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### Calibrating DFT Formation Enthalpy Calculations by Multifidelity Machine Learning

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**KEYWORDS:** formation enthalpy, stability, machine learning, DFT, multifidelity, transfer learning

#### INTRODUCTION

To accelerate the design of new materials, computational methods such as density functional theory  $(DFT)^1$  have been employed to generate large data sets that contain more than  $10^5$  entries of material properties, including the Materials Project (MP),<sup>2</sup> Open Quantum Materials Database (OQMD),<sup>3</sup> the Automatic Flow of Materials Discovery Library (AFLOW),<sup>4</sup> and the Joint Automated Repository for Various Integrated Simulations (JARVIS).<sup>5</sup> While the availability of such databases has boosted the exploration of novel materials,<sup>6–15</sup> it is important to note that most of the data is generated with computationally "cheap" DFT functionals such as Perdew–Burke–Ernzerhof (PBE),<sup>16</sup> which can, in turn, lead to nonnegligible errors when compared with experimental measurements.

As an example, the formation enthalpy  $(\Delta H_f)$  is a fundamental property that determines the thermodynamic stability of materials. The mean absolute error (MAE) between the computed  $\Delta H_f$  in these large DFT databases and experimental measurements is reported to be ~0.1 eV/atom.<sup>3,17</sup> Due to the sensitivity of phase stability to energy, such a difference might be the difference between a material that is readily synthesizable and one that is almost impossible to realize.<sup>18–20</sup> In addition, because of the limited amount of available experimental data, currently most machine learning (ML) models applied to materials are trained on DFT datasets,<sup>6,21–35</sup> making any error in the DFT calculations critical to the usefulness of such ML models.<sup>7,31,36,37</sup>

To improve the accuracy of formation enthalpy calculations, a number of density functionals have been developed, such as PBEsol,<sup>38</sup> SCAN,<sup>39</sup> r<sup>2</sup>SCAN,<sup>40</sup> and HSE,<sup>41</sup> which have shown significant improvement in the accuracy of formation enthalpy calculations.<sup>42–44</sup> On the other hand, except PBEsol, these more accurate functionals are computationally more expensive, limiting their utility for the generation of large databases.<sup>43,45</sup> Empirical corrections represent another, faster approach to improve the accuracy of the prediction of  $\Delta H_{\rm f}$ . For example, in the MP dataset,  $\Delta H_{\rm f}$  of certain materials (including oxides, phosphates, borates, and silicates) is empirically corrected by fitted element corrections,  $^{46}$  and in OQMD,  $\Delta H_{\rm f}$  is corrected by a chemical-potential fitting.<sup>3</sup> Very recently, Wang et al.<sup>47</sup> proposed a linear correction scheme with an error of 0.051 eV/atom compared with experimental values on a dataset with 222 materials containing certain anions and transition metals. Yet, despite this recent success in lowering the error for some chemical systems,<sup>48</sup> such corrections are based on the human understanding of specific chemistries and relatively simple assumptions and are thus difficult to be transferable across different chemistries.46,48 It would be beneficial to design prediction schemes that can automatically extract the chemistry-property relationship across different chemistries without human intervention, and data-driven ML meth-

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**Figure 1.** Illustrations of the machine learning frameworks and datasets used in this work. (a, b) Schematics of transfer learning and multifidelity machine learning in this work, respectively. In panel (a), first the  $\Delta H_f^{DFT}$  is used as a label to train an ML model, then the weights of the first ML model are transferred to initialize a second ML model, and then the  $\Delta H_f^{exp}$  is used as a label to train the second model; finally, the second model is used to predict  $\Delta H_f^{exp}$  of all materials in the large DFT dataset. In panel (b), first the dataset of the difference between  $\Delta H_f^{exp}$  and  $\Delta H_f^{DFT}$  is constructed  $(\Delta H_f^{diff})$ , then  $\Delta H_f^{diff}$  is used as a label to train an ML model with the  $\Delta H_f^{DFT}$  as an input feature, and finally the trained model is used to calibrate the difference between  $\Delta H_f^{DFT}$  and  $\Delta H_f^{exp}$  for all materials in the large DFT dataset. (c)  $\Delta H_f^{DFT}$  versus  $\Delta H_f^{exp}$ . (d)  $\Delta H_f^{diff}$  versus  $\Delta H_f^{DFT}$ .

ods<sup>18,24,26,28,29,32,45</sup> are promising candidates to learn the complex mapping between chemistry and  $\Delta H_{\rm f}$ .

One of the biggest challenges in machine learning of material properties is the lack of experimental data.<sup>49</sup> Efforts have been made to improve the performance of learning on small experimental datasets by extracting and transferring information from large DFT datasets. Currently, there are mainly two strategies to achieve the transfer between DFT and experimental datasets, transfer learning<sup>21,28,50-53</sup> and multifidelity machine learning.  $^{45,54-56}$  The idea of transfer learning (Figure 1a) is first learning large DFT datasets (source) using a large neural network and then transferring the weights of the network to the machine learning task of small experimental datasets (target). Although transfer learning has achieved success in problems where the source and target data sets are highly correlated, <sup>21,28,50,51</sup> the approach is mostly applied to neural network architectures, and if the correlation is not strong enough, transfer learning will not improve and may even deteriorate the learning performance.<sup>52</sup> Different from transfer learning where information is passed by transferring network parameters, in multifidelity machine learning (Figure 1b), information of cheap and low-fidelity data is directly passed to the learning task of expensive and high-fidelity data, either in the feature (input) level<sup>54</sup> or in the label (output) level.<sup>45,55–57</sup> In other words, the low-fidelity data can be used as a feature in the machine learning task of high-fidelity data or the task of machine learning the highfidelity data can be converted to the task of machine learning the difference between high-fidelity data and low-fidelity data, which is also known as  $\Delta$ -machine learning.<sup>57</sup> From the handful of previous studies, multifidelity machine learning has shown higher predictive power than single-fidelity ones (directly

learning the high-fidelity data) on material properties like band gaps and energies from different density functionals.<sup>45,55–57</sup> However, there is no previous work that adapts multifidelity machine learning at both feature and label levels at the same time.

In this work, we present a comprehensive machine learning study of  $\Delta H_{\rm f}^{\rm exp}$  using transfer learning and multifidelity machine learning. For the machine learning architectures, we compare four different models, random forests (RFs), multilayer perceptron (MLP), Representation Learning from Stoichiometry (ROOST),<sup>26</sup> and Crystal Graph Convolutional Neural Network (CGCNN).<sup>32</sup> We find that multifidelity RF in both the feature and label levels has the best prediction performance for  $\Delta H_{\rm f}^{\rm exp}$  with more than 30% reduction in MAE compared with DFT results from MP and improved performance compared to recent linear correction schemes<sup>47</sup> as well as more sophisticated density functionals like PBEsol,<sup>38</sup> SCAN,<sup>39</sup> and r<sup>2</sup>SCAN.<sup>40</sup> We also analyze the effects of machine learning architectures, featurization methods, and information transfer strategies on learning  $\Delta H_{\rm f}^{\rm exp}$  and  $\Delta H_{\rm f}^{\rm diff}$ . Further, the more accurate  $\Delta H_{\rm f}$  are applied to re-evaluate the thermodynamic stability of materials, and cases with underestimated stability in the MP database are discovered. We also use the machine learning model to find where current DFT deviates from experiments by explaining the model output.

#### RESULTS

#### Illustration of Machine Learning Frameworks and Datasets

In this work, we use two different strategies to learn  $\Delta H_{\rm f}^{\rm exp}$  with the assistance of information from the MP dataset, transfer



Figure 2. Comparison of machine learning models. (a) Mean average errors (MAEs) between predictions of  $\Delta H_f$  from some machine learning models and experimental measurements. Each type of machine learning model is trained 10 times to estimate the uncertainty levels. RF denotes random forest with compositional features from matminer,<sup>59</sup> and ROOST<sup>26</sup> and CGCNN<sup>32</sup> are two deep learning models that automatically extract materials' fingerprints from compositions and structures, respectively. Here, "dft." in front of "RF" means the model is trained with  $\Delta H_f^{DFT}$  as an input, "trans." in front of "ROOST" and "CGCNN" model is trained in a transfer learning manner, diff. model is trained on  $\Delta H_f^{diff}$ , and "exp." model is directly trained on  $\Delta H_f^{exp}$ . The dashed horizontal line corresponds to the MAE of  $\Delta H_f^{DFT}$ . (b)  $\Delta H_f^{exp}$  versus  $\Delta H_f^{ML}$  from the best RF model (the second from the left in panel (a)) and  $\Delta H_f^{DFT}$ . (c) MAE of predictions of  $\Delta H_f^{exp}$  with noise from RF and ROOST. Under each noise level, Gaussian noises with a standard deviation of noise level\*0.8 eV/atom (0.8 eV/atom is the standard deviation of the  $\Delta H_f^{exp}$  dataset) are added to both training set and test set. (d, e) Learning curves of different models. The MAE is for the test set. In panel (e), all of the curves are based on random forest, and "struct." means the model is trained with structural and compositional features, and "no struct." means the model is trained with only compositional features.

learning, and multifidelity machine learning (in the following, " $\Delta H_{\rm f}^{\rm DFT}$ " denotes the empirically corrected PBE  $\Delta H_{\rm f}$  by Jain et al. <sup>46</sup> from the MP database, V2021.03.22). As shown in Figure 1a, in transfer learning, a neural network is first trained on the large MP dataset, then weights of the neural network are transferred to initialize a second neural network, and finally, some of the weights of the second network are optimized by the small  $\Delta H_{\rm f}^{\rm exp}$  dataset. Once trained, the second neural network can serve to predict  $\Delta H_{\rm f}^{\rm exp}$  of materials in the large MP dataset. In multifidelity machine learning, as shown in Figure 1b, first the dataset of  $\Delta H_{\rm f}^{\rm diff}$  ( $\Delta H_{\rm f}^{\rm exp} - \Delta H_{\rm f}^{\rm DFT}$ ) is built and then machine learning models are trained on the  $\Delta H_{\rm f}^{\rm diff}$  dataset, with  $\Delta H_{\rm f}^{\rm DFT}$ 

also as an input feature of each material. Once trained, the machine learning model can serve to calibrate  $\Delta H_{\rm f}^{\rm DFT}$  by adding  $\Delta H_{\rm f}^{\rm diff}$  to  $\Delta H_{\rm f}^{\rm DFT}$  to obtain  $\Delta H_{\rm f}^{\rm exp}$ . The key difference between transfer learning and multifidelity machine learning is that in the former two networks are trained and information transfer is achieved by transferring network weights, while in the latter, only one model is trained and information transfer is achieved by learning the difference between two datasets and adding the  $\Delta H_{\rm f}^{\rm DFT}$  as one of the input features. In addition to the two basic strategies as shown in Figure 1a,b, variants are also tested in this work, including a combination of transfer learning and multifidelity machine learning (initializing a network from one

Fable 1. Comparison of MAEs between $\Delta H_{ m f}^{ m ex}$	$^{49}$ and $\Delta H_{ m f}$ from Different Density Functionals with Different Correction	15
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functional (correction)	PBE (random forest)	PBE (linear, Jain et al. <sup>46</sup> )	PBE (linear, Wang et al. <sup>47</sup> )	PBEsol (no) <sup>44</sup>	SCAN (no) <sup>44</sup>	r <sup>2</sup> SCAN (no) <sup>44</sup>
MAE (eV/atom)	0.0542	0.0935	0.0927	0.0973	0.1024	0.0825
<sup>a</sup> Different from Figure	2, the reported MAEs	here are based on a datas	set with 122 materials in th	ne test set that ha	ve all of the val	ues of $\Delta H_{ m f}$ from

different sources. The cell of "PBE (random forest)" is the PBE  $\Delta H_{\rm f}$  that is first corrected by Jain et al.<sup>46</sup> and then corrected by the best RF model in this work. "PBE (linear, Jain et al.<sup>46</sup>)" is the one used in the MP database before May 2021 (V2021.03.22) and is the one used as the low-fidelity data in this work ( $\Delta H_{\rm f}^{\rm DFT}$ ). "PBE (linear, Wang et al.<sup>47</sup>)" is the one used in the MP database after May 2021 (V2021.05.13). "(no)" in the right three cells at the upper row means that no correction is applied to the  $\Delta H_{\rm f}$  from the density functional.

trained on  $\Delta H_{\rm f}^{\rm DFT}$  and optimizing the newly initialized network by  $\Delta H_{\rm f}^{\rm diff}$ ) and multifidelity machine learning by only learning  $\Delta H_{\rm f}^{\rm diff}$  or only adding  $\Delta H_{\rm f}^{\rm DFT}$  as an input feature.

As described above, we choose four different machine learning architectures to realize transfer learning and/or multifidelity machine learning, which are RF, MLP, ROOST, and CGCNN. The choice aims to increase the variety of machine learning architectures to fairly evaluate the effect of transfer learning and multifidelity learning and to enlarge the hypothesis space to search for the best machine learning models for predicting  $\Delta H_{\rm f}^{\rm exp}$ . These ML architectures also provide varieties in terms of basic algorithms, input information, and featurization: MLP, ROOST, and CGCNN are based on neural networks, while RF is not; ROOST only needs compositions as an input, while CGCNN takes both compositions and threedimensional (3D) structures as input, and RF and MLP can be trained either with or without structural information; RF and MLP need human-engineered featurization, while ROOST and CGCNN learn fingerprints of materials in the training process.

In this work, we choose the Materials Project (MP) database (V2021.03.22) as the source of  $\Delta H_{\rm f}^{\rm DFT}$  because MP is a widely used large DFT database and the difference of  $\Delta H_{\rm f}$  between MP and other large DFT databases is not large. For example, the difference between  $\Delta H_{\rm f}$  of 563 materials from MP and OQMD is reported to be 0.028 eV/atom.<sup>3</sup> As for the experimentally measured  $\Delta H_{\rm fr}$  we combine the IIT dataset<sup>17</sup> and SSUB dataset<sup>58</sup> and remove the duplicates, leading to 1143 data points with available  $\Delta H_{\rm f}^{\rm exp}$ ,  $\Delta H_{\rm f}^{\rm DFT}$ , and DFT-optimized 3D atomic structures from MP. In addition to the value of  $\Delta H_{\rm f}^{\rm exp}$ , there are also uncertainty estimations in the IIT dataset,<sup>17</sup> from which one can see that the mean uncertainty of  $\Delta H_{\rm f}^{\rm exp}$  based on 499 materials is around 0.023 eV/atom. More details about the data collection procedure are provided in the Methods section.  $\Delta H_{\rm f}^{\rm DFT}$  and  $\Delta H_{\rm f}^{\rm exp}$  are compared in Figure 1c, from which one can see that  $\Delta H_{\rm f}^{\rm DFT}$  are already quite close to  $\Delta H_{\rm f}^{\rm exp}$  in value, and there is no clear systematic shift between  $\Delta H_{\rm f}^{\rm DFT}$  and  $\Delta H_{\rm f}^{\rm exp}$  As shown in Figure 1d, the distribution of  $\Delta H_{\rm f}^{\rm diff}$  is centered around zero, and there is no obvious correlation between  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm DFT}$ . From Figure 1c,d, one can see that  $\Delta H_{\rm f}^{\rm diff}$  has a narrower distribution than  $\Delta H_{\rm f}^{\rm exp}$  with the standard deviation of 0.1718 and 0.8000 eV/atom for the datasets of  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ , respectively.

#### Predicting $\Delta H_{\rm f}^{\rm exp}$ by Machine Learning

For the RF and MLP, compositional and structural features are provided from matminer<sup>59</sup> as input features (a list of features is provided in the Methods section), for ROOST only, the compositions are provided as input and it automatically learns the fingerprints of materials, and for CGCNN, the compositions and 3D atomic structures are provided as input and the fingerprints are learned in the training. To test the prediction performance, 20% of the 1143 materials are chosen randomly as the test set. Details about the training procedure are provided in the Methods section. As a baseline, for the test set, we find that the MAE between  $\Delta H_{\rm f}^{\rm DFT}$  and  $\Delta H_{\rm f}^{\rm exp}$  is 0.0955 eV/atom. The test results for some machine learning models are shown in Figure 2a with detailed lists of all machine learning models in Figure S3 and Table S1, and here we analyze the results from the following aspects:

(1) The best performance is achieved with the RF model that is trained on  $\Delta H_f^{\text{diff}}$  and has compositional features and  $\Delta H_f^{\text{DFT}}$  as input features (Figure 2a). The error for this best case, 0.0617 eV/atom, is roughly 30% lower than that of  $\Delta H_f^{\text{DFT}}$ . The parity plot of  $\Delta H_f^{\text{DFT}}$  and  $\Delta H_f^{\text{ML}}$  from the best RF model versus  $\Delta H_f^{\text{exp}}$  of the test set is shown in Figure 2b, from which one can observe that  $\Delta H_f$  from the best RF model aligns closer to the  $\Delta H_f^{\text{exp}}$  than  $\Delta H_f^{\text{DFT}}$ within the range from -5 to 1 eV/atom. Predictions from the best RF model also have a higher  $R^2$  score (0.99) than that from the DFT calculations in the MP database (0.97).

Recently, Kingsbury et al.44 have performed highthroughput calculations for 6000 materials by PBEsol,<sup>38</sup> <sup>59</sup> and r<sup>2</sup>SCAN functional.<sup>40</sup> In Table 1, MAEs SCAN,<sup>3</sup> between experimental  $\Delta H_{\rm f}$  and  $\Delta H_{\rm f}$  from different density functionals with different empirical corrections are listed. Different from Figure 2, the reported MAEs in Table 1 are based on a dataset with 122 materials that have all of the values of  $\Delta H_{\rm f}$  from different sources (these materials are in the test set mentioned above). One can observe that MAE of the best RF model is almost half of that of SCAN,<sup>39</sup> PBEsol,<sup>38</sup> and also almost half of that of the corrections from Jain et al.<sup>46</sup> and Wang et al.<sup>47</sup> The superiority of the best RF model over the metageneralized gradient approximation (meta-GGA) functionals (SCAN and r<sup>2</sup>SCAN) is encouraging because (i) the best RF model provides a lower error compared with more sophisticated density functionals, (ii) it is much faster than the self-consistent DFT simulations, especially with meta-GGA functionals, enabling one to screen  $\Delta H_{\rm f}$ of materials accurately in a high-throughput fashion. For example, for the 10<sup>5</sup> materials in large DFT databases such as MP, more accurate predictions of  $\Delta H_{\rm f}$  can be calculated by the RF models within minutes, while that from meta-GGA functionals may take months of calculations. For new materials without low-fidelity  $\Delta H_{\rm f}$ predictions yet (such as corrected PBE), computational cost for the low-fidelity  $\Delta H_{\rm f}$  should be added to the total cost of the best RF model.

As for the superiority of the best RF model over the recent linear correction scheme from Wang et al.,<sup>47</sup> as shown in Table 1, there are four possible explanations: (i) the RF model takes nonlinear effects into account, (ii) the compositional descriptors used here capture more information than simple stoichiometry used in Wang et al.,<sup>47</sup> (iii) the learned correction in Wang et al.,<sup>47</sup> is only from materials with certain anions and transition metals,

while in the present work, there is no such constraint, and (iv) the calibration scheme used here is built on empirically corrected PBE results as opposed to uncorrected PBE data in Wang et al.<sup>47</sup>

(2) Training the machine learning models on  $\Delta H_{\rm f}^{\rm diff}$  helps to reduce error compared with training models on  $\Delta H_{\rm f}^{\rm exp}$ directly, as, under the same condition (architecture and featurization), the models trained on  $\Delta H_{\rm f}^{\rm diff}$  always have lower MAE than that trained on  $\Delta H_{\rm f}^{\rm exp}$ . Here, we attribute the lower absolute error of learning  $\Delta H_{\rm f}^{\rm diff}$  to the fact that  $\Delta H_{\rm f}^{\rm diff}$  has a narrower distribution than  $\Delta H_{\rm f}^{\rm exp}$ with 5 times smaller standard deviation (0.17 versus 0.80 eV/atom). One can imagine that, if  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ have the same distribution except for a scaling factor of 1/5, then ideally the MAEs of ML models (with proper normalization) trained on  $\Delta H_{\rm f}^{\rm diff}$  should also be 1/5 of that trained on  $\Delta H_{\rm f}^{\rm exp}$ . However, the MAEs of models trained on  $\Delta H_{\rm f}^{\rm diff}$  are all larger than 1/5 of that trained on  $\Delta H_{\rm f}^{\rm exp}$ , suggesting that  $\Delta H_{\rm f}^{\rm diff}$  is easier to learn absolutely but harder to learn relatively than  $\Delta H_f^{exp}$ .

To further illustrate the above explanation, we use the  $R^2$  score, a unitless metric invariant to scaling, to show the relative difficulty of predicting  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ . The  $R^2$  of predictions of  $\Delta H_{\rm f}^{\rm diff}$  by the best RF model is 0.54 (here  $R^2$  of 0.54 is based on predicted  $\Delta H_{\rm f}^{\rm diff}$  versus true  $\Delta H_{\rm f}^{\rm diff}$ , while the  $R^2$  of 0.99 in Figure 2b is based on predicted  $\Delta H_{\rm f}^{\rm diff}$  predictions of  $\Delta H_{\rm f}^{\rm exp}$ ), while the  $R^2$  of predictions of  $\Delta H_{\rm f}^{\rm exp}$  by the same RF model is 0.94, suggesting that  $\Delta H_{\rm f}^{\rm exp}$  is easier to learn relatively than  $\Delta H_{\rm f}^{\rm diff}$ .

(3) Feeding  $\Delta H_{\rm f}^{\rm DFT}$  as one of the input features helps to lower the error, as with the same machine learning architecture (RF or MLP), label, and other features, models with  $\Delta H_{\rm f}^{\rm DFT}$  as one of the input features always have lower error than that without  $\Delta H_{\rm f}^{\rm DFT}$ . This effect is more significant when the models are trained on  $\Delta H_{\rm f}^{\rm exp}$ because, as shown in Figure 1c,  $\Delta H_{\rm f}^{\rm DFT}$  has a strong correlation with  $\Delta H_{\rm f}^{\rm exp}$ , while, as shown in Figure 1d, the correlation between  $\Delta H_{\rm f}^{\rm DFT}$  and  $\Delta H_{\rm f}^{\rm diff}$  is not obvious.

Combining analyses (2) and (3), one can observe that adapting the strategy of multifidelity machine learning might help to significantly lower prediction error if the difference between the different fidelity datasets has a narrower distribution than the high-fidelity dataset and/ or if there is a strong correlation between the different fidelity data sets. Machine learning models with both the modifications of changing labels and adding extra input features might outperform that with either single modification.

- (4) Similar to (3), transfer learning helps more when transferring from  $\Delta H_f^{\text{DFT}}$  to  $\Delta H_f^{\text{exp}}$  than from  $\Delta H_f^{\text{DFT}}$  to  $\Delta H_f^{\text{diff}}$  because of the stronger correlation between  $\Delta H_f^{\text{DFT}}$  and  $\Delta H_f^{\text{exp}}$ .
- (5) RF with human-engineered features performs better than ROOST and CGCNN, two deep representation learning models, when trained on  $\Delta H_{\rm f}^{\rm diff}$ , while RF performs similar to or worse than neural network-based models when trained on  $\Delta H_{\rm f}^{\rm exp}$ . Although it is not surprising that neural network-based deep learning algorithms do not show superior performance over RF due to the limited dataset size, <sup>52,60</sup> the effect of learning targets ( $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ ) on the relative performance of different machine learning models is interesting and worth discussion.

The different uncertainty levels between  $\Delta H_f^{\text{diff}}$  and  $\Delta H_f^{\text{exp}}$ might help to explain why RF performs better than neural network-based models when trained on  $\Delta H_f^{\text{diff}}$ , while there is no such superiority of RF when trained on  $\Delta H_f^{\text{exp}}$ . As discussed above,  $\Delta H_f^{\text{diff}}$  has a narrower distribution than  $\Delta H_f^{\text{exp}}$ . Because  $\Delta H_f^{\text{diff}} = \Delta H_f^{\text{exp}} - \Delta H_f^{\text{DFT}}$ , if we assume  $\Delta H_f^{\text{exp}}$  and  $\Delta H_f^{\text{DFT}}$  are two independent random variables, then  $\Delta H_f^{\text{diff}}$  would have larger uncertainty than  $\Delta H_f^{\text{exp}}$ . Therefore, the robustness of RF against uncertainty  $^{60-62}$  might explain the superiority of RF when trained on  $\Delta H_f^{\text{diff}}$ . The larger uncertainty level of  $\Delta H_f^{\text{diff}}$ might also help to explain why  $\Delta H_f^{\text{diff}}$  is harder to learn relatively than  $\Delta H_f^{\text{exp}}$  as in (2).

To further investigate the effect of uncertainty on the performance of machine learning models, RF and ROOST are employed to learn  $\Delta H_f^{exp}$  with random noises, a source of uncertainty. In Figure 2a, one can see that RF performs worse than ROOST when trained on  $\Delta H_f^{exp}$ . In Figure 2c, the MAEs of RF and ROOST and the corresponding noise levels are shown. One can see that, under low noise levels, the errors of RF are still higher than that of ROOST, while under high noise levels, the errors of RF become lower than that of ROOST. The different relative performances of RF and ROOST under different noise levels agree with the superiority of RF against uncertainty  $^{60-62}$  and support our hypothesis that the different uncertainty levels of the  $\Delta H_f^{diff}$  dataset and the  $\Delta H_f^{exp}$  dataset might explain why RF is better on the  $\Delta H_f^{diff}$  dataset.

In Figure 2e, we plot the learning curves of RF and ROOST on learning  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ , respectively. For learning  $\Delta H_{\rm f}^{\rm exp}$ , we observe that with a few data points, RF has smaller errors than ROOST, while with more than 400 data points, ROOST outperforms RF, which agrees with previous observations<sup>26,63</sup> that deep learning is powerful for large datasets, while classic machine learning is more suitable for small datasets. However, for learning  $\Delta H_{\rm f}^{\rm diff}$ , we observe that RF performs better than ROOST consistently for all dataset sizes. As for the rate of improvement with respect to dataset size (slope of learning curve), we observe that for RF, the slope on learning  $\Delta H_{\rm f}^{\rm diff}$  is slightly smaller than that on  $\Delta H_{\rm f}^{\rm exp}$ , while for ROOST, the slope on learning  $\Delta H_{\rm f}^{\rm diff}$  is significantly smaller than that on  $\Delta H_{\rm f}^{\rm exp}$ , which shows that the slopes of learning curves of machine learning models are affected by the quality of data: higher uncertainty of data, smaller slope of learning curves, and different machine learning models are affected differently: the slope of RF is less affected, while the slope of ROOST is more affected. Further empirical and theoretical studies are necessary to investigate the relation between data quality and the slope of the learning curve for different machine learning models. From the learning curves, we also expect that, with more  $\Delta H_{\rm f}^{\rm exp}$  data points in the future, learning  $\Delta H_f^{exp}$  directly by ROOST might be more powerful than learning  $\Delta H_f^{\text{diff}}$  by random forest.

Based on the fact that when trained on  $\Delta H_{\rm f}^{\rm diff}$ , random forest with human-engineered featurization outperforms neural network-based models, especially deep representation learning models, we suggest that for machine learning applications in the field of materials science, with limited data set size and without proof of a low uncertainty level of the data set, deep neural network-based representation learning algorithms<sup>24,26,32,64</sup> should not be the only type of models employed, and other feature engineering methods and machine learning architectures beyond neural networks should also be tested.

While there are some previous works that show that information on the local bonding environment can be used to correct formation enthalpies of certain materials like sulfides,  $^{65}$  fluorides,  $^{66}$  and oxides,  $^{48,66}$  in this work, the machine learning models with only compositions as input outperform those with both compositions and structures as input (Figures 2a and S3). One of the possible causes of the phenomenon is that there still lack the data points of polymorphs with the same composition but different  $\Delta H_{\rm f}^{\rm exp}$  in the current dataset, which suggests the urgency of building a comprehensive  $\Delta H_{\rm f}^{\rm exp}$  dataset with sufficient entries of polymorphs to comprehensively understand the role of structures in determining  $\Delta \bar{H_{\rm f}}^{\rm exp}.$  In Figure 2e, we plot the learning curves for random forest (RF) with and without structural features for learning  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ . We can observe that, for learning  $\Delta H_{\rm f}^{\rm diff}$  and  $\Delta H_{\rm f}^{\rm exp}$ , RF without structural features outperforms RF with structural features, while the slopes of learning curves of the RF models with structural features are larger than that of the RF models without structural features. A possible explanation is that models with structural features have more available information, more degrees of freedom, and therefore easier to overfit small data sets, while those additional information makes models with structural information more powerful and consequently with steeper learning curves. Based on the learning curves, we expect that with more data in the future, models with structural information might outperform those with only compositional information.

For the models only based on compositional information, such as random forest with only compositional features and ROOST, the corrections are the same for the polymorphs. Since the best model in this work is only based on compositional information, in the following sections, the analysis is purely based on compositions. However, there are also models based on structural information trained and tested in this work, such as random forest with compositional and structural features and CGCNN. Corrections from models with structural information are in principle different for polymorphs. In Table S2, we show the corrections from random forest (RF) with both compositional and structural features ("struct. RF diff." in Figure S3 and Table S1) to three pairs of polymorphs with recorded  $\Delta H_{\rm f}^{\rm exp}$ values and not in the training set. We find that, for all materials except CaSiO<sub>3</sub> wol.,  $\Delta H_{\rm f}^{\rm RF}$  is closer to  $\Delta H_{\rm f}^{\rm exp}$  than  $\Delta H_{\rm f}^{\rm DFT}$ , showing the ability of the RF model to correct the DFT prediction of  $\Delta H_{\rm f}$ . As for relative phase stability,  $\Delta H_{\rm f}^{\rm DFT}$ contradicts with  $\Delta H_{\rm f}^{\rm exp}$  for SiO<sub>2</sub> and TiO<sub>2</sub>. Unfortunately, for the two systems, corrections from RF cannot reverse the wrong phase stability estimation from DFT. A possible explanation is that the RF model mainly employs compositional information to learn and predict, as we find that compositional features contribute 80% of feature importance, while structural features only contribute 20% of feature importance. Therefore, the RF model predicts similar corrections to different structures with the same composition. More data points of  $\Delta H_{\rm f}^{\rm exp}$ , especially that of polymorphs, are necessary to develop machine learning models that rely more on structural information and are capable of reversing the wrong phase stability estimation of polymorphs from DFT.

We summarize the potential drawbacks of using one model versus the others for predicting  $\Delta H_{\rm f}$  as follows: (i) RF and MLP rely on off-the-shelf featurization, which means that they cannot capture information unknown to human beings. Therefore, they are typically less powerful than deep representation learning models such as ROOST and CGCNN for large datasets.<sup>26,63</sup> For predicting  $\Delta H_{\rm fr}$  although RF is the best model in this work, with more data points in the future, it is likely that RF will be less powerful than ROOST as shown by the learning curves in Figure

2d. (ii) ROOST and CGCNN are deep representation learning models that learn the features of materials automatically in the training process. Therefore, they are thought to be more powerful than models with off-the-shelf featurization, but their prediction performance might be worse with small datasets,<sup>26,63</sup> such as this work. (iii) MLP, ROOST, and CGCNN are neural network-based models. Compared with random forest, which is a decision tree-based ensemble model with hundreds of individual models, ensembles of neural networks are typically only composed of around 10 individual models because of the higher computational cost of neural networks.<sup>26</sup> Therefore, they might be less powerful than RF in cases where the number of models in ensembles is important,<sup>62</sup> such as the  $\Delta H_f^{\text{diff}}$  with high uncertainty in this work.<sup>62</sup>

#### Discovering Materials with Underestimated Stability in MP

With the best RF model that can significantly lower the error of  $\Delta H_{\rm f}$  from the MP database, we can calibrate  $\Delta H_{\rm f}$  of all materials in the MP database. The dataset with all of the calibrated  $\Delta H_{\rm f}$  is provided in the Supporting Information, and as an application, here we use the calibrated  $\Delta H_{\rm f}$  to re-evaluate the thermodynamic stability of all materials in the MP database by constructing the energy above hull  $(E_{hull})$  the energy difference between the candidate compound and the ground-state phase(s) in a compositional space.<sup>67</sup> More discussions about  $E_{\text{hull}}$  are provided in the Methods section and Figure S3). However, as Bartel et al.<sup>18</sup> pointed out, although sometimes DFT has large errors for the prediction of  $\Delta H_{\rm fr} \Delta H_{\rm fr}^{\rm DFT}$  of similar materials contain similar systematic errors, and when evaluating phase stability, the cancellation of systematic errors makes DFT more useful for evaluating the relative stability between compounds than some machine learning models with similar or even better accuracy with respect to  $\Delta H_{\rm f}^{\rm exp}$ .

Therefore, before screening  $E_{hull}$  for the full MP dataset, we first evaluate the performance of  $\Delta H_f^{DFT}$  and  $\Delta H_f^{ML}$  for evaluating the relative stability between compounds. Since there are only 229 materials in the test set, which are not enough for constructing phase diagrams and  $E_{hull}$ , we use the difference between  $\Delta H_f$  of pairs of compounds in the same chemical system to evaluate the relative stability between compounds. We list all 20 pairs of compounds in the same chemical system in the test set in Table 2, and we also plot the difference from experiments versus that from MP and machine learning (ML) in Figure 3a. One can see that ML outperforms MP in terms of the difference of  $\Delta H_f$  between compounds in the same chemical system, which shows that the ML model outperforms DFT for relative stability evaluation.

We next re-evaluate material stability using ML calibrated  $\Delta H_{\rm f}$  to construct  $E_{\rm hull}^{\rm ML}$  for all materials in the MP database using all compositions in MP. In chemical intuition, materials with smaller  $E_{\rm hull}$  tend to be more thermodynamically synthesizable and stable, <sup>19,20,68</sup> although  $E_{\rm hull} = 0$  is not a hard threshold for successful synthesis and room-temperature and pressure stabilities of materials because of other factors such as kinetics, <sup>69</sup> and in practice, empirical heuristics of several room-temperature  $k_{\rm B}T$  are used as stability thresholds. <sup>19,20,68</sup> In Figure 3b, the distributions of  $E_{\rm hull}$  of all materials in the MP database constructed from  $\Delta H_{\rm f}^{\rm DFT}$  and  $\Delta H_{\rm f}^{\rm ML}$  of all compositions in the MP database are shown, from which one can see that most materials have similar  $E_{\rm hull}^{\rm MP}$  and  $E_{\rm hull}^{\rm ML}$ , and majority of materials have close-to-zero  $E_{\rm hull}^{\rm MP}$  and  $E_{\rm hull}^{\rm ML}$ . More importantly, there are materials with large  $E_{\rm hull}^{\rm ML}$  and small  $E_{\rm hull}^{\rm ML}$ . These materials might have underestimated stabilities in

Table 2. Difference of  $\Delta H_{\rm f}$  between Pairs of Compounds in the Same Chemical System from Different Sources<sup>*a*</sup>

pair of compounds	experiment	materials project	machine learning in this work			
TiFe <sub>2</sub> -TiFe	0.0487	-0.1324	-0.1316			
BiI3-BiI	0.1075	0.1868	0.1193			
LuIr <sub>2</sub> -LuIr	-0.1502	-0.1664	-0.1826			
LaSi-La <sub>5</sub> Si <sub>3</sub>	0.143	0.1335	0.1229			
BMo <sub>2</sub> -BMo	-0.1858	-0.1856	-0.1972			
Na <sub>2</sub> O-NaO <sub>2</sub>	0.5435	0.5428	0.3328			
$BW_2 - B_5W_2$	-0.0591	0.5108	0.2408			
Co <sub>3</sub> O <sub>4</sub> -CoO	0.1229	-0.0302	-0.0553			
ZrCo <sub>2</sub> -Zr <sub>2</sub> Co	0.0974	0.0574	0.0553			
TmAg–TmAg <sub>2</sub>	0.1835	0.0088	0.1187			
PrNi5-PrNi	-0.0259	-0.0281	-0.0116			
TiAu <sub>2</sub> -TiAu	0.0179	-0.0026	-0.0243			
NdRh–NdRh <sub>2</sub>	0.0446	0.0202	0.0064			
CaO <sub>2</sub> –CaO	-1.0353	-1.1070	-1.075			
Zr <sub>5</sub> Si <sub>3</sub> -Zr <sub>5</sub> Si <sub>4</sub>	-0.2094	-0.0855	-0.0964			
Zr <sub>5</sub> Si <sub>3</sub> -ZrSi <sub>2</sub>	0.1181	0.1654	0.1397			
$Zr_5Si_4$ – $ZrSi_2$	0.3275	0.2509	0.2361			
Mn <sub>2</sub> Sb-MnSb	-0.0824	0.3453	0.1428			
CrSi-CrSi <sub>2</sub>	0.0090	-0.0783	-0.0280			
$Mn_{11}Si_{19}$ - $Mn_3Si$	0.0596	0.1276	0.0809			
<sup>a</sup> Difference of $\Delta H_{ m f}$ is the unit of eV/atom.						

MP. For example, there are 800 materials in the blue rectangle in the upper-left corner in Figure 3b that have  $E_{\rm hull}^{\rm MP} > 0.16 \ {\rm eV}/$  atom and  $E_{\rm hull}^{\rm ML} < 0.06 \ {\rm eV}/$  atom, among which there are around 100 already synthesized materials. (The thresholds are based on 6 times and 2 times of room-temperature  $k_{\rm B}T$ .<sup>19,20</sup>) As example, we list some materials in Table 3 with novel physical properties and/or potential applications with  $E_{\rm hull}^{\rm MP} > 0.16 \ {\rm eV}/$  atom and  $E_{\rm hull}^{\rm ML} < 0.06 \ {\rm eV}/$  atom, where there are both synthesized materials and hypothetical materials. One can see that there are a number of materials with various applications ranging from battery electrodes, <sup>70</sup> catalysts<sup>71–73</sup> to optical, <sup>74–76</sup> electronic, <sup>77,78</sup> magnetic <sup>79–83</sup> devices, and superconductors<sup>84,85</sup> for which  $E_{\rm hull}^{\rm ML}$  succeeds in explaining their synthesizability,

while  $E_{\text{hull}}^{\text{MP}}$  suggests a low likelihood of being synthesizable. One extreme example is MnSnIr,<sup>86</sup> a stable half-Heusler compound synthesized from a peritectic reaction,<sup>87</sup> of which  $E_{\rm hull}^{\rm MP}$  is considerably high (0.5117 eV/atom), while  $E_{\rm hull}^{\rm ML}$  is 0. The huge gap between  $E_{\rm hull}^{\rm MP}$  and  $E_{\rm hull}^{\rm ML}$  is mainly because of the large deviation between  $\Delta H_{\rm f}^{\rm DFT}$  (0.2945 eV/atom) and  $\Delta H_{\rm f}^{\rm ML}$  (-0.2363 eV/atom) of MnSnIr itself. As a comparison, the  $\Delta H_{\rm f}^{\rm exp}$  of MnSnIr is -0.3047 eV/atom, <sup>17</sup> which shows that, for this compound, DFT deviates significantly from the experiment, while our machine learning model can calibrate such a huge difference. A possible reason for the large error of  $\Delta H_{\rm f}^{\rm DFT}$  of MnSnIr is that, in Materials Project (V2021.03.22), the DFT + U correction is only applied to Mn-F, Mn-O, and Mn-S systems and not applied to systems without F, O, S such as the full ternary compound MnSnIr.<sup>46</sup> Large deviations between  $\Delta H_{\rm f}^{\rm DFT}$  and  $\Delta H_{\rm f}^{\rm exp}$  are also observed for other compounds containing Mn and Sn, such as MnSnAu ( $\Delta H_f^{DFT}$ :  $-0.0488 \text{ eV/atom}; \Delta H_{f}^{exp}: -0.5016 \text{ eV/atom}), \text{ MnSn}_{2}$ ( $\Delta H_{\rm f}^{\rm DFT}$ : 0.1363 eV/atom;  $\Delta H_{\rm f}^{\rm exp}$ : -0.0954 eV/atom), and  $Mn_2SnRu$  ( $\Delta H_f^{DFT}$ : 0.0789 eV/atom;  $\Delta H_f^{exp}$ : -0.1803 eV/ atom), which agrees with the observation in Figure 4b shown later that DFT tends to overestimate  $\Delta H_{\rm f}$  (more positive) of compounds with Mn and Sn. As a result, in the phase diagram of Mn-Sn, there are no stable intermetallic compounds according to  $\Delta H_{\rm f}^{\rm DFT}$ , which disagrees with the experimental phase diagram where there are several stable intermetallics including Mn<sub>3</sub>Sn, Mn<sub>3</sub>Sn<sub>2</sub>, and MnSn<sub>2</sub>.<sup>88</sup>

In addition to the already synthesized materials, those unrealized hypothetical materials provide potential opportunities for energy and environmental materials,<sup>89–91</sup> structural materials,<sup>92</sup> and electronic devices,<sup>93,94</sup> and as shown in Table 3 and Figure 3b, many of these materials that are estimated stable by  $E_{\rm hull}^{\rm ML}$  might have underestimated stability in the MP database.

There are also 1000 materials in the lower-right corner in Figure 3b that have  $E_{hull}^{MP} < 0.06 \text{ eV/atom}$  and  $E_{hull}^{ML} > 0.16 \text{ eV/atom}$ . Details of those materials can be obtained in the shared online dataset. An extreme example is LiNbGeO<sub>5</sub>,<sup>95</sup> a



**Figure 3.** Stability evaluation from energy above hull. (a) Difference of  $\Delta H_{\rm f}$  between pairs of compounds in the same chemical system from experiments versus that from MP and machine learning. (b) Distribution of energy above hull ( $E_{\rm hull}$ , in eV/atom) of all materials in the Materials Project<sup>2</sup> database calculated by the corrected PBE  $\Delta H_{\rm f}$  in MP ( $E_{\rm hull}^{\rm MP}$ ) versus that calculated by the machine learning  $\Delta H_{\rm f}$  in this work ( $E_{\rm hull}^{\rm ML}$ ). Here,  $E_{\rm hull}$  is constructed from all materials in the Materials Project database. The color scheme is used to show the (log 10 of) number of materials within a range of certain  $E_{\rm hull}^{\rm ML}$  and  $E_{\rm hull}^{\rm MP}$ , and the blue rectangle shows the area with  $E_{\rm hull}^{\rm MP} > 0.16 \text{ eV}/atom$  and  $E_{\rm hull}^{\rm ML} < 0.06 \text{ eV}/atom$ . (c) Appearance frequencies of number of elements of each material in the data sets. Here, "exp. dataset" is the  $\Delta H_{\rm f}^{\rm exp}$  used in this work, "MP database" is the set of all materials with  $E_{\rm hull}^{\rm MP} > 0.16 \text{ eV}/atom$  and  $E_{\rm hull}^{\rm ML} < 0.06 \text{ eV}/atom$ , and "MP stable, ML unstable" is the set of materials with  $E_{\rm hull}^{\rm MP} > 0.16 \text{ eV}/atom$ .

# Table 3. Examples of Materials That Have Novel Physical Properties and/or Potential Applications with $E_{\text{hull}}^{\text{MP}} > 0.16 \text{ eV/Atom}^{a}$ and $E_{\text{hull}}^{\text{ML}} < 0.06 \text{ eV/Atom}^{a}$

materials	MP ID	$E_{\rm hull}{}^{\rm MP}$	${E_{\rm hull}}^{\rm ML}$	characterization method(s)	comment/novel physical property/potential application
MnSnIr	mp-11480	0.5117	0	experiment	largest difference between $E_{ m hull}{}^{ m MP}$ and $E_{ m hull}{}^{ m ML}$
Ta <sub>3</sub> Pb	mp-1187214	0.3386	0	experiment	superconductor <sup>85</sup>
AgRh	mp-1183233	0.2633	0.0359	experiment	electrocatalyst <sup>71</sup>
FeCoSn	mp-1025124	0.1836	0.0384	experiment	tuning phase transitions for isostructural alloying <sup>96</sup>
SmCo <sub>4</sub> Ag	mp-1219086	0.1797	0.0493	experiment	positively correlated magnetization with temperature <sup>79</sup>
$Li_3(FeS_2)_2$	mp-753818	0.1697	0.0180	experiment	Li–FeS <sub>2</sub> battery electrode <sup>70</sup>
PdRu	mp-1186459	0.2277	0.0032	experiment	catalyst <sup>72</sup>
Ni <sub>3</sub> Ag	mp-1100764	0.2332	0	experiment	dual-frequency absorption <sup>74</sup>
$Rb_2NaTaF_6$	mp-1114459	0.2038	0	experiment	large anisotropic shift from both covalent and polarization spin transfer mechanisms $^{\rm 80}$
Nb <sub>3</sub> Tl	mp-569366	0.2083	0	experiment	superconductor <sup>84</sup>
UPb <sub>3</sub>	mp-1184128	0.1621	0	experiment	sharp metamagnetic transitions <sup>81</sup>
Cu <sub>3</sub> N	mp-1933	0.1865	0.0464	experiment	light recording media <sup>75</sup>
FeNi <sub>2</sub>	mp-1072076	0.1858	0.0292	experiment	size-dependent catalytic activity <sup>73</sup>
HfCo <sub>7</sub>	mp-1105489	0.2098	0.0500	experiment	rare-earth-free permanent magnets <sup>82</sup>
MnBi	mp-1185989	0.2078	0	experiment/DFT	half-metallic ferromagnetism <sup>78</sup>
Be <sub>2</sub> Si	mp-1009829	0.2352	0.0272	experiment/DFT	hybrid nodal-line semimetal <sup>77</sup>
Mn <sub>2</sub> Hg <sub>5</sub>	mp-30720	0.2362	0	experiment/DFT	$\pi$ -based covalent magnetism <sup>83</sup>
Ta <sub>3</sub> Bi	mp-1187199	0.3442	0	DFT	topological dirac semimetal <sup>93</sup>
MnCrSb	mp-1221652	0.2564	0	DFT	half-metallicity <sup>94</sup>
LiB <sub>11</sub>	mp-1180507	0.2084	0.0234	DFT	pseudo-plasticity <sup>92</sup>
NiAg <sub>3</sub>	mp-976762	0.1850	0	DFT	acetylene adsorbent <sup>91</sup>
$Li_2VN_2$	mp-1246112	0.1615	0.0279	DFT	Li-ion battery electrode <sup>89</sup>
LiGdO3	mp-1185401	0.3476	0.0575	machine learning	perovskite with high tolerance factor <sup>90</sup>
LiPmO <sub>3</sub>	mp-1185388	0.2815	0	machine learning	perovskite with high tolerance factor <sup>90</sup>

"The materials with the experiment as one of the characterization methods are synthesized materials, and others are currently only hypothetical.  $E_{\text{hull}}$  is in the unit of eV/atom.



**Figure 4.** Impact of each feature on model output. (a, b) Distributions of the impacts (SHAP values<sup>97</sup>) of compositional features and elemental fractions on the model output ( $\Delta H_{\rm f}^{\rm diff}$ ), respectively. The color represents the feature value (red high, blue low), and here only the top 10 features and elemental fractions with the highest sum of absolute SHAP values are shown. The inset figure in panel (b) illustrates the trends of DFT to underestimate or overestimate  $\Delta H_{\rm f}$  of materials with certain nonmetal elements. Here, the blue-shaded elements are those for which DFT tends to underestimate  $\Delta H_{\rm f}$  the red-shaded elements are those for which DFT tends to overestimate  $\Delta H_{\rm f}$  and boron shows a mixed trend.

synthesized compound with  $E_{\text{hull}}^{\text{MP}}$  of 0 and  $E_{\text{hull}}^{\text{ML}}$  of 0.4334 eV/atom.

To further investigate how MP and ML disagree with each other, the appearance frequencies of the number of elements in each material in four data sets are plotted in Figure 3c. One can see that in the exp. dataset used as the training set in this work, around 90% of the materials are binary compounds and 10% of the materials are ternary, while in the MP database, there are about 40% contain more than three elements. Since the training set does not cover material space with more than three elements, the ML predictions for materials with more than three elements are extrapolations and in general less reliable than that for binary and ternary compounds. For the set of materials unstable by MP and stable by ML, the distribution of the number of elements is similar to that of the exp. dataset where the majority of materials are binary or ternary, while in the set of materials stable by MP and unstable by ML, most materials have four or five elements. Here, the lack of materials with more than three elements in the current  $\Delta H_f^{exp}$  dataset suggests that the ML predictions for materials with more than three elements should be carefully checked if ML and MP disagree with each other, and it also suggests the urgency of building a comprehensive  $\Delta H_f^{exp}$  dataset with sufficient entries of materials with more than three elements.

# Data Mining Where $\Delta H_{\rm f}^{\rm DFT}$ Fails by Explaining the Multifidelity Model

In addition to predicting more accurate  $\Delta H_{\rm f}$  and examining the stability of materials, the random forest model trained on  $\Delta H_{
m f}^{
m diff}$  $(\Delta H_{\rm f}^{\rm exp} - \Delta H_{\rm f}^{\rm DFT})$  with human-engineered features can also serve as a data-mining approach to reveal where and how  $\Delta H_{\rm f}^{\rm DFT}$  deviates from  $\Delta H_{\rm f}^{\rm exp}$  (as above,  $\Delta H_{\rm f}^{\rm DFT}$  refers to the empirically corrected PBE  $\Delta H_{\rm f}$  by Jain et al.<sup>46</sup> in the Materials Project database), which provides clearer trends than machine learning models trained on  $\Delta H_{\rm f}^{\rm DFT}$  only. Here, we analyze the relationship between human-understandable features and  $\Delta H_{\rm f}^{\rm diff}$  by explaining the model, or for each material, calculating the impact of each feature on the model output (known as the SHAP value<sup>97</sup>). Previously, the error of  $\Delta H_f^{\text{DFT}}$  is mostly discussed in the context of certain anions,<sup>3,41,46</sup> cations,<sup>3</sup> and transition metals.<sup>3,41,42</sup> In Figure 4a, the impacts of the top 10 compositional features from matminer<sup>59</sup> with the highest sum of absolute SHAP values are shown. One can see that, in addition to anion properties ("max GSbandgap"; the detailed explanations of the descriptors are available in the matminer paper<sup>59</sup>) and cation properties ("max GSvolume", "max NdValence", "min CovalentRadius", "min Electronegativity"), the mean field of elemental properties ("band center", "mode CovalentRadius") and standard deviation of elemental properties ("std NpUnifilled", "std NdValence") are also among the most impactful properties with respect to  $\Delta H_{\rm f}^{\rm diff}$ . For example, with smaller band center (geometric mean of electronegativity<sup>59</sup>),  $\Delta H_{\rm f}^{\rm diff}$  tends to be larger and  $\Delta H_{\rm f}^{\rm DFT}$  tends to be smaller than  $\Delta H_{\rm f}^{\rm exp}$ , which means that DFT tends to underestimate  $\Delta H_{\rm f}$  of systems with a smaller mean electronegativity. A possible explanation for this trend is that, for a smaller geometric mean of electronegativity, the ability of atoms to bind the electrons near the atomic nuclei is weaker, and electrons tend to be more delocalized. Since the GGA approximation tends to overestimate the electron delocalization,  $^{98}\Delta H_{\rm f}^{\rm DFT}$  tends to be more negative for the systems with delocalized bonds (stronger bonding). Another example is with a larger standard deviation of the number of p valence electrons,  $\Delta H_{\rm f}^{\rm diff}$  tends to be smaller and  $\Delta H_f^{\text{DFT}}$  tends to be larger than  $\Delta H_f^{\text{exp}}$ , suggesting that DFT tends to overestimate  $\Delta H_{\rm f}$  of systems with greater differences among p electrons. This trend might be explained by the hypothesis that, with more different p electron configurations, in general, the compound is more ionic, and because of the fact that the GGA approximation tends to underestimate the electron localization, 98 DFT (PBE)  $\Delta H_{\rm f}$  tends to be more positive for the systems with localized bonds (weaker bonding).

As for the impacts of certain cations and anions, or impacts of certain elements, we build a decision tree model that takes stoichiometry as input, and the SHAP values of the fraction of each element are plotted in Figure 4b. One can see that, with a higher atomic fraction of S, O, and N, DFT tends to underestimate  $\Delta H_{\rm fr}$  while for a higher atomic fraction of Sn, Mn, P, I, Te, Ba, and Al, DFT tends to overestimate  $\Delta H_{\rm f}$ . There are more nonmetal elements (6) in the top 10 most impactful elements than metals (2) and metalloids (2). Particularly, there is an interesting pattern of how DFT treats different nonmetal elements: as shown in Figures 4b and S2, for strong oxidizing nonmetal elements in the upper-right corner of the periodic table, including F, O, N, S, and Cl, DFT tends to underestimate  $\Delta H_{\rm fr}$  while for those nonmetal elements with weaker oxidizing ability, DFT tends to overestimate  $\Delta H_{\rm f}$ . However, the degree of overestimation or underestimation does not simply correlate with the oxidizing ability. For example, as shown in Figures 4b and S1, F has a stronger oxidizing ability than O and S, but the degree of underestimation of  $\Delta H_{\rm f}^{\rm DFT}$  for fluorides is less than that of oxides and sulfides. There are two possible sources of errors that would result in the observed trend: on the one hand, the underestimation or overestimation of  $\Delta H_c$  of materials with certain elements might come from the element type-based empirical corrections,<sup>3,46</sup> and, on the other hand, the intrinsic limit of the GGA and GGA + U approximation might cause the different deviation patterns. For example, Seo et al.99 have proposed that the GGA + U method used for transition-metal oxides in the MP database<sup>46</sup> overestimates the degree of hybridization between the d orbitals of transition metals and p orbitals of oxygen and thus making the calculated  $\Delta H_{\rm f}$  more negative.

The trend in Figure 4a also agrees with that in Figure 4b. For example, for max GSbandgap and max GSvolume, they are calculated in the following procedure: first, the ground-state band gaps and ground-state volumes of all of the elements in the compound are listed, and then the maximum values of band gaps and volumes are picked up. Therefore, max GSbandgap and max GSvolume actually relate to the existence of certain elements in the compound. Specifically, max GSbandgap describes the presence of a specific anion in the compound, while max GSvolume describes that of cation. Larger max GSvolume,  $\Delta H_{\rm f}^{\rm DFT}$ , tends to be larger (more positive) than  $\Delta H_{\rm f}^{\rm exp}$ . An explanation for this trend is that with a larger max GSvolume, the cation element tends to have a larger ground-state volume (closer to the bottom-left of the periodic table with the maximum value at Cs). If the cation is closer to the bottom-left of the table, the compound in general will be more ionic. Therefore,  $\Delta H_{\rm f}^{\rm DFT}$  tends to be more positive for the systems with more ionic bonds, as mentioned above. On the other hand, for larger max GSbandgap,  $\Delta H_{\rm f}^{\rm DFT}$  tends to be smaller (more negative) than  $\Delta H_{\rm f}^{\rm exp}$ . This phenomenon might be explained by the fact that, with a larger max GSbandgap, the anionic element is closer to the upper-right corner of the periodic table, the maximum value at N, and according to Figure 4b, the compound tends to have more negative  $\Delta H_{\rm f}^{\rm DFT}$ .

In Wang et al.<sup>47</sup> all anionic corrections are negative, which is because their correction is applied to the original PBE results and PBE tends to overestimate the energy of diatomic gas molecules,<sup>100</sup> while the trend shown here is based on the empirically corrected PBE energies from MP that already take the effect of the overestimated energy of diatomic gas molecules into account.

#### DISCUSSION AND CONCLUSIONS

In this work, we conduct a comprehensive machine learning study to learn and predict the experimental formation enthalpy of materials. We use two different strategies to transfer information from a larger DFT dataset to a smaller experimental dataset, transfer learning and multifidelity machine learning, and we use four machine learning architectures to realize the two strategies (RF, MLP, ROOST, CGCNN). We find that the random forest (RF) model trained on the difference between experimental and DFT formation enthalpies with the DFT formation enthalpy as one of the input features can achieve the lowest error, which is almost half of that of DFT (empirically corrected PBE), and it also outperforms other more accurate but more computationally expensive density functionals, such as meta-GGA functionals. Beyond identifying the best model, we suggest that the deep neural network-based representation learning algorithms and transfer learning should not be the only machine learning architecture and information transfer strategy considered. Other feature engineering methods such as humanengineered features, machine learning architectures beyond neural networks such as random forest, and information transfer strategy such as multifidelity machine learning should also be tested in machine learning applications for materials science.

As an application, we employ the best-found random forest model to calibrate the formation enthalpy of all materials in the Materials Project database, which are then used to construct the energy above hull and discover potentially important materials that have an underestimated stability in the MP database. Further, we use the machine learning model as a data-mining approach to identify patterns in the performance of DFT, for example, in its tendency to underestimate the formation enthalpy of materials with elements in the upper-right corner of the periodic table.

This work is based on the Materials Project database queried on March 2021 (V2021.03.22). The methodology of this work can also be applied to the updated Materials Project database (such as V2021.05.13) and other large DFT databases. It is expected that, with more accurate low-fidelity data (DFT formation enthalpy), such as the very recent datasets by Kingsbury et al.<sup>44</sup> and by Schmidt et al.<sup>101</sup> with thousands of materials calculated by meta-GGA functionals, the method in this work can be used to provide more accurate calibration (exp. formation enthalpy).

One potential limitation of the multifidelity model used in this work is that it requires the availability of low-fidelity data for the whole material space of interest, as in this work, DFT formation enthalpy is required for learning the difference of formation enthalpy from the experiment and DFT. In cases where lowfidelity data is not available to all of the materials, transfer learning might be more appropriate to transfer information between different data sets. Another scenario not considered in the current multifidelity machine learning scheme is that, for some properties, there might be datasets with multiple levels of fidelity available. In such cases, in addition to incorporating different fidelity data into the input, the learning of differences might be conducted multiple times to enlarge the availability of high-fidelity data gradually.

More broadly, for machine learning applications with small datasets, choosing proper models and strategies is critical to the usefulness of the machine learning models. On the one hand, with small datasets, one should carefully compare the performance of deep representation learning and classic machine learning models based on off-the-shelf featurization and make the choice for production. Typically, with more than 10,000 data points, deep representation learning might be more powerful; with less than 500 data points, classic machine learning models might be more suitable; and with more than 500 but less than 10,000 data points, a careful comparison is necessary for employing a suitable model for production. On the other hand, if larger low-fidelity data sets are available, then information transfer might be useful to improve the learning and prediction of the high-fidelity data. There are two strategies, transfer learning and multifidelity learning, for the information transfer. Although there still lacks a theoretical guarantee or quantitative metric to estimate whether information transfer would help or not, empirically, the two strategies are worth trying if the highand low-fidelity datasets are strongly correlated.

#### METHODS

#### **Data Collection**

In this work, we construct the  $\Delta H_f^{exp}$  dataset by combining two sources from IIT<sup>17</sup> and SSUB,<sup>58</sup> and we use the Materials Project<sup>2</sup> database (V2021.03.22) to construct the  $\Delta H_f^{\rm DFT}$  dataset. For the  $\Delta H_f^{\rm diff}$  dataset, since the  $\Delta H_f^{\rm DFT}$  values are provided for some materials in the IIT dataset,  $\Delta H_f^{\rm diff}$  values for those materials are obtained by subtracting the provided  $\Delta H_f^{\rm DFT}$  from the provided  $\Delta H_f^{\rm exp}$ , and for materials from the SSUB dataset, since the chemical formula is the only identifier, we take the lowest  $\Delta H_f^{\rm exp}$  for each formula, and for the  $\Delta H_f^{\rm DFT}$  of these materials, we assign the lowest  $\Delta H_f^{\rm DFT}$  to each formula. For overlaps between the IIT dataset and SSUB dataset, we take the  $\Delta H_f^{\rm exp}$  from the IIT database as the IIT database is a more recent one.<sup>17</sup> Note that the mean absolute difference of  $\Delta H_f^{\rm exp}$  between our dataset and the recent dataset from Wang et al.<sup>47</sup> is only 0.007 eV/atom. Codes and a step-bystep instruction for constructing the dataset are provided in the Supporting Information.

#### Machine Learning Model Training Procedure

In this work, the dataset of the 1143  $\Delta H_{\rm f}^{\rm exp}$  is used for three purposes: (1) hyperparameter tuning for each machine learning model, (2) model evaluation, and (3) production or prediction of  $\Delta H_f$  of all materials in the Materials Project database (MP). For purposes (1) and (2), we first randomly reserve 20% data as the test set for model selection (these 20% data are also excluded in the larger MP dataset for transfer learning). Then, to determine the best set of hyperparameters for each model, with the remaining 80% data, we randomly reserve 20% of the remaining data  $(20\% \times 80\% = 16\%$  of total data) as the validation set to evaluate each specific set of hyperparameters and use 80% of the remaining data  $(80\% \times 80\% = 64\%$  of total data) to train the machine learning model with the given set of hyperparameters. We screen hyperparameters by grid search, and tables of search space of hyperparameters are provided in the Supporting Information. Finally, with the best-found hyperparameters for each model, we use the 80% of the data (training set + validation set in the hyperparameter search step) to train machine learning models 10 times with different initializations and evaluate model performance and uncertainty using the 20% data held out at the very beginning (test set). For purpose (3), production, for the best prediction performance, all available 1143 data points are used to train the best-found model with the best-found hyperparameter.

In this work, we use four different machine learning architectures to realize transfer learning and/or multifidelity machine learning, random forest (RF), multilayer perceptron (MLP), Representation Learning from Stoichiometry (ROOST),26 and Crystal Graph Convolutional Neural Network (CGCNN).<sup>32</sup> For ROOST, we feed the compositions of materials as input, and it learns the representations of materials, and for CGCNN, we feed the 3D atomic structures of materials as input, and it also learns the representations. RF and MLP are realized by scikitlearn,<sup>102</sup> and we use the descriptors from matminer<sup>59</sup> to feed RF and MLP as features of materials. Modules used to generate compositional features are ElementProperty, ElectronAffinity, BandCenter, CohesiveEnergy, Miedema, TMetalFraction, ValenceOrbital, and YangSolid-Solution, and modules used to generate structural features are GlobalSymmetryFeatures, StructuralComplexity, ChemicalOrdering, MaximumPackingEfficiency, MinimumRelativeDistances, Structural-Heterogeneity, AverageBondLength, AverageBondAngle, BondOrientationalParameter, CoordinationNumber, and DensityFeatures.

Since the dataset size is not large in this work, training of machine learning models is not time-consuming. Using a PC, for RF and MLP, the training time is within 10 min, and for ROOST and CGCNN, the training time is within an hour. However, if transfer learning is employed, then the training of models on the large DFT dataset is very time-consuming, requiring days of training time for all of the three neural network models. For the speed of prediction, although it is critical in machine learning-based interatomic potentials,<sup>103</sup> for the prediction of properties, it is typically not a crucial factor in choosing models. After initialization of features or graphs, which are time-consuming (hours of time) but reusable for multiple runs and tasks, all of the models in this work cost less than an hour to predict  $\Delta H_{\rm f}$  of ~100,000 materials in the Materials Project database.

#### **Energy above Hull**

In the Materials Project (MP), the energy above hull  $(E_{hull})$  is defined as the energy of decomposition of a material into the set of most stable materials at this chemical composition.<sup>2</sup> The decomposition is tested against all potential chemical combinations that result in the material's composition. A positive  $E_{hull}$  indicates that this material is unstable with respect to decomposition, and a zero  $E_{hull}$  indicates that this compound is stable with respect to decomposition. In this work, the energy above hull is defined in the same way as MP. A graphical illustration of  $E_{hull}$  is provided in Figure S2. PhaseDiagram module in Pymatgen<sup>104</sup> is used to calculate the  $E_{hull}$ . The inputs required by the PhaseDiagram module are the compositions and formation enthalpies, and the corresponding output is the energies vs composition diagram, from which the decomposition energies and  $E_{hull}$  can be calculated.

#### ASSOCIATED CONTENT

#### **3** Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/jacsau.2c00235.

Impact of top 50 impactful elements on  $\Delta H_{\rm f}^{\rm diff}$ , illustration of energy above hull, comparison of errors from predictions of  $\Delta H_{\rm f}^{\rm exp}$ , corrections to polymorphs, and search space of hyperparameters (PDF)

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#### **Author Contributions**

S.G., S.W., and J.C.G. conceived the idea, S.G. performed the machine learning analysis, Y.S.H. and J.C.G. supervised this work, and all authors contributed to the analysis of data and writing and editing of the paper.

#### Notes

The authors declare no competing financial interest.

All datasets, including the dataset of 1143 materials with experimental and MP formation enthalpies, the dataset of 122 materials used for comparison between different functionals with different corrections, and the dataset of 98,338 materials in the MP database with machine learning-predicted formation enthalpies and energy above hull, are provided at: https://doi.org/10.6084/m9.figshare.19100645.v1.

All scripts with their requirements and trained machine learning models are provided at: https://doi.org/10.6084/m9.figshare. 19100645.v1.

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