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USERS' GUIDE FOR
NUMERICAL MODELING OF BUOYANT PLUMES IN A TURBULENT, STRATIFIED ATMOSPHERE

by
Ralph G. Bennett
and
Michael W. Golay

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ABSTRACT

A widely applicable computational model of buoyant, bent-over plumes in realistic atmospheres is constructed. To do this, the two-dimensional, time-dependent fluid mechanics equations are numerically integrated, while a number of important physical approximations serve to keep the approach at a tractable level. A three-dimensional picture of a steady state plume is constructed from a sequence of time-dependent, two-dimensional plume cross sections--each cross section of the sequence is spaced progressively further downwind as it is advected for a progressively longer time by the prevailing wind. The dynamics of the plume simulations are quite general. The buoyancy sources in the plume include the sensible heat in the plume, the latent heat absorbed or released in plume moisture processes, and the heating of the plume by a radioactive pollutant in the plume. The atmospheric state in the simulations is also quite general. Atmospheric variables are allowed to be functions of height, and the ambient atmospheric turbulence (also a function of height) is included in the simulations.

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PREFACE

The VARR-II[40] computer code has been modified for the modeling of buoyant plumes in turbulent, stratified atmospheres. A description of the model and the results and conclusions that have been obtained to date were released in a previous report (MIT-EL 79-002). The purpose of the present report is to serve as a users' guide for the model. The first four chapters of MIT-EL 79-002 have been included in this report to introduce and describe the model; the detailed card input lists and sample problems are found in Chapter 5, and the Appendices. Chapter 6 introduces the model extensions that were considered in the original work.

1. PROBLEM DESCRIPTION AND SOLUTION

1.1 Introduction

With the rapidly increasing burden of air pollution over recent decades, the engineer's ability to analyze the behavior of an ever-widening assortment of effluents has not kept up with the importance of the consequences of the releases. The reason for this is that the "predictive" models of plume behavior that are currently available universally suffer from a lack of extendability. That is, they need to observe the behavior of an ensemble of the releases that they wish to model before they can form an accurate picture of the release. The models are useful only to the extent that an appropriate ensemble of plumes can be created for study, either as full-scale atmospheric releases, or as scaled-down laboratory experiments. Inasmuch as the important turbulent and thermal characteristics of the atmosphere cannot be simulated in the laboratory, and since an ensemble of plumes with catastrophic consequences (e.g., radioactive plumes from nuclear reactor accidents) may be impractical to produce, plume modeling has needed to take a more universal approach.

The purpose of this work is to construct a widely applicable model of plume behavior in realistic atmospheres. To do this, a "first principles" approach is adopted. A numerical integration of the fluid mechanics equation is undertaken, while a number of important physical approximations to the problem serve to keep the approach at a tractable level. The advantage of the model presented here is the ability to tackle problems outside of the scope of existing models without greatly increasing the resources spent on the analysis.

1.2 Background and Problem Description

1.2.1 Historical Background

Man has produced and observed bent-over buoyant plumes since the discovery of fire. However, the bent-over plume did not have any great impact on society until the advent of large industrial sources near population centers during the industrial revolution. The number of large industrial sources has increased steadily with the industrialization of many countries. In the recent past, the variety of releases from large industrial sources has increased greatly, and now includes the potentially more harmful effluents from chemical refining and combustion processes, nuclear power plants, and large cooling towers. Also, the steady growth of population centers almost always dictates that these new sources will be located in at least moderately populated areas.

Historically, the ability to analyze the effects of large releases and hence to develop technologies for their mitigation has not kept pace with the consequences of the releases. To date, the advances have been quite modest: early observations during the industrial revolution suggested the use of tall stacks for lessening the effects of large releases. The strong influence of the synoptic-scale weather on releases (first investigated in order to increase the effectiveness of chemical warfare agents) has largely motivated the Pasquill-type correlations of plume behavior. The hope of simply reducing the consequences by reducing the amount of effluents has stimulated an abundance of filtering, scrubbing, and effluent control technologies. However, increasingly important releases are certain to occur. A brief review here of the existing approaches to plume modeling can indicate the most promising avenue for study.

1.2.2 Characteristics of Bent-Over Buoyant Plumes

The character of the bent-over buoyant plume is central to all of the available plume models. When an effluent stream with a given upward momentum and initial buoyancy is released from a stack into a windy atmosphere, the plume is deflected downwind. This occurs partly because of pressure forces that develop around the plume, and partly because the plume entrains the ambient air, which mixes a lot of downwind momentum into the plume. The deflection quickly causes the plume to bend over (usually within about one stack height) and then to be carried downstream. The buoyancy of the plume is converted into kinetic energy, and the plume rises under this action for a considerable distance downwind. About 20 years ago it was noted[1] that the motion of the plume in cross section during this rise was essentially that of a two-dimensional turbulent vortex pair. Initially the vortex pair rises and grows without being too dependent upon atmospheric turbulence (although atmospheric stratification is always important). After the kinetic energy of the cross-sectional motions has essentially died out, the plume continues to disperse solely by atmospheric motions. It will be found in the review of plume models that only the detailed numerical plume models provide a method that can easily bridge between the regimes where plume turbulence dominates and where atmospheric turbulence dominates.

1.2.3 Overview of Plume Models

With regard to the detailed three-dimensional nature of plume motions, existing models of plume behavior are found to possess a wide variety of sophistication. The Pasquill-type models, the entrainment models, and the numerical models are considered here.

The Pasquill-type models develop a highly idealized picture of the fluid motions in and around the plume. Pollutants in the plume cross section are assumed to fit Gaussian distributions of height and width. In essence, the model parameters (standard deviations of the Gaussian distributions) are simply an ad-hoc replica of the experimental results; as such, the models are unable to predict in cases for which experiments have not been performed. The wealth of non-passive effluents and the rich variations in the meteorological state of the atmosphere serve to guarantee that cases outside of the Pasquill-type models will always exist.

The entrainment models develop a much less idealized, and much more physical picture of the fluid motions in the plume. In general, the models make use of the very elegant non-dimensional formulations and similarity relationships that are central to the theory of homogeneous isotropic turbulence. Typically the models are successful at analyzing the initial plume behavior, where the self-generated plume turbulence dominates over the atmospheric turbulence. The entrainment models are generally able to analyze plumes only in fairly simple atmospheres when analytical solutions are sought. But this is not the primary limitation of entrainment models, since in some cases their solutions are found on computers. The limitations of the entrainment models are the condition that the plume self-generated turbulence is dominant over the atmospheric turbulence, (which eventually breaks down for all plumes, commonly at downwind distances for which the solution is still needed) and the basic entrainment velocity assumption, which cannot be obtained from fundamental constants and scales in a straightforward way.

Numerical plume models are capable of developing the most detailed picture of the fluid motions in the plume. In general, the models seek to integrate a closed set of Reynolds-averaged fluid mechanics equations, either in two or three dimensions. Turbulence leads to a fundamental closure problem in writing this set of equations, so that each model will have a collection of closure assumptions that together form a turbulence model, aside from other assumptions that are made concerning the plume behavior. Numerical plume models are becoming capable of analyzing the most detailed cases, yet they are often limited by the large computing costs. Aside from the computer costs, the tasks of initializing and validating the problem with fully two- or three-dimensional data can also quickly become intractable. Until computer costs are reduced greatly, the most useful numerical plume models will likely have to be two-dimensional. The greatest benefit that comes from such models is the wider range of application of the models, and the ease of extending them to new cases.

1.2.4 Scope of the Work

This work constructs a three-dimensional solution of a steady state plume from a sequence of time-dependent two-dimensional plume cross sections; each plume cross section of the sequence being spaced progressively further downwind as it is advected for a progressively longer time by the prevailing wind. The two-dimensional cross sections are simulated with a time-dependent turbulent fluid mechanics code which integrates the time-averaged equations of continuity, momentum, energy, moisture, and pollutant. The behavior of an individual plume is modeled in this way until the height or radius of the plume reaches several hundred meters, which roughly corresponds to the plume cross section being tens of kilometers downwind of the source.

The dynamics of the plume simulations are quite general. The buoyancy sources in the plume encompass the sensible heat in the plume, the latent heat absorbed or released in plume moisture processes, and the radioactive decay heating of the plume by a radioactive pollutant species in the plume. Buoyancy from chemical reactions could be easily included. The atmospheric state in the simulations accepts atmospheric wind, temperature, water vapor, liquid water, background pollutant, turbulent eddy viscosity, and turbulent kinetic energy as functions of height. The turbulence is treated with the sophisticated second-order closure model of Stuhmiller[2], which allows the turbulent recirculation and entrainment of the plume cross section to be treated in a very natural way.

The model is validated against the Pasquill model[3] and the entrainment model of Richards[4] for idealized cases in which these models apply, and for several cases from the LAPPES[5] field data for actual large power plant stacks. Simulations are obtained for cases outside of the Pasquill and entrainment models, and while no specific field data for these cases exists, the behavior of the simulation agrees with the physical changes imposed on the problems.

2. LITERATURE REVIEW

The literature review in this work undertakes a broad survey of plume modeling. In the first section, existing numerical plume models are discussed, along with the experimental data base that is available for the validation of these detailed plume models. The first section also includes the research that has been done on computational and experimental modeling of two-dimensional line vortex pairs. It is important to include them since the results of such work are very easily interpreted in the context of air pollution problems. In the second section, existing numerical models of the planetary boundary layer are discussed. Again, these models are very easily extended to air pollution problems (with the inclusion of a pollutant transport equation and pollutant source), so it is important to include them in the review.

2.1 Numerical Plume Models

A large number of plume models have been developed that are available as computer programs. Several recent reviews[6-8] have reported dozens of such models, and it is important to make a distinction regarding them. A majority of the models employ the Gaussian plume assumption; as such, the computer is simply being used to look up and present the standard handbook calculations, with minor modifications in some cases. These are not"numerical plume models" in the sense that the primitive equations are not being integrated to show the plume development, although computers are being used. Such models are not considered further here. The remaining models in the reviews are truly numerical plume models, and they will be considered next, along with several models that were reported elsewhere.

2.1.1 Three-Dimensional Models

The most sophisticated numerical plume models to date have not yet attempted a second-order turbulence closure to the fully three-dimensional flow field for non-passive pollutants. Some of these features are found in each of the models discussed here, but not all of them. The notes of Rao[9] and Nappo[10] discuss the desirable features of three-dimensional numerical plume models, and provide a good introduction to future work that may be undertaken.

Donaldson's modeling[11] has concentrated on a second-order turbulence closure for a three-dimensional planetary boundary layer simulation with a passive pollutant. Because the pollutant is passive, and hence does not affect the flow field or its turbulence, the turbulence closure only addresses PBL turbulence, and is independent of the behavior of buoyant plumes. This is in contrast to the method in this work, where the second-order closure is "tuned" to the development of turbulent buoyant plumes, and is largely independent of PBL turbulence development. Lewellen's modeling[12] begins with a second-order closure to the passive pollutant transport equation, and then adopts the PBL flow field and turbulence from Donaldson's model.[11] Only integrations of the pollutant transport equation are needed in Lewellen's model because of the adoption of a complete PBL solution. Patankar's model[13] of a deflected turbulent jet in three-dimensions also uses a second-order closure model, but does not allow for buoyancy and stratification, although it does allow for non-isotropic turbulent transports in the vertical and horizontal directions. A fundamentally different approach to three-dimensional modeling is found in the Atmospheric Release Advisory Capability (ARAC) system.[15-22] A mass-consistent three-dimensional wind field is interpolated from a small set of local tower wind measurements and used to predict the advection of a passive pollutant. Turbulent diffusion is modeled with a zero equation model, although many other important features such as rainout, wet and dry deposition, and surface terrain have been added.

2.1.2 Two-Dimensional Models

Two two-dimensional numerical plume models have been found in the literature. Henninger's model[23] solves continuity, momentum, energy, and moisture with a less-sophisticated zero-equation turbulence closure, and with a more sophisticated treatment of moisture. For plumes in a wind, the model chooses the mesh alignment shown in Fig. 3.3.2.1b of Sec. 3.3.2, which is felt to be a less satisfactory choice than that of the present work. Taft's model[24] is much closer to the model in this work, since it adopts the same mesh alignment (see Fig. 3.3.2.1c in Sec. 3.3.2). The principal differences are that Taft's model employs a one-equation turbulence model, uses a more complex moisture model, and does not make any attempt to describe ambient atmospheric turbulence.

A number of two-dimensional numerical buoyant thermal models have evolved in the literature of meteorology, usually in support of efforts to parameterize the growth of rain clouds. The models have not been applied to air pollution directly, but could be easily converted. Lilly's model[25] seeks a self-preserving solution for the (dry) buoyant line thermal, and as such, would only be applicable for the early plume behavior when plume self-turbulence is dominating. Johnson's model[26] is used to study fog clearing on runways with helicopter downwash; while the moisture equations are more complex than that in this work, the eddy viscosity is assumed to be constant. Ogura's model[27] of rain cloud development also assumes a constant eddy viscosity, while Arnason's model[28] ignores eddy transports altogether. Liu's model[29] employs a stratification of atmospheric turbulence into two constant eddy viscosity layers. While the treatment of turbulence in these models is very simple, it should be emphasized that these models are focussed on precipitation modeling, and they are likely to be helpful in the improvement of the moisture model in this work. A recent review of precipitation modeling is found in Cotton.[30]

2.1.3 Experimental Studies

The field study that the model in this work is validated against is the Large Power Plant Effluent Study (LAPPES).[5] Complete field data for stack plumes from three mine-mouth coal-fired plants are found in the four volumes of the study: wind, temperature, and humidity profiles, plant operating characteristics, and plume SO_2 concentration cross sections are of the most interest in this work. The Chalk Point Cooling Tower Project (CPCTP)[31] is also of interest to this work since it provides cooling tower plume cross sections, but plant operating data[32] was not available during this work.

The experimental laboratory studies that this work is validated against are the papers of Tsang[33] and Richards.[4] The experiments study the behavior of two-dimensional line thermals released in a water tank. The ambient receiving fluid in the tank is both laminar and unstratified, and the thermals are fully turbulent.

2.2 Numerical Planetary Boundary Layer Modeling

A three-dimensional numerical model of the planetary boundary layer has been reported by Deardorff[34-36] that could easily be adapted to local air pollution studies, although the expense is likely to be prohibitive. The model solves the complete set of primitive equations (with an eighteen-equation model of turbulence) in a box that ranges 5 km on a side and 2 km deep. The numerical experiments to date have compared very favorably with several well-documented planetary boundary layer field studies.

To apply the model to a single source of pollutant, a single mesh cell could be initialized with sources of momentum, heat, moisture, pollutant, and turbulence. To accommodate this, a pollutant transport equation would have to be added, and an additional three-equation model of turbulent pollutant fluxes would need to be developed. Time-dependent or steady-state releases could be modeled in great detail in this way.

However, the model currently requires 15 seconds of CPU on a CDC-7600 to simulate 1 second of flow in the atmosphere. Also, the specification of boundary conditions on a three-dimensional mesh with accurate time-dependent micrometeorological data would require a very elaborate reporting network. Nonetheless, the model represents a more sophisticated and potentially more accurate approach than the model in this work.

3. HYDRODYNAMIC MODEL DEVELOPMENT

3.1 Introduction

In order to model buoyant plumes in the atmosphere, the equation set contained in the VARR-II computer code is reinterpreted and expanded. A reinterpretation of the hydrodynamic variables is necessary in order to satisfactorily account for the compressible nature of an atmosphere that is at rest. The equations are expanded in Sec. 3.2.1 to include the transport of a pollutant and radioactive decay heating by the pollutant, and in Sec. 3.2.2, where the transport of water vapor, cloud liquid water, and the energy released or absorbed during the phase changes of water substance are considered. Since so many fundamental changes are made here in reinterpreting the VARR-II equation set, this discussion of the model development undertakes a derivation of the equations; for completeness it reiterates the important assumptions contained in the VARR-II code which were developed outside of this work.

3.2 Hydrodynamic Model Equation Sets

3.2.1 Equations for Dry Atmospheres

The equations for a dry atmosphere are derived in this section. When the potential temperature is simply reinterpreted as the virtual potential temperature, these equations are applicable to moist plumes in moist atmospheres if none of the moisture undergoes a change of phase, and if the turbulent diffusion coefficients of heat and moisture are equal. A further discussion of virtual potential temperature is found in Sec. 3.2.2.1.

3.2.1.1 Reference State Decomposition

As a starting point for the model development, consider the three-dimensional compressible fluid mechanics equations, where the six primitive variables $\tilde{p}$, $\tilde{\rho}$, $\tilde{T}$, and $\tilde{u}_i$ are physically measurable values of the fluctuating pressure, density, temperature, and velocity, respectively:

Continuity Eq:

$$\frac{\partial \tilde{\rho}}{\partial t} + \frac{\partial}{\partial x_j} (\tilde{\rho}\tilde{u}_j) = 0 \qquad (3.1)$$

Momentum Eq:

$$\frac{\partial}{\partial t}(\tilde{\rho}\tilde{u}_i) + \frac{\partial}{\partial x_j}(\tilde{\rho}\tilde{u}_i\tilde{u}_j) = - \frac{\partial \tilde{p}}{\partial x_i} - \tilde{\rho} g_i + \mu \frac{\partial^2 \tilde{u}_i}{\partial x_j^2} \qquad (3.2)$$

Energy Eq:

$$\frac{\partial}{\partial t}(\tilde{\rho}\tilde{T}) + \frac{\partial}{\partial x_j} (\tilde{\rho}\tilde{u}_j\tilde{T}) = \frac{\tilde{u}_j}{c_p} \frac{\partial \tilde{p}}{\partial x_j} + \frac{\partial}{\partial x_j} k \frac{\partial \tilde{T}}{\partial x_j} + \frac{1}{c_p} \frac{\partial \tilde{p}}{\partial t} \qquad (3.3)$$

Equation of State:

$$\tilde{p} = \tilde{\rho} R_d \tilde{T} \tag{3.4}$$

These equations have property values μ, c_p, and k, which may depend upon temperature in general. The energy equation has neglected the kinetic energy in the fluid motions, and the equation of state is that for an ideal dry gas.

The variations of temperature, pressure, and density in a static atmosphere are usually "subtracted out" of these equations in meteorological analyses by a reference state decomposition. That is, equations of motion for perturbations about an adiabatic atmosphere are sought by decomposing the primitive variables as

$$\left\{\begin{array}{l}\text{the value}\\ \text{of a primi-}\\ \text{tive variable}\end{array}\right\} = \left\{\begin{array}{l}\text{its value in}\\ \text{an adiabatic}\\ \text{atmosphere}\\ \text{(function of}\\ \text{height only)}\end{array}\right\} + \left\{\begin{array}{l}\text{a departure}\\ \text{from the}\\ \text{state at}\\ \text{rest}\end{array}\right\} \tag{3.5}$$

or, in terms of the notation in this work

$$\tilde{p} \rightarrow p_o + p \tag{3.6}$$

$$\tilde{\rho} \rightarrow \rho_o + \rho \tag{3.7}$$

$$\tilde{T} \rightarrow T_o + T \tag{3.8}$$

$$\tilde{u}_i \rightarrow 0 + u_i \tag{3.9}$$

The state of the dry, adiabatic atmosphere is found by making the substitutions Eq. 3.6-Eq. 3.9 into Eq. 3.1-Eq. 3.4, and setting the time derivatives and the perturbations p, ρ, T, and u_i to zero. The continuity and energy equations become trivial under this substitution. The momentum equation becomes the hydrostatic equation:

$$\frac{dp_o}{dz} = -\rho_o g \tag{3.10}$$

The equation of state is simply

$$p_o = \rho_o R_d T_o \tag{3.11}$$

The First Law of Thermodynamics for an adiabatic process is

$$dQ = 0 = c_p dT_o - dp_o/\rho_o \tag{3.12}$$

Dividing by a displacement dz gives

$$\frac{dp_o}{dz} = \rho_o c_p \frac{dT_o}{dz} \tag{3.13}$$

and substitution of Eq. 3.13 into Eq. 3.10 gives Γ_d, the lapse rate of the dry adiabatic atmosphere:

$$\Gamma_d \equiv -\frac{dT_o}{dz} = \frac{g}{c_p} = 9.76\ ^{\circ}C/km \tag{3.14}$$

To this point the solution of the adiabatic atmosphere has been presented. Substituting the reference state decomposition, Eq. 3.6-Eq. 3.9 into the equations of motion, Eq. 3.1-Eq. 3.4, and using the results of the adiabatic atmosphere, Eq. 3.10 and Eq. 3.14, gives the equations of motion for the perturbations:

Continuity Equation

$$\frac{\partial u_j}{\partial x_j} = -\frac{u_j}{\rho_o}\frac{\partial \rho_o}{\partial x_j} + \frac{R_d}{c_p}\frac{k}{\rho_o}\frac{\partial^2 T}{\partial x_j^2} \simeq 0 \tag{3.15}$$

Momentum Equation:

$$\rho_o \frac{\partial u_i}{\partial t} + \rho_o u_j \frac{\partial u_i}{\partial x_j} = -\frac{\partial p}{\partial x_i} - \rho g_i + \mu_o \frac{\partial^2 u_i}{\partial x_j^2} \tag{3.16}$$

Energy Equation:

$$\rho_o \frac{\partial T}{\partial t} + \rho_o u_j \frac{\partial T}{\partial x_j} = \frac{R_d}{c_p}\frac{\partial^2 T}{\partial x_j^2} \tag{3.17}$$

Equation of State:

$$\frac{p}{p_o} = \frac{T}{T_o} + \frac{\rho}{\rho_o} + \frac{\rho T}{\rho_o T_o} \tag{3.18}$$

The fluid perturbations will generally be assumed to be incompressible in the Boussinesq sense. That is, changes in fluid density are assumed to be produced only by temperature changes, and not by pressure fluctuations. Neglecting the pressure fluctations in the equation of state, and noting that generally $\rho T \ll \rho_o T_o$, the equation of state becomes

$$\rho/\rho_o \simeq -T/T_o \tag{3.19}$$

which is the familiar Boussinesq equation of state. This equation allows the buoyancy term ($-\rho g_i/\rho_o$) in the momentum equation (Eq. 3.16) to be similarly approximated. The continuity equation (Eq. 3.15) becomes that of an incompressible fluid, assuming that the fluid motions do not rapidly mix deep layers of the fluid,[37] e.g., comparing length scales of velocity and density:

$$\left(\frac{1}{|u_j|}\left|\frac{\partial u_j}{\partial x_j}\right|\right)^{-1} << \left(\frac{1}{\rho_o}\left|\frac{\partial \rho_o}{\partial x_j}\right|\right)^{-1} \qquad (3.20)$$

and[11] that the heat conduction term in Eq. 3.1 is a small contribution to the divergence. Making these approximations, the equations for the perturbations may be written as

Continuity Eq.:

$$\frac{\partial u_j}{\partial x_j} = 0 \qquad (3.21)$$

Momentum Eq:

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho_o}\frac{\partial p}{\partial x_i} - \frac{\rho}{\rho_o} g_i + \frac{\mu_o}{\rho_o}\frac{\partial^2 u_i}{\partial x_j^2} \qquad (3.22)$$

Energy Eq:

$$\frac{\partial T}{\partial t} + u_j \frac{\partial T}{\partial x_j} = Pr^{-1}\frac{\mu_o}{\rho_o}\frac{\partial^2 T}{\partial x_j^2} \qquad (3.23)$$

Define the potential temperature, θ, as

$$\theta \equiv \tilde{T} \left(\frac{1000\text{mb}}{\tilde{p}} \right)^{R_d/c_p} \tag{3.24}$$

Differentiating with respect to height finds that the adiabatic atmosphere has a lapse rate of potential temperature of zero,

$$\frac{d\theta_o}{dz} = 0 \tag{3.25}$$

or that the potential temperature is a constant in an adiabatic atmosphere. Errors introduced by evaluating density with θ instead of $\tilde{T}$ are assumed to be small (this is investigated in Sec. 3.3.4). Neglecting the perturbation p with respect to p_o in Eq. 3.24, and approximating ρ_o as $\rho(\theta_o)$ in Eq. 3.22, the use of θ instead of T in the primitive equations (Eq. 3.21-Eq. 3.23) gives

Continuity Eq:

$$\frac{\partial u_j}{\partial x_j} = 0 \tag{3.26}$$

Momentum Eq:

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = - \frac{1}{\rho(\theta_o)} \frac{\partial p}{\partial x_i} - \frac{\rho(\theta) - \rho(\theta_o)}{\rho(\theta_o)} g_i + \nu \frac{\partial^2 u_i}{\partial x_j^2} \tag{3.27}$$

Energy Eq:

$$\frac{\partial \theta}{\partial t} + u_j \frac{\partial \theta}{\partial x_j} = \nu Pr^{-1} \frac{\partial^2 \theta}{\partial x_j^2} \tag{3.28}$$

The utility of the potential temperature formulation is that strong variations of pressure and density with height in the hydrostatic approximation of Eq. 3.10 are no longer present in the primitive equations. Initialization errors to the hydrostatic state, if included in the primitive equations, lead to strong transient fluid motions.[38] The transients are neatly avoided by this formulation.

To this point the fully three-dimensional fluid mechanics equations have been decomposed into an adiabatic reference state, and a flow field of perturbations about this state. A number of approximations have simplified the equations for the perturbations to those of a Boussinesq incompressible flow. The equations need to be ensemble-averaged and a turbulence closure formulated, and then the set must be finite-differenced for computer solution.

3.2.1.2 Reynolds Decomposition and Closure

To model the effects of turbulence on the mean flow, each primitive variable in the equation set is decomposed into its time-averaged and fluctuating parts as

$$\left\{\begin{array}{l}\text{the value of the}\\\text{perturbation of}\\\text{a primitive}\\\text{variable}\end{array}\right\} = \left\{\begin{array}{l}\text{its ensemble-}\\\text{averaged}\\\text{value}\end{array}\right\} + \left\{\begin{array}{l}\text{any fluctua-}\\\text{tions about}\\\text{its ensemble-}\\\text{average value}\end{array}\right\} \qquad (3.29)$$

which is represented here by the decompositions

$$p \rightarrow \bar{p} + p' \tag{3.30}$$

$$\theta \rightarrow \bar{\theta} + \theta' \tag{3.31}$$

$$\rho \rightarrow \bar{\rho} + \rho' \tag{3.32}$$

$$u_i \rightarrow \bar{u}_j + u_j' \tag{3.33}$$

Under this transformation, by selectively ensemble-averaging and subtracting the equations, and by making use of the continuity equation, the primitive equations become

Continuity Equations

$$\partial \bar{u}_j / \partial x_j = 0 \tag{3.34}$$

$$\partial u_j' / \partial x_j = 0 \tag{3.35}$$

Momentum Equations:

$$\frac{\partial \bar{u}_i}{\partial t} + \bar{u}_j \frac{\partial \bar{u}_i}{\partial x_j} = -\frac{1}{\rho(\theta_o)} \frac{\partial \bar{p}}{\partial x_i} + \frac{\rho(\bar{\theta}) - \rho(\theta_o)}{\rho(\theta_o)} g_i + \nu \frac{\partial^2 \bar{u}_i}{\partial x_j^2} - \frac{\partial}{\partial x_j} (\overline{u_i' u_j'}) \tag{3.36}$$

$$\frac{\partial u'_i}{\partial t} + \bar{u}_j \frac{\partial u_i'}{\partial x_j} + u_j' \frac{\partial \bar{u}_i}{\partial x_j} + u_j' \frac{\partial u_i'}{\partial x_j} - \frac{\partial}{\partial x_j} (\overline{u_i' u_j'}) = \frac{-1}{\rho(\theta_o)} \frac{\partial p'}{\partial x_i} - \frac{\rho(\theta') - \rho(\theta_o)}{\rho(\theta_o)} g_i + \nu \frac{\partial^2 u_i'}{\partial x_j^2} \tag{3.37}$$

Energy Equations:

$$\frac{\partial \bar{\theta}}{\partial t} + \bar{u}_j \frac{\partial \bar{\theta}}{\partial x_j} = \nu Pr^{-1} \frac{\partial^2 \bar{\theta}}{\partial x_j^2} - \frac{\partial}{\partial x_j} (\overline{u_j' \theta'}) \qquad (3.38)$$

$$\frac{\partial \theta'}{\partial t} + \bar{u}_j \frac{\partial \theta'}{\partial x_j} + u_j \frac{\partial \bar{\theta}}{\partial x_j} + u_j \frac{\partial \theta'}{\partial x_j} - \frac{\partial}{\partial x_j} (\overline{u_j' \theta'}) = \nu Pr^{-1} \frac{\partial^2 \theta'}{\partial x_j^2} \qquad (3.39)$$

The set of ensemble-averaged equations (i.e., Eq. 3.34, Eq. 3.36 and Eq. 3.38) suffer from the well-known closure problem due to the generation of the $\overline{u_i' u_j'}$ and $\overline{u_i' \theta'}$ terms by the non-linear advection terms in Eq. 3.27 and Eq. 3.28. Equations 3.37 and 3.39 may be manipulated to produce transport equations for these two new variables:

$$\frac{D}{Dt}(\overline{u_i' u_j'}) = - \overline{u_i' u_k'} \frac{\partial \bar{u}_j}{\partial x_k} - \overline{u_j' u_k'} \frac{\partial \bar{u}_i}{\partial x_k}$$ production terms

$$- \frac{\partial}{\partial x_k} (\overline{u_i' u_j' u_k'})$$ turbulent transport term

$$-\frac{1}{\rho_o} \frac{\partial}{\partial x_i} (\overline{p' u_j'}) - \frac{1}{\rho_o} \frac{\partial}{\partial x_j} (\overline{p' u_i'})$$ pressure diffusion terms

$$+ \frac{1}{\rho_o} \overline{p' \left(\frac{\partial u_i'}{\partial x_j} + \frac{\partial u_j'}{\partial x_i} \right)}$$ tendency toward isotropy term

$$+ \frac{1}{\theta_o} (g_i \overline{u_j'\theta'} + g_j \overline{u_i'\theta'})$$ buoyant production terms

$$+ \nu \frac{\partial^2 (\overline{u_i'u_j'})}{\partial x_k^2}$$ molecular diffusion terms

$$-2\nu \overline{\frac{\partial u_i'}{\partial x_k} \frac{\partial u_j'}{\partial x_k}}$$ dissipation term

(3.40)

$$\frac{D}{Dt} (\overline{u_i'\theta'}) = -\overline{u_j'u_i'} \frac{\partial \overline{\theta}}{\partial x_j} - \overline{u_j\theta'} \frac{\partial \overline{u}_i}{\partial x_j}$$ production terms

$$- \frac{\partial}{\partial x_j} (\overline{u_i'u_j'\theta'})$$ turbulent transport term

$$- \frac{1}{\rho_o} \frac{\partial}{\partial x_i} (\overline{p'\theta'})$$ pressure diffusion term

$$+ \frac{1}{\rho_o} \overline{p' \frac{\partial \theta'}{\partial x_i}}$$ tendency toward isotropy term

$$+ \frac{1}{\theta_o} g_i \overline{\theta'\theta'}$$ buoyant production term

$$+\nu \frac{\partial^2 (\overline{u_i'\theta'})}{\partial x_j^2}$$ molecular diffusion term

$$- 2\nu \overline{\frac{\partial u_i'}{\partial x_j} \frac{\partial \theta'}{\partial x_j}}$$ dissipation term

(3.41)

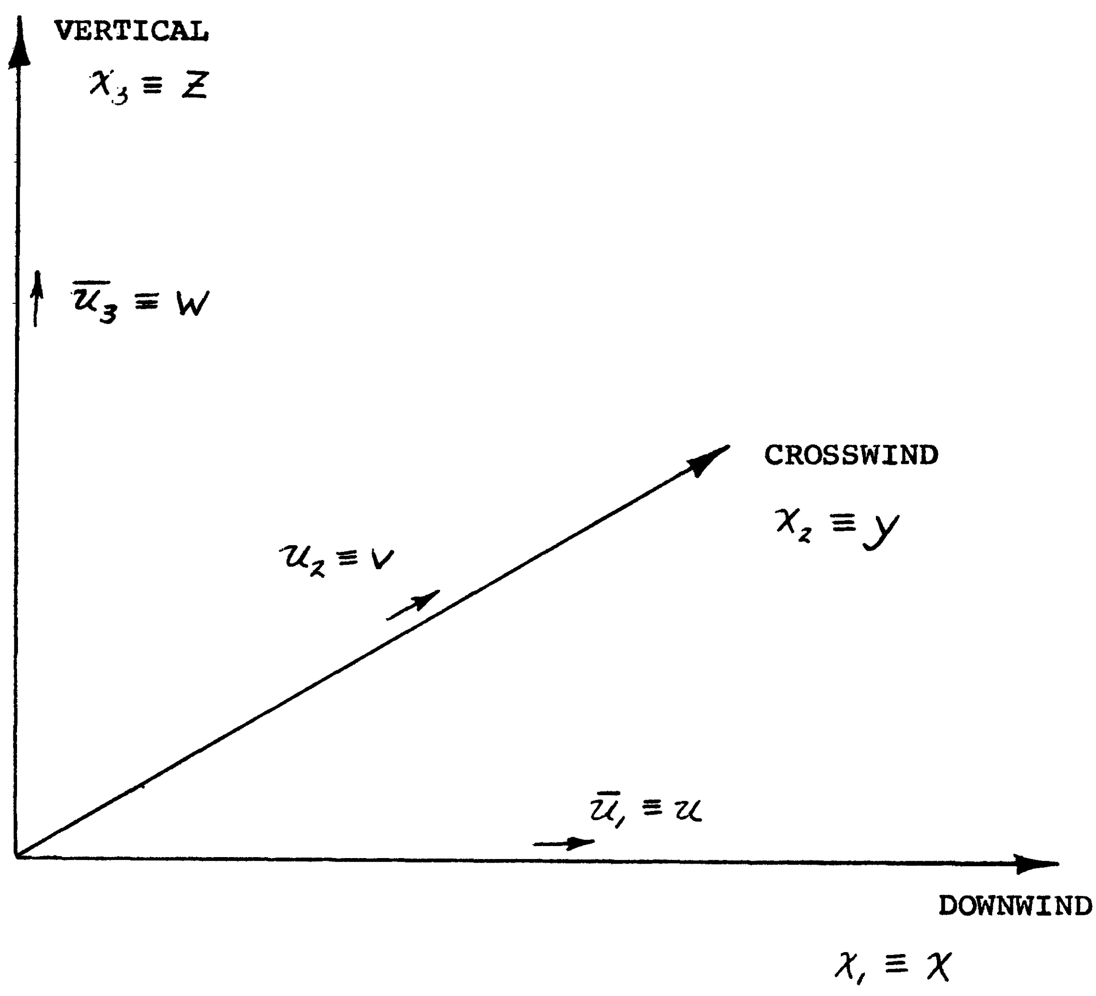
A discussion of the individual terms noted in Eq. 3.40 and Eq. 3.41 can be found elsewhere.[11] These equations were closed by Stuhmiller[2] and the results are listed here for completeness. In Eq. 3.40, the tendency toward isotropy term is neglected, because the turbulence is assumed to be homogeneous, and the molecular diffusion term is neglected because the flow is expected to be highly turbulent. The buoyant production term is also neglected, mainly in order to see how well the turbulence model can do without it, since it was neglected in Stuhmiller's turbulence model. It is found that the incorporation of this term would probably aid the model in reproducing the buoyant line-thermal results (see Sec. 5.2.2). By further making the assumption that the <u>average</u> flow is two-dimensional in the y-z axes of Fig. 3.1, the following closure is made for the trace of Eq. 3.40, which is the turbulence kinetic energy, q, $q \equiv \overline{u_i' u_i'}$,

$$\frac{Dq}{Dt} = 2\sigma\left(\left(\frac{\partial v}{\partial y}\right)^2 + \frac{1}{2}\left(\frac{\partial v}{\partial z} + \frac{\partial w}{\partial y}\right)^2 + \left(\frac{\partial w}{\partial z}\right)^2\right) - 4\alpha q^2 \sigma^{-1}$$
$$+ \Gamma\left(\frac{\partial}{\partial y}\sigma \frac{\partial q}{\partial y} + \frac{\partial}{\partial z}\sigma \frac{\partial q}{\partial z}\right) \qquad (3.42)$$

Figure 3.1

Flow Field Orientation

The flow field of Eqs. 3.42-3.47 is time-dependent and two-dimensional in the y-z axes. The relationship of the time-dependence to the (downwind) x-axis is discussed in Sec. 3.3.3.



The off-diagonal terms of the Reynolds stress tensor are related to a scalar eddy viscosity, σ, where $\overline{u_i' u_j'} = \frac{\sigma}{2}\left(\frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i}\right)$,

and σ has the following transport equation:

$$\frac{D\sigma}{Dt} = \frac{\sigma^2}{q}\left(\left(\frac{\partial v}{\partial y}\right)^2 + \frac{1}{2}\left(\frac{\partial v}{\partial z} + \frac{\partial w}{\partial y}\right)^2 + \left(\frac{\partial w}{\partial z}\right)^2\right) - \alpha q$$

$$+ \Gamma \frac{\sigma}{q}\left(\frac{\partial}{\partial y} \sigma\frac{\partial q}{\partial y} + \frac{\partial}{\partial z} \sigma \frac{\partial q}{\partial z}\right) - \Gamma_1 \left(\frac{\sigma^3}{q^2}\left(\frac{\partial}{\partial y} q \frac{\partial}{\partial y}\left(\frac{q}{\sigma}\right) + \frac{\partial}{\partial z} q\frac{\partial}{\partial z}\left(\frac{q}{\sigma}\right)\right)\right)$$

(3.43)

Finally, the turbulent fluxes of heat in Eq. 3.41 are related to the turbulent momentum fluxes through a reciprocal turbulent Prandtl number, γ_T, which is specified along with the three other turbulence constants α, Γ, and Γ_1. With this turbulence closure, the continuity, momentum, and energy equations become, in a two-dimensional flow

$$\frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \qquad (3.44)$$

$$\frac{\partial v}{\partial t} + \frac{\partial}{\partial y}(v^2) + \frac{\partial}{\partial z}(vw) = -\frac{1}{\rho(\theta_o)}\frac{\partial \bar{p}}{\partial y} + \frac{\partial}{\partial y}\left(\sigma\frac{\partial v}{\partial y}\right) + \frac{\partial}{\partial z}\left(\sigma \frac{\partial v}{\partial z}\right) \qquad (3.45)$$

$$\frac{\partial w}{\partial t} + \frac{\partial}{\partial y}(vw) + \frac{\partial}{\partial z}(w^2) = \frac{-1}{\rho(\theta_o)}\frac{\partial \bar{p}}{\partial z} + \frac{\partial}{\partial y}\left(\sigma\frac{\partial w}{\partial y}\right) + \frac{\partial}{\partial z}\left(\sigma\frac{\partial w}{\partial z}\right) - \left(\frac{\rho(\bar{\theta}) - \rho(\theta_o)}{\rho(\theta_o)}\right) g_z$$

(3.46)

$$\frac{\partial \bar{\theta}}{\partial t} + \frac{\partial}{\partial y}(\bar{\theta} v) + \frac{\partial}{\partial z}(\bar{\theta} w) = \frac{\partial}{\partial y}(\gamma_T \sigma \frac{\partial \bar{\theta}}{\partial y}) + \frac{\partial}{\partial z}(\gamma_T \sigma \frac{\partial \bar{\theta}}{\partial z}) \tag{3.47}$$

With an internal energy variable, I, defined as $I \equiv c_p \bar{\theta}$, equations 3.42-3.47 are solved by the VARR-II code. Additional pollutant and moisture transport equations are discussed in the next two sections, and possible modifications to these equations are discussed in section 6.2.

3.2.1.2 Pollutant Species Transport Equation

A transport equation for a pollutant species density, χ is added to the set of Eqs. 3.42-3.47. The pollutant is assumed to be a neutrally buoyant, passive species, although it may be contained in a buoyant stream of effluent. The assumption that the species is neutrally buoyant could be relaxed, but the model is felt to be useful in modeling most dilute pollutants in its present form. The turbulent diffusion of the pollutant is related to the eddy viscosity of momentum by a reciprocal turbulent Schmidt number, γ_χ. The transport equation may be written down as

$$\begin{bmatrix}\text{substantial derivative}\\ \text{of } \chi\end{bmatrix} = \begin{bmatrix}\text{turbulent transport}\\ \text{of } \chi\end{bmatrix} - \begin{bmatrix}\text{rate of}\\ \text{destruction}\\ \text{of } \chi\end{bmatrix} \tag{3.48}$$

which is represented here as

$$\frac{\partial \chi}{\partial t} + v\frac{\partial \chi}{\partial y} + w\frac{\partial \chi}{\partial t} = \frac{\partial}{\partial y}(\gamma_\chi \sigma \frac{\partial \chi}{\partial y}) + \frac{\partial}{\partial z}(\gamma_\chi \sigma \frac{\partial \chi}{\partial z}) - \sum_{i=1}^{N} \lambda_\chi^{(i)} \chi \qquad (3.49)$$

in the notation of Fig. 3.1.

The destruction of χ is assumed to be by radioactive decay into any of N decay channels, so that the rate of destruction of χ is the product of χ and the sum of its radioactive decay constants $\lambda_\chi^{(i)}$, in Eq. 3.49. This formulation makes no account of sources of the pollutant species through decay of radioactive precursors. It also ignores chemical reactions which could alter the pollutant concentration. However, the extension of the model to include these effects is straightforward.

3.2.1.4 Radioactive Decay Heating

The thermal energy released by radioactive decay of the pollutant is added to the specific internal energy of the fluid. Pollutants may decay by any one of N different decay channels with decay constant $\lambda_x^{(i)}$ and energy $E_\chi^{(i)}$. A fraction $F_\chi^{(i)}$ of the energy is deposited within the plume, yielding an energy release rate of

$$\left(c_p \frac{\partial \bar{\theta}}{\partial t}\right)_{\text{radioactive}} = \frac{4.151\text{x}10^{10} \ \frac{\text{BTU-atoms}}{\text{MeV-lb}_m\text{-mole}}}{\rho W_{mol\chi} / \chi} \sum_{i=1}^{N} F_{\chi}^{(i)} E_{\chi}^{(i)} \lambda_{\chi}^{(i)}$$

(3.50)

where $W_{mol\chi}$ is the molecular weight of χ in lb_m/lb_m-mole. Daughter radiations have been ignored in this formulation, but could be included with their own transport equation. Similarly, alterations of the energy balance caused by chemical reactions has not been treated in this work, but would be easy to address in extensions of this work.

3.2.2 Moist Equations

The inclusion of moisture is considered in this section with the purpose of pointing out the assumptions that allow the equations to be formulated with the concept of virtual potential temperature, in addition to two other moisture variables. The assumptions that are made in this section are important--the moisture model is not meant to be perfectly general; it is expected to do poorly when these assumptions are not valid.

3.2.2.1 Reference State Decomposition

Atmospheric moisture is assumed to be in either the liquid or vapor phases. The amount of vapor is described by the vapor density moisture variable, $\tilde{\rho}_{vap}$, and the amount of cloud liquid water is described by the liquid density moisture variable, $\tilde{\rho}_{liq}$. Transport equations for these two variables are written that take note of the turbulent transports of vapor and liquid, and the processes of evaporation and condensation that cause the interchange of vapor and liquid. First, however, the effect of moisture on the buoyancy of a parcel of air is developed and applied to the description of a hydrostatic reference state.

The density of a parcel of moist air is the sum of the dry air, vapor, and liquid densities:

$$\tilde{\rho} = \tilde{\rho}_{dry} + \tilde{\rho}_{vap} + \tilde{\rho}_{liq} \tag{3.51}$$

In this work the contribution to the density of the typically small amount of cloud liquid water is ignored, (there is usually no liquid water present in the simulations, and when it is present, it is typically less than 1% of the mass of the fluid), so that the concept of virtual potential temperature can be explored. Dropping the $\tilde{\rho}_{liq}$ term and applying the perfect gas law to $\tilde{\rho}_{dry}$ and $\tilde{\rho}_{vap}$ yields:

$$\tilde{\rho} = \frac{\tilde{p}_{dry}}{R_d T} + \frac{\tilde{p}_{vap}}{R_v T} \equiv \frac{(\tilde{p}_{dry}+\tilde{p}_{vap})}{R_d T_v} = \frac{\tilde{p}}{R_d T_v} \tag{3.52}$$

where $\tilde{p}$ is the total pressure, m_{vap} and m_{dry} are molecular weights and the virtual temperature, $\tilde{T}_v$, is

$$\tilde{T}_v \equiv \tilde{T} \left[\frac{1 + m_{dry}\tilde{\rho}_{vap}/m_{vap}\rho_{dry}}{1 + \tilde{\rho}_{vap}/\tilde{\rho}_{dry}} \right] \tag{3.53}$$

It is very important to note in Eq. 3.52 that the virtual temperature is a fictitious temperature that is used in the dry gas equation of state to give the density of moist air. Generally the virtual temperature is no more than a few degrees higher than the thermodynamic temperature for typical atmospheric conditions.

Following the development in Sec. 3.2.1.1, the variations of virtual temperature, pressure, and density of a static atmosphere are "subtracted out" by making a reference state decomposition:

$$\left\{\begin{array}{l}\text{the value of}\\ \text{a primitive}\\ \text{variable}\end{array}\right\} = \left\{\begin{array}{l}\text{its value in a uni-}\\ \text{formly moist adiabatic}\\ \text{atmosphere (function}\\ \text{of height only)}\end{array}\right\} + \left\{\begin{array}{l}\text{a departure}\\ \text{from the}\\ \text{state at}\\ \text{rest}\end{array}\right\} \tag{3.54}$$

Or, in the notation of this work:

$$\tilde{p} \rightarrow p_o + p \tag{3.55}$$

$$\tilde{\rho} \rightarrow \rho_o + \rho \tag{3.56}$$

$$\tilde{T}_v \rightarrow T_{vo} + T_v \tag{3.57}$$

$$\tilde{u}_i \rightarrow 0 + u_i \tag{3.58}$$

the only difference here to the reference state decomposition of Eqs. 3.6-3.9 is in the use of the (fictitious) virtual temperature in order to allow the use of an equation of state that is analogous to Eq. 3.4:

$$\tilde{\rho} = \tilde{p}/R_d\tilde{T}_v \tag{3.59}$$

Substituting Eqs. 3.55-3.58 into the primitive equation set (Eqs. 3.1-3.3 and Eq. 3.59), and setting the time derivatives and perturbations to zero yields the state of the moist adiabatic atmosphere. The continuity and energy equations are trivial (as before), and the momentum equation becomes the moist hydrostatic equation:

$$\frac{dp_o}{dz} = -\rho_o g \tag{3.60}$$

The equation of state is simply

$$p_o = \rho_o R_d T_{vo} \tag{3.61}$$

The first Law of Thermodynamics for an unsaturated adiabatic process in this atmosphere is

$$dQ = 0 = c_p^{moist}\, dT_{vo} - dp_o/\rho_o \tag{3.62}$$

Approximating the heat capacity for a moist gas, c_p^{moist}, as that of a dry gas, c_p, dividing by dz and substituting Eq. 3.62 into 3.60 yields an approximate lapse rate for a moist, unsaturated atmosphere which is the same as that for a dry adiabatic atmosphere:

$$\frac{-dT_{vo}}{dz} = \frac{g}{c_p} = 9.76^{o}C/km \tag{3.63}$$

To this point the resting state of a moist adiabatic atmosphere has been presented. The neglect of the effect of the liquid water on the total density has allowed the treatment of moisture to duplicate the dry atmosphere equations after the transformation of temperature to virtual temperature. The equations for the perturbations are identical to those of the dry atmosphere developed in Sec. 3.2.1.1, except that temperature is replaced by virtual temperature, and a latent heat release term is included:

Continuity Eq.

$$\frac{\partial u_j}{\partial x_j} = 0 \tag{3.64}$$

Momentum Eq.

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{1}{\rho_o}\frac{\partial p}{\partial x_i} + \frac{T_v}{T_{vo}} g_i + \frac{\mu_o}{\rho_o}\frac{\partial^2 u_i}{\partial x_j^2} \tag{3.65}$$

Energy Eq.

$$\frac{\partial T_v}{\partial t} + u_j \frac{\partial T_v}{\partial x_j} = \nu Pr^{-1}\frac{\partial^2 T_v}{\partial x_j^2} - \frac{L}{\rho c_p}\left(\frac{D\rho_{vap}}{Dt}\right)_{phase} \tag{3.66}$$

The latent heat release term is considered in Sec. 3.2.2.4.

Define the virtual potential temperature, θ_v, as

$$\theta_v \equiv \tilde{T}_v \left(\frac{1000}{\tilde{p}}\right)^{R_d/c_p^{moist}} \tag{3.67}$$

Again assume that c_p^{moist} is essentially equal to c_p. Differentiating with respect to height finds that the moist unsaturated adiabatic atmosphere has a lapse of virtual potential temperature that vanishes:

$$\frac{d\theta_{vo}}{dz} = 0 \tag{3.68}$$

The result here is that the virtual potential temperature is a constant in the reference state.

Neglecting the perturbation pressure, p, with respect to p_o in Eq. 3.56, the use of θ_v instead of T_v in the primitive equations (Eq. 3.64-Eq. 366) gives

Continuity Eq:

$$\frac{\partial u_j}{\partial x_j} = 0 \tag{3.69}$$

Momentum Eq:

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = \frac{-1}{\rho(\theta_{vo})} \frac{\partial p}{\partial x_i} - \frac{\rho(\theta_v) - \rho(\theta_{vo})}{\rho(\theta_{vo})} g_i + \nu \frac{\partial^2 u_i}{\partial x_j^2} \tag{3.70}$$

Energy Eq:

$$\frac{\partial \theta_v}{\partial t} + u_j \frac{\partial \theta_v}{\partial x_j} = \nu Pr^{-1} \frac{\partial^2 \theta_v}{\partial x_j^2} - \frac{L}{\rho c_p} \left(\frac{D\rho_{vap}}{Dt}\right)_{phase} \tag{3.71}$$

The result here is the same as in Sec. 3.2.1.1: the strong variation of pressure with height is no longer present in the primitive equations. This formulation is common (although in slightly different forms) among papers in meteorology.

Transport equations may be written down for the water vapor and liquid water densities according to the conservation scheme:

$$\left\{\begin{array}{l}\text{Eulerian time}\\ \text{rate of change}\\ \text{of vapor or}\\ \text{liquid}\end{array}\right\} = \left\{\begin{array}{l}\text{Diffusion of}\\ \text{vapor or}\\ \text{liquid}\end{array}\right\} + \left\{\begin{array}{l}\text{Gain or loss of}\\ \text{vapor or liquid}\\ \text{due to phase}\\ \text{changes}\end{array}\right\} \qquad (3.72)$$

or, in the notation of this work:

$$\frac{\partial \rho_{vap}}{\partial t} + u_j \frac{\partial \rho_{vap}}{\partial x_j} = \nu Sc_{vap}^{-1} \frac{\partial^2 \rho_{vap}}{\partial x_j^2} + \left(\frac{D\rho_{vap}}{Dt}\right)_{phase} \qquad (3.73)$$

$$\frac{\partial \rho_{liq}}{\partial t} + u_j \frac{\partial \rho_{liq}}{\partial x_j} = \nu Sc_{liq}^{-1} \frac{\partial^2 \rho_{liq}}{\partial x_j^2} - \left(\frac{D\rho_{vap}}{Dt}\right)_{phase} \qquad (3.74)$$

where the gain or loss of vapor due to phase changes, $(D\rho_{vap}/Dt)_{phase}$, identically shows up as a loss or gain of liquid, and Schmidt numbers that describe the molecular diffusion of vapor and liquid are introduced, respectively. The terminal fall velocities of the liquid water droplets are ignored. The $\left(\frac{D\rho_{vap}}{Dt}\right)_{phase}$ term is discussed in Sec. 3.2.2.3.

Note that any constant background (ambient atmospheric) value of ρ_{vap} and ρ_{liq} trivially satisfied these equations, so that no new information would be brought into the specification of the reference state by decomposing the variables in these transport equations. That is, ρ_{vap} and ρ_{liq} do not have a reference state "subtracted away" from them, unlike the other primitive variables $\tilde{p}$, $\tilde{\theta}_v$, and $\tilde{\rho}$.

3.2.2.2 Reynolds Decomposition and Closure

A Reynolds decomposition of the primitive equations is made as in Sec. 3.2.1.2. Each primitive variable in the equation set is decomposed into its ensemble-averaged and fluctuating parts:

$$p \rightarrow \bar{p} + p' \tag{3.75}$$

$$\theta \rightarrow \bar{\theta} + \theta_v' \tag{3.76}$$

$$\rho \rightarrow \bar{\rho} + \rho' \tag{3.77}$$

$$u_j \rightarrow 0 \quad + u_j' \tag{3.78}$$

$$\rho_{vap} \rightarrow \bar{\rho}_{vap} + \rho_{vap}' \tag{3.79}$$

$$\rho_{liq} \rightarrow \bar{\rho}_{liq} + \rho_{liq}' \tag{3.80}$$

By selectively ensemble-averaging and subtracting the equations, and by making use of the continuity equation, the primitive equations yield the following relationships:

Continuity Eq:

$$\frac{\partial \bar{u}_j}{\partial x_j} = 0 \tag{3.81}$$

Momentum Eq:

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = \frac{-1}{\rho(\theta_{vo})} \frac{\partial \bar{p}}{\partial x_i} - \frac{\rho(\bar{\theta}_v) - \rho(\theta_{vo})}{\rho(\theta_{vo})} g_i + \nu \frac{\partial^2 u_i}{\partial x_j^2}$$

$$- \frac{\partial}{\partial x_j} (\overline{u_i' u_j'}) \qquad (3.82)$$

Energy Eq:

$$\frac{\partial \bar{\theta}_v}{\partial t} + u_j \frac{\partial \bar{\theta}_v}{\partial x_j} = \nu Pr^{-1} \frac{\partial^2 \theta_v}{\partial x_j^2} - \frac{\partial}{\partial x_j} (\overline{u_j' \theta_v'}) - \frac{L}{\rho(\theta_v) c_p} \left(\frac{D\bar{\rho}_{vap}}{Dt} \right)_{phase} \qquad (3.83)$$

and the transport equations for moisture, Eq. 3.73 and Eq. 3.74 yield

Vapor Eq:

$$\frac{\partial}{\partial t} \bar{\rho}_{vap} + u_j \frac{\partial \bar{\rho}_{vap}}{\partial x_j} = \nu Sc_{vap}^{-1} \frac{\partial^2 \bar{\rho}_{vap}}{\partial x_j^2} - \frac{\partial}{\partial x_j} (\overline{\rho_{vap}' u_j'}) + \left(\frac{D\bar{\rho}_{vap}}{Dt} \right)_{phase} \qquad (3.84)$$

Liquid Eq:

$$\frac{\partial}{\partial t} \bar{\rho}_{liq} + u_j \frac{\partial \bar{\rho}_{liq}}{\partial x_j} = \nu Sc_{liq}^{-1} \frac{\partial^2 \bar{\rho}_{liq}}{\partial x_j^2} - \frac{\partial}{\partial x_j} (\overline{\rho_{liq}' u_j'}) - \left(\frac{D\bar{\rho}_{vap}}{Dt} \right)_{phase} \qquad (3.85)$$

Rather than providing the full equations for the correlated fluctuations $\overline{u_i' u_j'}$, $\overline{u_j' \theta_v'}$, $\overline{u_j' \rho_{vap}'}$, and $\overline{u_j' \rho_{liq}'}$, the turbulence closure is simply extended from that developed in Sec. 3.2.1.2. The closed set of equations in two-dimensions is, in the notation of Fig. 3.1

Continuity Eq:

$$\frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \tag{3.86}$$

Momentum Eqs:

$$\frac{Dv}{Dt} = \frac{-1}{\rho(\theta_{vo})}\frac{\partial \bar{p}}{\partial y} + \frac{\partial}{\partial y}\left(\sigma\frac{\partial v}{\partial y}\right) + \frac{\partial}{\partial z}\left(\sigma\frac{\partial v}{\partial z}\right)$$

$$\frac{Dw}{Dt} = \frac{-1}{\rho(\theta_{vo})}\frac{\partial \bar{p}}{\partial z} - \frac{\rho(\bar{\theta}_v) - \rho(\theta_{vo})}{\rho(\theta_{vo})} g_z + \frac{\partial}{\partial y}\left(\sigma\frac{\partial w}{\partial y}\right) + \frac{\partial}{\partial z}\left(\sigma\frac{\partial w}{\partial z}\right) \tag{3.87}$$

Energy Eq:

$$\frac{D}{Dt}(c_p\bar{\theta}_v) = \frac{\partial}{\partial y}\left(\gamma_T\sigma\frac{\partial(c_p\bar{\theta}_v)}{\partial y}\right) + \frac{\partial}{\partial z}\left(\gamma_T\sigma\frac{\partial(c_p\bar{\theta}_v)}{\partial z}\right) - \frac{L}{\rho(\theta_v)}\left(\frac{D\bar{\rho}_{vap}}{Dt}\right)_{phase} \tag{3.88}$$

Vapor Eq:

$$\frac{D}{Dt}\bar{\rho}_{vap} = \frac{\partial}{\partial y}\left(\gamma_v\sigma\frac{\partial\bar{\rho}_{vap}}{\partial y}\right) + \frac{\partial}{\partial z}\left(\gamma_v\sigma\frac{\partial\bar{\rho}_{vap}}{\partial z}\right) + \left(\frac{D\bar{\rho}_{vap}}{Dt}\right)_{phase} \tag{3.89}$$

Liquid Eq:

$$\frac{D}{Dt}\bar{\rho}_{liq} = \frac{\partial}{\partial y}\left(\gamma_L\sigma\frac{\partial\bar{\rho}_{liq}}{\partial y}\right) + \frac{\partial}{\partial z}\left(\gamma_L\sigma\frac{\partial\bar{\rho}_{liq}}{\partial z}\right) - \left(\frac{D\bar{\rho}_{vap}}{Dt}\right)_{phase} \tag{3.90}$$

Eddy Viscosity Eq:

$$\frac{D\sigma}{Dt} = \frac{\sigma^2}{q}\left(\left(\frac{\partial v}{\partial y}\right)^2 + \frac{1}{2}\left(\frac{\partial v}{\partial z} + \frac{\partial w}{\partial y}\right)^2 + \left(\frac{\partial w}{\partial z}\right)^2\right) - \alpha q +$$

$$+ \Gamma\frac{\sigma}{q}\left(\left(\frac{\partial}{\partial y}\sigma\frac{\partial q}{\partial y}\right)+\left(\frac{\partial}{\partial z}\sigma\frac{\partial q}{\partial z}\right)\right) - \Gamma_1\left(\frac{\sigma^3}{q^2}\frac{\partial}{\partial y}q\frac{\partial}{\partial y}\left(\frac{q}{\sigma}\right) + \frac{\partial}{\partial z}q\frac{\partial}{\partial z}\left(\frac{q}{\sigma}\right)\right) \tag{3.91}$$

Turbulence Kinetic Energy Eq:

$$\frac{Dq}{Dt} = 2\sigma\left(\left(\frac{\partial v}{\partial y}\right)^2 + \frac{1}{2}\left(\frac{\partial v}{\partial z} + \frac{\partial w}{\partial y}\right)^2 + \left(\frac{\partial w}{\partial z}\right)^2\right) - 4\alpha q\sigma^{-1}$$

$$+ \Gamma\left(\frac{\partial}{\partial y}\sigma\frac{\partial q}{\partial y} + \frac{\partial}{\partial z}\sigma\frac{\partial q}{\partial z}\right) \tag{3.92}$$

Pollutant Eq:

$$\frac{D\chi}{Dt} = \frac{\partial}{\partial y}\left(\gamma_\chi\sigma\frac{\partial \chi}{\partial y}\right) + \frac{\partial}{\partial z}\left(\gamma_\chi\sigma\frac{\partial \chi}{\partial z}\right) - \sum_{i=1}^{N}\lambda_\chi^{(i)}\chi \tag{3.93}$$

where reciprocal turbulent Prandtl and Schmidt numbers have been introduced, and are assumed to be constants.

3.2.2.3 Equilibrium Cloud Microphysics Model

The cloud microphysics model simply assumes that water vapor and liquid are always in equilibrium. Further, the surface tension of the liquid droplets is ignored. That is, phase equilibrium over a flat surface of water is assumed to exist. A phase diagram that illustrates this equilibrium is sketched in Fig. 3.2.2.3.1. The liquid-vapor equilibrium curve above $273^{o}K$ is the locus of points that the saturation vapor pressure, $e_{sat}(T)$, may take. The vapor density, ρ_{vap}, in the presence of liquid water would be $e_{sat}(T)/R_{vap}T$. If there is no liquid available to evaporate, then the vapor density may be less than this saturation value. Below $273^{o}K$ the subcooled liquid-vapor equilibrium (dashed line) is obeyed. No ice formation is allowed. The entire liquid-vapor equilibrium curve is given by Magnus' formula:[39]

$$\log_{10} e_{sat} = - \frac{2937.4}{T} - 4.9283 \log_{10} T + 23.5518 \qquad (3.94)$$

The $\left(\frac{D\bar{\rho}_{vap}}{Dt}\right)_{phase}$ term of Eq. 3.89 and Eq. 3.90 is simply adjusted to make the liquid and vapor coexist. The logic of the moisture model is illustrated in Fig. 3.2.2.3.2. Liquid and vapor are advected and diffused in an initial calculation for each computer cell. This generally results in a non-equilibrium moisture state in the cell, so the cell is allowed to evaporate or condense water in order to restore the equilibrium. The amount of evaporation or condensation in each cell is noted in order to provide the latent heat release term in the energy equation.

3.2.2.4 Latent Heat Source Term

The latent heat source term is calculated in each cell

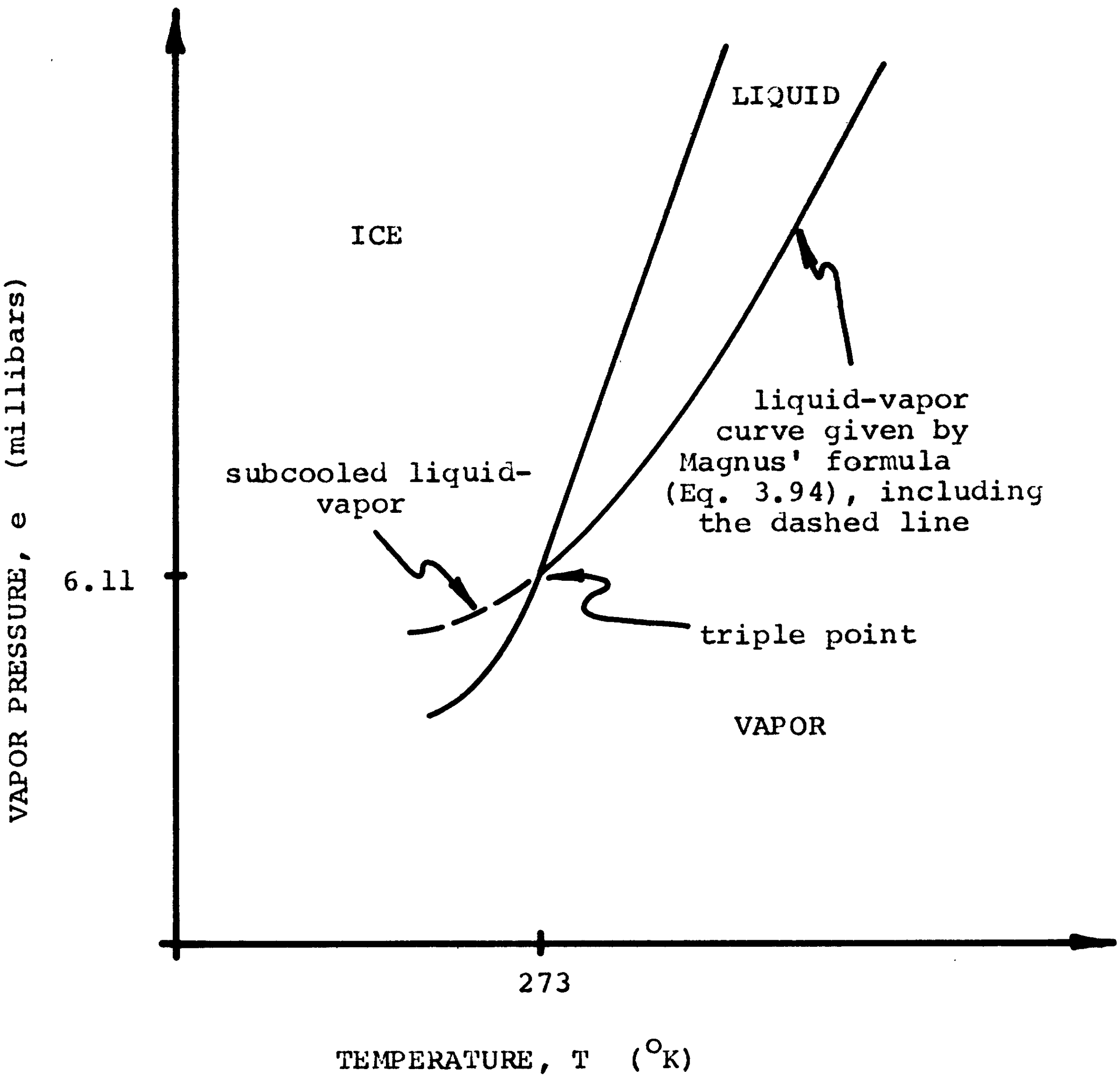


Fig. 3.2.2.3.1 Phase Diagram for Water Substance

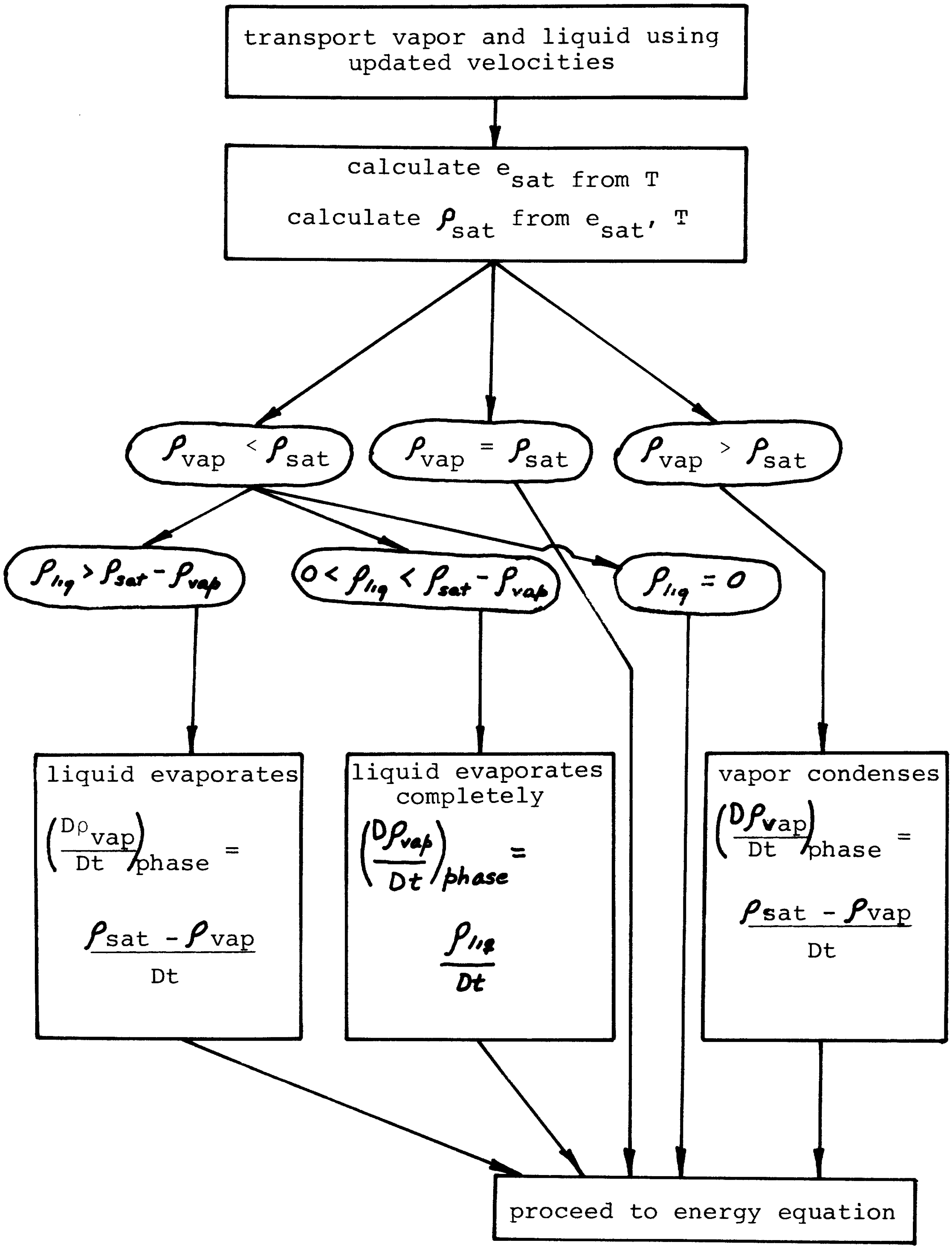


Fig. 3.2.2.3.2 Logic Diagram for the Equilibrium Moisture Calculation in a Single Cell during a Single Timestep

at every step depending on whether evaporation or condensation takes place. The latent heat release term is calculated as

$$\text{Latent Heat Release} \left[\frac{\text{BTU}}{\text{lb}_m\ \text{sec}}\right] = -\frac{L}{\rho(\theta_v)}\left(\frac{D\bar{\rho}_{vap}}{Dt}\right)_{phase} \quad (3.95)$$

where the latent heat of vaporization, L, is assumed to be a constant, 1075 BTU/lb_m. The $\left(\frac{D\rho_{vap}}{Dt}\right)_{phase}$ is found in the logic diagram of Fig. 3.2.2.3.2.

3.3 Model Solution Methodology

3.3.1 The VARR-II Fluid Mechanics Algorithm

The VARR-II computer code[40] is the starting point for the model development methodology in this work. In its original form, the VARR-II code solves the two-dimensional time-dependent turbulent fluid mechanics equations of continuity, momentum, and energy for a Boussinesq fluid. (The Boussinesq approximation to the momentum equation is considered in Sec. 3.2.1.1.) Two closure variables, the eddy viscosity, σ, and the turbulence kinetic energy, q, are also calculated from their own transport equations. The original VARR-II computer code is quite flexible in the choice of boundary conditions, allowing no-slip, free-slip, continuative inflow/outflow, or prescribed inflow/outflow boundaries.

The VARR-II fluid mechanics algorithm is the Simplified Marker and Cell (SMAC) method.[41] The computer mesh for this method is Eulerian in either Cartesian or cylindrical geometry, and the primitive variables are solved directly, with no transformation to vorticity-stream function variables. The algorithm divides naturally into two sections during each time step: In the first section the velocity field is updated using the previous velocity and pressure fields with mixed central and donor-cell differencing[42] of the equations. These velocities generally do not satisfy the continuity equation, so in a second section a pressure iteration adjusts these velocities until they satisfy continuity. Once the divergence-free updated velocity field is known, the energy and turbulence transport equations are updated, completing the calculational cycle of the time step.

The basic SMAC fluid mechanics algorithm has not been modified in this work. Pollutant and moisture transport equations have been added to the equation set, and they are updated in the same manner as the energy and turbulence variables, using the divergence-free updated velocity field. The stability of the method for problems of an atmospheric scale is considered in Sec. 5.2.1.

3.3.2 Orientation of the Computer Mesh

The optimal orientation of the two-dimensional computer solution mesh is discussed here. Consider the representative three-dimensional plume in Fig. 3.3.2.1a. The plume has bent over in the imposed (one-dimensional) wind field, and the plume boundaries monotonically expand as the plume proceeds downwind. The most natural possibilities of orienting a two-dimensional solution mesh on this flow are: (1) to align the mesh parallel to the wind and through the center of the plume, as in Fig. 3.3.2.1b, or (2) to align the mesh perpendicular to the flow, as in Fig. 3.3.2.1c.

The advantages of the "crosswind" alignment of Fig. 3.3.2.1c over the "downwind" alignment of Fig. 3.3.2.1b are immediately apparent. In the crosswind alignment a three-dimensional simulation results since in the downwind Lagrangian translation of the computational mesh the time variable becomes a surrogate for the downwind position x, where

$x = \int_0^t u(z(t))dt$. The downwind alignment is appropriate only for cases of line-source plumes--in which internal recirculation and entrainment will be of secondary importance to buoyant plume rise and atmospheric turbulent entrainment. Further, the crosswind alignment can take advantage of the centerline symmetry of the turbulent vortex pair to reduce the total mesh area by a factor of two, while the downwind

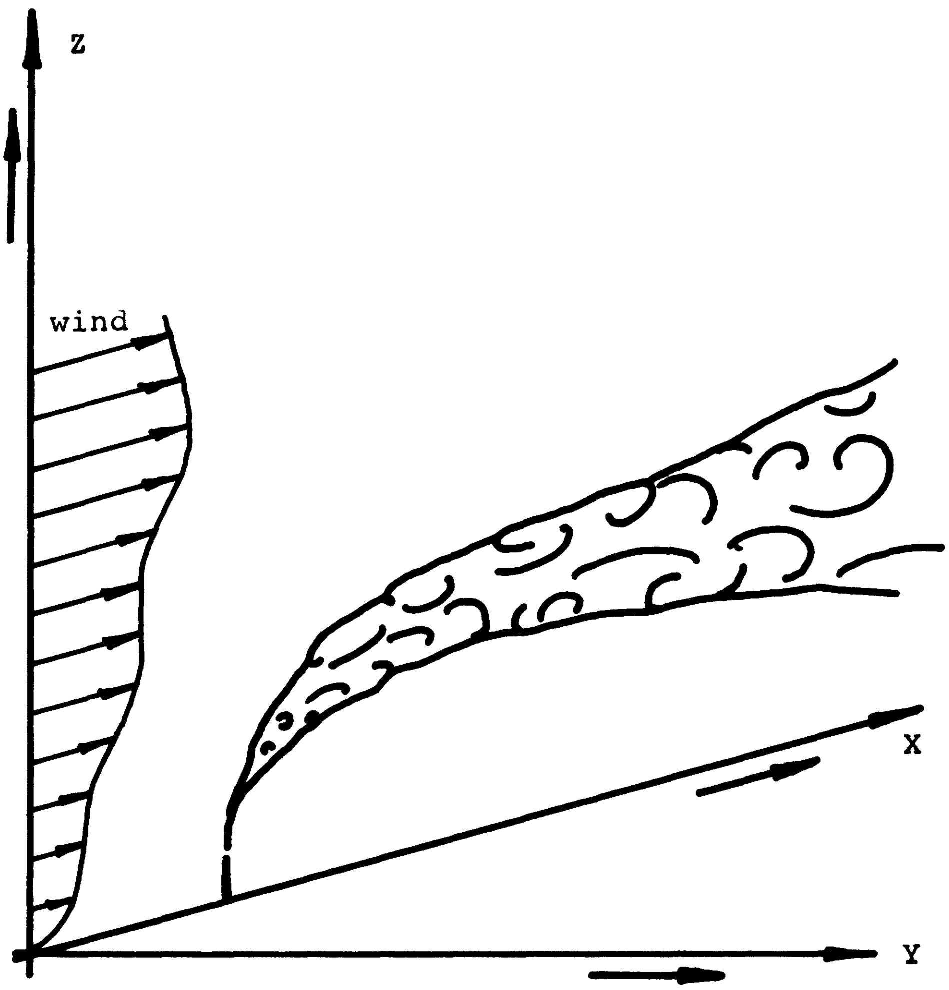


Fig. 3.3.2.1a Bent-Over Buoyant Plume with Ambient Thermal Stratification.

Fig. 3.3.2.1b

Mesh Alignment Appropriate for a Line Source Release

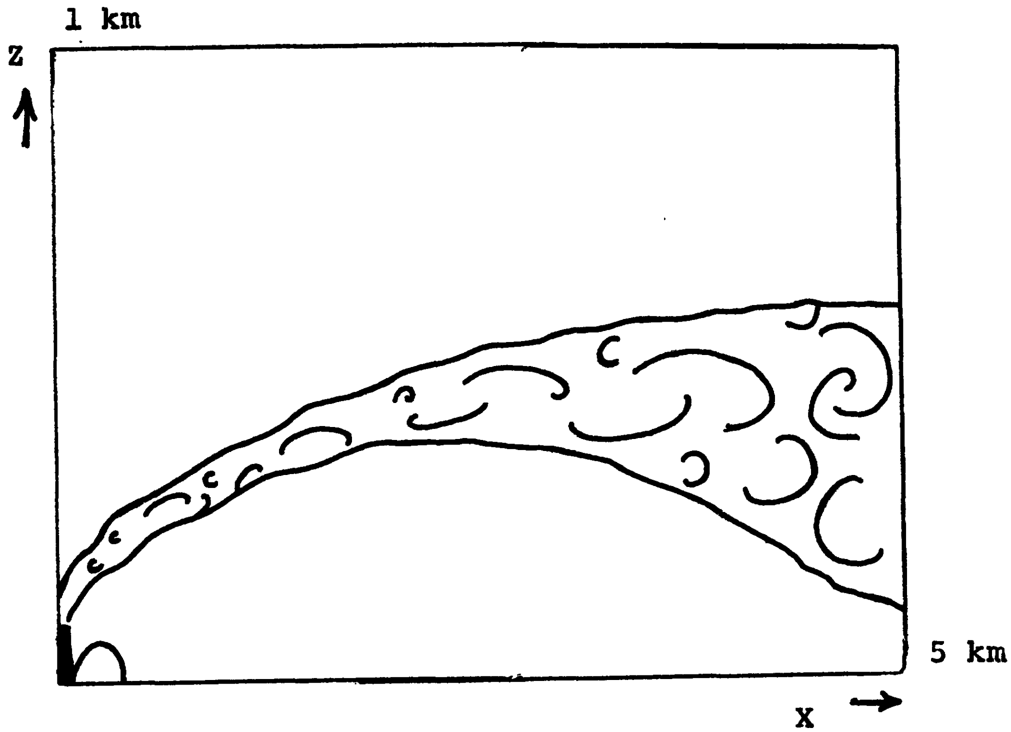
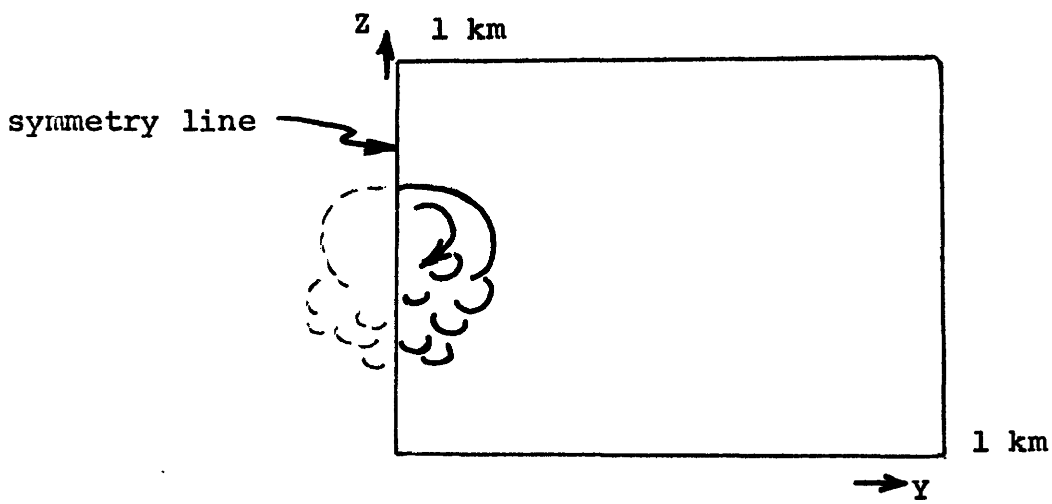


Fig. 3.3.2.1c

Mesh Alignment Appropriate for a Point Source Release



alignment scheme needs an extraordinarily long x-axis to model the same plume. Overall, the crosswind alignment scheme is about five times smaller than the downwind scheme. The velocity field in the crosswind alignment is that of a two-dimensional turbulent vortex, which typically exhibits strong shearing and entrainment of fluid. The velocity field in the downwind alignment is that of a two-dimensional turbulent deflected jet, which over most of the flow field exhibits a much smaller amount of shearing and entrainment. Clearly, the crosswind alignment scheme is expected to simulate the more important features of the flow.

The singular disadvantage of the crosswind alignment scheme is that it cannot explicitly calculate the shear-produced turbulence of the mean wind field, since the mean wind has no component in the y-z plane. The resolution of this problem is discussed in Sec. 4.3.3.

3.3.3 Downwind Advection of the Mesh

From the discussion in Sec. 3.3.2, the computer solution mesh is aligned perpendicular to the wind. The time evolution of the flow field of the plume cross section is drawn in Fig. 3.3.3.1. The choice of an appropriate downwind advection velocity of the computer mesh is needed in order to reconstruct

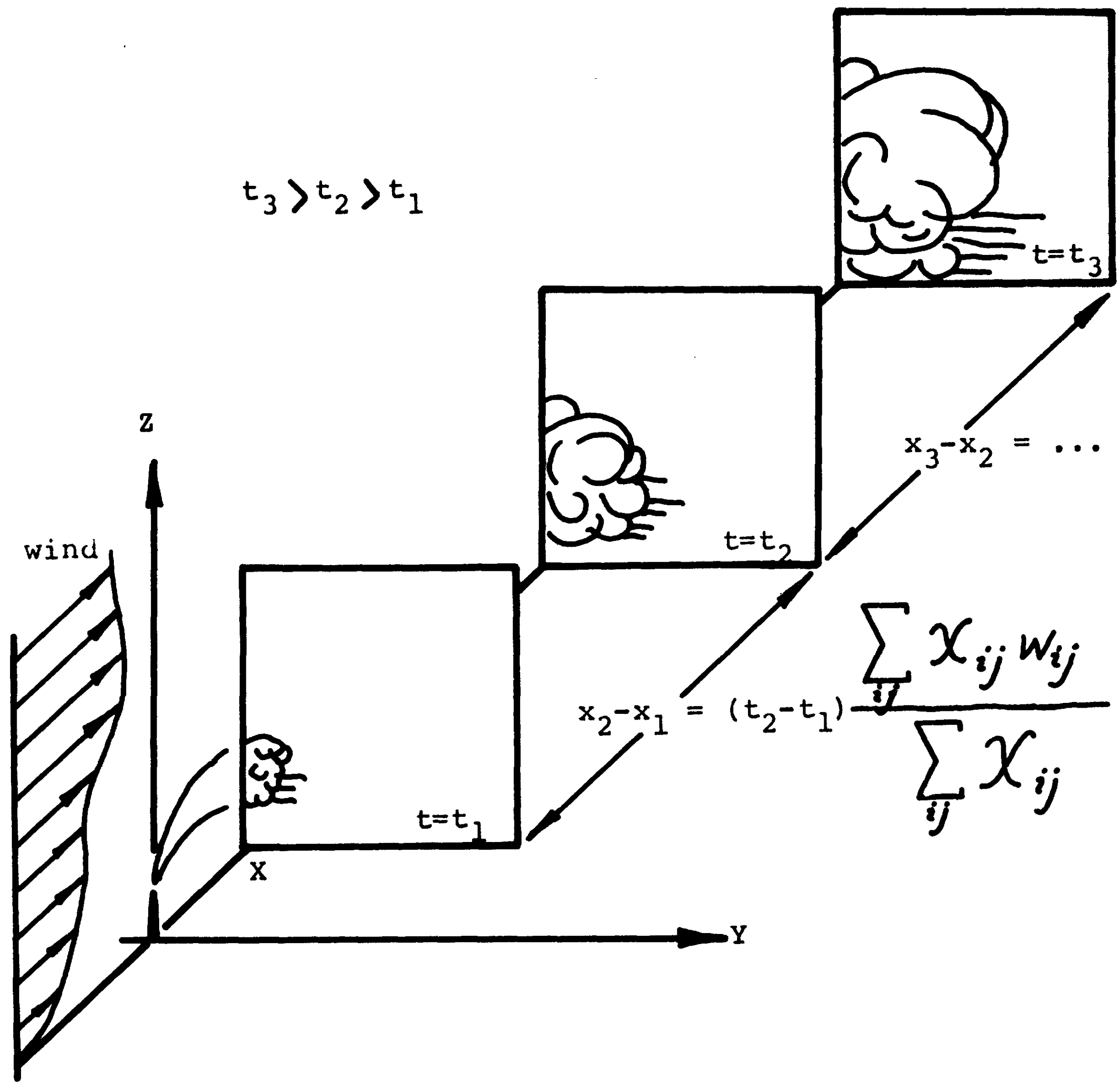


Fig. 3.3.3.1 Reconstruction of the Three-dimensional Plume. Wind vectors as a function of height are shown.

the full steady state plume, i.e., the time of the computer simulation must be related to a downwind distance. The choice is difficult because the wind profile dictates that fluid elements at different heights will advect downwind at different rates. A simple approximation is that the advection velocity should be equal to the "pollutant averaged" wind speed:

$$\frac{\Delta x}{\Delta t} = \frac{\int_0^\infty \int_0^\infty u(z)\ \chi(y,z)\,dy\,dz}{\int_0^\infty \int_0^\infty \chi(y,z)\,dy\,dz} \qquad (3.96)$$

The finite difference form of Eq. 3.96 is written in Fig. 3.3.3.1. The calculation of this quantity is performed in the "statistics package" of Sec. 3.3.7. A further refinement of the solution scheme is discussed in Sec. 6.2.1.

In practice, for plumes that are released from tall stacks, the amount of wind shear that the plume encounters is ordinarily moderate and does not greatly alter the plume behavior.

3.3.4 Property Data

The original VARR-II computer code allows for quadratic fitting of air property data versus temperature. In view of the fact that potential temperature is substituted for temperature in moist simulations, the scheme of fitting property data to temperature must be examined. The air property data to be fitted includes density, specific internal energy, dynamic viscosity, thermal conductivity, and heat capacity at constant pressure. The coefficients of the quadratic fits for dry air data[43] are listed in Table 3.3.4.1, along with the quadratic form that they are used in. The effect on the property value of the substitution of θ or θ_v for $\tilde{T}$ is considered next.

The use of $\tilde{T}$ or $\tilde{T}_v$ in the perfect gas law yields, by definition, the correct density of a dry or moist parcel of air, respectively. A quadratic fit of the perfect gas law over a small temperature range of interest would yield essentially exact results for the density as well. The calculation of densities with θ or θ_v substituted into the formula for $\tilde{T}$ is also appropriate because θ or θ_v vary from $\tilde{T}$ by very little compared to the absolute temperature. Recall that θ or θ_v is used in the problem formulation to eliminate the compressible nature of the hydrostatic atmosphere. The relevant density variations in the momentum equation are the relative density variations, and the criteria for the use of, say θ_v for T is that

$$\frac{\rho(\tilde{T})-\rho(T_o)}{\rho(T_o)} \simeq \frac{\rho(\theta_v)-\rho(\theta_{vo})}{\rho(\theta_{vo})} \qquad (3.97)$$

Table 3.3.4.1 Property Values of Air

				Constants		
i	symbol	property	units	a_i	b_i	c_i
1	ρ	density	lb_m/ft^3	2.0×10^{-7}	-1.78×10^{-4}	0.086394
2	I	internal energy	BTU/lb_m	4.3×10^{-6}	1.71×10^{-1}	78.357
3	ν	dynamic viscosity	$lb_m/ft \cdot sec$	-1.0×10^{-6}	1.92×10^{-3}	1.0932
4	K	thermal conductivity	$BTU/ft\ sec\ ^oR$	0	2.59×10^{-5}	0.01313
5	C_p	heat capacity at constant pressure	$BTU/lb_m\ ^oR$	0	-2.00×10^{-6}	0.24008

$$\text{property } i = a_i\ (T-460^oR)^2 + b_i\ (T-460^oR) + c_i$$

$(T \text{ in } ^oR)$

with a similar condition for θ in dry simulations. This relation holds with about four percent accuracy for the most extreme cases encountered in this work.

The specific internal energy is originally fitted versus T. Again, the fact that θ or θ_v is close to T compared to the absolute temperature allows them to be interchanged without significant error. The specific internal energy is accurate to about 4 percent under this substitution.

The values of dynamic viscosity and thermal conductivity are important only if the flow becomes laminar. None of the simulations in this work are expected to encounter regions of laminar flow, so the fitted values of molecular viscosity and thermal conductivity are unimportant.

The specific heat varies slowly with temperature, and the substitution of θ or θ_v for T results in only a 0.02 percent error for typical cases.

The necessary property data for equilibrium conditions of water vapor and cloud liquid water are included in Secs. 3.2.2.3 and 3.2.2.4. The inclusion of water in the simulations is assumed to have a negligible effect on the property data of the air-water mixture, except for the density, which is corrected through the use of the virtual temperature.

3.3.5 Mesh Initialization and Boundary Conditions

3.3.5.1 Input Profiles

Seven vertical profiles are required for a simulation. Five of the profiles serve to specify the boundary conditions on the computer mesh, one profile (the mean wind wpeed) is needed by the statistics package, and one profile (the hydrostatic pressure) is needed by the equilibrium moisture thermodynamics model. The required profiles are listed in Table 3.3.5.1. Each vertical profile consists of a set of values that are representative of the cell-centered temperature, wind speed, etc. The number of values is obviously equal to the number of fluid cells in the z-direction. The extension of the model to time-dependent vertical profiles is considered in Sec. 6.2.2.

3.3.5.2 Boundary Conditions

Boundary conditions must be specified for each of eight variables on the four walls of the computer mesh. The walls of the computer mesh are numbered in Fig. 3.3.5.1. Wall #1 is in the plume centerline with the real computer simulation to its left. For this purpose, wall #1 is a free-slip solid wall. Wall #4 always represents the earth, and is specified to be a no-slip wall. The earth is assumed to be a perfect

Table 3.3.5.1

Required Input Profiles

Atmospheric Profile	Units
virtual potential temperature	^oF
water vapor density	lb_m/ft^3
cloud liquid water density	lb_m/ft^3
eddy viscosity	ft^2/sec
turbulence kinetic energy	ft^2/sec^2
mean wind speed[A]	ft/sec
hydrostatic pressure[B]	millibars

A. The mean wind speed is required by the statistics package of Sec. 3.3.7.

B. The hydrostatic pressure is required by the equilibrium moisture thermodynamics model of Sec. 3.2.2.3.

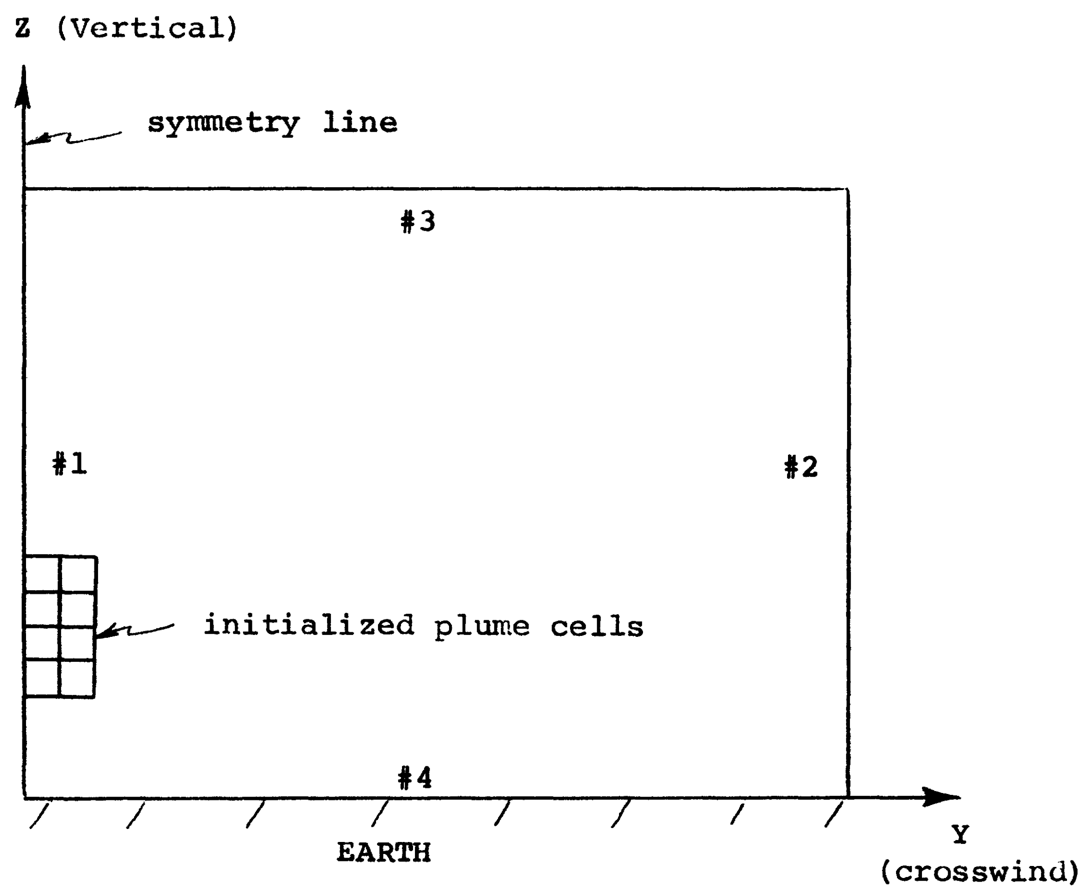


Fig. 3.3.5.1 Wall Numbering Scheme

reflector of pollutant and humidity in this work. This assumption could be easily modified to account for deposition of pollutant, sources of humidity, etc., for any case of specific interest. Walls #2 and #3 are chosen to be sufficiently far away from the plume so that negligible error is introduced in making them solid and free-slip. In practice, the plumes rise toward wall #3 and begin to deflect when their 10% boundary intersects the wall. This serves as a rough criterion on when to stop the computer simulation.

A summary of the boundary conditions is found in Table 3.5.5.2. The solid-wall, no-slip and free-slip conditions are found in the specification of the two velocity components, v and w. The reflective conditions are due to the "perfect reflecting walls" assumption; they are foregone at wall #2 for the five variables that are known as functions of height.

3.3.5.3 Mesh Initialization

The entire computer mesh in Fig. 3.3.5.2 is first initialized with the known atmospheric profiles of virtual potential temperature, eddy viscosity, turbulence kinetic energy, water vapor density, and cloud liquid water content. The entire mesh is initialized with a single background value of pollutant, and the velocity field is initialized to be at rest. The plume cells in the figure are then initialized by volume-averaging

Table 3.3.5.2

Boundary Conditions

Variable	Wall#1	Wall #2	Wall #3	Wall #4
y-velocity, v	S	S	F	N
z-velocity, w	F	F	S	S
virtual potential temperature	R	*	R	R
eddy viscosity	R	*	R	R
turbulence kinetic energy	R	*	R	R
pollutant	R	R	R	R
water vapor density	R	*	R	R
liquid water density	R	*	R	R

S--solid wall (normal velocity = 0)

N--no-slip (tangent velocity = 0)

F--free-slip (normal derivative of tangent velocity = 0)

R--reflective (normal derivative = 0)

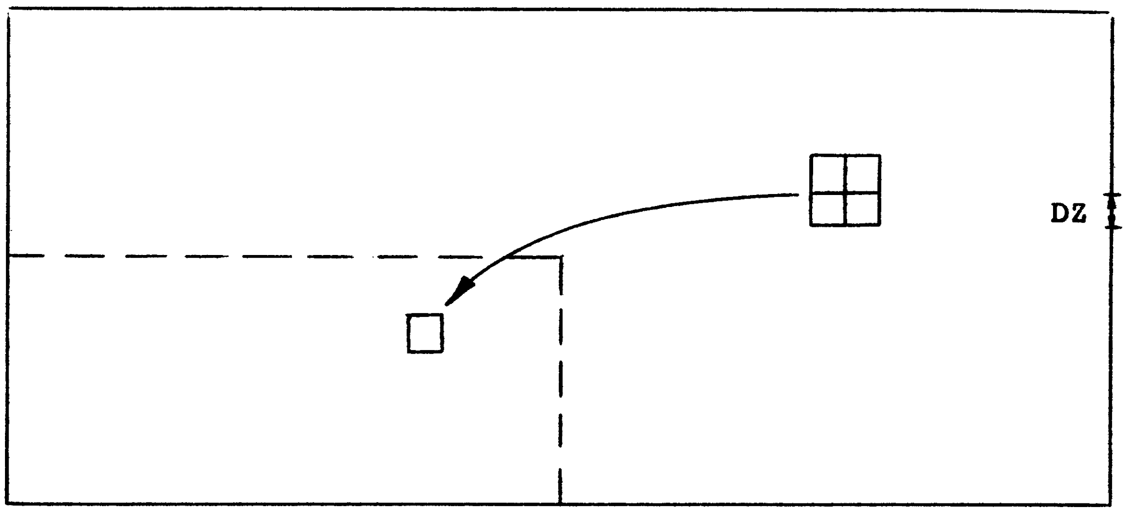
*--specified as profiles of height (z)

the plume sources of energy, pollutant, and moisture over those cells, using mean wind speed at that height to define the depth of the cells swept out in one second. The initial eddy viscosity and turbulence kinetic energy in the plume cells are set to about 100 times that of the surrounding atmosphere--in practice, the plume turbulence values very quickly relax into values that are consistent with the flow field. No initial volume-averaged momentum is given to the plume cells. Instead of this, an effective stack height increment due to momentum is added to the actual stack height in specifying the location of the center of the plume cells.

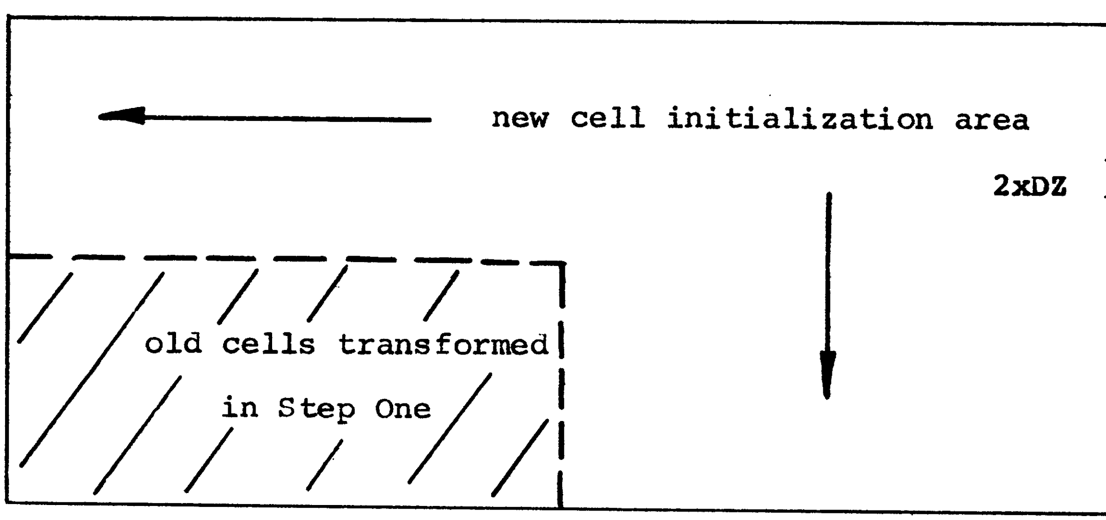
3.3.6 Mesh Coarsening Capability

Model programming has been undertaken to allow the mesh spacing to be doubled periodically during the simulations, while keeping the same number of fluid cells on the whole computer mesh. The motivation for this is the desire to keep the growing plume cross section away from the unphysical (solid wall) top and right mesh boundaries. When the simulation is "coarsened," the mesh spacing doubles, which reduces the plume cross section by a factor of four. The calculation is restarted, and the simulation proceeds on a mesh that has four times the area of the old mesh, but the same number of fluid cells.

The coarsening procedure is outlined in Fig. 3.3.6.1. In



(a) Step One - Four Cell Averaging



(b) Step Two - Initialization of New Cells

Figure 3.3.6.1 Mesh Coarsening Procedure Steps a first step (a) the entire mesh is swept over, four cells at a time. Note that the number of cells vertically or horizontally must be even in order to do this. The fluid variables in these four cells are averaged in the following way: the cell specific internal energy, momenta, and turbulence kinetic energy are mass-averaged over the four cells, since these variables are defined on a per unit mass of air basis. The cell pollutant, eddy viscosity, and moisture variables are simply averaged over the four cells, since these variables are not defined on a per unit mass of air basis. The cell pressure is set to zero, which conforms with the usual starting guess procedures in running VARR-II. The average cell made up from these four cells is now stored in its proper place on the larger mesh, which is half of the distance to the origin vertically and horizontally. When the entire mesh has been swept, four cells at a time, the old mesh has now been relocated in the lower left corner, and is one-fourth of its old size.

In a second step (b) the remaining three-quarters of the mesh needs to be initialized. This "new" area is swept row-by-row in ascending order. The velocity field is assumed to be initially at rest, and the pressure field is initially set to zero. The remaining atmospheric state variables are all specified from a master library of profiles. When the "new" area has been initialized, the calculation is restarted with the vertical and horizontal mesh spacings doubled.

The computer mesh may be coarsened up to five times during a simulation--this would result in a final mesh that is $2^5 \times 2^5 = 1024$ times as large as the original mesh. The five times are user specified, and need not take place at regular intervals.

3.3.7 Plume Statistics Package

At regular intervals specified by the user, the program calls on a statistics package to calculate a number of important plume statistics without printing out the data of the entire computer mesh. The quantities that are reported by the statistics package are listed in Table 3.3.7.1. The average plume advection velocity is the feature discussed in Sec. 3.3.3, and is defined in Eq. 3.96.

Table 3.3.7.1

Data Reported by the Plume Statistics Package

Quantity	Units
Time of Simulation	sec
Total Number of Problem Iterations	(none)
Current Number of Pressure Iterations	(none)
Current Time Step Size	sec
Center Height of Pollutant Field	ft
Total Specific Internal Energy on Mesh	BTU
Average Downwind Advection Velocity	ft/sec
Plume Downwind Distance	ft

4. DESCRIPTION OF ATMOSPHERIC TURBULENCE

4.1 Introduction

This chapter describes in detail how atmospheric turbulence is represented in the model. The description begins with the knowledge (e.g., from a set of measurements) of the common atmospheric variables as functions of height: the set includes the wind speed and direction, virtual potential temperature, water vapor density, and cloud liquid water density. The important processes that are responsible for the characteristic shapes of these profiles are outlined, and the concept of layers in the atmosphere arises naturally in the explanation of the interdependencies of the profiles. With a working knowledge of the dominant phenomena in the atmospheric layers, the problem of prescribing the atmospheric turbulence is undertaken. For the model in this work, the atmospheric turbulence is specified with profiles of eddy viscosity and turbulence kinetic energy. The relation of these two variables to the other profiles, and their inclusion into the model occupies most of this chapter.

4.2 Atmospheric Profiles of Wind, Temperature, and Humidity

The vertical atmospheric profiles considered in this work are assumed to have been measured with some appropriate meteorological instruments over a flat terrain. For instance, a tower with a series of instruments at various heights would produce essentially pointwise values of the variables, which could then be linearly interpolated between the measurement heights to produce the full profiles. It is assumed that the measurements were time-averaged for at least 20 minutes so that there is very little time-dependence in the profiles. Alternatively, a radiosonde (balloon) ascent is commonly used for measuring vertical profiles, although the measurement averaging times are not long enough to completely average over the larger atmospheric eddies.

The measured atmospheric wind profiles have several common features. First, the atmospheric wind vanishes at the ground. This is in accord with the no-slip velocity boundary condition of real fluids. Second, the time-averaged (i.e., averaged over about 20 minutes) vertical velocity is very small at any height. This is because the very low frequency (of the order of 1 per day) vertical velocities are due to the synoptic scale subsiding or lifting motions associated with fronts; these velocities are usually only about 10 cm/sec. Because the average vertical velocities are small, the wind at any height is assumed to be parallel to the ground. Generally, the wind speed increases with height and commonly exhibits some turning with height--

especially in the first several hundred feet of elevation, where pressure gradient, Coriolis, and frictional forces are all important.

The fact that the wind vector may very roughly approximate a logarithmic profile,[44] an Ekman spiral,[45] or a thermal wind relation,[46] is only of minor interest here since the actual wind profile determines the behavior of an individual plume. In this work, the turning of the wind with height is not represented in the hydrodynamic simulations, although the prospect of including it is considered among the extensions of the model outlined in Sec. 6.2. Also, the difficulty of defining an average wind direction when there are only light, variable winds at a station dictates that the computer simulations are not expected to be accurate for winds of less than about 5 knots.

The temperature and humidity profiles directly provide the information about the local stability of vertical atmospheric and plume motions. No approximations to the temperature or humidity profiles are needed to incorporate them into the simulations. The temperature and humidity profiles are used to evaluate the virtual potential temperature profile: Note that in defining equations for virtual potential temperature (Eq. 3.53 and Eq. 3.67) the temperature, humidity, and pressure are required at any height. To this end the pressure profile could have been measured by itself, or calculated with any of a number of approximations (dry hydrostatic, moist hydrostatic, various interpolations between points, etc.) Whatever assumptions are made, the pressure profile consistent with these assumptions must be input to the simulation where it is used to recalculate the correct temperature from the virtual potential temperature and humidity for the equilibrium moisture thermodynamics model.

4.3 Turbulence in the Planetary Boundary Layer

4.3.1 Introduction

The planetary boundary layer (PBL) is a boundary layer in a rotating, stratified, multi-component fluid whose moisture component can undergo changes of phase. Further, the boundary conditions on fluxes of momentum, sensible and latent heats, and radiant energy can vary greatly over large and small distances (i.e., distances that are large or small in comparison to the depth of the boundary layer), and are typically strongly coupled to the flow. Although a number of excellent reviews have been written[47-57] at many levels of detail, the basic notions of turbulence in the planetary boundary layer are developed here with the aim of pointing out the limitations of the description of the PBL turbulence embodied in the computer simulations.

4.3.2 Layers in the PBL and Important Processes

Without much loss in generality, it is assumed in this work that all of the energy in turbulent atmospheric motions ultimately comes from the sun. Although it is possible to conceive of special situations where this is not quite true (for example, the turbulence near a busy expressway, much of which is caused by mechanical stirring and buoyant exhausts), the atmopsheres which are encountered in this work are free of man-made turbulence, except for the buoyant plumes themselves! For the purposes of illustration, the solar energy which produces atmospheric turublence may be divided into two streams: (1) that part of the solar energy that produces the large synoptic-scale pressure patterns on the earth, which in turn drives the wind and produces turbulence in regions of the atmosphere of sufficiently large wind shear, and (2) that part of the solar energy that produces the local thermal stratification of the atmopshere, which in turn produces turbulence in regions of sufficiently unstable stratification. The turbulence that is produced by the first stream is called "mechanically produced turbulence," and that produced by the second stream is called "buoyancy produced turbulence." The thermal stratification that is produced by the second stream is usually formulated in terms of virtual potential temperature, so that moisture and latent heat effects are naturally included in the "buoyancy produced turbulence." There are two mechanisms that destroy atmospheric turbulence: (1) viscous dissipation, which is always at work in a turbulent flow, and (2) buoyant destruction, which is present in regions of stable thermal stratification.

From the preceding discussion it is expected that in a region in steady state the mechanisms of turbulence production and destruction will be balanced, and that the turbulence kinetic energy will maintain a value that is commensurate with the destruction rate. Very commonly in micrometeorological studies, the regions that these processes are studied in are simplified to layers, so that the description of atmospheric turbulence becomes one-dimensional--the single dimension is then height. The situation is illustrated in Fig. 4.3.2.1. In the uppermost layer of laminar flow, the strong geostrophic winds usually have very small wind shears with height, and are usually associated with stably stratified air, so that there is little or no turbulence. The next layer down usually is a region of buoyancy produced turbulence with only small wind shear--the buoyancy is typically from solar heating at the ground and latent heat release in cloud formation (clouds obviously affect the amount of solar heating at the ground, so that these effects are strongly coupled). The layer nearest

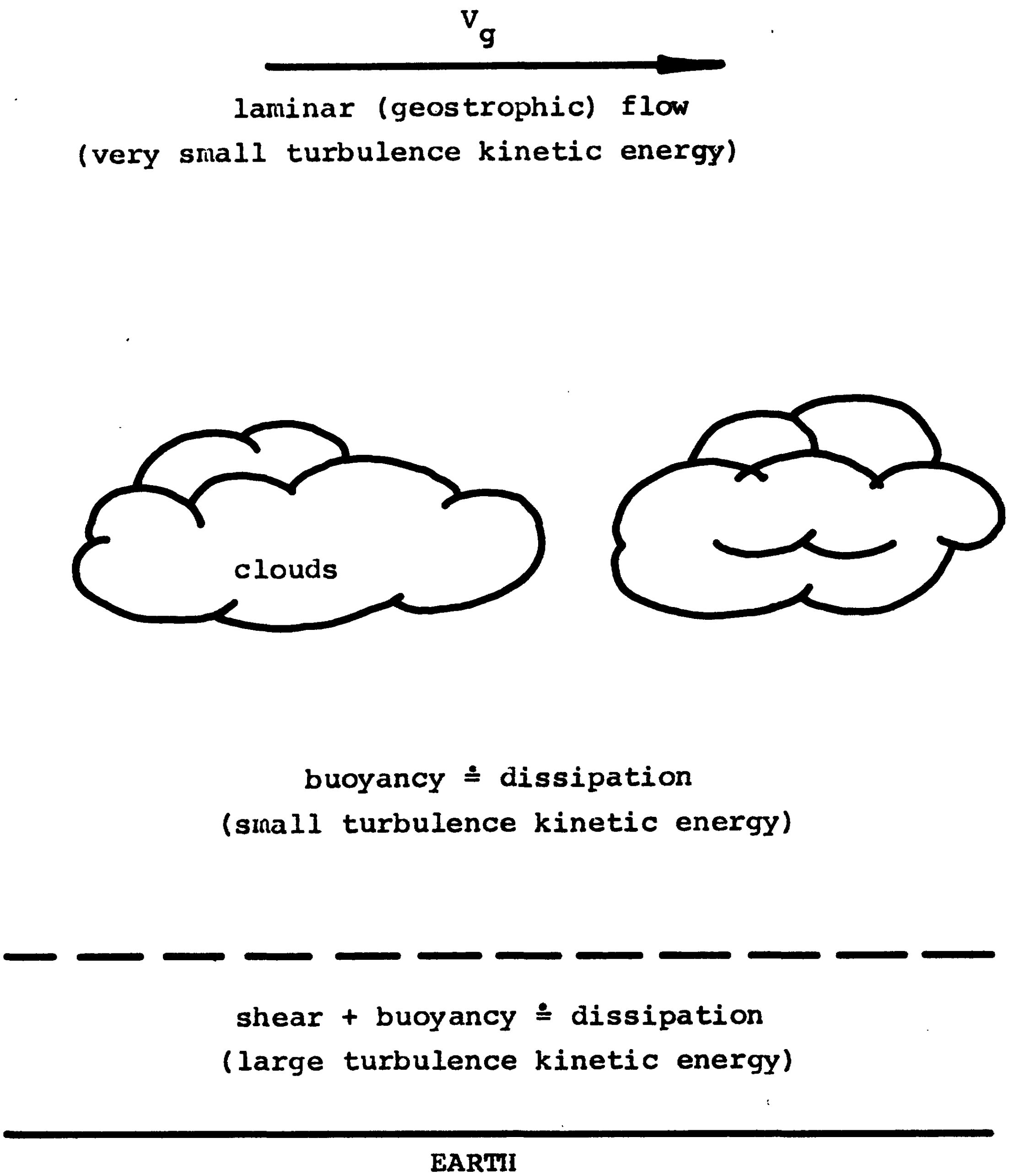


Fig. 4.3.2.1 The Concept of Layers in the Planetary Boundary Layer. Atmospheric turbulence is assumed to be variable in one-dimension only in this figure. The turbulence is steady-state.

to the ground typically exhibits a lot of wind shear due to the no-slip condition at the ground, so that mechanically produced turbulence is present in addition to buoyant production, and turbulence kinetic energy is usually a maximum somewhere in this layer.

The particular illustration of atmospheric layers in Fig. 4.3.2.1 is certainly not unique. Many investigators have coined names for layers to illustrate different refinements on the processes in the PBL. Such terms as the surface layer, Ekman layer, subcloud layer, cloud layer, inner layer, outer layer, tower layer, convection layer, inversion layer, superadiabatic layer, and viscous sublayer are common, but they do not represent anything more sophisticated than treating the atmosphere as one-dimensional.

The prospect of treating the atmospheric state as two-dimensional--now including its downwind development as well as its profile with height--is considered in Sec. 5.4.1 in conjunction with the modeling of a fumigation episode.

4.3.3 Prescription of the Eddy Viscosity

The prescription of the eddy viscosity in the two-dimensional mesh of the crosswind alignment scheme of Fig. 3.3.2.1c is considered in this section. It was mentioned in Sec. 3.3.2

that the absence of any mean wind component (by definition) in the crosswind direction means that, away from the plume, and as far as the computer simulation is concerned, there is no explicit mechanical production of turbulence in the atmosphere. In fact, what takes place in the atmosphere is that the turbulence kinetic energy component, $\overline{u'^2}$, and the Reynolds stress, $\overline{u'w'}$, of the downwind x-z plane are feeding into the crosswind y-z plane turbulence kinetic energy component, $\overline{v'^2}$, and Reynolds stress, $\overline{v'w'}$, through the return to isotropy term in Eq. 3.40. For this work, the assumption is made that the return to isotropy term is very strong, so that the turbulence is <u>isotropic</u>. Experiments on atmospheric return to isotropy indicate that this assumption is reasonably good.[58] It is seen in the discussion of the results in Chapter Five that this is probably the most limiting assumption in the work with regard to being able to model real atmospheres. The eddy viscosity as a function of height in the downwind x-z plane is estimated from a number of prescriptions for eddy viscosity that are correlated from mean wind and temperature profiles, then the eddy viscosity in the crosswind y-z plane is assumed to be the same as in the x-z plane under the assumption of isotropy.

The incorporation of an ambient eddy viscosity profile on the simulation mesh finds two problems. First, any arbitrary eddy viscosity imposed on the mesh cells at the start of the simulation will, in the absence of sufficient mechanical and buoyant production, rapidly decay down to the molecular kinematic viscosity. Second, the turbulence field inside the plume must be allowed to develop on its own. The method of incorporating the ambient eddy viscosity profile in light of these problems is as follows: to start the simulation, the cells outside of the initial plume cells are initialized with the eddy viscosity profile, depending on their height in the mesh. After each time step, each cell on the mesh is tested to see if it has fallen below the prescribed eddy viscosity profile at its height. If it has, its eddy viscosity is simply reset to the ambient value. If it has not fallen below the ambient value, presumably because either the plume-induced turbulence or the turbulently diffused turbulence from neighboring cells is dominating, then the cell eddy viscosity value is left alone. In this way, the far field always maintains the ambient atmospheric turbulence values, and the plume turbulence, if greater than the ambient turbulence, is left to develop on its own. Overall, this method has the effect of adding a non-uniform source term to the eddy viscosity equation--the term always adjusts itself to yield the original eddy viscosity in the far field, and to "turn itself off" if the plume turbulence is dominating. Mathematically, the inequality

$$\sigma(y,z,t) \geq \sigma_{library}(z) \qquad (4.1)$$

has been added to the equation set, where $\sigma_{libary}(z)$ is the prescribed eddy viscosity profile as a function of height.

Before discussing the available prescriptions of eddy viscosity, it should be noted that the potentially most accurate method of prescribing the eddy viscosity for an individual release would be to actually measure it in the field--perhaps simply by estimating it from bivane wind fluctuation data. The effort in this work to arrive at workable prescriptions from the micrometeorological literature is motivated by the total absence of these measurements in existing plume field data. The particular prescriptions that are recommended here are used only because they offer a simple way to estimate the eddy viscosity profile.

A number of prescriptions for the eddy viscosity in the outer boundary layer of the atmosphere as a function of height have been reviewed.[59-64] A summary of the various prescriptions is presented in Table 4.3.3.1, where they are separated into two major groups--those that require wind speed and direction profiles, and those that do not. Those which do not require wind profiles as input are easier to use because the wind profiles need not be measured (e.g., with instrumented towers or

Table 4.3.3.1 Comparison of Eddy Viscosity Prescriptions

Author(s)	Atmospheric Stability in which the Prescription is Applicable		
	Neutral	Stable	Unstable
* * Prescriptions that require wind speed and direction versus height:			
Blackadar[59]	yes	no	no
Blackadar and Ching[60]	no	no	yes
Yamamoto and Shimanuki[61]	yes	yes	yes
Nieuwstadt[64]	yes	yes	yes
Prescriptions that do not require wind profiles:			
O'Brien[62]	yes	yes	yes
Bornstein[63]	yes	yes	yes

balloons). However, they are not expected to be as accurate, since the wind profile has taken an ideal shape. All of the models in Table 4.3.3.1 are searched for applicability to neutral, stable, and unstable atmospheres.

It is recommended that if the wind speed and direction profiles have been measured, the prescriptions of Blackadar,[59,60] and Yamamoto and Shimanuki[61] should be used. If the wind speed and direction profiles have not been measured, the prescriptions of Bornstein[63] or O'Brien[62] should be used. The prescription of Nieuwstadt[64] requires a substantial numerical analysis of the profiles and has not been tested.

Any of these prescriptions must be used with caution since all of them are only capable of providing an estimate to the eddy viscosity. The greatest difficulty in using these prescriptions is that they typically require values for quantities that were not measured, such as the heat flux at the ground, the roughness height, geostrophic velocity, etc.

4.3.4 Prescription of the Turbulence Kinetic Energy

The prescription of the turbulence kinetic energy (TKE) in the two-dimensional mesh of the crosswind alignment scheme of Fig. 3.3.2.1c is considered in this section. The turbulence kinetic energy suffers from exactly the same problem as the eddy viscosity in Sec. 4.3.3.: in the absence of explicit buoyant and mechanical production of turbulence on the two-dimensional mesh, the turbulence kinetic energy would gradually decay away entirely. To satisfactorily avoid this problem, the concept of the turbulent "return to isotropy" is again invoked to allow the turbulent kinetic energy produced by the mean flow shearing and buoyancy to be fed into the crosswind motions. A turbulence kinetic energy profile is needed, so that it may maintain the turbulence for mesh cells that lack the sufficient turbulence production in exactly the same way that an eddy viscosity profile maintains the eddy viscosity for the mesh.

Ideally, the TKE profile should be measured or deduced from other profiles for an actual atmosphere. In fact, however, prescriptions for the turbulence kinetic energy from mean wind and temperature profiles are not generally available in the literature. The actual prescription of the turbulence kinetic energy profile in this work has had to come from the following, very approximate analysis of the transport equations.

Consider the TKE transport equation in a region away from the plume. The vertical and horizontal velocities, v and w, are zero, and the eddy viscosity, σ, and TKE, q, are functions of height, z, only; with the resulting expression being

$$\frac{\partial q}{\partial t} = \frac{-4\alpha q^2}{\sigma} + \Gamma \frac{\partial}{\partial z} \left(\sigma \frac{\partial q}{z}\right) \tag{4.2}$$

For a properly time-independent TKE, there must be a balance of dissipation and diffusion in Eq. 4.2; or

$$\frac{4\alpha q^2}{\sigma} = \Gamma \frac{\partial}{\partial z} \left(\sigma \frac{\partial q}{\partial z}\right) \tag{4.3}$$

Performing a scale analysis of the terms, noting that $\Gamma/4\alpha \cong 10$ and that the depth of the planetary boundary layer is taken equal to L_{eddy}, one obtains the result

$$q \sim 10 \frac{\sigma^2}{L^2_{eddy}} \tag{4.4}$$

For typical values in the atmosphere, $\sigma \sim 100$ ft^2/sec and $L_{eddy} \sim 10^3$ft, giving the value

$$\frac{q}{\sigma} \sim 10^{-3} \text{ sec}^{-1} . \tag{4.5}$$

Note that for a highly idealized picture of turbulence,[65] with eddies of a single size, L_{eddy}, and velocity, u_{eddy},

$$q \sim u^2_{eddy} , \tag{4.6}$$

$$\sigma \sim u_{eddy} L_{eddy} , \tag{4.7}$$

and therefore

$$\frac{q}{\sigma} \sim \frac{u_{eddy}}{L_{eddy}} \quad [\text{sec}^{-1}] . \tag{4.8}$$

This states that q/σ is simply the inverse of the eddy turnover time. The scale analysis (Eq. 4.5) of the q transport equation shows that the choice $q \sim 10^{-3} \sec^{-1} \sigma$ should roughly allow q to have a constant value. The fact that this choice of q agrees with the eddy turnover time of roughly the most diffusive atmospheric eddies[66] (10^3 seconds, or about 15 minutes) lends support to the idea that σ and q have been chosen consistently in this scheme.

The crude specification of $q_{library}(z)$ has been found to be satisfactory in this work primarily because the turbulence kinetic energy only indirectly influences the eddy viscosity, so that errors in estimating TKE are tolerated much more than the errors in estimating the eddy viscosity. The preceding analysis, since it is a scale analysis, only provides a very approximate estimate of the turbulence kinetic energy profile. Mathematically, the inequality

$$q(y,z,t) > q_{library}(z) = 10^{-3} \sec^{-1} \sigma_{library}(z) \quad (4.9)$$

has been added to the equation set, where $q_{library}(z)$ is the prescribed turbulence kinetic energy profile as a function of height.

5. CARD INPUT AND SAMPLE PROBLEMS

The VARR-II[40] computer code has been modified for the modeling of buoyant plumes in turbulent, stratified atmospheres. This chapter is intended to illustrate the use of the modified code for users that are already familiar with the VARR-II code. Users that are not familiar with VARR-II should consult the VARR-II Users' Guide.[40] All users should note that a previous alteration[68] of the VARR-II code from CDC to IBM machines has removed the extensive film plotting routines (Sec. III.C in the VARR-II Users' Guide), and has also removed the packing of the cell flag index (Sec. III.F). The current modifications have not updated the program tape dump and restart capability (Sec. III.D), although this could be re-established with a minimal amount of programming.

The remainder of this chapter will discuss the alterations to the input data cards found in Sec. III.B of the VARR-II Users' Guide[40], and then several numerical examples are presented.

5.1 Overall Program Support

The modified program has a moderately larger storage requirement than the previous code, but the program support devices are the same. The code now stores 25 variables for each fluid cell (real or imaginary), where the previous code only stored 19. In the current version, the total program storage for a 20 x 20 (real) cell mesh is about 175K bytes of CPU. The program reads input on device 5 in card format (when IVDI=5 in Statement No. 94 in Appendix D), and writes output on device 6 (when IVDØ=6 in Statement No. 95 in Appendix D). Device 6 should be a line printer since nearly the full 120 characters per line are used. Of course, disc, mag tape, or microfiche could be used instead of a line printer.

Running time in CPU is, of course, dependent on the time step size in the problems. The time step size is selected by the program at each time step, and is usually from one-tenth of a second to several seconds. The selection of a time step size is performed by the code.[67] where it always chooses the smallest step size from a choice of a diffusion condition,

$$DT = \frac{TSTEP}{\max(\sigma)\ (\frac{1}{DY^2} + \frac{1}{DZ^2})} , \tag{5.1}$$

a Courant condition,

$$DT = \frac{TSTEP\ \ \min(DY,DZ)}{\max(v,w)} , \tag{5.2}$$

or a simple rate of change condition,

$$\frac{.2\ \max\ (v,w)}{(\max(v,w) - \max\ (v_{old},w_{old}) + 10^{-6}} , \tag{5.3}$$

where TSTEP in the VARR-II Users' Guide has a value of 0.25. As a practical matter, it is found that the time steps have to be reduced beyond these conditions by about a factor of 25 for the mesh cell sizes encountered in this work. This 25-fold reduction is accomplished by giving TSTEP a value of 0.01

(note that Eq. 5.3 is virtually never the most limiting step size). This allows the code to conserve energy in the computer mesh cells within an acceptable tolerance. The nonconservation of energy arises from the first order accuracy of the differencing scheme for the advection terms. Full donor cell differencing of the advection terms is found to give the best answers in the simulations--less than full donor cell differencing produces noticeable nonlinear instabilities in the flow. Running times on the IBM370/168 are usually about 10 to 15 minutes per thousand time steps.

5.2 Card Input Decks

The generation of input decks is considered in detail in the Appendices, where the additional input variables are defined and the detailed card formats are listed. Many of the input variables are discussed in Section 3.3 and in Chapter 4. To illustrate several different problems, three input decks are listed in the following sections.

5.2.1 The Dry, Buoyant Line-Thermal

Card input for the dry, buoyant line-thermal is listed in Table 5.2.1. Briefly, the problem simulates the rise of an initially quiet, warm parcel of air in a neutrally stratified dry atmosphere. Results from this problem are given as a sample problem in Sec. 5.3.1.

5.2.2 LAPPES[5] Plume of 20 October 1967

Card input for the essentially dry, buoyant plume from the Keystone #1 combustion stack is listed in Table 5.2.2.

Table 5.2.1 Card Input for the Dry, Buoyant Line-Thermal

```
      20         20         1                                                                0001
 CROSSWIND RECKONING--NEUTRAL LAYER, LAMINAR ATMOSPHERE                                      0002
   0.01     10.0      5.0    800.0   80.00 8 1 0 3 1  4 10                                   0003
 100.00   200.00      0.   .-32.2      1.0      1.0      0.0     1.60  -0.001      10.0      0004
1 1 1 1     -1.0    0.045   1.50                0.75 .00015  0.0009360.00013                 0005
  2.44     4.9      3.       0.01  0                                    0.0                  0006
   0.00     0.00     1.48                                                                    0007
    1.0     50.0     50.0    0.010 3  1                                                      0008
.0000043.1707      78.357.0000002-.000178.086394 -.000001.001916 1.0932                      0009
   0.     .0000259.013129    0.    -.000002.24008      1.0                                   0010
      -2         2        2        0        0         0         1                            0011
    0.0     30.0    800.0     30.0                                                           0012
    0.0     50.0    800.0     50.0                                                           0013
    0.0      1.0    800.0      1.0                                                           0014
10000.0                                                                                      0015
    0                                                                                        0016
    0                                                                                        0017
    0                                                                                        0018
    0                                                                                        0019
    0                                                                                        0020
    0                                                                                        0021
    0                                                                                        0022
   2   21     2   21 1                                                                       0023
86.9028   0.001      1.0      0.0      0.0 0.00001.0000001.0000001                           0024
   2     2    4     4 1                                                                      0025
90.0000   100.0    100.0      0.0      0.0    1.00.0000001.0000001                           0026
    0                                                                                        0027
   1.00        2     29.0     1.00     1.00                                                  0028
   0.00     1.00     1.00                                                                    0029
   0.00     1.00     1.00                                                                    0030
     20    800.0    800.0    800.0    800.0   800.0                                          0031
86.9028    0.001      1.0                    1000.00     1.00                                0032
86.9028    0.001      1.0                    1000.00     1.00                                0033
86.9028    0.001      1.0                    1000.00     1.00                                0034
86.9028    0.001      1.0                    1000.00     1.00                                0035
86.9028    0.001      1.0                    1000.00     1.00                                0036
                                                                                      PAGE   1
```

of Table 5.2.1

Table 5.2.1 Card Input for the Dry, Buoyant Line-Thermal (Continued)

86.9028	0.001	1.0	1000.00	1.00	0037
86.9028	0.001	1.0	1000.00	1.00	0038
86.9028	0.001	1.0	1000.00	1.00	0039
86.9028	0.001	1.0	1000.00	1.00	0040
86.9028	0.001	1.0	1000.00	1.00	0041
86.9028	0.001	1.0	1000.00	1.00	0042
86.9028	0.001	1.0	1000.00	1.00	0043
86.9028	0.001	1.0	1000.00	1.00	0044
86.9028	0.001	1.0	1000.00	1.00	0045
86.9028	0.001	1.0	1000.00	1.00	0046
86.9028	0.001	1.0	1000.00	1.00	0047
86.9028	0.001	1.0	1000.00	1.00	0048
86.9028	0.001	1.0	1000.00	1.00	0049
86.9028	0.001	1.0	1000.00	1.00	0050
86.9028	0.001	1.0	1000.00	1.00	0051
-1					0052

Table 5.2.2 Card Input for the LAPPES[5] Plume of 20 October 1967.

```
     20          20         1                                                      0001
  KEYSTONE PLANT #1--BLACKADAR TURBULENCE VALUES 20 OCT 67                         0002
   0.01   200.0     10.0   1800.0 1250.00 8 1 0 3 1  4 10                          0003
 492.00  164.00     0.    -32.2     1.0      1.0     0.0     1.60  -0.001    10.0  0004
1 1 1 1    -1.0    0.045   1.5               0.75 .00015  0.0009360.00013          0005
  2.44    4.9      3.       0.01  0                                 0.0            0006
   0.00    0.00     1.48                                                           0007
    1.0    50.0    50.0    0.025 3  1                                              0008
.0000043.1707      78.357.0000002-.000178.086394 -.000001.001916 1.0932            0009
  0.    .0000259.013129   0.    -.000002.24008       1.0                           0010
     -2          2        2        0        0        0        1                    0011
    0.0    30.0  1800.0    30.0                                                    0012
    0.0    50.0  1800.0    50.0                                                    0013
    0.0     1.0  1800.0     1.0                                                    0014
 10000.0                                                                           0015
      0                                                                            0016
      0                                                                            0017
      0                                                                            0018
      0                                                                            0019
      0                                                                            0020
      0                                                                            0021
      0                                                                            0022
    1    22     2     2 1                                                          0023
  84.747   0.003     .317     0.00     0.000.005293                                0024
    1    22     3     3 1                                                          0025
  84.952   0.010     .985     0.00     0.000.005293                                0026
    1    22     4     4 1                                                          0027
  85.123    .067    6.710     0.00     0.000.005293                                0028
    1    22     5     5 1                                                          0029
  85.277    .021    2.068     0.00     0.000.005293                                0030
    1    22     6     6 1                                                          0031
  85.466   0.002     .181     0.00     0.000.005293                                0032
    1    22     7     7 1                                                          0033
  86.492    .025    2.450     0.00     0.000.005293                                0034
    1    22     8     8 1                                                          0035
  86.663    .016    1.616     0.00     0.000.005293                                0036
```

PAGE 1 of Table 5.2.2

Table 5.2.2 Card Input for the LAPPES[5] Plume of 20 October 1967 (Continued)

```
   1    22      9      9  1                                                  0037
 86.766     3.134  313.392    0.00      0.000.005293                         0038
   1    22     10     10  1                                                  0039
 86.886     2.741  274.085    0.00      0.000.005293                         0040
   1    22     11     11  1                                                  0041
 86.971     0.371   37.067    0.00      0.000.005293                         0042
   1    22     12     12  1                                                  0043
 87.005     0.637   63.653    0.00      0.000.005293                         0044
   1    22     13     13  1                                                  0045
 87.023     0.849   84.853    0.00      0.000.005293                         0046
   1    22     14     14  1                                                  0047
 86.988     1.334  133.367    0.00      0.000.005293                         0048
   1    22     15     15  1                                                  0049
 87.023     0.883   88.304    0.00      0.000.005293                         0050
   1    22     16     16  1                                                  0051
 87.074     1.173  117.346    0.00      0.000.005293                         0052
   1    22     17     17  1                                                  0053
 87.108     0.420   42.005    0.00      0.000.005293                         0054
   1    22     18     18  1                                                  0055
 87.040     0.425   42.535    0.00      0.000.005293                         0056
   1    22     19     19  1                                                  0057
 87.074     2.151  215.066    0.00      0.000.005293                         0058
   1    22     20     20  1                                                  0059
 87.091     2.824  282.405    0.00      0.000.005293                         0060
   1    22     21     21  1                                                  0061
 87.194     0.219   21.921    0.00      0.000.005293                         0062
   2     2      6      6  1                                                  0063
85.5511     100.0    100.0    0.00      0.00      0.23                       0064
   2     2      7      7  1                                                  0065
86.5776     100.0    100.0    0.00      0.00      0.23                       0066
   2     2      8      8  1                                                  0067
86.7487     100.0    100.0    0.00      0.00      0.23                       0068
   0                                                                         0069
   1.00         2     29.0    1.00      1.00 .005293      0.00               0070
   0.00      1.00     1.00                                                   0071
   0.00      1.00     1.00                                                   0072
```

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of Table 5.2.2

Table 5.2.2 Card Input for the LAPPES[5] Plume of 20 October 1967 (Continued)

20	1800.0	1800.0	1800.0	1800.0	1800.0		0073
84.747	0.003	.317.0000001		0.00	1000.0	2.5	0074
84.952	0.010	.985.0000001		0.00	1000.0	4.9	0075
85.123	.067	6.710.0000001		0.00	1000.0	20.7	0076
85.277	.021	2.068.0000001		0.00	1000.0	28.9	0077
85.466	0.002	.181.0000001		0.00	1000.0	26.4	0078
86.492	.025	2.450.0000001		0.00	1000.0	29.1	0079
86.663	.016	1.616.0000001		0.00	1000.0	33.0	0080
86.766	3.134	313.392.0000001		0.00	1000.0	37.3	0081
86.886	2.741	274.085.0000001		0.00	1000.0	42.3	0082
86.971	0.371	37.067.0000001		0.00	1000.0	44.3	0083
87.005	0.637	63.653.0000001		0.00	1000.0	43.5	0084
87.023	0.849	84.853.0000001		0.00	1000.0	42.4	0085
86.988	1.334	133.367.0000001		0.00	1000.0	40.7	0086
87.023	0.883	88.304.0000001		0.00	1000.0	39.1	0087
87.074	1.173	117.346.0000001		0.00	1000.0	37.6	0088
87.108	0.420	42.005.0000001		0.00	1000.0	36.4	0089
87.040	0.425	42.535.0000001		0.00	1000.0	36.4	0090
87.074	2.151	215.066.0000001		0.00	1000.0	38.2	0091
87.091	2.824	282.405.0000001		0.00	1000.0	37.8	0092
87.194	0.219	21.921.0000001		0.00	1000.0	36.0	0093
-1							0094

Briefly, the problem simulates the behavior of the plume emanating from an 800 ft tall stack at about 7 A.M. Eastern Time. The plume and ambient weather were documented in the LAPPES study[5] (Volume 2). Results from this problem are presented as a sample problem in Sec. 5.3.2. This input deck is included to illustrate the input of a pollutant (here SO_2 in gm/ft^3), and to illustrate the input of available wind speed and temperature profiles, and the inclusion of ambient atmospheric turbulence profiles. The ambient turbulence in the neutral layer (above 350 m elevation) is calculated from Blackadar's prescription.[59] The ambient turbulence in the stable layer (below 350 m elevation) is simply Blackadar's prescription[59] suppressed by a factor of 100 to make a rough account of the suppression of the turbulence by the stable stratification. Comparisons between the numerical simulations and the LAPPES experiments are found in MIT-EL 79-002.

5.2.3 Moist, Buoyant Line-Thermal

Card input for the moist, buoyant line-thermal is listed in Table 5.2.3. Briefly, the problem simulates the rise of a very nearly saturated warm parcel of air in a cool environment. As the parcel begins to rise, its temperature falls rapidly and moisture begins to condense within a few seconds. This input deck is included to illustrate the input of moisture

Table 5.2.3 Card Input for the Moist, Buoyant Line-Thermal

```
       20         20         1                                                                      0001
 BOGUS ATMOSPHERE--MOISTURE CHECKOUT                                                                0002
.00001     4.00       5.0     800.0   300.00 8  1  0  3  1   4  10                                  0003
 100.00  100.00       0.     -32.2       1.0      1.0      0.0      1.60  -0.001      10.0          0004
1 1 1 1    -1.0     0.045     1.5                0.75 .00015  0.0009360.00013                       0005
  2.44     4.9      3.       0.01   0                                     0.0                       0006
   0.00    0.00      1.48                                                                           0007
    1.0    30.0      30.0   0.0001 3  1                                                             0008
.0000043.1707      78.357.0000002-.000178.086394 -.000001.001916 1.0932                             0009
  0.     .0000259.013129     0.     -.000002.24008       1.0                                        0010
       -2         2         2         0         0         0         1                               0011
    0.0    30.0     800.0     30.0                                                                  0012
    0.0    50.0     800.0     50.0                                                                  0013
    0.0     1.0     800.0      1.0                                                                  0014
10000.0                                                                                             0015
    0                                                                                               0016
    0                                                                                               0017
    0                                                                                               0018
    0                                                                                               0019
    0                                                                                               0020
    0                                                                                               0021
    0                                                                                               0022
   2    21      2     21 1                                                                          0023
83.4819   0.001       1.0      0.0       0.0 0.00001.0001720     0.00                               0024
   2     2      4     5 1                                                                           0025
90.3271   100.0     100.0      0.0       0.0 0.00001.000914      0.00                               0026
    0                                                                                               0027
   1.00       2      29.0     1.00      1.00                                                        0028
   0.00    1.00      1.00                                                                           0029
   0.00    1.00      1.00                                                                           0030
     20   800.0     800.0    800.0     800.0    800.0                                               0031
86.9028   0.001       1.0                      1000.0                                               0032
86.9028   0.001       1.0                       995.0                                               0033
86.9028   0.001       1.0                       990.0                                               0034
86.9028   0.001       1.0                       985.0                                               0035
86.9028   0.001       1.0                       980.0                                               0036
```

PAGE 1
of Table 5.2.3

Table 5.2.3 Card Input for the Moist, Buoyant Line-Thermal (Continued)

86.9028	0.001	1.0	975.0	0037
86.9028	0.001	1.0	970.0	0038
86.9028	0.001	1.0	965.0	0039
86.9028	0.001	1.0	960.0	0040
86.9028	0.001	1.0	955.0	0041
86.9028	0.001	1.0	950.0	0042
86.9028	0.001	1.0	945.0	0043
86.9028	0.001	1.0	940.0	0044
86.9028	0.001	1.0	935.0	0045
86.9028	0.001	1.0	930.0	0046
86.9028	0.001	1.0	925.0	0047
86.9028	0.001	1.0	920.0	0048
86.9028	0.001	1.0	915.0	0049
86.9028	0.001	1.0	910.0	0050
86.9028	0.001	1.0	905.0	0051
-1				0052

variables. Temperatures must now be interpreted as virtual potential temperatures since there is an appreciable amount of moisture in the cells. The absolute pressure profile is not a real profile, but simply is an estimated profile. In practice, the unstable nature of the explicit differencing of the moisture model imposes a very small time step on the problem (about 100 times smaller than usual). Results from this calculation are not given as a sample problem because of this restriction.

5.3 Sample Problem Results

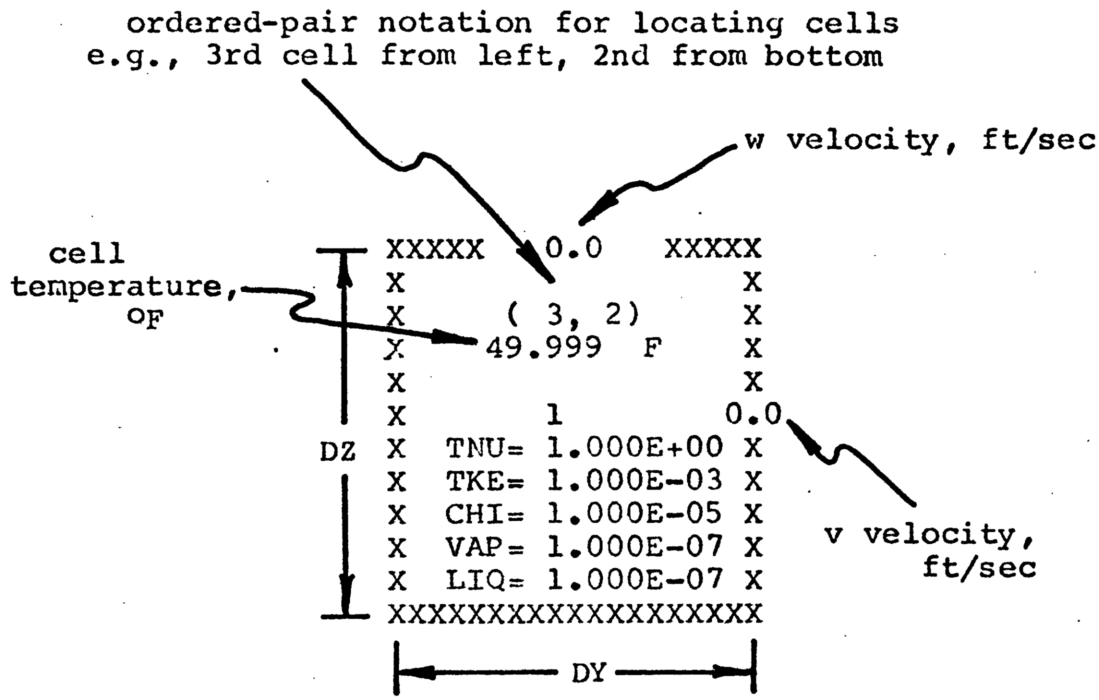
The interpretation of the sample problem output listing is illustrated in Fig. 5.3.1. Each box in the figures that follow Fig. 5.3.1 represents an individual fluid cell. A map of the entire mesh cell storage is produced by the VRPRT subroutine. Only a small region of the entire problem is found in each of the figures--the figures are roughly centered on the regions of strongest flow.

5.3.1 The Dry, Buoyant Line-Thermal

Results from the dry, buoyant line-thermal are presented in Figures 5.3.2 to 5.3.5. The moisture values may be disregarded in the figures. A further discussion of the results is found in MIT-EL 79-002.

5.3.2 LAPPES[5] Plume of 20 October 1967

Results from the tall stack of the Keystone plant are presented in Fig. 5.3.6. Only the mesh cells at the beginning of the simulation are shown. The plume several kilometers downwind extends over many cells and is discussed further in MIT-EL 79-002.



TNU is eddy viscosity in ft^2/sec

TKE is turbulence kinetic energy in ft^2/sec^2

CHI is pollutant concentration in lbm/ft^3

VAP is water vapor density in lbm H_2O/ft^3

LIQ is liquid water density in lbm H_2O/ft^3

Fig. 5.3.1. Key to Cellwise Quantities for Figs. 5.3.2, 5.3.3, 5.3.4, 5.3.5, and 5.3.6.

```
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 8)      X   ( 3, 8)      X   ( 4, 8)      X   ( 5, 8)      X   ( 6, 8)      X
X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 7)      X   ( 3, 7)      X   ( 4, 7)      X   ( 5, 7)      X   ( 6, 7)      X
X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 6)      X   ( 3, 6)      X   ( 4, 6)      X   ( 5, 6)      X   ( 6, 6)      X
X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 5)      X   ( 3, 5)      X   ( 4, 5)      X   ( 5, 5)      X   ( 6, 5)      X
X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 4)      X   ( 3, 4)      X   ( 4, 4)      X   ( 5, 4)      X   ( 6, 4)      X
X   68.088  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+02 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E+02 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E+00 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 3)      X   ( 3, 3)      X   ( 4, 3)      X   ( 5, 3)      X   ( 6, 3)      X
X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
X                X                X                X                X                X
X   ( 2, 2)      X   ( 3, 2)      X   ( 4, 2)      X   ( 5, 2)      X   ( 6, 2)      X
X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X   49.999  F    X
X                X                X                X                X                X
O     1     0.0      1     0.0      1     0.0      1     0.0      1     0.0
X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X TNU= 1.000E+00 X
X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X TKE= 1.000E-03 X
X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X CHI= 1.000E-05 X
X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X VAP= 1.000E-07 X
X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X LIQ= 1.000E-07 X
XXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXXXXXX  0.0  XXXXX
```

Fig. 5.3.2. Initialized Plume Cross Section at 0 sec.
DY = 100 ft, DZ = 200 ft.
Disregard moisture values.

```
XXXXX   0.215 XXXXXXXXX   0.107 XXXXXXXXX   0.142 XXXXXXXXX   0.073 XXXXXXXXX   0.041 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 8)       X     ( 3, 8)       X     ( 4, 8)       X     ( 5, 8)       X     ( 6, 8)       X
X    49.992  F      X    50.019  F      X    50.137  F      X    49.922  F      X    49.922  F      X
X                   X                   X                   X                   X                   X
O      1       0.073      1       0.120      1       0.148      1       0.121      1       0.126
X  TNU= 1.005E+00 X  TNU= 1.007E+00 X  TNU= 1.005E+00 X  TNU= 1.003E+00 X  TNU= 1.001E+00 X
X  TKE= 1.039E-03 X  TKE= 1.014E-03 X  TKE= 1.009E-03 X  TKE= 1.006E-03 X  TKE= 1.001E-03 X
X  CHI= 1.084E-05 X  CHI= 1.001E-05 X  CHI= 1.000E-05 X  CHI= 9.999E-06 X  CHI= 9.999E-06 X
X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.001E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.348 XXXXXXXXX   0.232 XXXXXXXXX   0.209 XXXXXXXXX   0.005 XXXXXXXXX   0.029 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 7)       X     ( 3, 7)       X     ( 4, 7)       X     ( 5, 7)       X     ( 6, 7)       X
X    50.109  F      X    49.964  F      X    49.957  F      X    49.777  F      X    50.089  F      X
X                   X                   X                   X                   X                   X
O      1       0.209      1       0.294      1       0.277      1       0.254      1       0.218
X  TNU= 1.000E+00 X  TNU= 1.039E+00 X  TNU= 1.024E+00 X  TNU= 1.010E+00 X  TNU= 1.004E+00 X
X  TKE= 7.111E-03 X  TKE= 1.239E-03 X  TKE= 1.050E-03 X  TKE= 1.019E-03 X  TKE= 1.007E-03 X
X  CHI= 2.144E-04 X  CHI= 1.398E-05 X  CHI= 1.004E-05 X  CHI= 9.996E-06 X  CHI= 1.000E-05 X
X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.791 XXXXXXXXX   0.380 XXXXXXXXX   0.150 XXXXXXXXX  -0.045 XXXXXXXXX  -0.028 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 6)       X     ( 3, 6)       X     ( 4, 6)       X     ( 5, 6)       X     ( 6, 6)       X
X    50.172  F      X    49.985  F      X    50.012  F      X    50.040  F      X    50.068  F      X
X                   X                   X                   X                   X                   X
O      1       0.875      1       0.756      1       0.543      1       0.430      1       0.276
X  TNU= 2.255E+00 X  TNU= 1.018E+00 X  TNU= 1.047E+00 X  TNU= 1.028E+00 X  TNU= 1.027E+00 X
X  TKE= 3.841E-01 X  TKE= 1.945E-02 X  TKE= 1.626E-03 X  TKE= 1.061E-03 X  TKE= 1.052E-03 X
X  CHI= 1.611E-02 X  CHI= 5.960E-04 X  CHI= 2.124E-05 X  CHI= 1.012E-05 X  CHI= 1.000E-05 X
X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   2.530 XXXXXXXXX   0.153 XXXXXXXXX  -0.260 XXXXXXXXX  -0.266 XXXXXXXXX  -0.345 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 5)       X     ( 3, 5)       X     ( 4, 5)       X     ( 5, 5)       X     ( 6, 5)       X
X    54.088  F      X    50.324  F      X    50.061  F      X    50.234  F      X    49.888  F      X
X                   X                   X                   X                   X                   X
O      1       2.009      1       1.302      1       0.711      1       0.392      1       0.180
X  TNU= 1.840E+01 X  TNU= 3.753E+00 X  TNU= 1.141E+00 X  TNU= 1.084E+00 X  TNU= 1.078E+00 X
X  TKE= 4.772E+00 X  TKE= 7.725E-01 X  TKE= 5.368E-02 X  TKE= 2.722E-03 X  TKE= 1.176E-03 X
X  CHI= 2.405E-01 X  CHI= 3.218E-02 X  CHI= 1.717E-03 X  CHI= 4.576E-05 X  CHI= 1.032E-05 X
X  VAP= 2.000E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.001E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   6.566 XXXXXXXXX  -1.302 XXXXXXXXX  -1.462 XXXXXXXXX  -0.889 XXXXXXXXX  -0.738 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 4)       X     ( 3, 4)       X     ( 4, 4)       X     ( 5, 4)       X     ( 6, 4)       X
X    61.240  F      X    50.768  F      X    49.888  F      X    49.908  F      X    49.770  F      X
X                   X                   X                   X                   X                   X
O      1      -0.536      1      -0.461      1      -0.319      1      -0.260      1      -0.157
X  TNU= 4.347E+01 X  TNU= 2.428E+01 X  TNU= 4.466E+00 X  TNU= 1.035E+00 X  TNU= 1.071E+00 X
X  TKE= 1.122E+01 X  TKE= 3.101E+00 X  TKE= 9.614E-02 X  TKE= 1.592E-03 X  TKE= 1.146E-03 X
X  CHI= 6.256E-01 X  CHI= 6.555E-02 X  CHI= 1.012E-03 X  CHI= 1.180E-05 X  CHI= 9.999E-06 X
X  VAP= 2.000E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 1.999E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   5.434 XXXXXXXXX  -1.077 XXXXXXXXX  -1.117 XXXXXXXXX  -0.775 XXXXXXXXX  -0.582 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 3)       X     ( 3, 3)       X     ( 4, 3)       X     ( 5, 3)       X     ( 6, 3)       X
X    49.735  F      X    50.207  F      X    49.860  F      X    49.943  F      X    50.116  F      X
X                   X                   X                   X                   X                   X
O      1      -2.248      1      -1.472      1      -0.924      1      -0.626      1      -0.426
X  TNU= 3.361E+00 X  TNU= 3.074E+00 X  TNU= 1.050E+00 X  TNU= 1.151E+00 X  TNU= 1.073E+00 X
X  TKE= 8.053E-01 X  TKE= 2.349E-01 X  TKE= 5.556E-03 X  TKE= 1.337E-03 X  TKE= 1.148E-03 X
X  CHI= 1.287E-02 X  CHI= 3.665E-03 X  CHI= 4.321E-05 X  CHI= 1.004E-05 X  CHI= 1.000E-05 X
X  VAP= 1.999E-07 X  VAP= 2.001E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   1.012 XXXXXXXXX   0.435 XXXXXXXXX  -0.102 XXXXXXXXX  -0.217 XXXXXXXXX  -0.154 XXXXX
X                   X                   X                   X                   X                   X
X     ( 2, 2)       X     ( 3, 2)       X     ( 4, 2)       X     ( 5, 2)       X     ( 6, 2)       X
X    49.659  F      X    49.999  F      X    49.957  F      X    49.915  F      X    49.964  F      X
X                   X                   X                   X                   X                   X
O      1      -0.492      1      -0.710      1      -0.678      1      -0.583      1      -0.50
X  TNU= 1.008E+00 X  TNU= 1.000E+00 X  TNU= 1.147E+00 X  TNU= 1.068E+00 X  TNU= 1.038E+00 X
X  TKE= 4.085E-03 X  TKE= 1.858E-03 X  TKE= 1.323E-03 X  TKE= 1.139E-03 X  TKE= 1.075E-03 X
X  CHI= 2.747E-05 X  CHI= 1.101E-05 X  CHI= 1.005E-05 X  CHI= 9.999E-06 X  CHI= 9.999E-06 X
X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXX
```

Fig. 5.3.3. Plume Cross Section at 20 sec.
DY = 100 ft, DZ = 200 ft.
Disregard moisture values.

```
XXXXX    2.792 XXXXXXXXX    1.040 XXXXXXXXX    0.609 XXXXXXXXX    0.168 XXXXXXXXX   -0.170 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 8)    X      ( 3, 8)    X      ( 4, 8)    X      ( 5, 8)    X      ( 6, 8)    X
X     50.809  F   X     50.137  F   X     50.082  F   X     49.999  F   X     49.936  F   X
X                 X                 X                 X                 X                 X
O      1      1.592      1      1.860      1      1.585      1      1.118      1      0.843
X  TNU= 5.087E+00 X  TNU= 2.169E+00 X  TNU= 1.658E+00 X  TNU= 2.012E+00 X  TNU= 1.370E+00 X
X  TKE= 4.702E-01 X  TKE= 1.135E-01 X  TKE= 2.026E-02 X  TKE= 6.234E-03 X  TKE= 2.047E-03 X
X  CHI= 4.895E-02 X  CHI= 1.078E-02 X  CHI= 1.448E-03 X  CHI= 1.383E-04 X  CHI= 1.682E-05 X
X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX    5.963 XXXXXXXXX    1.573 XXXXXXXXX    0.074 XXXXXXXXX   -0.752 XXXXXXXXX   -0.714 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 7)    X      ( 3, 7)    X      ( 4, 7)    X      ( 5, 7)    X      ( 6, 7)    X
X     52.397  F   X     50.927  F   X     50.165  F   X     49.888  F   X     49.999  F   X
X                 X                 X                 X                 X                 X
O      1      1.790      1      2.327      1      1.898      1      1.345      1      0.966
X  TNU= 1.364E+01 X  TNU= 6.094E+00 X  TNU= 2.564E+00 X  TNU= 1.746E+00 X  TNU= 1.560E+00 X
X  TKE= 1.420E+00 X  TKE= 5.864E-01 X  TKE= 1.550E-01 X  TKE= 3.042E-02 X  TKE= 5.690E-03 X
X  CHI= 1.422E-01 X  CHI= 5.542E-02 X  CHI= 1.527E-02 X  CHI= 2.390E-03 X  CHI= 2.289E-04 X
X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX    9.535 XXXXXXXXX    2.644 XXXXXXXXX   -0.778 XXXXXXXXX   -1.852 XXXXXXXXX   -1.471 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 6)    X      ( 3, 6)    X      ( 4, 6)    X      ( 5, 6)    X      ( 6, 6)    X
X     52.903  F   X     51.870  F   X     50.733  F   X     50.137  F   X     50.006  F   X
X                 X                 X                 X                 X                 X
O      1      0.651      1      1.127      1      0.740      1      0.562      1      0.313
X  TNU= 1.802E+01 X  TNU= 1.130E+01 X  TNU= 4.335E+00 X  TNU= 1.775E+00 X  TNU= 1.980E+00 X
X  TKE= 1.815E+00 X  TKE= 1.200E+00 X  TKE= 3.780E-01 X  TKE= 7.838E-02 X  TKE= 1.715E-02 X
X  CHI= 1.763E-01 X  CHI= 1.146E-01 X  CHI= 4.295E-02 X  CHI= 8.167E-03 X  CHI= 9.445E-04 X
X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   10.633 XXXXXXXXX    3.637 XXXXXXXXX   -1.545 XXXXXXXXX   -2.236 XXXXXXXXX   -1.998 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 5)    X      ( 3, 5)    X      ( 4, 5)    X      ( 5, 5)    X      ( 6, 5)    X
X     52.119  F   X     51.607  F   X     50.324  F   X     50.096  F   X     49.943  F   X
X                 X                 X                 X                 X                 X
O      1     -1.157      1     -1.622      1     -1.372      1     -0.988      1     -0.833
X  TNU= 1.677E+01 X  TNU= 1.198E+01 X  TNU= 2.832E+00 X  TNU= 1.397E+00 X  TNU= 1.922E+00 X
X  TKE= 1.643E+00 X  TKE= 1.242E+00 X  TKE= 2.058E-01 X  TKE= 3.337E-02 X  TKE= 8.061E-03 X
X  CHI= 1.300E-01 X  CHI= 1.046E-01 X  CHI= 2.520E-02 X  CHI= 2.410E-03 X  CHI= 1.479E-04 X
X  VAP= 2.000E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX    8.533 XXXXXXXXX    2.676 XXXXXXXXX   -1.061 XXXXXXXXX   -1.458 XXXXXXXXX   -1.665 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 4)    X      ( 3, 4)    X      ( 4, 4)    X      ( 5, 4)    X      ( 6, 4)    X
X     50.858  F   X     50.394  F   X     50.061  F   X     49.902  F   X     49.811  F   X
X                 X                 X                 X                 X                 X
O      1     -1.958      1     -2.552      1     -2.173      1     -1.733      1     -1.269
X  TNU= 1.359E+01 X  TNU= 1.141E+01 X  TNU= 4.348E+00 X  TNU= 2.004E+00 X  TNU= 2.577E+00 X
X  TKE= 1.267E+00 X  TKE= 8.776E-01 X  TKE= 1.592E-01 X  TKE= 1.617E-02 X  TKE= 8.188E-03 X
X  CHI= 5.792E-02 X  CHI= 3.061E-02 X  CHI= 8.101E-03 X  CHI= 5.101E-04 X  CHI= 2.975E-05 X
X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 1.999E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX    4.668 XXXXXXXXX    1.477 XXXXXXXXX   -0.350 XXXXXXXXX   -0.614 XXXXXXXXX   -0.739 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 3)    X      ( 3, 3)    X      ( 4, 3)    X      ( 5, 3)    X      ( 6, 3)    X
X     49.978  F   X     49.735  F   X     49.714  F   X     49.936  F   X     50.103  F   X
X                 X                 X                 X                 X                 X
O      1     -1.689      1     -1.970      1     -1.765      1     -1.500      1     -1.166
X  TNU= 5.732E+00 X  TNU= 3.192E+00 X  TNU= 2.453E+00 X  TNU= 2.150E+00 X  TNU= 2.200E+00 X
X  TKE= 4.311E-01 X  TKE= 1.307E-01 X  TKE= 4.032E-02 X  TKE= 7.152E-03 X  TKE= 5.154E-03 X
X  CHI= 6.642E-03 X  CHI= 2.758E-03 X  CHI= 9.150E-04 X  CHI= 5.188E-05 X  CHI= 1.138E-05 X
X  VAP= 2.000E-07 X  VAP= 1.999E-07 X  VAP= 1.999E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX    1.202 XXXXXXXXX    0.886 XXXXXXXXX    0.151 XXXXXXXXX    0.018 XXXXXXXXX   -0.036 XXXXX
X                 X                 X                 X                 X                 X
X      ( 2, 2)    X      ( 3, 2)    X      ( 4, 2)    X      ( 5, 2)    X      ( 6, 2)    X
X     49.583  F   X     50.061  F   X     50.089  F   X     49.985  F   X     49.874  F   X
X                 X                 X                 X                 X                 X
O      1     -0.619      1     -1.082      1     -1.137      1     -1.113      1     -1.078
X  TNU= 2.115E+00 X  TNU= 2.726E+00 X  TNU= 3.230E+00 X  TNU= 2.270E+00 X  TNU= 1.936E+00 X
X  TKE= 2.472E-02 X  TKE= 1.924E-02 X  TKE= 1.210E-02 X  TKE= 5.171E-03 X  TKE= 3.723E-03 X
X  CHI= 7.881E-05 X  CHI= 2.391E-05 X  CHI= 1.320E-05 X  CHI= 1.038E-05 X  CHI= 1.001E-05 X
X  VAP= 1.998E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 2.000E-07 X  VAP= 1.999E-07 X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX    0.0   XXXXXXXXX    0.0   XXXXXXXXX    0.0   XXXXXXXXX    0.0   XXXXXXXXX    0.0   XXXXX
```

Fig. 5.3.4. Plume Cross Section at 80 sec.
DY = 100 ft, DZ = 200 ft.
Disregard moisture values.

```
XXXXX    4.626 XXXXXXXXX   2.064 XXXXXXXXX    0.917 XXXXXXXXX    0.397 XXXXXXXXX    0.014 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2,12)      X     ( 3,12)      X     ( 4,12)      X     ( 5,12)      X     ( 6,12)      X
X    50.588  F     X    50.255  F     X    50.047  F     X    49.950  F     X    49.929  F     X
X                  X                  X                  X                  X                  X
0       1      1.270      1      2.036       1      2.201       1      2.037       1      1.739
X  TNU= 8.396E+00 X  TNU= 6.390E+00 X  TNU= 4.089E+00 X  TNU= 2.994E+00 X  TNU= 2.371E+00 X
X  TKE= 5.048E-01 X  TKE= 3.143E-01 X  TKE= 1.147E-01 X  TKE= 3.513E-02 X  TKE= 1.140E-02 X
X  CHI= 3.858E-02 X  CHI= 1.840E-02 X  CHI= 6.147E-03 X  CHI= 1.435E-03 X  CHI= 2.628E-04 X
X  VAP= 3.857E-02 X  VAP= 1.839E-02 X  VAP= 6.137E-03 X  VAP= 1.425E-03 X  VAP= 2.528E-04 X
X  LIQ= 7.714E-02 X  LIQ= 3.678E-02 X  LIQ= 1.228E-02 X  LIQ= 2.850E-03 X  LIQ= 5.056E-04 X
XXXXX    7.165 XXXXXXXXX   3.601 XXXXXXXXX    1.249 XXXXXXXXX    0.067 XXXXXXXXX   -0.586 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2,11)      X     ( 3,11)      X     ( 4,11)      X     ( 5,11)      X     ( 6,11)      X
X    50.990  F     X    50.699  F     X    50.352  F     X    50.144  F     X    50.012  F     X
X                  X                  X                  X                  X                  X
0       1      1.191      1      2.153       1      2.442       1      2.207       1      1.794
X  TNU= 1.321E+01 X  TNU= 1.106E+01 X  TNU= 6.546E+00 X  TNU= 4.055E+00 X  TNU= 2.917E+00 X
X  TKE= 8.242E-01 X  TKE= 7.557E-01 X  TKE= 3.537E-01 X  TKE= 1.313E-01 X  TKE= 4.229E-02 X
X  CHI= 6.519E-02 X  CHI= 4.620E-02 X  CHI= 2.292E-02 X  CHI= 8.101E-03 X  CHI= 2.071E-03 X
X  VAP= 6.518E-02 X  VAP= 4.620E-02 X  VAP= 2.291E-02 X  VAP= 8.091E-03 X  VAP= 2.061E-03 X
X  LIQ= 1.304E-01 X  LIQ= 9.239E-02 X  LIQ= 4.582E-02 X  LIQ= 1.618E-02 X  LIQ= 4.123E-03 X
XXXXX    9.549 XXXXXXXXX   5.520 XXXXXXXXX    1.825 XXXXXXXXX   -0.401 XXXXXXXXX   -1.429 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2,10)      X     ( 3,10)      X     ( 4,10)      X     ( 5,10)      X     ( 6,10)      X
X    51.031  F     X    50.962  F     X    50.560  F     X    50.186  F     X    49.999  F     X
X                  X                  X                  X                  X                  X
0       1      0.616      1      1.358       1      1.676       1      1.520       1      1.199
X  TNU= 1.373E+01 X  TNU= 1.449E+01 X  TNU= 9.508E+00 X  TNU= 5.302E+00 X  TNU= 3.155E+00 X
X  TKE= 8.007E-01 X  TKE= 1.077E+00 X  TKE= 6.129E-01 X  TKE= 2.499E-01 X  TKE= 8.170E-02 X
X  CHI= 6.982E-02 X  CHI= 6.276E-02 X  CHI= 3.956E-02 X  CHI= 1.769E-02 X  CHI= 5.453E-03 X
X  VAP= 6.982E-02 X  VAP= 6.275E-02 X  VAP= 3.955E-02 X  VAP= 1.768E-02 X  VAP= 5.443E-03 X
X  LIQ= 1.396E-01 X  LIQ= 1.255E-01 X  LIQ= 7.910E-02 X  LIQ= 3.536E-02 X  LIQ= 1.089E-02 X
XXXXX   10.783 XXXXXXXXX   7.009 XXXXXXXXX    2.458 XXXXXXXXX   -0.720 XXXXXXXXX   -2.077 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2, 9)      X     ( 3, 9)      X     ( 4, 9)      X     ( 5, 9)      X     ( 6, 9)      X
X    50.837  F     X    50.934  F     X    50.657  F     X    50.269  F     X    50.006  F     X
X                  X                  X                  X                  X                  X
0       1     -0.008      1      0.230       1      0.396       1      0.339       1      0.298
X  TNU= 1.243E+01 X  TNU= 1.430E+01 X  TNU= 1.031E+01 X  TNU= 5.267E+00 X  TNU= 2.875E+00 X
X  TKE= 6.941E-01 X  TKE= 1.077E+00 X  TKE= 6.959E-01 X  TKE= 2.578E-01 X  TKE= 7.728E-02 X
X  CHI= 6.017E-02 X  CHI= 6.223E-02 X  CHI= 4.516E-02 X  CHI= 2.060E-02 X  CHI= 6.351E-03 X
X  VAP= 6.016E-02 X  VAP= 6.222E-02 X  VAP= 4.515E-02 X  VAP= 2.059E-02 X  VAP= 6.341E-03 X
X  LIQ= 1.203E-01 X  LIQ= 1.245E-01 X  LIQ= 9.030E-02 X  LIQ= 4.117E-02 X  LIQ= 1.268E-02 X
XXXXX   10.763 XXXXXXXXX   7.474 XXXXXXXXX    2.795 XXXXXXXXX   -0.823 XXXXXXXXX   -2.149 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2, 8)      X     ( 3, 8)      X     ( 4, 8)      X     ( 5, 8)      X     ( 6, 8)      X
X    50.636  F     X    50.754  F     X    50.539  F     X    50.179  F     X    50.026  F     X
X                  X                  X                  X                  X                  X
0       1     -0.501      1     -0.884       1     -0.849       1     -0.739       1     -0.602
X  TNU= 1.112E+01 X  TNU= 1.154E+01 X  TNU= 8.778E+00 X  TNU= 4.489E+00 X  TNU= 2.716E+00 X
X  TKE= 6.304E-01 X  TKE= 8.211E-01 X  TKE= 5.674E-01 X  TKE= 1.979E-01 X  TKE= 6.111E-02 X
X  CHI= 4.694E-02 X  CHI= 5.021E-02 X  CHI= 4.157E-02 X  CHI= 1.996E-02 X  CHI= 6.007E-03 X
X  VAP= 4.693E-02 X  VAP= 5.020E-02 X  VAP= 4.156E-02 X  VAP= 1.995E-02 X  VAP= 5.997E-03 X
X  LIQ= 9.386E-02 X  LIQ= 1.004E-01 X  LIQ= 8.310E-02 X  LIQ= 3.991E-02 X  LIQ= 1.199E-02 X
XXXXX    9.763 XXXXXXXXX   6.718 XXXXXXXXX    2.861 XXXXXXXXX   -0.613 XXXXXXXXX   -1.882 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2, 7)      X     ( 3, 7)      X     ( 4, 7)      X     ( 5, 7)      X     ( 6, 7)      X
X    50.408  F     X    50.498  F     X    50.442  F     X    50.165  F     X    49.971  F     X
X                  X                  X                  X                  X                  X
0       1     -0.865      1     -1.592       1     -1.882       1     -1.710       1     -1.444
X  TNU= 9.805E+00 X  TNU= 8.357E+00 X  TNU= 5.846E+00 X  TNU= 3.547E+00 X  TNU= 2.685E+00 X
X  TKE= 5.612E-01 X  TKE= 5.329E-01 X  TKE= 3.141E-01 X  TKE= 1.221E-01 X  TKE= 4.248E-02 X
X  CHI= 3.381E-02 X  CHI= 3.368E-02 X  CHI= 2.736E-02 X  CHI= 1.410E-02 X  CHI= 3.847E-03 X
X  VAP= 3.381E-02 X  VAP= 3.367E-02 X  VAP= 2.735E-02 X  VAP= 1.409E-02 X  VAP= 3.837E-03 X
X  LIQ= 6.760E-02 X  LIQ= 6.732E-02 X  LIQ= 5.470E-02 X  LIQ= 2.818E-02 X  LIQ= 7.675E-03 X
XXXXX    8.017 XXXXXXXXX   5.265 XXXXXXXXX [illegible] XXXXXXXXX   -0.251 XXXXXXXXX   -1.348 XXXXX
X                  X                  X                  X                  X                  X
X     ( 2, 6)      X     ( 3, 6)      X     ( 4, 6)      X     ( 5, 6)      X     ( 6, 6)      X
X    50.269  F     X    50.151  F     X    50.033  F     X    49.964  F     X    49.950  F     X
X                  X                  X                  X                  X                  X
0       1     -1.128      1     -1.997       1     -2.373       1     -2.180       1     -1.849
X  TNU= 8.597E+00 X  TNU= 6.132E+00 X  TNU= 4.005E+00 X  TNU= 3.183E+00 X  TNU= 3.128E+00 X
X  TKE= 4.803E-01 X  TKE= 3.263E-01 X  TKE= 1.464E-01 X  TKE= 6.664E-02 X  TKE= 3.131E-02 X
X  CHI= 2.207E-02 X  CHI= 1.786E-02 X  CHI= 1.155E-02 X  CHI= 5.717E-03 X  CHI= 1.660E-03 X
X  VAP= 2.206E-02 X  VAP= 1.785E-02 X  VAP= 1.154E-02 X  VAP= 5.707E-03 X  VAP= 1.650E-03 X
X  LIQ= [illegible] X  LIQ= [illegible] X  LIQ= [illegible] X  LIQ= [illegible] X  LIQ= [illegible] X
XXXXX    5.380 XXXXXXXXX   3.528 XXXXXXXXX    1.523 XXXXXXXXX    0.131 XXXXXXXXX   -0.692 XXXXX
```

Fig. 5.3.5. Plume Cross Section at 200 sec.
DY = 100 ft, DZ = 200 ft.
Disregard moisture values.

```
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2,10)          X     ( 3,10)          X     ( 4,10)          X     ( 5,10)          X     ( 6,10)          X
X    49.902  F         X    49.902  F         X    49.902  F         X    49.902  F         X    49.902  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 2.741E+02 X  TNU= 2.741E+02 X  TNU= 2.741E+02 X  TNU= 2.741E+02 X  TNU= 2.741E+02 X
X  TKE= 2.741E+00 X  TKE= 2.741E+00 X  TKE= 2.741E+00 X  TKE= 2.741E+00 X  TKE= 2.741E+00 X
X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2, 9)          X     ( 3, 9)          X     ( 4, 9)          X     ( 5, 9)          X     ( 6, 9)          X
X    49.202  F         X    49.202  F         X    49.202  F         X    49.202  F         X    49.202  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 3.134E+02 X  TNU= 3.134E+02 X  TNU= 3.134E+02 X  TNU= 3.134E+02 X  TNU= 3.134E+02 X
X  TKE= 3.134E+00 X  TKE= 3.134E+00 X  TKE= 3.134E+00 X  TKE= 3.134E+00 X  TKE= 3.134E+00 X
X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2, 8)          X     ( 3, 8)          X     ( 4, 8)          X     ( 5, 8)          X     ( 6, 8)          X
X    49.098  F         X    48.599  F         X    48.599  F         X    48.599  F         X    48.599  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 1.000E+02 X  TNU= 1.616E+00 X  TNU= 1.616E+00 X  TNU= 1.616E+00 X  TNU= 1.616E+00 X
X  TKE= 1.000E+02 X  TKE= 1.600E-02 X  TKE= 1.600E-02 X  TKE= 1.600E-02 X  TKE= 1.600E-02 X
X  CHI= 2.300E-01 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2, 7)          X     ( 3, 7)          X     ( 4, 7)          X     ( 5, 7)          X     ( 6, 7)          X
X    48.100  F         X    47.601  F         X    47.601  F         X    47.601  F         X    47.601  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 1.000E+02 X  TNU= 2.450E+00 X  TNU= 2.450E+00 X  TNU= 2.450E+00 X  TNU= 2.450E+00 X
X  TKE= 1.000E+02 X  TKE= 2.500E-02 X  TKE= 2.500E-02 X  TKE= 2.500E-02 X  TKE= 2.500E-02 X
X  CHI= 2.300E-01 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2, 6)          X     ( 3, 6)          X     ( 4, 6)          X     ( 5, 6)          X     ( 6, 6)          X
X    42.098  F         X    41.598  F         X    41.598  F         X    41.598  F         X    41.598  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 1.000E+02 X  TNU= 1.810E-01 X  TNU= 1.810E-01 X  TNU= 1.810E-01 X  TNU= 1.810E-01 X
X  TKE= 1.000E+02 X  TKE= 2.000E-03 X  TKE= 2.000E-03 X  TKE= 2.000E-03 X  TKE= 2.000E-03 X
X  CHI= 2.300E-01 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2, 5)          X     ( 3, 5)          X     ( 4, 5)          X     ( 5, 5)          X     ( 6, 5)          X
X    40.496  F         X    40.496  F         X    40.496  F         X    40.496  F         X    40.496  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 2.068E+00 X  TNU= 2.068E+00 X  TNU= 2.068E+00 X  TNU= 2.068E+00 X  TNU= 2.068E+00 X
X  TKE= 2.100E-02 X  TKE= 2.100E-02 X  TKE= 2.100E-02 X  TKE= 2.100E-02 X  TKE= 2.100E-02 X
X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
X                      X                      X                      X                      X                      X
X     ( 2, 4)          X     ( 3, 4)          X     ( 4, 4)          X     ( 5, 4)          X     ( 6, 4)          X
X    39.595  F         X    39.595  F         X    39.595  F         X    39.595  F         X    39.595  F         X
X                      X                      X                      X                      X                      X
0      1        0.0    1        0.0           1        0.0           1        0.0           1        0.0
X  TNU= 6.710E+00 X  TNU= 6.710E+00 X  TNU= 6.710E+00 X  TNU= 6.710E+00 X  TNU= 6.710E+00 X
X  TKE= 6.700E-02 X  TKE= 6.700E-02 X  TKE= 6.700E-02 X  TKE= 6.700E-02 X  TKE= 6.700E-02 X
X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X  CHI= 5.293E-03 X
X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X  VAP= 0.0       X
X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X  LIQ= 0.0       X
XXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   XXXXXXXXX   0.0   >>>>>
```

Fig. 5.3.6. Initialized Plume Cross Section for the Keystone No. 1 Stack on 20 October 1967. DY = 150 m, DZ = 50 m.

6. RECOMMENDATIONS FOR MODEL EXTENSIONS

6.1 Calculational Scheme to Include Wind Shear Effects

A brief overview of a plausible calculational scheme that would address one of the important effects of wind shear on the plume dynamics is discussed here. The effect is that of the dilution of the plume properties as the plume rises into progressively stronger winds. The process is sketched in Fig. 6.2.1.1, and is well-known to plume modelers. A constant release of pollutant (illustrated in Fig. 6.2.1.1), momentum, sensible heat, moisture, etc., diluted into air that moves with a velocity $u(Z_o)$ will have a density proportional to the inverse of the velocity. A plume property that is released into a stronger wind, $u(Z)$, will be correspondingly more dilute. This effect is important in buoyant plumes when the plume updrafts and downdrafts in the presence of a wind shear cause parcels of the plume to change their downwind advection rate. Clearly, the problem is fully three-dimensional (although it can be in steady state), but a very restrictive assumption may afford a useful recasting of the two-dimensional problem. This assumption is discussed next.

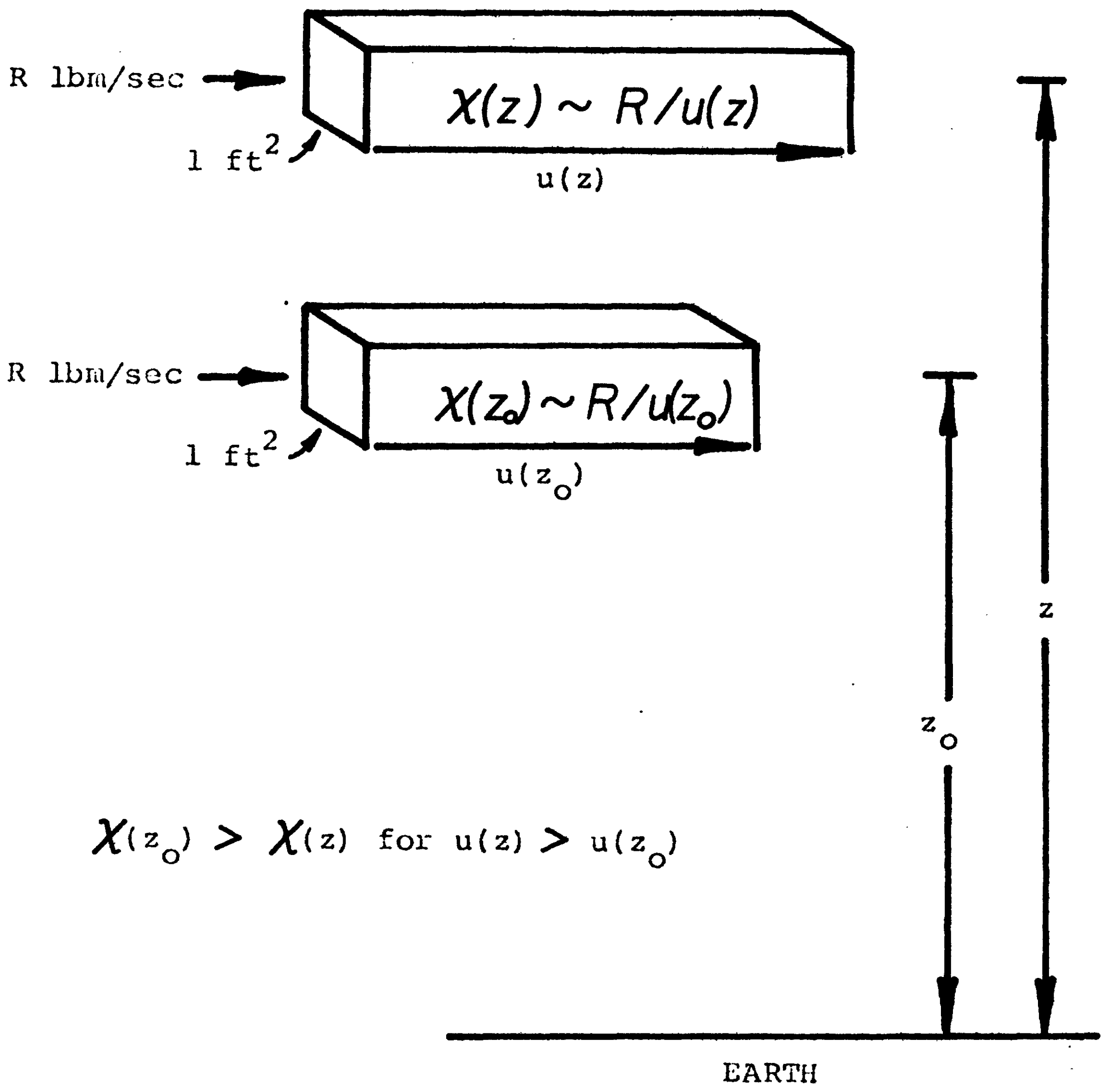


Fig. 6.2.1.1 Dilution of a Steady Release of Pollutant.

Consider the advection and turbulent diffusion of a pollutant in three dimensions (the results extend directly to momentum, sensible heat, etc.):

$$\frac{\partial \chi}{\partial t} + u\frac{\partial \chi}{\partial x} + v\frac{\partial \chi}{\partial y} + w\frac{\partial \chi}{\partial z} = \gamma_\chi \sigma \nabla^2 \chi \qquad (6.1)$$

Assuming that the system is in steady state, we have

$$u\frac{\partial \chi}{\partial x} + v\frac{\partial \chi}{\partial y} + w\frac{\partial \chi}{\partial z} = \gamma_\chi \sigma \nabla^2 \chi \qquad (6.2)$$

In the presence of a steady uniform wind field, u_o, the first term is commonly interpreted as the time-rate-of-change for an observer moving with the wind, and is written as $\frac{\partial \chi}{\partial t_o}$, where $u_o t_o = \chi$. This contains the important assumption that the plume <u>always</u> has the downwind velocity u_o--implying infinite accelerations at the stack exit, to be sure. In a strong wind field the downwind diffusion is commonly neglected with respect to the downwind advection, so the gradient operator has only y and z derivatives. If the wind field is allowed to have shears, then the first term may be represented as

$$u(z)\frac{\partial \chi}{\partial x} = \frac{u(z)}{u(z_o)}\left(u(z_o)\frac{\partial \chi}{\partial x}\right) = \frac{u(z)}{u(z_o)}\frac{\partial \chi}{\partial t_o} \qquad (6.3)$$

where u_o has been arbitrarily chosen to be $u(z_o)$. This interpretation allows the equation to be formulated as

$$\frac{\partial \chi}{\partial t_o} + \frac{u(z_o)}{u(z)} \left(v \frac{\partial \chi}{\partial y} + \frac{\partial \chi}{\partial z}\right) = \frac{u(z_o)}{u(z)} \gamma_\chi \sigma \left(\frac{\partial^2 \chi}{\partial y^2} + \frac{\partial^2 \chi}{\partial z^2}\right) \qquad (6.4)$$

This equation holds the assumption that any parcel of air in the plume, when advected into a region of stronger wind, immediately takes on the local wind velocity and is correspondingly diluted. Note that it also causes parcels that are decelerated to concentrate their properties, which is physically unrealistic, but hopefully is not too serious an error since plume rise and updrafts are almost always stronger than downdrafts. The important feature that this scheme hopes to address is the dilution (usually by about 10 to 50 percent) of plume buoyancy, momentum, and moisture, which affect the plume dynamics. The procedure could be extended to every transport equation in the equation set--only the effect on the divergence condition in the fluid mechanics algorithm has not been studied. Its satisfaction would still be required as a constraint on the solution.

6.2 Calculational Scheme for Time-Dependent Release or Weather

The simulation of "mildly" time-dependent plumes can be made with the model. Essentially, the governing assumption here is that the prevailing weather or effluent properties will advect downwind, and never affect the flow that precedes or follows it. The situation is developed in Fig. 6.2.2.1, where a stack is assumed to have a set of exit properties, Ω, that are piecewise-constant in time over periods of 100 sec. To reconstruct the behavior, an initial simulation with the properties at time t_o, $\Omega(t_o)$ is made to 300 sec. The plume properties changed at time t_o + 100 sec, so a second simulation is made with properties $\Omega(t_o + 100)$ to 200 sec. Again the plume properties changed at time t_o + 200 sec, so a third simulation is made with properties $\Omega(t_o + 200)$ to 100 sec. The actual plume is then "cut and pasted" from the pertinent data in the simulations as shown at the bottom of the figure. The calculation is somewhat wasteful, since 600 sec of simulation produces only 300 sec of results--but the scheme surely saves time and storage over a fully three-dimensional calculation. Eventually, for sufficiently "strong" time-dependence the scheme becomes too laborious with respect to a three-dimensional calculation.

6.3 Cloud Microphysics Model

The limited success of the equilibrium moisture thermodynamics model is due to its explicit differencing. In short, the model is ignorant of the latent heat released in a current timestep, and it adjusts the equilibrium conditions without

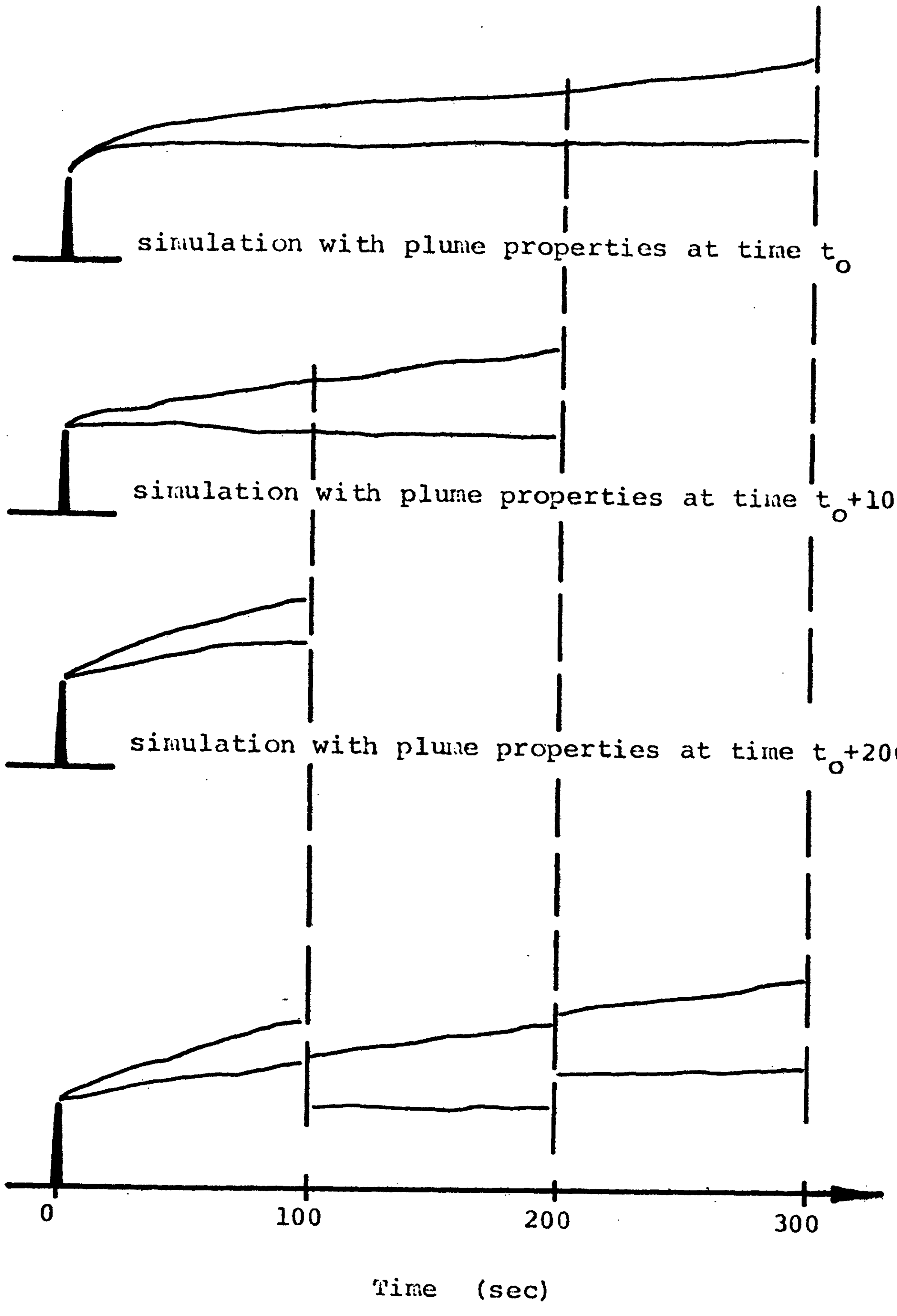


Fig. 6.2.2.1 Simulation of a Time-Dependent Plume in Steady-State Weather. Scheme is discussed in the text.

this knowledge. The resultant oscillations in the equilibrium conditions are not surprising, nor is the ability to control them with very small timesteps. If the calculation was made implicit--essentially iterating on the coupled latent heat release equation and Magnus' formula for liquid-vapor equilibrium--the timesteps could be relaxed back to their original size.

The prospect of incorporating a non-equilibrium moisture model is not investigated in this work. The limitations of the equilibrium model have not been sufficiently explored to justify the change at this point.

NOMENCLATURE

A_o	initial line-vortex area (ft^2)
C	experimental constant, 1.9
c_p	heat capacity at constant pressure (BTU/lb_m °R)
c_p^{moist}	heat capacity of moist air at constant pressure (BTU/lb_m °R)
DT	timestep size (sec)
DY	cell width (ft)
DZ	cell height (ft)
$e_{sat}(T)$	saturation vapor pressure of water (mb)
$E_\chi^{(i)}$	energy of the i^{th} decay channel from pollutant species χ (MeV)
$F_\chi^{(i)}$	fractional energy deposition for i^{th} radioactive decay channel from pollutant species χ
g	acceleration due to gravity (ft/sec^2)
g_i	vector acceleration due to gravity (ft/sec^2)
I	specific internal energy (BTU/lbm)
k	thermal conductivity (BTU/ft-sec-°R)
L	buoyancy parameter (ft)
L_{eddy}	eddy length scale (ft)
L_{vap}	latent heat of vaporization of water (BTU/lb_m)
N	experimental constant, 3.0
$\tilde{p}$	physically measurable pressure (millibars)
p	pressure perturbation about an adiabatic reference state (mb)
p_o	pressure in a quiet adiabatic atmosphere (mb)

$\overline{p}$	time average pressure perturbation (mb)
p'	fluctuating pressure perturbation (mb)
Pr	Prandtl number
$q, q(y,z,t)$	turbulence kinetic energy per unit lb_m (ft^2/sec^2)
$q_{library}(Z)$	prescribed turbulence kinetic energy profile (ft^2/sec^2)
Q	heat (BTU)
Q_H	heat emitted at stack exit (BTU/sec)
$R(T)$	plume radius as a function of time (ft)
R_{dry}, R_d	gas constant for dry air (ft^3 mb/lb_m°R)
R_{vap}, R_v	gas constant for water vapor (ft^3mb/lb_m°R)
Sc_{liq}	Schmidt number for liquid water
Sc_{vap}	Schmidt number for water vapor
t, T	time (seconds)
t_o	x/u_o (sec)
T_*	time coordinate of virtual origin (sec)
$\tilde{T}$	physically measurable temperature (°R)
T	temperature perturbation about an adiabatic reference state (°R)
T_o	temperature in a quiet adiabatic atmosphere (°R)
T_s	temperature of stack effluent (°R)
$\tilde{T}_v$	virtual temperature (°R)
T_{vo}	virtual temperature in a quiet adiabatic atmosphere (°R)
u	downwind velocity (ft/sec)
u_o, U	windspeed, constant with height (ft/sec)
u_{eddy}	turbulent velocity scale in an eddy (ft/sec)
$\tilde{u}_i, \tilde{u}_j$	velocity (ft/sec)
u_i, u_j	velocity (ft/sec)

$\bar{u}_i, \bar{u}_j$	time average velocity (ft/sec)
u_i', u_j'	fluctuating velocity (ft/sec)
$\overline{u_i' \, u_j'}$	Reynolds stress tensor (ft^2/sec^2)
$\overline{u_i' \, \theta'}$	correlation of fluctuating velocity and temperature
$\overline{u_i' \, u_j' \, u_k'}$,	triple correlation of fluctuating velocity (ft^3/sec^3)
v	crosswind velocity (ft/sec)
V_g	geostrophic wind (ft/sec)
w	vertical velocity (ft/sec)
$W_{mol,\chi}$	molecular weight of the pollutant species (lb_m/lb_m-mole)
X	downwind distance (ft)
x_i, x_j	cartesian coordinate (ft)
y	crosswind distance (ft)
z	height (ft)
z_*	height coordinate of virtual origin (ft)

α, α_1	turbulence constants
γ_L	reciprocal turbulent Schmidt number for liquid water
γ_T	reciprocal turbulent Prandtl number for heat
γ_V	reciprocal turbulent Schmidt number for water vapor
γ_χ	reciprocal turbulent Schmidt number for pollutant
Γ	turbulence constant
Γ_1	turbulence constant
Γ_d	dry adiabatic lapse rate (°R/ft)
ε_h	eddy diffusivity of heat (ft^2/sec)
ε_m	eddy diffusivity of momentum (ft^2/sec)
ε_χ	eddy diffusivity of pollutant (ft^2/sec)
$\tilde{\theta}$	potential temperature (°R)
θ	potential temperature perturbation about an adiabatic reference state (°R)
θ_o	potential temperature in a quiet adiabatic atmosphere (°R)
$\overline{\theta}$	time average potential temperature (°R)
θ'	fluctuating potential temperature (°R)
θ_v	virtual potential temperature (°R)
θ_{vo}	virtual potential temperature in a quiet adiabatic atmosphere (°R)
$\overline{\theta}_v$	time average virtual potential temperature (°R)
θ_v'	fluctuating virtual potential temperature (°R)
$\lambda_x^{(i)}$	decay constant for i^{th} radioactive decay channel from pollutant species χ (sec^{-1})

μ	dynamic viscosity (lb_m/sec ft)
ν	kinematic viscosity (ft^2/sec)
ρ_{dry}	density of dry air (lbm/ft^3)
ρ_{liq}	liquid water density (lbm/ft^3)
$\bar{\rho}_{liq}$	time average liquid water density (lbm/ft^3)
ρ'_{liq}	fluctuating liquid water density (lbm/ft^3)
ρ_s	density of stack effluent (lbm/ft^3)
ρ_{sat}	saturation water vapor density (lbm/ft^3)
ρ_{vap}	water vapor density (lbm/ft^3)
$\bar{\rho}_{vap}$	time average water vapor density (lbm/ft^3)
ρ'_{vap}	fluctuating water vapor density (lbm/ft^3)
$\sigma, \sigma(y,z,t)$	eddy viscosity (same as ϵ_m) (ft^2/sec)
$\sigma_{library}(z)$	prescribed eddy viscosity profile (ft^2/sec)
χ	pollutant density (lbm/ft^3)

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APPENDIX A

Definitions of Important Variables Added to the VARR-II Code for Simulating Plume Behavior

Definitions of Important Variables Added to VARR-II for Simulating Plume Behavior

Variable	Meaning	Units
BKGND	background pollutant concentration	lbm/ft^3
CHI(IK)	pollutant concentration, χ	lbm/ft^3
CHIØ(IK)	pollutant concentration at the previous timestep	lbm/ft^3
CHII	pollutant concentration input variable	lbm/ft^3
DWNDS	downwind distance	ft
EFRAC(J)	fraction of the energy of the J^{th} radiation deposited in the plume, $F_x^{(j)}$	-
ELAM(J)	energy of the J^{th} radioactive decay channel, $E_x^{(j)}$	MeV
GAML	reciprocal turbulent Schmidt number for cloud liquid water, γ_L	-
GAMV	reciprocal turbulent Schmidt number for water vapor, γ_V	-
GAMX	reciprocal turbulent Schmidt number for pollutant, γ_X	-
LIQ(IK)	cloud liquid water density, ρ_{liq}	lbm/ft^3
LIQØ(IK)	cloud liquid water density at the previous timestep	lbm/ft^3
LIQI	cloud liquid water density input variable	lbm/ft^3
NCHAN	number of decay channels to be input	-
NPRØF	number of input profiles to be input	-
RLAM(J)	decay constant of the J^{th} decay channel, $\lambda_x^{(j)}$	sec^{-1}
RLAMB	net decay constant, $\sum_{j=1}^{NCHAN} \lambda_x^{(j)}$	sec^{-1}
SER	specific energy release rate of the radioactive pollutant	MeV/sec
SMSIE	total internal energy on the mesh (assumed 1 ft deep)	BTU

Variable	Meaning	Units
TRSTRT(J)	time for program coarsening (J=1, 2, ... 5)	sec
VELCHI	pollutant-averaged velocity	ft/sec
VAP(IK)	water vapor density, ρ_{vap}	lbm/ft^3
VAPØ(IK)	water vapor density, at the previous timestep	lbm/ft^3
VAPI	water vapor density input variable	lbm/ft^3
WMØLX	molecular weight of the pollutant	lbm/lbm-mole
WWSP(J)	wind speed profile variable	ft/sec
WZAP(J)	absolute pressure profile variable	mb
WZLQ(J)	liquid water profile variable	lbm/ft^3
WZSIE(J)	specific internal energy profile variable	BTU/lbm
WZTQ(J)	turbulence kinetic energy profile variable	ft^2/sec
WZTS(J)	eddy viscosity profile variable	ft^2/sec
WZVP(J)	water vapor profile variable	lbm/ft^3
YPLUME	plume center height	ft

APPENDIX B

Card Formats for Input Variables

Card Formats for Input Variables

Card No.	Input Variables/Card	Format
1*	IBR, KBR, IPRFM	(2(5X,I5),7X,I2)
2	LABEL	(10A8)
3*	DT, TPRT, TPLT, TWTD, TFIN, ITAPW, NPRT, IDIAG, LPR, IØBS, IDG, KDG	(5F8.3, 5I2, 2I3)
4*	DX, DZ, GX, GZ, ALX, ALZ, CYL, B_O, EPS, VMIN	(10F8.3)
5	KWR, KWL, KWT, KWB, FSLIP, ALP, GAM, ALP_O, GAM_1, NU, TQJET, TSJET	(4I2, 8F8.3)
6	AW, BW, CW, WEPS, KDERBC, UBRI, UBRI, UBLI, WBTI, WBBI	(4F8.3,I2,4F8.3)
7	WØBI, UØBI, CSUBPØ	(3F8.3)
8*	TGAM, T_O, TI, TSTEP, MAT, NRESEX	(4F8.3, 2I2)
9	AI, BI, CI, AR, BR, CR, AMU, BMU, CMU	(10F8.3)
10	AK, BK, CK, ACP, BCP, CCP	(10F8.3)
11*	NFLOW, NT1, NT2, NT3, NT4, NT5, NTAU	(7X, I3,5(5X,I3), 7X, I3)
12*	TYMF(I), FN(I)	(8F8.3)
13*	TYMYT1(I), T1N(I)	(8F8.3)
14*	TYMT2(I), T2N(I)	(8F8.3)
15*	TAU(I)	(8F8.3)
16*	I, CØFA, CØFB, CØFC	(3X,I3,2X,3F8.3)
17*	I, CØFA, CØFB,CØFC	(3X,I3,2X,3F8.3)
18*	I, CØFA, CØFB,CØFC	(3X,I3,2X,3F8.3)

Card No.	Input Variables/Card	Format
19*	I, CØFA, CØFB, CØFC	(3X,I3,2X,3F8.3)
20*	I, CØFA, CØFB, CØFC	(3X,I3,2X,3F8.3)
21*	I, CØFA, CØFB, CØFC	(3X,I3,2X,3F8.3)
22*	I, K, RXC, RZC	(2(3X,I3),2(5X,F8.3)
23*	NL, NR, NB, NT, ICELTYP	(4I5,I2)
24*	SIEI, TQI, TSI, UI, WI, CHII, VAPI, LIQI	(8F8.3)
25**	NGØP, NOVP, DRØU, XDIV, YDIV	(2(7X,I2),3(6X,F8.3))
26	IGØP(I)	(6X,6I2)
27	VNTP(I), NCVTYP(I)	(4(5X,I2,1X,I3))
28	IBR, KBR, IPRFM	(2(5X,I5),7X,I2)
29*	GAMX, NCHAN, WMØLX, GAMV, GAML, BKGND, DWNDS	(F8.3,I8,5F8.3)
30*	RLAM, ELAM, EFRAC	(3F8.3)
31*	NPRØF, TRSTRT(1), TRSTRT(2), TRSTRT(3), TRSTRT(4), TRSTRT(5)	(I8,5F8.3)
32*	WZSIE, WZTQ, WZTS, WZVP, WZLQ, WZAP, WWSP	(7F8.3)
33*	IBR, KBR, IPRFM	(2(5X,I5),7X,I2)

*See Special Notes to Input

**Cards No. 25-28 in the original VARR-II input have been omitted entirely in this version.

Special Notes to Input

Card No.	
1	Do not attempt to "restart" the program (i.e., storing or retrieving the program storage on or from magnetic tape or disc) unless additional programming has been performed that would "restart" the variables added to VARR-II. Set IPRFM=1 to allow the statistics package (instead of the film generated plots) to be printed out.
3	TPLT is now "time when to print statistics" (sic). Always set TWTD > TFIN, and/or make device 8 equal to DUMMY. Set ITAPW = 8. In IDIAG, grind time and CPU time have been omitted. Set LPR = 3, and IØBS = 0.
4	Set ALX = ALZ = 1.0, and CYL = 0.0
8	TI is ignored by the program. TSTEP should have a value of about 10^{-2}.
11-15	All of the values on these cards are unimportant for problems that have no inflow/outflow and no obstacle cells. However, the code cannot skip these cards, so dummy information must be supplied.
16-22	Set I = 0.
23-24	Because of the solid-wall boundary conditions, only the real fluid cells on the mesh need to be initialized. Cards of type 23 and 24 can be repeated as many times as desired when initializing; the sequence is terminated when NL = 0 on Card 23. Note that CHII, VAPI, and LIQI have been added to Card 24.
25-28	These cards have been dropped from the input list.
29	See Appendix A for definitions.
30	This card is repeated NCHAN times with the values corresponding to J=1,...NCHAN. See Appendix A for definitions.
31	See Appendix A for definitions.

Card No.

32 This card is repeated NPROF times with the values corresponding to J=1, ... NPROF. For a problem that is 20 real cells high, the code needs 20 values for each variable if there are no mesh coarsenings. If there is one mesh coarsening carried out, the code needs 30 values (consisting of the first 20 plus 10 more to initialize the new cell area). If there are two mesh coarsenings carried out, the code needs 40 values, etc. The cell center height at which a profile needs to be defined can be generated by considering Figs B.1 and B.2. See Appendix A for definitions.

33 Set IBR = -1 to terminate the problem.

J	WZ____(J) to be defined at a height:	
⋮	⋮	
$\frac{4KBR}{2} + 1$	KBR(4DZ) + 4DZ	
$\frac{4KBR}{2}$	KBR(4DZ) - 2DZ	$\frac{KBR}{2}$ cells, each with height 4DZ
⋮	⋮	
$\frac{3KBR}{2} + 2$	KBR(2DZ) + 6DZ	
$\frac{3KBR}{2} + 1$	KBR(2DZ) + 2DZ	
$\frac{3KBR}{2}$	KBR(2DZ) - DZ	$\frac{KBR}{2}$ cells, each with height 2DZ
$\frac{3KBR}{2} - 1$	KBR(2DZ) - 3DZ	
⋮	⋮	
KBR + 2	KBR(DZ) + 3DZ	
KBR + 1	KBR(DZ) + DZ	
KBR	KBR(DZ) - DZ/2	KBR cells, each with height DZ
KBR - 1		
⋮	⋮	
3	5DZ/2	
2	3DZ/2	
1	DZ/2	

EARTH

Figure B.1 Profile generation for problems with mesh coarsening. KBR real cells are placed on the computer mesh at a time. The cell height is DZ initially. The cell center height at which each of the seven profiles must be specified is developed in the figure.

J	WZ___(J) to be found at a height:	
.	.	10 cells, each 400 ft. high
42	.	
41	4200 ft	
40	3900	10 cells, each 200 ft. high
.	.	
32	.	
31	2100	
30	1950	10 cells, each 100 ft. high
.	.	
22	1150	
21	1050	
20	975	20 cells, each 50 ft. high
.	.	
3	125	
2	75	
1	25 ft	

EARTH

Fig. B.2. Profile generation for a particular problem. The problem is 20 cells high, each of which is 50 feet tall initially.

APPENDIX C

Statement Number Cross-References

Statement Number Cross-References

The statement number cross-references are intended to aid the user in understanding the purpose of the altered or added FORTRAN statements. Any statement that was altered or added is labeled in columns 73-80 with a "card entry" that begins with the initials RGB or MWG.

The first cross-reference consists of 12 effects or problems that are solved by the cards that are listed below the problem statement. For example, a constant heat flux from the top wall of an obstacle cell (Effect No. 12) is permitted when a single statement (No. 1688) is altered. Statements that were removed from the code are not listed.

A second cross-reference allows any altered or added statement to be identified with the problem that it helps to solve. For example, statement #1688 is identified with effect #12--and looking up effect #12 in the first cross-reference shows that no other cards were involved in the solution to that problem.

EFFECTS OR PROBLEM(S) CONSIDERED EFFECT NO. 1

1. Non-executable statements for COMMON, DIMENSION, REAL, INTEGER, or EQUIVALENCE CARDS. (Two executable statements (91,92) are included here since they are related to program control.)

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
MAIN	RGB MN60A,B	32,36,53,55,56,86,91,92
"	RGB MN01A	35,85
"	RGB VM62A	50,52
"	RGB VM55A,B	51,54
IDLE	RGB MN60A,B	125,129,146,148,149,179
"	RGB MN01A	128,178
"	RGB VM62A	143,145
"	RGB VM55A,B	144,147
VRPRT	RGB MN60A,B	392,398,415,417,418,448
"	RGB MN01A	397,447
"	RGB VM62A	412,414
"	RGB VM55,A,B	413,416
VSET	RGB MN60,A,B	512,516,533,535,536,566
"	RGB MN01A	515,565
"	RGB VM62A	530,532
"	RGB VM55,A,B	531,534

EFFECTS OR PROBLEM(S) CONSIDERED — EFFECT NO. 1

non-executable (continued)

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
MESHMK	RGB MN60A,B	685,689,706,708,709,739
"	RGB MN01A	688,738
"	RGB VM62A	703,705
"	RGB VM55A,B	704,707
VM	RGB MN60A,B	1071,1077,1094,1096,1097,1127
"	RGB MN01A	1076,1126
"	RGB VM62A	1091,1093
"	RGB VM55A,B	1092,1095

EFFECTS OR PROBLEM(S) CONSIDERED EFFECT NO. 2

1. Boundary conditions for crosswind runs for the variables U, W, SIE, TQ, TS.

2. Set $\sigma \geq \sigma_{library}(Z)$ and $q \geq q_{library}(Z)$

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM50A	1466,1847
VM	RGB VM51A	1301,1305,1307,1309,1467, 1489,2199,2200
VM	RGB VM02A	1302,1369-71,1379

EFFECTS OR PROBLEM(S) CONSIDERED	EFFECT NO. 3

1. Boundary conditions for crosswind runs for the variable, CHI.

2. Pollutant transport equation.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM52A,B,C	1310-12,1475-77,1959,1980, 1988,2047-52,2277-78,2358,2366, 2469

EFFECTS OR PROBLEM(S) CONSIDERED	EFFECT NO. 4

1. Cell initialization from input data.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
MESHMK	RGB MK01A,02A	946,952,960
"	RGB MK60A	930-31,953-54,961-62,1027, 1049-50

EFFECTS OR PROBLEM(S) CONSIDERED — EFFECT NO. 5

1. Atmospheric profile read-in and printout for variables,

WZSIE	(internal energy)
WZTQ	(turbulence kinetic energy)
WZTS	(eddy viscosity)
WZVP	(water vapor)
WZLQ	(cloud liquid water)
WZAP	(pressure)
WWSP	(wind speed)

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM62A	1153-58,1162,1169
VM	RGB VM55A	1151-52, 1159-60, 1165-67, 1172-74, 1179-81
VM	RGB VM70A	1161,1168,1175

EFFECTS OR PROBLEM(S) CONSIDERED EFFECT NO. 6

1. Moisture model in subroutine VM (initialization of cell moisture is done elsewhere), including input, boundary conditions, and transport equations.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM60A,B	1072,1133-37,1163-64,1170-71, 1177-78,1313-16,1478-81, 1960-61, 1981-82,1989-90, 2053-64,2359-60,2367-68,2470-71
VM	RGB VM62A	2225-26,2230-55
VM	RGB VM61A	2201-24

EFFECTS OR PROBLEM(S) CONSIDERED EFFECT NO. 7

1. Mesh coarsening capability.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
IDLE	RGB ID55A	202-209, 214-327
IDLE	RGB ID70A	210-213
VM	RGB VM55A,B	1132,2553-56,2564-68
VM	RGB ID55A,B	2557-63

EFFECTS OR PROBLEM(S) CONSIDERED — EFFECT NO. 8

1. Cell by cell output of variables by the printing subroutine.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VRPRT	RGB MØ60A	394
"	RGB MØ01A	451-507*

*The entire section was altered, although not all of the cards have card entries.

EFFECTS OR PROBLEM(S) CONSIDERED	EFFECT NO. 9

1. Plume statistics package.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM54A,B	2518-21, 2529-30,2545-47
VM	RGB VM70A	2514-17,2522-28,2531-33
VM	RGB VM55B	2548-50

EFFECTS OR PROBLEM(S) CONSIDERED | EFFECT NO. 10

1. Radioactive decay heating.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM56A	1073,1138-50,2227-29,2273-74, 2276

EFFECTS OR PROBLEM(S) CONSIDERED — EFFECT NO. 11

1. Turbulence model errors.
2. SIEX error.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM000	2193-94
"	MWG 04/78	2195-96
"	RGB VM01A	1361,1416,1526,1591,1816, 1877

EFFECTS OR PROBLEM(S) CONSIDERED EFFECT NO. 12

1. Constant heat flux from obstacle top wall.

SUBROUTINE(S)	CARD ENTRIES	PROGRAM STATEMENT NUMBERS
VM	RGB VM03A	1688

Statement Number	Effect Number	Statement Number	Effect Number
32	1	946	4
35	1	9-954	4
36	1	960-962	4
50-56	1	1027	4
85-86	1	1049-50	4
91-92	1	1071	1
125	1	1072	6
128-129	1	1073	10
143-149	1	1076-77	1
178-179	1	1091-97	1
202-209	7	1126-27	1
210-213	7	1132	7
214-327	7	1133-37	6
392	1	1138-50	10
394	8	1151-62	5
397-398	1	1163-64	6
412-418	1	1165-69	5
447-448	1	1170-71	6
451-507	8	1172-76	5
512	1	1177-78	6
515-516	1	1179-81	5
530-536	1	1301-02	2
56-566	1	1305	2
685	1	1307	2
688-689	1	1309	2
73-709	1	1310-12	3
738-739	1	1313-16	6
930-931	4	1361	11

Statement Number	Effect Number
1369-71	2
1379	2
1416	11
1466-67	2
1475-77	3
1478-81	6
1489	2
1526	11
1591	11
1688	12
1816	11
1847	2
1877	11
1959	3
1960-61	6
1980	3
1981-82	6
1988	3
1989-90	6
2047-52	3
2053-64	6
2193-96	11
2199-00	2
2201-26	6
2227-29	10
2230-55	6
2273-74	10

Statement Number	Effect Number
2276	10
2277-88	3
2358	3
2359-60	6
2366	3
2367-68	6
2469	3
2470-71	6
2514-33	9
2545-50	9
2553-68	7

APPENDIX D

Computer Code Listing

```
**************************************************************** ERAS0010
*                                                              * ERAS0020
*       TO SET ELEMENTS OF REAL OR INTEGER ARRAYS TO ZERO. A1,A2,... * ERAS0030
*       ARE ARRAY NAMES AND N1,N2,... ARE INTEGER VALUES OR    * ERAS0040
*       EXPRESSIONS GIVING THE ARRAY SIZES.                    * ERAS0050
**      I.E. - CALL ERASE(C,26*31,N,7*31,E,254)               ** ERAS0060
*                                                              * ERAS0070
**************************************************************** ERAS0080
ERASE    START 0                                                 ERAS0090
         SAVE  (14,12),,*                                        ERAS0100
         BALR  12,0                                              ERAS0110
         USING *,12                                              ERAS0120
         SR    0,0                                               ERAS0130
         SR    2,2              PARAMETER LIST INDEX=0           ERAS0140
         L     6,=F'4'                                           ERAS0150
E1       L     3,0(2,1)         LOAD 3 WITH ARRAY ADDRESS        ERAS0160
         L     4,4(2,1)         LOAD 4 WITH ADDRESS OF ARRAY LENGTH ERAS0170
         L     7,0(4)           LOAD 7 WITH ARRAY LENGTH-1 TIMES 4 ERAS0180
         SLA   7,2                                               ERAS0190
         SR    7,6                                               ERAS0200
         SR    5,5                                               ERAS0210
E2       ST    0,0(5,3)         STORE ZERO                       ERAS0220
         BXLE  5,6,E2                                            ERAS0230
         LTR   4,4              TEST FOR LAST ARGUMENT IN LIST   ERAS0240
         BM    RETN                                              ERAS0250
         A     2,=F'8'                                           ERAS0260
         B     E1               PICK UP NEXT ARGUMENT PAIR       ERAS0270
RETN     RETURN (14,12),T                                        ERAS0280
         END                                                     ERAS0290
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1   VTP
      REAL NU,LIQ,LIQO,LIQI,LOUT                                 RGBMN60A
      DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
     1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
     2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                    RGBMN01A
     A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                             RGBMN60A
```

```
3    ,TYMF (25) ,FN (25) ,TYMT1 (25) ,T1N (25) ,TYMT2 (25) ,T2N(25) ,
4    COFBA (25) ,COFBB (25) ,COFBC (25) ,COFTA(25) ,COFTB (25) ,COFTC (25) ,
5    COFRA (25) ,COFRB (25) ,COFRC (25) ,COFLA (25) ,COFLB (25) ,COFLC (25) ,
6    OFOBTA (25) ,OFOBTB (25) ,OFOBTC (25) ,
7    OFOBRA(25) ,OFOBRB(25) ,OFOBRC(25) ,TAU (10) ,USL(32) ,USLOB (20) ,
8    USROB (20) ,USTOB (20) ,USBOB (20)
9,COFBD(25) ,COFBE (25) ,COFTD (25) ,COFTE (25) ,COFTF (25) ,COFBF (25) ,
*COFRD(25) ,COFRE(25) ,COFLD(25) ,COFLE(25) ,COFRF(25) ,COFLF (25) ,
AOFOBTD (25) ,OFOBTE (25) ,OFOBRD (25) ,OFOBRE (25) ,
B  OFOBTF (25) ,OFOBRF (25) ,
CTYMT3 (25) ,TYMT4 (25) ,TYMT5(25) ,T3N (25) ,T4N (25) ,T5N (25) ,
*  IICFR(1) ,IICFL (1) ,IICFT (1) ,IICFB (1)
*    ,ZERO1(1165) ,ZERO2 (608) ,ZERO3(16) ,ZERO4(3)
 DIMENSION ZSIE(22) ,ZTQ (22) ,ZTS (22) ,ZVP (22) ,ZLQ (22) ,ZAP(22) ,WSP (22) RGBVM62A
 DIMENSION TRSTRT (5) ,WZSIE(100) ,WZTQ(100) ,WZTS(100)                       RGBVM55A
A,WZVP(100) ,WZLQ(100) ,WZAP (100) ,WWSP (100)                                RGBVM62A
 COMMON/VRCOM/A (14000)                                                       RGBMN60A
 COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ,            RGBVM55A
AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                             RGBMN60A
B,WSP,WWSP,BKGND,DWNDS                                                        RGBMN60B
 COMMON /VRCON/ ALP,ALP0,ALX,ALZ,B0,BETA,BUFL,CFI(9),CFS(9),CYL,
1    DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2    IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3    IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
4    LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5    TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
*   ,USR(32) ,UST(22) ,USB (22) ,USO (10) ,FFX3,FFY3
6    ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7    T0,SIEI,IDG,KDG,TI,MAT,RHO0,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8    T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9    COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
*    OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1    USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*   ,CSUBPO,EPS0,RDXDZS,RLENGH ,TQJET,TSJET
 COMMON /FLMCON/ DROU,DROU0,IPRFM
 COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
```

```
     1                  ,VMIN
      COMMON/PROP/SIGN
     COMMON/EXTRA/NT3,NT4,NT5,TYMT3,TYMT4,TYMT5,T3N,T4N,T5N,COFBD,
    1COFBE,COFBF,COFTD,COFTE,COFTF,COFRD,COFRE,COFRF,COFLD,COFLE,
    2COFLF,OFOBTD,OFOBTE,OFOBTF,OFOBRD,OFOBRE,OFOBRF,IRESET,
    *NCYCLS,TADD,NIV,IOBRAN
      COMMON/INDEX/NWPCL,K2NCL
      COMMON/LARGE/DIFFCO(2400)
     EQUIVALENCE (A(1),CF),(A(2),U),(A(3),W),(A(4),P),(A(5),TQ),
    1   (A(6),TS),(A(7),ER,CQ),(A(8),UO),(A(9),WO),(A(10),TQO),
    2   (A(11),TSO),(A(12),SIE),(A(13),SIEO),(A(14),RX),(A(15),RZ),
    3   (A(16),IICFR),(A(17),IICFL),(A(18),IICFT),(A(19),IICFB),
    A   (A(20),CHI),(A(21),CHIO),                               RGBMN01A
    B   (A(22),VAP),(A(23),VAPO),(A(24),LIQ),(A(25),LIQO),      RGBMN60A
    4   (ZERO1(1),ALP),(ZERO2(1),NT3),(ZERO3(1),AI),(ZERO4(1),DROU)
C NOTE. END - END OF NON-EXECUTABLE STATEMENTS .
C
C NOTE. NWPC = NUMBER OF WORDS PER MESH CELL .
      CALL ERASE (ZERO1,1165,ZERO2,608,ZERO3,16,ZERO4,3,A,14000) RGBMN60A
      NWPC=25                                                   RGBMN60A
      NWPCL = 4
      IVDI=5
      IVDO=6
  100 WRITE(IVDO,1)
      READ(IVDI,2) IBR,KBR,IPRFM,NCYCLS,TADD,IRESET
      ERF=0
      IF( IPRFM.GT.0 ) CALL FLMINI
      IF( IBR ) 700,400,400
 400  PRINT 11
      CALL VSET
      WRITE(IVDO,3)
      IF( ERF.EQ.1 ) GO TO 700                                  VRC42002
      PRINT 12
      CALL VM
      IF( ERF.EQ.1 ) GO TO 700                                  VRC50002
      GO TO 100
```

```
  700 IF( IPRFM.GT.0 ) CALL FLMFIN
C ***** FORMATS ***** FORMATS ***** FORMATS ***** .
    1 FORMAT(1H1,22H MAIN PROGRAM CALLED .)
   2  FORMAT(2(5X,I5),7X,I2,I11,F10.4,5X,I5)
  3   FORMAT(1H ,27H SUBROUTINE VSET FINISHED .)
  11  FORMAT(1H ,25H SUBROUTINE VSET CALLED .)
  12  FORMAT(1H ,23H SUBROUTINE VM CALLED .)
      STOP
      END                                                        VRC70004
      BLOCK DATA
      COMMON/LARGE/DIFFCO(2400)
      REAL DIFFCO/2400*1.0/
      END
      SUBROUTINE IDLE
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1   VTP
      REAL NU,LIQ,LIQO,LIQI,LOUT                                 RGBMN60A
      DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
     1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
     2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                    RGBMN01A
     A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                             RGBMN60A
     3   ,TYMF(25),FN(25),TYMT1(25),T1N(25),TYMT2(25),T2N(25),
     4   COFBA(25),COFBB(25),COFBC(25),COFTA(25),COFTB(25),COFTC(25),
     5   COFRA(25),COFRB(25),COFRC(25),COFLA(25),COFLB(25),COFLC(25),
     6   OFOBTA(25),OFOBTB(25),OFOBTC(25),
     7   OFOBRA(25),OFOBRB(25),OFOBRC(25),TAU(10),USL(32),USLOB(20),
     8   USROB(20),USTOB(20),USBOB(20)
     9,COFBD(25),COFBE(25),COFTD(25),COFTE(25),COFTF(25),COFBF(25),
     *COFRD(25),COFRE(25),COFLD(25),COFLE(25),COFRF(25),COFLF(25),
     AOFOBTD(25),OFOBTE(25),OFOBRD(25),OFOBRE(25),
     B  OFOBTF(25),OFOBRF(25),
     CTYMT3(25),TYMT4(25),TYMT5(25),T3N(25),T4N(25),T5N(25),
     *  IICFR(1),IICFL(1),IICFT(1),IICFB(1)
     *   ,ZERO1(1165),ZERO2(608),ZERO3(16),ZERO4(3)
      DIMENSION ZSIE(22),ZTQ(22),ZTS(22),ZVP(22),ZLQ(22),ZAP(22),WSP(22)RGBVM62A
      DIMENSION TRSTRT(5),WZSIE(100),WZTQ(100),WZTS(100)         RGBVM55A
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```
A,WZVP(100),WZLQ(100),WZAP(100),WWSP(100)                                RGBVM62A
 COMMON/VRCOM/A(14000)                                                   RGBMN60A
 COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ,      RGBVM55A
AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                        RGBMN60A
B,WSP,WWSP,BKGND,DWNDS                                                   RGBMN60B
 COMMON /VRCON/ ALP,ALPO,ALX,ALZ,BO,BETA,BUFL,CFI(9),CFS(9),CYL,
1   DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2   IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3   IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
4   LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5   TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
*  ,USR(32),UST(22),USB(22),USO(10),FFX3,FFY3
6   ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7   TO,SIEI,IDG,KDG,TI,MAT,RHOO,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8   T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9   COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
*   OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1   USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*  ,CSUBPO,EPSO,RDXDZS,RLENGH ,TQJET,TSJET
 COMMON /FLMCON/ DROU,DROUO,IPRFM
 COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
1                 ,VMIN
  COMMON/PROP/SIGN
 COMMON/EXTRA/NT3,NT4,NT5,TYMT3,TYMT4,TYMT5,T3N,T4N,T5N,COFBD,
1COFBE,COFBF,COFTD,COFTE,COFTF,COFRD,COFRE,COFRF,COFLD,COFLE,
2COFLF,OFOBTD,OFOBTE,OFOBTF,OFOBRD,OFOBRE,OFOBRF,IRESET,
*NCYCLS,TADD,NIV,IOBRAN
  COMMON/INDEX/NWPCL,K2NCL
  COMMON/LARGE/DIFFCO(2400)
 EQUIVALENCE (A(1),CF),(A(2),U),(A(3),W),(A(4),P),(A(5),TQ),
1    (A(6),TS),(A(7),ER,CQ),(A(8),UO),(A(9),WO),(A(10),TQO),
2    (A(11),TSO),(A(12),SIE),(A(13),SIEO),(A(14),RX),(A(15),RZ),
3    (A(16),IICFR),(A(17),IICFL),(A(18),IICFT),(A(19),IICFB),
A    (A(20),CHI),(A(21),CHIO),                                           RGBMN01A
B    (A(22),VAP),(A(23),VAPO),(A(24),LIQ),(A(25),LIQO),                  RGBMN60A
4    (ZERO1(1),ALP),(ZERO2(1),NT3),(ZERO3(1),AI),(ZERO4(1),DROU)
```

```
      ENTRY TAPREA
      REWIND 8
       READ(8) A,ZERO1,ZERO2,ZERO4,NWPCL
      WRITE(IVDO,50) TD,TIMET,NCYC
      IDATIN=1
      NCYCB=NCYC
      IRSTRT=1
C *****FORMATS ***** FORMATS ***** FORMATS *****
 50   FORMAT(1H ,19H TAPE FILE NUMBER =,I4,9H  TIMET =,1PE12.4,
     1   16H  CYCLE NUMBER =,I6)
      RETURN
      ENTRY TAPWRI
      TD=TD+1
      ITW=ITAPW
      REWIND 8
      WRITE(8) A,ZERO1,ZERO2,ZERO4,NWPCL
      WRITE(IVDO,51) TD,TIMET,NCYC
C *****FORMATS ***** FORMATS ***** FORMATS *****
 51   FORMAT(1H ,19H TAPE FILE NUMBER =,I4,9H  TIMET =,1PE12.4,
     1   16H  CYCLE NUMBER =,I6)
      RETURN
      ENTRY COARSE                                                  RGBID55A
C  RESTART ON A COARSER MESH FOR IBR AND KBR EVEN ONLY              RGBID55A
      IHALF=IBP2/2                                                  RGBID55A
      KHALF=KBP2/2                                                  RGBID55A
C  MANAGES ATMOSPHERIC PROFILES DURING RESTARTS ON A COARSER MESH   RGBID55A
      DO 90 K=2,KHALF                                               RGBID55A
      ZTQ(K)=(ZTQ(2*K-2)+ZTQ(2*K-1))/2.0                            RGBID55A
      ZTS(K)=(ZTS(2*K-2)+ZTS(2*K-1))/2.0                            RGBID55A
      ZLQ(K)=(ZLQ(2*K-2)+ZLQ(2*K-1))/2.0                            RGBID70A
      ZVP(K)=(ZVP(2*K-2)+ZVP(2*K-1))/2.0                            RGBID70A
      ZAP(K)=(ZAP(2*K-2)+ZAP(2*K-1))/2.0                            RGBID70A
      WSP(K)=(WSP(2*K-2)+WSP(2*K-1))/2.0                            RGBID70A
 90   ZSIE(K)=(ZSIE(2*K-2)+ZSIE(2*K-1))/2.0                         RGBID55A
      ZSIF(1)=ZSIE(2)                                               RGBID55A
      ZTS(1)=ZTS(2)                                                 RGBID55A
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```
      ZTQ(1)=ZTQ(2)                                                     RGBID55A
      ZLQ(1)=ZLQ(2)                                                     RGBID70A
      ZVP(1)=ZVP(2)                                                     RGBID70A
      ZAP(1)=ZAP(2)                                                     RGBID70A
      WSP(1)=WSP(2)                                                     RGBID70A
      KHP1=KHALF+1                                                      RGBID55A
      DO 95 K=KHP1,KBP1                                                 RGBID55A
      ZTQ(K)=WZTQ((NRSTRT*KBR/2)+K-1)                                   RGBID55A
      ZTS(K)=WZTS((NRSTRT*KBR/2)+K-1)                                   RGBID55A
      ZLQ(K)=WZLQ((NRSTRT*KBR/2)+K-1)                                   RGBID70A
      ZVP(K)=WZVP((NRSTRT*KBR/2)+K-1)                                   RGBID70A
      ZAP(K)=WZAP((NRSTRT*KBR/2)+K-1)                                   RGBID70A
      WSP(K)=WWSP((NRSTRT*KBR/2)+K-1)                                   RGBID70A
   95 ZSIE(K)=WZSIE((NRSTRT*KBR/2)+K-1)                                 RGBID55A
      ZSIE(KBP2)=ZSIE(KBP1)                                             RGBID55A
      ZTS(KBP2)=ZTS(KBP1)                                               RGBID55A
      ZTQ(KBP2)=ZTQ(KBP1)                                               RGBID55A
      ZLQ(KBP2)=ZLQ(KBP1)                                               RGBID70A
      ZVP(KBP2)=ZVP(KBP1)                                               RGBID70A
      ZAP(KBP2)=ZAP(KBP1)                                               RGBID70A
      WSP(KBP2)=WSP(KBP1)                                               RGBID70A
C  RECOMPUTES DATA ASSOCIATED WITH DZ, DX FOR USE IN VM                 RGBID55A
      DX=2.0*DX                                                         RGBID55A
      DZ=2.0*DZ                                                         RGBID55A
      RDX=1./DX                                                         RGBID55A
      RDZ=1./DZ                                                         RGBID55A
      HDX=.5*DX                                                         RGBID55A
      HDZ=.5*DZ                                                         RGBID55A
      RDZS=1./(DZ*DZ)                                                   RGBID55A
      BETA=.5*BO/(RDX*RDX+RDZ*RDZ)                                      RGBID55A
      EPSB=4.*NU/AMIN1(DX,DZ)                                           RGBID55A
      RDXDZS=1./(RDX*RDX+RDZ*RDZ)                                       RGBID55A
      X1=FLOAT(IBR)*DX                                                  RGBID55A
      Z1=FLOAT(KBR)*DZ                                                  RGBID55A
      RLENGH=1./AMAX1(X1,Z1)                                            RGBID55A
C  BEGINS CELL BY CELL AVERAGING                                        RGBID55A
```

```
      DO 100 I=2,IBP1                                                   RGBID55A
      DO 100 K=2,KBP1                                                   RGBID55A
      IK=1+NWPC*(((I-1)*KBP2)+K-1)                                      RGBID55A
      IF(I.GT.IHALF.OR.K.GT.KHALF) GO TO 200                            RGBID55A
C   COMPUTES INDICES FOR FLUID CELLS                                    RGBID55A
      J=2*(I-1)                                                         RGBID55A
      L=2*(K-1)                                                         RGBID55A
      IKR=1+NWPC*(((J-1)*KBP2)+L-1)                                     RGBID55A
      J=2*I-1                                                           RGBID55A
      IPKR=1+NWPC*(((J-1)*KBP2)+L-1)                                    RGBID55A
      L=2*K-1                                                           RGBID55A
      IPKPR=1+NWPC*(((J-1)*KBP2)+L-1)                                   RGBID55A
      J=2*(I-1)                                                         RGBID55A
      IKPR=1+NWPC*(((J-1)*KBP2)+L-1)                                    RGBID55A
C   COMPUTES FLUID CELL DENSITIES FOR CELL MASS AVERAGING               RGBID55A
      CIT=CI-SIE(IKR)                                                   RGBID55A
      TEMPLL=SI(AI,BI,CIT,-1)                                           RGBID55A
      CIT=CI-SIE(IPKR)                                                  RGBID55A
      TEMPLR=SI(AI,BI,CIT,-1)                                           RGBID55A
      CIT=CI-SIE(IKPR)                                                  RGBID55A
      TEMPUL=SI(AI,BI,CIT,-1)                                           RGBID55A
      CIT=CI-SIE(IPKPR)                                                 RGBID55A
      TEMPUR=SI(AI,BI,CIT,-1)                                           RGBID55A
      RHOLL=AR*TEMPLL*TEMPLL+BR*TEMPLL+CR                               RGBID55A
      RHOLR=AR*TEMPLR*TEMPLR+BR*TEMPLR+CR                               RGBID55A
      RHOUL=AR*TEMPUL*TEMPUL+BR*TEMPUL+CR                               RGBID55A
      RHOUR=AR*TEMPUR*TEMPJR+BR*TEMPUR+CR                               RGBID55A
      RHOSUM=RHOLL+RHOLR+PHOUL+RHOUR                                    RGBID55A
C   MASS AVERAGING OF FLUID CELLS FOR RESTART ON COARSER MESH           RGBID55A
      U(IK)=(U(IKR)*RHOLL+U(IPKR)*RHOLR+U(IKPR)*RHOUL+U(IPKPR)*RHOUR)/RHRGBID55A
     AOSUM                                                              RGBID55A
      UO(IK)=(UO(IKR)*RHOLL+UO(IPKR)*RHOLR+UO(IKPR)*RHOUL+UO(IPKPR)     RGBID55A
     A*RHOUR)/RHOSUM                                                    RGBID55A
      W(IK)=(W(IKR)*RHOLL+W(IPKR)*RHOLR+W(IKPR)*RHOUL+W(IPKPR)*RHOUR)/RHRGBID55A
     AOSUM                                                              RGBID55A
      WO(IK)=(WO(IKR)*RHOLL+WO(IPKR)*RHOLR+WO(IKPR)*RHOUL+WO(IPKPR)     RGBID55A
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```
     A*RHOUR)/RHOSUM                                                      RGBID55A
      TS(IK)=(TS(IKR)+TS(IPKR)+TS(IKPR)+TS(IPKPR))/4.00                   RGBID55A
      TSO(IK)=(TSO(IKR)+TSO(IPKR)+TSO(IKPR)+TSO(IPKPR))/4.0               RGBID55A
      TQ(IK)=(TQ(IKR)*RHOLL+TQ(IPKR)*RHOLR+TQ(IKPR)*RHOUL+TQ(IPKPR)       RGBID55A
     A*RHOUR)/RHOSUM                                                      RGBID55A
      TQO(IK)=(TQO(IKR)*RHOLL+TQO(IPKR)*RHOLR+TQO(IKPR)*RHOUL+TQO(IPKPR)RGBID55A
     A*RHOUR)/RHOSUM                                                      RGBID55A
      SIE(IK)=(SIE(IKR)*RHOLL+SIE(IPKR)*RHOLR+SIE(IKPR)*RHOUL+SIE(IPKPR)RGBID55A
     A*RHOUR)/RHOSUM                                                      RGBID55A
      SIEO(IK)=(SIEO(IKR)*RHOLL+SIEO(IPKR)*RHOLR+SIEO(IKPR)*RHOUL+SIEO(IRGBID55A
     APKPR)*RHOUR)/RHOSUM                                                 RGBID55A
      CHI(IK)=(CHI(IKR)+CHI(IPKR)+CHI(IKPR)+CHI(IPKPR))/4.0               RGBID55A
      CHIO(IK)=(CHIO(IKR)+CHIO(IPKR)+CHIO(IKPR)+CHIO(IPKPR))/4.0          RGBID55A
      VAP(IK)=(VAP(IKR)+VAP(IPKR)+VAP(IKPR)+VAP(IPKPR))/4.0               RGBID70A
      VAPO(IK)=(VAPO(IKR)+VAPO(IPKR)+VAPO(IKPR)+VAPO(IPKPR))/4.0          RGBID70A
      LIQ(IK)=(LIQ(IKR)+LIQ(IPKR)+LIQ(IKPR)+LIQ(IPKPR))/4.0               RGBID70A
      LIQO(IK)=(LIQO(IKR)+LIQO(IPKR)+LIQO(IKPR)+LIQO(IPKPR))/4.0          RGBID70A
      P(IK)=0.0                                                           RGBID55A
      GO TO 100                                                           RGBID55A
C  INITIALIZATION OF CELLS THAT WEREN'T IN THE PREVIOUS RUN              RGBID55A
  200 U(IK)=0.0                                                           RGBID55A
      UO(IK)=0.0                                                          RGBID55A
      W(IK)=0.0                                                           RGBID55A
      WO(IK)=0.0                                                          RGBID55A
      SIE(IK)=ZSIE(K)                                                     RGBID55A
      SIEO(IK)=ZSIE(K)                                                    RGBID55A
      TS(IK)=ZTS(K)                                                       RGBID55A
      TSO(IK)=ZTS(K)                                                      RGBID55A
      TQ(IK)=ZTQ(K)                                                       RGBID55A
      TQO(IK)=ZTQ(K)                                                      RGBID55A
      CHI(IK)=BKGND                                                       RGBVM70A
      CHIO(IK)=BKGND                                                      RGBVM70A
      LIQ(IK)=ZLQ(K)                                                      RGBVM70A
      LIQO(IK)=ZLQ(K)                                                     RGBVM70A
      VAP(IK)=ZVP(K)                                                      RGBVM70A
      VAPO(IK)=ZVP(K)                                                     RGBVM70A
```

```
      P(IK)=0.0                                                      RGBID55A
  100 CONTINUE                                                       RGBID55A
      RETURN                                                         RGBID55A
      ENTRY FILMCO
      RETURN
      ENTRY FLMCAL
      RETURN
      ENTRY  FLMINI
      RETURN
      ENTRY  FLMFIN
      RETURN
      ENTRY FLMGEN
      RETURN
      ENTRY VREQ
      RETURN
      ENTRY VRFLM
      RETURN
      END
      FUNCTION SI(XTBL,YTBL,X,N)
      COMMON/PROP/SIGN
      DIMENSION XTBL(1),YTBL(1)
      IF( N.LT.0 ) GO TO 200
      IF(X.LT.XTBL(1)) GO TO 16
      IF(X.GT.XTBL(N)) GO TO 31
      DO 10 I=1,N
      IF(X.EQ.XTBL(I)) GO TO 21
      IF(X.LT.XTBL(I)) GO TO 26
   10 CONTINUE
   16 J1 = 1
      J2 = 2
      GO TO 50
   21 SI = YTBL(I)
      GO TO 100
   26 J1 = I-1
      J2 = I
      GO TO 50
```

```
   31 J1 = N-1
      J2 = N
   50 SI=YTBL(J1)+(YTBL(J2)-YTBL(J1))*(X-XTBL(J1))/(XTBL(J2)-XTBL(J1))
  100 RETURN
C NOTE. ROOTS OF QUADRATIC EQUATION - A*X**2 + B*X + C =0.0 .
  200 A=XTBL(1)
      B=YTBL(1)
      C=X
       IF(A.NE.0.0) GO TO 205
       SI=-1.0*C/B
       RETURN
 205   CONTINUE
      D=B*B - 4.*A*C
      IF( D ) 210,220,220
  210 PRINT 211
      RETURN
  220 DS=SQRT( D )
      IF (SIGN) 224,224,226
  224 SI = -1.0 * (B + DS) / (2.0 * A)
      GO TO 230
  226 SI = (DS - B) / (2.0 * A)
      GO TO 230
  230 CONTINUE
      RETURN
C ***** FORMATS ***** FORMATS ***** FORMATS ***** .                OLAY0029
  211 FORMAT(1H ,28H ERROR - ROOTS ARE COMPLEX .)
      END
      SUBROUTINE VRPRT
      DIMENSION TPT(50,50)
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1VTP,CFOUT
      REAL NU,LIQ,LIQO,LIQI,LOUT                                    RGBMN60A
      DIMENSION UOUT(7),VOUT(7),IOUT(7),KOUT(7),CFOUT(7),QOUT(7),
     1SOUT(7),TOUT(7),XOUT(7),GOUT(7),LOUT(7)                       RGBMO60A
      DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
     1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
```

```
2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                            RGBMN01A
A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                                    RGBMN60A
3   ,TYMF(25),FN(25),TYMT1(25),T1N(25),TYMT2(25),T2N(25),
4   COFBA(25),COFBB(25),COFBC(25),COFTA(25),COFTB(25),COFTC(25),
5   COFRA(25),COFRB(25),COFRC(25),COFLA(25),COFLB(25),COFLC(25),
6   OFOBTA(25),OFOBTB(25),OFOBTC(25),
7   OFOBRA(25),OFOBRB(25),OFOBRC(25),TAU(10),USL(32),USLOB(20),
8   USROB(20),USTOB(20),USBOB(20)
9,COFBD(25),COFBE(25),COFTD(25),COFTE(25),COFTF(25),COFBF(25),
*COFRD(25),COFRE(25),COFLD(25),COFLE(25),COFRF(25),COFLF(25),
AOFOBTD(25),OFOBTE(25),OFOBRD(25),OFOBRE(25),
B  OFOBTF(25),OFOBRF(25),
CTYMT3(25),TYMT4(25),TYMT5(25),T3N(25),T4N(25),T5N(25),
*  IICFR(1),IICFL(1),IICFT(1),IICFB(1)
*   ,ZERO1(1165),ZERO2(608),ZERO3(16),ZERO4(3)
 DIMENSION ZSIE(22),ZTQ(22),ZTS(22),ZVP(22),ZLQ(22),ZAP(22),WSP(22)RGBVM62A
 DIMENSION TRSTRT(5),WZSIE(100),WZTQ(100),WZTS(100)                 RGBVM55A
A,WZVP(100),WZLQ(100),WZAP(100),WWSP(100)                          RGBVM62A
 COMMON/VRCOM/A(14000)                                              RGBMN60A
 COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ,  RGBVM55A
AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                  RGBMN60A
B,WSP,WWSP,BKGND,DWNDS                                             RGBMN60B
 COMMON /VRCON/ ALP,ALPO,ALX,ALZ,BO,BETA,BUFL,CFI(9),CFS(9),CYL,
1   DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2   IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3   IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
4   LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5   TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
*  ,USR(32),UST(22),USB(22),USO(10),FFX3,FFY3
6   ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7   TO,SIEI,IDG,KDG,TI,MAT,RHOO,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8   T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9   COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
*   OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1   USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*  ,CSUBPO,EPSO,RDXDZS,RLENGH ,TQJET,TSJET
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```
      COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
     1                ,VMIN
       COMMON/PROP/SIGN
      COMMON/EXTRA/NT3,NT4,NT5,TYMT3,TYMT4,TYMT5,T3N,T4N,T5N,COFBD,
     1COFBE,COFBF,COFTD,COFTE,COFTF,COFRD,COFRE,COFRF,COFLD,COFLE,
     2COFLF,OFOBTD,OFOBTE,OFOBTF,OFOBRD,OFOBRE,OFOBRF,IRESET,
     *NCYCLS,TADD,NIV,IOBRAN
       COMMON/INDEX/NWPCL,K2NCL
      COMMON /FLMCON/ DROU,DROUO,IPRFM
       COMMON/LARGE/DIFFCO(2400)
      EQUIVALENCE (A(1),CF),(A(2),U),(A(3),W),(A(4),P),(A(5),TQ),
     1   (A(6),TS),(A(7),ER,CQ),(A(8),UO),(A(9),WO),(A(10),TQO),
     2   (A(11),TSO),(A(12),SIE),(A(13),SIEO),(A(14),RX),(A(15),RZ),
     3   (A(16),IICFR),(A(17),IICFL),(A(18),IICFT),(A(19),IICFB),
     A   (A(20),CHI),(A(21),CHIO),                                       RGBMN01A
     B   (A(22),VAP),(A(23),VAPO),(A(24),LIQ),(A(25),LIQO),              RGBMN60A
     4   (ZERO1(1),ALP),(ZERO2(1),NT3),(ZERO3(1),AI),(ZERO4(1),DROU)
C NOTE. END - END OF NON-EXECUTABLE STATEMENTS .
C     PRODUCES A CELL BY CELL OUTPUT OF STORED VARIABLES (22 X 22 ONLY)
      WRITE(IVDO,5)
   96 DO 103 ILOOP=1,4
      IREST=(ILOOP-1)*5
   97 DO 102 KLOOP=1,5
      KREST=(KLOOP-1)*5
   98 DO 100 KINV=1,5
      K=23-KINV-KREST
      IF(K.EQ.0) GO TO 101
      DO 99 IPART=1,7
      I=IPART+IREST
      IK=1+NWPC*(((I-1)*KBP2)+K-1)
      UOUT(IPART)=U(IK)
      VOUT(IPART)=W(IK)
      IOUT(IPART)=I
      KOUT(IPART)=K
      CFOUT(IPART)=CF(IK)
      QOUT(IPART)=TQ(IK)
```

```
      SOUT(IPART)=TS(IK)
      XOUT(IPART)=CHI(IK)                                    RGBM001A
      GOUT(IPART)=VAP(IK)                                    RGBM060A
      LOUT(IPART)=LIQ(IK)                                    RGBM060A
      SIEC=SIE(IK)
      CIT=CI-SIEC
      TOUT(IPART)=SI(AI,BI,CIT,-1)
      IF(CF(IK).GE.30)  TOUT(IPART)=P(IK)
   99 CONTINUE
      WRITE(IVDO,20)  (VOUT(L),L=1,7)
      WRITE(IVDO,10)
      WRITE(IVDO,30)  (IOUT(L),KOUT(L),L=1,7)
      WRITE(IVDO,40)  (TOUT(L),L=1,7)
      WRITE(IVDO,10)
      WRITE(IVDO,50)  (CFOUT(L),UOUT(L),L=1,7)
      WRITE(IVDO,70)  (SOUT(L),L=1,7)
      WRITE(IVDO,60)  (QOUT(L),L=1,7)
      WRITE(IVDO,80)  (XOUT(L),L=1,7)                        RGBM001A
      WRITE(IVDO,85)  (GOUT(L),L=1,7)                        RGBM060A
      WRITE(IVDO,90)  (LOUT(L),L=1,7)                        RGBM060A
  100 CONTINUE
  101 WRITE(IVDO,7)  TIMET,NCYC,ITER,DT
      WRITE(IVDO,5)
  102 CONTINUE
  103 CONTINUE
      RETURN
    5 FORMAT('1')
    7 FORMAT(1H ,5HTIME=,1PE12.4,3H , ,14HCYCLE NUMBER =,I5,3H , ,
     1 28H PRESSURE ITERATION NUMBER =,I4,3H , ,4HDT =,E12.4)
   10 FORMAT(' ',7('X',17X))
   20 FORMAT(' ',7(5HXXXXX,1X,F7.3,1X,4HXXXX))
   30 FORMAT(' ',7(1HX,5X,'(',I2,',',I2,')',5X))
   40 FORMAT(' ',7(1HX,3X,F7.3,1X,' F',4X))
   50 FORMAT(' ',3X,7(4X,I2,5X,F7.3))
   60 FORMAT(' ',7(1HX,2X,'TKE=',1PE10.3,1X))
   70 FORMAT(' ',7(1HX,2X,'TNU=',1PE10.3,1X))
```

```
80   FORMAT(' ',7(1HX,2X,'CHI=',1PE10.3,1X))                          RGBM001A
85   FORMAT(' ',7(1HX,2X,'VAP=',1PE10.3,1X))                          RGBM060A
90   FORMAT(' ',7(1HX,2X,'LIQ=',1PE10.3,1X))                          RGBM060A
     END
     SUBROUTINE VSET
     INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
    1   VTP
     REAL NU,LIQ,LIQO,LIQI,LOUT                                        RGBMN60A
     DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
    1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
    2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                          RGBMN01A
    A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                                    RGBMN60A
    3   ,TYMF(25),FN(25),TYMT1(25),T1N(25),TYMT2(25),T2N(25),
    4   COFBA(25),COFBB(25),COFBC(25),COFTA(25),COFTB(25),COFTC(25),
    5   COFRA(25),COFRB(25),COFRC(25),COFLA(25),COFLB(25),COFLC(25),
    6   OFOBTA(25),OFOBTB(25),OFOBTC(25),
    7   OFOBRA(25),OFOBRB(25),OFOBRC(25),TAU(10),USL(32),USLOB(20),
    8   USROB(20),USTOB(20),USBOB(20)
    9,COFBD(25),COFBE(25),COFTD(25),COFTE(25),COFTF(25),COFBF(25),
    *COFRD(25),COFRE(25),COFLD(25),COFLE(25),COFRF(25),COFLF(25),
    AOFOBTD(25),OFOBTE(25),OFOBRD(25),OFOBRE(25),
    B  OFOBTF(25),OFOBRF(25),
    CTYMT3(25),TYMT4(25),TYMT5(25),T3N(25),T4N(25),T5N(25),
    4  IICFR(1),IICFL(1),IICFT(1),IICFB(1)
    *   ,ZERO1(1165),ZERO2(608),ZERO3(16),ZERO4(3)
     DIMENSION ZSIE(22),ZTQ(22),ZTS(22),ZVP(22),ZLQ(22),ZAP(22),WSP(22)RGBVM62A
     DIMENSION TRSTRT(5),WZSIE(100),WZTQ(100),WZTS(100)               RGBVM55A
    A,WZVP(100),WZLQ(100),WZAP(100),WWSP(100)                          RGBVM62A
     COMMON/VRCOM/A(14000)                                              RGBMN60A
     COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ, RGBVM55A
    AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                  RGBMN60A
    B,WSP,WWSP,BKGND,DWNDS                                              RGBMN60B
     COMMON /VRCON/ ALP,ALPO,ALX,ALZ,BO,BETA,BUFL,CFI(9),CFS(9),CYL,
    1   DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
    2   IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
    3   IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
```

```
     4   LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
     5   TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
     *  ,USR(32),UST(22),USB(22),USO(10),FFX3,FFY3
     6   ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
     7   TO,SIEI,IDG,KDG,TI,MAT,RHOO,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
     8   T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
     9   COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
     *   OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
     1   USLOB,USROB,USTOB,USBOB,UMAX,WMAX
     *  ,CSUBPO,EPSO,RDXDZS,FLENGH ,TQJET,TSJET
      COMMON /FLMCON/ DROU,DROUO,IPRFM
      COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
     1                 ,VMIN
       COMMON/PROP/SIGN
      COMMON/EXTRA/NT3,NT4,NT5,TYMT3,TYMT4,TYMT5,T3N,T4N,T5N,COFBD,
     1COFBE,COFBF,COFTD,COFTE,COFTF,COFRD,COFRE,COFRF,COFLD,COFLE,
     2COFLF,OFOBTD,OFOBTE,OFOBTF,OFOBRD,OFOBRE,OFOBRF,IRESET,
     *NCYCLS,TADD,NIV,IOBRAN
       COMMON/INDEX/NWPCL,K2NCL
       COMMON/LARGE/DIFFCO(2400)
      EQUIVALENCE (A(1),CF),(A(2),U),(A(3),W),(A(4),P),(A(5),TQ),
     1    (A(6),TS),(A(7),ER,CQ),(A(8),UO),(A(9),WO),(A(10),TQO),
     2    (A(11),TSO),(A(12),SIE),(A(13),SIEO),(A(14),RX),(A(15),RZ),
     3    (A(16),IICFR),(A(17),IICFL),(A(18),IICFT),(A(19),IICFB),
     A    (A(20),CHI),(A(21),CHIO),                             RGBMN01A
     B    (A(22),VAP),(A(23),VAPO),(A(24),LIQ),(A(25),LIQO),    RGBMN60A
     4    (ZERO1(1),ALP),(ZERO2(1),NT3),(ZERO3(1),AI),(ZERO4(1),DROU)
C NOTE. END - END OF NON-EXECUTABLE STATEMENTS .
C
C
C NOTE. VSET IS RESPONSIBLE FOR MESH,PARTICLE AND FILM INITIALIZATION .
C
      IDATIN=0
      IF( IBR.EQ.0 ) CALL TAPREA
C NOTE. READS,WRITES PRIMARY INPUT DATA .
      READ(IVDI,1) LABEL
```

```
      READ(IVDI,2)    DT,TPRT,TPLT,TWTD,TFIN,ITAPW,NPRT,IDIAG,LPR,IOBS
     1 ,IDG,KDG
      WRITE(IVDO,50) IBR,KBR,IPRFM,NCYCLS,TADD,IRESET
      WRITE(IVDO,1) LABEL
      WRITE(IVDO,51) DT,TPRT,TPLT,TWTD,TFIN,ITAPW,NPRT,IDIAG,LPR,IOBS
     1 ,IDG,KDG
      RDT=1./DT
      IF( IPRFM.LT.1 ) TPLT=2.*TFIN
      TPL=TPLT
      TPR=TPRT
      TTD=TWTD
      IF( IDATIN.LT.1 ) GO TO 100
      TIMET=TIMET+TADD
      TWTD=TIMET
      TPRT=TWTD
      TPLT=TPRT
      CALL MESHMK
      IF (IPRFM.LT.1) GO TO 500
      CALL FLMGEN
      CALL FILMCO
      GO TO 500
C NOTE. INITIALIZES CONSTANTS .
  100 TIMET=0.0
      IRSTRT=0
      TD=0                                                      VRS12001
      NCYC=0                                                    VRS12002
      NCYCB=0
      EM6=1.E-6                                                 VRS12014
C NOTE. INITIALIZES CELL INDEX QUANTITIES .
      IBP1=IBR + 1
      KBP1=KBR+1                                                VRS12402
      IBP2=IBR+2                                                VRS12404
      KBP2=KBR+2                                                VRS12406
      I2K2=IBP2*KBP2*NWPC                                       VRS12408
      KNC=KBR*NWPC
      K2NC=KBP2*NWPC                                            VRS12412
```

```
      K2NCL = KBP2 * NWPCL
      IKP2=IBR*K2NC                                        VRS12420
      IKMK =I2K2 + 2*K2NC
      RIBKB= 1./FLOAT(IBR*KBR)
C NOTE. GENERATES BOTH MESH AND FILM REGIONS , RESPECTIVELY .
      CALL MESHMK
      IF( IPRFM.LT.1 ) GO TO 2000
      CALL FLMGEN
      CALL FILMCO
2000  WRITE(IVDO,60)
  500  K2NCL=KBP2*NWPCL
      WRITE (IVDO,70)
       WRITE(IVDO,80)
      I1=2
      K1=2
      I2=IBP1
      K2 = KBP1
      KKL = 0
      KK = 0
      DO 511 I=I1,I2
      KK = KK + K2NC
      KKL = KKL + K2NCL
      LWPC = 1
      LWPCL = 1
      DO 510 K=K1,K2
      LWPC = LWPC + NWPC
      LWPCL = LWPCL + NWPCL
      IK = KK + LWPC
      IKL = KKL + LWPCL
      IPK = IK + K2NC
      IMK = IK - K2NC
      IKP = IK + NWPC
      IKM = IK - NWPC
      CPC = CP(IK)
      CPR = CP (IPK)
      CPL = CP(IMK)
```

```
      CFT = CF(IKP)
      CFB = CF(IKM)
      IF (CFC.NE.1) GO TO 510
      IF (CFR.NE.1) DIFFCO( IKL  ) = 0.0
      IF (CFL.NE.1) DIFFCO(IKL+2)= 0.0
      IF (CFT.NE.1) DIFFCO( IKL+1) = 0.0
      IF (CFB.NE.1) DIFFCO( IKL+3) = 0.0
      DCR = DIFFCO(IKL)
      DCT = DIFFCO(IKL+1)
      DCL = DIFFCO(IKL+2)
      DCB = DIFFCO(IKL+3)
       WRITE(IVDO,75) I,K,IK,IKL,CFC,CFR,CFT,CFL,CFB,DCR,DCT,DCL,DCB
  510 CONTINUE
 511  CONTINUE
  520 RETURN
C ***** FORMATS ***** FORMATS ***** FORMATS ***** .
    1 FORMAT(20A4)
    2 FORMAT(5F8.3,5I2,2I3)
 50   FORMAT(1H ,4X,4HIBR=,I5,/,5X,4HKBR=,I5,/,3X,6HIPRFM=,I2,/,5X,
     1 8HNCYCLST=,I10,/,5X,5HTADD=,E12.5,5X,7HIRESET=,I5)
   51 FORMAT(1H ,5X,3HDT=,1PE12.5/4X,5HTPRT=,E12.5/4X,5HTPLT=,E12.5/
     1 4X,5HTWTD=,E12.5/4X,5HTFIN=,E12.5/3X,6HITAPW=,I2/4X,5HNPRT=,I2/
     2 3X,6HIDIAG=,I2/5X,4HLPR=,I2/4X,5HIOBS=,I2/5X,4HIDG=,I3/5X,4HKDG=,
     3 I3)
   52 FORMAT(1H ,104H *** ERROR 001 - MESH ARRAY A() IS DIMENSIONED TOO
     1SMALL FOR MESH PARAMETERS ,I.E.   IBR  AND  KBR . ***)
   60 FORMAT(1H ,63H NOTE. COMPLETION OF     VSET     - VARR II SET UP G
     1ENERATION .)
  70  FORMAT(1H1)
 75    FORMAT(1H ,9I6,4F6.1)
 80    FORMAT(1H ,5X,1HI,5X,1HK,4X,2HIK,3X,3HIKL,3X,3HCFC,3X,3HCFR,3X,
     1 3HCFT,3X,3HCFL,3X,3HCFB,3X,3HDCR,3X,3HDCT,3X,3HDCL,3X,3HDCB)
      END                                                               VRS99999
      SUBROUTINE MESHMK
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1   VTP
```

```
 REAL NU,LIQ,LIQO,LIQI,LOUT                                             RGBMN60A
 DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                                RGBMN01A
A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                                         RGBMN60A
3   ,TYMF(25),FN(25),TYMT1(25),T1N(25),TYMT2(25),T2N(25),
4   COFBA(25),COFBB(25),COFBC(25),COFTA(25),COFTB(25),COFTC(25),
5   COFRA(25),COFRB(25),COFRC(25),COFLA(25),COFLB(25),COFLC(25),
6   OFOBTA(25),OFOBTB(25),OFOBTC(25),
7   OFOBRA(25),OFOBRB(25),OFOBRC(25),TAU(10),USL(32),USLOB(20),
8   USROB(20),USTOB(20),USBOB(20)
9,COFBD(25),COFBE(25),COFTD(25),COFTE(25),COFTF(25),COFBF(25),
*COFRD(25),COFRE(25),COFLD(25),COFLE(25),COFRF(25),COFLF(25),
AOFOBTD(25),OFOBTE(25),OFOBRD(25),OFOBRE(25),
B  OFOBTF(25),OFOBRF(25),
CTYMT3(25),TYMT4(25),TYMT5(25),T3N(25),T4N(25),T5N(25),
*  IICFR(1),IICFL(1),IICFT(1),IICFB(1)
*   ,ZERO1(1165),ZERO2(608),ZERO3(16),ZERO4(3)
 DIMENSION ZSIE(22),ZTQ(22),ZTS(22),ZVP(22),ZLQ(22),ZAP(22),WSP(22)     RGBVM62A
 DIMENSION TRSTRT(5),WZSIE(100),WZTQ(100),WZTS(100)                     RGBVM55A
A,WZVP(100),WZLQ(100),WZAP(100),WWSP(100)                               RGBVM62A
 COMMON/VRCOM/A(14000)                                                  RGBMN60A
 COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ,      RGBVM55A
AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                       RGBMN60A
B,WSP,WWSP,BKGND,DWNDS                                                  RGBMN60B
 COMMON /VRCON/ ALP,ALPO,ALX,ALZ,BO,BETA,BUFL,CFI(9),CFS(9),CYL,
1   DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2   IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3   IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
4   LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5   TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
   ,USR(32),UST(22),USB(22),USO(10),FFX3,FFY3
6   ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7   TO,SIEI,IDG,KDG,TI,MAT,RHOO,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8   T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9   COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
```

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*     OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1     USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*     ,CSUBPO,EPSO,RDXDZS,RLENGH ,TQJET,TSJET
      COMMON /FLMCON/ DROU,DROUO,IPRFM
      COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
1                   ,VMIN
        COMMON/PROP/SIGN
      COMMON/EXTRA/NT3,NT4,NT5,TYMT3,TYMT4,TYMT5,T3N,T4N,T5N,COFBD,
     1COFBE,COFBF,COFTD,COFTE,COFTF,COFRD,COFRE,COFRF,COFLD,COFLE,
     2COFLF,OFOBTD,OFOBTE,OFOBTF,OFOBRD,OFOBRE,OFOBRF,IRESET,
     *NCYCLS,TADD,NIV,IOBRAN
        COMMON/INDEX/NWPCL,K2NCL
        COMMON/LARGE/DIFFCO(2400)
      EQUIVALENCE (A(1),CF),(A(2),U),(A(3),W),(A(4),P),(A(5),TQ),
1       (A(6),TS),(A(7),ER,CQ),(A(8),UO),(A(9),WO),(A(10),TQO),
2       (A(11),TSO),(A(12),SIE),(A(13),SIEO),(A(14),RX),(A(15),RZ),
3       (A(16),IICFR),(A(17),IICFL),(A(18),IICFT),(A(19),IICFB),
A       (A(20),CHI),(A(21),CHIO),                                  RGBMN01A
B       (A(22),VAP),(A(23),VAPO),(A(24),LIQ),(A(25),LIQO),         RGBMN60A
4       (ZERO1(1),ALP),(ZERO2(1),NT3),(ZERO3(1),AI),(ZERO4(1),DROU)
C NOTE. END - END OF NON-EXECUTABLE STATEMENTS .
C
C NOTE. MESHMK IS RESPONSIBLE FOR GENERATION OF MESH SUBREGIONS .
C NOTE. READS,WRITES PRIMARY MESH INPUT DATA .
      READ(IVDI,1)    DX,DZ,GX,GZ,ALX,ALZ,CYL,BO,EPS,VMIN          MESH   6
      READ (IVDI,2)  KWR,KWL,KWT,KWB,FSLIP,ALP,GAM,ALPO,GAM1,NU,TQJET,
     * TSJET
      READ(IVDI,7)    AW,BW,CW,WEPS,KDERBC,UBRI,UBLI,WBTI,WBBI
      READ(IVDI,8)    WOBI,UOBI,CSUBPO
      READ(IVDI,10)    TGAM,TO,TI,TSTEP,MAT,NRESEX
      READ(IVDI,1)    AI,BI,CI,AR,BR,CR,AMU,BMU,CMU
      READ (IVDI,1)  AK,BK,CK,ACP,BCP,CCP,SIGN
      READ(IVDI,11)  NFLOW,NT1,NT2,NT3,NT4,NT5,NTAU
      WRITE(IVDO,61)  NFLOW,NT1,NT2,NT3,NT4,NT5,NTAU
       IF(NFLOW.GT.0)  GO TO  190
       NIV=1.0
```

```
      NFLOW=-NFLOW
 190  CONTINUE
     READ(IVDI,12)    ( TYMF(I),FN(I),I=1,NFLOW )
     READ(IVDI,12)    ( TYMT1(I),T1N(I),I=1,NT1 )
     READ(IVDI,12)    ( TYMT2(I),T2N(I),I=1,NT2 )
      IF(NT3.EQ.0) GO TO 195
     READ(IVDI,12)  (TYMT3(I),T3N(I),I=1,NT3)
      IF(NT4.EQ.0) GO TO 195
     READ(IVDI,12)  (TYMT4(I),T4N(I),I=1,NT4)
      IF(NT5.EQ.0) GO TO 195
     READ(IVDI,12)  (TYMT5(I),T5N(I),I=1,NT5)
 195  CONTINUE
     IF( NTAU.LT.1 ) GO TO 200
     READ(IVDI,12)    ( TAU(I),I=1,NTAU )
C NOTE. READ COEFFICIENTS A,B, AND C FOR THE BOTTOM EXTERIOR BOUNDARY .
 200 READ(IVDI,13) I,COFA,COFB,COFC,COFD,COFE,COFF
     IF( I.LT.1 ) GO TO 210
     COFBA(I)=COFA
     COFBB(I)=COFB
     COFBC(I)=COFC
     COFBD(I)=COFD
     COFBE(I)=COFE
     COFBF(I)=COFF
     WRITE(IVDO,64) I,COFBA(I),COFBB(I),COFBC(I),COFBD(I),COFBE(I),
    1 COFBF(I)
     GO TO 200
C NOTE. READ COEFFICIENTS A,B, AND C FOR THE   TOP  EXTERIOR BOUNDARY .
 210 READ(IVDI,13) I,COFA,COFB,COFC,COFD,COFE,COFF
     IF( I.LT.1 ) GO TO 220
     COFTA(I)=COFA
     COFTB(I)=COFB
     COFTC(I)=COFC
     COFTD(I)=COFD
     COFTE(I)=COFE
     COFTF(I)=COFF
     WRITE(IVDO,64) I,COFTA(I),COFTB(I),COFTC(I),COFTD(I),COFTE(I),
```

```
    1  COFTF(I)
      GO TO 210
C NOTE. READ COEFFICIENTS A,B, AND C FOR THE RIGHT  EXTERIOR BOUNDARY .
 220  READ(IVDI,13) I,COFA,COFB,COFC,COFD,COFE,COFF
      IF( I.LT.1 ) GO TO 230
      COFRA(I)=COFA
      COFRB(I)=COFB
      COFRC(I)=COFC
      COFRD(I)=COFD
      COFRE(I)=COFE
      COFRF(I)=COFF
      WRITE(IVDO,64)  I,COFRA(I),COFRB(I),COFRC(I),COFRD(I),COFRE(I),
    1  COFRF(I)
      GO TO 220
C NOTE. READ COEFFICIENTS A,B, AND C FOR THE  LEFT  EXTERIOR BOUNDARY .
 230  READ(IVDI,13) I,COFA,COFB,COFC,COFD,COFE,COFF
      IF( I.LT.1 ) GO TO 240
      COFLA(I)=COFA
      COFLB(I)=COFB
      COFLC(I)=COFC
      COFLD(I)=COFD
      COFLE(I)=COFE
      COFLF(I)=COFF
      WRITE(IVDO,64) I,COFLA(I),COFLB(I),COFLC(I),COFLD(I),COFLE(I),
    1  COFLF(I)
      GO TO 230
C NOTE. READ COEFFICIENTS A,B, AND C FOR THE   TOP INTERIOR OBSTACLE .
 240  READ(IVDI,13) I,COFA,COFB,COFC,COFD,COFE,COFF
      IF( I.LT.1 ) GO TO 250
      OFOBTA(I)=COFA
      OFOBTB(I)=COFB
      OFOBTC(I)=COFC
      OFOBTD(I)=COFD
      OFOBTE(I)=COFE
      OFOBTF(I)=COFF
      WRITE(IVDO,64)  I,OFOBTA(I),OFOBTB(I),OFOBTC(I),OFOBTD(I),
```

```
     1OFOBTE(I),OFOBTF(I)
      GO TO 240
C NOTE. READ COEFFICIENTS A,B, AND C FOR THE RIGHT INTERIOR OBSTACLE .
 250  READ(IVDI,13) I,COFA,COFB,COFC,COFD,COFE,COFF
      IF( I.LT.1 ) GO TO 310
      OFOBRA(I)=COFA
      OFOBRB(I)=COFB
      OFOBRC(I)=COFC
      OFOBRD(I)=COFD
       OFOBRE(I)=COFE
      OFOBRF(I)=COFF
      WRITE(IVDO,64) I,OFOBRA(I),OFOBRB(I),OFOBRC(I),OFOBRD(I),
     1OFOBRE(I),OFOBRF(I)
      GO TO 250
  310 READ(IVDI,14)   I,K,RXC,RZC
      WRITE(IVDO,65)  I,K,RXC,RZC
      IF( I.LT.1 ) GO TO 320
      IK=(K-1)*NWPC + (I-1)*K2NC + 1
      RX(IK)=RXC
      RZ(IK)=RZC
      GO TO 310
  320 CONTINUE
      WRITE(IVDO,50) DX,DZ,GX,GZ,ALX,ALZ,CYL,BO,EPS,VMIN                MESH   8
      WRITE (IVDO,51) KWR,KWL,KWT,KWB,FSLIP,ALP,GAM,ALP0,GAM1,NU,TQJET,
     * TSJET
      WRITE(IVDO,59) AW,BW,CW,WEPS,KDERBC,UBRI,UBLI,WBTI,WBBI
      WRITE(IVDO,58) WOBI,UOBI,CSUBPO
      WRITE(IVDO,60)  TGAM,TO,TI,TSTEP,MAT,NRESEX
      WRITE(IVDO,52) AI,BI,CI,AR,BR,CR,AMU,BMU,CMU
      WRITE (IVDO,53) AK,BK,CK,ACP,BCP,CCP,SIGN
      WRITE(IVDO,61)  NFLOW,NT1,NT2,NTAU
      WRITE(IVDO,57)    ( TAU(I),I=1,NTAU )
      NMAX=AMAX0( NFLOW,NT1,NT2 )
      WRITE(IVDO,62)
      DO 319 I=1,NMAX
      WRITE(IVDO,63)  I,TYMF(I),FN(I),TYMT1(I),T1N(I),TYMT2(I),T2N(I)
```

```
  319 CONTINUE
       NMAX=AMAX0(NT3,NT4,NT5)
       DO 321 I=1,NMAX
      WRITE(IVDO,66) TYMT3(I),T3N(I),TYMT4(I),T4N(I),TYMT5(I),T5N(I)
 321   CONTINUE
C NOTE. GENERATION OF MESH CELL SIZES .
      RDX=1./DX                                                         VRS12004
      RDZ=1./DZ                                                         VRS12006
      HDX=.5*DX                                                         VRS12018
      HDZ=.5*DZ                                                         VRS12020
      RDZS=1./(DZ*DZ)
      BETA=.5*B0/(RDX*RDX + RDZ*RDZ)                                    VRS12022
      IF( KDERBC.GT.0 ) FSLIP=1.0
      IF( CYL.GT.1.E-6 ) KWL=1
      EPSB=4.*NU/AMIN1( DX,DZ )
      NTPAS=1
      IF( ALX.LT.EM6 .OR. ALZ.LT.EM6 ) NTPAS=2
      RDXDZS=1./( RDX*RDX + RDZ*RDZ )
      X1=FLOAT(IBR)*DX
      Z1=FLOAT(KBR)*DZ
      RLENGH=1./AMAX1( X1,Z1 )
      EPS0=EPS
      TR=TI + 459.7
C NOTE. CALCULATION OF SPECIFIC MATERIAL FOR SIE INITIAL AND RHO0 .
      GO TO( 400,420,440,460 ),MAT
C NOTE. COMPUTATION FOR SODIUM MATERIAL .
  400 SIEII=0.38935*TR - 0.553E-4*TR**2 + 0.1137E-7*TR**3 - 29.02
      RHOII=59.566 - 7.9504E-3*TI - .2872E-6*TI**2 + 0.06035E-9*TI**3
      RHO0=59.566 - 7.9504E-3*T0 - 0.2872E-6*T0**2 + 0.06035E-9*T0**3
      AT=397.17/TR + 1.0203
      TMU=(10.0**AT/3600.)/TR**0.4925
      NU=TMU/RHOII
      TK=0.015085 - 5.2167E-6*TI + 5.809E-10*TI**2
      CSUBP=0.38935 - 1.106E-4*TI + 0.3411E-7*TI**2
      RPRAN=TK/( CSUBP*TMU )
      GO TO 500
```

```
C NOTE. COMPUTATION FOR WATER MATERIAL .
  420 SIEII=1.0004*TI - 32.013
      RHOII=62.742 - 0.372E-2*TI - 0.44E-4*TI**2
      RHOO =62.742 - 0.372E-2*TO - 0.44E-4*TO**2
      BT=446.0/( TI+207.0 ) - 5.0
      TMU=1.622*10.**BT
      NU=TMU/RHOII
      TK=8.369E-5 + 2.368E-7*TI - 5.89E-10*TI**2
      CSUBP=1.0004
      RPRAN=TK/( CSUBP*TMU )
      GO TO 500
  440 SIEII=  AI*TI*TI +  BI*TI + CI
      RHOII=  AR*TI*TI +  BR*TI +  CR
      RHOO =  AR*TO*TO +  BR*TO +  CR
      TMU  = AMU*TI*TI + BMU*TI + CMU
      TK   =  AK*TI*TI +  BK*TI +  CK
      CSUBP= ACP*TI*TI + BCP*TI + CCP
      NU=TMU/RHOII
      RPRAN=TK/( CSUBP*TMU )
      GO TO 500
  460  CONTINUE
      NU=TMU/RHOII
      RPRAN=TK/( CSUBP*TMU )
C NOTE. NL=NUMBER OF LEFT MOST CELL , NR=NUMBER OF RIGHT MOST CELL ,
C NOTE. GENERATION OF INTERIOR MESH CELLS ,I.E. FLUID AND OBSTACLE .
  500 IF(IDATIN.GT.0.AND.IRESET.EQ.0) GO TO 590
      READ(IVDI,5)    NL,NR,NB,NT,ICELTY
      WRITE(IVDO,54) NL,NR,NB,NT,ICELTY
      IF( NL.EQ.0 ) GO TO 700
      READ(IVDI,6) SIEI,TQI,TSI,UI,WI,CHII,VAPI,LIQI                    RGBMK60A
      WRITE(IVDO,55) SIEI,TQI,TSI,UI,WI,CHII,VAPI,LIQI                  RGBMK60A
      I1=NL
      I2=NR
      K1=NB
      K2=NT
      KK=1 + (I1-2)*K2NC
```

```
      DO 589 I=I1,I2
      KK=KK + K2NC
      LWPC=(K1-2)*NWPC
      DO 579 K=K1,K2
      LWPC=LWPC + NWPC
      IK=KK + LWPC
      CF(IK)=ICELTY
C NOTE. FOR OBSTACLES WITH TAU FACTORS - SET SIEI = OBSTACLE TEMPERA -
C NOTE. TURE IN F DEGREES .
      SIE(IK)=SIEI                                              RGBMK01A
      IF( ICELTY.GE.30 .AND. NTAU.GT.0 ) P(IK)=SIEI
      TQ(IK)=TQI
      TS(IK)=TSI
      U(IK)=UI
      W(IK)=WI
      CHI(IK)=CHII                                              RGBMK02A
      VAP(IK)=VAPI                                              RGBMK60A
      LIQ(IK)=LIQI                                              RGBMK60A
      SIEO(IK)=SIE(IK)
      TQO(IK)=TQ(IK)
      TSO(IK)=TS(IK)
      UO(IK)=U(IK)
      WO(IK)=W(IK)
      CHIO(IK)=CHI(IK)                                          RGBMK02A
      VAPO(IK)=VAP(IK)                                          RGBMK60A
      LIQO(IK)=LIQ(IK)                                          RGBMK60A
  578 CONTINUE
  579 CONTINUE
  589 CONTINUE
      GO TO 500
  590 CONTINUE
C NOTE. GENERATION OF EXTERIOR BOUNDRY MESH CELLS .
  700 I1=1
      TSMAX=-1.0E+20
      TMAX=TSMAX
      WMAX=TMAX
```

```
      UMAX=WMAX
      TSMIN=+1.0E+20
      TMIN=TSMIN
      WMIN=TMIN
      UMIN=WMIN
      TQMAX=-1.E+20
      I2=IBP2
      K1=1
      K2=KBP2
      KK=1 + (I1-2)*K2NC
      DO 789 I=I1,I2
      KK=KK + K2NC
      LWPC=(K1-2)*NWPC
      DO 779 K=K1,K2
      LWPC=LWPC + NWPC
      IK=KK + LWPC
      UMAX=AMAX1( UMAX,U(IK) )
      WMAX=AMAX1( WMAX,W(IK) )
      UMIN=AMIN1( UMIN,U(IK) )
      WMIN=AMIN1( WMIN,W(IK) )
      TSMAX=AMAX1( TSMAX,TS(IK) )
      TSMIN=AMIN1( TSMIN,TS(IK) )
      TQMAX=AMAX1( TQMAX,TQ(IK) )
      CFC= CF(IK)
      IF( K.EQ.K1 .AND. CFC.LT.11 ) CF(IK)=10
      IF( K.EQ.K2 .AND. CFC.LT.11 ) CF(IK)=10
      IF( I.EQ.I1 .AND. CFC.LT.11 ) CF(IK)=10
      IF( I.EQ.I2 .AND. CFC.LT.11 ) CF(IK)=10
      IF( I.EQ.I1 .AND. K.EQ.K1 ) CF(IK)=2
      IF( I.EQ.I1 .AND. K.EQ.K2 ) CF(IK)=2
      IF( I.EQ.I2 .AND. K.EQ.K1 ) CF(IK)=2
      IF( I.EQ.I2 .AND. K.EQ.K2 ) CF(IK)=2
      IF( CFC.LT.20 .OR. IOBS.EQ.0 ) GO TO 770
C NOTE. FLAGS CELLS SURRONDING THE OBSTACLE CELL.
      CFR=CF(IK+K2NC)
      CFL=CF(IK-K2NC)
```

```
      CFT=CF(IK+NWPC)
      CFB=CF(IK-NWPC)
      IICFR(IK)=1
      IICFL(IK)=1
      IICFT(IK)=1
      IICFB(IK)=1
      IF (CFR.NE.1) IICFR(IK)=0
      IF (CFL.NE.1) IICFL(IK)=0
      IF (CFT.NE.1) IICFT(IK)=0
      IF (CFB.NE.1) IICFB(IK)=0
770   CONTINUE
779   CONTINUE
789   CONTINUE
      RETURN
C ***** FORMATS ***** FORMATS ***** FORMATS ***** .
    1 FORMAT (10F8.3)
    2 FORMAT (4I2,8F8.3)
    5 FORMAT (4I5,I2)
    6 FORMAT(8F8.3)                                                     R3BMK60A
    7 FORMAT(4F8.3,I2,4F8.3)
    8 FORMAT(3F8.3)
   10 FORMAT(4F8.3,2I2)
   11 FORMAT(7X,I3,5(5X,I3),7X,I3)
   12 FORMAT(8F8.3)
   13 FORMAT(3X,I3,2X,6F8.3)
   14 FORMAT(2(3X,I3),2(5X,F8.3))
   50 FORMAT(1H ,5X,3HDX=,1PE12.5/6X,3HDZ=,E12.5/6X,3HGX=,E12.5/
     1 6X,3HGZ=,E12.5/5X,4HALX=,E12.5/5X,4HALZ=,E12.5/5X,4HCYL=,E12.5/
     2 6X,3HB0=,E12.5/5X,4HEPS=,E12.5/4X,5HVMIN=,E12.5)
   51 FORMAT(1H ,4X,4HKWR=,I2/5X,4HKWL=,I2/5X,4HKWT=,I2/5X,4HKWB=,I2/
     1 3X,6HFSLIP=,1PE12.5/5X,4HALP=,E12.5/5X,4HGAM=,E12.5/4X,5HALPO=,
     2E12.5/4X,5HGAM1=,E12.5/6X,3HNU=,E12.5/3X,6HTQJET=,E12.5/3X,
     36HTSJET=,E12.5)
   52 FORMAT(1H ,5X,3HAI=,1PE12.5/6X,3HBI=,E12.5/6X,3HCI=,E12.5/
     1 6X,3HAR=,E12.5/6X,3HBR=,E12.5/6X,3HCR=,E12.5/5X,4HAMU=,E12.5/
     2 5X,4HBMU=,E12.5/5X,4HCMU=,E12.5)
```

```
 53 FORMAT(1H ,5X,3HAK=,1PE12.5/6X,3HBK=,E12.5/6X,3HCK=,E12.5/5X,
   14HACP=,E12.5/5X,4HBCP=,E12.5/,5X,4HCCP=,E12.5/5X,5HSIGN=,E12.5)
 54 FORMAT(1H ,3HNL ,I5,3HNR ,I5,3HNB ,I5,3HNT ,I5,8HICELTYP ,I2)
 55 FORMAT(1H ,3X,5HSIEI=,1PE12.5/5X,4HTQI=,E12.5/5X,4HTSI=,E12.5/
   16X,3HUI=,E12.5/6X,3HWI=,E12.5/5X,4HCHI=,E12.5/5X,4HVAP=,E12.5/5X,4RGBMK60A
   2HLIQ=,E12.5)                                                   RGBMK60A
 57 FORMAT(1H ,20H TAU FOR OBSTACLES =,7(2X,1PE12.5))
 58 FORMAT(1H ,3X,5HWOBI=,1PE12.5/4X,5HUOBI=,E12.5/1X,8HCSUBPOB=,
   1 E12.5)
 59 FORMAT(1H ,5X,3HAW=,1PE12.5/6X,3HBW=,E12.5/6X,3HCW=,E12.5/
   1 4X,5HWEPS=,E12.5/2X,7HKDERBC=,I2/4X,5HUBRI=,E12.5/4X,5HUBLI=,
   2 E12.5/4X,5HWBTI=,E12.5/4X,5HWBBI=,E12.5)
 60 FORMAT(1H ,3X,5HTGAM=,1PE12.5/6X,3HTO=,E12.5/6X,3HTI=,E12.5/
   1 3X,6HTSTEP=,E12.5/5X,4HMAT=,I2/1X,8HNRESEXP=,I2)
61    FORMAT(1H ,7H NFLOW ,I3,5H NT1 ,I3,5H NT2 ,I3,5H NT3 ,I3,5H NT4 ,
   1  I3,5H NT5 ,I3,6H NTAU ,I3)
 62 FORMAT(1H ,3X,1HI,9X,4HTYMF,12X,2HFN,11X,5HTYMT1,11X,3HT1N,11X,
   1 5HTYMT2,11X,3HT2N)
 63 FORMAT(1H ,2X,I3,2X,6(2X,1PE11.4,2X))
64    FORMAT(1H ,3H I ,I3,2X,6F8.3)
 65 FORMAT(1H ,3H I ,I3,3H K ,I3,5H RXC ,F8.3,5H RZC ,F8.3)
66    FORMAT(1H ,///,22X,6(2X,1PE11.4,2X))
      END
      SUBROUTINE VM
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1   VTP
      REAL NU,LIQ,LIQO,LIQI,LOUT                                   RGBMN60A
      REAL LIQL,LIQR,LIQT,LIQB,LIQC,LIQCO                          RGBVM60A
      DIMENSION EFRAC(5),RLAM(5),ELAM(5)                           RGBVM56A
      DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
     1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
     2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                      RGBMN01A
     A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                               RGBMN60A
     3   ,TYMF(25),FN(25),TYMT1(25),T1N(25),TYMT2(25),T2N(25),
     4   COFBA(25),COFBB(25),COFBC(25),COFTA(25),COFTB(25),COFTC(25),
     5   COFRA(25),COFRB(25),COFRC(25),COFLA(25),COFLB(25),COFLC(25),
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6    OFOBTA(25),OFOBTB(25),OFOBTC(25),
7    OFOBRA(25),OFOBRB(25),OFOBRC(25),TAU(10),USL(32),USLOB(20),
8    USROB(20),USTOB(20),USBOB(20)
9,COFBD(25),COFBE(25),COFTD(25),COFTE(25),COFTF(25),COFBF(25),
*COFRD(25),COFRE(25),COFLD(25),COFLE(25),COFRF(25),COFLF(25),
AOFOBTD(25),OFOBTE(25),OFOBRD(25),OFOBRE(25),
B  OFOBTF(25),OFOBRF(25),
CTYMT3(25),TYMT4(25),TYMT5(25),T3N(25),T4N(25),T5N(25),
*  IICFR(1),IICFL(1),IICFT(1),IICFB(1)
*    ,ZERO1(1165),ZERO2(608),ZERO3(16),ZERO4(3)
 DIMENSION ZSIE(22),ZTQ(22),ZTS(22),ZVP(22),ZLQ(22),ZAP(22),WSP(22) RGBVM62A
 DIMENSION TRSTRT(5),WZSIE(100),WZTQ(100),WZTS(100)                 RGBVM55A
A,WZVP(100),WZLQ(100),WZAP(100),WWSP(100)                           RGBVM62A
 COMMON/VRCOM/A(14000)                                              RGBMN60A
 COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ,  RGBVM55A
AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                   RGBMN60A
B,WSP,WWSP,BKGND,DWNDS                                              RGBMN60B
 COMMON /VRCON/ ALP,ALPO,ALX,ALZ,BO,BETA,BUFL,CFI(9),CFS(9),CYL,
1    DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2    IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3    IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
4    LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5    TIMEI,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
*   ,USR(32),UST(22),USB(22),USO(10),FFX3,FFY3
6    ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7    TO,SIEI,IDG,KDG,TI,MAT,RHOO,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8    T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9    COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
*    OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1    USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*   ,CSUBPO,EPSO,RDXDZS,RLENGH ,TQJET,TSJET
 COMMON /FLMCON/ DROU,DROUO,IPRFM
 COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
1                ,VMIN
  COMMON/PROP/SIGN
 COMMON/EXTRA/NT3,NT4,NT5,TYMT3,TYMT4,TYMT5,T3N,T4N,T5N,COFBD,
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     1COFBE,COFBF,COFTD,COFTE,COFTF,COFRD,COFRE,COFRF,COFLD,COFLE,
     2COFLF,OFOBTD,OFOBTE,OFOBTF,OFOBRD,OFOBRE,OFOBRF,IRESET,
     *NCYCLS,TADD,NIV,IOBRAN
       COMMON/INDEX/NWPCL,K2NCL
       COMMON/LARGE/DIFFCO(2400)
      EQUIVALENCE  (A(1),CF),(A(2),U),(A(3),W),(A(4),P),(A(5),TQ),
     1    (A(6),TS),(A(7),ER,CQ),(A(8),UO),(A(9),WO),(A(10),TQO),
     2    (A(11),TSO),(A(12),SIE),(A(13),SIEO),(A(14),RX),(A(15),RZ),
     3    (A(16),IICFR),(A(17),IICFL),(A(18),IICFT),(A(19),IICFB),
     A    (A(20),CHI),(A(21),CHIO),                              RGBMN01A
     B    (A(22),VAP),(A(23),VAPO),(A(24),LIQ),(A(25),LIQO),     RGBMN60A
     4    (ZERO1(1),ALP),(ZERO2(1),NT3),(ZERO3(1),AI),(ZERO4(1),DROU)
C NOTE. END - END OF NON-EXECUTABLE STATEMENTS .
C NOTE. VM IS RESPONSIBLE FOR CALCULATION OF BOUNDARY CONDITIONS
C NOTE. AND EQUATIONS .
      NRSTRT=1                                                   R3BVM55A
      READ(IVDI,57) GAMX,NCHAN,WMOLX,GAMV,GAML,BKGND,DWNDS        RGBVM60B
   57 FORMAT(F8.3,I8,5F8.3)                                       RGBVM60B
      WRITE(IVDO,58) GAMX,NCHAN,WMOLX,GAMV,GAML,BKGND             RGBVM60A
   58 FORMAT(10H   GAMX =  ,F8.4,I5,' DECAY CHANNELS   MOLEC WT = ',F8.3/RGBVM60A
     110H  GAMV =  ,F8.4/10H  GAML =  ,F8.4/10H  BKGND = ,E8.4)  RGBVM60A
      WRITE(IVDO,64)                                              RGBVM56A
   64 FORMAT(54H  DECAY CHANNEL    LAMBDA (1/SEC)  ENERGY (MEV) FRACT.) RGBVM56A
      READ(IVDI,65) (RLAM(J),ELAM(J),EFRAC(J),J=1,NCHAN)          RGBVM56A
   65 FORMAT(3F8.3)                                               R3BVM56A
      WRITE(IVDO,66) (J,RLAM(J),ELAM(J),EFRAC(J),J=1,NCHAN)       RGBVM56A
   66 FORMAT(8X,I1,13X,F8.5,7X,F8.5,3X,F6.4)                     RGBVM56A
      RLAMB=0.0                                                   RGBVM56A
      SER=0.0                                                     R3BVM56A
      DO 98 J=1,NCHAN                                             RGBVM56A
      SER=SER+RLAM(J)*ELAM(J)*EFRAC(J)                            RGBVM56A
   98 RLAMB=RLAMB+RLAM(J)                                         RGBVM56A
      WRITE(IVDO,67) RLAMB,SER                                    RGBVM56A
   67 FORMAT(' RLAMB = ',E10.5,' SPEC. ENERGY RELEASE = ',E10.5)  RGBVM56A
      READ(IVDI,62) NPROF,(TRSTRT(L),L=1,5)                       RGBVM55A
   62 FORMAT(I8,5F8.3)                                            RGBVM55A
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      READ(IVDI,56) (WZSIE(K),WZTQ(K),WZTS(K),WZVP(K),WZLQ(K),WZAP(K),WWRGBVM62A
     ASP(K),K=1,NPROF)                                                  RGBVM62A
   56 FORMAT(7F8.3,24X)                                                 RGBVM62A
      WRITE(IVDO,59) (WZSIE(K),WZTQ(K),WZTS(K),WZVP(K),WZLQ(K),WZAP(K),WWRGBVM62A
     ASP(K),K=1,NPROF)                                                  RGBVM62A
   59 FORMAT(' ',7F10.3)                                                RGBVM62A
C  TRANSFER OF PROFILES BEFORE ANY RESTART CASES                        RGBVM55A
      DO 99 K=2,KBP1                                                    RGBVM55A
      WSP(K)=WWSP(K-1)                                                  RGBVM70A
      ZAP(K)=WZAP(K-1)                                                  RGBVM62A
      ZVP(K)=WZVP(K-1)                                                  RGBVM60A
      ZLQ(K)=WZLQ(K-1)                                                  RGBVM60A
      ZSIE(K)=WZSIE(K-1)                                                RGBVM55A
      ZTQ(K)=WZTQ(K-1)                                                  RGBVM55A
   99 ZTS(K)=WZTS(K-1)                                                  RGBVM55A
      WSP(1)=0.0                                                        RGBVM70A
      ZAP(1)=0.0                                                        RGBVM62A
      ZVP(1)=ZVP(2)                                                     RGBVM60A
      ZLQ(1)=ZLQ(2)                                                     RGBVM60A
      ZSIE(1)=ZSIE(2)                                                   RGBVM55A
      ZTQ(1)=ZTQ(2)                                                     RGBVM55A
      ZTS(1)=ZTS(2)                                                     RGBVM55A
      WSP(KBP2)=0.0                                                     RGBVM70A
      ZAP(KBP2)=0.0                                                     RGBVM62A
      ZVP(KBP2)=ZVP(KBP1)                                               RGBVM60A
      ZLQ(KBP2)=ZLQ(KBP1)                                               RGBVM60A
      ZSIE(KBP2)=ZSIE(KBP1)                                             RGBVM55A
      ZTQ(KBP2)=ZTQ(KBP1)                                               RGBVM55A
      ZTS(KBP2)=ZTS(KBP1)                                               RGBVM55A
C NOTE. CALCULATION OF CONSTANTS AND PREASSIGNED BRANCHES .
      IF( IRSTRT.EQ.0 ) GO TO 100
      CALL VRPRT
      IF( IDROU.GT.0 ) DROU=DROU0*AMIN1(DX,DZ)/AMAX1(UMAX,WMAX,EM6)
      IF( IPRFM.GT.0 ) CALL VRFLM
      IRSTRT=0
  100 ITER=0
```

```
      ICALI=1
      X1=AMAX1( UMAX, WMAX )
      VELOLD=X1
      EPS=EPS0*X1*RLENGH
      IF( X1.LT.VMIN ) EPS=EPS0*VMIN*RLENGH
      IF( EPS0.LT.EM6 ) EPS=ABS( EPS0 )
      ASSIGN 2000 TO KBC
C NOTE. COMPUTATION OF FNTAU,T1NTAU AND T2NTAU .
      FNTAU=SI( TYMF,FN,TIMET,NFLOW )
      T1NTAU=SI( TYMT1,T1N,TIMET,NT1 )
       IF(NT2.EQ.0) GO TO 107
      T2NTAU=SI( TYMT2,T2N,TIMET,NT2 )
       IF(NT3.EQ.0) GO TO 107
      T3NTAU=SI(TYMT3,T3N,TIMET,NT3)
       IF(NT4.EQ.0) GO TO 107
      T4NTAU=SI(TYMT4,T4N,TIMET,NT4)
       IF(NT5.EQ.0) GO TO 107
      T5NTAU=SI(TYMT5,T5N,TIMET,NT5)
 107   CONTINUE
C NOTE. ZERO OUT THE CQ(IK) ARRAY FOR TAU FACTORS IN SIE EQUATION .
      I1=2
      I2=IBP1
      K1=2
      K2=KBP1
      KK=1
      ITAUCN=0
      DO 109 I=I1,I2
      KK=KK + K2NC
      LWPC=0
      DO 109 K=K1,K2
      LWPC=LWPC + NWPC
      IK=KK + LWPC
      CQ(IK)=0.0
  109 CONTINUE
      IF( NCYCB.LT.NCYC ) GO TO 1000
C NOTE. CALCULATION OF DIAGNOSTIC CONSTANTS .
```

```
      ASSIGN 12500 TO KDAGTU
C NOTE. PREASSIGN BRANCHES FOR RESISTANCE EQUATIONS , I.E. RX AND RZ .
      RXC=0.0
      RZC=0.0                                                           VM212002
      ASSIGN 2300 TO KRXRZ                                              VM212004
      IF( NWPC.GT. 13 ) ASSIGN 2250 TO KRXRZ
C NOTE. PREASSIGN BRANCHES FOR PLANE - CYL=0.0 - OR CYLINDRICAL
C NOTE. - CYL=1.0 - COORDINATES .
      FCU=0.0
      FCW=0.0                                                           VM215002
      RL=1.0
      RC=RL
      RR=RC
      DR=DX
      RRL=1.0
      RRC=RRL
      RRR=RRC
      RRRC=1.0
      RRP=RRRC
      RDR=RDX
      RDRS=1./( DR*DR )
      RDRM=RDR
      RDRP=RDRM
      RDZM=RDZ
      RDZP=RDZM
      ASSIGN 2400 TO KCLU                                               VM215006
      ASSIGN 2500 TO KCLW
      ASSIGN 2220 TO KRU                                                VM215010
      IF( CYL.LT.EM6 ) GO TO 120
      ASSIGN 2370 TO KCLU                                               VM215014
      ASSIGN 2470 TO KCLW                                               VM215016
      ASSIGN 2215 TO KRU                                                VM215018
  120 ASSIGN 13000 TO KDIAG
      IF( IDIAG.LT.1 ) GO TO 200
      ASSIGN 12200 TO KDIAG
      IF( IDIAG.GT.1 ) ASSIGN 12500 TO KDIAG
```

```
  200 TSUM=0.0
      TIOSUM=0.0
C
C NOTE. COMPUTATION OF BOUNDARY CONDITIONS .
C
1000  LWPC=1 - NWPC
      IF( KDERBC.LT.1 ) GO TO 1100
C
C NOTE. COMPUTATION OF RIGHT AND LEFT BOUNDARY CONDITIONS .
1100  LWPC=1 - NWPC
      I1=1
      I2=IBP2
      K1=1
      K2=KBP2
      NDERR=0
      NDERL=0
      NCOFR=0
      NCOFL=0
      DO 1289 K=K1,K2
      LWPC=LWPC+NWPC                                          VM111002
      IMK=LWPC
      CFL= CF(IMK)
      ICFL=CFL
      IPK=IMK + IKP2
      IPPK=IPK + K2NC
      IMKT=IMK + K2NC
      IPKT=IPK
      CFR= CF(IPPK)
      ICFR=CFR
      IF( CFL.NE.2 ) GO TO 1105
      IF( K.EQ.K2 ) GO TO 1103
      IMKT=IMK + K2NC + NWPC
      IPKT=IPK + NWPC
      CFL= CF(IMK+NWPC)
      CFR= CF(IPPK+NWPC)
      GO TO 1105
```

```
1103  IMKT=IMK + K2NC - NWPC
      IPKT=IPK - NWPC
      CFL= CF(IMK-NWPC)
      CFR= CF(IPPK-NWPC)
 1105 W(IMK)=W(IMKT)                                              RGBVM51A
      W(IPPK)=W(IPK)                                              RGBVM02A
C NOTE. COMPUTATION OF REFLECTIVE BOUNDARY CONDITIONS ON TQ AND TS .
      SIE(IMK)=SIE(IMKT)
      SIE(IPPK)=ZSIE(K)                                           RGBVM51A
      TQ(IMK)=TQ(IMKT)
      TQ(IPPK)=ZTQ(K)                                             RGBVM51A
      TS(IMK)=TS(IMKT)
      TS(IPPK)=ZTS(K)                                             RGBVM51A
      CHI(IMK)=CHI(IMKT)                                          RGBVM52A
      CHI(IPPK)=0.0                                               RGBVM52A
      IF(U(IPKT).GT.0.0) CHI(IPPK)=CHI(IPKT)                      RGBVM52A
      VAP(IMK)=VAP(IMKT)                                          RGBVM60A
      VAP(IPPK)=ZVP(K)                                            RGBVM60A
      LIQ(IMK)=LIQ(IMKT)                                          RGBVM60A
      LIQ(IPPK)=ZLQ(K)                                            RGBVM60A
      GO TO ( 1120,1130,1140,1150 ),KWL
C NOTE. COMPUTATION OF RIGID  LEFT  WALL BOUNDARY CONDITION .
1120  U(IMK)=0.0
      GO TO 1180                                                  VM114002
C NOTE. COMPUTATION OF CONTINUATIVE  LEFT  WALL BOUNDARY CONDITION .
1130  IF( ITER.GT.0 ) GO TO 1180
      U(IMK)=U(IMK+K2NC)
      W(IMK) = -W(IMK+K2NC)
      W(IMK-NWPC) = -W(IMK+K2NC-NWPC)
      GO TO 1180                                                  VM115004
C NOTE. COMPUTATION OF PERIODIC  LEFT  WALL BOUNDARY CONDITION .
1140  U(IMK)=U(IPK)
      GO TO 1180
C NOTE. VARIABLE BOUNDARY OPTION AT LEFT WALL .
1150  NCFL=CFL - 9
      GO TO ( 1152,1130,1155,1160 ),NCFL
```

```
C NOTE. RIGID BOUNDARY SECTION AT LEFT WALL .
1152  NRIGID=KDERBC + 1
      GO TO( 1120,1153 ),NRIGID
C NOTE. DERIVED BOUNDARY CONDITION AT LEFT WALL .
1153  WC=W(IMKT)
      IF( K.EQ.1 ) GO TO 1120
      IF (K.GE.(KBR+1)) GO TO 1120
      ICF1=CF(IMKT)
      IF (ICF1.GE.30) GO TO 1120
      QC=TQ(IMKT)
      SC=TS(IMKT)
      NDERL=NDERL + 1
      WSA=USL(NDERL)
      QW=5.*WSA*WSA
      W(IMK) = -WC
      SW = WSA * WSA * HDX/WC
      TQ(IMK)=2.*QW - QC
      TS(IMK)=2.*SW - SC
      GO TO 1120
C NOTE. CONSTANT INFLOW AT LEFT WALL .
1155  U(IMK)=UBLI
      GO TO 1180
C NOTE. VARIABLE OR FUNCTIONAL INFLOW AT LEFT WALL .
1160  IF( ICFL.EQ.2 ) GO TO 1180
      NCOFL=NCOFL + 1
      TI=COFLB(NCOFL)*T1NTAU + COFLC(NCOFL)*T2NTAU
     1+COFLD(NCOFL)*T3NTAU+COFLE(NCOFL)*T4NTAU+COFLF(NCOFL)*T5NTAU
      ASSIGN 1162 TO KIROBC
      SIEX=SIE(IMKT)                                                    RGBVM01A
      GO TO 1500
1162  AREAK=3.14159265*FLOAT(2*K-3)*DZ*DZ
      IF( CYL.LT.1.0 ) AREAK=DZ
      FLK=COFLA(NCOFL)*FNTAU
      UBAR=FLK/RHOII
      U(IMK)=UBAR/AREAK
       IF(NIV.EQ.1) U(IMK)=FLK
```

```
      SIE(IMK)=SIEII                                              RGBVM02A
      TS(IMK)=TS(IPK)                                             RGBVM02A
      TQ(IMK)=TQ(IPK)                                             RGBVM02A
1180  GO TO( 1220,1230,1240,1250 ),KWR
C NOTE. COMPUTATION OF RIGID RIGHT  WALL BOUNDARY CONDITION .
1220  U(IPK)=0.0
      GO TO 1280                                                  VM124002
C NOTE. COMPUTATION OF CONTINUATIVE RIGHT  WALL BOUNDARY CONDITION .
1230  IF( ITER.GT.0 ) GO TO 1280
      U(IPPK)=U(IPK-K2NC)
      W(IPPK-NWPC)=W(IPK-NWPC)                                    RGBVM02A
      GO TO 1280                                                  VM125004
C NOTE. COMPUTATION OF PERIODIC RIGHT  WALL BOUNDARY CONDITION .
1240  U(IPPK)=U(IMK+K2NC)
      W(IPPK)=W(IMK+K2NC)
      GO TO 1280
C NOTE. VARIABLE BOUNDARY OPTION AT RIGHT WALL .
1250  NCFR=CFR - 9
      GO TO( 1252,1230,1255,1260 ),NCFR
C NOTE. RIGID BOUNDARY SECTION AT RIGHT WALL .
1252  NRIGID=KDERBC + 1
      GO TO( 1220,1253 ),NRIGID
C NOTE. DERIVED BOUNDARY CONDITION AT RIGHT WALL .
1253  WC=W(IPKT)
      IF (K.GE.(KBR+1)) GO TO 1220
      IF( K.EQ.1 ) GO TO 1220
      ICF2=CF(IPKT)
      IF (ICF2.GE.30) GO TO 1220
      QC=TQ(IPKT)
      SC=TS(IPKT)
      NDERR=NDERR + 1
      WSA=USR(NDERR)
      QW=5.*WSA*WSA
 1256 SW = WSA * WSA * HDX/WC
      W(IPPK) = -WC
      TQ(IPPK)=2.*QW-QC
```

```
      TS(IPPK)=2.*SW-SC
      GO TO 1220
C NOTE. CONSTANT INFLOW AT RIGHT WALL .
1255  U(IPK)=UBRI
      GO TO 1280
C NOTE. VARIABLE OR FUNCTIONAL INFLOW AT RIGHT WALL .
1260  IF( ICFR.EQ.2 ) GO TO 1280
      NCOFR=NCOFR + 1
      TI=COFRB(NCOFR)*T1NTAU + COFRC(NCOFR)*T2NTAU
     1+COFRD(NCOFR)*T3NTAU+COFRE(NCOFR)*T4NTAU+COFRF(NCOFR)*T5NTAU
      ASSIGN 1262 TO KIROBC
      SIEK=SIE(IPKT)                                            R3BVM01A
      GO TO 1500
 1262 AREAK = 3.14159265 * 2 * IBR * DR * DZ
      IF( CYL.LT.1.0 ) AREAK=DZ
      FLK=COFRA(NCOFR)*FNTAU
      UBAR=FLK/RHOII
      U(IPK)=UBAR/AREAK
       IF(NIV.EQ.1) U(IPK)=FLK
       SIEC=SIE(IPKT)
       SIEW=SIEII
       SIE(IPPK)=(2*SIEW+(ALX-1.0)*SIEC)/(1.0+ALX)
      QC = TQ(IPKT)
      QW = TQJET * U(IPK)*U(IPK)
      SC = TS(IPKT)
      SW = TSJET * U(IPK) * DZ
       SW=ABS(SW)
       QW=AMAX1(QW,1.0E-5)
       SW=AMAX1(SW,NU)
       TQ(IPPK)=(2*QW+(ALX-1.0)*QC)/(1.0+ALX)
       TS(IPPK)=(2*SW+(ALX-1.0)*SC)/(1.0+ALX)
1280  CONTINUE                                                  VM128000
1289  CONTINUE                                                  VM128900
C NOTE. COMPUTATION OF TOP AND BOTTOM BOUNDARY CONDITIONS .
      NDERB=0
      NDERT=0
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```
      NCOFB=0
      NCOFT=0
      KK=1 - K2NC
      DO 1489 I=I1,I2
      KK=KK+K2NC                                                VM131002
      IKM=KK
      CFB= CF(IKM)
      ICFB=CFB
      IKP=IKM + KNC
      IKPP=IKP + NWPC
      CFT= CF(IKPP)
      ICFT=CFT
      IKMT=IKM + NWPC
      IKPT=IKP
      IF( CFB.NE.2 ) GO TO 1305
      IF( I.EQ.I2 ) GO TO 1303
      IKMT=IKM + K2NC + NWPC
      IKPT=IKP + K2NC
      CFB= CF(IKM+K2NC)
      CFT= CF(IKPP+K2NC)
      GO TO 1305
 1303 IKMT=IKM - K2NC + NWPC
      IKPT=IKP - K2NC
      CFB= CF(IKM-K2NC)
      CFT= CF(IKPP-K2NC)
 1305 U(IKM)=-U(IKMT)                                           RGBVM50A
      U(IKPP)=U(IKP)                                            RGBVM51A
C NOTE. COMPUTATION OF REFLECTIVE BOUNDARY CONDITIONS ON TQ AND TS .
      SIE(IKM)=SIE(IKMT)
      SIE(IKPP)=SIE(IKPT)
      TQ(IKM)=TQ(IKMT)
      TQ(IKPP)=TQ(IKPT)
      TS(IKM)=TS(IKMT)
      TS(IKPP)=TS(IKPT)
      CHI(IKM)=CHI(IKMT)                                        RGBVM52A
      CHI(IKPP)=0.0                                             RGBVM52A
```

```
      IF(W(IKPT).GT.0.0)  CHI(IKPP)=CHI(IKPT)                    RGBVM52A
      VAP(IKM)=VAP(IKMT)                                          RGBVM60A
      VAP(IKPP)=VAP(IKPT)                                         RGBVM60A
      LIQ(IKM)=LIQ(IKMT)                                          RGBVM60A
      LIQ(IKPP)=LIQ(IKPT)                                         RGBVM60A
      GO TO( 1320,1330,1340,1350 ),KWT
C NOTE. COMPUTATION OF RIGID  TOP   WALL BOUNDARY CONDITION .
1320  W(IKP)=0.0
      GO TO 1380                                                  VM134002
C NOTE. COMPUTATION OF CONTINUATIVE  TOP   WALL BOUNDARY CONDITION .
1330  IF( ITER.GT.0 ) GO TO 1380
      W(IKPP)=W(IKP-NWPC)
      U(IKPP-K2NC)=U(IKP-K2NC)                                    RGBVM51A
      GO TO 1380                                                  VM135004
C NOTE. COMPUTATION OF PERIODIC  TOP   WALL BOUNDARY CONDITION .
1340  W(IKPP)=W(IKM+NWPC)
      U(IKPP)=U(IKM+NWPC)
      GO TO 1380
C NOTE. VARIABLE BOUNDARY OPTION AT TOP WALL .
1350  NCPT=CPT - 9
      GO TO( 1352,1330,1355,1360 ),NCPT
C NOTE. RIGID BOUNDARY SECTION AT TOP WALL .
1352  NRIGID=KDERBC + 1
      GO TO( 1320,1353 ),NRIGID
C NOTE. DERIVED BOUNDARY CONDITION AT TOP WALL .
1353  UCT=U(IKP)
      IF( I.EQ.1 ) GO TO 1320
      IF (I.GE.(IBR+1)) GO TO 1320
      ICP3=CP(IKP)
      IF (ICP3.GE.30) GO TO 1320
      QCT=TQ(IKP)
      SCT=TS(IKP)
      NDERT=NDERT + 1
      USAT=UST(NDERT)
      QWT=5.*USAT*USAT
 1356 SWT = USAT * USAT * DDZ /UCT
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```
      U(IKPP) = -UCT
      TQ(IKPP)=2.*QWT - QCT
      TS(IKPP)=2.*SWT - SCT
      GO TO 1320
C.NOTE  CONSTANT INFLOW AT TOP WALL .                                  RGB/03/78
1355  W(IKP)=WBTI
      GO TO 1380
C NOTE. VARIABLE OR FUNCTIONAL INFLOW AT TOP WALL .
1360  IF( ICPT.EQ.2 ) GO TO 1380
      NCOFT=NCOFT + 1
      TI=COFTB(NCOFT)*T1NTAU + COFTC(NCOFT)*T2NTAU
     1+COFTD(NCOFT)*T3NTAU+COFTE(NCOFT)*T4NTAU+COFTF(NCOFT)*T5NTAU
      ASSIGN 1362 TO KIROBC
      SIEX=SIE(IKPT)                                                    RGBVM01A
      GO TO 1500
1362  AREAI=3.14159265*FLOAT(2*I-3)*DR*DR
      IF( CYL.LT.1.0 ) AREAI=DX
      FLI=COFTA(NCOFT)*FNTAU
      WBAR=FLI/RHOII
      W(IKP)=WBAR/AREAI
       IF(NIV.EQ.1) W(IKP)=FLI
       SIEC=SIE(IKP )
       SIEW=SIEII
       SIE(IKPP)=(2*SIEW+(ALZ-1.0)*SIEC)/(1.0+ALZ)
      QCT=TQ(IKP)
      QWT=TQJET*W(IKP)*W(IKP)
      SCT=TS(IKP)
      SWT=TSJET*W(IKP)*DR
       SWT=ABS(SWT)
       QWT=AMAX1(QWT,1.0E-5)
       SWT=AMAX1(SWT,NU)
       TQ(IKPP)=(2*QWT+(ALZ-1.0)*QCT)/(1.0+ALZ)
       TS(IKPP)=(2*SWT+(ALZ-1.0)*SCT)/(1.0+ALZ)
1380  GO TO( 1420,1430,1440,1450 ),KWB
C NOTE. COMPUTATION OF RIGID BOTTOM WALL BOUNDARY CONDITION .
1420  W(IKM)=0.0
```

```
      GO TO 1480
C NOTE. COMPUTATION OF CONTINUATIVE BOTTOM WALL BOUNDARY CONDITION .
1430  IF( ITER.GT.0 ) GO TO 1480
      W(IKM)=W(IKM+NWPC)
      U(IKM)=-U(IKM+NWPC)
      U(IKM-K2NC)=-U(IKM+NWPC-K2NC)
      GO TO 1480                                          VM145004
C NOTE. COMPUTATION OF PERIODIC BOTTOM WALL BOUNDARY CONDITION .
1440  W(IKM)=W(IKP)
      GO TO 1480
C NOTE. VARIABLE BOUNDARY OPTION AT BOTTOM WALL .
1450  NCFB=CFB - 9
      GO TO( 1452,1430,1455,1460 ),NCFB
C NOTE. RIGID BOUNDARY SECTION AT BOTTOM WALL .
1452  NRIGID=KDERBC + 1
      GO TO( 1420,1453 ),NRIGID
C NOTE. DERIVED BOUNDARY CONDITION AT BOTTOM .
1453  IK=IKM + NWPC
      IF( I.EQ.1 ) GO TO 1420
      IF (I.GE.(IBR+1)) GO TO 1420
      ICF4=CF(IK)
      IF (ICF4.GE.30) GO TO 1420
      UCB=U(IK)
      QCB=TQ(IK)
      SCB=TS(IK)
      NDERB=NDERB + 1
      USAB=USB(NDERB)
      QWB=5.*USAB*USAB
 1456 SWB=USAB*USAB*HDZ/UCB
      U(IKM)=-UCB
      TQ(IKM)=2.*QWB - QCB
      TS(IKM)=2.*SWB - SCB
      GO TO 1420
C NOTE. CONSTANT INFLOW AT BOTTOM WALL .
1455  W(IKM)=WBBI
      GO TO 1480
```

```
C NOTE. VARIABLE OR FUNCTIONAL INFLOW AT BOTTOM WALL .
1460  IF( ICFB.EQ.2 ) GO TO 1480
      NCOFB=NCOFB + 1
      TI =COFBB(NCOFB)*T1NTAU + COFBC(NCOFB)*T2NTAU
     1+COFBD(NCOFB)*T3NTAU+COFBE(NCOFB)*T4NTAU+COFBF(NCOFB)*T5NTAU
      ASSIGN 1462 TO KIROBC
      SIEX=SIE(IKMT)                                              RGBVM01A
      GO TO 1500
1462  AREAI=3.14159265*FLOAT(2*I-3)*DR*DR
      IF( CYL.LT.1.0 ) AREAI=DX
      FLI=COFBA(NCOFB)*FNTAU
      WBAR=FLI/RHOII
      W(IKM)=WBAR/AREAI
       IF(NIV.EQ.1) W(IKM)=FLI
       SIEC=SIE(IK  )
       SIEW=SIEII
       SIE(IKM )=(2*SIEW+(ALZ-1.0)*SIEC)/(1.0+ALZ)
      QCB=TQ(IK)
      QWB=TQJET*W(IKM)*W(IKM)
      SCB=TS(IK)
      SWB=TSJET*W(IKM)*DR
       QWB=AMAX1(QWB,1.0E-5)
       SWB=AMAX1(SWB,NU)
       TQ(IKM )=(2*QWB+(ALZ-1.0)*QCB)/(1.0+ALZ)
       TS(IKM )=(2*SWB+(ALZ-1.0)*SCB)/(1.0+ALZ)
1480  CONTINUE                                                    VM148000
1489  CONTINUE                                                    VM148900
      GO TO 1700
C NOTE. COMPUTATION OF SIE AND RHO FOR VARIABLE OR FUNCTIONAL INFLOW
C NOTE. AT A BOUNDARY WALL .
1500  TR=TI + 459.7
      GO TO( 1510,1520,1530,1540 ),MAT
C NOTE. COMPUTATION FOR SODIUM MATERIAL .
1510  SIEII=0.38935*TR - 0.553E-4*TR*TR + 0.1137E-7*TR*TR*TR-29.02
      RHOII=59.566 - 7.9504E-3*TI - .2872E-6*TI*TI + 0.06035E-9*TI*TI*TI
      AT=397.17/TR + 1.0203
```

```
      TMU=(10.0**AT/3600.)/TR**0.4925
      TK=0.015085 - 5.2167E-6*TI + 5.809E-10*TI*TI
      TEMP =-385.27 + 2.6602*SIEX + 5.9894E-04*SIEX*SIEX +
     1       1.5575E-06*SIEX*SIEX*SIEX-2.9048E-09*SIEX*SIEX*SIEX*SIEX+
     2       1.15427E-12*SIEX*SIEX*SIEX*SIEX*SIEX
      IF( ICSUBP.GT.0 ) TI=TEMP
      CSUBP=0.38935 - 1.106E-4*TI + 0.3411E-7*TI*TI
      GO TO 1550
C NOTE. COMPUTATION FOR WATER MATERIAL .
 1520 SIEII=1.0004*TI - 32.013
      RHOII=62.742 - 0.372E-2*TI - 0.44E-4*TI*TI
      BT=446.0/( TI+207.0 ) - 5.0
      TMU=1.622*10.**BT
      TK=8.369E-5 + 2.368E-7*TI - 5.89E-10*TI*TI
      TEMP=0.9996*SIEX + 32.0002
      CSUBP=1.0004
      GO TO 1550
 1530 SIEII=  AI*TI*TI +  BI*TI + CI
      RHOII=  AR*TI*TI +  BR*TI +  CR
      TMU  = AMU*TI*TI + BMU*TI + CMU
      TK   =  AK*TI*TI +  BK*TI +  CK
      CIT=CI-SIEX
      TEMP=SI( AI,BI,CIT,-1 )
      CSUBP= ACP*TI*TI + BCP*TI + CCP
      GO TO 1550
 1540 CONTINUE
 1550 NU=TMU/RHOII
      RPRAN=TK/( CSUBP*TMU )
      GO TO KIROBC,( 1162,1262,1362,1462,1605,1615,1625,1635,1736,1756 )
C
C NOTE. COMPUTATION OF THE TAU FACTOR FOR USE IN THE SIE EQUATION .
C
C NOTE. FLUID CELL TO THE   LEFT OF THE IK OBSTACLE .
 1600 ICSUBP=0
      IF( ITAUCN.GT.1 .OR. NTAU.LT.1 ) GO TO 1714
      ASSIGN 1605 TO KIROBC
```

```
      SIEX=SIE(IMK)
      ICSUBP=1
      GO TO 1500
 1605 NTAU=CFC - 29
      RTAU=1./TAU(NTAU)
      P(IK)=1./(1.+DT*RTAU)*( P(IK) + DT*RTAU*TEMP )
      CQ(IMK)=CSUBPO*RTAU*( TEMP-P(IK) )
      ICSUBP=0
      GO TO 1714
C NOTE. FLUID CELL TO THE BOTTOM OF THE IK OBSTACLE .
 1610 ICSUBP=0
      IF( ITAUCN.GT.1 .OR. NTAU.LT.1 ) GO TO 1724
      ASSIGN 1615 TO KIROBC
      SIEX=SIE(IKM)
      ICSUBP=1
      GO TO 1500
 1615 NTAU=CFC - 29
      RTAU=1./TAU(NTAU)
      P(IK)=1./(1.+DT*RTAU)*( P(IK) + DT*RTAU*TEMP )
      CQ(IKM)=CSUBPO*RTAU*( TEMP-P(IK) )
      ICSUBP=0
      GO TO 1724
C NOTE. FLUID CELL TO THE   TOP  OF THE IK OBSTACLE .
 1620 ICSUBP=0
      IF( ITAUCN.GT.1 .OR. NTAU.LT.1 ) GO TO 1744
      ASSIGN 1625 TO KIROBC
      SIEX=SIF(IKP)
      ICSUBP=1
      GO TO 1500
 1625 NTAU=CFC - 29
      RTAU=1./TAU(NTAU)
      CQ(IKP)=CSUBPO*RTAU*(TI-P(IK))
      ICSUBP=0
      GO TO 1744
C NOTE. FLUID CELL TO THE  RIGHT OF THE IK OBSTACLE .
 1630 ICSUBP=0
```

R3BVM03A

```
      IF( ITAUCN.GT.1 .OR. NTAU.LT.1 ) GO TO 1764
      ASSIGN 1635 TO KIROBC
      SIEX=SIE(IPK)
      ICSUBP=1
      GO TO 1500
 1635 NTAU=CFC - 29
      RTAU=1./TAU(NTAU)
      P(IK)=1./(1.+DT*RTAU)*( P(IK) + DT*RTAU*TEMP )
      CQ(IPK)=CSUBPO*RTAU*( TEMP-P(IK) )
      ICSUBP=0
      GO TO 1764
C
C NOTE. COMPUTATUON OF OBSTACLE SUBREGIONS BOUNDARY CONDITIONS .
C
 1700 KK=1
      ITAUCN=ITAUCN + 1
      I1=2
      I2=IBP1
      K1=2
      K2=KBP1
      IF( IOBS.EQ.0 ) GO TO 1990
      NDERR=0
      NDERL=0
      NDERB=0
      NDERT=0
      NCOFT=0
      NCOFR=0
      DO 1789 I=I1,I2
      KK=KK + K2NC
      LWPC=0
      DO 1779 K=K1,K2
      LWPC=LWPC + NWPC
      IK=KK + LWPC
      IMK=IK - K2NC
      IKM=IK - NWPC
      IKP=IK + NWPC
```

```
      IPK=IK + K2NC
      ICFC=CF(IK)
      CFC=ICFC
      IF( CFC.EQ.1 )  GO TO 1778
      CFT=IICFT(IK)+1
      CFB=IICFB(IK)+1
      CFR=IICFR(IK)+1
      CFL=IICFL(IK)+1
      IF( CFT.GT.1 )  GO TO 1710
      IF( CFB.GT.1 )  GO TO 1710
      IF( CFR.GT.1 )  GO TO 1710
      IF( CFL.GT.1 )  GO TO 1710
      U(IK)=0.0
      U(IMK)=0.0
      W(IK)=0.0
      W(IKM)=0.0
      TS(IK)=0.0
      TQ(IK)=0.0
      SIE(IK)=0.0
      GO TO 1770
C NOTE. OBSTACLE BOUNDARY CONDITION AT THE  LEFT  FACE .
1710  GO TO( 1720,1600 ),CFL
C NOTE. NON-FLUID CELL TO THE  LEFT  OF THE IK OBSTACLE .
1712  U(IMK)=0.0
      GO TO 1720
C NOTE. FLUID CELL TO THE   LEFT OF THE IK OBSTACLE .
1714  U(IMK)=0.0
      NRIGID=KDERBC + 1
      GO TO ( 1715,1716 ),NRIGID
C NOTE. RIGID BOUNDARY AT THE   LEFT FACE .
1715  W(IK)=FSLIP*W(IMK)
      SIE(IK)=SIE(IMK)
      TQ(IK)=TQ(IMK)
      TS(IK)=TS(IMK)
      GO TO 1720
C NOTE. DERIVED BOUNDARY CONDITION AT THE  LEFT  FACE .
```

```
1716  WC=W(IMK)
      QC=TQ(IMK)
      SC=TS(IMK)
      NDERL=NDERL + 1
      WSA=USLOB(NDERL)
      QW=5.*WSA*WSA
      SW=WSA*WSA*HDX/WC
      W(IK)=-WC
      TQ(IK)=2.*QW - QC
      TS(IK)=2.*SW - SC
      GO TO 1712
C NOTE. OBSTACLE BOUNDARY CONDITION AT THE BOTTOM FACE .
1720  GO TO( 1730,1610 ),CFB
C NOTE. NON-FLUID CELL TO THE BOTTOM OF THE IK OBSTACLE .
1722  W(IKM)=0.0
      GO TO 1730
C NOTE. FLUID CELL TO THE BOTTOM OF THE IK OBSTACLE .
1724  W(IKM)=0.0
      NRIGID=KDERBC + 1
      GO TO( 1725,1726 ),NRIGID
C NOTE. RIGID BOUNDARY AT THE BOTTOM FACE .
1725  U(IK)=FSLIP*U(IKM)
      SIE(IK)=SIE(IKM)
      TQ(IK)=TQ(IKM)
      TS(IK)=TS(IKM)
      GO TO 1730
C NOTE. DERIVED BOUNDARY CONDITION AT THE BOTTOM FACE .
1726  UCT=U(IKM)
      QCT=TQ(IKM)
      SCT=TS(IKM)
      NDERB=NDERB + 1
      USAT=USBOB(NDERB)
      QWT=5.*USAT*USAT
      SWT=USAT*USAT*HDZ/UCT
      U(IK)=-UCT
      TQ(IK)=2.*QWT - QCT
```

```
      TS(IK)=2.*SWT - SCT
      GO TO 1722
C NOTE. OBSTACLE BOUNDARY CONDITION AT THE   TOP  FACE .
1730  IF( CFC.GE.30 ) GO TO 1740
C NOTE. VARIABLE BOUNDARY OPTION AT THE  TOP  FACE .
      NCFT=CFC - 21
      GO TO( 1732,1734,1740,1740,1740 ),NCFT
C NOTE. CONSTANT INFLOW AT THE  TOP  FACE .
1732  W(IK)=WOBI
      GO TO 1745
C NOTE. VARIABLE OR FUNCTIONAL INFLOW AT THE TOP FACE .
1734  NCOFT=NCOFT + 1
      TI=OFOBTB(NCOFT)*T1NTAU + OFOBTC(NCOFT)*T2NTAU
     1+OFOBTD(NCOFT)*T3NTAU+OFOBTE(NCOFT)*T4NTAU+OFOBTF(NCOFT)*T5NTAU
      ASSIGN 1736 TO KIROBC
      SIEX=SIE(IKP)                                              RGBVMO1A
      GO TO 1500
1736  AREAI=3.14159265*FLOAT(2*I-3)*DR*DR
      IF( CYL.LT.1.0 ) AREAI=DX
      FLI=OFOBTA(NCOFT)*FNTAU
      WBAR=FLI/RHOII
      W(IK)=WBAR/AREAI
       IF(NIV.EQ.1) W(IK)=FLI
       SIEC=SIE(IKP )
       SIEW=SIEII
       SIE(IK  )=(2*SIEW+(ALZ-1.0)*SIEC)/(1.0+ALZ)
      QCT = TQ(IKP)
      QWT = TQJET * W(IK)*W(IK)
      SCT = TS(IKP)
      SWT = TSJET * W(IK) * DR
       QWT=AMAX1(QWT,1.0E-5)
       SWT=AMAX1(SWT,NU)
       TQ(IK  )=(2*QWT+(ALZ-1.0)*QCT)/(1.0+ALZ)
       TS(IK  )=(2*SWT+(ALZ-1.0)*SCT)/(1.0+ALZ)
      U(IK)=FSLIP*U(IKP)
      GO TO 1750
```

```
C NOTE. OBSTACLE BOUNDARY CONDITION AT THE   TOP  FACE .
1740  GO TO( 1750,1620 ),CFT
C NOTE. NON-FLUID CELL TO THE   TOP  OF THE IK OBSTACLE .
1742  W(IK)=0.0
      GO TO 1750
C NOTE. FLUID CELL TO THE   TOP  OF THE IK OBSTACLE .
1744  W(IK)=0.0
      NRIGID=KDERBC + 1
      GO TO( 1745,1746 ),NRIGID
C NOTE. RIGID BOUNDARY AT THE   TOP  FACE .
 1745 U(IK)=-U(IKP)                                          RGBVM50A
      SIE(IK)=SIE(IKP)
      TQ(IK)=TQ(IKP)
      TS(IK)=TS(IKP)
      GO TO 1750
C NOTE. DERIVED BOUNDARY CONDITION AT THE   TOP  FACE .
1746  UCT=U(IKP)
      QCT=TQ(IKP)
      SCT=TS(IKP)
      NDERT=NDERT + 1
      USAT=USTOB(NDERT)
      QWT=5.*USAT*USAT
      SWT = USAT * USAT * HDZ/UCT
      U(IK) = -UCT
      TQ(IK)=2.*QWT - QCT
      TS(IK)=2.*SWT - SCT
      GO TO 1742
C NOTE. OBSTACLE BOUNDARY CONDITION AT THE  RIGHT FACE .
1750  IF( CFC.GE.30 ) GO TO 1760
C NOTE. VARIABLE BOUNDARY OPTION AT THE RIGHT FACE .
      NCFR=CFC - 21
      GO TO( 1776,1776,1776,1752,1754 ),NCFR
C NOTE. CONSTANT INFLOW AT THE RIGHT FACE .
1752  U(IK)=UOBI
      GO TO 1765
C NOTE. VARIABLE OR FUNCTIONAL INFLOW AT THE RIGHT FACE .
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1754  NCOFR=NCOFR + 1
      TI=OFOBRB(NCOFR)*T1NTAU + OFOBRC(NCOFR)*T2NTAU
     1+OFOBRD(NCOFR)*T3NTAU+OFOBRE(NCOFR)*T4NTAU+OFOBRF(NCOFR)*T5NTAU
      ASSIGN 1756 TO KIROBC
      SIEX=SIE(IPK)                                                RGBVM01A
      GO TO 1500
 1756 AREAK = 3.14159265 * 2*(I-1) * DR * DZ
      IF( CYL.LT.1.0 ) AREAK=DZ
      FLK=OFOBRA(NCOFR)*FNTAU
      UBAR=FLK/RHOII
      U(IK)=UBAR/AREAK
       IF(NIV.EQ.1) U(IK)=FLK
       SIEC=SIE(IPK )
       SIEW=SIEII
       SIE(IK  )=(2*SIEW+(ALX-1.0)*SIEC)/(1.0+ALX)
      QC = TQ(IPK)
      QW = TQJET * U(IK)*U(IK)
      SC = TS(IPK)
      SW = TSJET * U(IK) * DZ
       QW=AMAX1(QW,1.0E-5)
       SW=AMAX1(SW,NU)
       TQ(IK  )=(2*QW+(ALX-1.0)*QC)/(1.0+ALX)
       TS(IK  )=(2*SW+(ALX-1.0)*SC)/(1.0+ALX)
      W(IK)=FSLIP*W(IPK)
      GO TO 1770
C NOTE. OBSTACLE BOUNDARY CONDITION AT THE  RIGHT FACE .
1760  GO TO( 1770,1630 ),CFR
C NOTE. NON-FLUID CELL TO THE  RIGHT OF THE IK OBSTACLE .
1762  U(IK)=0.0
      GO TO 1770
C NOTE. FLUID CELL TO THE  RIGHT OF THE IK OBSTACLE .
1764  U(IK)=0.0
      NRIGID=KDERBC + 1
      GO TO( 1765,1766 ),NRIGID
C NOTE. RIGID BOUNDARY AT THE  RIGHT FACE .
1765  W(IK)=FSLIP*W(IPK)
```

```
      SIE(IK)=SIE(IPK)
      TQ(IK)=TQ(IPK)
      TS(IK)=TS(IPK)
      GO TO 1770
C NOTE. DERIVED BOUNDARY CONDITION AT THE  RIGHT FACE .
1766  WC=W(IPK)
      QC=TQ(IPK)
      SC=TS(IPK)
      NDERR=NDERR + 1
      WSA=USROB(NDERR)
      QW=5.*WSA*WSA
      SW = WSA * WSA * HDX/WC
      W(IK) = -WC
      TQ(IK)=2.*QW - QC
      TS(IK)=2.*SW - SC
      GO TO 1762
1770  IF( CFT.EQ.2 .AND. CFC.GE.30 ) W(IK)=0.0
1776  IF( CFR.EQ.2 .AND. CFC.LT.25 ) U(IK)=0.0
1778  CONTINUE
1779  CONTINUE
1789  CONTINUE
1990  GO TO KBC,( 2000,2990,4100,5000,5060 )
C
C NOTE. CHECKS FOR INITIAL CYCLES PRINTS ,I.E. NPRT=0 NO PRINT,
C NOTE. NPRT=1 CYCLE 0 PRINT AND NPRT=2 CYCLE 0,1 PRINTS .
C
2000  IF( NCYC.LT.NPRT ) GO TO 2010
      GO TO 2030                                          VM200004
2010  CALL VRPRT
      IF( IPRFM.GT.0 ) CALL VRFLM
C NOTE. CALL TO THE VARIABLE RESISTANCE SUBROUTINE .
C NOTE. BEGIN THE N PASS PHASE OF THE TILDE EQUATION SECTION .
2030  DO 2999 NTE=1,NTPAS
      IF( NWPC.GT.11 ) CALL VREQ
C
C NOTE. U AND W TILDE VELOCITY EQUATIONS SECTION .
```

```
C
C NOTE. TRANSFERS VELOCITIES TO STORAGE ARRAY( AT TIME=N ) .
      K1=1
      K2=KBP2
      LWPC=1 - NWPC
      DO 2109 K=K1,K2
      LWPC=LWPC+NWPC                                                  VM210008
      IK=LWPC
      IKS=I2K2 + IK
      SIE(IKS)=SIE(IK)
      U(IKS)=U(IK)
      W(IKS)=W(IK)
      TQ(IKS)=TQ(IK)
      TS(IKS)=TS(IK)
      CHI(IKS)=CHI(IK)                                                R3BVM52A
      VAP(IKS)=VAP(IK)                                                RGBVM60A
      LIQ(IKS)=LIQ(IK)                                                RGBVM60A
 2109 CONTINUE                                                        VM210900
      I1=2
      I2=IBP1
      K1=2
      K2=KBP2
      KK=0
      KKL = 0
      DO 2989 I=I1,I2
      KK=KK+K2NC                                                      VM221002
      KKL = KKL + K2NCL
      LWPCL = 1
      LWPC=1
      IKMS=I2K2 + 1
      SIE(1)=SIE(IKMS)
      U(1)=U(IKMS)
      W(1)=W(IKMS)
      TQ(1)=TQ(IKMS)
      TS(1)=TS(IKMS)
      CHI(1)=CHI(IKMS)                                                RGBVM52A
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```
      VAP(1)=VAP(IKMS)                                              RGBVM60A
      LIQ(1)=LIQ(IKMS)                                              RGBVM60A
      SIE(IKMS)=SIE(KK+1)
      U(IKMS)=U(KK+1)
      W(IKMS)=W(KK+1)
      TQ(IKMS)=TQ(KK+1)
      TS(IKMS)=TS(KK+1)
      CHI(IKMS)=CHI(KK+1)                                           RGBVM52A
      VAP(IKMS)=VAP(KK+1)                                           RGBVM60A
      LIQ(IKMS)=LIQ(KK+1)                                           RGBVM60A
      GO TO KRU,( 2215,2220 )                                       VM221012
C NOTE. COMPUTATION OF RADIUS CONSTANTS IN THE I DIRECTION .
2215  RR=FLOAT(I-1)*DX
      RC=RR-HDX
      RL=RR-DX
      RRR=1./RR
      RRC=1./RC
      RRC1=RR + HDX
      RRRC=1./RRC1
      RRP=RR + DR
2220  DO 2979 K=K1,K2
C NOTE. COMPUTATION OF CELL INDICES .
      LWPC=LWPC+NWPC                                                VM222002
      IK=KK + LWPC
      LWPCL = LWPCL + NWPCL
      IKL = KKL + LWPCL
      DCR = DIFFCO(IKL)
      DCT = DIFFCO(IKL+1)
      DCL = DIFFCO(IKL+2)
      DCB = DIFFCO(IKL+3)
C NOTE. BYPASS OBSTACLE CELLS .
      CPC=CP(IK)
      IPK=IK + K2NC
      IKP=IK + NWPC
      IMKS=I2K2 + LWPC
      IKMS=IMKS - NWPC
```

```
      UR=U(IPK)
      UC=U(IK)
      UL=U(IMKS)
      WT=W(IKP)
      WC=W(IK)
      WB=W(IKMS)
      PC=P(IK)
      PR=P(IPK)
      PT=P(IKP)
      SIEC=SIE(IK)
      SIER=SIE(IPK)
      SIET=SIE(IKP)
      SIEL=SIE(IMKS)
      SIEB=SIE(IKMS)
      SIECO=SIEO(IK)
      UCO=UO(IK)
      WCO=WO(IK)
C NOTE. COMPUTATION OF TQ AND TS CONSTANTS .
      TQC=TQ(IK)
      TQR=TQ(IPK)
      TQT=TQ(IKP)
      TQL=TQ(IMKS)
      TQB=TQ(IKMS)
      TQCO=TQO(IK)
      TSC=TS(IK)
      TSR=TS(IPK)
      TST=TS(IKP)
      TSL=TS(IMKS)
      TSB=TS(IKMS)
      TSCO=TSO(IK)
      CHIC=CHI(IK)                                         RGBVM52A
      CHIR=CHI(IPK)                                        RGBVM52A
      CHIT=CHI(IKP)                                        RGBVM52A
      CHIL=CHI(IMKS)                                       RGBVM52A
      CHIB=CHI(IKMS)                                       RGBVM52A
      CHICO=CHIO(IK)                                       RGBVM52A
```

```
      VAPC=VAP(IK)                                                      RGBVM60A
      VAPR=VAP(IPK)                                                     RGBVM60A
      VAPT=VAP(IKP)                                                     RGBVM60A
      VAPL=VAP(IMKS)                                                    RGBVM60A
      VAPB=VAP(IKMS)                                                    RGBVM60A
      VAPCO=VAPO(IK)                                                    RGBVM60A
      LIQC=LIQ(IK)                                                      RGBVM60A
      LIQR=LIQ(IPK)                                                     RGBVM60A
      LIQT=LIQ(IKP)                                                     RGBVM60A
      LIQL=LIQ(IMKS)                                                    RGBVM60A
      LIQB=LIQ(IKMS)                                                    RGBVM60A
      LIQCO=LIQO(IK)                                                    RGBVM60A
      IF( CPC.NE.1 )  GO TO 2700
      TSTR=.25*( TSR + TSC + TST + TS(IKP+K2NC) )
      TSBR=.25*( TSR + TSC + TSB + TS(IPK-NWPC) )
      TSTL=.25*( TSL + TSC + TST + TS(IMKS+NWPC) )
      IF( ICALI.EQ.2 ) GO TO 2500
      GO TO KRXRZ,( 2250,2300 )                                         VM222028
C NOTE. STORAGE OF SUBSCRIPTED RX(),RZ() TO CONSTANT RXC AND RZC .
2250  RXC=RX(IK)*ABS( UC )**NRESEX
      RZC=RZ(IK)*ABS( WC )**NRESEX
C NOTE. COMPUTATION OF U TILDE FLUXES .
2300  URA=.5*(UC+UR)                                                    VM230000
      URAA=ABS(URA)                                                     VM230002
      ULA=.5*(UL+UC)                                                    VM230004
      ULAA=ABS(ULA)                                                     VM230006
      FUX=.5*RDX*( URA*(UC+UR) + ALX*URAA*(UC-UR) - ULA*(UL+UC)         VM230008
     1          -ALX*ULAA*(UL-UC) )                                     VM230010
      WTA=.5*(WC+W(IPK))
      WTAA=ABS(WTA)                                                     VM230014
      WBA=.5*(WB+W(IPK-NWPC))
      WBAA=ABS(WBA)                                                     VM230018
      FUZ=.5*RDZ*( WTA*(UC+U(IKP)) + ALZ*WTAA*(UC-U(IKP))
     1          - WBA*(U(IKMS)+UC) - ALZ*WBAA*(U(IKMS)-UC) )
C NOTE. CALCULATION OF THE U TILDE DIFFUSION TERMS .
      DURR=RDRP*RRRC*TSR*( RRP*UR - RR*UC )
```

```
      DURL=RDR*RRC*TSC*( RR*UC - RL*UL )
      DUR=RDR*( DURR - DURL )
      DUZ=RDZ*( TSTR*(U(IK?)-UC)*RDZP - TSBR*(UC-U(IKMS))*RDZM )
      FUT=DUR + DUZ
      GO TO KCLU,( 2370,2400 )
C NOTE. COMPUTATION OF THE U TILDE CYLINDRICAL FLUX TERM .
2370  FCU=.5*RRR*( URA*URA + ULA*ULA + .5*ALX*URAA*(UC-UR)
     1             + .5*ALX*ULAA*(UL-UC) )                      VM237002
C NOTE. COMPUTATION OF W TILDE FLUXES .
2400  UTA=.5*(UC+U(IKP))
      UTAA=ABS(UTA)                                             VM240002
      ULT=.5*(UL+U(IMKS+NWPC))
      ULTA=ABS(ULT)                                             VM240006
      WTA=.5*( WC+WT )
      WTAA=ABS( WTA )
      WBA=.5*( WB+WC )
      WBAA=ABS( WBA )
      FWX=.5*RDX*( UTA*(WC+W(IPK)) + ALX*UTAA*(WC-W(IPK))
     1           - ULT*(W(IMKS)+WC) - ALX*ULTA*(W(IMKS)-WC) )
      FWZ=.5*RDZ*( WTA*(WC+WT) + ALZ*WTAA*(WC-WT)               VM240012
     1           - WBA*(WB+WC) - ALZ*WBAA*(WB-WC) )             VM240014
C NOTE. CALCULATION OF THE W TILDE DIFFUSION TERMS .
      DWRR=RDRP*RR*TSTR*(W(IPK)-WC)
      DWRL=RDRM*RL*TSTL*(WC-W(IMKS))
      DWR=RRC*RDR*( DWRR - DWRL )
      DWZ=RDZP*( TST*(WT-WC)*RDZ - TSC*(WC-WB)*RDZ )
      FWT=DWR + DWZ
      GO TO KCLW,( 2470,2500 )
C NOTE. COMPUTATION OF THE W TILDE CYLINDRICAL FLUX TERM .
2470  FCW=.25*RRC*( UTA*(WC+W(IPK)) + ULT*(W(IMKS)+WC)
     1             + ALX*UTAA*(WC-W(IPK)) + ALX*ULTA*(W(IMKS)-WC) )
C NOTE. COMPUTATION  OF BOTH  Q AND SIGMA TURBULANCE QUANTITIES .
2500  TQRA=.5*(TQC+TQR)
      IF( ICALI.EQ.1 ) GO TO 2591
      TQLA=.5*(TQC+TQL)
      TQTA=.5*(TQC+TQT)
```

```
      TQBA=.5*(TQC+TQB)
      TSRA=.5*(TSC+TSR)
      TSLA=.5*(TSC+TSL)
      TSTA=.5*(TSC+TST)
      TSBA=.5*(TSC+TSB)
C NOTE. CALCULATION OF THE SIJ  TERM,I.E. THE SOURCE TERM .
      SIJ=RDRS*(UC-UL)**2 + RDZS*(WC-WB)**2 + .25*CYL*(RRC*(UC+UL))**2 +
     1    0.03125*( RDZ*( U(IKP)+U(IMKS+NWPC)-U(IKMS)-U(1) )
     2           + RDR*( W(IPK)+W(IPK-NWPC)-W(IMKS)-W(1) ) )**2
C NOTE. CALCULATION OF THE Q EQUATION CONVECTION TERMS .
      CQR=-.5*RRC*RDR*( RR*( UC*(TQC+TQR)  + ALX*ABS(UC)*(TQC-TQR) )
     1               - RL*( UL*(TQL+TQC)  + ALX*ABS(UL)*(TQL-TQC) ) )
      CQZ=-.5*RDZ*(WC*(TQC+TQT) + ALZ*ABS(WC)*(TQC-TQT)
     1           - WB*(TQB+TQC) - ALZ*ABS(WB)*(TQB-TQC) )
C NOTE. CALCULATION OF THE Q EQUATION DIFFUSION TERM .
      DQRR = RRC * RDR * (RR * TSRA * (TQR - TQC)) * DCR
      DQRL = RRC * RDR * (RL * TSLA * ( TQC - TQL)) * DCL
      DQR = RDR * ( DQRR - DQRL)
      DQZT = RDZ * ( TSTA * ( TQT - TQC )) * DCT
      DQZB = RDZ * ( TSBA * ( TQC - TQB )) * DCB
      DQZ = RDZ * ( DQZT - DQZB)
C NOTE. CALCULATION OF THE Q EQUATION DECAY TERM .
      DQ=4.*ALP*TQC/( TSC+1.E-20 )
C NOTE. CALCULATION OF THE NEW Q AT TIME N+1 .
      TQ(IK)=(1./(1.+DT*DQ))*( TQCO + DT*(CQR+CQZ+2.*TSC*SIJ +
     1                        GAM*(DQR+DQZ)) )
C NOTE. COMPUTATION  OF SIGMA QUANTITIES .
C NOTE. CALCULATION OF THE SIGMA EQUATION CONVECTION TERMS .
      CSR=-.5*RRC*RDR*( RR*( UC*(TSC+TSR)  + ALX*ABS(UC)*(TSC-TSR) )
     1               - RL*( UL*(TSL+TSC)  + ALX*ABS(UL)*(TSL-TSC) ) )
      CSZ=-.5*RDZ*( WC*(TSC+TST)  + ALZ*ABS(WC)*(TSC-TST)
     1            - WB*(TSB+TSC)  - ALZ*ABS(WB)*(TSB-TSC) )
C NOTE. CALCULATION OF THE SIGMA EQUATION DIFFUSION TERM .
      IF( I.LT.I2 ) GO TO 2502
      IFLGS=0
      IFLGQ=0
```

```
      IF( TQR.LT.0.0 ) IFLGQ=1
      IF( TSR.LT.0.0 ) IFLGS=1
      IFLG1=IFLGQ+IFLGS
      IF( IFLG1.EQ.2 ) TQR=-TQR
 2502 IF( K.GT.K1 ) GO TO 2504
      IFLGS=0
      IFLGQ=0
      IF( TQB.LT.0.0 ) IFLGQ=1
      IF( TSB.LT.0.0 ) IFLGS=1
      IFLG1=IFLGQ + IFLGS
      IF( IFLG1.EQ.2 ) TQB=-TQB
 2504 IF( K.LT.KBP1 ) GO TO 2506
      IFLGS=0
      IFLGQ=0
      IF( TQT.LT.0.0 ) IFLGQ=1
      IF( TST.LT.0.0 ) IFLGS=1
      IFLG1=IFLGQ + IFLGS
      IF( IFLG1.EQ.2 ) TQT=-TQT
 2506 IF( I.GT.I1 ) GO TO 2508
      IFLGS=0
      IFLGQ=0
      IF( TQL.LT.0.0 ) IFLGQ=1
      IF( TSL.LT.0.0 ) IFLGS=1
      IFLG1=IFLGQ + IFLGS
      IF( IFLG1.EQ.2 ) TQL=-TQL
 2508 CONTINUE
      DSRR = RRC * RDR * ( RR * TQRA * ( TQR/TSR - TQC/TSC )) * DCR
      DSRL = RRC * RDR * ( RL * TQLA * (TQC/TSC - TQL/TSL )) * DCL
      DSR = RDR * ( DSRR - DSRL)
      DSZT = RDZ * ( TQTA * ( TQT/TST - TQC/TSC)) * DCT
      DSZB = RDZ * ( TQBA * ( TQC/TSC - TQB/TSB )) * DCB
      DSZ = RDZ * ( DSZT - DSZB)
C     DIJ=GAM*TSC/TQC*( DQR+DQZ ) - GAM1*TSC*TSC*TSC/TQC*TQC*(DSR+DSZ)  RGBVM000
      DIJ=GAM*TSC/TQC*( DQR+DQZ ) - GAM1*TSC*TSC*TSC/TQC**2*(DSR+DSZ)   RGBVM000
C     DS=4.*ALPO*TQC/( TSC+1.E-20 )                                     MWG04/78
      DS=ALP*TQC/(TSC+1.E-20)                                           MWG04/78
```

```
C NOTE. CALCULATION OF THE NEW SIGMA AT N+1 .
      TS(IK)=(1./(1.+DT*DS))*( TSCO+DT*(CSR+CSZ+TSC*TSC/TQC*SIJ+DIJ) )
      IF(TQ(IK).LT.ZTQ(K)) TQ(IK)=ZTQ(K)                                RGBVM51A
      IF(TS(IK).LT.ZTS(K)) TS(IK)=ZTS(K)                                RGBVM51A
C  CALCULATION OF TERMS IN THE VAP TRANSPORT EQUATION                   RGBVM61A
      CVR=.5*RRC*RDR*( RR*( UC*(VAPC+VAPR)  + ALX*ABS(UC)*(VAPC-VAPR) )  RGBVM61A
     1               - RL*( UL*(VAPL+VAPC)  + ALX*ABS(UL)*(VAPL-VAPC) ) )RGBVM61A
      CVZ=.5*RDZ*( WC*(VAPC+VAPT)  + ALZ*ABS(WC)*(VAPC-VAPT)             RGBVM61A
     1           - WB*(VAPB+VAPC)  - ALZ*ABS(WB)*(VAPB-VAPC) )           RGBVM61A
       DVRR=RDR*(RR*GAMV*TSRA*DCR*(VAPR-VAPC))                          RGBVM61A
       DVRL=RDR*(RL*GAMV*TSLA*DCL*(VAPC-VAPL))                          RGBVM61A
       DVR=RRC*RDR*(DVRR-DVRL)                                          RGBVM61A
       DVZT=RDZ*(GAMV*TSTA*DCT*(VAPT-VAPC))                             RGBVM61A
       DVZB=RDZ*(GAMV*TSBA*DCB*(VAPC-VAPB))                             RGBVM61A
       DVZ=RDZ*(DVZT-DVZB)                                              RGBVM61A
      VAP(IK)=VAPCO+DT*(-CVR-CVZ+DVR+DVZ)                               RGBVM61A
C  CALCULATION OF TERMS IN THE LIQ TRANSPORT EQUATION                   RGBVM61A
      CLR=.5*RRC*RDR*( RR*( UC*(LIQC+LIQR)  + ALX*ABS(UC)*(LIQC-LIQR) )  RGBVM61A
     1               - RL*( UL*(LIQL+LIQC)  + ALX*ABS(UL)*(LIQL-LIQC) ) )RGBVM61A
      CLZ=.5*RDZ*( WC*(LIQC+LIQT)  + ALZ*ABS(WC)*(LIQC-LIQT)             RGBVM61A
     1           - WB*(LIQB+LIQC)  - ALZ*ABS(WB)*(LIQB-LIQC) )           RGBVM61A
       DLRR=RDR*(RR*GAML*TSRA*DCR*(LIQR-LIQC))                          RGBVM61A
       DLRL=RDR*(RL*GAML*TSLA*DCL*(LIQC-LIQL))                          RGBVM61A
       DLR=RRC*RDR*(DLRR-DLRL)                                          RGBVM61A
       DLZT=RDZ*(GAML*TSTA*DCT*(LIQT-LIQC))                             RGBVM61A
       DLZB=RDZ*(GAML*TSBA*DCB*(LIQC-LIQB))                             RGBVM61A
       DLZ=RDZ*(DLZT-DLZB)                                              RGBVM61A
      LIQ(IK)=LIQCO+DT*(-CLR-CLZ+DLR+DLZ)                               RGBVM61A
C                                                                       RGBVM62A
C  EQUILIBRIUM MOISTURE THERMODYNAMICS SECTION                          RGBVM62A
       CIT=CI-SIEC                                                      RGBVM56A
      TEMPC=SI(AI,BI,CIT,-1)                                            RGBVM56A
      RHOC=AR*TEMPC*TEMPC+BR*TEMPC+CR                                   RGBVM56A
C  CALCULATE THE ABSOLUTE THERMODYNAMIC TEMPERATURE  (DEG C)            RGBVM62A
      ABT=(TEMPC+459.7)*((ZAP(K)/1000.)**.2856)/(1.+0.61*VAP(IK)/RHOC)/1RGBVM62A
     A.8                                                                RGBVM62A
```

```
C  CALCULATE THE SATURATION VAPOR PRESSURE   (MB)                RGBVM62A
      EVAP=10.**(-2937.4/ABT-4.9283*ALOG10(ABT)+23.5518)          RGBVM62A
C  CALCULATE THE VAPOR DENSITY AT SATURATION   (LBM/CU FT)        RGBVM62A
      RHOS=RHOC*0.61*EVAP/ZAP(K)                                  RGBVM62A
      IF(VAP(IK).LT.RHOS) GO TO 300                               RGBVM62A
      IF(VAP(IK).EQ.RHOS) GO TO 320                               RGBVM62A
C  CONDENSE VAPOR AND RELEASE LATENT HEAT                         RGBVM62A
      LIQ(IK)=LIQ(IK)+VAP(IK)-RHOS                                RGBVM62A
      CQ(IK)=CQ(IK)-((VAP(IK)-RHOS)*1075.0)/(DT*RHOC)             RGBVM62A
      VAP(IK)=RHOS                                                RGBVM62A
      GO TO 320                                                   RGBVM62A
C  EVAPORATE LIQUID AND ABSORB LATENT HEAT                        RGBVM62A
  300 IF(LIQ(IK).LE.0.0) GO TO 320                                RGBVM62A
      IF(LIQ(IK).LE.RHOS-VAP(IK)) GO TO 310                       RGBVM62A
      LIQ(IK)=LIQ(IK)-RHOS+VAP(IK)                                RGBVM62A
      CQ(IK)=CQ(IK)+((RHOS-VAP(IK))*1075.0)/(DT*RHOC)             RGBVM62A
      VAP(IK)=RHOS                                                RGBVM62A
      GO TO 320                                                   RGBVM62A
  310 CQ(IK)=CQ(IK)+(LIQ(IK)*1075.0)/(DT*RHOC)                    RGBVM62A
      VAP(IK)=VAP(IK)+LIQ(IK)                                     RGBVM62A
      LIQ(IK)=0.0                                                 RGBVM62A
  320 CONTINUE                                                    RGBVM62A
C                                                                 RGBVM62A
C
C NOTE. COMPUTATION OF SPECIFIC INTERNAL ENERGY .
C
C NOTE. CALCULATION OF THE SIE EQUATION CONVECTION TERMS .
2590  CIR=.5*RRC*RDR*( RR*( UC*(SIEC+SIER) + ALX*ABS(UC)*(SIEC-SIER) )
     1                - RL*( UL*(SIEL+SIEC) + ALX*ABS(UL)*(SIEL-SIEC) ) )
      CIZ=.5*RDZ*( WC*(SIEC+SIET) + ALZ*ABS(WC)*(SIEC-SIET)
     1           - WB*(SIEB+SIEC) - ALZ*ABS(WB)*(SIEB-SIEC) )
C NOTE. CALCULATION OF THE SIE EQUATION DIFFUSION TERMS .
      GAMT=TGAM
      IF( TSC.LE.NU ) GAMT= RPRAN
       DIRR=RDR*(RR*GAMT*TSRA*DCR*(SIER-SIEC))
       DIRL=RDR*(RL*GAMT*TSLA*DCL*(SIEC-SIEL))
```

```
      DIR=RRC*RDR*(DIRR-DIRL)
      DIZT=RDZ*(GAMT*TSTA*DCT*(SIET-SIEC))
      DIZB=RDZ*(GAMT*TSBA*DCB*(SIEC-SIEB))
      DIZ=RDZ*(DIZT-DIZB)
C  CALCULATION OF DECAY HEAT  (BTU/LBM*SEC)                       RGBVM56A
     DECHT=4.150934E10*CHI(IK)*SER/(RHOC*WMOLX)                   RGBVM56A
C NOTE. COMPUTATION OF THE NEW SPECIFIC INTERNAL ENTERGY AT N+1 .
     SIE(IK)=SIECO + DT*( -CIR - CIZ + DIR + DIZ - CQ(IK)+DECHT)  RGBVM56A
C  CALCULATION OF TERMS IN THE CHI TRANSPORT EQUATION             RGBVM52C
     CXR=.5*RRC*RDR*( RR*( UC*(CHIC+CHIR) + ALX*ABS(UC)*(CHIC-CHIR) )  RGBVM52C
    1          - RL*( UL*(CHIL+CHIC) + ALX*ABS(UL)*(CHIL-CHIC) ) )RGBVM52C
     CXZ=.5*RDZ*( WC*(CHIC+CHIT) + ALZ*ABS(WC)*(CHIC-CHIT)        RGBVM52C
    1          - WB*(CHIB+CHIC) - ALZ*ABS(WB)*(CHIB-CHIC) )       RGBVM52C
      DXRR=RDR*(RR*GAMX*TSRA*DCR*(CHIR-CHIC))                     RGBVM52C
      DXRL=RDR*(RL*GAMX*TSLA*DCL*(CHIC-CHIL))                     RGBVM52C
      DXR=RRC*RDR*(DXRR-DXRL)                                     RGBVM52C
      DXZT=RDZ*(GAMX*TSTA*DCT*(CHIT-CHIC))                        RGBVM52C
      DXZB=RDZ*(GAMX*TSBA*DCB*(CHIC-CHIB))                        RGBVM52C
      DXZ=RDZ*(DXZT-DXZB)                                         RGBVM52C
     CHI(IK)=CHICO*(1.0-RLAMB*DT)+DT*(-CXR-CXZ+DXR+DXZ)           RGBVM52C
     GO TO 2650
C NOTE. CALCULATION OF SPECIFIC MATERIAL FOR TEMPERATURE AND
C NOTE. RELATIVE DENSITY .
2591 GO TO ( 2592,2594,2596,2598 ),MAT
C NOTE. CALCULATION OF SODIUM MATERIAL FOR TEMPERATURE AND RHO .
2592 TEMPC=-385.27 + 2.6602*SIEC + 5.9894E-04*SIEC*SIEC +
    1      1.5575E-06*SIEC**3 - 2.9048E-09*SIEC**4 +
    2      1.15427E-12*SIEC**5
     TEMPT=-385.27 + 2.6602*SIET + 5.9894E-04*SIET*SIET +
    1      1.5575E-06*SIET**3 - 2.9048E-09*SIET**4 +
    2      1.15427E-12*SIET**5
     TEMPR=-385.27 + 2.6602*SIER + 5.9894E-04*SIER*SIER +
    1      1.5575E-06*SIER**3 - 2.9048E-09*SIER**4 +
    2      1.15427E-12*SIER**5
     RHOC=59.566 - 7.9504E-3*TEMPC - 0.2872E-6*TEMPC*TEMPC +
    1     0.06035E-9*TEMPC*TEMPC*TEMPC
```

```
      RHOT=59.566 - 7.9504E-3*TEMPT - 0.2872E-6*TEMPT*TEMPT +
     1      0.06035E-9*TEMPT*TEMPT*TEMPT
      RHOR=59.566 - 7.9504E-3*TEMPR - 0.2872E-6*TEMPR*TEMPR +
     1      0.06035E-9*TEMPR*TEMPR*TEMPR
      RHOA=0.5*( RHOC+RHOT )
      RHOAX=0.5*( RHOC+RHOR )
      RHOX=( RHOAX-RHOO )/RHOO
      RHOZ=( RHOA-RHOO )/RHOO
      GO TO 2600
C NOTE. CALCULATION OF WATER  MATERIAL FOR TEMPERATURE AND RHO .
 2594 TEMPC=0.9996*SIEC + 32.0002
      TEMPT=0.9996*SIET + 32.0002
      TEMPR=0.9996*SIER + 32.0002
      RHOC=62.742 -0.372E-2*TEMPC - 0.44E-4*TEMPC*TEMPC
      RHOT=62.742 -0.372E-2*TEMPT - 0.44E-4*TEMPT*TEMPT
      RHOA=0.5*( RHOC+RHOT )
      RHOA=0.5*( RHOC+RHOR )
      RHOZ=( RHOA-RHOO )/RHOO
      RHOR=62.742 -0.372E-2*TEMPR - 0.44E-4*TEMPR*TEMPR
      RHOX=( RHOA-RHOO )/RHOO
      GO TO 2600
 2596 CIT=CI - SIEC
      TEMPC=SI( AI,BI,CIT,-1 )
      CIT=CI-SIET
      TEMPT=SI( AI,BI,CIT,-1 )
      CIT=CI-SIER
      TEMPR=SI( AI,BI,CIT,-1 )
      RHOC=AR*TEMPC*TEMPC + BR*TEMPC + CR
      RHOT=AR*TEMPT*TEMPT + BR*TEMPT + CR
      RHOR=AR*TEMPR*TEMPR + BR*TEMPR + CR
      RHOA=0.5*( RHOC+RHOT )
      RHOZ=( RHOA-RHOO )/RHOO
      RHOA=0.5*( RHOC+RHOR )
      RHOX=( RHOA-RHOO )/RHOO
      GO TO 2600
 2598 CONTINUE
```

```
C NOTE. COMPUTATION OF FULL TILDE EQUATIONS AT TIME=N+1 .
2600  IF( ICALI.EQ.2 ) GO TO 2650
      U(IK)=(1./(1.+DT*RXC))*( UCO + DT*( RDX*(PC-PR) + RHOX*GX
     1                          - FUX - FUZ - FCU + FUT ) )
      W(IK)=(1./(1.+DT*RZC))*( WCO + DT*( RDZ*(PC-PT) + RHOZ*GZ
     1                          - FWX - FWZ - FCW + FWT ) )
2650  IF( ICALI.EQ.1 ) GO TO 2700
C NOTE. UPDATING THE Q EQUATION WITH THE RESISTANCE FACTORS .
      RXC=RX(IK)*ABS( UO(IK) )**NRESEX
      RXL=RX(IMK)*ABS( UO(IMK) )**NRESEX
      RZC=RZ(IK)*ABS( WO(IK) )**NRESEX
      RZB=RZ(IKM)*ABS( WO(IKM) )**NRESEX
2700  U(1)=U(IMKS)
      W(1)=W(IMKS)
      TQ(1)=TQ(IMKS)
      TS(1)=TS(IMKS)
      SIE(1)=SIE(IMKS)
      CHI(1)=CHI(IMKS)                                          RGBVM52B
      VAP(1)=VAP(IMKS)                                          RGBVM60A
      LIQ(1)=LIQ(IMKS)                                          RGBVM60A
      SIE(IMKS)=SIEC
      U(IMKS)=UC
      W(IMKS)=WC
      TQ(IMKS)=TQC
      TS(IMKS)=TSC
      CHI(IMKS)=CHIC                                            RGBVM52B
      VAP(IMKS)=VAPC                                            RGBVM60A
      LIQ(IMKS)=LIQC                                            RGBVM60A
2979  CONTINUE
2989  CONTINUE
      ASSIGN 2990 TO KBC
      IF( NTE.LT.NTPAS ) GO TO 1100
2990  CONTINUE
2999  CONTINUE
      IF( ICALI.EQ.2 ) GO TO 5050
C NOTE. IMPLICIT PRESSURE ITERATION .
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```
4050  IPC=0
      ASSIGN 4100 TO KBC
      GO TO 1100                                                    VM452002
C NOTE. BEGIN PRESSURE ITERATION AFTER SETING BOUNDARY CONDITIONS .
4100  I1=2
      I2=IBP1
      K1=2
      K2=KBP1
      KK=1
      DO 4489 I=I1,I2
      KK=KK + K2NC
      LWPC=0
      RADD=(FLOAT(I)-1.5)*DX                                        VM412006
      RRADD=1./RADD                                                 VM412008
      IF( CYL.LT.EM6 ) RRADD=0.0                                    VM412010
      DO 4479 K=K1,K2
      LWPC=LWPC + NWPC
      IK=KK + LWPC
      IMK=IK - K2NC
      IKM=IK - NWPC
      CPC=CP(IK)
      IF( CPC.NE.1 ) GO TO 4479
      D=RDX*(U(IK)-U(IMK)) + RDZ*(W(IK)-W(IKM)) +.5*RRADD*(U(IK)+U(IMK))
      DTP=-BETA*D                                                   VM420002
      RXC=RX(IK)*ABS( UO(IK) )**NRESEX
      RXL=RX(IMK)*ABS( UO(IMK) )**NRESEX
      RZC=RZ(IK)*ABS( WO(IK) )**NRESEX
      RZB=RZ(IKM)*ABS( WO(IKM) )**NRESEX
      U(IK)=U(IK) + RDX*DTP/(1.+DT*RXC)
      U(IMK)=U(IMK) - RDX*DTP/(1.+DT*RXL)
      W(IK)=W(IK) + RDZ*DTP/(1.+DT*RZC)
      W(IKM)=W(IKM) - RDZ*DTP/(1.+DT*RZB)
      P(IK)=P(IK) + RDT*DTP
C NOTE. CHECKS FOR CONVERGENCE OF PRESSURE FIELD .
      IF( ABS(D).GT.EPS ) IPC=1
4470  CONTINUE
```

```
4479  CONTINUE
4489  CONTINUE
      ITER=ITER + 1
       IF(ITER.LT.1500) GO TO 4510
C NOTE. PRESSURES FAILED TO CONVERGE WITHIN 999 ITERATIONS .
      WRITE(IVDO,50)
       ERR=AMIN1(1.0,.1*NCYC)
      GO TO 4600
4510  IF( IFC.EQ.1 ) GO TO 4050
4600  ASSIGN 5000 TO KBC
      ITERC=ITER
      ITER=0
      GO TO 1100                                          VM452002
C
C NOTE. COMPUTES THE DIVERGENCE ERRORS - ER(IK) .
C
5000  ICALI=2
      GO TO 2030
5050  ASSIGN 5060 TO KBC
      GO TO 1100
5060  ITER=ITERC
      I1=1
      I2=IBP2
      K1=1
      K2=KBP2
      KK=1 - K2NC
      DMX=0.0
      TSMAX=-1.E+20
      TMAX=TSMAX
      WMAX=TMAX
      UMAX=WMAX
      TMIN=+1.E+20
      WMIN=TMIN
      UMIN=WMIN
      PMAX=-1.E+20
      TQMAX=PMAX
```

```
      DO 5029 I=I1,I2
      KK=KK + K2NC
      LWPC=-NWPC
      RRADD=1./( (FLOAT(I)-1.5)*DX )
      DO 5019 K=K1,K2
      LWPC=LWPC + NWPC
      IK=KK + LWPC
      IMK=IK - K2NC
      IKM=IK - NWPC
      CFC=CF(IK)
      IF( CFC.NE.1 ) GO TO 5001
      ER(IK)= RDX*( U(IK)-U(IMK)) + RDZ*( W(IK)-W(IKM))
      DMX=AMAX1( DMX,ABS(ER(IK)) )
     1             + .5*CYL*RRADD*( U(IK)+U(IMK))
 5001 SIEO(IK)=SIE(IK)
      TQO(IK)=TQ(IK)
      TSO(IK)=TS(IK)
      UO(IK)=U(IK)
      WO(IK)=W(IK)
      SIEO(IK)=SIE(IK)
      CHIO(IK)=CHI(IK)                                       RGBVM52B
      VAPO(IK)=VAP(IK)                                       RGBVM60A
      LIQO(IK)=LIQ(IK)                                       RGBVM60A
      SIEC=SIE(IK)
      IF( CFC.GE.30 ) GO TO 5018
      GO TO( 5002,5004,5006,5008 ),MAT
C NOTE. COMPUTATION OF TEMPERATURE FOR SODIUM MATERIAL .
 5002 TEMP =-385.27 + 2.6602*SIEC + 5.9894E-04*SIEC*SIEC +
     1       1.5575E-06*SIEC**3 - 2.9048E-09*SIEC**4 +
     2       1.15427E-12*SIEC**5
      GO TO 5010
C NOTE. COMPUTATION OF TEMPERATURE FOR WATER MATERIAL .
 5004 TEMP=0.9996*SIEC + 32.0002
      GO TO 5010
 5006 CIT=CI-SIEC
      TEMP=SI( AI,BI,CIT,-1 )
```

```
      GO TO 5010
5008  CONTINUE
5010  UMAX=AMAX1( UMAX,U(IK) )
      WMAX=AMAX1( WMAX ,W(IK) )
      TMAX=AMAX1( TMAX,TEMP )
      TSMAX=AMAX1( TSMAX,TS(IK) )
      UMIN=AMIN1( UMIN,U(IK) )
      WMIN=AMIN1( WMIN,W(IK) )
      TMIN=AMIN1( TMIN,TEMP )
      TQMAX=AMAX1( TQMAX,TQ(IK) )
      PMAX=AMAX1( PMAX,P(IK) )
      IF( I.EQ.IDG .AND. K.EQ.KDG ) GO TO 5012
      GO TO 5018
5012  UDG=U(IK)
      WDG=W(IK)
      TDG=TEMP
      TIM=TIMET + DT
5018  CONTINUE
5019  CONTINUE
5029  CONTINUE
      IF( ERF.LT.1 ) GO TO 10000
      CALL VRPRT
      IF( IPRFM.GT.0 ) CALL VRFLM
      RETURN
C
C NOTE. UPDATES TIME AND NUMBER OF CYCLES .
C
10000 TIMET=TIMET + DT
      NCYC=NCYC + 1
      SMSIE=0.0                                                 RGBVM70A
      SMCHI=0.0                                                 RGBVM70A
      FCHI=0.0                                                  RGBVM70A
      VELCHI=0.0                                                RGBVM70A
C     COMPUTE PLUME CENTER AND SIGMA (HEIGHT) FOR CHI DISTRIBUTION  RGBVM54B
      DO 11150 K=2,KBP1                                         RGBVM54A
      DO 11160 I=2,IBP1                                         RGBVM54A
```

```
      IK=1+NWPC*(((I-1)*KBP2)+K-1)                                      RGBVM54A
      CIT=CI-SIE(IK)                                                    RGBVM70A
      TEMPC=SI (AI,BI,CIT,-1)                                           RGBVM70A
      RHOC=AR*TEMPC*TEMPC+BR*TEMPC+CR                                   RGBVM70A
      SMSIE=SMSIE+(RHOC*DX*DZ*SIE(IK))                                  RGBVM70A
      SMCHI=SMCHI+(CHI(IK)-BKGND)                                       RGBVM70A
      FCHI=FCHI+(FLOAT(K)-1.5)*DZ*(CHI(IK)-BKGND)                       RGBVM70A
      VELCHI=VELCHI+WSP(K)*(CHI(IK)-BKGND)                              RGBVM70A
11160 CONTINUE                                                          RGBVM54A
11150 CONTINUE                                                          RGBVM54A
      YPLUME=FCHI/SMCHI                                                 RGBVM70A
      VELCHI=VELCHI/SMCHI                                               RGBVM70A
      DWNDS=DWNDS+VELCHI*DT                                             RGBVM70A
      IF( IDIAG.GT.0 ) WRITE(IVDO,51)  TIMET,NCYC,ITER,DT,DMX
      IF( IDIAG.EQ.0 ) GO TO 11000
C NOTE. CHECKS ON TIME WHEN TO PRINT AND/OR PLOT FILM .
      IF (IDATIN.EQ.1) GO TO 11001
11000 IF( TIMET+1.0E-5 .LT. TPRT ) GO TO 11100
      TPRT=TPRT + TPR
      CALL VRPRT
      GO TO 11100
11001 TPRT=TPRT+TPR
11100 IF( IPRFM.LT.1 .OR. TIMET+1.0E-5.LT.TPLT ) GO TO 11200
      TPLT=TPLT + TPL
      WRITE(IVDO,60) YPLUME,VELCHI,DWNDS                                RGBVM54B
   60 FORMAT(' ',15HPLUME CENTER AT,F8.2,6H FEET.,15H PLUME SPEED IS,   RGBVM54A
     1F8.2,22H  DOWNWIND DISTANCE IS,F6.0)                              RGBVM54B
      WRITE(IVDO,63) SMSIE                                              RGBVM55B
   63 FORMAT(4H    ,'TOTAL  ENERGY   ON MESH IS  ',E12.5)               RGBVM55B
      WRITE(IVDO,51) TIMET,NCYC,ITER,DT,DMX                             RGBVM55B
      CALL VRFLM
11200 CONTINUE
C  TIMING SECTION FOR RESTARTING PROGRAM ON A COARSER MESH              RGBVM55A
11300 IF(TIMET+1.0E-5.LT.TRSTRT(NRSTRT)) GO TO 11400                    RGBVM55A
      CALL COARSE                                                       RGBVM55A
      NRSTRT=NRSTRT+1                                                   RGBVM55A
```

```
      DR=DX                                                             RGBID55B
      RDR=RDX                                                           RGBID55B
      RDRS=1./(DR*DR)                                                   RGBID55B
      RDRM=RDR                                                          RGBID55B
      RDRP=RDRM                                                         RGBID55B
      RDZM=RDZ                                                          RGBID55B
      RDZP=RDZM                                                         RGBID55B
      WRITE(IVDO,40) TIMET,DX,DZ                                        RGBVM55A
   40 FORMAT(22H  PROGRAM RESTART AT  ,F10.3,12H SECONDS    ,'  DX = ', RGBVM55A
     AF6.2,'  DZ = ',F6.2)                                              RGBVM55A
      CALL VRPRT                                                        RGBVM55A
11400 CONTINUE                                                          RGBVM55A
C NOTE. CHECKS ON TIME WHEN TO WRITE MAG TAPE FILE .
12000 IF( TWTD.GE.1.E+5 ) GO TO 12100
      IF (IDATIN.EQ.1) GO TO 12001
      IF( TIMET+1.0E-5 .LT. TWTD ) GO TO 12100
      TWTD=TWTD + TTD
      CALL TAPWRI
      GO TO 12100
12001 TWTD=TWTD+TTD
C NOTE. COMPUTATION OF SPECIFIC DIAGNOSTIC VARIABLES .
12100 GO TO KDIAG,( 12200,12500,13000 )
C NOTE. OUTPUT OF DIAGNOSTIC VARIABLES IF IDIAG=1 FROM CARD NO. 3 .
12200 WRITE(IVDO,54) IDG,KDG,UDG,WDG,TDG,UMAX,UMIN,WMAX,WMIN,TMAX,TMIN
     1 ,TSMAX, EPS
C
C NOTE. COMPUTATION OF TIMING IN VARIOUS PORTIONS OF THE PROGRAM .
C
12500  IF( TIMET+1.E-10 .LT. TFIN ) GO TO 13000
C
C NOTE. CHECKS ON TIME WHEN TO FINISH .
C
13000 IF( TSTEP.LT.EM6 ) GO TO 13010
      IF( NCYC.LT.2 ) GO TO 13010
      ALENG=AMIN1( DX,DZ )
      VEL=AMAX1( UMAX,WMAX )
```

```
      IF ( VEL.GT.EM6 ) DT=TSTEP*ALENG/VEL
      DTDIF=TSTEP*RDXDZS/TSMAX
      VELNEW=AMAX1( UMAX,WMAX )
      TAUDT=0.20*VELNEW/( VELNEW-VELOLD+EM6 )
      TAUDT=ABS( TAUDT )
      DT=AMIN1( DT,DTDIF,TAUDT )
      RDT=1./DT
13010 IDATIN=0
      IF( TIMET+1.0E-5 .LT. TFIN ) GO TO 100
      RETURN
C **** * FORMATS ***** FORMATS ***** FORMATS ***** .
   50 FORMAT(1H ,75H *** ERROR 004 - PRESSURES FAILED TO CONVERGE WITHIN
     1 1500  ITERATIONS . ***)
   51 FORMAT(1H ,5HTIME=,1PE12.4,3H , ,14HCYCLE NUMBER =,I5,3H , ,
     1 28H PRESSURE ITERATION NUMBER =,I4,3H , ,4HDT =,E12.4,3H , ,
     2 16HMAX DIVERGENCE =,E12.4)
   52 FORMAT(1H ,5X,62H THE FOLLOWING DIAGNOSTICS OCCUR AFTER TIME HAS B
     1EEN UPDATED .)
   54 FORMAT(1H ,5X,2HI=,I3,3H K=,I3,4H  U=,1PE12.5,4H  W=,E12.5,
     1 4H  T=,E12.5,3H * ,6H UMAX=,E12.5,6H UMIN=,E12.5/6H WMAX=,E12.5,
     2 6H WMIN=,E12.5,17X,7H  TMAX=,E12.5,7H  TMIN=,E12.5,7H TSMAX=,
     3 E12.5/7H    EPS=,E12.5)
   55 FORMAT(1H ,5X,10HTIME/CYC =,1PE10.3,10H TOT TIME=,E10.3,
     1 10HI/O T/CYC=,E10.3,10H TOT I/O =,E10.3)
      END                                                      VM999991
```

```
************************************************************************ ERAS0010
*                                                                      * ERAS0020
*       TO SET ELEMENTS OF REAL OR INTEGER ARRAYS TO ZERO. A1,A2,...   * ERAS0030
*       ARE ARRAY NAMES AND N1,N2,... ARE INTEGER VALUES OR            * ERAS0040
*       EXPRESSIONS GIVING THE ARRAY SIZES.                            * ERAS0050
**      I.E. - CALL ERASE(C,26*31,N,7*31,E,254)                       ** ERAS0060
*                                                                      * ERAS0070
************************************************************************ ERAS0080
ERASE    START 0                                                         ERAS0090
         SAVE  (14,12),,*                                                ERAS0100
         BALR  12,0                                                      ERAS0110
         USING *,12                                                      ERAS0120
         SR    0,0                                                       ERAS0130
         SR    2,2             PARAMETER LIST INDEX=0                    ERAS0140
         L     6,=F'4'                                                   ERAS0150
E1       L     3,0(2,1)        LOAD 3 WITH ARRAY ADDRESS                 ERAS0160
         L     4,4(2,1)        LOAD 4 WITH ADDRESS OF ARRAY LENGTH       ERAS0170
         L     7,0(4)          LOAD 7 WITH ARRAY LENGTH-1 TIMES 4        ERAS0180
         SLA   7,2                                                       ERAS0190
         SR    7,6                                                       ERAS0200
         SR    5,5                                                       ERAS0210
E2       ST    0,0(5,3)        STORE ZERO                                ERAS0220
         BXLE  5,6,E2                                                    ERAS0230
         LTR   4,4             TEST FOR LAST ARGUMENT IN LIST            ERAS0240
         BM    RETN                                                      ERAS0250
         A     2,=F'8'                                                   ERAS0260
         B     E1              PICK UP NEXT ARGUMENT PAIR                ERAS0270
RETN     RETURN (14,12),T                                                ERAS0280
         END                                                             ERAS0290
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1   VTP
      REAL NU,LIQ,LIQO,LIQI,LOUT                                         RGBMN60A
      DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
     1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
     2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                            RGBMN01A
     A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                                     RGBMN60A
```

```
3    ,TYMF(25),FN(25),TYMT1(25),T1N(25),TYMT2(25),T2N(25),
4    COFBA(25),COFBB(25),COFBC(25),COFTA(25),COFTB(25),COFTC(25),
5    COFRA(25),COFRB(25),COFRC(25),COFLA(25),COFLB(25),COFLC(25),
6    OFOBTA(25),OFOBTB(25),OFOBTC(25),
7    OFOBRA(25),OFOBRB(25),OFOBRC(25),TAU(10),USL(32),USLOB(20),
8    USROB(20),USTOB(20),USBOB(20)
9,COFBD(25),COFBE(25),COFTD(25),COFTE(25),COFTF(25),COFBF(25),
*COFRD(25),COFRE(25),COFLD(25),COFLE(25),COFRF(25),COFLF(25),
AOFOBTD(25),OFOBTE(25),OFOBRD(25),OFOBRE(25),
B  OFOBTF(25),OFOBRF(25),
CTYMT3(25),TYMT4(25),TYMT5(25),T3N(25),T4N(25),T5N(25),
*  IICFR(1),IICFL(1),IICFT(1),IICFB(1)
*   ,ZERO1(1165),ZERO2(608),ZERO3(16),ZERO4(3)
 DIMENSION ZSIE(22),ZTQ(22),ZTS(22),ZVP(22),ZLQ(22),ZAP(22),WSP(22) RGBVM62A
 DIMENSION TRSTRT(5),WZSIE(100),WZTQ(100),WZTS(100)                 RGBVM55A
A,WZVP(100),WZLQ(100),WZAP(100),WWSP(100)                           RGBVM62A
 COMMON/VRCOM/A(14000)                                              RGBMN60A
 COMMON/RGB/RLAMB,CHII,GAMX,NRSTRT,TRSTRT,ZSIE,ZTQ,ZTS,WZSIE,WZTQ,  RGBVM55A
AWZTS,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                   RGBMN60A
B,WSP,WWSP,BKGND,DWNDS                                              RGBMN60B
 COMMON /VRCON/ ALP,ALP0,ALX,ALZ,B0,BETA,BUFL,CFI(9),CFS(9),CYL,
1    DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2    IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3    IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL(20),
4    LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5    TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
*   ,USR(32),UST(22),USB(22),USO(10),FFX3,FFY3
6    ,AW,BW,CW,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7    T0,SIEI,IDG,KDG,TI,MAT,RHO0,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8    T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9    COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
*    OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1    USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*   ,CSUBPO,EPS0,RDXDZS,RLENGH ,TQJET,TSJET
 COMMON /FLMCON/ DROU,DROU0,IPRFM
 COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
```

```
********************************************************************* ERAS0010
*                                                                   * ERAS0020
*       TO SET ELEMENTS OF REAL OR INTEGER ARRAYS TO ZERO. A1,A2,...* ERAS0030
*       ARE ARRAY NAMES AND N1,N2,... ARE INTEGER VALUES OR         * ERAS0040
*       EXPRESSIONS GIVING THE ARRAY SIZES.                         * ERAS0050
**      I.E. - CALL ERASE(C,26*31,N,7*31,E,254)                    ** ERAS0060
*                                                                   * ERAS0070
********************************************************************* ERAS0080
ERASE   START 0                                                       ERAS0090
        SAVE  (14,12),,*                                              ERAS0100
        BALR  12,0                                                    ERAS0110
        USING *,12                                                    ERAS0120
        SR    0,0                                                     ERAS0130
        SR    2,2              PARAMETER LIST INDEX=0                 ERAS0140
        L     6,=F'4'                                                 ERAS0150
E1      L     3,0(2,1)         LOAD 3 WITH ARRAY ADDRESS              ERAS0160
        L     4,4(2,1)         LOAD 4 WITH ADDRESS OF ARRAY LENGTH    ERAS0170
        L     7,0(4)           LOAD 7 WITH ARRAY LENGTH-1 TIMES 4     ERAS0180
        SLA   7,2                                                     ERAS0190
        SR    7,6                                                     ERAS0200
        SR    5,5                                                     ERAS0210
E2      ST    0,0(5,3)         STORE ZERO                             ERAS0220
        BXLE  5,6,E2                                                  ERAS0230
        LTR   4,4              TEST FOR LAST ARGUMENT IN LIST         ERAS0240
        BM    RETN                                                    ERAS0250
        A     2,=F'8'                                                 ERAS0260
        B     E1               PICK UP NEXT ARGUMENT PAIR             ERAS0270
RETN    RETURN (14,12),T                                              ERAS0280
        END                                                           ERAS0290
      INTEGER BUFL,CF,CF1,CFB,CFC,CFI,CFL,CFR,CFS,CFT,CQF,ERF,TD,VNTP,
     1   VTP
      REAL NU,LIQ,LIQO,LIQI,LOUT                                      RGBMN60A
      DIMENSION CF(1),CQ(1),QCON(1),P(1),RX(1),RZ(1),TQ(1),TS(1),U(1),
     1   W(1),ER(1),FFX3(102),FFY3(102),PBTIM(2),UO(1),WO(1),TQO(1),
     2   TSO(1),SIE(1),SIEO(1),CHI(1),CHIO(1)                         RGBMN01A
     A,VAP(1),VAPO(1),LIQ(1),LIQO(1)                                  RGBMN60A
```

```
3    ,TYMF (25) ,FN (25) ,TYMT1 (25) ,T1N (25) ,TYMT2 (25) ,T2N(25) ,
4    COFBA (25) ,COFBB (25) ,COFBC (25) ,COFTA(25) ,COFTB (25) ,COFTC (25) ,
5    COFRA (25) ,COFRB (25) ,COFRC (25) ,COFLA (25) ,COFLB (25) ,COFLC (25) ,
6    OFOBTA (25) ,OFOBTB (25) ,OFOBTC(25) ,
7    OFOBRA(25) ,OFOBRB(25) ,OFOBRC(25) ,TAU (10) ,USL(32) ,USLOB (20) ,
8    USROB (20) ,USTOB (20) ,USBOB (20)
9,COFBD(25) ,COFBE (25) ,COFTD (25) ,COFTE (25) ,COFTF (25) ,COFBF (25) ,
*COFRD(25) ,COFRE(25) ,COFLD(25) ,COFLE(25) ,COFRF(25) ,COFLF (25) ,
AOFOBTD (25) ,OFOBTE(25) ,OFOBRD (25) ,OFOBRE (25) ,
B  OFOBTF (25) ,OFOBRF (25) ,
CTYMT3 (25) ,TYMT4 (25) ,TYMT5(25) ,T3N (25) ,T4N (25) ,T5N (25) ,
*   IICFR(1) ,IICFL (1) ,IICFT (1) ,IICFB (1)
*     ,ZERO1(1165) ,ZERO2 (608) ,ZERO3(16) ,ZERO4(3)
 DIMENSION ZSIE(22) , ZTQ (22) ,ZTS (22) ,ZVP (22) ,ZLQ (22) ,ZAP(22) ,WSP(22) RGBVM62A
 DIMENSION TRSTRT (5) ,WZSIE(100) ,WZTQ(100) ,WZTS(100)                     RGBVM55A
A,WZVP(100) ,WZLQ(100) ,WZAP (100) ,WWSP (100)                               RGBVM62A
 COMMON/VRCOM/A (14000)                                                      RGBMN60A
 COMMON/RGB/RLAMB, CHII, GAMX, NRSTRT, TRSTRT, ZSIE, ZTQ, ZTS, WZSIE, WZTQ,  RGBVM55A
AWZTS ,NPROF,WZVP,WZLQ,ZVP,ZLQ,GAML,GAMV,VAPI,LIQI                           RGBMN60A
B,WSP,WWSP, BKGND, DWNDS                                                     RGBMN60B
 COMMON /VRCON/ ALP,ALP0,ALX,ALZ,B0,BETA,BUFL,CFI (9),CFS(9),CYL,
1    DT,DX,DZ,EM6,EPS,ERF,FSLIP,GAM,GAM1,GX,GZ,HDX,HDZ,I,I1,I2,I2K2,
2    IBP1,IBP2,IBR,IDATIN,IDIAG,IKP2,IOBS,IRSTRT,ITAPW,ITER,IVDI,
3    IVDO,K,K1,K2,K2NC,KBP1,KBP2,KBR,KNC,KWB,KWL,KWR,KWT,LABEL (20) ,
4    LPR,NCYC,NCYCB,NPRT,NU,NWPC,RDT,RDX,RDZ,RDZS,RIBKB,ROI,TD,TFIN,
5    TIMET,TIOSUM,TPL,TPLT,TPR,TPRT,TQI,TSI,TTD,TWTD,UI,WI
*   ,USR(32) ,UST(22) ,USB (22) ,USO (10) ,FFX3,FFY3
6    ,AW,BW,CW ,EPSB,UBLI,UBRI,WBBI,WBTI,WEPS,WOBI,NTPAS,TGAM,CSUBP,
7    T0,SIEI,IDG,KDG,TI,MAT,RHO0,AT,TMU,TK,TYMF,FN,TYMT1,T1N,TYMT2,
8    T2N,RPRAN,NRESEX,NFLOW,NT1,NT2,TSTEP,KDERBC,UOBI,COFBA,COFBB,
9    COFBC,COFTA,COFTB,COFTC,COFRA,COFRB,COFRC,COFLA,COFLB,COFLC,
*    OFOBTA,OFOBTB,OFOBTC,OFOBRA,OFOBRB,OFOBRC,TAU,NTAU,USL,
1    USLOB,USROB,USTOB,USBOB,UMAX,WMAX
*   ,CSUBP0,EPS0,RDXDZS,RLENGH ,TQJET, TSJET
 COMMON /FLMCON/ DROU,DROU0,IPRPM
 COMMON /VRMAT3/ AI,BI,CI,AR,BR,CR,AMU,BMU,CMU,AK,BK,CK,ACP,BCP,CCP
```