COMPUTER-AIDED TOLERANCE ANALYSIS

OF

BOUNDARY GEOMETRY REPRESENTATIONS OF ASSEMBLIES

by

Nathan Graham

Submitted to the Department of Mechanical Engineering
In Partial Fulfillment of the Requirement of the Degree of

BACHELOR OF SCIENCE IN MECHANICAL ENGINEERING

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY (June, 1982)

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ABSTRACT

A method of tolerance analysis was developed. Its purpose is to determine the percentage of individually produced components which can be assembled given a distribution of tolerances. The method was implemented on a Digital Equipment Corporation VAX 11/750 digital computer using the VMS operating system in the form of an interactive FORTRAN program. The program extracts information on dimensions from a boundary geometry data representation and its output is conceptual model known as a tolerance chain.

Thesis Supervisor: David C. Gossard

Title: Associate Professor of Mechanical Engineering

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1.Ø INTRODUCTION

A designer of an assembly chooses particular dimensions satisfy certain engineering constraints. to impossible for the components of the assembly to manufactured to the exact dimensions specified, so the designer specifies an allowable range, or tolerance for each Tolerances are chosen in such a way that dimension. components fit together tightly, but may be assembled Tolerances are chosen so that the disassembled easily. dimensions are accurate enough for the part to function but not so accurate as to entail high manufacturing costs statistical nature to the unnecessarily. Due manufacturing processes, most but not all of the assemblies will have dimensions that lie within the range of the As a result, some of the assemblies may not tolerances. function, or it may not be possible to assemble the components.

The term "confidence level" refers to the percentage of assemblies that have a specified critical dimension which falls within a specified range. The goal of this study is to estimate the confidence level, based on statistical models of the machining processes required to produce each dimension. This method will be implemented as a computer program and tested on a case study using a three dimensional model of the assembly.

This procedure for tolerance analysis that is based on a method developed by Bjorke (1). of the University of Trondheim, the Norwegian Institute of Technology and the Production Engineering Laboratory at the Foundation of Scientific and Industrial Research, Trondheim, Norway.

Bjorke defines tolerance control as: "determining the tolerance of a functional dimension as a function of the confidence level based on given data concerning individual dimensions in the assembly." The method developed in this report is concerned with finding the confidence level from a complete given set of dimensions and tolerances.

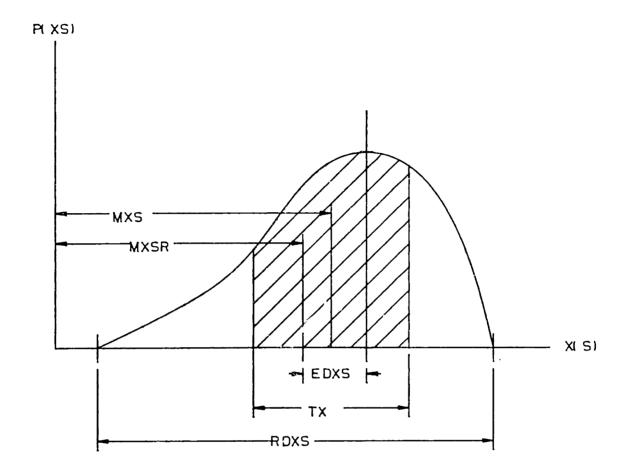
2.0 TOLERANCE CHAINS

2.1 FUNCTIONAL DIMENSIONS

A functional or sum dimension, denoted by Xs, is a critical dimension. It affects the function of the assembly more than other dimensions. For each analysis there is only one sum dimension. For example the clearance between a shaft and a hole operation of rotating machinery would be a candidate sum dimension.

The statistical behavior of the sum dimension may be modelled by a beta probability distribution (fig.2.1). There are a number of statistical parameters that define the shape and size of the curve. MXSR is the distance to the middle of the range of the dimension. RDXS is the range of variation of the dimension. The expectation of the statistical part of the sum dimension is EDXS. TX is the tolerance of the sum dimension and MXS is the distance to the middle of the tolerance zone. The width of the hump of the curve is governed by variance of the sum dimension, VARDX.

Unlike a normal distribution, a beta distribution may be assymetrical. This increases the accuracy of the results, because many machining processes can not be expressed in terms of a normal probability distribution. The normal distribution is a special case of the more general beta distribution in which EDXS is equal to zero. The expressions governing the beta distribution are given in



PROBABILITY DISTRIBUTION OF SUM DIMENSION

appendix A.

Statistical parameters of the sum dimension are found by summing up the influence of individual dimensions, measured at a common location and in a common direction. This direction is known as the sum direction. The confidence level is given by the area under probability distribution curve bounded by the tolerance of the sum dimension. This area is shown hatched in fig. 2.1.

2.2 FUNDAMENTAL EQUATIONS

To describe the influence of other dimensions on the sum dimension, Bjorke introduces the concept of the fundamental equation.

$$Xs = f(X(1), X(2), ... X(i), ... X(N))$$
 (2.1)

where X(i) is an actual dimension in an assembly. In most cases, tolerances are small deviations, dX, in the nominal size of a dimension. This implies that The fundamental equation may be linearized.

$$X = MX + dX (2.2)$$

where MX is the distance to the middle of the tolerance zone. Equation (1) now becomes.

$$Xs = \sum_{i=1}^{N} A(i) * X(i)$$
 (2.3)

where A(i) is a signed constant. A linearized fundamental equation corresponds to the mathematical concept of a chain. The links or elements of the chain are dimensions. In the following sections, the fundamental equation will often be referred to as a tolerance chain, and the terms in the right

hand side of the fundamental equation will be referred to as links.

3.Ø CHAIN LINKS

3.1 CLASSIFICATION OF LINKS

To determine the influence of a chain link (dimension) on the sum dimension, it is necessary to determine the relation between the link and the sum dimension. The link must be classified in terms of geometry, direction, magnitude and vector type. Also the statistical nature of that dimension must be determined.

Dimensions are classified under two types of geometries. They are spans and gaps. A span is the distance between surfaces on a part. A gap is the distance between surfaces on mating parts. There are also two types of directions. A lumped direction has a given but uncertain size. A distributed direction is uncertain as a whole. For instance the gap direction of an unrestrained shaft in a bore is totally uncertain with respect to the sum direction.

Gap magnitudes may also be lumped or distributed. Clearances are gaps that are always positive and interferences are always negative. Gaps that are indeterminately positive or negative are called transitions.

There are three vector types for dimensions. They are line, plane, and space. A dimension is a line vector when the dimension and its variation lay completely within or parallel to the axis of the sum dimension. A plane vector denotes a dimension lying completely within a plane containing the sum dimension, or a dimension lying

completely within a plane parallel to the plane containing the sum dimension. When a dimension is not lying within the same plane as or a plane parallel to a plane containing the sum dimensin it is a space vector. A diagram of link classifications is shown in fig.3.1.

3.2 STATISTICAL PARAMETERS

The statistical parameters of a link are determined from the statistical parameters of the machining process required to produce the dimension associated with that link. The shapes of the distribution curves for commonly used machining processes have been expressed in terms of two unit distribution parameters and listed in appendix B. They are the unit expectation (EZ) and the unit variance (VarZ).

The Transformation between the unit statistical parameters and the parameters of the dimension in question are given by

$$dX = RdX * (Z - \emptyset.5)$$
 (3.1)

where dX is there statistical part of dimension, RdX is the range of the dimension, and Z is one of the unit parameters. In many manufacturing procedures components having dimensions outside the tolerance zone do not pass through inspection. Therefore we may say that, for components in an assembly, the range is equal to the tolerance

$$RdX = TX (3.2)$$

The sum of a variate and a constant

$$Y = X + a \tag{3.3}$$

is given by

		Span	Gap	
	J Pan		Lumped Magnitude	Distributed Magnitude
Lir Vec	ne tor	-		
Plane Vector	Lumped Dir- ection			
	Distri- buted Dir- ection	*		
Spo	ice ctor			

3.1 Link Classification

$$EY = EX + a (3.4)$$

$$VarY = Varx$$
 (3.5)

Using equations 3.1 through 3.5, it is now possible to express the expectation and the variance of a dimension by

$$EdX = TX * (EZ - \emptyset.5)$$
 (3.6)

$$VardX = TX**2 * VarZ$$
 (3.7)

To obtain unit parameters from the tables in appendix B, a dimension must be classified in terms of form element. An example of a form element of a dimension is the distance between a reference plane and a center line. For each form element there is a set of technological processes, such as turning, grinding, or milling. For each technological process a range of tolerances is given that correspond to a range of unit parameters. Tolerances are expressed in international tolerance grades (2). Unit parameters are found by linear interpolation between the grade range and the parameter range. So given the international tolerance grade and knowledge of the form element, statistical parameters that define the probability distribution for a given dimension may be found in a table.

4.0 ANALYSIS PROCEDURE

To analyze a tolerance chain, it is necessary to carry out two major tasks. The first task is to specify the characteristics of each link in the tolerance chain. The second task is to analyze the tolerance chain and estimate a confidence level for the assembly.

Once a tolerance chain has been chosen, there are four steps in the specification of a link. The first is chosing the sign of the link. The sign of a link depends on its relation to the sum dimension in the fundamental equation. The sign is represented by the signed constant, A, in equation 3.2. If an increase in the magnitude of a dimension increases the magnitude of the sum dimension the sign of that dimension is positive. If an increase in the magnitude of a dimension decreases the magnitude of the sum dimension the sign of that dimension decreases the magnitude of the sum dimension the sign of that dimension is negative.

The second step is to classify the link as discussed in section 3.1. The classification of a link may require as many as six pieces of information or as few as two pieces of information, depending on the class.

The last two steps consist of indicating the dimension(s) of the link and choosing the unit parameters for each dimension. For a gap dimension there will be two dimensions for each link. The dimensions and tolerances are indicated by pointing to a particular component in the assembly data structure and then pointing to a dimension on

that component. The unit parameters are chosen by first defining the form element of the dimension using appendix B as a guide. Finally a technological process must be selected from a list of possibilities for each form element.

The analysis of a tolerance chain is carried out in three steps. In the first step, a transformation is carried out on each link, to convert unit statistical parameters into dimension statistical parameters. Also the amount of influence each link has on the sum dimension is determined. As part of this process it is necessary to determine the international tolerance grade of each set of tolerances and dimensions from a table of grades. The tolerance grade is used to interpolate between minimum and maximum values in the table of unit parameters.

The statistical parameters of each dimension are found by applying equation 2.3 to the middle of the range, the range, the expectation, and the variance of each link

$$MXrs = \sum_{i=1}^{N} A(i) * MX(i)$$
 (4.1)

$$RXs = \sum_{i=1}^{N} |A(i)| * TX(i)$$
 (4.2)

EdXs =
$$\sum_{i=1}^{N} A(i) * TX(i) * (EZ(i) - 0.5)$$
 (4.3)

$$VardXs = \sum_{i=1}^{N} A(i)**2 * TX**2 * VarZ(i)$$
 (4.4)

where 's' indicates the sum dimension. These equations vary depending on the classifications, in terms of the geometry, vector type, direction, and magnited type, of each link. The equations above apply to a line vector span. A full set of the link equations listed in the analysis subprograms in appendix D.

In the second step, the statistical parameters for all the links are summed to determine the statistical parameters of the sum dimension. The parameters of the sum dimension are used to generate the beta probability distribution curve of the sum dimension. The necessary calculations are given in appendix A. The beta function requiures the generation of the gamma function. Since the confidence level is defined by the area under the distribution curve, numeric integration is carried out on the beta function. The bounds of integration are the minimum and maximum allowable dimensions. An example of this procedure will be given in section 6.4.

5.0 STRUCTURE of COMPUTER PROGRAM

This section discusses the structure of the computer program that was developed to carry out the procedures mentioned in the previous sections. The program, called TOLANAL, which stands for tolerance analysis, is partially listed in appendix D. The source code is written in VAX FORTRAN IV-PLUS and it was developed on a Digital Equipment Corpation VAX 11/750 minicomputer in the Computer-Aided Design Laboratory in the Department of Mechanical Engineering.

TOLANAL was written using structured programming techniques. In other words, the program is divided up into many modules or subprograms. Some of the subprograms may themselves be broken up into smaller pieces. Each module is designed to carry out a specific task. This technique increases the amount of coding that is required, but it decreases the effort involved in debugging and maintainence.

The main module in TOLANAL is a program called CONTROL. CONTROL calls all of the other subprograms directly or indirectly. It is at the top of a hierarchy of program modules. One level below CONTROL, there are ten modules that are called directly by CONTROL. They are START, PROMPT, HELP, QUIT, GET, ADD, EDIT, ANALYZE, SHOW, and SAVE. Each of these modules may contain its own set of subprograms. One module may use subprograms that are part of another module. There are forty-two subroutines which,

when added together, represent over one thousand lines of FORTRAN. The subroutines are listed in appendix E.

5.1 PROMPT

The module that is central to the interacive operation of the program is PROMPT. As the name implies, PROMPT prompts the user whenever any information is required. The PROMPT library consists of three subprograms, USER_PROMPT, LOOKUP, and MAKE_UPPER_CASE. PROMPT prompts the user by displaying text on the screen followed by a greater than sign, '>'. When the user is working in the highest level of TOLANAL, the prompt is 'TOL>'. If the user is in the EDIT module, the prompt is 'EDIT>', as in "edit what?". This system of prompts lets the user to know which task is active.

The first section of PROMPT checks for consistency of data input type. Data being requisted may be of three different types, real numbers, integer numbers, or character strings. If the data requested is a real number and a real number is not entered there are six possibilities. First PROMPT checks to see if any thing was entered at all. The user may have just hit the return key without entering anything. If that was not the case, the input is then checked to see if it was an integer. If the number is an integer, the number is converted to a real number. If the number is not an integer, then PROMPT checks whether or not the input was a command or 'valid' character string. If a real number is requested as input, PROMPT goes through a

simular process.

PROMPT processes both commands and 'valid' character strings in the same manner. An example of an 'valid' character string is 'LINK', as in response to 'show what?'. The process begins by converting the input string to upper case. To do this PROMPT calls subroutine MAKE_UPPER_CASE. Upper and lower case letters have different internal computer representations and in a comparison between 'show' and 'SHOW' no match would be found.

After the string has been converted to upper case subroutine LOOKUP is called. Subroutine LOOKUP compares the input string to a list of allowable responses. Each string in the list corresponds to an OpCode Number (Operation Code). When a match is found, LOOKUP returns the OpCode associated with that match. If no match is made the OpCode equals 2. A match can be made on any group of unique first letters in the command. That is, 'ed' would match on 'EDIT'. If more than one match is made, for example 'e' matching on 'EDIT' and 'EXIT', LOOKUP returns and ambiguous command code of OpCode equal to three, and the ambiguities are displayed on the screen.

5.2 GET and SAVE

To retrieve any data stored in disk files there is the GET module. Within the GET task the user may retrieve an assembly file by invoking the GET_ASSEMBLY suprogram, or a previously specified tolerance chain may be retrieve by

invoking GET_CHAIN. These subrograms don't access disk files directly. Instead they call three basic subrograms, GET_INTEGER_ARRAY, GET_REAL_ARRAY and GET_CHAR_ARRAY. These three subprograms open files and read the contents into arrays. GET_CHAIN and GET_ASSEMBLY both store the name of the most recently used file, so that if ther user has been working on the same files over a period of days, he/she can just hit a carriage return to have the same file retrieved at the beginning of a session.

Corresponding to GET there is a module called SAVE which does the reverse file operations. SAVE writes data files onto disk storage. The corresponding subprograms in the SAVE library are PUT_CHAIN, PUT_INTEGER_ARRAY, PUT_REAL_ARRAY, and PUT_CHARACTER_ARRAY.

5.3 START

Module START is the first subprogram called by CONTROL.

It is only called once during a session. This module retrieves tables used by TOLANAL from disk storage using the GET subprograms. All of the tables are in a directory named 'Dmal:[Nathan.Data]'.

The table of tolerance grades is stored in a file named 'Grade.Dat'. The file is read into an array of twenty-one rows by twenty columns called Tol_Grade_Table. The rows in the array represent a range of dimensions, and the columns of the array represent international tolerance grades. Each entry in the table is a tolerance. The last two columns

contain the minimum and maximum dimension of the range of dimensions in a particular row. All values in disk file are in milimeters. START converts these values to inches.

The tables containing the unit statistical parameters for specific machining processes are stored in five files. They are divided into two groups. One group contains information on the form elements, Form.Dat, and Form.Nam. The other group of files contains information on the technological processes, Tech.Dat, Tech.Nam, and Tech.Val. The data was seperated into five files to facilitate editing of the process tables and to separate integer, real, and character data so that they could be handled by the GET subprograms.

An additional table was necessary to define three graphical functions. These functions were required for the analysis of transition line gaps and lumped direction plane gaps. There were no analytical expressions available for these functions, so in order to evaluate them a least squares fit was made using a Chebyshev polynomial of the form

 $P(x) = b(1)*T(\emptyset,t) + b(2)*T(1,t) ... + b(m)*T((m-1),t)$ (5.2) The coefficients, b(i), for the three functions, are stored in three files named Zeta(n).Fit. START reads from these files into three arrays named Zeta(n)_Fit. At this point START calls GET_ASSEMBLY, which prompts the user for the name of the file that contains the dimensions of the assembly. To run an analysis TOLANAL has to have access to an assembly. Another important piece of information is whether the user wishes to work on an old tolerance chain or start a new tolerance chain. If the user wishes to work on an old chain, START calls GET_CHAIN, which prompts the user for the name of the old chain. If the user wishes to work on a new chain, then START calls the input routine ADD_LINK, and the user begins entering a new chain.

5.4 ADD

The ADD module is very crucial the tolerance chain analysis. This routine leads the user through the specification of the tolerance chain. The specification of chain requires a great amount of user-computer interaction. For some types of links there may be up fifteen pieces of information that are required. The data structure of the tolerance chain data is shown in appencix D. The arrays that contain the information on the individual links are set up so that the index of the first is zero. This position is reserved for the dimension, ie. link number zero is the sum dimension. ADD consists mainly of two subprograms, ADD LINK ADD_LINK_DIM. In ADD_LINK each link is classified by one of the catagories presented in section 3.1. ADD LINK DIM stands for add link dimension. In this routine, the specifies any dimensions associated with that link.

is an additional subprogram named GET_TOL_GRADE, which uses the dimension information, supplied in the previous routine, to find the international tolerance grade for a dimenison and its tolerance. To find the grade, a search is conducted through an array, TOL_GRADE_TABLE. GET_TOL_GRADE is within ADD because the user requires the tolerance grade in order to choose a technological process.

5.5 ANALYZE

The main purpose of TOLANAL is analyzing the tolerance chain. All of the analysis is carried out in the ANALYZE module. ANALYZE calls LINK_ANALYSIS to obtain the statical parameters of each link. At the same time these values are being summed up to obtain the statistical parameters of the sum dimension.

To obtain the unit statistical parameters, EZ and VarZ, for a particlular dimension, LINK_ANALYSIS calls the subprogram GET_PARAM. GET_PARAM retrieves the required values from the technology process table. Often it is necessary to perform linear interpolation between entries in the table. As you might expect, INTERPOLATE exists for that reason.

Once the unit parameters have been chosen, LINK_ANALYSIS performs the the transformations on the unit parameters. There are a number of subprograms that carry out this operation for specific classes of links. For example, there is a subprogram called DD_PLANE_GAP_ANALYSIS.

DD stands for distributed direction.

The line gap analysis and the lumped direction plane gap analysis require three graphic functions that are expressed using a Chebyshev polynomial of the form

$$P(x) = b(1)*T(\emptyset,t) + b(2)*T(1,t) ...+ b(m)*T((m-1),t) (5.2)$$

The independent variable, x, is transformed into the variable, t, which has a range of -1 to +1.

$$t = (x-xo)/xd (5.3)$$

$$xo = -(xr+x1)/(xr-x1)$$
 (5.4)

$$xd = 2/(xr-x1)$$
 (5.5)

where xl and xr bound the range of the fitted data points. T(k,t), obeys the recursive formula

$$T(k,t) = 2t * T((k-1),t) - T((k-2),t) ; k>=2$$
 (5.6) with starting values

$$T(\emptyset,t) = 1 \tag{5.7}$$

$$T(1,t) = t ag{5.8}$$

The coefficients, b(i), are in three arrays named Zeta(n)_Fit. The first two values in the array are xo and xd.

With the statistical parameters of the sum dimension in hand, we are ready to generate the probablity distribution The area of integration beneath the curve and curve. bounded by the tolerance zone will determine the confidence The generation of the distribution curve level. should be except for one point that straightforward expression beta probability mentioned. The for a distribution curve requires the generation of the gamma

function. To handle this subprogram DLN_GAMMA_FUNCTION was written.

The name DLN_GAMMA_FUNCTION stands for the double precision computer representation of the natural log of the gamma function. The computer can handle numbers up to 10 raised to the 38th power. Numbers greater than this are common in this particular application. The natural log of the function was used to prevent the generation of numbers in excess of the computers capacity. To preserve as much accuracy as possible the numbers were represented in double precision. This allows for numbers of greater magnitude a greater number of significant digits.

Subprogram CONF sets up the parameters for the generation of the beta distribution curve. The curve is generated by subprogram BETA. CONF then calls INTEGRATE, a Simpson's rule integration routine. INTEGRATE calls BETA to obtain values of the beta function at each integration step. The integration is performed once on the whole curve and a second time on the portion of the curve that is bounded by the tolerance of the sum dimension. The area in the tolerance zone is divided by the total area and the result is the confidence level.

6.0 OPERATION of PROGRAM

6.1 INPUT REQUIREMENTS

This section explains the interactive operation of TOLANAL and gives brief examples of input and output. The operation of the program requires access to thirteen data files:

ASSEMNAME.DAT	FORM.DAT	ZETA1.FIT
CHAINNAME.DAT	FORM.NAM	ZETA2.FIT
HELP.HLP	TECH.DAT	ZETA3.FIT
OPDATA.DAT	TECH.NAM	
	TECH.VAL	
	GRADE.DAT	

The program is designed to be run interactively. It is operated using a set of general user commands, which activate various tasks. In a task, the user is prompted for specific answers. The keyboard input to the program is in the form of charcter string commands, character string keywords, integer numbers and real numbers. To speed data input in the ADD module, allowable responses are assigned integer values, for example 'span=1'. If the question was what geometry type, you could enter '1'.

There are eight generic commands. Each command may have pseudonyms. For example you may use 'EXIT' instead of 'QUIT'. The full set of commands are:

Command

Pseudonym(s)

- ADD

INPUT, SPECIFY

ANALYZE

RUN

CHANGE

EDIT, MODIFY

GET

READ

HELP

WHAT, ?

QUIT

EXIT, STOP

SHOW

LOOK, DISPLAY, TYPE, PRINT,

PLOT

SAVE

WRITE, PUT

There is also a set of keywords that act as qualifiers for the commands. This allows interaction such as 'SHOW'> PROCESS'.

OLD

NEW

TABLES

ASSEMBLY

CHAIN

LINK

DIMENSION

FORM

TECHNOLOGY

PROCESS

PROBABILITY

DISTRIBUTION

Any command or keyword may be abbreviated by n first letters as long as the abbreviation is unique within the total set of commands and keywords. 'CHA' is not a legal abbreviation, since it could mean either 'CHANGE' or 'CHAIN'.

6.2 START-UP PROCEDURE

The program is activated by running the executable image CONTROL.EXE. After the program has been started, the first thing that happens, is the program prompts the user for the name of the assembly file that is going to be analyzed. This step has to be carried out before any chains can be built or analyzed. If the user wishes to retrieve the most recently used file she/he can press the return key, and the name is called up from disk storage.

Next, the user is asked whether an old or new chain will be analyzed. If the response is 'OLD' the user is prompted for the chain name. If the response is 'NEW' the program goes into the input mode. The first link is link number zero and it represents the sum dimension.

6.3 DATA INPUT

To define a tolerance chain the user puts the program into the 'ADD' mode by entering 'ADD' or one of it pseudonyms. In the 'ADD' mode the program guides the user through each of the possible sixteen steps required to define each chain link. If the input of any previous steps causes a step to be unecessary, the step is skipped. For instance a line vector does not require any specifications on its direction. If user exits from the 'ADD' mode at any step, chain specification resumes at the same step the next time the 'ADD' command is issued. From this point on anytime the 'ADD' command is used, input will begin with the

last step of the last link. All links must be completed before they can be edited. Every link in the chain must be complete, before the chain can be analyzed.

Ιf session must be terminated before specification of the chain is complete the chain may be saved by issuing the 'SAVE' command. The user will be prompted for a file name. If the response is a carriage return TOLANAL will use the most recent name of a tolerance file and it will write over the old file. 'QUIT' command is issued to end a tolerance analysis sesison, the user will be asked if the current chain should be saved. This is meant to prevent the loss of tolerance chain data that was for time consuming to input.

A formated output of the tolerance chain can be displayed on the screen using the 'SHOW' command. If a hardcopy of this information is required the 'PRINT' command should be used. This command sends the formatted data to a file instead of the screen. The name of the file is 'TolChain.Lis'.

6.4 EXAMPLE RUN

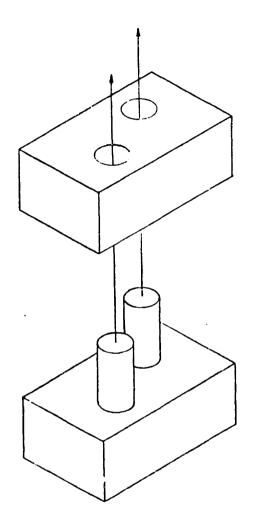
The assembly case study consists of two mating parts. One component is a rectangular prism with two parallel cylinders (or pins) projecting from one face. The other component is prisim of the same dimensions as the first except that it has two parallel holes in one face (fig.6.1-3). The assembly is stored using the data structure described in the MIT CADLAB Technical Document no.

The critical or sum dimension for this assembly is the clearance between the pin and its mating hole. Either pin hole pair may be chosen. The dimensions that affect the sum dimension are the distances between centers of the holes and the pins and the clearance between the second pin and its hole. These dimensions play major roles in determining whether or not the parts may be assembled (fig.6.4).

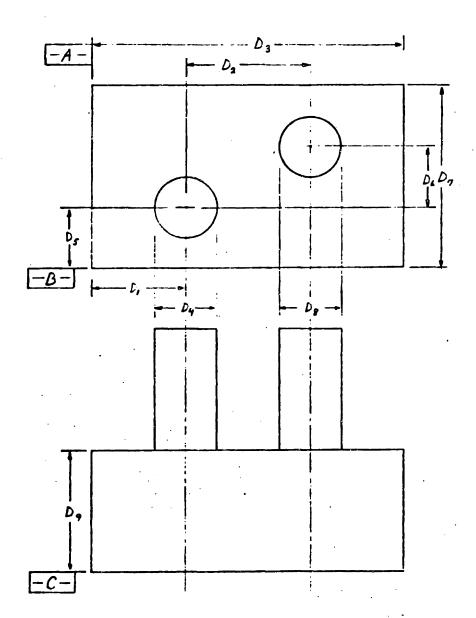
We will represent our chain as

$$X_S = X(1) - X(2) - X(3)$$
 (6.1)

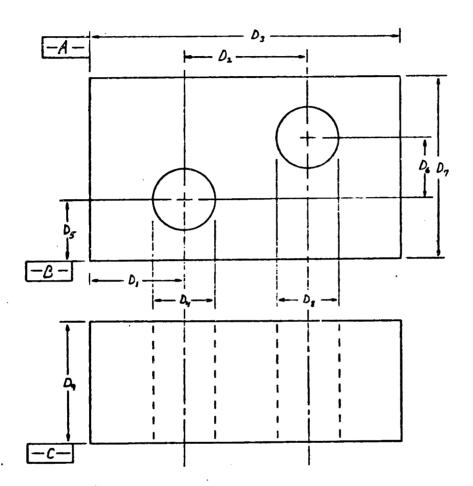
Xs is the gap between the hole dimension number four on female component and the pin dimension number four on the mail component. X(1) is the distance between the centers of the two holes. X(1) is made up of the components of Df2 and Df6 in the sum direction (fig.6.5). The convention is Df2 means dimension number 2 on the female component. Df2 makes an angle of 26.6 degrees with the sum direction and Df6 makes an angle of 63.4 degrees with the sum direction. X(2)



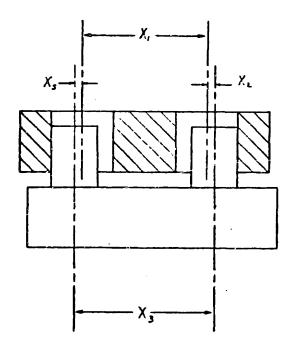
6.1 Exploded Drawing



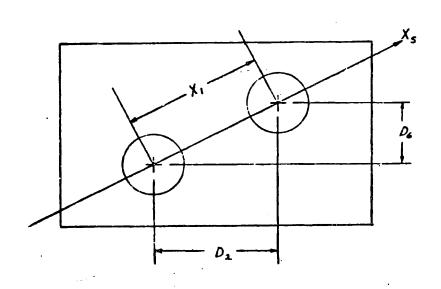
6.2 Male Component Drawing



6.3 Female Component Drawing



6.4 Schematic of Tolerance chain



6.5 Sum Direction

is the clearance gap between Df8 and Dm8. X(3) is made up of Dm2 and Dm6.

For our fundamental equation the dimension X(1) and X(3) are lumped direction plane vector spans. The dimension X(2) is a plane vector gap of distributed direction and lumped magnitude. Also note that A(1) is positive, and A(2) and A(3) are negative.

The form elements of the dimensions in question are as follows. Df2, Df6, Dm2, and Dm6 are the distance between center lines, form element number six. Df4 and Df8 are internal cylinders, form element number 2. And Dm4 and Dm8 are external cylinders, form element number 1.

The follow three pages contain a sample run. It begins by reading in a assembly file and entering the sum dimension. Then it skips to the reading in of a chain that was previously completed.

SAMPLE INPUT and OUTPUT

TOL

Enter assembly name.

Press <RETURN> for default to most recent Assembly.

GET>ASSEMBLY>COMP2

RUN OLD chain or NEW chain ?

RUN>NEW

Input SUM DIMENSION

Dimension seometry type:

1 = Span
 2 = Gap

ADD>LINK>GEOM>2

Enter component# of internal dimension

ADD>LINK>DIM>COMP#>2

Enter dimension#

ADD>LINK>DIM#>4

Process form element type :

- 1 External cylinders
- 2 Internal cylinders
- 3 Radial runout of cylindrical surfaces
- 4 Distance between external parallel planes
- 5 Distance between internal parallel planes
- 6 Distance between external and internal parallel planes
- 7 Parallelism, perpendicularity and angularity between surfaces
- 8 The distance from a center line to a ref plane
- 9 llism, l_arity, and <arity between a center line and a reference plane
- 10 The distance between center lines
- 11 Parallelism, perpendicularity and ansularity between center lines

ADD>LINK>DIM>FORM#>1

SAMPLE INPUT and OUTPUT

Tolerance Grade = IT6

technolosy	name	max.srade	min.grade
1 2	Roush turnins Grindins	IT11 IT7	IT13 IT9
3	Face milling	IT5	IT7

ADD>LINK>TECH#>3

Enter component# of external dimension

ADD>LINK>DIM>COMP#>1

Enter dimension#

ADD>LINK>DIM#>4

Process form element type :

- 1 External cylinders
- 2 Internal cylinders
- 3 Radial runout of cylindrical surfaces
- 4 Distance between external parallel planes
- 5 Distance between internal parallel planes
- 6 Distance between external and internal parallel planes
- 7 Parallelism, perpendicularity and angularity between surfaces
- 8 The distance from a center line to a ref plane
- 9 | lism, | arity, and (arity between a center line and a reference plane
- 10 The distance between center lines
- 11 Parallelism, perpendicularity and angularity between center lines

ADD>LINK>DIM>FORM#>2

Tolerance Grade = IT7

technoloax	name	max.srade	min.srade
1	Borins	IT11	IT13
2	Drillins	IT10	IT14
3	Grinding	IT8	IT10
4	Reamins	IT7	IT9
5	Face milling	IT5	IT7
6	Honins	IT4	176

ADD>LINK>TECH#>4

SAMPLE INPUT and OUTPUT

ink#			Geom(2)							
0	-	+	•	1 L			0.0		1	
:=====:	= = = : 	Design	======= ation 				m(10)			
	1	Inter		-			1		1116	====
	1	Desisn	======= ation 				m(14)			
	1	Exter					2		1177	

ink number 1

isn of link (+ or -)

DD>LINK>SIGN>G

TOL>GET

Do you wish to retrieve a chain or assembly file?

GET>CHAIN

Enter chain name, press <RETURN> for default to most recent chain name

GET>CHAIN>

Chain name is CHAIN2

TOL>ANALYZE

12.4% of the assemblies will have a sum dimension within the specified tolerance

TOL>GUIT

Do you want to save the chain?

QUIT>NO

\$

7.0 CONCLUSIONS

In conclusion I would like to offer a few opinions and recommendations and also describe constraints put on the problem by this particular solution.

This method of tolerance anlysis is based on assumptions about the shapes of the probability distribution curves of dimensions. There are a list of common shapes in The exact shape of the distribution curve appendix B. depends highly upon the practices of the associated manufacturing facility. Each facility would have their own set of curves. The above conditions imply that the process table should be flexible. As it stands now TOLANAL has no tools for editing the process tables. But the tools could be easily developed and incorporated into the rest of the program. In the program the internal data structure of the technological process tables, was designed with editing in mind. All that is necessary is to write a process editing subprogram and put it in the 'EDIT' module.

Another point to be made is that a large amount of data that is input by hand for each link. It would be very beneficial to reduce this load on the user. It should not be necessary for the user to input some of this information since it is already stored in the assembly data structure.

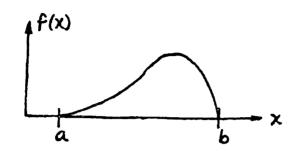
An example of implied specifications is the specification of form element. If the dimension is a diameter it will have an associated edge. The edge will be part of a cylindrical surface representing a hole or a shaft. If it is part of a hole, there will be no surfaces at both ends of the hole. Therefore the form element is an internal cylinder. Once a sum direction has been chosen, it is possible to find the vector type of a dimension in the same manner.

TOLANAL is just a foundation on which many tools can be built. There are a lot of features that should be added to TOLANAL, and it was set up so that extra feature could be added with minimal impact on the rest of the system. A few modifications have been suggested that may make this a very powerful tool. In an ideal situation, a manufacturing facility would use this program in conjunction with designers to analyze an assembly that has been completely designed on a computer-aided design system to determine what percentage of a certain critical dimension on assemblies would meet dimensional specifications.

REFERENCES

- Computer-Aided Tolerancing, Oyvind Bjorke, Tapir publishers 1978, Trondheim, Norway.
- 2. Engineering Drawing and Design, 2nd Ed., Cecil Jensen and Jay Helsel McGraw-Hill Book Company 1979, United States.

APPENDIX A BETA PROBABILITY DISTRIBUTION



$$f(x) = \frac{1}{(b-a)B(r,\eta)} \left(\frac{x-a}{b-a}\right)^{r-1} \left(1 - \left(\frac{x-a}{b-a}\right)\right)$$
 (A. 1)

$$a = MXsr - RdX/2 (A.2)$$

$$b = MXsr + RdX/2 (A.3)$$

$$T = \frac{(EX-a)^2(b-EX) - var X(EX-a)}{var X(b-a)}$$
(A.4)

$$\eta = \frac{(EX-a)(b-EX)^2 - var X(b-EX)}{var X(b-a)}$$
(A.5)

$$EX = MXsr + EdX$$
 (A.6)

$$Var X = Var d X$$
 (A.7)

$$B(r,\eta) = \frac{\Gamma(r)\Gamma(\eta)}{\Gamma(r+\eta)} \tag{A.8}$$

$$\Gamma = \int_{0}^{\infty} t^{x-1} e^{-t} dt \tag{A.9}$$

APPENDIX B

TECHNOLOGICAL PROCESS TABLES

		7	.X	Ε	. Z	var2	
Form element	Technological process	min	max	min	max	min	max
External cylinders	Rough turning	IT11	1713	0.40	0.60	0.034	0.054
	Finishing turning	IT7	179	0.40	0.60	0.030	0.054
	Grinding	IT5	1T7	0.50	0.55	0.028	0.547
Internal cylinders	Rough turning	IT11	IT13	0.40	0.50	0.034	0.054
	Drilling	IT10	IT14	0.40	0.50	0.034	0.066
	Finishing turning	IT8	1710	0.40	0.50	0.030	0.040
•	Reaming	IT7	179	0.45 0.40	0.50	0.028	0.047
	Grinding Honing	IT5	1T7 1T6	0.45	0.50	0.028	0.034
**************************************	;						
Radial runout of	Turning	0.02	0.10	0.30	0.40	0.035	0.040
cylindrical sufaces	Grin ding	0.01	0.02	0.30	0.40	0.035	0.038
The distance between	Cut off	IT12	IT16	0.30	0.70	0.040	0.083
external parallel	Turning	1710	IT13	0.50	0.65	0.028	0.054
planes	Milling, planing	1710	IT15	0.40	0.60	0.028	0.054
	Grinding	175	IT7	0.45	0.55	0.028	0.050
		<u> </u>					<u></u>

APPENDIX B

TECHNOLOGICAL PROCESS TABLES

Form element	Technological process	T	x	F	z	varz		
TOTAL ETEMENT	recimological process	min	max	min	max	min	max	
The distance between	Turning	IT10	1713	0.40	0,60	0.034	0.054	
internal parallel	Milling, planing	IT10	1715	0.38	0.62	0.034	0.054	
planes .	Grinding	175	IT7	0.38	0.62	0.040	0.050	
The distance between external planes	Turning Milling, planing Grinding	TT10 IT10 IT5	IT13 IT15 IT7	0.40 0.50 0.48	0.60 0.55 0.52	0.034 0.034 0.034	0.054 0.054 0.050	
Parallelism, perpen- dicularity and	Planing	<u>0.1</u> 300	0.2 300	0.50	0.50	0.034	0.054	
angularity between surfaces	Milling	<u>0.1</u> 300	0.3 300	0.50	0.50	0.034	0.040	
	Grinding	0.02 300	0.1 300	0.50	0.50	0.040	0.054	

APPENDIX B

TECHNOLOGICAL PROCESS TABLES

Form element	Technological process	T	х	E	z	varZ	
19km element	recimological process	min	max	min	max	min	max,
The distance from a center line to a reference plane	Boring Face milling Face grinding	1T7 1T9 1T6	1T10 1T12 1T9	0.48 0.50 0.65	0.52 0.65 0.70	0.028 0.028 0.047	0.040 0.047 0.056
Parallelism, perpendicularity and angularity between a center line and a reference plane	Boring Face milling Face grinding	0.05 300 0.1 300 0.05 300	0.1 300 0.3 300 0.1 300	0.50 0.50 0.50	0.50 0.50 0.50	0.034	0.047 0.040 0.047
. The distance between center-lines	Boring	IT7	IT10	0.50	0.55	0.026	0.047

APPENDIX B TECHNOLOGICAL PROCESS TABLES

Form element	Technological process	T	ζ	E	Z	var2	
rotm element	rorm element recimological process		max	min	max	min	тах
Parallelism, perpen- ducularity and angularity between center lines	Boring	0.05	0.2	0.5	0.5	0.034	0.047
						·	
							·
						,	
	4						

APPENDIX C

LIST OF SUBROUTINES

Subprogram Name	Source File	Module Library
ADD I TAIV	ADDIN FOR	1.00
ADD_LINK ADD_LINK_DIM	ADDIM.FOR	ADD
ADD_LINK_DIM	ADDLINK.FOR	ADD
ANALIZE	ANALYZE. FOR	ANALYZE
BETA CONF	CONF.FOR CONF.FOR	ANALYZE
CONTROL	CONTROL.FOR	ANALYZE
		CONTROL ANALYZE
DD PLANE GAP ANALYSIS DINTEGRATE	DDANAL.FOR DINTEG.FOR	=-
DLNGAMMAFUNCTION		ANALYZE
EDIT	DLNGAMMA.FOR EDIT.FOR	ANALYZE EDIT
EDIT LINK	EDITLINK.FOR	EDIT
GAP ANALYSIS	GAPANAL. FOR	ANALYZE
GET	GET. FCR	GET
GET ASSEMBLY	GETASSEM.FOR	GET
GET_ASSEMBET GET_CHAIN	GETCHAIN. FOR	
GET CHAR ARRAY	GETCHAR. FOR	GET
GET INTEGER ARRAY	GETINT.FOR	GET
GET LINK PARAM	GETPARAM.FOR	
GET OPDATA	GETOPDATA.FOR	
GET REAL ARRAY	GETREAL. FOR	GET
GET TOL GRADE	GETGRADE . FOR	ADD
GRADE SYMBOL	GRADESYM.FOR	
HELP	HELP.FOR	CONTROL
INTERPOLATE	INTERP. FOR	ANALYZE
LD PLANE GAP ANALYSIS	LDANAL.FOR	ANALYZE
LINE GAP ANALYSIS	LGANAL.FOR	ANALYZE
LINK ANALYSIS	LINKANAL.FOR	ANALYZE
LOOKUP	LOOKUP.FOR	PROMPT
MAKE UPPER CASE	MAKEUP.FOR	PROMPT
POLYNOMIAL	POLYCURV.FOR	
PRINT LINK	PRINT.FOR	SHOW
PUT CHAIN	PUTCHAIN.FOR	SAVE
PUT CHAR ARRAY	PUTCHAR.FOR	
PUT INTEGER ARRAY	PUTINT.FOR	SAVE
PUT REAL ARRAY	PUTREAL. FOR	SAVE
QUIT	QUIT.FOR	CONTROL
SAVE	SAVE.FOR	SAVE
SHOW	SHOW.FOR	SHOW
SHOW LINK	SHOWLINK.FOR	SHOW
SPAN ANALYSIS	SPANANAL. FOR	ANALYZE
$\mathtt{STAR}\overline{\mathtt{T}}$	START.FOR	START
USER PROMPT	PROMPT.FOR	PROMPT
_		

```
C Data structure of tolerance chain
Parameter
                         MLink = 100
                        MLinkDim = 2*MLink
        Parameter
C-----
        Integer Link( 8, Ø:MLink )
C
        Filename AssemName.Lin
C
        Link( l, I ) Status
                                          1-16
        Link( 2, I ) Geometry 1-2 Span, Gap
Link( 3, I ) Vector 1-3 Line, Plane, Space
Link( 4, I ) Direction 1-2 Lumped, Distributed
Link( 5, I ) Magnitude 1-2 Lumped, Distributed
Link( 6, I ) Distribution 1-2 Normal, Rectangular
Link( 7, I ) Link Diml Pntr
Link( 8, I ) Link Dim2 Pntr
С
        Link( 2, I )
C
Ċ
C
C
С
        Real Link Value (6, 0:MLink)
C
        Filename AssemName.LiV
С
        Link Value( 1, I )
                                 Signed Const
        Link_Value( 2, I )
Link_Value( 3, I )
C
                                Angle
                                                  Theta if lumped dir
C
                                Middle X Range
                                                  Mxr
                               Range Dx
Expectation Dx
        Link_Value( 4, I )
Link_Value( 5, I )
C
                                                  Rd x
C
                                                  Edx
C
        Link Value (6, I)
                                Variance Dx
                                                  Vardx
        Integer Link Dim( 4, MLinkDim )
C
        Filename AssemName.LiD
        Link_Dim( 1, I )
Link_Dim( 2, I )
C
                                 Comp Pntr
С
                                Dim \overline{\mathsf{V}}alue Pntr
С
        Link Dim(3, I)
                                Form Pntr
        Link Dim(4, I)
C
                                 Tech Pntr
        Real
                Link Dim Value( MLinkDim )
C
        Filename AssemName.LDV
C
        Link Dim Value( 1, I ) Grade
C
                 Depending on Form Element
C
                 1. = IT1, ...
C
                 \emptyset.02 = \emptyset.02,...
C
                 \emptyset.1 = \emptyset.1/300....
        Common / Chain /
                                 Link,
                                                  NLink,
        1
                                 Link Value,
        1
                                 Link Dim,
                                                  NLinkDim,
        1
                                 Link Dim Value,
        1
                                 Link Pntr
```

```
C Data Structure of internally stored tables
                     MForm = 11
       Parameter
                     MTech = 32
       Parameter
       Parameter
                     MTechName = 14
       Integer Form( 11, MForm )
C
       Filename Form.Dat
C
       Form( 1, I ) No Tech
С
       Form( 2, I )
                     Techl Pntr
C
       Form( 11, I )
                     TechlØ Pntr
       Character *80 Form Name( MForm )
C
       Filename Form.Nam
       Integer Tech( 2, MTech )
C
       Filename Tech.Dat
       Tech( 1, I ) Form Pntr
C
C
       Tech( 2, I )
                     Tech Name Pntr
       Character *20 Tech Name( MTechName )
C
       Filename Tech.Nam
       Real Tech Value (6, MTech)
C
       Filename Tech. Val
       Tech Value( 1, I )
C
                            Grade Min
       Tech_Value( 2, I )
Tech_Value( 3, I )
С
                            Grade Max
C
                            Unit Exp Min
C
       Tech Value (4,I)
                            Unit Exp Max
       Tech_Value( 5, I )
C
                            Unit_Var_Min
       Tech Value (6, I)
                            Unit Var Max
       Common / Process /
                            Form,
                                           NForm,
                                                  NFormName,
                            Tech,
       1
                                           NTech.
                                                  NTechName,
                            Tech Value
       1
       Common / Process Name / Form Name,
                            Tech Name
                            Grade Table( 20, 21 )
       Common / Grade /
                            MZetaCoef = 20
       Parameter
                            Zetal_Coef( MZetaCoef ), NZetal_Coef,
       Common / Zeta Fit /
                            Zeta2 Coef( MZetaCoef ), NZeta2 Coef,
                            Zeta3 Coef( MZetaCoef ), NZeta3 Coef
       1
```

```
Program TOLANAL
Include ' Dmal:[Nathan.Common]Status.Cmn'
      Call Start
10
      If ( OpCode .Lt. 600 .Or. OpCode .Ge. 2000 )
      Call User Prompt( 'TOL>', Com, Ans, IVal, Val)
C-----
      If ( OpCode .Ge. 400 .And. OpCode .Lt. 500 ) Then
         Mode = \emptyset
         Call Help
      Else If (Opcode .Ge. 500 .And. OpCode .Lt. 600 ) Then
         Mode = Quit Mode
         Call Quit
         If ( Opcode .Eq. 2001 .Or. Opcode .Eq. 2002 ) Go To 999
      Else If ( OpCode .Ge. 1000 .And. OpCode .Lt. 1100 ) Then
         Mode = Get Mode
         Call Get
      Else If ( OpCode .Ge. 1100 .And. OpCode .Lt. 1200 ) Then
         Mode = Add Mode
         Call Add Link
      Else If (Op\overline{C}ode .Ge. 1200 .And. OpCode .Lt. 1300 ) Then
         Mode = Edit Mode
         Call Edit
      Else If ( OpCode .Ge. 1300 .And. OpCode .Lt. 1400 ) Then
         Mode = Analyze Mode
         Call Analyze
         OpCode = 500
      Else If ( OpCode .Ge. 1400 .And. OpCode .Lt. 1500 ) Then
         Mode = Show Mode
         Call Show
      Else If ( OpCode .Ge. 1500 .And. OpCode .Lt. 1600 ) Then
         Mode = Save Mode
         Call Save
      Else If ( OpCode .Ge. 2000 ) Then
         Write ( 6, 801 )
         Format(/' *** Invalid at this level ***'/)
801
         End If
      Go To 10
999
      Continue
      End
```

```
Subroutine User Prompt( Prompt, Type, Ans, IVal, Val )
Include 'Dmal:[Nathan.Common]Opdata.Cmn'
      Include 'Dmal: [Nathan.Common]Status.Cmn'
      Character *(*) Prompt
      Byte String(20)
                        ______
      Write( 6, 801 ) Prompt
Format(/' ', A,$)
8Ø1
      Read ( 5, 701 ) Length, ( String(I), I=1, Length )
      Format ( Q, 20A1 )
7Ø1
      If ( Length .Eq. \emptyset ) Then
          OpCode = 1
          Return
      Else If ( Type .Eq. Integ Data ) Then
          Decode(Length, 702, String, Err=601) IVal
         Format( I10 )
7Ø2
         OpCode = \emptyset
          Return
      Else If ( Type .Eq. Real Data ) Then
          Decode( Length, 703, String, Err=601 ) Val
         Format( F10.5 )
7Ø3
          Decode( Length, 704, String, Err=601 ) Ans
          If ( Index( Ans, '.') .Eq. 0 ) Then
             Length = Length + 1
             String(Length) = '.'
             Decode(Length, 703, String, Err=601) Val
             End If
          OpCode = \emptyset
          Return
          End If
      Decode( Length, 704, String, Err=602 ) Ans
6Ø1
      Format( A )
704
      Call Make Upper Case( Ans )
6Ø2
      Call Lookup (Ans, Opcode)
      If ( Opcode .Eq. 2 ) Write( 6, 802 )
          Format(/' **** Unkown Command **** '/
802
                   Type "HELP" for help '/
1
                 1
      If ( Opcode .Eq. 3 ) Write( 6, 803 )
          Format(/' *** Ambiguous Command ** '/)
                     _____
      Return
      End
```

```
Subroutine Make Upper Case (String)
C-----
C Convert all lowercase letters to uppercase,
 and remove leading blanks.
C-----
    Character *(*) String
    Character Letter *1
    L = Len (String)
C------
C String --> STRING
C-----
    Do 200 I = 1, L
     Letter = String (I:I)
     Check if Letter is lowercase.
C
     If ( (Letter .ge. 'a') .and. (Letter .le. 'z') ) Then
      Number = Ichar (Letter) lascii to integer
      Number = Number -32
      Letter = Char (Number) linteger to ascii
     Endif
     String = String (:I-l) // Letter // String (I+l:)
200
    Continue
C-----
C ___String --> String____
             Do 300 I = 1, L
     If (String (:1) .eq. ' ') String = String (2:)
300
    Return
    End
```

```
Subroutine Lookup (Command, Opcode)
C-----
 Search through lookup table for the opcode
C which corresponds to this command.
      Include 'Dmal:[Nathan.Common]OpData.Cmn'
      Integer Opcode
      Character Command *(*)
      Character First Ambiguous Name *10
                                 10pcode for Opcode not found.
      Opcode = 2
      LocSpace = Index (Command, ' ')
      Do 100 I = 1, Nop
        If ( Command (:LocSpace-1)
             .eq. Op Name (I)(:LocSpace-1) ) Then
C
             Write (\overline{6}, 1\emptyset) Op Number (I), Op Name (I)
             Format (1H , 'Opcode: ', I6, ', ', A)
10
С
С
         Check for multiple command equivalence.
C
         If ( (Opcode .eq. 2) ) Then
             First Ambiguous Name = Op Name (I)
             Opcode = Op Number (I)
         Else
                                 !Redundent command.
             Opcode = 3
             Write( 6, 804 ) Op Name( I ), char(7)
             Format(lh,5x,A)
8Ø4
         Endif
        Endif
100
      Continue
      If ( (Opcode .eq. 3) ) Write( 6, 804 ) First Ambiguous Name
      Return
      End
```

```
Data structure of all analysis routines
C-----
     Integer Geometry, Vector, Direction, Magnitude, Distribution
           A, Mx, Ux, Lx, Tx, Ez, Varz,
           Mxa, Uxa, Lxa, Txa, Eza, Varza, Mxb, Uxb, Lxb, Txb, Ezb, Varzb,
     2
           Varoxr, Varxr, Exr, Mxr, Rdx, Edx, Vardx
     Parameter
                 Span = 1,
                 Gap = 2,
     2
                 Line = 1,
     3
                 Plane = 2,
     4
                 Space = 3,
     5
                 Lumped = 1,
     6
                 Distributed = 2,
     7
                 Normal = 1,
     8
                 Rectangular = 2
C This is to be included in all analysis routines
C-----
     A = Link Value( 1, Link Pntr )
     Geometry = Link( 2, Link Pntr )
     Vector =
                Link( 3, Link Pntr )
     Direction = Link( 4, Link Pntr )
Magnitude = Link( 5, Link Pntr )
     Distribution = Link( 6, Link Pntr )
C-----
     If ( Geometry . Eq. Span ) Then
     Call Get Link Param( 1, Mx, Ux, Lx, Tx, Ez, Varz, Theta )
     Else If ( Geometry . Eq. Gap ) Then
     Call Get Link Param( 1, Mxa, Uxa, Lxa, Txa, Eza, Varza, Theta )
     Call Get Link Param ( 2, Mxb, Uxb, Lxb, Txb, Ezb, Varzb, Theta )
     End If
```

```
Subroutine Span Analysis
This routine finds this statistitical contribution of
C
C
      a span chain link to the sum dimension of the tolerance
С
      chain, depending on the link vector type.
      Include '[Nathan.Common]Assembly.Cmn'
      Include '[Nathan.Common]Chain.Cmn'
      Include '[Nathan.Common]GetParam.Cmn'
      Include '[Nathan.Common]GetParam.Inc'
      If ( Geometry .Eq. Line ) Then
         Mxr = A \star Mx
         Rdx = Abs(A) * Tx
         Edx = A * Tx * (Ez - \emptyset.5)
         Vardx = A^*2 * Tx^*2 * Varz
           ______
      Else If ( Geometry . Eq. Plane ) Then
        - - -
         If ( Direction .Eq. Lumped ) Then
            Mxr = Cos( Theta ) * Mx
            Rdx = Abs(A*Cos(Theta)) * Tx
            Edx = A*Cos(Theta) * Tx * (Ez - 0.5)
            Vardx = (A*Cos(Theta))**2 * Tx**2 * Varz
           ______
         Else If ( Direction .Eq. Distributed ) Then
            Mxr = \emptyset.
            Rdx = Abs(A) * 2. * Tx
            Edx = \emptyset.
            Varozr = Varz + Ez**2
            Vardx = A**2 * 0.5 * Txr**2 * Varozr
            End If
         End If
      Link Value( 3, Link Pntr ) = Mxr
      Link Value( 4, Link Pntr ) = Rdx
      Link Value( 5, Link Pntr ) = Edx
      Link Value( 6, Link Pntr ) = Vardx
      Return
      End
```

```
Subroutine Line Gap Analysis
C
       This routine finds this statistitical contribution of
С
       each line gap chain link to the sum dimension of the
C
       tolerance chain, depending on the magnitued type.
       Include '[Nathan.Common]Chain.Cmn'
       Include '[Nathan.Common]Tables.Cmn'
       Include '[Nathan.Common]GetParam.Cmn'
       Include '[Nathan.Common]GetParam.Inc'
       -----
       If ( Magnitude .Eq. Lumped ) Then
C
           ------
          If ( Lxb .Ge. Uxa ) Then
C
              Clearance Lxb >= Uxa
              Mxr = (A/2.) * (Mxb - Mxa)
              Rdx = (Abs(A)/2.) * (Txb - Txa)
              Edx = (A/2.) * (Txb * (Ezb-0.5) - Txa * (Eza-0.5) )
              Vardx = (A^{**}2/4.) * (Txb^{**}2 * Varzb + Txa^{**}2 * Varza)
C
              Else If ( Lxb .Le. Uxa .And. Uxb .Ge. Lxa ) Then
C
              Transition Lxb <= Uxa and Uxb >= Lxa
              Exr = \emptyset.5 * (Mxb - Mxa + Txb*(Ezb-\emptyset.5) - Txa*(Eza-\emptyset.5))
              Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
              sigm xr = Sqrt( Varxr )
              zeta = Exr / sigma xr
              zeta Ex = Polynomial( zeta, NZetal Coef, Zetal Coef )
              If (Distribution .Eq. Rectangular) Then
              zeta Varx = Polynomial( zeta, NZeta2 Coef, Zeta2 Coef )
             Else If ( Distribution .Eq. Normal ) Then
              zeta Varx = Polynomial( zeta, NZeta3 Coef, Zeta3 Coef)
              End If
              Mxr = (A/4.) * (Uxb - Lxa)
             Rdx = (Abs(A)/2.) * (Uxb - Lxa)
              Edx = A * zeta Ex * sigma xr - Mxr
             Vardx = A**2 * zeta Varx * Varxr
C
          Else If ( Uxb .Le. Lxa ) Then
C
C
              Interference Uxb <= Lxa
C
             Neglected
             Mxr = \emptyset.
             Rdx = \emptyset.
             Edx = \emptyset.
             Vardx = \emptyset.
C
             End If
```

```
Else If ( Magnitude .Eq. Distributed ) Then
C
          If ( Distribution .Eq. Normal ) Then
               _____
С
              Norm Distr Center Loc
C
              Exr = \emptyset.5 * (Mxb - Mxa + Txb*(Ezb-\emptyset.5) - Txa*(Eza-\emptyset.5))
              Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
              Varxoxr = Varxr + Exr^{*2}
              Mxr = \emptyset.
              Rdx = Abs(A) * (Uxb - Lxa)
              Edx = \emptyset.
              Vardx = (A**2/9.) * Varxoxr
              С
          Else If ( Distribution .Eq. Rectangular ) Then
C
C
              Rect Distr Center Loc
              Exr = \emptyset.5 * (Myb - Mxa + Txb*(Ezb-\emptyset.5) - Txa*(Eza-\emptyset.5))
              Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
              Varxoxr = Varxr + Exr**2
              Mxr = \emptyset.
              Rdx = Abs(A) * (Uxb - Lxa)
              Edx = \emptyset.
              Vardx = (A**2/3.) * Varxoxr
C
              End if
C
          End if
       ______
       Link Value( 3, Link Pntr ) = Mxr
       Link Value( 4, Link Pntr ) = Rdx
Link Value( 5, Link Pntr ) = Edx
       Link Value( 6, Link Pntr ) = Vardx
       Return
       End
```

```
Function Polynomial( X, Poly_Deg, Coef )
C This routine evaluated the Chebychev polynomial
                        Real X, Z, Coef( 1 ), T( 100 )
     Integer Poly_Deg
     Z = Coef(1)*(X+1.5) + Coef(2)
     T(1) = 1.
     T(2) = Z
     If ( Poly Deg .Gt. 2 ) Then
C
       Do 10 \text{ k=3, Poly Deg}
          T(k) = 2 \times T(k-1) - T(k-2)
1Ø
          Continue
C
       End If
     Polynomial = \emptyset.
    Do 20 I=1, Poly Deg
       Polynomial = Polynomial + Coef( I + 2) * T( I )
20
       Continue
    Return
```

```
Subroutine LD Plane Gap Analysis
\mathbf{C}
        This routine finds this statistitical contribution of
C
        each chain link to the sum dimension of the tolerance
C
        chain, for lumped direction plane gaps.
C------
        Include '[Nathan.Common]Chain.Cmn'
Include '[Nathan.Common]Tables.Cmn'
        Include '[Nathan.Common]GetParam.Cmn'
        Include '[Nathan.Common]GetParam.Inc'
        If ( Magnitude .Eq. Lumped ) Then
            If ( Lxb .Ge. Uxa ) Then
\mathbf{C}
               Clearance Lxb >= Uxa
               Mxr = (A*Cos(Theta)/2.) * (Mxb - Mxa)
               Rdx = (Abs(A*Cos(Theta))/2.) * (Txb - Txa)
               Edx = (A*Cos(Theta)/2.)*(Txb*(Ezb-0.5)-Txa*(Eza-0.5))
               Vardx = (A*Cos(Theta)**2/4.)*(Txb**2*Varzb+Txa**2*Varza)
C
           Else If ( Lxb .Le. Uxa .And. Uxb .Ge. Lxa ) Then
C
               Transition Lxb <= Uxa and Uxb >= Lxa
               Exr = 0.5 * (Mxb - Mxa + Txb*(Ezb-0.5) - Txa*(Eza-0.5))
               Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
               sigm xr = Sqrt( Varxr )
               zeta = Exr / sigma xr
               zeta Ex = Polynomial( zeta, NZetal Coef, Zetal Coef )
               If (Distribution .Eq. Rectangular) Then
               zeta Varx = Polynomial( zeta, NZeta2 Coef, Zeta2 Coef )
               Else If ( Distribution .Eq. Normal ) Then
               zeta Varx = Polynomial( zeta, NZeta3 Coef, Zeta3 Coef )
               End If
               Mxr = (A*Cos(Theta)/4.) * (Uxb - Lxa)
               Rdx = (Abs(A*Cos(Theta))/2.) * (Uxb - Lxa)
               Edx = A*Cos(Theta) * zeta Ex * sigma xr - Myr
               Vardx = A*Cos(Theta)**2 * zeta Varx * Varxr
C
           Else If (Uxb .Le. Lxa ) Then
C
C
               Interference Uxb <= Lxa</pre>
C
               Neglected
C
               Mxr = \emptyset.
               Rdx = \emptyset.
               Edx = \emptyset.
               Vardx = \emptyset.
C
               End If
```

```
Else If ( Magnitude . Eq. Distributed ) Then
             -----
          If ( Distribution .Eq. Normal ) Then
C
              Norm Distr Center Loc
              Exr = \emptyset.5 * (Mxb - Mxa + Txb*(Ezb-\emptyset.5) - Txa*(Eza-\emptyset.5))
             Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
              Varxoxr = Varxr + Exr**2
             Mxr = \emptyset.
              Rdx = Abs(A*Cos(Theta)) * (Uxb - Lxa)
              Edx = \emptyset.
              Vardx = (A*Cos(Theta)**2/9.) * Varxoxr
              Else If ( Distribution .Eq. Rectangular) Then
              Rect Distr Center Loc
              Exr = \emptyset.5 * (Mxb - Mxa + Txb*(Ezb-\emptyset.5) - Txa*(Eza-\emptyset.5))
              Varxr = 0.25 * (Txb**2 * Varzb + Txa**2 * Varza)
              Varxoxr = Varxr + Exr**2
              Mxr = \emptyset.
              Rdx = Abs(A*Cos(Theta)) * (Uxb - Lxa)
              Vardx = (A*Cos(Theta)**2/3.) * Varxoxr
C
              End if
C
          End if
        Link_Value( 3, Link_Pntr ) = Mxr
Link_Value( 4, Link_Pntr ) = Rdx
       Link Value( 5, Link Pntr ) = Edx
       Link Value( 6, Link Pntr ) = Vardx
       Return
       End
```

```
Subroutine DD Plane Gap Analysis
This routine finds this statistitical contribution of
С
С
     each chain link to the sum dimension of the tolerance
     chain, for distributed direction plane gaps.
C
C-----
     Include '[Nathan.Common]Chain.Cmn'
     Include '[Nathan.Common]GetParam.Cmn'
     Include '[Nathan.Common]GetParam.Inc'
C-----
     If ( Magnitude . Eq. Lumped ) Then
                             _____
C
         Exr = \emptyset.5 * (Mxb - Mxa + Txb * (Ezb-0.5) - Txa * (Eza-0.5))

Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
        Varxoxr = Varxr + Exr**2
        Mxr = \emptyset.
        Rdx = Abs(A) * (Uxb - Lxa)
        Edx = \emptyset.
        Vardx = (A**2/2.) * Varxoxr
         ______
C
     Else If ( Magnitude .Eq. Distributed ) Then
C
         ______
        Exr = \emptyset.5 * (Mxb - Mxa + Txb * (Ezb-0.5) - Txa * (Eza-0.5))
        Varxr = \emptyset.25 * (Txb**2 * Varzb + Txa**2 * Varza)
        Varxoxr = Varxr + Exr**2
        Mxr = \emptyset.
        Rdx = Abs(A) * (Uxb - Lxa)
        Edx = \emptyset.
        Vardx = (A**2/4.) * Varxoxr
C
      ______
     Link Value( 3, Link Pntr ) = Mxr
     Link Value( 4, Link Pntr ) = Rdx
     Link Value( 5, Link Pntr ) = Edx
     Link Value( 6, Link Pntr ) = Vardx
     Return
     End
```

```
Subroutine Conf( Middle Sum Dim Range,
                       Range Sum Dim,
       2
                       Expectation Sum Dim,
       3
                       Variance Sum Dim,
                       Middle Sum Dim Tol,
                       Tolerance Sum Dim,
                       Confidence Level )
       This routine finds the confidence level from a given
C
С
       set of statistcal parameters for the sum dimension.
С
       Method - integrate the area under the probability
\boldsymbol{C}
       function using tolerance of the sum dIMension as the
       limits of integration.
C-----Routines required - LnGammaFunction, Dintegrate
Middle Sum Dim Range,
       Real
               Middle Sum Dim Tol
       Double Precision DLnGG, DLnGE, DLnGGE
       Double Precision Beta, Const, Gamma, Eta, AA, BB,
                       XLiml, Xlim2, Conf Area, Whole Area
       Common /Beta Param/ Const, Gamma, Eta, AA, BB
       External Beta
       AA = Middle Sum Dim Range - Range Sum Dim / 2.
       If ( AA .Le. 1. ) Then
           Middle Sum Dim Tol = Middle Sum Dim Tol -
               ( Middle Sum Dim Range - Range Sum Dim ) + 1.
           Middle_Sum_Dim_Range = Range Sum Dim +1.
       AA = Middle Sum Dim Range - Range Sum Dim / 2.
       BB = Middle Sum Dim Range + Range Sum Dim / 2.
       EX = Expectation Sum Dim + Middle Sum Dim Tol
       Gamma = ((EX-AA)**2 * (BB-EX) - Variance Sum Dim * (EX-AA))
       1  / ( Variance Sum Dim * Range Sum Dim T)
ETA = ( (EX-AA) * (BB-EX)**2 - Variance Sum Dim * (BB-EX) )
               / ( Variance Sum Dim * Range Sum Dim )
       Call DLnGammaFunction( Gamma , DLnGG, IER )
       Call DLnGammaFunction( Eta, DLnGE, IER )
       Call DLnGammaFunction( (Gamma +ETA) , DLnGGE, IER )
       Const = DLnGGE - DLnGG - DLnGE
```

```
XLiml = Middle Sum Dim Tol - Tolerance Sum Dim / 2.
       IF ( XLiml .LT. (\overline{AA}*1.\overline{0}0001D0) ) XLiml = \overline{AA}*1.000001D0
       XLim2 = Middle Sum Dim Tol + Tolerance Sum Dim / 2.
       IF ( XLim2 \cdot GT \cdot (BB * \emptyset \cdot 99999D\emptyset) ) <math>XLim2 = BB * \emptyset \cdot 99999D\emptyset
       Call Dintegrate (XLiml, XLim2, Integ Step, Beta, Conf Area)
       XLiml = AA * 1.00001D0
       XLim2 = BB * \emptyset.99999D\emptyset
       Confidence Level = Conf Area / Whole Area * 1.0D+2
       Return
       End
                       Function Beta(X)
       Double Precision Beta, Const, Gamma, Eta, AA, BB, ZZ
       Common /Beta Param/ Const, Gamma, Eta, AA, BB
       Beta = Exp(Const + (Gamma-1.0D0)*Log((X-AA)/(BB-AA))
                            + (Eta-1.0D0)*Log(1.-(X-AA)/(BB-AA)))
       Return
       End
```

```
Subroutine DLnGammaFunction(X, DLnG, Ier)
Double Precision X, Xo, DLnG, DTabGamma
      Integer N. Ier
C-----Approximation to tabulated values of the gamma function
C-----for arguments 1 < Xo <= 2
     DTabGamma( Xo ) = 1.0D0 - 0.57710166D0 * (Xo-1.0D0)
                       + Ø.98585399DØ * (Xo-1.0DØ)**2
     2
                       - Ø.87642182DØ * (Xo-1.ØDØ)**3
     3
                       + Ø.83282120D0 * (Xo-1.0D0)**4
                      - Ø.5684729ØDØ * (Xo-1.0DØ)**5
     4
     5
                      + Ø.25482049D0 * (Xo-1.0D0)**6
                      -0.05149930D0 * (Xo-1.0D0)**7
     Ier = \emptyset
     If ( X .Gt. 1.0D+38 ) Then
           Ier = 2
     Else If ( X .Ge. 1.0D0 ) Then
           N = IdInt(X) - 1
           Xo = Mod(X, 1.0D0) + 1.0D0
           DLnG = Log( DTabGamma( Xo ) )
           Do 10, k=0, (N-1)
10
                 DLnG = DLnG + Log(k + Xo)
     Else If ( X .Le. Ø.0D0 ) Then
           \cdotIer = 1
     Else
           DLnG = Log(DTabGamma(X + 1.0D0) / X)
     End If
     Return
     End
Subroutine DIntegrate( a, b, n, Function, Area )
C----- Simpson's numeric Integration
Double Precision a, b, h, Coef, Function, Area
     Coef(k) = 2 + 2 * Mod(k, 2)
     h = (b - a) / n
     Area = Function( a ) + Function( b )
     Do 10 k=1, (n-1)
           Area = Area + Coef( k ) * Function( a + k * h )
10
           Continue
     Area = (h / 3.0D0) * Area
     Return
     End
```