

DEPARTMENT OF MATERIALS SCIENCE AND ENGINEERING
MASSACHUSETTS INSTITUTE OF TECHNOLOGY

3.225 Electronic and Mechanical Properties of Materials

Summer Term 2002

Problem Set #4
Due: Day #6

1. A silicon step junction diode with a cross-sectional area $A = 10^{-4} \text{ cm}^2$ has a doping of $N_A = 10^{17} \text{ cm}^{-3}$ and $N_D = 10^{15} \text{ cm}^{-3}$. Let $\mu_e = 801 \text{ cm}^2/\text{V}\cdot\text{s}$ and $\tau_e = 0.1 \mu\text{s}$ on the p-side; and let $\mu_h = 477 \text{ cm}^2/\text{V}\cdot\text{s}$ and $\tau_h = 1 \mu\text{s}$ on the n-side.

a) Calculate the current through the diode at room temperature ($KT/q = 0.026 \text{ V}$) if

- (i) $V_A = -50 \text{ V}$,
- (ii) $V_A = -0.1 \text{ V}$, and
- (iii) $V_A = 0.2 \text{ V}$.

b) Assuming that the mobilities and lifetimes do not vary significantly with temperature, repeat part (a) for $T = 500 \text{ K}$.

c) Summarize in your own words what has been exhibited by this problem.

2. A forward-biased silicon diode is sold commercially as a temperature sensor. To use it to measure temperature, it is forward biased with a constant current source and V_A is measured as a function of T .

a) Derive an equation for $V_A(T)$ by letting D/L for holes and electrons be independent of T using the energy gap dependence of

$$E_G = 1.17 - \frac{(4.73 \times 10^{-4})T^2}{(T + 636)} \text{ (eV)}, \quad \text{where } T \text{ is in K.}$$

b) If $n_i = 1.5 (10^{10}) \text{ cm}^{-3}$, $kT = 0.026 \text{ eV}$, $I_0 = 10^{-15} \text{ A}$, and $I = 10^{-4} \text{ A}$ at room temperature (300 K), calculate a formula for $V_A(T)$ and plot it vs. T from 20°C to 200°C. Note it is nearly linear.

c) Derive a formula for dV_A/dT (in mV/K) and determine the slope of the plot of part (b).

3. *P-n* junctions serve as the basis of photovoltaic solar cells. Sketch the I-V characteristics of a junction with
 - a) no illumination,
 - b) illumination with generation rate $G_L = G_{L0}$, and
 - c) illumination with generation rate $G_L = 2G_{L0}$.

4. (Livingston) 16.10