22.01 Introduction to Ionizing Radiation Fall 2003 Problem Set #2

Due Date: Wednesday, September 24, 2003

Show all work. Provide units on all answers.

- 1. Show that $_{26}^{55}Fe$, which decays to $_{25}^{55}Mn$ by electron capture, cannot decay by positron emission.
- 2. A parent nuclide decays by beta-particle emission into a stable daughter. The major radiations, energies (MeV), and frequencies are:

 β : 3.92 max (7%), 3.10 max (5%), 1,60 max (88%)

γ: 2.32 (34%), 1.50 (54%), 0.820 (49%)

e: 0.818, 0.805

- (a) Draw the decay scheme.
- (b) What is the maximum energy that the antineutrino can receive in this decay?
- (c) What is the value of the internal-conversion coefficient?
- (d) Estimate the L-shell electron binding energy of the daughter nuclide.
- (e) Would daughter x-rays be expected also? Why or why not?
- 3. (a) Calculate the Q value for K orbital-electron capture by the $^{37}_{18}Ar$ nucleus, neglecting the electron binding energy.
- (b) Repeat (a), including the binding energy, 3.20 keV, of the K-shell electron in argon.
- (c) What becomes of the energy released as a result of this reaction?
- 4. The activity of a radioisotope is found to decrease to 45% of its original value in 30 days.
 - (a) What is the decay constant?
 - (b) What is the half-life?
- 5. How long will it take for each of the following radioisotopes to decrease to 0.0001% of its initial activity?
 - (a) ⁶⁴ Copper
 - (b) 41 Scandium
 - (c) ⁹⁹ Technetium
 - (d) 99m Technetium

- 6. A 6.2-mg sample of ⁹⁰Sr is in secular equilibrium with its daughter ⁹⁰Y.
 (a) How many Bq of ⁹⁰Sr are present?

 - (b) How many Bq of ⁹⁰Y are present?
 - (c) What is the mass of the ⁹⁰Y present?
 - (d) What will the activity of the ⁹⁰Y be after 100 y?
- 7. Carbon-14 has a half-life of 5730 years.
 - (a) If you start with one mole of ¹⁴C and wait 1500 years, how much is left?
 - (b) What would be the activity (Bq) of the ¹⁴C sample at 1500 years?
- 8. Three rock samples are being dated by the 40 K/ 40 Ar method. The following data are obtained for the number of parent atoms (40 K) and daughter atoms (40 Ar) in each. What are the ages of rock samples A, B and C?

Sample	⁴⁰ K atoms present	⁴⁰ Ar atoms present
A	7497	1071
В	11480	3827
С	839	2517

- 9. Calculate the number of grams contained in a 1.0 Ci source of the following nuclides:

 - (a) ¹⁸F (b) ¹⁴C (c) ²²²Rn (d) ²³⁵U
- 10. Assume that the equilibrium specific activity of ¹⁴C is 15 Bq per gram total carbon. A sample of wood from an archaeological site is analyzed and found to contain a ¹⁴C activity of 6.1 Bq/g. What is the date you would assign to this site? [You can ignore corrections to the 14 C/ 12 C ratio.]