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### *Impact-induced glass-to-rubber transition of polyurea under high-velocity temperature-controlled microparticle impact*

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1           Impact-induced glass-to-rubber transition of polyurea under  
2           high-velocity temperature-controlled microparticle impact

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15           **ABSTRACT**

16           Deformation-induced glass transition in segmented elastomers has been proposed to allow highly-desirable  
17           enhanced energy dissipation. In this study, we investigate the temperature-dependent micro-scale impact  
18           response of polyurea at a fixed impact velocity. We observe a local elevated impact energy absorption around  
19           115°C, which is attributed to the glass-to-rubber transition temperature under the present high-rate dynamic  
20           loading. Dielectric spectroscopy was performed and the soft-segmental  $\alpha_2$ -relaxation was extracted and fit with  
21           a Havriliak–Negami function. The  $\alpha_2$ -relaxation frequency at 115°C correlates well with an order-of-magnitude  
22           estimate of the equivalent frequency of deformation. This work further supports the importance of the dynamical  
23            $T_g$  as an important consideration in the design of impact resistant materials.  
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26 High mechanical energy absorption in lightweight materials is a greatly desirable trait for many commercial  
27 applications involving high strain rate deformations such as helmets, automotive crashworthiness materials, and  
28 impact-resistant devices<sup>1-3</sup>. Elastomers offer desirable properties in such applications including high mechanical  
29 damping capabilities, remarkable toughness, high chemical resistance, and low cost<sup>3,4</sup>. Polyurea, in particular,  
30 was shown to exhibit a uniquely robust ballistic impact response, purportedly as a result of its propensity to  
31 undergo a strain-rate-induced glass transition under ballistic impact<sup>5,6</sup>. This discovery led to a heightened  
32 interest in the high-strain-rate responses of various segmented elastomers including polyurea, polyurethane, and  
33 poly(urethane urea)<sup>5,7-13</sup>. Through control of molecular moieties, one can design these hierarchical elastomers  
34 to express different degrees of separation and mixing (incomplete segment segregation) between the hard and  
35 soft segment phases, which directly impact the segmental relaxation dynamics and therefore the rate-dependent  
36 mechanical behavior<sup>9,14,15</sup>.

37 In polyurea synthesized with a poly(tetramethylene oxide) (PTMO) soft segment molecular weight of 650  
38 g/mol (thereafter named PU650), segmental motions attributed to soft segments were shown to consist of two  
39  $\alpha$ -relaxations: a fast segmental motion ( $\alpha_1$ ) related to unrestricted motion of soft segments in the soft-segment  
40 rich phase and a slower motion related to constrained soft segments attached to hard domains ( $\alpha_2$ )<sup>16</sup>. For a quasi-  
41 static deformation rate ( $10^{-2} \text{ s}^{-1}$ ), Castagna et al. estimated the glass transition temperatures  $T_g$  associated with  
42 the  $\alpha_1$ -relaxation and the  $\alpha_2$ -relaxation processes to be  $-53^\circ\text{C}$  and  $22^\circ\text{C}$ , respectively<sup>16</sup>. For higher deformation  
43 rates, the glass transition temperatures shift toward higher values following a Vogel-Fulcher-Tammann law; the  
44 higher-rate transitions are often referred to as “dynamic glass transitions”. It is well known that energy  
45 dissipation is significantly increased at the glass transition temperature<sup>17</sup>. Based on this premise, Bogoslovov &  
46 Roland demonstrated that a strain-rate-induced glass transition leads to enhanced energy dissipation upon  
47 impact of elastomers for which the characteristic deformation rate is comparable to the segmental relaxation  
48 kinetics, which in their study corresponded to the  $\alpha_1$ -relaxation<sup>5</sup>.

49 Most studies focusing on the high-rate response of hierarchical polymers rely on broadband dielectric  
50 spectroscopy as a well-established tool that can reach frequencies up to  $10^7 \text{ s}^{-1}$ , thereby guiding the design of  
51 impact-resistant materials<sup>18-20</sup>. However, few experimental works have directly validated this guidance through  
52 direct measurements of high-velocity impact. The development and use of the laser-induced particle impact test

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53 (LIPIT), a microballistic platform<sup>21</sup>, has yielded extensive impact data on segmented elastomers<sup>10,13</sup> reaching  
54 strain-rates of  $\sim 10^8$  s<sup>-1</sup>. These micro-impact studies have demonstrated the importance of intersegmental mixing  
55 and hydrogen bonding networks in the high-strain-rate responses of the elastomers<sup>11,12,22</sup>. In this study, we  
56 investigate the high-strain-rate glass transition of polyurea by conducting temperature-controlled experiments  
57 at a fixed micro-impact velocity. We aim to directly measure the dynamic glass-to-rubber transition associated  
58 with the relaxation dynamics of constrained soft segments near the hard phase, which were reported to  
59 correspond to the  $\alpha_2$ -relaxation in polyurea<sup>16</sup>. Our results represent the first LIPIT high-velocity microscale  
60 impacts at non-ambient temperatures and direct measurements of a dynamic phase transition temperature at the  
61 associated high strain rates.

62

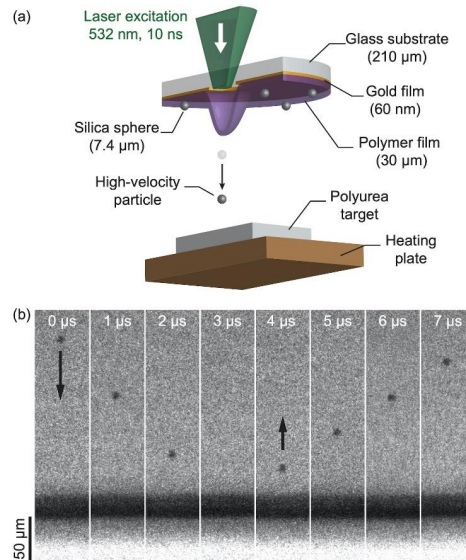
63 The polyurea target was synthesized in a 1:1 stoichiometric ratio of a modified curative, polycarbodiimide-  
64 modified diphenylmethane diisocyanate (MDI) (Isonate 143L, RCS Rocket Motor Components) and an  
65 oligomeric diamine (Versalink® P650), based on poly(tetramethylene oxide di-p-aminobenzoate) (PTMO) with  
66 a molecular weight of 650 g/mol (obtained from Evonik). After mixing, the reactants were cast between two  
67 glass plates with a 1-mm thick rubber spacer and polymerized at room temperature for 48 days. The specimen  
68 was then placed in a desiccator for 8 days and aged for more than 14 days prior to testing<sup>16,23</sup>. Sample heating  
69 was achieved with a resistive heating plate with a polyimide conduction surface (Icstation, 12V, 7W), controlled  
70 by a digital proportional-integral-derivative (PID) thermostat (Inkbird, ITC-100VL). The polyurea sample was  
71 secured to the heating plate with adhesive tape along the edges. Temperature was measured with a thermocouple  
72 at the top surface of the target and used as feedback into the PID thermostat.

73 Microparticle impact experiments were conducted using the LIPIT platform, schematically represented in  
74 Fig. 1. First, a launch pad is assembled by depositing a gold film (60-nm thick) and spin-coating a polymer film  
75 (polyurea, 30- $\mu$ m thick) onto a glass substrate (210  $\mu$ m thick). This assembly is kept under vacuum for 24 hours  
76 and then cured at 85°C for 18 hours. Silica spheres (7.4- $\mu$ m diameter) are deposited and dispersed across the  
77 surface of the polymer film. Prior to each launch, a single silica sphere is selected for acceleration using a CCD  
78 camera. Acceleration is achieved via ablation of the sacrificial gold film with a high-energy laser pulse (Nd-  
79 YAG, 532-nm wavelength, 10-ns duration). Ablation induces a rapid expansion of the polymer film which

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80 subsequently accelerates the particle into free space toward the target, placed around 2 mm away from the  
 81 launching pad. The trajectory of the particle, both prior to and after impact, is observed with a microscope (10×  
 82 objective, 40-cm tube lens) and an ultra-high-speed multi-frame camera (SIMX16, Specialized Imaging). The  
 83 illumination is provided by a second laser pulse (640-nm wavelength, 30- $\mu$ s duration). The camera yields a 16-  
 84 frame sequence of the impact event with variable interframe time and a minimum exposure time of 5 ns. More  
 85 details regarding the launch pad preparation and the optical system can be found in our previous works<sup>13,24</sup>.  
 86



87  
 88 **FIG. 1.** (a) Schematic representation of the LIPIT platform. A particle is accelerated toward a polyurea target following  
 89 ablation of a sacrificial gold film with a high-energy laser pulse. (b) Representative image sequence of a silica sphere (7.4  
 90  $\mu$ m) impacting a polyurea target at 23°C. The impact and rebound velocities are measured to be 65 m/s and 39 m/s,  
 91 respectively.

92  
 93 A representative image sequence of a silica sphere impacting the polyurea target at 23°C is shown in Fig.  
 94 1b. From this image sequence, the impact and subsequent rebound velocities were measured to be 65 m/s and  
 95 39 m/s, respectively. The coefficient of restitution, the ratio between rebound  $V_r$  and impact velocities  $V_i$ , was  
 96 calculated to be 0.60. In this study, a series of impacts was performed within a tight range of impact velocities

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97 (60-72 m/s) while varying the target temperature from 23°C (room temperature) to nearly 160°C. To better  
98 resolve temperature effects on the coefficient of restitution, we chose a velocity range for which the coefficient  
99 of restitution value is high at room temperature<sup>12</sup>. Within this impact velocity range, the coefficient of restitution  
100 varies by less than 3% as a function of impact velocity at constant temperature. The coefficient of restitution  
101 variation with temperature is shown in Fig. 2a. Variation of the coefficient of restitution as a function of  
102 temperature has been used to study the dynamic glass-to-rubber transition in polymers, where a pronounced  
103 change in energy absorption upon impact is observed at the transition temperature<sup>25-28</sup>.

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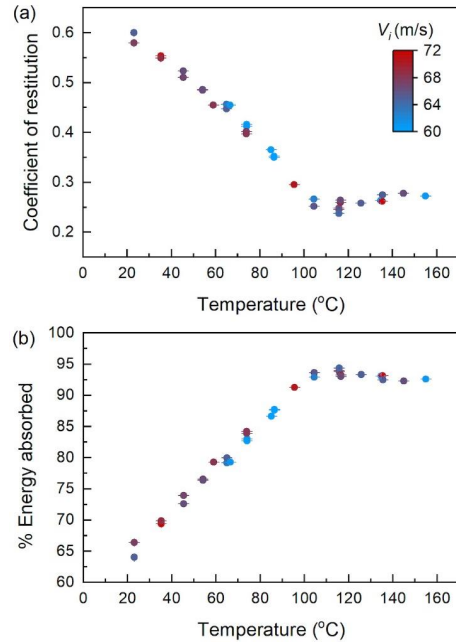
105 A minimum in the coefficient at ~115°C corresponds to a maximum in relative energy absorption  $\%E_a$ ,  
106 calculated as  $\%E_a=1-V_r^2/V_i^2$  (Fig. 2b). As temperature increases, the polyurea target behavior transitions from  
107 glassy-like to leathery, corresponding to the maximum observed energy absorption, and eventually to rubbery-  
108 like with a slightly lower energy absorption. We define a first-order characteristic contact time  $t_c$  as the sum of  
109 the time to reach full penetration  $h_{max}$  and the time to detach from the sample, assuming a penetration velocity  
110 of  $V_i$  and an exit velocity of  $V_r$ :

$$111 \quad t_c = h_{max} \left( \frac{1}{V_i} + \frac{1}{V_r} \right) \quad (1)$$

112 Because of the shadow cast by the sample, it is not possible to image the penetration of the particle inside  
113 the target close to the surface and thus  $h_{max}$  is not measured in our experiments. We can however anticipate the  
114 penetration depth to be on the order of a few microns or less based on previous experiments performed on  
115 similar materials<sup>10</sup>.

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116

117 **FIG. 2.** (a) Coefficient of restitution (COR) as a function of target temperature for impacts around 65 m/s onto the polyurea  
118 target. The COR decreases rather smoothly with increasing temperature until it reaches a minimum at around 115°C and  
119 then increases slightly at higher temperatures. The minimum is indicative of a dynamic glass-to-rubber transition. (b)  
120 Percentage energy absorbed during impact a function of temperature.

121

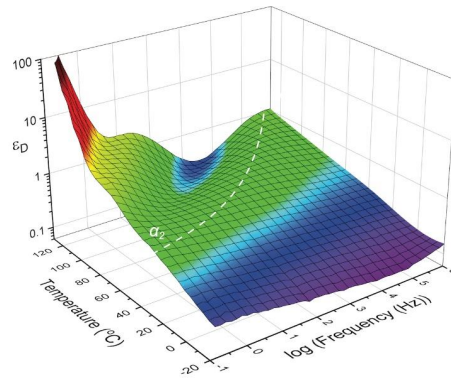
122 Dielectric relaxation measurements were carried out using a Novocontrol Concept 40 Broadband Dielectric  
123 Spectrometer to characterize the material segmental dynamics and identify the relevant relaxation times. A  
124 polyurea specimen (0.54-mm thick), sputter-coated with a thin gold layer (5-nm thick) on both sides, was  
125 sandwiched between two 1-cm diameter brass electrodes to form a parallel-plate capacitor. Measurements were  
126 conducted isothermally with an AC voltage  $V_{rms}$  of 1.5 V with specimen temperatures varying from -20°C to  
127 130°C (5°C steps) and applied frequencies from  $10^{-1}$  to  $10^6$  Hz. We follow the procedure described by  
128 Fragiadakis and Runt to analyze the dielectric results<sup>19</sup>. The derivative representation  $\epsilon_D$  of the dielectric  
129 permittivity is shown in Fig. 3 with:

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$$\varepsilon_D = -\frac{\pi}{2} \frac{d\varepsilon'}{d \ln \omega} \quad (2)$$

131 The derivative form of the permittivity allows a better visualization of the relaxation processes by eliminating  
 132 dc conduction losses, which obscure the loss peaks in the measured  $\varepsilon''$  data. From the dielectric spectrum,  
 133 presented in Fig. 3, we identify the peak characteristic of the  $\alpha_2$ -relaxation corresponding to the constrained soft  
 134 segmental motions. We note that the  $\alpha_1$ -relaxation is not pronounced over the studied temperature and frequency  
 135 range as also suggested by Castagna et al.<sup>16</sup>



136  
 137 **FIG. 3.** Derivative representation of the dielectric relaxation data  $\varepsilon_D$  as a function of temperature and frequency revealing  
 138 the locus of the  $\alpha_2$ -relaxation peak.

139  
 140 The frequency of the maximum  $\alpha$ -relaxation mode,  $f_{max}$ , can be extracted by fitting the dielectric loss  $\varepsilon''$  with  
 141 a Havriliak–Negami function<sup>29</sup>:

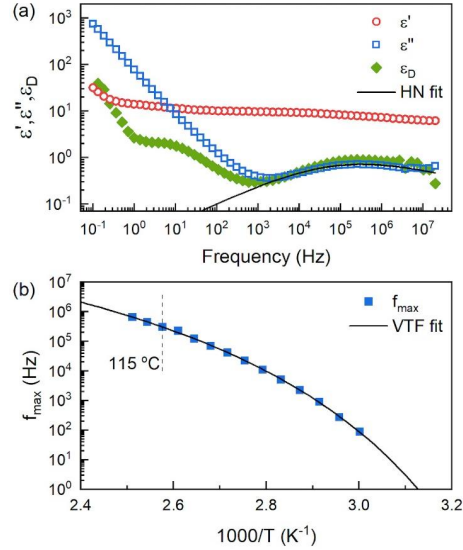
$$\varepsilon^* = \varepsilon' - i\varepsilon'' = \varepsilon_\infty + \frac{\Delta\varepsilon}{(1+(if/f_{HN})^m)^n} \quad (3)$$

143 where  $\varepsilon_\infty$  is the infinite-frequency dielectric constant,  $\Delta\varepsilon$  is the dielectric strength,  $m$  and  $n$  are shape  
 144 parameters related to the breadth of the relaxation and the high frequency asymmetry, respectively, and  $f_{HN}$  is a  
 145 characteristic frequency. The dielectric strength, the width and shape parameters, and the characteristic  
 146 frequency were fitted for all temperatures. The fit at 115°C is shown in Fig. 4, along with the dielectric data at  
 147 that temperature.



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149 **FIG. 4.** (a) Dielectric spectra for polyurea at 115°C. Real and imaginary parts (open symbols) and derivative  $\epsilon_D$ . The  $\alpha_2$ -  
150 relaxation peak is fitted with a Havriliak–Negami (HN) function (b) Arrhenius plot of segmental relaxation peak frequency  
151 ( $f_{max}$ ) data fitted with Vogel-Fulcher-Tammann function.

152

153 The characteristic frequency  $f_{HN}$  is related to the frequency of the maximum loss  $f_{max}$  through:

$$154 \quad f_{max} = f_{HN} \left( \frac{\sin \frac{\pi m}{2+2n}}{\sin \frac{\pi m n}{2+2n}} \right)^{1/m} \quad (4)$$

155 The obtained  $f_{max}$  values shown in Fig. 4 give the temperature-dependence of the maximum loss frequency.

156 The  $\alpha$ -relaxation obeys a Vogel-Fulcher-Tammann (VFT) temperature dependence with:

157

$$158 \quad f_{max} = f_0 \exp \left( \frac{-B}{T-T_0} \right) \quad (5)$$

159 where  $f_0$ ,  $B$  and  $T_0$  (Vogel temperature) are constants. The fit yielded  $f_0 = 10^{10}$  Hz,  $B = 1300$  K<sup>-1</sup>, and  $T_0 =$   
160 263 K. The  $\alpha_2$ -relaxation peak frequency measured at around 115°C ( $\pm 5^\circ$ C) is in the range  $2\text{--}5 \times 10^5$  Hz. The  
161 corresponding relaxation time,  $\tau$ , is calculated to be  $\sim 500$  ns, from the relation  $\tau = 1/2\pi f_{max}$ .<sup>30</sup>

162 Assuming, as a first order, that the impact is a half cycle of a sinusoidal vibration, we can calculate the  
163 equivalent frequency of the experiment to be  $f_{impact} = 1/2 t_c$ . In the absence of direct measurement for penetration

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164 depth, we assume  $h_{max}$  to be the particle diameter and estimate  $f_{impact} \sim 8 \times 10^5$  Hz (Eq. 1). The concept of  
165 equivalent frequency has been proposed decades ago<sup>25</sup> and is simplistic in nature as it eludes the range of  
166 frequencies achieved during impact. However, it provides a reasonable order-of-magnitude approximation<sup>25</sup> and  
167 allows us to compare it with the  $\alpha_2$ -relaxation frequency  $f_{max}$  and thus to validate that we are probing the  $\alpha_2$   
168 dynamics of the soft segments near the interface. Furthermore, based on the dielectric measurements performed  
169 by Castagna et al., we anticipate that, for impacts at 65 m/s, we would observe the glass transition corresponding  
170 to the  $\alpha_1$ -relaxation at about -5°C. Future efforts will be dedicated into implementing a cooling stage to support  
171 this hypothesis.

172

173 In summary, through microparticle impact measurements on a temperature-controlled polyurea target, we  
174 directly measure the dynamic glass-to-rubber transition temperature of polyurea at a high strain rate ( $\sim 10^5$  s<sup>-1</sup>).  
175 Dielectric spectroscopy results confirm that the observed transition corresponds to the  $\alpha_2$ -relaxation of the soft  
176 segments near the hard-segment interfaces. Our results align with those of Bogoslovov & Roland<sup>5</sup>, which  
177 showed that molecular relaxation is induced when the segmental dynamics become comparable to the  
178 mechanical strain rate, resulting in increased energy dissipation. This work further supports the importance of  
179 the dynamic  $T_g$  in impact mitigation and indicates that the results should help guide the design of impact-  
180 resistant materials.

181

182 The data that support the findings of this study are available from the corresponding author upon reasonable  
183 request.

184

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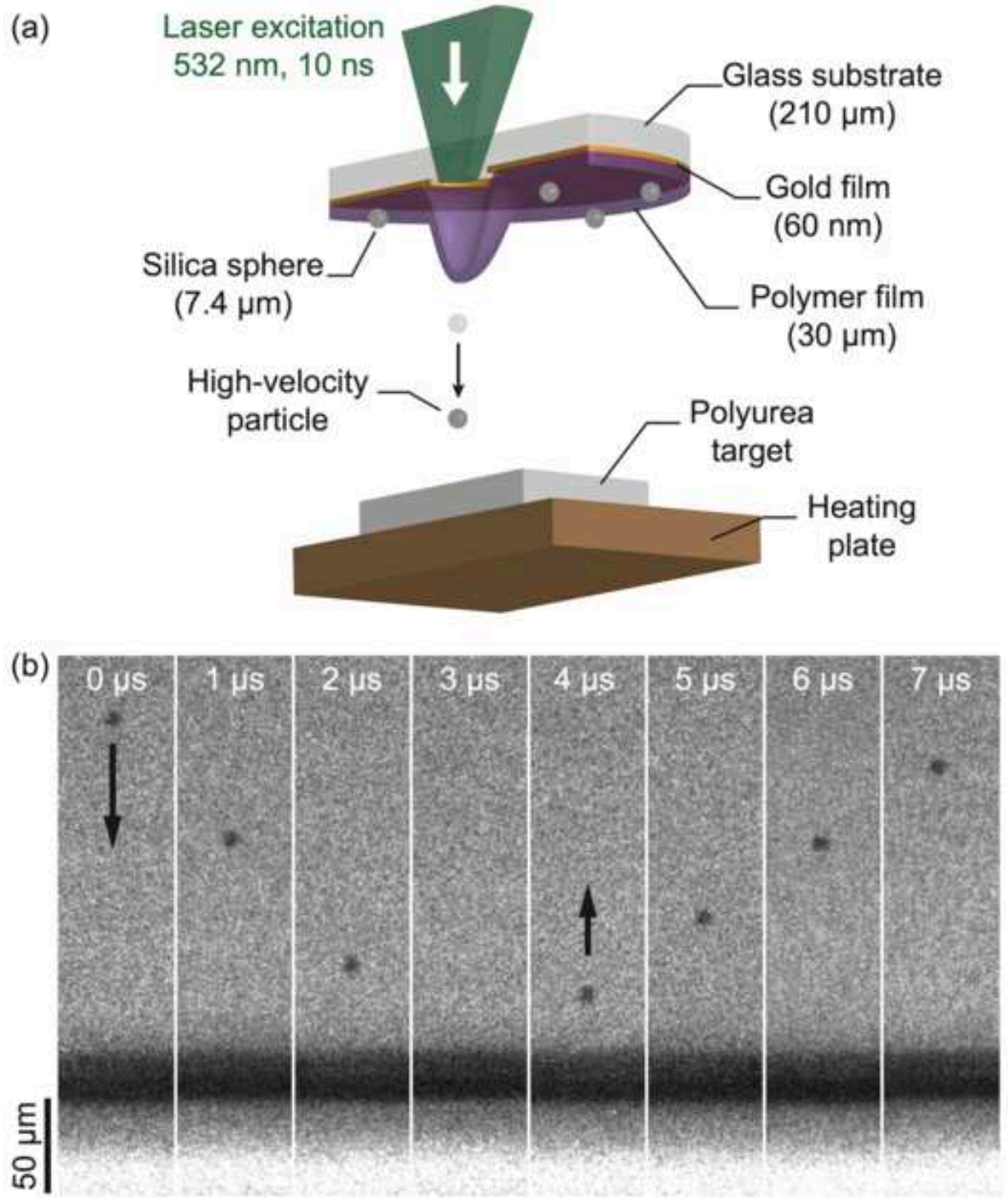
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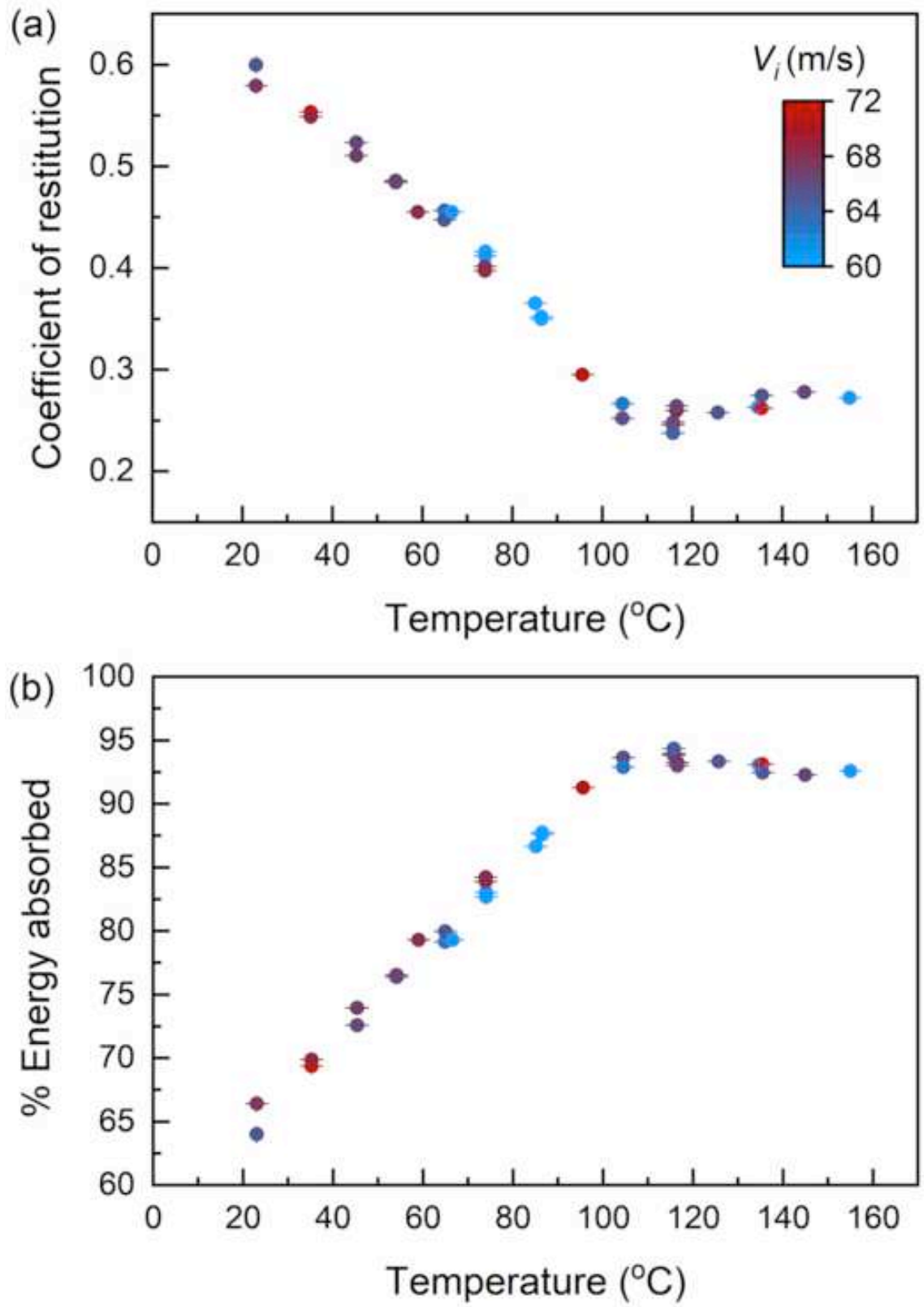
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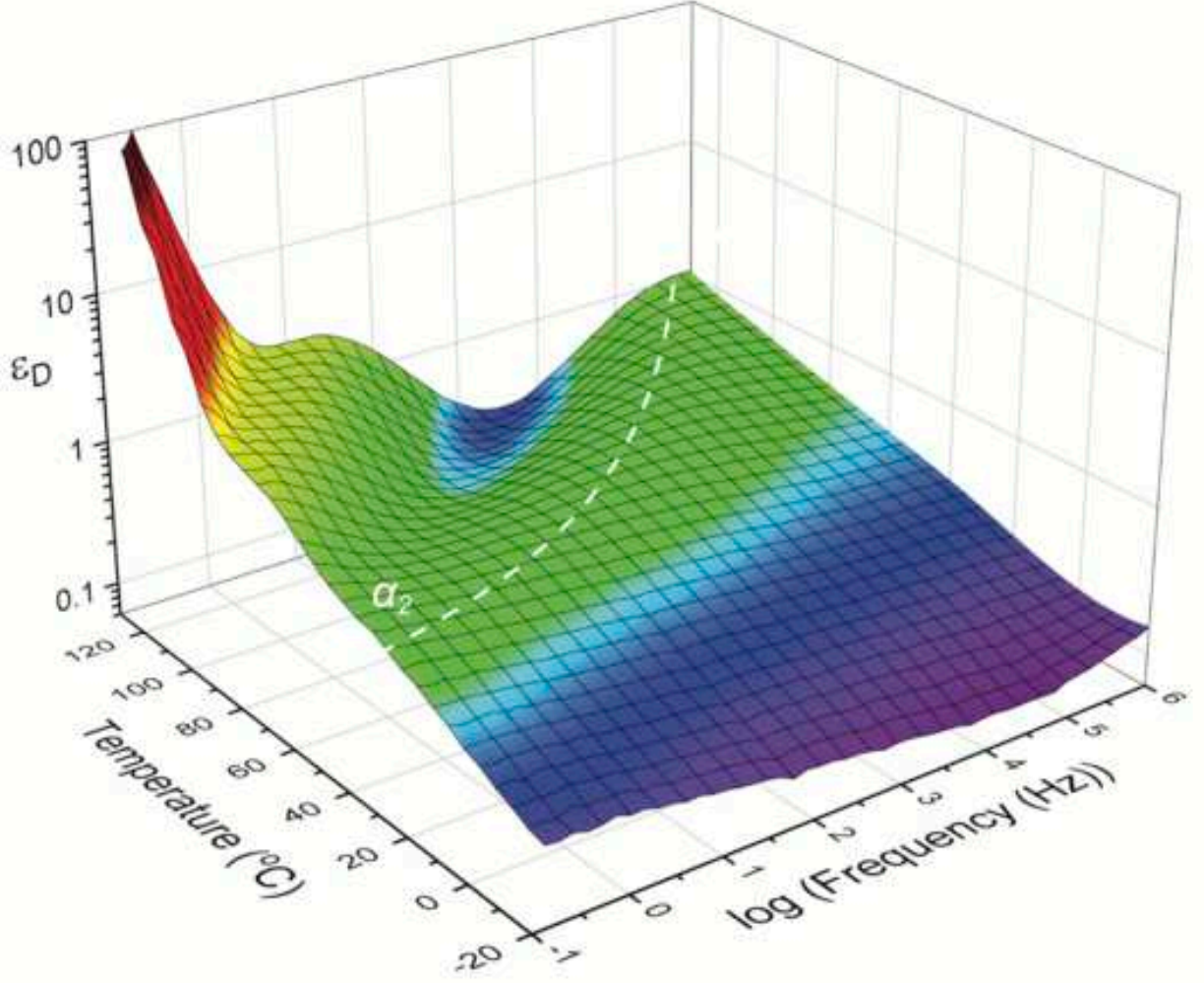


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