the shipment mode decision is actually made. These units are only one item and can be readily shipped without the other items on the overall Purchase Order.

Purchase Order	PO Product	PO Product Quantity	Allocated Quantity	Sales Order	SO Product	SO Product Quantity
A1	1	200	125	1X	1	175
		200	75	2Y	1	125
	2	80	40	1X	2	40
		80	40	3Z	2	40
B2	1	100	50	1X	1	175
		100	50	2Y	1	125

Figure 3-2: Example Allocation Between Purchase and Sales Orders

3.1.2 Sales Orders

Analogous to a PO, a Sales Order (SO) is the unit of demand for products and the unit of communication between a retailer and the manufacturer. Typically, a large proportion of SOs are established prior to the POs, i.e. the manufacturer gets a good idea of the demand in the marketplace prior to telling the contract manufacturers what to make. This makes planning easier and more accurate. The manufacturer will write the POs based on the SOs that come in, adjusted by forecasts internal to the manufacturer about how demand may change as time unfolds.

The general structure of an SO is identical to the PO as described in Fig. 3-1. The SO represents a sale of products from the manufacturers to its customers. Sales orders are compiled together by the manufacturer and POs are written to the contract manufacturers in order to fulfill the demand. At the time when the POs are delivered at the port, there exists an allocation of the PO orders to the SO requests. An example of this allocation is shown in Fig. 3-2. While this allocation may change during shipping or at the DC, this work assumes that the allocation known at the time of shipment remains the same throughout the rest of the process.

Unlike the PO, the unit of decision is the entire sales order, with multiple items from different POs all arriving and being shipped out together. It is crucial to the customer that the different items arrive at the same time (like a matching pair of shorts and shirt), so the SO remains a multi-item object in the modeling while each PO in the model is a unique item.

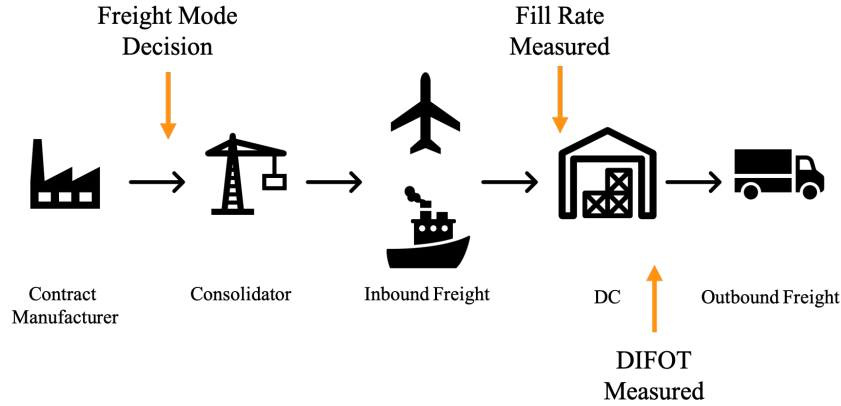


Figure 3-3: Simplified Supply Chain with Decision and Metrics Timing

3.1.3 Relevant Metrics

Most supply chain decisions like shipment mode are made before contract manufacturers deliver products to the manufacturer. The efficacy of all decisions are measured across the industry by commonplace ex-post metrics counting the proportion of orders that were complete by required outbound shipment date and how close incomplete sales orders were to complete. Complete SO metrics include ‘Delivered In Full and On Time’ (DIFOT) or what percentage of SOs met all constraints. Incomplete metrics measure how close sales orders came to being in full and on time—for example fill rate of a given order measures the percentage of product that is available on a certain order at a certain time.

Metrics like fill rate are important for tracking internal performance of the supply chain, but focusing too much on improving fill rate can lead to pyrrhic victories. For example, fill rate increasing from 70% to 80% may not improve service if fill rate must be at least 90% on a single order for the manufacturer to ship the product to the retailer without contractual penalties. While improving fill rate is likely to correlate to improving customer service, modern techniques make it possible to attempt to instead directly improve complete order metrics like DIFOT. An optimization based framework can take into account these strong non-linearities where simple heuristics and goals may fail.

See Fig. 3-3 for a process flow diagram outlining the process with decision and

metric measurement timing within it. Crucially, fill rate is a metric internal to the distribution center, but DIFOT measures the outbound performance of the DC, which the customer will also see.

For our task specifically, any expedited order will improve the fill rate by increasing the fill rate at time t or by making the order full at $t' < t$ or both. However, this may not improve the DIFOT metric as expediting late product may not be sufficient to trigger the shipment conditions to have the product ship earlier. The non-linear relationship between expediting and DIFOT improvement is precisely what makes optimization algorithms an attractive link between data and improved outcomes. Highly manual decision processes are bound to target more linear relationships like fill rate as opposed to non-linear metrics like DIFOT. Regardless of the metric targeted for improvement, the modeling has fundamental information constraints, discussed below.

A key previous analysis attempted to identify the ex-post effectiveness of expediting an order by building a counterfactual inventory position if the order had not been expedited. If the actual shipments of the product would have caused the distribution center to stock out in the counterfactual world, then the shipment is labeled ‘effective’. This analysis showed that a large portion of the expedited items were ineffective—largely due to expedited products sitting in the distribution center waiting for other products to arrive and the shipment to fill up to an adequate level to be shipped.

3.2 Existing Process

Currently, each month planners sit down with account managers and evaluate the current state of the supply chain and the expected service levels. Where service levels are unsatisfactory (for example, product class A for customer X is on average trending late for 50% of sales orders), products from the given product class will be expedited on SOs that are allocated to that customer. There is a budget target for all expediting across all customers, and the most strategically important customers hold the most

sway.

Due to the transit times available from shipping providers, the decision of freight mode choice takes place before relevant data may be available. Decisions about freight mode are made up to a month before the order arrives at the departure port, and over two months before the estimated arrival time at the onshore distribution center (assuming product is shipped by vessel). During these two months, several important factors can change or become known (such as actual consumer demand), so many decisions are made with limited data.

Current processes heavily weight the input of customers, as they have a crucial consumer-facing perspective of what types of products (materials, colors, or styles) are selling well at full price from different manufacturers. The input from these customers does not take into account tradeoffs between customers or the overall cost of the system, so costs increase easily without a full understanding of what expedited shipments will truly add value to the customers writ large.

The advantages of the highly manual system include an understanding of customer needs for expedited supply and the root causes of those needs, be it imminent unmet demand, a promotion, or key products for internal marketing. People understand better than a machine what the end customers want to feel from their manufacturers and how those needs have been met in the past. With that in mind, we set out to develop a method that would leverage the prioritization and customer service intuition developed from a largely manual process and incorporate modern analytics to better meet the targets the process is already striving towards.

Finally, the current business process has variable budgets depending on the available resources and the nature of the supply chain service levels. Therefore, the initial budget decisions about air freight spend are to be made in a separate environment from the tactical decisions of which POs to expedite. With that in mind, the proposed approach will allow for the most important decisions to be prioritized regardless of the budget.

The stakeholders in this process were not dissatisfied with several of the fundamentals of the process—a monthly review time seemed satisfactory, the level of engagement

was good, and parties understand that this process can be improved either by lowering costs, increasing effectiveness, or both. The stakeholder process to determine an effective way to augment this decision with analytics explored many options, and the most effective is summarized below.

3.2.1 Process Outputs

This consultative stakeholder process ends with a determination of the shipping mode for each PO. As discussed, this decision is made for each item separately, allowing for red t-shirts to be air freighted and white t-shirts to go by sea, even if they were ordered from the contract manufacturer together and we refer to each item on its own as a PO.

This mode choice can result in product being shipped by air, by sea, or by a new combination mode called sea-air where it is ocean shipped to a different port then air freighted the remainder of the way—generally at a slightly lower cost to basic air freight. Mimicking this output is the chief actionable decision of the model. These decisions go to the consolidators who follow the instructions about how to ship the product, and also to internal transportation teams who work to secure the specific capacity necessary. This portion of the process remains largely unchanged but will be working with different decisions after the implementation of the optimization model.

3.3 Proposed Changes

This optimization model will fit into a business decision process that is mostly unchanged. The decisions will still take place approximately monthly, and during that process, the shipment modes will be decided for the orders that are arriving at departure ports in the next month. This means that the model will not have to run particularly quickly, but will need to fit into the current workflow well and be flexible.

The model will use an objective function that will maximize service levels subject to a budget constraint, with service levels defined below but crucially shifting the measure from inbound service to outbound service (i.e. no reward for air freighting a

product into a DC, only a reward for shipping it out of the DC).

There are several other options for evaluating efficiency of production that we did not pursue. One straightforward option is to evaluate the costs and benefits of the target decisions in the same units (often currency), and maximize the profits subject to constraints. While this would be a clean way to determine the best outcome, it is not the method we chose primarily due to the difficulty generating a currency-based metric that accurately represents service levels. Not only is an estimate of revenue or profit based on when a product is delivered to a customer very uncertain, the retail space has many other factors influencing how much more valuable a given product is on time than it would be if it were late. The amount of marketing spent for the product from the selling brand or the point-of-sale retailer, the availability of substitutes, presence of other brands, presentation of the product with a suite of complements, and the relationship history between the wholesaler and retailer all factor in to the value of on-time delivery of a certain product. Fully incorporating all of these factors into an accurate dollar impact, let alone dollar impact per unit was not feasible. Given the uncertainty of such a measure, it would not combine well with the relative certainty of the financial costs of the network for a single unit. Instead, we focused on a non-financial measure of value for each product, and maximized that value subject to a cost constraint on financial expense.

These confounding factors suggested leveraging the human intuition surrounding the decision processes, as the end business objective is customer satisfaction at reasonable cost and the people involved in the decision have years of experience. The goal then is to standardize and quantify the intuition so that the best decisions can be scaled across the entire set of orders.

During several workshops with the stakeholders, we developed metrics to quantify the tradeoffs between different categories of goods and different lateness of delivery. See below in Fig. 3-4 for an illustrative chart showing categories of products and the relative value of each. Crucially, we standardized the process by implementing the following key ideas:

1. **Perishability:** A quantitative representation of the value of a product category

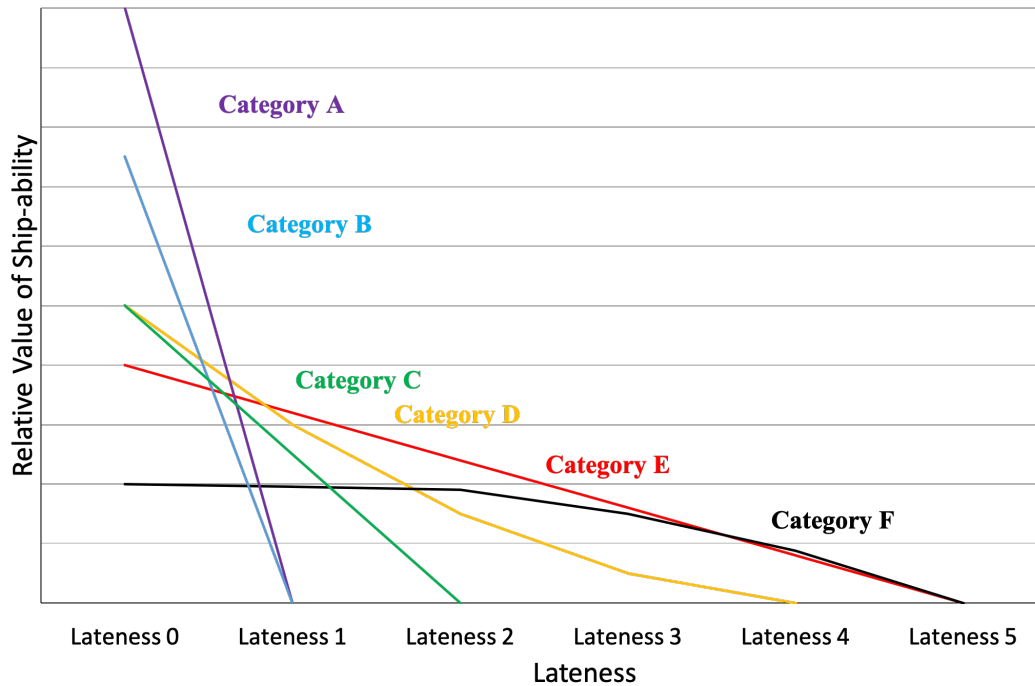


Figure 3-4: Perishability and Relative Value by Category of Product

as a function of when it ships to the customer.

2. **Categorization:** Each product belongs to one of several product categories to simplify the tradeoffs between products.
3. **Reference Value:** A consistent value across all product categories where the value of products is equal. See the bottom right of Fig. 3-4 and note that no matter which category a product is in, all products are worth the same in the final lateness category.

Perishability

This approach institutes the idea of perishability into the decision, highly related to product obsolescence. Retailers thrive on new, innovative products but the life cycle of those products can be dangerously short. For example, imagine a ‘Boston Marathon 2020’ T-shirt that may be classified as Category A or Category B in Fig. 3-4. This type of product is highly perishable, if it doesn’t reach shelves before a

very short window (often minutes or hours for some product), it is worthless. This life cycle is important to note because it could be the case that product could be expedited to make it less late, but not to make it within a window of value. These lost causes may as well be placed on a ship, given they will have to be sold at a discount or loss anyway. Conversely, a simple black pair of shorts may be in season for months or years, and lateness has less of an impact on the value of that product. Only once contractual charges come into effect does lateness severely impact the value to the manufacturer.

Reference Value

The tradeoffs between different category perishability begins with an equal starting point. In the case of Fig. 3-4, each unit of product is worth the same if it is delivered during Lateness 5. While this is not a reasonable assumption on its face given the difference between the value of a high end pair of shoes and a pair of socks, it is a reasonable approximation of the profits on the sale. If customers cancel or return very late product, a reasonable assumption is that the manufacturer recovers its cost by selling the product at cost through discount channels. The value of each category can then be compared to this reference value when product is in lateness category 5. As explained above, this 'at-cost' worthlessness can be true for much earlier delivery categories for more perishable product (see product categories A and B immediately becoming worthless).

3.4 Use in Optimization and Communication

This classification and quantification feed directly into the objective function for the optimization problem. The exact formulation is described in Sec. 4.1, and follows the idea that a product of a given category arriving at a given lateness will have value as shown in Fig. 3-4. The model has the ability to improve this objective function by deciding to ship product by faster modes to arrive during better lateness times. This will incur higher costs, so the model must choose to expedite the units that will most

cheaply improve the total value.

Two specific improvements that can be seen purely from this formulation are the abandonment of lost causes and optimal tradeoffs. First, imagine a product in Category A which will arrive in Lateness 5 via the slowest (and cheapest) shipping mode and will arrive in Lateness 1 via the fastest (and most expensive) mode. In this case, the framework will show that both outcomes are equally bad, with arrival at Lateness 1 costing much more. Second, in a case where two products are both arriving in Lateness 2, where one is Category C and another is Category A, expediting both products to arrive in Lateness 0 will set up a scenario where the increase in value due to the Category A unit is twice the increase of the Category C unit. If the Category C unit can be expedited for less than half the cost of the Category A unit, then the model will choose to ship two Category C units over one Category A unit. In general, products have remarkably similar shipping costs, so Category A will be prioritized over Category C.

One way that was effective in communicating the concept of relative value and confirming the relative values of each category is to look at the implied values of one ‘point’ given the approximate margin of each category. See Table 3.1 for a table showing an example of the decrease in value of each category if it moves from Lateness 0 to Lateness 1. Using approximate data on the margin earned by a product in each category, we can use the difference between the value attributed to each category between Lateness 0 and Lateness 1 to calculate the implied probability of cancellation, and ensure that the results approximate reality. For example, we can see that our customers would behave similarly with respect to Category A or Category B products being Lateness 1 or greater—they would immediately cancel the order. The value to the manufacturer is different between the categories because of the margin difference, not the a difference in the customer’s behavior. A contrasting pattern can be seen by comparing Categories C and D, where the margin earned by the manufacturer on each product is similar, but a higher value is assigned to Category C being Lateness 0 over Lateness 1 than is assigned to Category D. This would then imply that though the manufacturer is indifferent between either product selling, due to the retailers

Table 3.1: Example of Tradeoffs to Calibrate Objective Values

Category	Normalized Value of Points Difference	Normalized Margin	Probability of Cancellation
A	100	100	1.00
B	75	75	1.00
C	25	50	0.50
D	20	50	0.40
E	8	20	0.40
F	1	20	0.05

higher likelihood of cancelling a product in Category C, it ought to have a higher on-time value to the manufacturer.

Chapter 4

Formulation of Model

The mathematical formulation of our model is a tiered network flow model where the flows between nodes represent product, and each product must flow through four tiers listed below. For mathematical notation, the four tiers are indexed by i , j , k , and l , respectively.

1. The Purchase Order Tier: One node for each purchase order
2. The Mode Tier: For each purchase order, one node per viable shipment mode
3. The Lateness Tier: For each sales order, one node per viable lateness of that order
4. The Sales Order Tier: One node for each sales order

Product flows through exactly one node in each tier from purchase to sales order through one each of three types of edges on the network, labeled α , β , and γ , respectively. These are discussed more in Sec. 4.1.1

1. $\alpha_{i,j}$ the flow from PO tier node i to mode tier node j
2. $\beta_{j,k}$ the flow from mode tier node j to lateness tier node k
3. $\gamma_{k,l}$ the flow from lateness tier node k to SO tier node l

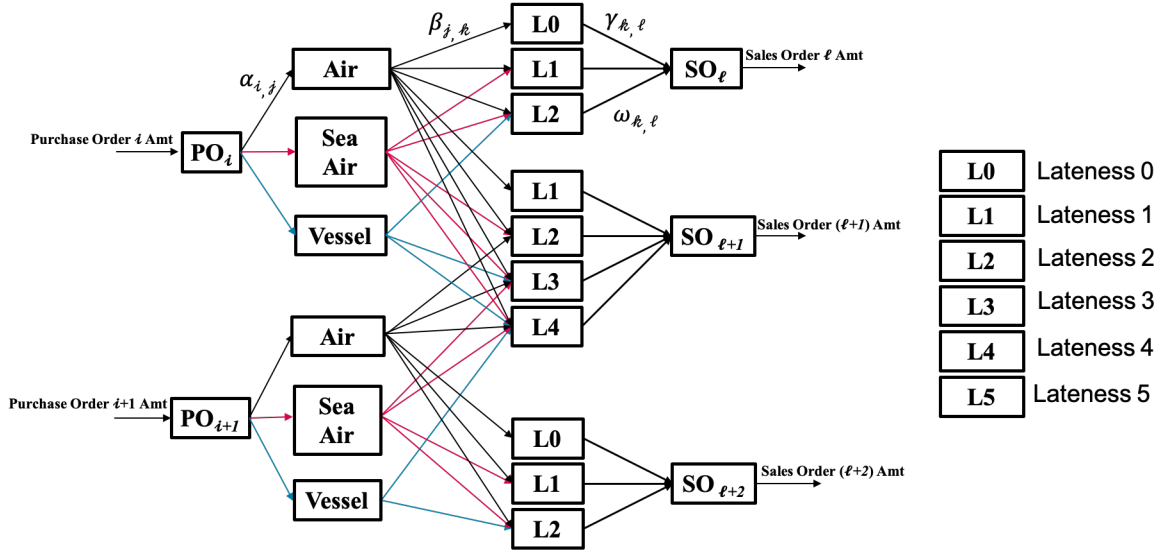


Figure 4-1: Illustrative Diagram of Model.

Before diving into the mathematical mechanics, there are a few assumptions I made which are summarized below and help explain the translation to the real-world decision process discussed in Chapter 3.

- Each PO has a given number of units of one item associated with it, and each SO has a given number of units each of several different items on it. The allocation of which POs deliver what quantity of items to which SOs is fixed and taken as given.
- The timing of the POs arrival, mode-dependent travel times, and dates required for SO latenesses to be fulfilled is all deterministic, fixed, and taken as given.
- This model is intended to be run approximately monthly and the chief actionable output is the transportation mode decision for each PO¹

See Fig.4-1 for an illustrative diagram where each tier of nodes is represented as a column of boxes and each type of edge the connections between them. The first two and last two tiers have relatively simple flows: the number of products on each purchase and sales order is fixed *a priori* which fixes the flow into and out of the

¹In reality, PO line, recalling the discussion in Sec. 3.1.1

system. The flows from each purchase order to its associated mode tier nodes is allowed (and no flows to any other purchase order's mode tier nodes are allowed). Similarly, each lateness tier node has a connection to only one sales order node. The connections between the mode tier and lateness tier nodes are more complicated. The allocation between a PO and an SO is fixed *a priori* and a connection is established between a given mode node and lateness node if and only if product is allocated from the PO associated with the mode to the SO associated with the lateness *and* the timing of shipping that PO via the associated mode will allow for delivery to the SO at the specified lateness.

Qualitatively, the definition of these connections is how the timing constraints of the order book are represented in the network structure. See Fig. 4-2 for a timeline of important dates and their relevance to the model determination. For the example PO and SO in the figure, the red dots are dates that are set contractually and taken as given. The consolidator processing time, mode-dependent transit times, DC processing (inbound and outbound) and outbound shipment times are all random variables in reality, but are assumed to be constants. The consolidator processing time and DC processing and shipment times are added to and subtracted from the consolidator arrival date and customer arrival date, respectively to get the two black dots (dates) in the figure. These dates are also taken as fixed and given. The time between these two dates relative to the mode's shipment time determines the earliest possible lateness available between the PO and the SO of interest via that mode. More concretely, in Fig. 4-2, air shipment would allow for delivery by lateness 0 (or later), sea-air would allow delivery by lateness 1 (or later), and vessel shipment would allow delivery by lateness 2.

This means that between the PO and the SO represented by the example Fig. 4-2, β decision variables would be established from the 'Air' node to all latenesses, from the 'Sea-Air' node to lateness nodes 1 and later, and from the 'Vessel' node to all latenesses 2 and later.

Allowing product to flow through the network in specified ways emulates the timing of the order book. The constraints on the lateness variables using binary

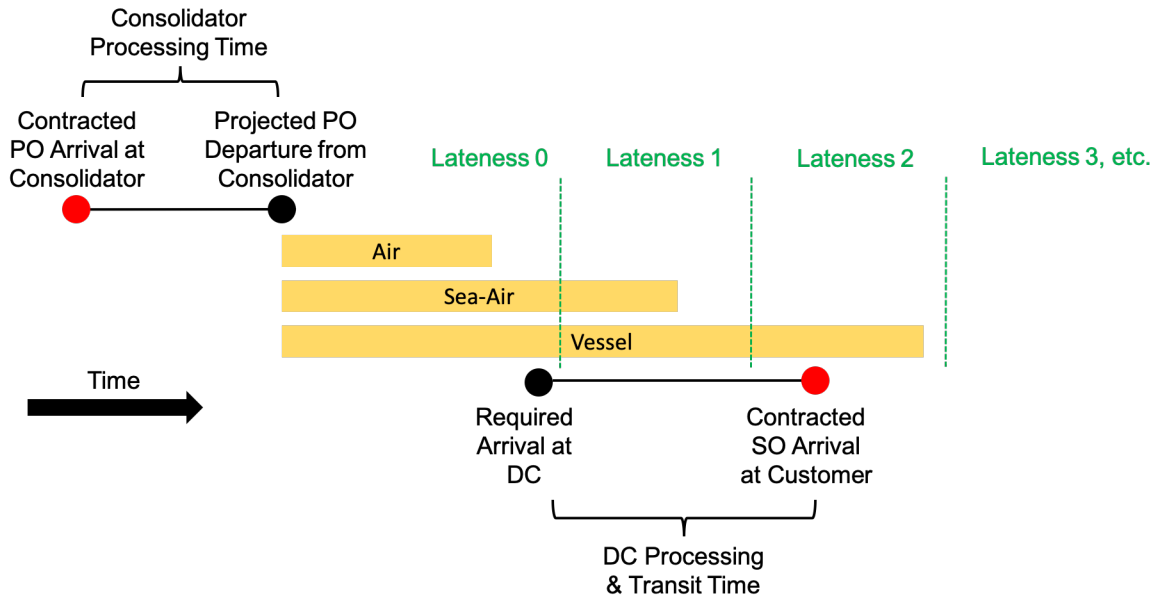


Figure 4-2: Timeline of Key Dates and Lateness

variables are the key to mimicking the idea that orders cannot be shipped until they are sufficiently full. This is mathematically defined below but works as follows:

- Each flow from a lateness node to its SO has two decision variables associated with it: γ and ω .
- γ is continuous and represents the number of products flowing, while ω is binary and represents a choice to service the SO primarily through that lateness
- One set of constraints forces γ to be sufficiently high (e.g. at least 90% of the total SO quantity) if the associated $\omega = 1$
- One set of constraints forces there to be exactly one ω equal to 1 for each SO
- The objective function is a function of ω , rewarding only the lateness when the vast majority of the order is shipped. This choice is further discussed in Sec. 4.1.3

4.1 Mathematical Model Definition

4.1.1 Decision Variables

The decision variables generally refer to the amount of product flowing on each of the edges in Fig.4-1 shown as arrows labeled α , β , and γ . The decision variables labeled ω are binary variables described above. We also create a slack decision variable $LaneSlack_{Cntry,Mode}$ to help constrain the air freight capacity out of individual countries depending on procured capacity.

- $\alpha_{i,j}$: This is a binary decision variable to denote that PO_i will travel by mode j , where $j = 1, 2, 3$ corresponding to vessel, sea air, and air modes, respectively. Each PO_i will have three $\alpha_{i,j}$ variables associated with it representing the choice of one of three modes. This decision variable is different from β and γ in that it does not represent the number of units flowing along the path. For constraint sum notation, we define a set J_i where $|J_i| = 3$ and the elements are the three indices of j for the associated Air, Sea Air, and Vessel nodes.
- $\gamma_{k,l}$: These decision variables are similar to $\alpha_{i,j}$ and represent the lateness choices for each SO (rather than the mode choices for each PO). For each SO l , the first lateness defined is the earliest time that the first unit allocated to SO_l can arrive by the fastest shipment mode. The last lateness is the latest time that the last unit allocated to SO_l could arrive by the slowest shipment mode. All lateness levels between these two boundary levels are also defined. Each $\gamma_{k,l}$ is non-negative and represents the number of units on SO_l that are fulfilled via lateness k . These values are most readily constrained by ship-ability constraints, discussed more in Sec.4.1.3. Again for notation, we define a set K_l where the elements are the indices of k associated with the various lateness times that can service SO_l .
- $\beta_{i,j,k,l}$: This is the number of units from PO i shipped by mode j to serve PO l via lateness k . These variables are the flow from the mode nodes to the lateness nodes and are the mechanism that link POs and SOs. This variable is created if

PO i has product allocated to SO l and choosing mode j will allow that product to arrive by lateness k . Like γ , they are non-negative and represent number of units flowing.

- $\omega_{k,l}$: These binary decision variables are associated one-to-one with $\gamma_{k,l}$ and represent the choice to service SO_l primarily through lateness k . As such, exactly one $\omega_{k,l}$ variable is required to equal one for each set of $k \in K_l$.

4.1.2 Objective Function

As explained in Chap. 3, we have defined the relative value to the manufacturer of various product categories as a function of lateness of the product and maximize this value subject to budget constraints. This allows for a fairly simple objective function. Each SO l will have various quantities of different products, and the value of all of these products being shipped at a certain lateness k can be calculated and is a constant for each SO and each lateness called $V_{k,l}$. The objective function is then simply the sum of these constants times the associated decision variable $\omega_{k,l}$, a binary decision signifying if that product was shipped at that lateness.

This has some drawbacks that will be discussed in Sec. 4.1.3 further, but allows for a linear function of the value of the product dependent on when that product is expected to leave the manufacturer's distribution center for the customer. The model is run with a budget constraint, then a pareto frontier is defined by running several cases with various budget levels.

4.1.3 Constraints

The constraints can be broken into four general classes:

1. **Balance Constraints:** Force the flows into and out of each node to be equal.
2. **Allocation Constraints:** Force the product from a certain PO to flow to a certain SO in some way to ensure all product goes where it was ordered.

3. **Fill Rate Constraints:** Forces one of the lateness nodes to have at least a certain fraction of the total units for each SO. Meant to model requirements at manufacturer's distribution centers that require some amount of the product for a certain order to be available before a job is created to pick, pack, and ship that product.

4. **Other Business Realities:** Including system budget constraints, shipping mode lane capacity constraints, and inability to split POs across multiple modes.

Using the sets of decision variables described above, the optimization problem takes the following form.

$$\alpha, \beta, \gamma, \omega, LaneSlack \quad \max \quad \sum_{k,l} V_{k,l} \omega_{k,l} \quad (4.1a)$$

s.t.

$$\sum_j \alpha_{i,j} = 1 \quad \forall i, \quad (4.1b)$$

$$\alpha_{i,j} * POAmt_i = \sum_{k,l} \beta_{i,j,k,l} \quad \forall j \in J_i, \quad \forall i, \quad (4.1c)$$

$$\sum_{j \in J_i, k \in K_l} \beta_{i,j,k,l} = AllocQty_{i,l} \quad \forall \{i, l\}, \quad (4.1d)$$

$$\sum_{i,j} \beta_{i,j,k,l} = \gamma_{k,l} \quad \forall k \in K_l \quad \forall l, \quad (4.1e)$$

$$\sum_{k \in K_l} \omega_{k,l} = 1 \quad \forall l, \quad (4.1f)$$

$$\gamma_{k,l} + M * (1 - \omega_{k,l}) \geq ShipThresh * SOAmt_l \quad \forall k \in K_l \quad \forall l, \quad (4.1g)$$

$$\sum_{i,j} Cost_{i,j} * \alpha_{i,j} + \sum_{Cntry, Mode} LaneSlack_{Cntry, Mode} * Overage_{Cntry, Mode} \leq TotalBudget, \quad (4.1h)$$

$$\sum_{i \in Cntry, j \in Mode} POAmt_i * \alpha_{i,j} - LaneSlack_{Cntry, Mode} \leq LaneSize_{Cntry, Mode} \quad \forall Cntry, Mode, \quad (4.1i)$$

$$\alpha_{i,j} \in \{0, 1\}, \quad (4.1j)$$

$$\beta_{j,k} \geq 0, \quad (4.1k)$$

$$\gamma_{k,l} \geq 0, \quad (4.1l)$$

$$\omega_{k,l} \in \{0, 1\}, \quad (4.1m)$$

$$LaneSlack_{Cntry, Mode} \geq 0 \quad (4.1n)$$

The four classes of constraints are discussed further below, non-negativity and binary constraints 4.1j through 4.1n are discussed above in Sec. 4.1.1.

1. **Balance Constraints:** Constraints described by equations 4.1b, 4.1c, and

- 4.1e, ensure that product flows from PO nodes to SO nodes in one path. They (in order) require one order to flow out of the 'PO' node via exactly one of the mode nodes, the binary mode choice to match with the equivalent units that flow from the mode node to the lateness nodes, and finally from the lateness nodes to the sales order nodes.
2. **Allocation Constraints:** Constraint 4.1d enforces the allocation of product from purchase order i to sales order l by requiring the sum of all relevant β variables to equal the allocation quantity constant ($AllocQty_{i,l}$).
 3. **Fill Rate Constraints:** The order fill rate is governed by constraints 4.1f and 4.1g. Constraint 4.1g is a big M integer constraint requiring γ to exceed some fraction of the total Sales Order (or shipment) quantity if the associated ω is equal to one. Constraint 4.1f forces exactly one ω to equal one for each Sales Order. The ShipThresh constant could in theory vary for each Sales Order, but for most analyses presented in this thesis is set at 95% for all SOs. These constraints represent another aspect of the service level that the manufacturer delivers to its customers. When a shipment leaves the manufacturer's distribution center for delivery to the customer, a certain fraction (hopefully all) of the order must be present in order for the order to meet contractual obligations between the manufacturer and the retailer. In reality, these specifications can be complex and specific, but this model approximates these requirements with a simple requirement that at least some fraction (95%) of all product must be present for the order to ship.
 4. **Other Business Realities:** Constraint 4.1h restricts the total budget, while 4.1i restricts the shipment capacity by country while allowing for more expensive per-unit overages via slack variables.

The way the objective function is formulated in combination with the fill rate constraints is one high impact decision on the interpretability of the optimization. There are two principal options: a weighting coefficient times each ω variable (used)

or a weighting coefficient times each β variable (not used). Using β or ω as the decision variables in the objective are the two choices that maintain the spirit of the Fill Rate constraint. Each has a benefit but also allows for different pathological cases rewarding when product is actually delivered or rewarding when the order the product is on satisfies the fill rate constraint. In each example, imagine a SO with several different products, and relatively small amount (not enough to preclude satisfying the shipment threshold constraint) of very valuable product.

When using β , we gain the benefit of only adding to the objective function when each individual item arrives, but we could imagine a scenario where the valuable product arrives very early, crediting the objective function for early delivery without having enough of the order to allow for shipment that early. Conversely, while using ω , the vast majority of product could arrive very early while the valuable product is late. The order looks like it is ship-able early and the objective function is credited for delivering the entire order, despite some valuable product arriving later.

The pathological β case was deemed more likely to happen due to the low cost and high reward of the case and the likelihood of additional business processes preventing the pathological ω case with check-ins on valuable product. Therefore, we chose to use ω as the decision variable in the objective function.

4.2 Sensitivities and Extensions

4.2.1 Parameter Sensitivity Analysis

The Mixed-Integer formulation of the model precluded the use of shadow prices on constraints to easily determine the marginal impact of changes in constraints on the objective function, so I evaluated the impact of changing the fill rate requirement for shipments and the requirement that inbound orders be shipped as whole orders. The first involves changing the 95% threshold discussed above to values of 50%, 80% and 90%, while the second involves relaxing the constraint that α is a binary variable and instead allowing it to take any value between 0 and 1.

For the fill rate constraint, the discussion immediately prior to this section is highly relevant. When relaxing the constraint away from a 100% requirement, the approximation of the entirety of the order being fulfilled in the week in which the fill rate requirement is met becomes less accurate and the modeling suggestions more tenuous to claim will lead to positive real world outcomes.

The α decision variables can be relaxed from integer to continuous on the set $[0,1]$. This means that only a fraction of the PO is shipped by certain modes instead of the entire quantity of items being shipped together. The correlation to realizable outcomes under the current setup becomes near impossible to draw, but the modeled benefits do provide concrete business case grounding in the potential benefits to implementing more advanced processes to allow for split shipments and partial expediting. This would allow a PO that has mostly on-time product on it to carve off part for air freight but leave the rest for vessel shipping.

4.2.2 Forecasted Demand

A third ‘parameter’ that I tested the sensitivity was more structural to the model—the timing of the order and the requirement that the order be delivered when the customer said it ought to arrive. Often times the actual consumer demand lags the customer demand significantly. If the manufacturer can predict this lag and work to service consumer demand, that would buy the supply chain time to use slower shipment methods. The goal behind altering this constraint is to evaluate the benefit to inbound shipment expediting if the manufacturer were better able to predict end consumers consumption and deliver to customers to meet that demand in lieu of delivering to the customers’ stated preferences. Many products are ordered on contracts that run throughout the duration of the season, so customers may order several months of supply on a contract for arrival at the beginning of the season, only to need a fraction of the product immediately. While this is a small impact of a more parsimoniously run supply chain, there should be myriad reasons for a just-in-time arrival system to meet customer demand, and I investigated the impact on inbound freight expediting.

This is a two step process: first, finding consumer demand and the discrepancy

from customer's stated demand, and second predicting this demand early enough to differentiate the inbound freight service based on meeting consumer demand. In this study, we use one customer as an example where the retailer has significant insight into their operations and these data are readily available. This would require significant insight into point-of-sale data to understand how each customer sells products to consumers, so I evaluated it on one customer first to identify the maximum opportunity size that could be attained before investing in premier consumer prediction and stronger data sharing relationships.

Chapter 5

Optimization Results

The results presentation uses differences between scenarios to drive conclusions and recommendations. The model is run with different constraint parameters and the optimal output describes the set of actions that would elicit the best service level in that situation. Specifically, the following three sets of scenarios form the basis of the results:

1. **Vessel Only:** This case is a floor on the service level showing the best possible service level if all products are forced to move through the slowest mode. This case solves very quickly, as the mode choice decision variables are fixed for each order, and the service levels are strictly increasing as earlier service levels are chosen for each delivery.
2. **As Planned and As Executed Reality:** These cases are meant to mimic reality and represent the service levels given the as planned transportation modes (when the POs were originally written), and the as executed transportation modes (after the one-month prior process to incrementally air freight products). The discrepancy between the two is the process that this tool aims to augment: the manual switching of orders from slow to fast modes approximately one month prior to shipment. Similar to the Vessel Only case, these cases take the decisions about mode for each order as fixed and the model optimizes service level quite simply.

3. **Optimal Scenarios:** These cases have unconstrained modes for each purchase order and a budget constraint to restrict spend. Shipping orders by faster modes incurs higher costs and penalizes the budget constraint. The model then can fully optimize for shipment mode across the entire order book. Different cases at different budget levels then create a pareto frontier delineating the trade offs between cost and optimal service level.

5.1 Analysis of Potential Improvement

Below the results are discussed from one representative month: the data included are the order book for one month of orders filtered to the product allocated to Distribution Center orders for the top 20 customers who have received product by air freight (those customers account for some 70% of air freight volume, while the Distribution Center orders are about 50% of total volume, as discussed earlier). The resulting set of orders is some 15,000 SOs and 20,000 POs, with over 600,000 possible combinations of PO, shipment mode, lateness, and SO. These figures are relatively consistent across the recent months used for internal analyses, and the results shown in the discussion below are generally representative of the results in all months. This monthly analysis filtered to customers with high air freight usage is the setup under which the model will be run when implemented. These decisions are the ones the end users are looking for guidance on as they represent the vast majority of the discretionary expedite decisions.

The optimal scenarios sketch out a pareto frontier where service level is maximized subject to budget constraints. The best strategy for the manufacturer under the service level tradeoffs established by the perishability in Sec. 3.3 is at or between one of the points labeled in orange in Fig. 5-1. The ‘As Planned’ scenario is made months in advance when the orders are first written, so it is expected that the scenario will not be optimal as more information becomes available. However, under the current paradigm, the blue ‘As Executed’ scenario shows the current state after re-evaluating the shipments prior to arrival at port. One way to examine the success of

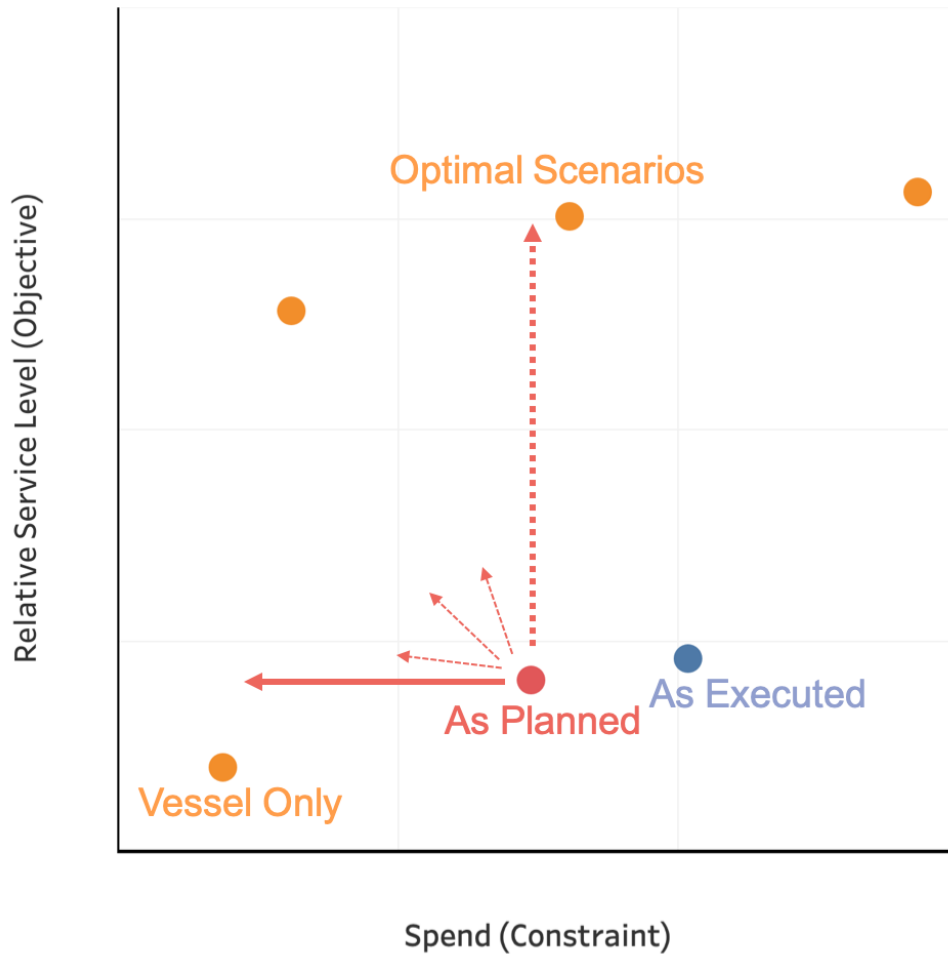


Figure 5-1: Budget and service level by scenario.

this optimization is to move in any direction between the solid and dashed red arrows in Fig. 5-1, shown by the small arrows.

The lack of a unifying metric relating service level to supply chain spend or to profit mean that it is beyond the scope of the optimization as formulated to prescribe an optimal spend along this frontier of scenarios. However, the multiple scenarios can provide guidance about where a sensible spending budget would be based on the retailer's implied value of increased service level. This concept is illustrated below in Fig. 5-2. By choosing either the 'As Planned' or 'As Executed' scenario relative to the 'Vessel Only' case, we can approximate the average value of the increased service level as the slope of the line between the two points¹. The slope of this line

¹Using the 'As Planned' scenario is shown in the chart

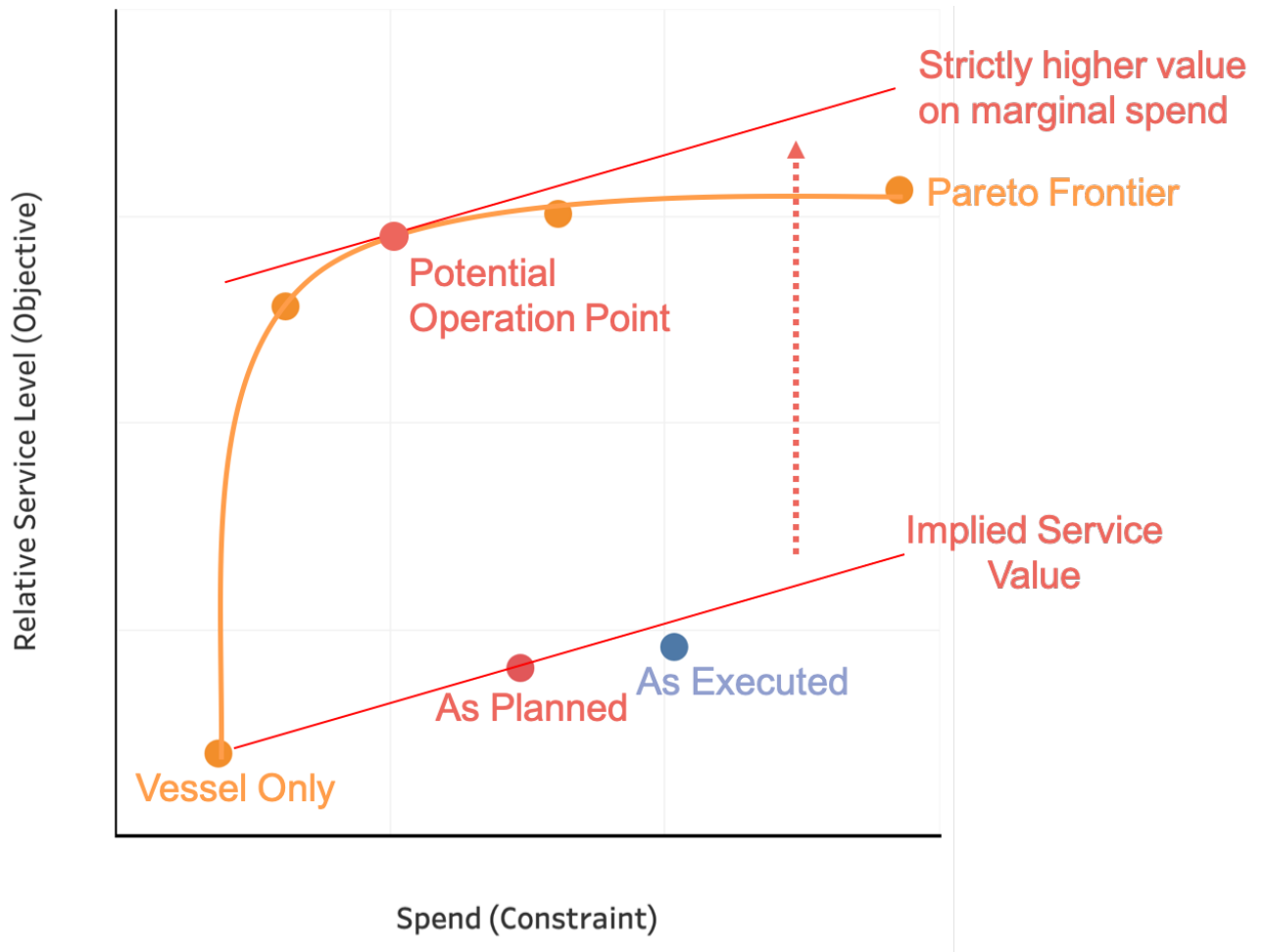


Figure 5-2: Value of service approximation

is some measure of the average value that the manufacturer currently generates from expediting product. If we see where on the pareto frontier this line would be tangent, we know that operating at that point would mean that the marginal investments in budget up to that point generated a strictly higher return than the current case does on average: a point at which may be straightforward to convince business users to operate. This may not be the point at which the business decides to operate, but by viewing the decisions in terms of these shadow prices to determine the value of increasing budget, we can begin to put the decisions made along the pareto frontier in an understandable business context.

More simplistically, the trend of the diminishing returns with the size of the expediting investment is easy to see through the basic results of Fig. 5-1. There are

Table 5.1: Units by Shipment Mode and Lateness

Lateness	Air Freight			Sea Air			Vessel		
	Actual	Planned	Optimal	Actual	Planned	Optimal	Actual	Planned	Optimal
Lateness 0	69,665	123,777	138,870	378	25	73,425	2,000,855	1,956,028	2,114,934
Lateness 1	22,079	30,477	58,515	10,546	4	3,064	1,147,047	1,141,044	1,074,805
Lateness 2	18,743	12,823	20,257	2,440	-	8,638	604,649	623,961	663,665
Lateness 3	58,277	39,115	2,848	-	-	1,570	376,228	360,771	212,863
Lateness 4	51,346	14,250	7,136	-	-	9,442	914,196	877,952	460,676
Lateness 5	88,154	53,450	16,110	16	-	864	1,951,927	2,082,869	2,448,863

This is example data from the actual and planned scenarios and an optimal scenario with a budget approximately equal to the actual amount spent.

large service level gains to be had through a small use of expediting, but the marginal returns trail off very quickly. It is also evident that the optimization formulation is significantly better at identifying those opportunities than the manual processes, as shown both by the low relative level of the manual process outcomes, but also by the relatively small gain between the ‘As Planned’ and ‘As Executed’ scenarios. The cost increase between those two scenarios could capture the vast majority of service level increases the optimization can deliver.

5.1.1 Implementing Improvements

The analyses above show that there is plenty of room to improve, and that the optimization can identify different sets of purchase orders that will lead to higher service levels than the current solutions. In lieu of blindly following the optimal results, we can see why the optimal cases perform better than the current solutions and what strategies may need to be employed to achieve those results.

There are a few patterns in the table that are useful for informing future strategy decisions and investigating why air freight spend may have been high in the first place relative to the service level. First, we see that the actual and planned scenarios both have a significant amount of air freight in latenesses 3,4, and 5 relative to the optimal scenario. Specifically, we see that there is some >60% increase in the amount of air freight arriving in lateness 5 between the planned and actual scenario. An air freighted lateness 5 unit in the ‘planned’ scenario is a unit that was scheduled to be

air freighted when written then ends up arriving via air very late (e.g. through factory delays). The incremental addition of lateness 5 air freight units in the ‘actual’ scenario means a PO was projected to arrive very late via vessel, and even after being manually switched to air freight during the switching process was still projected to arrive very late. This increase in lateness 5 units from ‘planned’ to ‘actual’ is interesting as the model would never choose to air freight products in the last lateness if it could be avoided as the last lateness category is open ended and could therefore always be achieved by vessel².

It is therefore crucial to understand why this product was shipped in reality and how those attitudes can impact or be impacted by the modeling runs. The takeaway from additional analyses and discussions was that a large amount of long-lifecycle product has been on backorder from several customers. Planners are therefore choosing to air ship the product into the market where it is often consumed almost immediately. This leads to a continued dearth of product and the cycle continues. This satisfied demand therefore generates much lower margins than it would have had it been shipped by sea. The counterargument is that the demand may have disappeared by then if the market is not continuously supplied when the manufacturer decides to switch from air to ocean freight. These discussions were crucial to understand the motivations for air freighting, the potential limitations of the model, and some decision patterns that may be worth revisiting after the modeling runs. While the product is in demand from customers, more investigation is needed if air freight is the best way to acquiesce to those requests and if it improves the long-term outcomes of the manufacturer’s operations.

There is also a curious result surrounding the heavy use of sea-air in the optimal scenario. The modeling parameters I gathered suggest that the use of an intermediate, slightly cheaper but slower mode of transportation would be advantageous. The use of sea-air is in its infancy and the procurement costs and estimates are mostly forward-

²The 16,110 units air freighted amount in lateness 5 shown in Table 5.1 are due to the integer constraints of the shipping mode and is 0 in scenarios where the shipment decision variables are continuous. This product is on POs where some allocations are for earlier SOs (lateness 0-4) and some is allocated to SOs that choose lateness 5.

looking instead of based on years of experience of costs, advantages, and flaws. As such, capacity has been kept low as the mode experience expands. However, the modeling shows that often air freight provides unnecessary speed to the supply chain, and the use of a slower, cheaper option could save costs at comparable service. One caveat is that the sea-air option is only very slightly cheaper and significantly slower, so there could be fixed costs that are not included in marginal shipping rates with establishing a robust third shipping option. The linear model will tend toward cost savings no matter how incrementally small. These results however do show that there is significant opportunity for air-freight-based solutions that are slower and cheaper.

5.1.2 Solver Decisions and Model Solve Time

In this implementation-minded modeling approach, the base results of the current operations guided the choices surrounding modeling detail and solver parameters. As discussed with Fig. 5-1, the current manual executions were not capturing a significant portion of the value shown to be possible through optimization. Implementing the optimal solution at comparable budget as current levels suggested a very large service level increase over the current operations, so the focus quickly shifted from finding the provably optimal solution in each case to finding a good solution, and for the results shown here and through the stakeholder process, the MIP gap for solver optimality was set at 5%. This large gap was implemented to improve the run time of the branch-and-bound search over a large solution space, and to show to business users that near optimal (and significantly improved) results could be found in a time palatable for incorporation in their workflows. The large MIP gap did however hinder the exploration of understanding exactly the optimal improvements with very high spend as various optimal runs with different budget constraints may return identical solutions, but these questions were purely academic, as such high budget spends were impossible³. Gurobi generally followed a similar trend for all cases and found solutions

³For example, the two highest budget cases in Fig. 5-1 have a budget above the ‘Vessel Only’ case that differs by a factor of two, but the difference in optimal solutions is less than 5% and therefore within the MIP tolerance

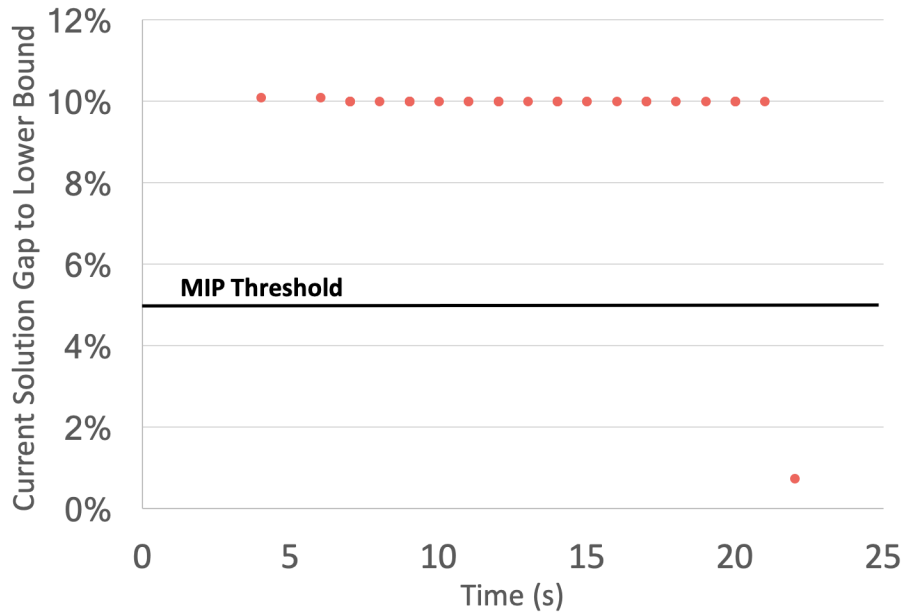


Figure 5-3: Typical Gurobi MIP Gap Pattern

well within that tolerance, however there were certain cases that were exceptions, and a 5% gap was palatable to the business users, so it remained in place.

Most runs also demonstrated a similar pattern in not making notable changes to the best bound on the solution in order to trigger quitting the solve, but instead found significantly better solutions at the end of the solve than the incumbent solution it had for most of the solve process.

5.2 Sensitivity Analyses

The base case conclusions use multiple cases across various budget levels to evaluate the efficacy of different strategies. It is also important to look at the sensitivity to other assumptions to stress test the results and glean insights about the usefulness of the modeling presented here.

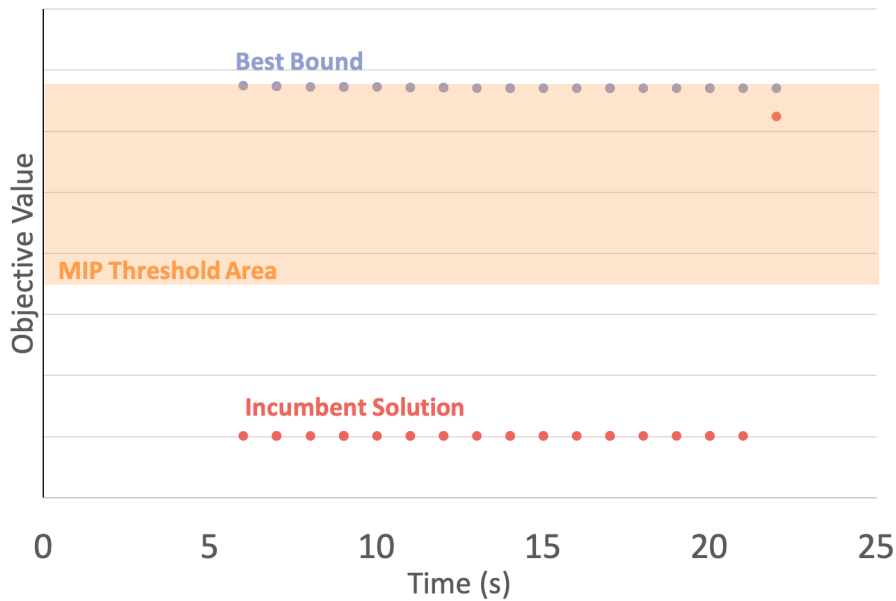


Figure 5-4: Typical Gurobi Solution Pattern

5.2.1 Fill Rate Sensitivity

This set of sensitivity runs evaluates the model’s reaction to changing parameters associated with the fill rate constraint level. As discussed in Sec. 4.1.3, the base results use a 95% threshold. In Fig. 5-5, the pareto frontiers achieved with different threshold levels are presented. Due to the desire to maintain linearity, the objective function is credited with the delivery of the entire order if the minimum fill rate is met. Shown in the figure is one impact of that decision: for fill rate requirements of only 50%, the service levels are shown as higher in the optimization problem due to the relaxation of these constraints. If half of all product arrives in Lateness 0 and half in Lateness 3, the 50% fill rate case counts the entire order (via the sum of the categories of its constituent products) as Lateness 0, while the 95% fill rate case would count the entire order as Lateness 3.

This comparison is slightly disingenuous because comparisons between the two on the absolute measure of service level are not the best way to think about the relative merits of each constraint. As is expected when 50% of an order is considered ‘full’, there will be a significant amount of product left behind. With 95% fill rates, the

vast majority of product will be leaving the distribution center when the model says the whole order leaves. These are very different paradigms, but both can be useful when considering the cyclical and seasonal nature of retail. Most clothing companies stock largely different assortments during the winter and summer and retailers will often change the entire layouts of stores to accommodate. That leads to highly differentiated attitudes towards service at the beginning and ends of seasons from both the manufacturer and the retailer. For products that are ordered to kick off a new season, high service levels are required to fill the store shelves, create sets of products that are merchandised together, fill displays, and offer products in all sizes. Products ordered just one month later are instead filling in at the end of the previous season—odd size runs, missing pieces, and half-full orders may be more acceptable by both the manufacturer and the retailer as the season where the product is viable ends imminently.

This attitude difference means that modeling both the cases with higher and lower fill rate constraints has value, but the use case with higher fill rate requirements is likely still more useful. As product is being expedited at relatively high cost, low-value, half-full orders are not worth air freighting product to fill. Instead, attitudes shift to making do with what product remains. During the beginning of the season when fill rate requirements are higher, the results of the model are also more accurate, as the discrepancy between the service levels provided by following the strategy the model provides (yielding 95% fill rates) and the service level the model perceives it provides (100% fill rate). As noted earlier, this constraint is also customizable for each SO, and therefore can be adjusted for more complicated needs in the future.

The lower fill rate strategies do have interesting implications for how to manage air freight expenditures under that low service level paradigm. As can be seen in Fig. 5-6, the benefits of air freighting are quickly realized when only 50% of product is necessary to sufficiently fill an order. This implies that as order requirements loosen as the season progresses, the benefit of high air freight budgets evaporate, and minimal spend can capture nearly all potential benefits.

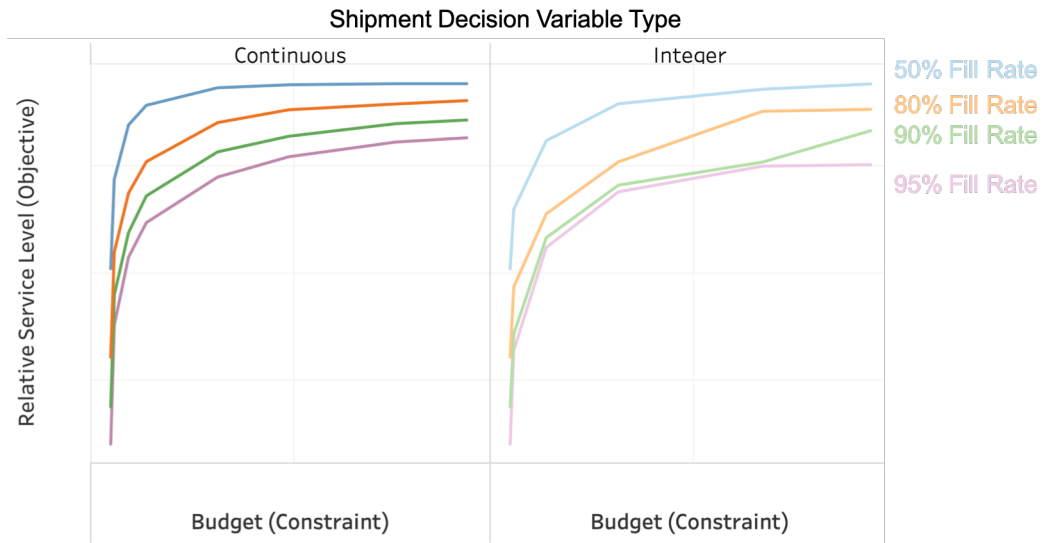


Figure 5-5: Pareto Frontiers with Different Fill Rate Constraints and Variable Types for Shipment Decisions

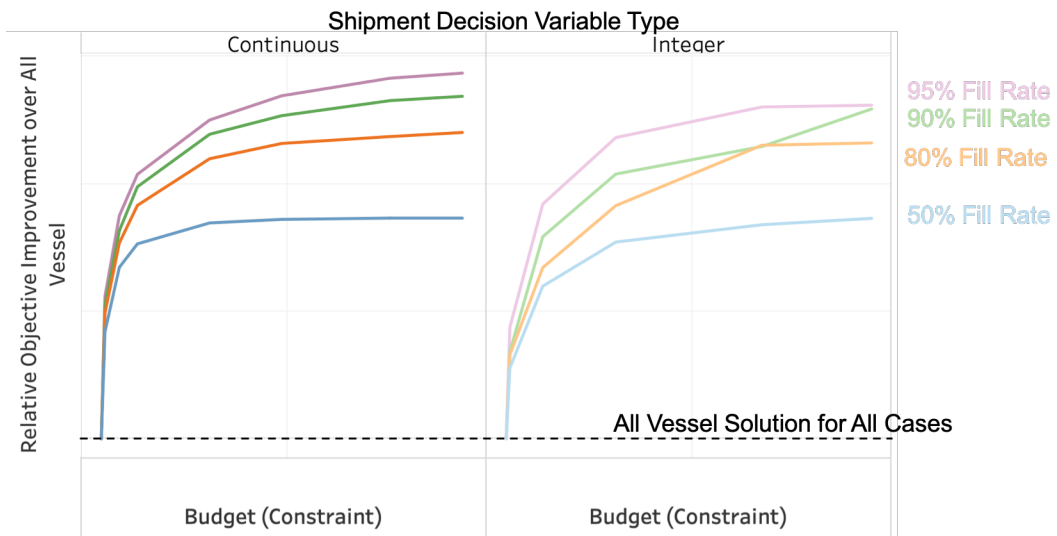


Figure 5-6: Pareto Frontiers with Different Fill Rate Constraints and Variable Types for Shipment Decisions Showing Improvement over Vessel Cases

5.2.2 Discrete Mode Choice Relaxation

The simple implementation of this modeling would require that each purchase order is shipped in its entirety via one mode. A dynamic supply chain may be able to split up orders and ship only a portion of the order by each mode, expediting only what is necessary and sending the rest by sea. To model this, we relax the constraint that the α decision variables for each order must be binary, and instead allow it to take any value between 0 and 1. The constraint requiring the sum of all α for each order equal 1 remains. The comparisons between the cases requiring integer solutions and allowing for continuous relaxations can be seen in Figs. 5-5 and 5-6.

Fig. 5-6 shows the trends present particularly well. The continuous relaxation consistently outperforms the integer formulation at similar budget levels and reaches the plateau earlier where additional spend does not increase service levels. For lower fill rate constraints like the blue 50% constraint curves, the two curves do reach similar points eventually. However, for the more heavily constrained models like the purple 95% curves, the continuous relaxation continues to substantially outperform its integer equivalent.

This relatively better performance is operationally irrelevant however. The operational complexity of changing logistics software, shipping and receiving processing, and other infrastructure to accommodate split shipments is likely to not be worth the incremental payoff. There are bound to be plenty of challenges with the current implementation of this analysis, and the order of magnitude of possible service level increases or cost reductions are quite similar to the split shipments case. For an illustration of these scale differences, see Fig. 5-7.

5.2.3 Deliver-to-need

Customers often place a contract style order with the manufacturer. This contract allows for a reservation of units at the manufacturer's DC with smaller shipments calling off the units on that contract over the course of the season. If the manufacturer air freights the entire contracted amount into the DC at the beginning of the season,

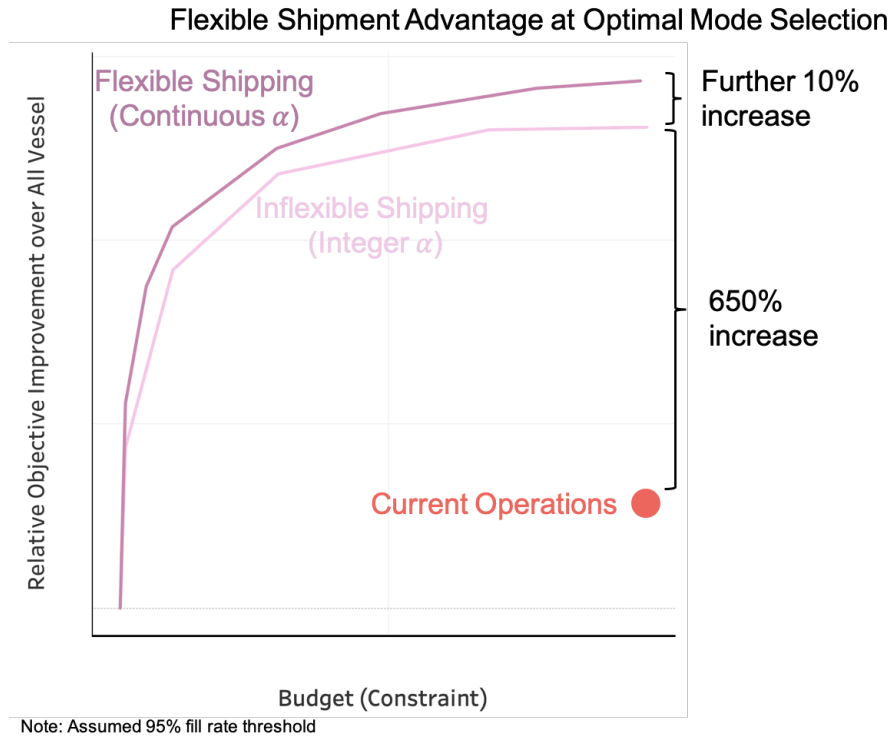


Figure 5-7: Pareto Frontiers with Different Shipment Decision Variable Types Compared to Current Operations

there will be many units that are not actually ordered from the customer until much later. There will undoubtedly be benefits from meeting this customer demand more exactly instead of holding large amounts of product that is not needed until late in the season. I attempted to estimate the actual customer call-off shipments using historical data of similar products to see what the inbound transportation savings might be, but the forecast accuracy was not high enough to implement the idea.

5.3 Prioritization and Guidance on Implementation

The base model determined an optimal frontier where air freight strategy could operate given the underlying assumptions of the model but there was no insight into whether decreasing spending or increasing service would be a priority for making operations better. Both are improvements over the current state. The inclusion of carbon emissions makes a strong case that reducing air freight spend/use over the

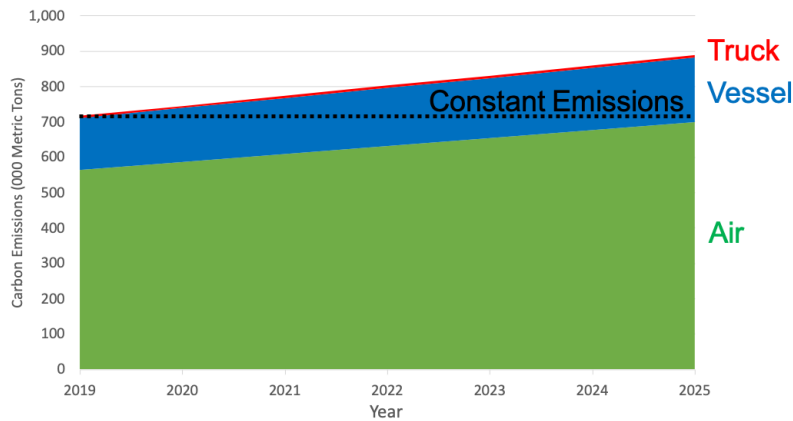


Figure 5-8: Inbound Freight Carbon Contributions by Mode

next several years is crucial to being a leader among brands concerned about the environmental impact of their operations.

Fig. 5-8 shows a simple growth chart of emissions for the inbound transportation of the manufacturer by mode using public corporate growth projections evenly across all products. If the manufacturer wants to decrease emissions from all segments that contribute, inbound freight would have to reduce emissions by an amount equal to all non-air emissions by 2025 in order to simply keep at 2019 emissions levels. Eliminating all vessel carbon contributions is infeasible short of on-shoring all operations, an impossibility barring geopolitical realignment on a scale never seen in modern history. Therefore reducing air freight (by far the largest contributor as-is) is crucial in meeting carbon reduction goals. This model has shown that in total, service can be maintained at lower air freight cost (and therefore use, as cost is almost directly proportional to air freight emissions).

The perishability metrics developed in Sec. 3.3 will guide the decision about which products are least valuable, but during discussions about where to focus air freight cuts, several stakeholders raised concerns that the six categories are too simplistic to determine what not to air freight. The perishability metric was designed to mimic the different reactions customers might have if product were late under various circumstances. As such, it performs well when it doesn't radically impact the mix of who is given high service and what they receive broadly. It works best as a re-prioritization

of the existing order book. The reaction to a late key launch-day style is different to late long-lifecycle product and perishability captures that well. However, with large changes in service, a poor reaction from customer A may be received internally differently from customer B. Late product in category Z with a large marketing budget and high price point may be more important than category Y, with small marketing outlays and low prices.

Combining these effects with a recommended carbon price⁴ reveals some interesting trends in profitability of different product categories when carbon is taken into account. This analysis estimates the average profit for a large class of products (e.g. dollars earned per unit for all running shoes) that the manufacturer earns when selling to customers. Then, a per-unit air freight cost is subtracted, including both the cost charged by the shipper and the implied cost of emitted carbon. The dollar values are suppressed, but we can see in Fig. 5-9 that several categories would not earn a profit for the manufacturer. If the manufacturer implemented carbon pricing and continued air freighting these classes of product, they would effectively be selling product at a loss. For example, Category 3 would be a candidate for halting air freight as it is high volume, but has no profitability once air freighted.

There are many ways forward incorporating this data including further scaling or segmenting perishability values by profit margin, or capping quantities of less profitable categories. Both would result in prioritizing the least profitable categories to reduce air freight quantities.

⁴\$100/MT is the assumption from the UN global compact (<https://www.unglobalcompact.org/take-action/action/carbon>)

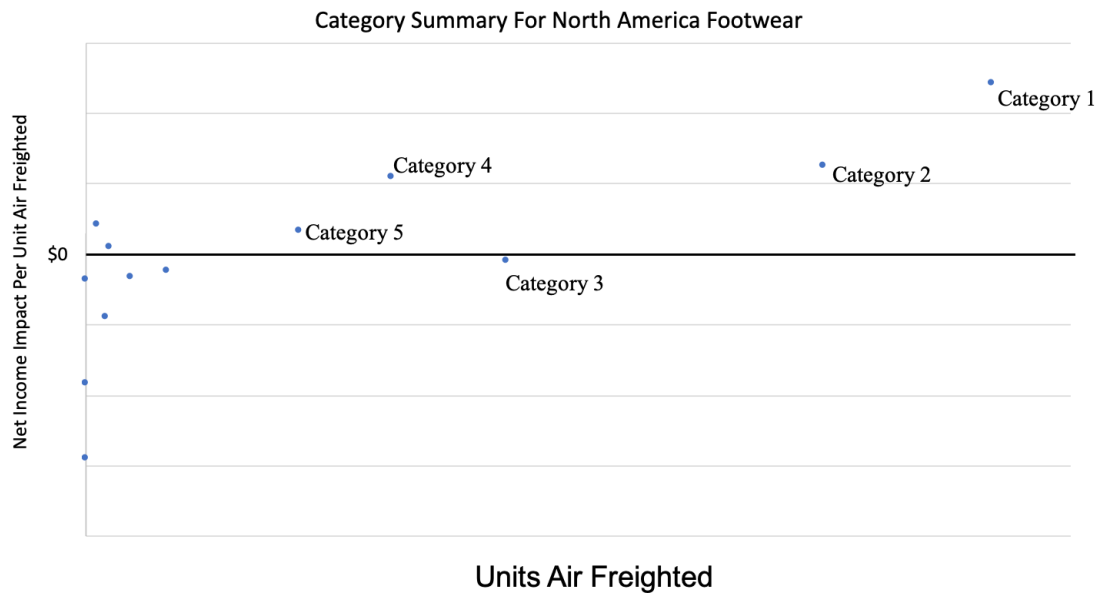


Figure 5-9: Margin After Air Freight Including Carbon Costs

Chapter 6

Conclusions and Future Work

In this thesis, I developed a network optimization approach to improve the outcomes of expediting inbound freight orders for a brand with distributed manufacturing and multiple customers. The approach determined the optimal transportation mode for each order from contract manufacturers and the optimal lateness at which to fulfill each shipment to customers. Among the many constraints on the system were the budget available for transportation costs, the fill rate of shipments, and the allocation of products from orders to shipments. The optimization used product categorization and valuation from business users of the tool to inform the value of on-time products and the rate at which various categories degraded in value with increasing lateness. Tests of the model at a large retail brand showed that the vast majority of service level gains come from the initial spend beyond the minimum required by the cheapest transportation mode, and that marginal returns to increased spend decline quickly.

There are three major categories of future work that could help to improve this models applicability, potentially partially mutually exclusive: simplification, formulation developments, and parameter improvements.

Simplification: A simpler model will be easier to understand for end users and faster to run. Run time increases could make more scenarios with different parameters easy to test, make solving the model in real-time during meetings and conversations feasible. The run time decreases due to loosening model solver restrictions did leave to scenarios that took minutes to run, but for a solution to be truly scaleable to

the entire order book and for planners to have the ability to test new ideas in real time, the solve time will need to decrease. A simpler model will also likely aid the interpretability of the results and make for clearer decisions based off of the results

Formulation Developments: Another direction to move this work is one of additional complexity, if not in modeling mathematics then in conceptual design and applicability. One key assumption that could be broken in the modeling is the idea that all units from a given PO are mapped to a specific SO. In reality, there is some re-shuffling that can be done to pool all different orders of product A and optimally allocate the on-hand and pipeline inventory of product A across all different shipments that have requested product A. This approach may need to more explicitly model the on-hand inventory within warehouses, and its applicability requires a more flexible treatment of inventory in reality. The model explored in this thesis has the advantage of a given unit being earmarked for a specific shipment, which may be the best approach for satisfying customers and organizing the supply chain. Breaking this assumption could lead to a much more powerful model to not only expedite what is necessary but to allocate exiting inventory optimally across different customer requests. With this increased scope and power, however may come a decreased application to the problem of optimizing air freight decisions.

Parameter Improvement: Perhaps the most realistic and obvious next step is to better inform parameters through data analysis, rather than via human input. This model relied quite heavily on a stakeholder-based method to discuss the various categories of products and their relative values to use as weights in the objective function. These constituent weights $v_{p,l}$ as discussed in Sec. 4.1.2 are designed to best mimic what the people running the decision process intend to happen. This has a tremendous amount of value both in the decisions it generates, but also in helping to solicit buy-in from the interested stakeholders that the model will not be dramatically changing outcomes, but instead making more consistent decisions.

Informing these parameters using sell-through rates, forecasted demand, marketing spend, and better understanding of the value that marginal improvements in service levels to customers bring to the manufacturer would be one way to imbibe

the entire decision making process with consumer-based data and to make better decisions overall. In attempting to use a data-driven approach to inform these values, I found that the supply chain data availability were inadequate to meet the needs of other interested stakeholders, and that analysing this marginal value would require much more data from across the enterprise that was not available or was controlled by areas without a strong sponsor and understanding of the supply chain impact of their data. In a future state with centralized, accessible data regarding the preferences of disparate business units, this type of analysis may be feasible and fruitful.

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