Anomalous Eurasian Snow Extent and the Wintertime AO

by

Elizabeth Whitin Lundgren

B.S., Environmental Engineering Science
B.S., Physics

Massachusetts Institute of Technology
(2007)

Submitted to the Department of Civil and Environmental Engineering
in partial Fulfillment of the Requirements for the Degree of
Master of Science
in Civil and Environmental Engineering

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Abstract

The winter mode of the Arctic Oscillation (AO) is the dominating influence on extratropical winter climate variability in the Northern Hemisphere (NH). The phase of the Arctic Oscillation is characterized by trends in temperature, precipitation, air pressure, and storm tracks over the North Atlantic region, and affects northeastern North America, Europe, and parts of the Mediterranean. While predictability of the AO phase would benefit socio-economic sectors in these densely populated regions by enabling greater foreknowledge of energy demands, precipitation intensity, and storm frequency, it is currently not particularly skillful. Previous studies have demonstrated a link between autumn snow over Eurasia and the AO mode and have proposed a dynamical pathway describing the mechanism that links them.

The goal of this thesis is to present new evidence of a significant relationship between anomalous snow cover and the winter AO phase. Observational evidence of a significant link between extremely high (low) October snow extent anomalies over Eurasia and the negative (positive) AO winter phase is presented. Significant positive (negative) vertical wave activity flux (WAF) anomalies in the stratosphere during December and January are shown to occur following autumns with significantly high (low) snow extent, supporting the dynamical pathway proposed in previous studies. It is concluded that a significant mean snow extent anomaly over Eurasia in October could serve as a predictor for the AO phase of the following winter.

Thesis Supervisor: Dara Entekhabi
Title: Bacardi and Stockholm Water Foundations Professor
Dedicated to my mother,  
Nancy Whitin Truslow Lundgren  

Acknowledgments

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Chapter 1
Introduction and motivation

The weather of the extratropics in the Northern Hemisphere (NH) is most severe during winter months. Europe and northeastern North America are particularly prone to fluctuations of the severity of winter weather from year to year. Unfortunately, weather prediction on timescales greater than a couple of weeks is very poor for the North Atlantic region. The large variability of air temperatures and the frequency and intensity of winter storms therefore pose formidable challenges to the socio-economic sectors of these densely populated regions of the world. With little warning of what weather each winter will bring, the planning of the allocation of resources necessary for adequately coping with the winter climate with minimal cost is exceedingly difficult.

Scientists have long known that winter surface climate over Europe and the northeastern parts of North America are strongly influenced by the Arctic Oscillation (AO). The AO, like the more well-known El Nino/Southern Oscillation (ENSO), is an atmospheric mode of variability describing the large-scale state of the atmosphere. While ENSO largely accounts for the fluctuations of climate in the tropics, the AO explains much of the variance of the atmosphere in the extratropical Northern Hemisphere. The predictive skill of the AO, however, is not as good as that of ENSO. While ENSO is closely correlated with the temperature of the Pacific Ocean, a water body with very high thermal inertia, the AO is an internal mode, largely independent of forcings external to the atmosphere, and therefore much more difficult to predict.

Research over the past couple decades, however, has demonstrated that the AO can be modulated by external conditions, such as ocean temperatures and the cryosphere. In particular, there is good evidence suggesting a significant relationship between snow cover over Eurasia in autumn and the atmospheric state in the Northern Hemisphere in winter. A dynamical pathway from surface snow conditions to the winter NH circulation involving the propagation of stationary planetary waves and coupling between the troposphere and the stratosphere has also gained considerable credence. The possibility that an external measurable condition, such as snow extent, precedes winter conditions on seasonal
timescales brings hope of improving the predictive skill for the AO and winter weather over the North Atlantic regions.

While researchers have explored the relationship between snow extent and winter climate in both modeling and observational studies in the past, and have proposed a model for the dynamic mechanism linking the two phenomena, results have been limited by a trade-off between quality and quantity of available atmospheric data. The sensitivity of variability of winter climate and snow cover require many decades of reliable data to assess meaningful relationships between them. Atmospheric data sets extending back in time to before the 1970s have been derived using either outdated data assimilation methods or different data assimilation methods for different time periods, and are therefore not particularly reliable. Data sets derived consistently with one modern data assimilation method are more ideal. Until recently, however, such high quality data sets have not had large temporal ranges.

The following thesis presents observational work investigating the relationship between autumn snow extent over Eurasia and winter climate dynamics in the Northern Hemisphere using results of the ERA-40 Project. Released in 2007 by the European Centre for Medium-range Weather Forecasting, the ERA-40 Project is the result of the most recent large-scale re-analysis project incorporating multiple observational data sets and modern assimilation models. It has been deemed an improvement upon previous sets of global atmospheric data (Uppula, et al. 2005). Spanning from August 1957 to September 2002, it has a temporal range superior to other atmospheric data sets of similar caliber, enabling it to yield the most reliable results to date for the relationship between anomalous autumn Eurasian snow extent and the winter AO mode.

The research presented in this thesis seeks to answer several questions. First, is the correlation between October snow extent over Eurasia and the climatic conditions during the following winter found in previous studies a result of atmospheric persistence alone? Second, given that snow and atmospheric circulation both vary on decadal timescales, are the relationships between autumn snow and winter climate reported in the literature artifacts of short records of data? Last, is the dynamic pathway between snow and the Arctic Oscillation proposed in previous studies statistically significant?

The thesis will be structured in the following way. An overview of climate science and a literature review of previous related work done will be introduced to the reader in Chapter 2. Chapter 3 will present and discuss the Arctic Oscillation (AO) seasonal teleconnection patterns and the evolution of the AO from 1957 to 2002. An analysis and discussion of October Eurasian snow extent data and the identification of anomalous snow years will follow in Chapter 4. In Chapter 5, a significant relationship between anomalous autumn snow extent and the winter phase of the AO will be demonstrated. Chapter 6 will
present evidence supporting a dynamic pathway between surface snow conditions and the winter zonal mean circulation. Finally, a summary of results and concluding remarks will appear in Chapter 7.
Chapter 2
Background

The following chapter introduces the topics of climate science and atmospheric dynamics and provides a review of previous research relevant to this thesis. It starts with a background in the dynamics of the atmosphere, focusing on the troposphere, stratosphere, and interactions between them via planetary waves. Next, atmospheric variability is discussed with particular emphasis on the Arctic Oscillation. Finally, the surface energy balance of snow as well as research work on the relationship between snow and climate are presented.

2.1 Atmospheric dynamics

2.1.1 The Troposphere and the Stratosphere

The troposphere and the stratosphere are the two layers of the atmosphere closest to the Earth’s surface. The troposphere is the bottom layer of the atmosphere, spanning vertically from the Earth’s surface to anywhere from 5 km above sea-level over the poles to 18 km above sea-level over the tropics. As the densest layer of the atmosphere, it contains approximately 80% of atmospheric mass and is the only region of the atmosphere in which clouds and precipitation occur. Air pressure in the troposphere decreases logarithmically with elevation, from around 1000 mb at sea-level to near 250 mb at the top. The stratosphere is located above the troposphere, separated from it by the thin tropopause. It extends from near the top of the troposphere to between 40 and 50 km above mean sea-level, with air pressures around 250 mb at the bottom, 150 mb near the middle, and 50 mb at the top.

The troposphere is the boundary layer between the atmosphere and the Earth’s surface and is the most turbulent layer of the atmosphere. Its turbulence is indicative of a high level of baroclinicity which is the result of a complex combination of external forcings: mechanical forcing from orography, thermal forcing from land-sea interactions and the
cryosphere, radiative forcing from the sun, and physical forcing due to the rotation of the Earth. The troposphere is particularly turbulent in the extratropics, where the variability of solar radiation is largest and the effects of the rotation of the Earth on air flow trajectories are most pronounced. In these regions, the circulation of the troposphere is highly asymmetric about the pole, dominated by regional cyclonic systems, including both counter-clockwise rotating cyclones and clockwise rotating anti-cyclones, characterized by low and high pressure systems respectively.

Peak turbulence in the Northern Hemisphere (NH) extratropics occurs in winter when atmospheric thermal gradients are maximal. While the extratropical oceans remain relatively warm in winter due to the high thermal inertia of large bodies of water, the continental land masses become relatively cold with the seasonal drop in solar heating. In addition, the differences in insolation between the tropics and the pole are greatest in winter. Both of these phenomena result in the strongest latitudinal and meridional thermal gradients over the mid to high latitudes of the entire year. Winter is therefore also the time of the most severe climate for the Northern Hemisphere extratropical regions, with particularly strong cyclones, such as the classic Nor’easters over North America, and anticyclones, such as the extremely cold Siberian High over Eurasia.

The stratospheric atmosphere lies above the turbulent realm of precipitation and most storms and is largely barotropic, meaning its air density is dependent only on air pressure. As primarily barotropic, the stratosphere is in approximate hydrostatic equilibrium and is therefore quite stable. In the Northern Hemisphere, the circulation in the stratosphere is governed chiefly by the polar vortex and is characterized by the zonal jet which circles roughly symmetrically around the pole. Associated with the zonal jet is the zonal wind which is strongest in the extratropics during winter months when westerlies dominate the stratospheric flow.

While the polar vortex and the zonal wind are primarily stratospheric phenomena, they can influence the circulation and climate of the troposphere through downward coupling between the two layers. Disruptions to the strength of the polar vortex result in changes in the mean zonal wind flow, affecting the circulation below. Several studies have attributed tropospheric conditions to changes in the stratospheric circulation. Hartley et al (1998) showed that disruption of the polar vortex in the Northern Hemisphere stratosphere during winter significantly influences the climate of the upper troposphere. Using observational data, Thompson et al. (2001) showed that a weakening of the polar vortex affects surface weather resulting in a greater frequency of severe cold events over the North Atlantic and East Asia. In a modeling study, Scaife et al. (2005) concluded that downward coupling between the stratosphere and the troposphere accounts for most of the

2.1.2 Planetary waves

Most disruptions to the polar vortex are caused by atmospheric coupling between the stratosphere and the troposphere, through the upward propagation of planetary waves from the troposphere to the stratosphere. Atmospheric waves of many different wavelengths and directions pervade the atmosphere. However, the direction and strength of the zonal wind place limitations on which waves can successfully propagate vertically and how far they can travel. Generally, waves with longer wavelengths are able to propagate further in the presence of stronger westerlies in the atmosphere (Serreze and Barry, 2005). Wintertime, when the zonal mean wind is strongest, is therefore the optimal time for the vertical propagation of planetary waves. Indeed, conditions are most favorable during this time for particularly strong planetary waves with long wavelengths, on the order of half of the zonal perimeter, to penetrate into the stratosphere and weaken the polar vortex.

Planetary waves originate in the troposphere and can be enhanced or dampened near the surface where orographic and thermal forcings are present (Chen and Trenberth 1988, Plumb 1985). Thermal gradients set up by surface conditions, such as sea ice, snow cover, and sea surface temperatures (SST), are a source of baroclinicity and thereby affect wave production. Similarly, mountains affect wave production by effectively disrupting horizontal air flow and creating local pressure gradients.

The modulation of planetary waves is greatest in the presence of both thermal gradients and mountains. The impacts of diabatic forcing and orography on planetary waves are non-linear, with the effects of both thermal and mechanical forcing together greater than the sum of their individual contributions (Ringler and Cook 1988). Differences also exist between the effects of diabatic heating and cooling on both planetary wave and cyclonic activity. While the presence of diabatic heating and orography together enhance cyclonic activity and dampen the upward propagation of waves, diabatic cooling and orography together enhance both anti-cyclonic systems and upward wave production (Chen and Trenberth 1988, Ringler and Cook 1998). The likelihood of enhanced upward vertical wave propagation is therefore greatest over mountainous and cold regions.

For this reason, the region of greatest vertical wave propagation is Eurasia. Eurasia is the largest contiguous land mass on the planet and is home to the most extreme and variable surface conditions in the extratropics of the NH. The continent is shielded from relatively warm ocean air by Europe to the west and its air flow is blocked to the south and
east by numerous mountain ranges, including the towering Tibetan Plateau, extending to the highest elevations on the planet. This unique geography enables the growth of the Siberian High, the massive high pressure system that dominates the region’s winter climate, making Siberia the coldest and harshest place on Earth during winter months, and also the largest source of vertically propagating stationary waves.

2.2 Modes of variability

2.2.1 Teleconnection patterns

While the atmosphere is constantly in chaotic and turbulent flux on short timescales of days and weeks, close scrutiny of large-scale variability reveals recurring patterns in the relationships between the atmospheric states of different geographical regions on much greater timescales. These observed patterns of variability occur with low frequencies, on the order of months to decades (Barnston and Livezey 1987), and are referred to as teleconnection patterns. Defined by Wallace and Gutzler (1981) as the “contemporaneous correlation between geopotential heights on a given pressure surface at widely separated points on Earth,” teleconnection patterns essentially show the simultaneous variability between distant parts of the globe. They can be derived for different regions of the globe using different points of reference for correlation and feature “centers of action,” geographical areas where co-variability is largest. Robust patterns that are consistently replicated using different methods are known as atmospheric modes of variability.

There are multiple modes of variability that are well-documented for the Earth’s atmosphere, with the most well-known being the El Niño/Southern Oscillation. ENSO is a tropical phenomenon that is characterized by an oscillation between two extreme atmospheric states, El Niño and La Niña, with a period ranging from two to seven years (Ahrens, 2009). Each phase of ENSO greatly impacts surface climate across the globe, particularly over tropical locations. An El Niño event, for example, is accompanied by a greater frequency of typhoon development over the tropical central Pacific, a weakening of Indian monsoons, and the development of fewer hurricanes over the tropical Atlantic Ocean (Ahrens, 2009).

Though ENSO is an atmospheric mode of variability, it is the result of coupling between the atmosphere and the ocean. Variability of ENSO is significantly correlated with variability of surface temperatures of the Pacific Ocean. El Niño is associated with a warming of the eastern Pacific Ocean while La Niña is associated with colder than average
surface waters over the central and eastern parts of the tropical Pacific. Because the thermal inertia of oceans is very high, observations of sea surface temperatures allow very skilled prediction of the phases of ENSO and their anticipated weather patterns months in advance.

There are many lesser known modes of variability outside of the tropics that have also been identified. These include the Pacific/North American Mode (PNA), the Eurasian Mode (EUR), the Northern Annular Mode (NAM), the North Atlantic Oscillation (NAO), and the Arctic Oscillation (AO). Meteorologists have been aware of the NAO for the longer than all of the other modes of variability. First identified by Walker and Bliss in 1932, it is characterized by a north-south oscillation of atmospheric mass over the North Atlantic, is strongest in winter, and affects weather over the North Atlantic region (Walker and Bliss 1932, van Loon and Rogers 1978). Other patterns have emerged as mathematical techniques for identifying patterns of variability have been improved. The PNA features centers of action over the North Pacific and the western and eastern parts of the United States and is most pronounced at the 500 mb pressure level. The EUR is similar in influence to the PNA but is characterized by a center of action over Eurasia. The NAM and AO are largely symmetric about the origin and strongly resemble one another, except in winter when the AO features a pressure dipole over the North Atlantic similar to the NAO.

There is some confusion in the literature regarding the differences, if any, between the AO, NAO, and NAM modes. The surface manifestation of the AO in wintertime strongly resembles the NAO pattern. It is thus sometimes used interchangeably with the NAO. The AO is also thought to potentially have the same underlying mechanisms as the Northern Annual Mode (NAM) (Vallis et al. 2004). In this thesis, I will refer only to the AO with the implicit understanding that the regional NAO generally dominates the hemispheric AO during wintertime in the Northern Hemisphere and the AO and the NAM are potentially the same mode.

### 2.2.2 Arctic Oscillation

The Arctic Oscillation is the dominant mode of variability in the mid to high latitudes of the Northern Hemisphere. It is a barotropic mode and exists separately from the turbulence of the troposphere. The AO is strongest during winter and extends from the surface to the stratosphere during this time (Thompson and Wallace 1998, Baldwin and Dunkerton 1999). The AO teleconnection pattern in winter features two oppositely signed centers of action over the northern Atlantic Ocean. The surface manifestation of the AO is characterized by a pressure dipole with a low pressure system over the North Atlantic basin.
off the western coast of Iceland and a relatively high pressure system over Azores to the south whose strengths vary negatively with each other (Wallace and Gutzler 1981, Thompson and Wallace 1998).

The strength of the winter AO, measured by the strength of the pressure gradient over the North Atlantic and also referred to as the AO phase, impacts surface weather, including temperature distribution, precipitation intensity, and storm frequency, over densely populated North Atlantic regions (Walker and Bliss 1932; van Loon and Rogers 1978; Serreze et al. 1997). In the positive phase, the pressure gradient between the two centers of action is particularly strong, resulting in anomalous westerlies over the Atlantic Ocean, warmer than normal temperatures over Europe and the eastern United States, colder temperatures over the northwestern part of the Atlantic, and a shift of storm tracks north over Europe. Conversely, the negative phase is characterized by a particularly weak pressure gradient, and is accompanied by anomalous easterlies, an opposite trend in temperatures, and more storm activity over Western Europe and the northeastern parts of the United States (Hurrell et al. 2003).

The AO is an internal mode of the atmosphere, meaning its existence is a result of the physics of the atmosphere alone, not a product of coupling of the atmosphere with surface conditions as is the case with ENSO. Internal variability of the atmosphere alone, however, fails to explain all of the inter-annual variance of the AO mode over the past several decades (Feldstein 2002). Recent studies have suggested, however, that while external forcings at the surface do not cause the AO, anomalous conditions external to the atmosphere may modulate the strength of the AO, accounting for the unexplained variance (Kodera and Yamazaki 1994, Kodera 1995, Gong et al. 2002). Extreme surface conditions may serve as pathway “triggers,” influencing the progression to a particular phase of the AO given the right conditions (Cohen et al. 2002).

Multiple surface conditions have been linked with the atmospheric circulation and climate to varying degrees. Examining the influence of snow depth, Lu (2008) found a correlation between snow depth over the Tibetan Plateau and the winter Arctic Oscillation. Variability of sea surface temperatures and atmospheric circulation in the Northern Hemisphere has been shown to be correlated on both interannual and interdecadal timescales (Kushnir 1994, Robertson et al. 2000). Further studying SSTs, Saunders and Qian (2002) showed that sea surface temperatures can predict the NAO winter phase weeks in advance with mild success. In addition to snow depth and SSTs, sea ice extent has also been studied. Murray and Simmons (1995) demonstrated that a decrease in sea-ice extent in the past can be linked with weakening westerlies and lower tropospheric warming, and Wang and Ikeda (2000) showed that fluctuations of sea ice are correlated with changes in the Arctic.
Oscillation. Ross and Walsh (1986) looked at the effects of both sea ice and snow cover on local temperatures determining both could be used for short-term forecasting over the United States. Also studying snow cover, Watanabe and Nitta (1998) found that abrupt changes in the winter atmosphere were preceded by anomalous snow cover extents over Eurasia and Cohen and Entekhabi (1999) demonstrated a correlation between Eurasian snow cover in fall and the strength of the winter zonal mean wind.

Of all of the external surface conditions that have been studied for their relationship with the atmosphere, snow extent has received the most attention. While correlations exist between climate and sea surface temperatures, sea ice, and snow depth, their respective lag times are not as great as that for the correlation between snow extent and the winter atmosphere. Snow extent is therefore the strongest contender to serve as a skillful predictor of the winter AO phase.

2.3 Snow and climate

Snow has long been known to influence local climate. Local surface temperature and snow cover variability are significantly correlated, with snow cover reducing local air temperatures (Namias 1962, Dewey 1977, Walsh et al. 1982). The net effect on local temperatures is due to the different physical properties of snow and land. The higher albedo of snow results in a greater percentage of incident short-wave radiation reflected and less solar heat absorbed. More long-wave radiation is lost due to the higher thermal emissivity of snow. In addition, snow cover has a lower thermal conductivity than soil, insulating the ground and suppressing sensible heat flux from the ground to the air. Lastly, the melting of snow acts as a latent heat sink, absorbing heat from the air locally.

While the effects of snow on local temperatures have been documented for many decades, the relationship between snow cover and climate on larger scales has only been explored more recently. Hoskins and Karoly (1981) opened the door to such research by showing that the internal dynamics of the atmosphere may propagate local surface temperature anomalies, such as those produced by snow, to remote distances, enabling local thermal anomalies to impact the general circulation on larger scales. In addition, snow cover interannual variability has been linked with hemispheric atmospheric variability, and anomalous continental snow cover has been shown to influence NH surface climate in winter (Gutzler and Rosen 1992, Walland and Simmons 1997).

Snow cover over the Eurasian continent in particular has emerged as having a relationship with atmospheric circulation. Anomalous snow cover over Eurasia in spring has
been significantly linked with the strength of the Southeast Asian monsoon and the general atmospheric circulation of East Asia (Barnett 1989, Clark and Serreze 2000). Most notable, however, has been the evidence that Eurasian snow cover in autumn affects the winter climate of the region. Significant correlations between autumn Eurasian snow extent and winter Eurasian surface temperatures, remote pressure levels, and the zonal mean wind have all been demonstrated in observational studies (Foster 1983, Walsh and Ross 1988, Cohen and Entekhabi 1999, Cohen et al. 2001).

In particular, a growing body of literature has linked the AO with autumn Eurasian snow cover. Saito et al. (2003) performed an observational study in which a significant correlation between Eurasian autumn snow extent and the winter AO was discovered from 1971 to 2001. Cohen and Entekhabi (2001) used general circulation models (GCM) to show that the NH winter atmospheric circulation incorporating Eurasian snow cover as a boundary condition strongly resembled the AO mode. Gong et al (2002) also used GCMs to demonstrate that imposing significant autumn snow cover over Siberia resulted in AO signals originating in the fall over Siberia. Another modeling study concluded that the impact on the AO using significant snow extent over North America was not comparable to that using Siberian snow cover extent (Gong et al., 2003).

A dynamical pathway involving the diabatic cooling of snow cover, the production of stationary planetary waves, and the coupling of the troposphere and the stratosphere is the leading theoretical mechanism linking autumn Eurasian snow extent and the winter AO. Cohen et al. (2002) postulate that diabatic cooling from extensive snow cover over Eurasia can enhance vertical wave propagation, thereby triggering a dynamic pathway involving the penetration of tropospheric planetary waves into the stratosphere, a weakening of the polar vortex, a deceleration of the zonal mean flow, and a consequent downward refraction of the zonal flow anomaly from the stratosphere to the surface. In this way, the anomalous thermal cooling associated with anomalous snow extent in autumn, the season of largest snow extent variability, may trigger an internal atmospheric mechanism and modulate the wintertime strength of the AO.
Chapter 3
The Arctic Oscillation

Atmospheric variability in winter in the Northern Hemisphere extratropics is dominated by the Arctic Oscillation (AO). Fluctuations in the strength of the AO often mirror fluctuations in the mean state of the atmosphere in time. Because the AO phase in winter has important implications for surface conditions over Europe, eastern North America, and parts of the Mediterranean, understanding the variability of the atmosphere in space and time is vital for improvements in predictive skill.

In this chapter, variability of the AO mode and the NH atmosphere in winter are assessed for the period of September 1957 to August 2002. The seasonal teleconnection patterns of the AO and general patterns of co-variability of different levels of the atmosphere are derived and presented with a discussion of methods used. The percentage of variance explained by each teleconnection pattern is shown to be greatest in January for all pressure levels. A seasonal and monthly index time series of the AO and the mean state of the atmosphere are described and the variability of the mean state of the atmosphere in winter over forty-five years is discussed. Finally, correlations between atmospheric indexes of consecutive months are calculated and conclusions about atmospheric memory are presented.

3.1 Teleconnection patterns

3.1.1 Sea-level

Atmospheric teleconnection patterns are derived using empirical orthogonal function (EOF) analysis. EOF analysis, also referred to as principle component analysis (PCA), is a mathematical method developed in the twentieth century to capture covariability of data with both spatial and temporal dimensions. The substantial correlations between atmospheric data on very large spatial and temporal scales make EOF analysis particularly useful for the study of atmospheric variables. Empirical orthogonal functions are defined as
the orthonormal eigenvectors of the correlation matrix of time- and space-varying data. The eigenvector with the largest eigenvalue captures the majority of variance of the data field. It is possible to derive teleconnection patterns by decomposing a spatial field of time series data into EOFs and mapping the ones with the greatest eigenvalues onto spatial fields.

The teleconnection pattern of the Arctic Oscillation is defined as the first empirical orthogonal function of sea-level pressure in the Northern Hemisphere. In the absence of sea-level pressure data, geopotential height anomalies at the 1000 mb pressure level may be used. The geopotential height is the gravitational potential energy per unit mass of a given pressure level divided by the standard gravity at mean sea-level. It represents the vertical distance above mean-sea level at which the air pressure is equivalent to the pressure level of interest. Co-variability of geopotential heights for a constant pressure level are indicative of co-variability of atmospheric pressure and the general circulation of the atmosphere. Geopotential heights at 1000 mb, approximately mean sea-level, display the

Figure 3.1: Seasonal AO teleconnection patterns for September 1957 to August 2002 computed as the first empirical orthogonal functions of geopotential heights at 1000 mb.
same variability as sea-level air pressures and therefore can be used in EOF analysis to
determine the AO teleconnection pattern.

The first EOF of each season was found using the mean seasonal geopotential
anomalies for the period September 1957 to August 2002. Mean seasonal geopotential
height anomalies were calculated using mean monthly geopotential height data provided in
the ECMWF (European Centre for Medium-range Weather Forecasting) ERA-40 Reanalysis
Project data set. Data points represent mean geopotential heights over a 5 degrees latitude by
5 degrees longitude grid. Seasons are defined as three month intervals; September, October,
and November (SON) for fall, December, January, and February (DJF) for winter, March,
April, and May (MAM) for spring, and June, July, and August (JJA) for summer. Because
the AO is largely an extratropical phenomenon, only data from 20 degrees latitude to the pole
in the Northern Hemisphere was included in this analysis and all analyses that follow in this
thesis.

The AO seasonal teleconnection patterns are shown in Figure 3.1. Areas of color
indicate regions of high variability, with the darkest shadings indicating areas in which
variability is largest. Blue and red regions illustrate how the atmospheric states over these
regions vary with each other; areas of the same color positively co-vary while regions that
are opposite in color co-vary negatively. For instance, the fall EOF1 pattern features a red
area over the Arctic and several areas of blue over the mid-latitudes, particularly over
Northern Europe and the northern part of the Pacific Ocean. The variability of these areas
explains the majority of the variance of the geopotential heights during the fall period with
pressure anomalies over the Arctic and mid-latitude regions tending to occur simultaneously
and with opposite sign.

The most prominent feature common to all AO seasonal patterns is the negative
co-variability of atmospheric pressure over the Arctic and the mid-latitude regions. While
the highly variable region over the Arctic is fairly symmetric around the pole, the areas of
greatest variability in the mid-latitudes are highly asymmetric. Largest negative co-
variability of atmospheric pressure between the Arctic and the mid-latitudes occurs between
the pole and two “centers of action,” one over the Atlantic Ocean and continuing onto the
European continent and the other over the North Pacific, most prominently during fall and
spring. The winter AO pattern is characterized by a pressure dipole with “centers of action”
over the Atlantic basin east of Greenland and off the coast of Spain. This pattern indicates
the tendency for simultaneous and opposite variability of the geopotential heights over the
dipole centers; when the geopotential heights over one center become elevated, those over
the other become depressed. The net effect is a fluctuation in the strength of the north-south
pressure gradient in the region.
3.1.2 Other pressure levels

While the AO pattern is defined by variability at the surface, patterns of variability at pressure levels above the surface are useful for identifying the extent of the influence of the AO as well as other areas of co-variability in the atmosphere. Seasonal teleconnection patterns were derived for pressure levels beyond mean sea-level pressure, from 700 mb in the troposphere to 50 mb in the stratosphere. The patterns show asymmetrical centers of action similar to those of the AO and which are strongest at 500 mb. In winter, the pressure dipole of the AO pattern persists up to the mid-stratosphere, indicating the far-reaching impact of the AO on the atmospheric state during this period. While most tropospheric patterns are highly asymmetrical, patterns in the stratosphere are symmetrical about the pole except in winter, with little if any negative covariance between the Arctic and

Figure 3.2: Interpolated contour plot of percentage of geopotential height variance explained by first empirical orthogonal function of mean seasonal geopotential heights at varying pressure levels.
Figures of seasonal teleconnection patterns can be found in Appendix A. The teleconnection pattern of each season does not explain all of the variation of the geopotential height anomalies. As mentioned in section 3.1.1, information about the amount of variance captured by each pattern lies in the eigenvalue of the first EOF. Figure 5.2 shows an interpolated contour plot of the percentage of variance of geopotential variability explained by the first EOF for different pressure levels and seasons. The figure clearly shows the dominance of the first EOF during winter extending from the surface, throughout the troposphere, and into the stratosphere. The winter AO pattern explains 34.5% of the variability of the winter (DJF) geopotential anomalies at 1000 mb, the largest percentage of variability explained for the troposphere and lower stratosphere over all seasons. In addition, with the exception of the upper stratosphere, the percentage of variance explained by the first EOF is greatest in winter for all pressure levels analyzed. This trend indicates the dominance of the Arctic Oscillation mode in atmospheric variability during winter months.

### 3.2 Evolution of the AO

While the AO teleconnection patterns show co-variability of the atmospheric state in space and time, they do not give any information about periods of fluctuation. To assess how the strength of the AO and the general state of the atmosphere vary in time, monthly and seasonal indexes were developed to represent the contribution of each year to the variability patterns.

Each index time series spans forty-five years and is based on the first empirical orthogonal function for a specific time period and pressure level. Each index is found by projecting a vector of mean geopotential anomalies for a fixed time period of a given year onto the first EOF eigenvector. The series of indexes that result from the projections of anomalies of all years onto the first EOF are normalized, yielding an index time series with zero mean and unit standard deviation.

The index time series for winter (DJF) at 1000 mb represents the fluctuation of the annual strength of the AO. The series is plotted in Figure 2.3 with years shown corresponding to December of the winter of each index. Strongly negative (positive) indexes indicate the negative (positive) phase of the AO. The 1976-1977 winter stands out as featuring an exceptionally strong negative phase of the AO while a strongly positive phase occurred during winter of 1988-1989. The AO index time series also shows a general shift from mostly negative AO phases prior to the late 1980s to mostly positive phases afterwards.
Figure 3.3: Winter EOF1 index time series for 1000 mb geopotential heights. Winters span December of the year indicated to February of the following year.

This phenomenon has been noted by researchers in the past and has largely been theorized to be caused by interdecadal variation, although the increasing concentrations of greenhouse gases in the atmosphere are also theorized by some to be a factor.

### 3.3 Atmospheric persistence

Correlations between consecutive indexes of a given EOF1 index time series enable an assessment of memory in the atmosphere. Because each index is representative of the mean state of the atmosphere, persistence of an index value for a given pressure level in time is indicative of atmospheric persistence. Understanding when and where atmospheric persistence is greatest improves the identification of potential skillful predictors of climate.
To assess the persistence of the atmospheric state on monthly timescales, monthly EOF1 indexes were developed based on the first empirical orthogonal functions of mean monthly geopotential heights for various pressure levels. For each pressure level, intra-monthly correlations of the monthly index time series were computed and significance testing of the correlation was performed. Figure 3.4 shows an interpolated plot of all correlations significantly different from zero.

As the figure shows, there is a notable difference in atmospheric persistence between the troposphere and the stratosphere. While there are significantly high correlations between consecutive monthly indexes in the stratosphere, particularly during summer months and from late fall into winter, persistence in the troposphere is limited to winter months and a brief period during the summer. The stability of the barotropic stratosphere accounts for the
high level of atmospheric memory in the stratospheric layer, with particularly high correlations in summer likely due to the general uniformity of the NH stratosphere in summer when the polar vortex is stable and the stratosphere approaches radiative equilibrium. In contrast, the relatively few periods of significant correlations in the troposphere result from a high level of baroclinicity.

The atmospheric memories of the stratosphere and the troposphere from early fall to late winter have particular relevance to prediction of the AO winter phase. The insignificant tropospheric atmospheric memory throughout the fall months show no atmospheric precursors to the winter AO in the troposphere during the fall. Once it has been established in December, however, persistence of the winter AO phase in the troposphere is seen over all winter months. In the stratosphere, however, persistence exists beginning in October and lasting until spring, though not very strongly. The weak stratospheric persistence is likely due to the high stability of the stratosphere relative to the troposphere. The findings imply that while the mean monthly atmospheric states in the troposphere in fall may not predict the mean winter state of the atmosphere, those in the stratosphere beginning in November may, but to a very limited degree.
Chapter 4
Eurasian snow cover

The analysis of the variability of snow extent has historically been limited by inadequate or non-existent snow records. The examination of the variability and trends connected with years with anomalous snow cover is particularly susceptible to bias due to a lack of data points. Fortunately, work has been done over the past few decades to reconstruct a reliable historical snow extent time series for the globe based on data collected using both old and modern methods.

This chapter presents the snow data that were used for the research presented in this thesis. First, the history and challenges of snow data collection are discussed. Next, the snow data set used is introduced along with observations and comparisons with a data set incorporating more recent observations. Finally, years with anomalous snow extent, the topic of future chapters, are identified.

4.1 Snow Data

The extent of snow cover in the Northern Hemisphere has been documented remotely using satellite imagery since 1966 (Matson et al. 1986). The National Oceanic and Atmospheric Administration (NOAA) has compiled weekly satellite charts since that time with increasing resolution and accuracy as technology has advanced. However, certain challenges will always remain in interpreting real snow extent from satellite imagery, including the lack of data due to clouds, the difficulty in distinguishing between snow and clouds over mountainous areas, and the low visibility of snow over large, dense forests (Robinson 1993). While methodologies for estimating snow coverage were developed soon after satellite imagery became available, the methodology most widely regarded as best in quality was developed by Robinson in 1993. Robinson formulated a new algorithm to more accurately derive continental snow extent extending back in time to 1972. Also known as the Rutgers routine, Robinson's methodology is currently used by the Rutgers Snow Lab to
derive continental snow extent from incoming satellite data.

While remote sensing has enabled reliable estimations of snow extent over vast areas of land for nearly four decades, snow cover data over an even longer period is desirable for the study of anomalous snow events. The more crude land-based observations of snow cover are thus essential for determining snow extent for years before widespread satellite use. While the earliest records of in situ observations of snow cover in the Northern Hemisphere date back over a century, the geographical areas they are available for are limited. In addition, the data records contain many gaps in time. In the past decade, meteorologist Ross D. Brown has addressed these challenges by reconstructing monthly snow cover extent for much of North America and the Eurasian continent using historical records of in situ snow cover observations and reconstructed snow cover data. He was able to reconstruct snow cover extent over Eurasia during October.

Figure 4.1: Comparison of two normalized index time series representing mean snow extent over Eurasia during October.
cover data for North America going back to 1915 for all months and for Eurasia going back to 1922 for October, March, and April (Brown 2000).

Cohen et al. (2007) combined both Robinson's analysis of satellite data and Brown's reconstruction of in situ snow cover observations to develop a time series of mean snow cover over Eurasia in October from 1948 to 2004. The data was normalized to yield an index time series with positive and negative values representing multiples of standard deviations above and below average mean snow extents respectively.

To test the robustness of the data set, another index time series was calculated using a shorter time period but more recent snow cover values, and was compared with the longer index time series. The new series includes only satellite data, spans from October of 1967 to 2008 with the exception of 1969 when data was not available, and was collected

![Figure 4.2: Autocorrelation of snow extent index time series derived by Cohen et al., 2007. The time series spans from 1948 to 2004.](image)

Figure 4.2: Autocorrelation of snow extent index time series derived by Cohen et al., 2007. The time series spans from 1948 to 2004.
entirely by NOAA and made available from the Snow Lab of Rutgers University. The two
index time series are shown in Figure 4.1, with the indexes using only satellite data
represented as open circles and the indexes of the longer series by Cohen et al. (2007)
connected by lines.

The autocorrelation of the longer time series is shown in Figure 4.2. The most
pronounced variability of October Eurasian snow extent occurs with a frequency of about six
years. There is a strong negative autocorrelation for indexes with a lag of around twenty
years. Over the decades for which snow data is available, a shift from a tendency of positive
snow indexes to negative is clearly displayed. This shift occurred in the late seventies to
early eighties, approximately in the middle of the period over which snow data was
considered.

The two series match very well until the 1990s in which the shorter satellite data
indexes are markedly lower than the longer series index values, indicating the trend of
decreased mean snow extent over the past few decades in comparison to the last sixty years.
The observed change in average snow extent implies that one of the following is true:
October snow extent varies on decadal timescales, changes in climate over the past twenty
years have resulted in less snow, or both decadal variation and global change is occurring. It
is certain that snow extent indeed varies on decadal timescales. Whether climate change is
impacting snow extent or not, the decadal variability of snow makes using a long snow data
set imperative in the study of the relationship between snow and the atmosphere. The index
developed by Cohen et al. (2007), incorporating snow data going back to 1948, was thus
used for all snow analyses presented in this thesis henceforth.

4.2 Anomalous snow years

To study the relationship between anomalous snow extent in October and the
atmospheric state of the following winter, fourteen Octobers with the most extreme snow
extent indexes were chosen to represent years with anomalous autumn snow cover. A total
of seven years of each extreme was chosen to minimize clustering while retaining a good
spread of data points. The years chosen for analysis are shown in Table 4.1. Hypothesis
testing shows that the mean anomalously high and low snow index sets are both significantly
different from the mean index over all years with 95% confidence. Anomalous snow years
referenced throughout the rest of this thesis refer to the seven highest and seven lowest
indexes for the years shown in Table 4.1.
<table>
<thead>
<tr>
<th>High Snow Winters</th>
<th>Oct. Snow Index</th>
<th>Low Snow Winters</th>
<th>Oct. Snow Index</th>
</tr>
</thead>
<tbody>
<tr>
<td>1959-1960</td>
<td>1.76</td>
<td>1963-1964</td>
<td>-0.71</td>
</tr>
<tr>
<td>1970-1971</td>
<td>1.52</td>
<td>1990-1991</td>
<td>-1.00</td>
</tr>
</tbody>
</table>

Table 4.1: Winters preceded by seven highest (column 1) and lowest (column 3) mean snow cover anomalies over Eurasia in October and their respective snow indexes.
Chapter 5
Snow and the AO

The strength of the Arctic Oscillation in winter is difficult to predict months in advance because of the apparent lack of direct coupling between the atmosphere and any external parameters with large lag time. Evidence has emerged, however, that snow cover extent, acting as a large-scale thermal boundary condition for the NH atmosphere, may modulate the strength of the AO months in advance. In particular, anomalous fall snow extents may serve as skillful seasonal predictors of the winter AO phase.

This chapter presents observational evidence of a significant relationship between October Eurasian snow extent and the mean state of the atmosphere in the Northern Hemisphere. The snow index presented in Chapter 4 and the EOF1 indexes described in Chapter 3 are compared and correlations are determined. Mean monthly composites of geopotential anomalies following anomalous October Eurasian snow extents are presented and analyzed, demonstrating a significant link between anomalous snow extent and the winter AO phase. Finally, trends in the mean stratospheric states in winters following anomalous October snow cover are discussed.

5.1 Autumn snow and the winter atmosphere

To quantify the relationship between mean October snow extent over Eurasia in the fall and the monthly mean state of the atmosphere over time, Pearson correlations were found between the snow index time series and the EOF1 monthly index for different pressure levels and months. An interpolated contour plot of the correlations between October snow and the EOF1 indexes for September through February is shown in Figure 5.1. Most noticeable is the sign of the correlations between the snow and atmospheric indexes: all correlations are negative. This indicates an inverse relationship between October snow extent and the atmosphere.

The highest correlations occur during January throughout the troposphere and the
stratosphere, with maximum correlation occurring in the mid to lower stratosphere. Correlations for January are significantly different from zero at the 99% confidence level for all pressure levels indicating a significant relationship between October snow extent over Eurasia and the state of the atmosphere from the surface to the upper stratosphere during January. In December, correlation between snow extent and the atmosphere is significant at the 99% level only in the stratosphere and is considerably less than the correlation for the same levels of the atmosphere in January. The significant correlations appear to emerge in the stratosphere starting in November and do not extend to the surface until late December into early January. After January, all correlations between the state of the atmosphere and October snow extent abruptly fall to insignificant levels.

The largest correlations shown in Figure 5.1 occur in January at 150 mb. This correlation between October Eurasian snow extent and stratospheric conditions in January is visible when comparing the EOF1 and snow index time series on the same plot. Figure 5.2 displays the snow index time series and the January monthly mean EOF1 index time series.
Figure 5.2: January EOF1 index time series for 150 mb (solid line) and inverted Eurasian mean October snow index (dashed line).

for 150 mb, with the snow index inverted to show positive correlation. Similarities in shapes of the time series occur throughout much of the time period. Most noticeable are the concurrent anomalies in winter 1976-1977, when the negative phase of the Arctic Oscillation was particularly strong. That winter was preceded by an anomalously large snow extent across Eurasia in October.

5.2 Anomalous snow and the AO phase

The largest correlations between autumn snow extent and the mean state of the atmosphere occur during January, when the Arctic Oscillation is the most dominant factor in the atmospheric state, as shown in Chapter 3. It is useful to remember that the sign of the
EOF1 index at 1000 mb indicates the phase of the AO. Therefore, the significant correlation between the monthly EOF1 index at 1000 mb in winter and snow extent in October indicates a correlation between October snow cover and the phase of the Arctic Oscillation. To further explore the relationship between snow and the AO phase, surface pressure anomalies were examined.

Surface pressure anomalies show the strength of the AO and therefore yield information about the AO phase. As discussed in the previous chapter, the surface manifestation of the winter Arctic Oscillation is a pressure dipole over the North Atlantic region. The pressure dipole features a low pressure system centered off of the eastern coast of Greenland and a relatively high pressure system centered over Azores to the south. The strength of the pressure gradient between the two systems characterizes the AO phase. The positive phase of the AO, with a strong pressure gradient over the North Atlantic region, features above mean surface pressures over Europe and below mean pressures over Iceland and the surrounding areas. The negative AO phase, on the other hand, with a weak pressure gradient between the two centers of action, is indicated by negative pressure anomalies over Europe and positive pressure anomalies towards the pole.

As explained in Chapter 3, geopotential height variability at 1000 mb represents a good approximation of the variability of sea-level pressure and was therefore used to assess trends in the pressure gradient over the North Atlantic following anomalous snow extent in October. For certain grid areas, however, this approximation is not entirely accurate due to topographical realities. For example, most regions of central Greenland reach elevations above 2000 m where surface pressures are below 850 mb. In this region, geopotential at the 1000 mb pressure level does not make sense. A discussion of the limitations of the data set posed by topography as well as the areas for different pressure levels that should not be included in the data analysis are shown in Appendix B. For the North Atlantic region, generally only data over the area of Greenland needs to be neglected for pressure levels greater than 700 mb.

Composites of winter mean geopotential height anomalies at 1000 mb following anomalous October snow extent were constructed to determine if significant trends in the surface pressure gradient over the North Atlantic followed anomalous snow extents. Composites of monthly geopotential anomalies for years associated with anomalously high or low mean October snow extents in Eurasia were constructed separately. Each composite represents the mean of seven mean monthly geopotential anomaly data fields. Months analyzed spanned from Junes preceding anomalous snow cover extent in October to the Augusts following them. Anomalies were determined by substracting the mean geopotential monthly cycle calculated using all forty-five years of ERA-40 data from the geopotential
Figure 5.3: Areas of significant mean geopotential anomalies at 1000 mb for composites of December (top), January (middle), and February (bottom) following anomalous high October Eurasian snow extent (left column) and anomalous low October Eurasian snow extent (right column). Red (blue) areas indicate significantly high (low) anomalies. Light and dark shading represents 95% and 99% confidence levels respectively.

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data of considered months.

Significance testing of the geopotential anomaly composites was performed to determine the areas of the Northern Hemisphere in which the mean anomaly for years following anomalous snow years is significantly different from zero, the mean anomaly over all years. Figure 5.3 displays the areas of the anomalous snow year composites with geopotential anomalies significant at the 90% and 95% confidence levels for December, January, and February.

A consistent and inverse pattern is observable between high and low snow year composites for all three winter months, with the pattern appearing strongest in January and weakest in February. In December, a large region of significantly elevated geopotential anomalies near the surface is present just south of the pole over Eurasia following anomalously extensive Eurasian snow cover in October. During the same month, but following anomalously low snow cover extent, a similarly sized area of significantly depressed geopotential anomalies occurs over the same general region. The December composites also show the development of significant geopotential anomalies in southern Europe and Northern Africa for high snow years and the entire European continent for low snow years. For each December composite, the smaller anomalous region features geopotential anomalies that are opposite in sign to the anomalies significant over the larger area to the north and west.

The patterns of the January composites are similar to those of December but the areas of significant anomalies are greatly expanded. While the near-Arctic areas of significant anomalies in December are offset from the pole towards Eurasia, these areas expand and shift towards the pole in January. The small areas of significant anomalies near Europe, meanwhile, greatly expand in all directions except north.

The January patterns strongly resemble the dipole pressure pattern associated with the January Arctic Oscillation. In addition, the signs of the anomalies for the two January composites are inverted, indicating differences in the strength of the pressure gradient over the Northern Atlantic and therefore the Arctic Oscillation phase. The pattern of the January high snow year composite, with elevated pressures towards the Arctic and below mean pressures in the mid-latitudes, indicates a weak pressure gradient over the North Atlantic region, a sign of the negative phase of the Arctic Oscillation. The pattern of the January low snow year composite, on the other hand, shows the opposite extreme. The elevated heights over Europe and the eastern Atlantic Ocean and the depressed heights over the Arctic imply a very strong pressure gradient between the two regions, indicative of the positive phase of the Arctic Oscillation. The dipole pattern largely disappears in February, reflecting the destabilization of the AO after January.
Figure 5.4: Areas of significant mean geopotential anomalies at 150 mb for composites of December (top) and January (bottom) following anomalous high October Eurasian snow extent (left column) and anomalous low October Eurasian snow extent (right column). Red (blue) areas indicate significantly high (low) anomalies. Light and dark shading represents 95% and 99% confidence levels respectively.

Note that patterns shown are anomalies significant with 90% confidence or more, with the majority of those in the areas of interest significant at the 95% confidence level. The dipole patterns of both January composites, therefore, indicate the two significant extremes of the strength of the Arctic Oscillation, with significantly weaker AO signals (negative phase) following anomalously low October Eurasian snow extent and significantly stronger AO signals (positive phase) following Octobers with high snow cover. It is therefore concluded that there exists a significant link between anomalous snow extent over Eurasia in October and the AO phase of the following winter.
Figure 5.5: Significant mean geopotential anomalies at 1000 mb for November following high snow extent (left) and low snow extent (right). Red (blue) areas indicate significantly high (low) anomalies. Light and dark shading represents 95% and 99% confidence levels respectively.

### 5.3 Anomalous geopotential heights

As demonstrated in Chapter 3, the Arctic Oscillation influences the atmosphere from the surface to the stratosphere in winter. In addition, high correlations exist between October snow cover and the state of the atmosphere in the stratosphere during December and January, as shown in section 5.1. To explore whether a relationship exists between anomalous snow extents and significant trends in geopotential heights for pressure levels above mean sea-level, geopotential anomaly composites for pressure levels extending beyond the surface to 50 mb in the upper stratosphere were computed for the same time periods as presented in section 5.2.

Significance testing of all composites reveal significant trends in geopotential anomalies over the Arctic and North Atlantic, primarily during December and January, for all pressure levels. While the largest areas of significance occur at the surface for both months, as shown in Figure 5.3, the significant patterns extend throughout the troposphere and into the stratosphere. Figure 5.4 shows the areas of significant mean geopotential anomalies at 150 mb, located in the approximate middle of the stratosphere, for December
and January following anomalously high and low snow extents in October. The dipole pattern is clearly visible along with the inversion of the signs of the anomalies between high and low snow year composites. Appendix C contains figures for other pressure levels and months.

While no clear significant trends in geopotential anomalies exist consistently throughout the atmosphere during other months, sea-level surface regions of Eurasia display anomalies during November, when the Siberian High typically strengthens. Figure 5.5 shows the areas of significant mean geopotential anomalies for 1000 mb during this time, a month after anomalous snow extent over Eurasia. A large area of significantly elevated heights is present over the Eurasian continent following high snow extents indicating a stronger than average Siberian High. However, the southern band of the region can be mostly neglected due to the topography of the Tibetan Plateau. Perhaps more interesting is the larger area of depressed geopotential heights over western Siberia to eastern Europe following Octobers with anomalously low snow extents, implying a significantly weaker than normal Siberian High. These results are consistent with the theory that diabatic cooling enhances the development of anti-cyclones such as the Siberian High. Below average snow cover effectively results in below average diabatic cooling at the surface which could theoretically prevent the normal enhancement of the Siberian High, resulting in below average surface pressures.
Chapter 6
Dynamic pathway

As discussed in Chapter 1, atmospheric dynamics are dominated by the motion of waves in the atmosphere. In the extratropics during winter, long planetary waves may propagate vertically from the troposphere to the stratosphere, weakening the strength of the polar vortex and disrupting air circulation in the stratosphere. Stratospheric zonal mean wind anomalies can then refract downwards into the troposphere, affecting circulation patterns and surface weather. In this way, regional tropospheric conditions can impact surface weather at remote locations on a hemispheric scale.

Eurasian snow cover in autumn is theorized to influence the mean state of the atmosphere in winter in this way, through the enhancement of vertically propagating planetary waves. In this chapter, evidence for vertical waves as part of a dynamic pathway between anomalous October snow cover and the winter phase of the AO is presented. Some background about wave activity flux (WAF) is given, followed by the presentation of the mean WAF for the Northern Hemisphere in the troposphere during winter from 1957-1958 to 2001-2002. WAF anomalies during winters following extreme Eurasian autumn snow cover are shown and discussed. Finally, evidence for significantly anomalous high (low) vertical WAF in the stratosphere in winter following anomalous high (low) October Eurasian snow extent is presented.

6.1 Wave activity flux

The propagation of planetary waves is measured as wave activity flux, a three-dimensional local diagnosis of fluctuations of wave propagation. Developed by Plumb (1985), wave activity flux is a parallel to the Eliassen-Palm (EP) flux, a descriptor of vertical and latitudinal wave propagation. EP flux is not ideal for the study of local waves because it describes the average wave propagation per latitude and therefore longitudinal variations in wave activity are obscured by zonal averaging. The more general wave activity flux
decomposes wave flux into latitudinal, longitudinal, and vertical components. It is thus ideal for the study of local wave phenomena. WAF describes stationary wave activity that is the result of linear, quasi-geostrophic disturbances that occur within a zonal flow, a good approximation of the planetary waves relevant to tropospheric-stratospheric coupling and the general circulation of the atmosphere (Plumb 1985). Wave activity flux is calculated from the wind velocity, geopotential, temperature, and vertical temperature gradient deviations from the zonal mean. The mathematics of the calculation of wave activity flux are detailed in Appendix D.

The mean wave activity flux composite for winters (DJF) from 1957-1958 to 2001-2002 at 700 mb is shown in Figure 6.1. DJF WAF was calculated as the mean of monthly mean WAF fields, which were calculated using monthly mean ERA-40 values for
geopotential, wind velocity, and air temperature. The directions of wave propagation parallel to the surface are shown by quivers. Vertical WAF is indicated by color. Positive vertical WAF indicates propagation away from the surface while negative WAF indicates downward propagation.

It is evident from the figure that vertical propagation of planetary waves over the Northern Hemisphere is overwhelmingly either positive or near zero. Vertical WAF is generally only non-negligible in the zonal band from 45 to 60 degrees latitude. While vertical WAF is strong over both ocean basins in this region, it is maximum over the Eurasian/eastern Asian land mass. Vertical WAF over all other continents is significantly weaker.

The high values of vertical WAF over the Eurasian continent is consistent with the unique geography and climate of Eurasia. As described in Chapter 2, WAF is enhanced by the combination of diabatic cooling and orography. During winter months, the Siberian High dominates the circulation of Eurasian air with little interference from warm sea air intrusion because of the expansiveness of the continent. As a result, Eurasia is home to the coldest continental temperatures on Earth during winter. In addition, the extensive mountains of the region act as barriers to the flow, further locking the high pressure system in place. In contrast, the winter high pressure system over Canada is readily weakened by the penetration of warm air from the surrounding oceans.

6.2 Anomalous vertical WAF and snow

6.2.1 Zonal WAF anomalies

Given that planetary waves are enhanced by diabatic cooling at the surface, snow extent over Eurasia is a potential modulator of the strength of vertical WAF over the region. To assess the relationship between snow extent anomalies over Eurasia and trends in planetary wave strength, WAF anomalies were calculated in 6-hr time intervals and composites were constructed for years with anomalously high and low October snow extent. Wave activity flux anomalies along the 60n zonal band from 30E to 150E longitudes, spanning from eastern Europe to the eastern Pacific, were calculated from early November to late February. Both monthly mean and bi-monthly composites were compiled for months following anomalous snow years. Bi-monthly composites for late December and early January following Octobers with anomalous high and low snow extents are shown in Figures 6.2 and 6.3, respectively. See Appendix G for figures for other time periods.
Figure 6.2: Mean vertical zonal WAF anomalies for late Decembers (top) and early
Januarys (bottom) following anomalously high mean October Eurasian snow cover.
Vertical and horizontal components are scaled by 0.05 and 10 respectively.

All composites show high regional variance of WAF in the troposphere with
anomalies varying greatly in intensity, direction in both meridional and vertical dimensions,
and over time. This large variance is a result of the high level of turbulence in the
troposphere. WAF in the troposphere is highly variable, on timescales of days, due to the
high eddy momentum flux associated with storms in the planetary boundary layer. The eddy
momentum flux of storms heavily influences the strength of atmospheric waves and their
direction of propagation.

Stratospheric anomalies, on the other hand, persist in both time and space.
Persistent trends are evident in Figures 6.2 and 6.3 particularly for the vertical propagation of
waves over Eurasia. Eurasia spans from around 60 to 120 degrees East, the center of the
meridional range analyzed. In Figure 6.2, the vertical component of stratospheric anomalies
for both late December and early January following Octobers with high Eurasian snow
Figure 6.3: Mean vertical zonal WAF anomalies for late Decembers (top) and early Januarys (bottom) following anomalously low mean October Eurasian snow cover. Vertical and horizontal components are scaled by 0.05 and 10 respectively.

extents are clearly positive over Eurasia for all stratospheric pressure levels shown. This indicates an elevated flux of vertically propagating planetary waves. Figure 6.3, the composite for low snow years, shows vertical anomalies over the same region to be consistently negative, signifying a below average flux of waves propagating vertically. Other composites, shown in Appendix E, show similar trends starting in late November and ending after early January. The strongest and most consistent anomalies across the zonal band, however, are featured in late December and early January.

6.2.2 Significant anomalies

Significance testing of the vertical WAF anomalies reveals that patterns of
Figure 6.4: Areas of significant mean vertical WAF anomalies at 150 mb for late Decembers (left column) and early Januaries (right column) following anomalously high (top) and low (bottom) mean October Eurasian snow cover. Red (blue) areas indicate significantly high (low) anomalies. Light and dark shading represents 95% and 99% confidence levels respectively.

Anomalous vertical WAF significant at the 90% and 95% confidence levels occur in the stratosphere and not in the troposphere. The stratosphere is largely removed from the turbulent mixing in the troposphere and consequently significant trends over timescales equivalent to the ones analyzed in this study are more readily visible. Significant anomalies in the stratosphere were most pronounced during late December and early January. Significant areas of vertical WAF anomalies at 150 mb for these time periods are shown in Figure 6.4. Red (blue) color covers areas with significantly above (below) average vertical WAF with light and dark shading representing 90% and 95% confidence levels respectively. What stands out are the large swaths of color in the upper right quadrants, covering Eurasia and eastern Asia. For both late December and early January, vertical WAF at 150 mb
Figure 6.5: Areas of significant mean vertical WAF anomalies at 50 mb for late Decembers (left column) and early Januarys (right column) following anomalously high (top) and low (bottom) mean October Eurasian snow cover. Red (blue) areas indicate significantly high (low) anomalies. Light and dark shading represents 95% and 99% confidence levels respectively.

Following anomalously high snow extents over Eurasia are significantly above normal while vertical WAF at the same pressure level following anomalously low snow extents are significantly below normal.

This trend is even more pronounced further up in the stratosphere. Figure 6.5 shows areas of significant vertical WAF at 50 mb for the same time period as Figure 6.4. However, it is noticeable that areas of depressed anomalies for low snow years are much more expansive than the elevated anomalies of high snow years for both pressure levels. In addition, the depressed anomalies more consistently cover the expanse of the Eurasian continent.

Patterns of significant anomalies were considerably weaker for other time
periods. One exception is the low snow years composite for late November which showed significantly depressed vertical WAF across much of Eurasia, eastern Asia, and the north Pacific. However, the strength of the pattern did not continue into early December and high snow years did not show any significant patterns until late December. See Appendix F for more figures.
Chapter 7
Summary and conclusions

This thesis presents observational evidence of a relationship between October Eurasian snow cover extent and the winter Arctic Oscillation, the dominant mode of extratropical variability in the Northern Hemisphere. While previous studies have demonstrated a link between Eurasian snow cover and the Arctic Oscillation, several questions have remained that this thesis seeks to answer. First, can atmospheric persistence alone explain the correlation between winter atmospheric conditions and Eurasian October snow extent? As shown in Chapter 3, the correlations between consecutive monthly EOF1 indexes are insignificant in the troposphere between autumn and winter, indicating negligible tropospheric persistence. Weak stratospheric persistence is observed over the same period, indicating that atmospheric persistence is not the sole explanation for the significant correlation between October snow cover and the AO in winter.

Second, are the relationships between winter NH climate and autumn Eurasian snow extent found in previous studies an artifact of analyzing short records of data for variables with much longer timescales of variability? Previous similar studies have generally used data sets a couple decades long, while both snow and the AO phase vary on decadal timescales. The interpretation of the correlation between snow and the AO as more significant than it actually therefore becomes a possibility. Because both snow extent and the AO phase vary on decadal timescales, a reliable assessment of the correlation between the two must include data that spans several decades. This thesis presents evidence for a significant correlation between Eurasian snow extent and the AO phase from the analysis of data spanning forty-five years, from 1957 to 2002. Getting this result for such a long time range implies the relationship is not simply a result of the analysis of phenomena during a short window of time but is robust over the complete cycles of variability of both snow cover and the AO phase.

Last, is the mechanism linking autumn snow cover and the winter AO, proposed in the literature as a dynamic pathway involving the vertical propagation of stationary planetary waves from the troposphere to the stratosphere, statistically significant? As shown
in Chapter 6, positive (negative) anomalous October snow extent over Eurasia is followed by
significant positive (negative) vertical wave activity flux anomalies over the same region in
December and January. These results support previous theories that anomalous snow extent
may influence the NH winter circulation through the modulation of the production of
vertically propagating stationary waves and further indicate that the evidence supporting the
mechanism is significant.

Future work is necessary to better establish the dynamic pathway between snow
cover and the AO in more fine detail. While significant stratospheric anomalies following
anomalous autumn snow cover are presented in this thesis, evidence of tropospheric
anomalies preceding the stratospheric anomalies is still lacking. Due to the shorter
timescales of tropospheric variability relative to stratospheric variability, analyses on much
shorter timescales than used in the work presented, on the order of days as opposed to weeks,
are necessary to capture significant tropospheric trends. The results of such analyses could
lead to greater insight as to whether modulation of the stratosphere leading to a particular AO
phase is indeed preceded by significant anomalies in the troposphere.

The significant correlation between October Eurasian snow extent and the winter
AO phase demonstrated in this thesis is particularly relevant to predicting the impacts of
global warming on the NH winter climate. The positive AO phase may become more
frequent if anomalously low autumn snow extent over Eurasia occurs more often, a likely
occurrence given a continuous increase in mean global temperature. This would increase the
likelihood of mild winters in Europe and the northeastern United States and also affect
weather patterns over other parts of eastern North America and the Mediterranean. The
physical pathway between snow and the AO may be one mechanism through which the
enhanced greenhouse effect manifests itself as a change in the atmosphere in the extratropics
in winter. It is recommended that general climate models be used to test the sensitivity of
this mechanism to better understand how autumn snow cover may be used in predicting the
AO winter mode on seasonal timescales and the effects of global warming on climate change
in the North Atlantic regions in winter.
Appendix A

Seasonal EOF1 patterns

Seasonal EOF1 patterns for September 1957 to August 2002 are shown below. Colorbars for all figures are equivalent to that shown in Figure 3.1 on p. 25.

Figure A.1: Fall (SON) EOF1 patterns for different pressure levels.
Figure A.2: Winter (DJF) EOF1 patterns for different pressure levels.
Figure A.3: Spring (MAM) EOF1 patterns for different pressure levels.
Figure A.4: Summer (JJA) EOF1 patterns for different pressure levels.
Appendix B
Topography

The topography of continents rises far above sea level in many regions of the Northern Hemisphere. The Rocky Mountains and Greenland both reach up to over 4000 m, while the highest elevation on the planet is on the Tibetan Plateau, with an average elevation of 4500 m above sea-level. Since air pressure decreases with increasing elevation, the air pressure at the surface in these areas are far below mean sea-level pressure. This is illustrated in Figure B.1 which shows the mean surface pressures over the Northern

Figure B.1: Mean NH surface pressures (mb) from January 1949 to May 2008.

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Hemisphere from January 1949 to May 2008. Mean surface pressures were calculated using data from the NCEP/NCAR Reanalysis project.

Climatic analysis of pressure levels close to mean sea-level pressure are therefore not applicable to all parts of the globe. Atmospheric data sets often interpolate gridded data fields at constant pressure levels to allow for complete sets of data even if they include grid points at which the pressure levels do not exist anywhere at or above the surface. These data points, therefore, must be neglected when analyzing atmospheric data. Figure B.2 shows the mean December surface pressures for the Northern Hemisphere with grid areas with surface pressures less than 950 mb in white. Data for grid points in white should be neglected for pressure levels greater than 950 mb. In addition, due to the small fluctuations of surface pressure around 1000 mb, all data at 1000 mb should be interpreted with caution.

Figure B.2: Mean December surface pressures for the Northern Hemisphere from 1949 to 2007. White areas indicate surface pressure levels below 950 mb.
Appendix C

Significant geopotential anomalies

The results of significance testing of monthly mean geopotential anomaly composites for years with anomalously high and low snow extent over Eurasia in October are presented on the following pages. Areas of significant anomalies are shown for the months of September through February. For each figure, red (blue) areas indicate significantly high (low) geopotential anomalies and light and dark shading represent 95% and 99% confidence levels respectively.
Figure C.1: Areas of significant anomalies for monthly mean geopotential composites of September preceding anomalously high (left column) and low (right column) Eurasian October snow extents at 1000 mb (top), 700 mb (middle), and 500 mb (bottom).
Figure C.2: Areas of significant anomalies for monthly mean geopotential composites of September preceding anomalously high (left column) and low (right column) Eurasian October snow extents at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Figure C.3: Areas of significant anomalies for monthly mean geopotential composites of October following anomalously high (left column) and low (right column) Eurasian October snow extents at 1000 mb (top), 700 mb (middle), and 500 mb (bottom).
Figure C.4: Areas of significant anomalies for monthly mean geopotential composites of October following anomalously high (left column) and low (right column) Eurasian October snow extents at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Figure C.5: Areas of significant anomalies for monthly mean geopotential composites of November following anomalously high (left column) and low (right column) Eurasian October snow extents at 1000 mb (top), 700 mb (middle), and 500 mb (bottom).
Figure C.6: Areas of significant anomalies for monthly mean geopotential composites of November following anomalously high (left column) and low (right column) Eurasian October snow extents at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Figure C.7: Areas of significant anomalies for monthly mean geopotential composites of December following anomalously high (left column) and low (right column) Eurasian October snow extents at 1000 mb (top), 700 mb (middle), and 500 mb (bottom).
Figure C.8: Areas of significant anomalies for monthly mean geopotential composites of December following anomalously high (left column) and low (right column) Eurasian October snow extents at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Figure C.9: Areas of significant anomalies for monthly mean geopotential composites of January following anomalously high (left column) and low (right column) Eurasian October snow extents at 1000 mb (top), 700 mb (middle), and 500 mb (bottom).
Figure C.10: Areas of significant anomalies for monthly mean geopotential composites of January following anomalously high (left column) and low (right column) Eurasian October snow extents at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Figure C.11: Areas of significant anomalies for monthly mean geopotential composites of February following anomalously high (left column) and low (right column) Eurasian October snow extents at 1000 mb (top), 700 mb (middle), and 500 mb (bottom).
Figure C.12: Areas of significant anomalies for monthly mean geopotential composites of February following anomalously high (left column) and low (right column) Eurasian October snow extents at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Wave activity flux was calculated using the formulation derived by Plumb (1985). The three components of WAF, denoted as $F_{s,x}$, $F_{s,y}$, and $F_{s,z}$ below, are in the eastward, poleward, and upward directions respectively. The diagnostic is as follows:

\[
F_{s,x} = \left( p \cdot \cos \phi \right) \times \left( v''^2 - \frac{1}{(2 \Omega a \sin \phi)} \frac{\partial (v' \Phi')}{\partial \lambda} \right) \tag{D.1}
\]

\[
F_{s,y} = \left( p \cdot \cos \phi \right) \times \left( -u'v' - \frac{1}{(2 \Omega a \sin \phi)} \frac{\partial (u' \Phi')}{\partial \lambda} \right) \tag{D.2}
\]

\[
F_{s,z} = \left( p \cdot \cos \phi \right) \times \left( \frac{2 \Omega \sin \phi}{S} \left( v''^2 - \frac{1}{(2 \Omega a \sin \phi)} \frac{\partial (T' \Phi')}{\partial \lambda} \right) \right) \tag{D.3}
\]

where,

- $p =$ air pressure in mb / 1000 mb [-]
- $\phi =$ latiditude [rad]
- $\lambda =$ longitude [rad]
- $\Omega =$ angular velocity of the Earth [rad s\(^{-1}\)]
- $a =$ radius of the Earth [m]
- $S =$ static stability [K m\(^{-1}\)]
- $u'$ = deviation of the local zonal wind from the zonal mean [m s\(^{-1}\)]
- $v'$ = deviation of the local meridional wind from the zonal mean [m s\(^{-1}\)]
- $\Phi'$ = deviation of the local geopotential from the zonal mean [m\(^2\) s\(^{-2}\)]
- $T'$ = deviation of the local air temperature from the zonal mean [K]

The static stability, $S$, is calculated using the following relations:

\[
S = \frac{P}{H} \frac{d \hat{T}}{dz} + \frac{R_g \hat{T}}{C_p H} \tag{D.4}
\]
\[ H = \frac{\dot{R} \hat{T}}{g} \]

where,

\( \hat{T} \) = areal mean temperature for area north of 20N latitude [K]

\( P \) = air pressure [mb]

\( z \) = elevation above mean sea-level [m]

\( H \) = constant scale height [m]

\( R_d \) = dry air gas constant, 270 J kg\(^{-1}\) K\(^{-1}\)

\( C_p \) = specific heat at constant pressure for dry air, 1004 J kg\(^{-1}\) K\(^{-1}\)

\( \dot{R} \) = average gas constant in the troposphere, 298.0 J kg\(^{-1}\) K\(^{-1}\)

\( \dot{T} \) = average temperature in the troposphere, 250.0 K

\( g \) = gravitational constant, 9.81 m s\(^{-2}\)
Appendix E

WAF anomaly profiles

Profiles of composite WAF anomalies across the zonal band of 60N latitude, from 30E to 150E longitude, for two week periods following anomalous snow extent over Eurasia in October, were computed for early and late November, December, January, and February. The results are presented in the figures over the next few pages. Vertical and horizontal components of all figures are scaled by 0.05 and 10 respectively.
Figure E.1: Vertical zonal WAF anomaly composite for early November following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.2: Vertical zonal WAF anomaly composite for late November following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.3: Vertical zonal WAF anomaly composite for early December following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.4: Vertical zonal WAF anomaly composite for late December following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.5: Vertical zonal WAF anomaly composite for early January following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.6: Vertical zonal WAF anomaly composite for late January following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.7: Vertical zonal WAF anomaly composite for early February following anomalously high (top) and low (bottom) October Eurasian snow extents.
Figure E.8: Vertical zonal WAF anomaly composite for late February following anomalously high (top) and low (bottom) October Eurasian snow extents.
Appendix F

Vertical WAF significant anomalies

This appendix presents the results of significance testing of vertical WAF anomaly composites for two week periods following anomalous snow extent over Eurasia in October. Composites showing areas of significant anomalies during early and late November, December, January and February are shown for varying pressure levels from 700 mb to 50 mb. In each figure, red (blue) areas indicate significantly high (low) vertical WAF anomalies and light and dark shading represent 95% and 99% confidence levels respectively.

Figure F.1: Areas of significant vertical WAF anomalies for high snow years (left) and low snow years (right) during early November at 700 mb.
Figure F.2: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during early November at 500 mb (top), 250 mb (middle), and 150 mb (bottom).
Figure F.3: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during early November at 50 mb (top), and late November at 700 mb (middle) and 500 mb (bottom).
Figure F.4: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late November at 250 mb (top), 150 mb (middle) and 50 mb (bottom).
Figure F.5: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during early December at 700 mb (top), 500 mb (middle), and 250 mb (bottom).
Figure F.6: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during early December at 150 mb (top) and 50 mb (middle), and late December at 700 mb (bottom).
Figure F.7: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late December at 500 mb (top), 250 mb (middle), and 150 mb (bottom).
Figure F.8: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late December at 50 mb (top), and early January for 700 mb (middle) and 500 mb (bottom).
Figure F.9: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during early January at 250 mb (top), 150 mb (middle), and 50 mb (bottom).
Figure F.10: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late January at 7000 mb (top), 500 mb (middle), and 250 mb (bottom).
Figure F.11: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late January at 150 mb (top) and 50 mb (middle), and early February for 700 mb (bottom).
Figure F.12: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during early February at 500 mb (top), 250 mb (middle) and 150 mb (bottom).
Figure F.13: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late February at 700 mb (top), 500 mb (middle) and 250 mb (bottom).
Figure F.14: Areas of significant vertical WAF anomalies for high snow years (left column) and low snow years (right column) during late February at 150 mb.
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