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Relativistic cyclotron radiation detection of tritium decay electrons as a new technique for measuring the neutrino mass

Benjamin Monreal*

Department of Physics, University of California, Santa Barbara, California, USA

Joseph A. Formaggio

Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge Massachusetts, USA (Received 18 April 2009; published 9 September 2009)

The shape of the beta-decay energy distribution is sensitive to the mass of the electron neutrino. Attempts to measure the endpoint shape of tritium decay have so far seen no distortion from the zero-mass form, thus placing an upper limit of $m_{\nu\beta} < 2.3$ eV. Here, we show that a new type of electron energy spectroscopy could improve future measurements of this spectrum and therefore of the neutrino mass. We propose to detect the coherent cyclotron radiation emitted by an energetic electron in a magnetic field. For mildly relativistic electrons, like those in tritium decay, the relativistic shift of the cyclotron frequency allows us to extract the electron energy from the emitted radiation. We present calculations for the energy resolution, noise limits, high-rate measurement capability, and systematic errors expected in such an experiment.

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I. INTRODUCTION

Ever since Enrico Fermi's theory of beta-decay [1], it has been known that the neutrino mass has an effect on the decay kinematics. Measurements have always suggested that this mass is very small, with successive experiments giving upper limits [2,3], most recently $m_{\nu\beta} < 2.3$ eV. The upcoming KATRIN tritium experiment [4] anticipates having a sensitivity of 0.20 eV at 90% confidence. Oscillation experiments, however, tell us that the tritium beta-decay neutrinos are an admixture of at least two mass states, at least one of which has a nonzero mass, such that the effective mass must satisfy $m_{\nu\beta} > 0.005$ eV under the normal hierarchy or $m_{\nu\beta} > 0.05$ eV in the inverted hierarchy [5]. The neutrino mass is an important component of precision cosmology [6], and it may reflect physics at the grand unified theory scale [7]; this provides a strong motivation to find a way to measure tritium beta decay accurately enough to see $m_{\nu\beta}$ down to the oscillation bounds. However, classical spectrometers are limited by the need to transport electrons out of a source.

Tritium decays with a half-life of 12.32 y and maximum electron kinetic energy E of $E_0 = 18575$ eV; the effect of a nonzero neutrino mass is to shift this maximum down to $E_0 - m_{\nu e}$ and to suppress the phase space within a few $m_{\nu e}$ of this endpoint [8]. We note two points about the behavior of an 18575 eV electron in a magnetic field. First, the electron will follow a circular or spiral path with a cyclotron frequency of

$$\omega = \frac{\omega_0}{\gamma} = \frac{qB}{m_e + E}.$$
 (1)

Note, in particular, that this frequency depends on the electron Lorentz factor γ and hence the electron kinetic energy *E*, but does not depend on the pitch angle θ , the angle between the electron velocity and the magnetic field direction. Second, the electron emits coherent cyclotron radiation [9] at frequency $\omega = 2\pi f$; for a wide range of parameters, the power emitted is large enough to be detectable but not so large as to rapidly change the electron's energy. This radiation spectrum therefore is sensitive to the electron energy, and its detection gives us a new form of nondestructive spectroscopy.

II. EXPERIMENTAL CONCEPT

Consider the arrangement shown in Fig. 1. A lowpressure supply of tritium gas is stored in a uniform magnetic field generated by a solenoid magnet. Tritium decay events release electrons with 0 < E < 18575 eV (and velocity $0 < \beta < \beta_e$ where $\beta_e = 0.2625$) in random directions θ relative to the field vector. The electrons follow spiral paths with a velocity component $v_{||} = \beta \cos(\theta)$ parallel to the magnetic field. Each electron emits microwaves at frequency ω and a total power that depends on β and θ

$$P(\beta,\theta) = \frac{1}{4\pi\epsilon_0} \frac{2q^2\omega_0^2}{3c} \frac{\beta^2 \sin^2(\theta)}{1-\beta^2},$$
 (2)

which are detected by an antenna array. We propose to detect the radiation and measure its frequency spectrum, thus obtaining ω and hence *E*.

Although the emitted radiation is narrowband with frequency ω , the signal seen in a stationary antenna is more complicated; generally it includes a Doppler shift due to v_{\parallel} , some dependence on the electron-antenna distance, and

^{*}bmonreal@physics.ucsb.edu

BENJAMIN MONREAL AND JOSEPH A. FORMAGGIO

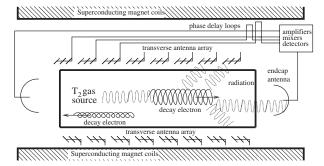


FIG. 1. Schematic of the proposed experiment. A chamber encloses a diffuse gaseous tritium source under a uniform magnetic field. Electrons produced from beta decay undergo cyclotron motion and emit cyclotron radiation, which is detected by an antenna array. See text for more details.

the differential angular power distribution of the emission. The detected signal thus depends on the antenna configuration, and may have a nontrivial frequency content. We discuss two candidate antenna choices and the signal expected in each.

In the first case, we place the tritium source inside of a waveguide, and collect the microwaves with two "endcap" antennae at the ends of the tube. For each electron, both antennae will see Doppler-shifted radiation (one redshift, one blueshift) due to the motion of the guiding center. If we can detect both of these components, both the electron energy and pitch angle are uniquely determined.

In the second case, consider a long array of evenly spaced antennae oriented transverse to the magnetic field. Any single transverse antenna may see the electron passing by, resulting in a complex, broadband "siren" signal,

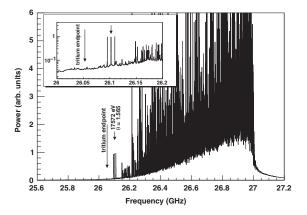


FIG. 2. Simulated microwave spectrum, showing the cyclotron emission of 10^5 tritium decays over 30 μ s in a 10 m long uniform magnet ($\omega_0/2\pi = 27$ GHz, B ~ 1 T) with a finely spaced transverse antenna array. e⁻-T₂ scattering is neglected. The short arrow points out a triplet of spectral peaks generated by an individual high-energy, high-pitch angle electron; the central peak is the cyclotron frequency and the sidebands are due to AM modulation. The log-scale inset zooms in on this electron and the endpoint region.

PHYSICAL REVIEW D 80, 051301(R) (2009)

which sweeps from blueshift to redshift. However, the coherent sum signal from all of the antennae in the array must be quasiperiodic. If the antennae are spaced closely enough, and their signals summed with an appropriate choice of delay lines, almost all of the complex Doppler effects sum incoherently across the array, while the unshifted cyclotron frequency sums coherently. The final summed periodic signal appears as a "carrier wave" at frequency ω with an amplitude modulation, because the antenna response varies periodically along the electron's path, and other small effects (see Fig. 2). In frequency space, these modulations appear as sharp sidebands of the cyclotron frequency.

III. ENERGY RESOLUTION

In order to measure the electron energy to a precision ΔE , we need to measure the frequency to a relative precision of $\Delta f/f = \Delta E/m_{e}$. For $\Delta E = 1$ eV this implies $\Delta f/f = 2 \times 10^{-6}$. In order to achieve a frequency precision of Δf , we need to monitor the signal for $t_{\min} = 2/\Delta f$, according to Nyquist's theorem. This is a key number for several aspects of the experiment; for concreteness, we discuss a reference design with a 1 T magnetic field and a $\Delta E = 1.0$ eV energy resolution. First, we want the beta electrons to have mean free flight times longer than t_{\min} (30 μ s in the reference design). Because of T₂-e⁻ scattering, this places a constraint on the density of the source. The T_2 -e⁻ inelastic scattering cross section [10] at 18 keV is $\sigma_i = 3 \times 10^{-18}$ cm², so in order to achieve the appropriate mean free path the T₂ density cannot exceed $\rho_{max} =$ $(t_{\min}\beta c\sigma)^{-1}$ (1.4 × 10¹¹/cm³ or 4 µTorr in the reference design). It also places a constraint on the physical size of the apparatus; we presume that our measurement ends when the particle reaches the end of some instrumented region, although this is not necessarily the case. If we want to be able to measure particles with minimum pitch angle θ_{\min} , the instrumented region needs to be of length l = $t_{\min}\beta c \cdot \cos(\theta_{\min})$ long; in practice, engineering constraints on l may set θ_{\min} . Finally, t_{\min} also places a constraint on the magnetic field. The electron continuously loses energy via cyclotron radiation; we want to complete our frequency measurement before it has lost energy ΔE due to radiative emission.

IV. BANDWIDTH AND DATA RATE

One great advantage of the MAC-E filter technique used by experiments such as Mainz [2], Troitsk, [3], and KATRIN is the ability to effortlessly reject extremely large fluxes of low-energy electrons, and to activate the detector and data acquisition only for the small fraction of decays near the endpoint. A cyclotron emission spectrometer will be exposed to all of the tritium decays in its field of view (Fig. 2); therefore, it is important that we be able to process these decays without unreasonable pileup.

The main tool for separating signal from background is the high-resolution and high-linearity nature of frequencydomain analysis. Electrons with E = 0 will generate fundamental signals at f = 27.992490 GHz; 18.575 keV electrons will emit fundamentals at about 27.010 643 GHz; as each 1 eV analysis bin is about 50 kHz wide the full region of interest (ROI) is perhaps 1 MHz wide. Detecting a narrow signal in the endpoint ROI is, by itself, insufficient to confidently identify an endpoint electron, since this band is also populated by the low-frequency sidebands of the much more numerous low-energy electrons; we will need to detect at least two spectral lines, possibly three, in order to confidently identify an electron. Any possible confusion source has a lower power than a real ROI source at the same frequency, but because power measurements will be noisy, to be conservative we choose not to rely on them.

Other parameters conspire to mitigate sideband confusion. In order for a low-energy electron to put any sideband at all into the ROI, it must have a large v_{\parallel} to generate the Doppler shift; however, a large v_{\parallel} also leads to a quick exit from the spectrometer (and consequently a broad signal) and to lower emitted power (both due to the quick exit and the β_{\perp}^2 term in the power). Also, the inelastic scattering cross section increases like 1/E for low-energy electrons; if our source is filled with gas such that endpoint electrons have only the minimum tolerable path length, then lowenergy electrons will be suppressed and broadened by a large factor. Accidental coincidences may still occur, however. If the detection criterion requires simply two highpower spectral peaks in coincidence, we estimate that a T_2 source strength of 10000 Bq would give an accidentaltrigger rate comparable to KATRIN's background event rate of one per 10¹³ effective source decays. Requiring a third spectral peak raises this allowable source strength to approximately 10⁹ Bq.

We expect to have many cross-checks to remove accidental coincidences, such as location and polarization data, phase and power relationships between peaks, and so on. Furthermore, for a real multiplet of peaks, all components will appear and disappear from the spectrum at the same time; we expect to be able to suppress the final accidental coincidence rate by at least a few orders of magnitude. Full analysis is beyond the scope of this paper.

The data acquisition rate of our system will be determined by the *full* bandwidth over which we will search for spectral peaks, including fundamentals and sidebands. This could be 100 MHz in the transverse antenna case or several GHz in the endcap antenna case.

V. POWER AND NOISE

It is important that single electrons can be detected well above the noise; first, to avoid false events from noise fluctuations; second, to approach as nearly as possible the Nyquist limit on the frequency resolution; third, to

PHYSICAL REVIEW D 80, 051301(R) (2009)

increase the precision of total-power measurements and start/stop time estimates for each detected electron.

For our reference design with B = 1 T, $\Delta E = 1$ eV, each resolution bin covers 50 kHz. This bandwidth shows a thermal noise power of 6.5×10^{-19} W/K, compared with a possible signal power in the neighborhood of 10^{-15} W. In this frequency band, widely available amplifiers have 10–20 K noise temperatures. For lower magnetic fields, the signal strength varies as B², while the endpoint bandwidth varies as B, so the signal to noise gets worse.

A second noise source comes from the incoherent signals of nonendpoint and/or low-pitch beta electrons. For our 1-T, 30 μ s-analysis-period reference design, each 50 kHz analysis bin near 26 GHz will show approximately 10^{-24} W/Bq of tritium noise. This is compatible with robust signal detection in the presence of the 10^8 – 10^9 Bq source allowed by pileup limitations. We note that this nonthermal power will have non-Gaussian fluctuations.

VI. SYSTEMATIC ERRORS

This technique presents a very different systematic error budget than MAC-E filter experiments. The spectrometer continuously monitors all decay energies, and thus is immune to slow source strength drifts. We anticipate using an essentially static tritium gas whose electrostatic potential is fixed at both ends; this precludes large systematics due to source charging, voltage stability, flow-related Doppler shifts, and T⁻ ion traps. Microwave frequency measurements are stable at the 10^{-12} level.

We have two defenses against magnetic field drifts; first, NMR probes can monitor the total field to a precision of 10^{-7} or better. Second, a weak ^{83m}Kr conversion electron source [11] could be injected directly into the source region, and the position and width of its narrow 30.5 keV L_3 -32 line could be monitored with very high precision. This would also monitor the mechanical stability of the detector array, field direction shifts, and data-analysis biases. Magnetic field inhomogeneities are a source of concern; from the perspective of a purely frequencydomain analysis, they would be a source of line broadening. High-precision energy analysis in a realistic instrument may need to rely on mixed time and frequencydomain analysis, or even pure time-domain pulse fitting. Since these complications are "lossless," we suppose for now that we will eventually be able to recover near-ideal frequency precision in spite of small inhomogeneities.

With respect to scattering, the situation of a microwave spectrometer is unusual. This spectrometer has the ability to run with very low source column densities, and therefore to avoid large spectral distortion due to e^--T_2 scattering, and the attendant uncertainties. On the other hand, we have seen that a larger source column density may be useful for rapidly scattering low-energy electrons and preventing them from generating narrow-line signals, but this may reinsert the scattering systematic error. Electrons may

BENJAMIN MONREAL AND JOSEPH A. FORMAGGIO

also scatter off of the source tube walls. There are two possible avenues for avoiding scattering-related systematics. First, we could use multi-antenna measurements to fiducialize a surface-free, apertureless source. Also, a real scattering event does not simply *change* the electron's energy, but it also broadens or splits its cyclotron emission line; we may be able to detect such scattering event by event.

The excitation spectrum of the $(T^{3}He)^{+}$ daughter ion [12] is unaffected by any improved T₂ measurement technique; it imposes an irreducible 0.36 eV energy spread on high-energy decays, with a difficult-to-estimate systematic error, which the KATRIN collaboration estimates as contributing $\Delta m^{2} < 6 \times 10^{-3} \text{ eV}^{2}$. It is worth considering whether a future experiment could use an atomic *T* source; this is beyond the scope of this paper.

VII. NEUTRINO MASS SENSITIVITY

For simplicity, consider an T₂ experiment that merely counts the T₂ decay rate into the range $E_0 - 1.0 \text{ eV} < E < E_0$ with no background. This quantity is 3.5×10^{-13} in the zero-mass neutrino case and 3.3×10^{-13} for an effective neutrino mass of $m_v = 0.2 \text{ eV}$. In the absence of systematic errors, in order to distinguish these cases with 95% confidence, the experiment would need to observe a total of 3×10^{15} tritium decays, or about 10⁸ Bq-years, which is comparable to our rough estimate of a single confusionlimited data channel. Sensitivity to $m_v = 0.1 \text{ eV}$, comparable with a KATRIN-like systematic error of $\Delta m^2 =$ 0.01 eV^2 would require only 2×10^9 Bq y, which could be achieved by using multiple antenna arrays simultaneously to suppress pileup.

To increase the energy resolution of a microwave spectrometer, we require longer and longer observation times. Surprisingly, this tends to *improve* the single-event sensitivity of the experiment, since the long integrations and narrow bandwidths give us additional noise suppression capabilities. We see no fundamental barrier to improving the energy resolution to 0.36 eV, the irreducible width due

PHYSICAL REVIEW D 80, 051301(R) (2009)

to final state excitations. A more detailed estimate will require a better-specified experimental model with realistic noise, scattering systematics, and signal extraction.

Even in the absence of additional details, we wish note the parameters of an experiment with sensitivity to a neutrino mass as low as 0.007 eV, at the mass scale suggested by solar and reactor neutrino oscillation data. First, the situation unambiguously demands an atomic tritium source, with extremely small molecular tritium contamination; such a source has yet to be developed. Suppose we demand an energy resolution of 0.03 eV; in light of radiative broadening this demands a magnetic field of about B = 0.01 T and observations lasting 100 ms to obtain this precision on 270 MHz cyclotron radiation. At this low frequency, although the emitted power is much reduced, the narrower bandwidth contributes to an acceptable signal-to-noise ratio. In the absence of systematic errors, a 2σ detection of an 0.007 eV neutrino mass requires 10^{20} events, or 4×10^{12} Bq-y (100 Ci-y) of decay data; since we have specified a 100 ms dwell time per observation, a 100 Ci source would supply 3.7×10^{11} electrons per time bin. Our previous pileup limit of \sim 3000 decays per time bin will be relaxed by a factor of the frequency resolution [13], so we can tolerate 10^5 decays per time bin. Under these circumstances, we can accumulate the desired statistics with 3×10^6 parallel measurement channels.

In summary, we show that it is possible to measure the energies of tritium beta-decay electrons by spectroscopy of their cyclotron radiation emission in a magnetic field. With this technique we can perform an array of new and powerful measurements of the endpoint of tritium beta decay.

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