

AN EXPERIMENT IN LARGE-SCALE AIR-SEA INTERACTION

by

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Submitted to the Department of Meteorology  
on October 2, 1979 in partial fulfillment of the requirements  
for the Degree of Master of Science

## ABSTRACT

Parsons' (1969) two-layer, wind-driven, steady-state, mid-latitude,  $\beta$ -plane ocean model is used as the principal component in a study of oceanic heat transport. Parsons' solution for the flow in the upper layer is combined with a solution for the flow in the directly-driven lower layer to give the surface layer flow everywhere in the basin. Fixed distributions of atmospheric wind stress and surface level atmospheric temperature are applied at the top boundary of the ocean. Heat is presumed to flow across the air-sea interface as a linear function of the difference between the anemometer level atmospheric temperature and the sea surface temperature. This heat is assumed well mixed in a surface oceanic mixed layer whose distribution is specified and held fixed and whose mean depth is taken to be 100 m.

Given a value of the magnitude of the fixed distribution of wind stress, and steady-state ocean circulation is calculated. The oceanic mixed layer thermodynamic equation ,

is then integrated to equilibrium as an initial value problem. A Lagrangian method in which parcels are followed around streamlines with the flow with heat being added according to the air-sea temperature difference is employed. The equilibrium distribution of vertical heat flux at the air-sea interface is derived from the atmospheric and equilibrium oceanic temperature distributions and the vertical heat flux law. The northward flux of heat across latitude walls in the basin is calculated.

The sensitivities of the oceanic temperatures and fluxes to the wind stress driving, constant of proportionality in the linear heat flux law, and north south temperature difference of the zonally symmetric atmospheric temperatures are determined. Comparisons are made of model results with observations.

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## I. Introduction

Recent findings have stimulated work on the oceans' role in climate dynamics. Results of data analyses (Vonder Haar and Oort, 1973; Oort and Vonder Haar, 1976) and calculations with complex global numerical models (Manabe et al., 1975; Bryan et al., 1975) suggest that the poleward oceanic heat transports are an important component of the global energy budget.

A major portion of the northward transport of heat by the ocean is the heat transported by the wind-driven circulation in the upper ocean. Large-scale horizontal ocean circulations forced by atmospheric winds transport water laterally in rotational circulations. As the water circulates its characteristics are modified through interactions with the surface layers of the atmosphere.

In the northward branch of the oceanic flow pattern tropical water is exposed to decreasing atmospheric temperatures above. This situation leads to cooling of the ocean surface and warming of the lower atmosphere by an upward turbulent flux of heat from the ocean. In the southward branch of the gyre cold northern water is modified through exposure to the progressively warmer air above, with cooling occurring in the atmosphere and warming taking place at the surface of the ocean.

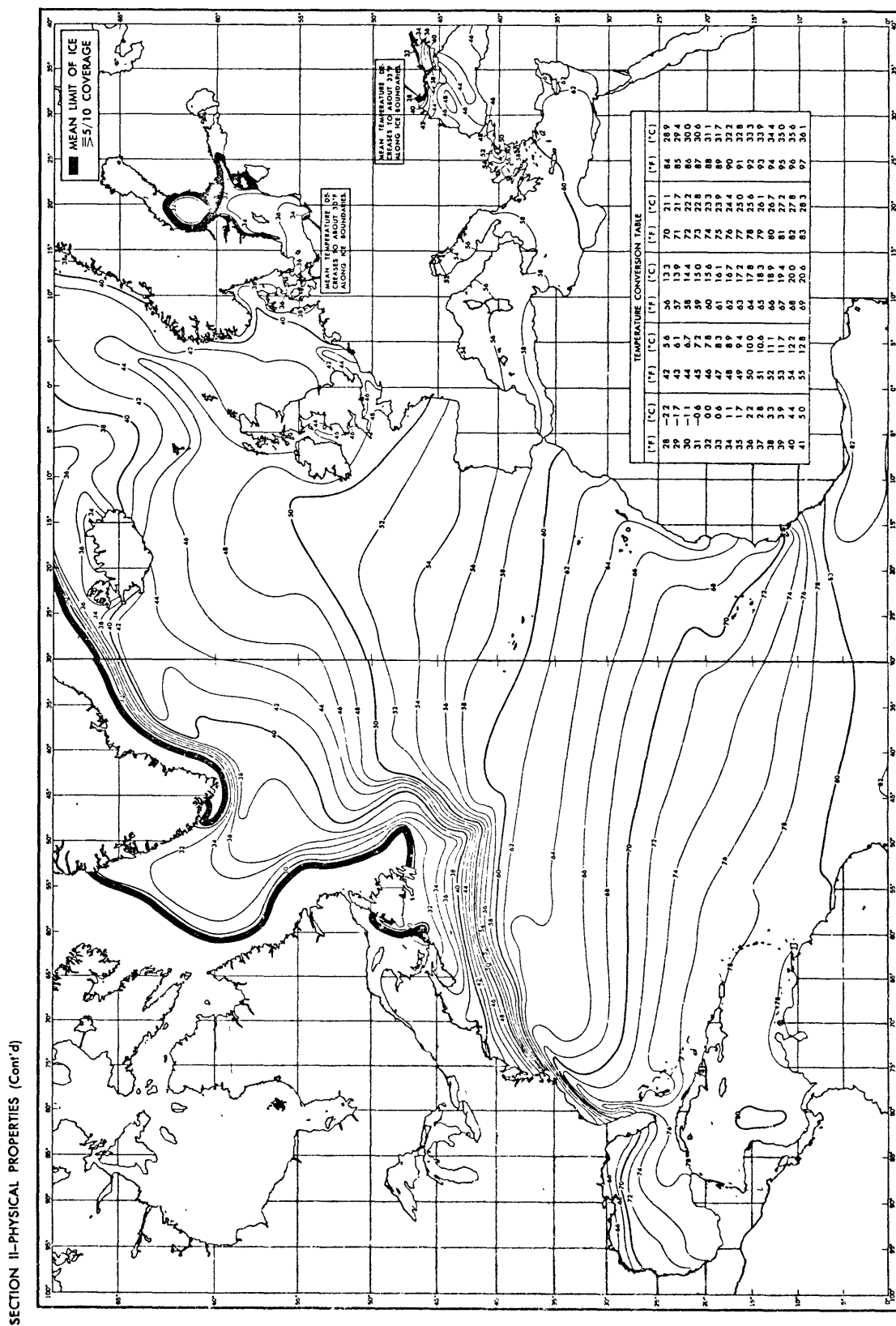
About the upper 100-200 m of the ocean undergo a seasonal



temperature cycle. This is about an order of magnitude more mass than in the entire atmosphere. Due to the substantially greater specific heat of water as compared to air as well as the differences in mass involved, the atmosphere responds much more quickly than the ocean to the annual cycle in solar forcing. As will be seen below, however, the response of the ocean surface temperature to the seasonal forcing cycle is noteworthy.

We present in Figs. 10a and 10b observed March and August mean sea surface temperatures from the U.S. Naval Oceanographic Atlas of the North Atlantic Ocean. The most outstanding feature of the March distribution is the intense front which exists off the North American coast from Cape Hatteras to Nova Scotia. Seaward of this front is a region in which the isotherms are strongly bowed to the north. In the interior of the ocean the temperature pattern is predominantly zonal with gradients much weaker than near the coastlines. Near the African coast there is a sharp intrusion of cold water to the south.

The August distribution of sea surface temperatures is similar in many respects to the March distribution, but there is a notable discrepancy. With the exception of the area westward of the British Isles, there is a general decrease in the meridional temperature gradient from the winter case. This effect is most pronounced in the southern half of the North Atlantic and near western boundaries.



**Fig. 10a.** Mean March Sea-Surface Temperature in °F  
(from U.S. Naval Oceanographic Atlas of the  
North Atlantic Ocean)

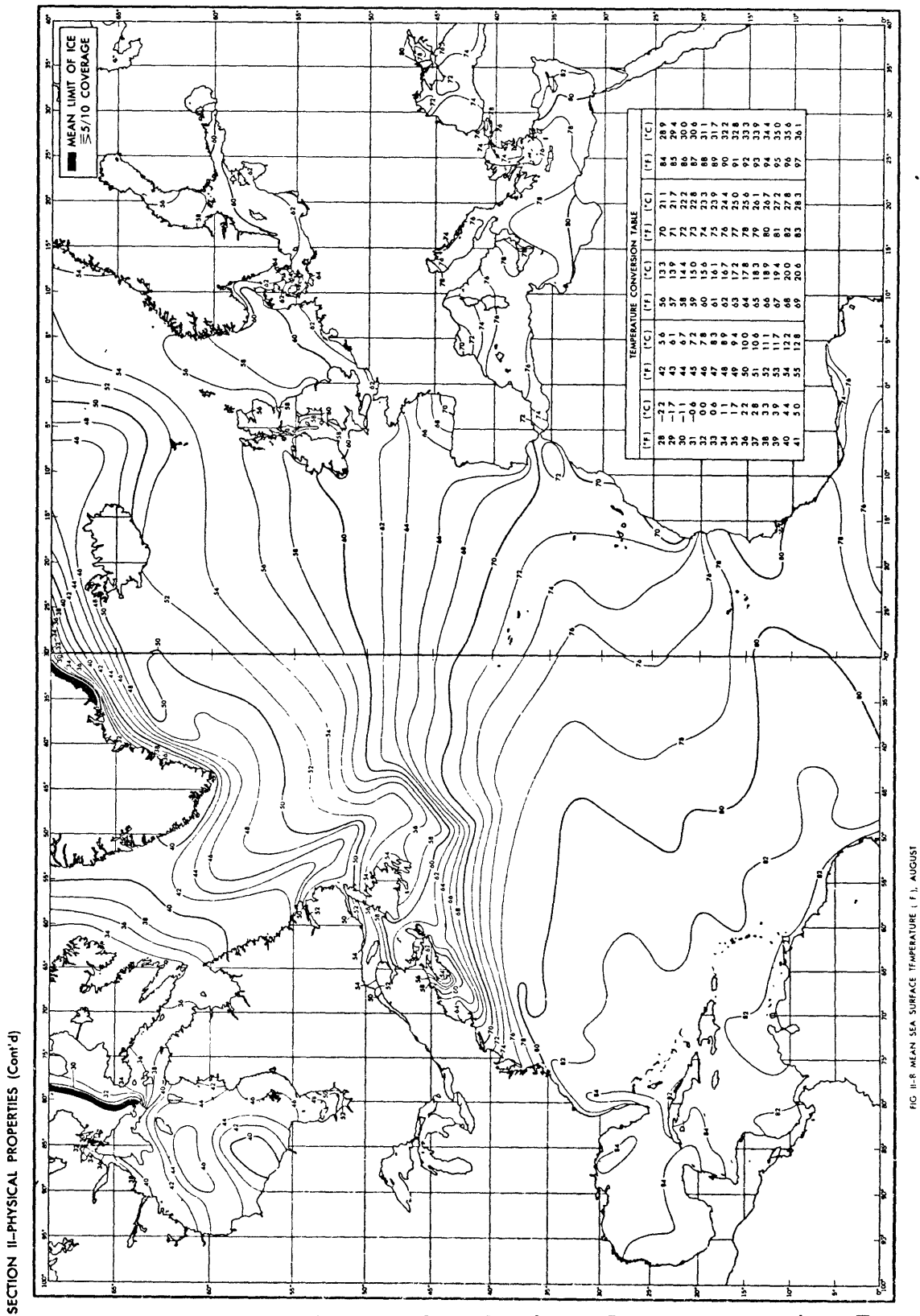


Fig. 10b. Mean August Sea-Surface Temperature in °F (from U.S. Naval Oceanographic Atlas of the North Atlantic Ocean)

FIG. 10-B. MEAN SEA SURFACE TEMPERATURE (F.), AUGUST

On the extreme western side of the ocean the August pattern is quite similar in shape, not strength, to that existing in March. We see a front that is still fairly strong bordered on its southeastern side by a tongue of warm water protruding past Cape Hatteras. On the extreme eastern side of the ocean there is again a southward intrusion of cold water, although not as sharp.

The most dramatic disparity between the two maps occurs in the interior in the southeastern region. A zonal temperature gradient is present in the August distribution which replaces the essentially meridional March gradient. This dramatic seasonal shift in the mid-Atlantic sea surface temperature distribution has not been satisfactorily explained.

Bunker and Worthington (1976) have used bulk aerodynamic exchange equations to compute the vertical flux of energy through the surface of the North Atlantic Ocean for a 32 year period. Their study is the most detailed of its kind as they had access to a much more complete set of surface marine observation than was previously available. The dependence of the exchange coefficients on wind speed and air stability were included in the calculations. Fluxes were calculated from individual observations of wind and temperature and then averaged.

Fig. 12b shows the resulting distribution of the net heat gain of the North Atlantic Ocean expressed in units of

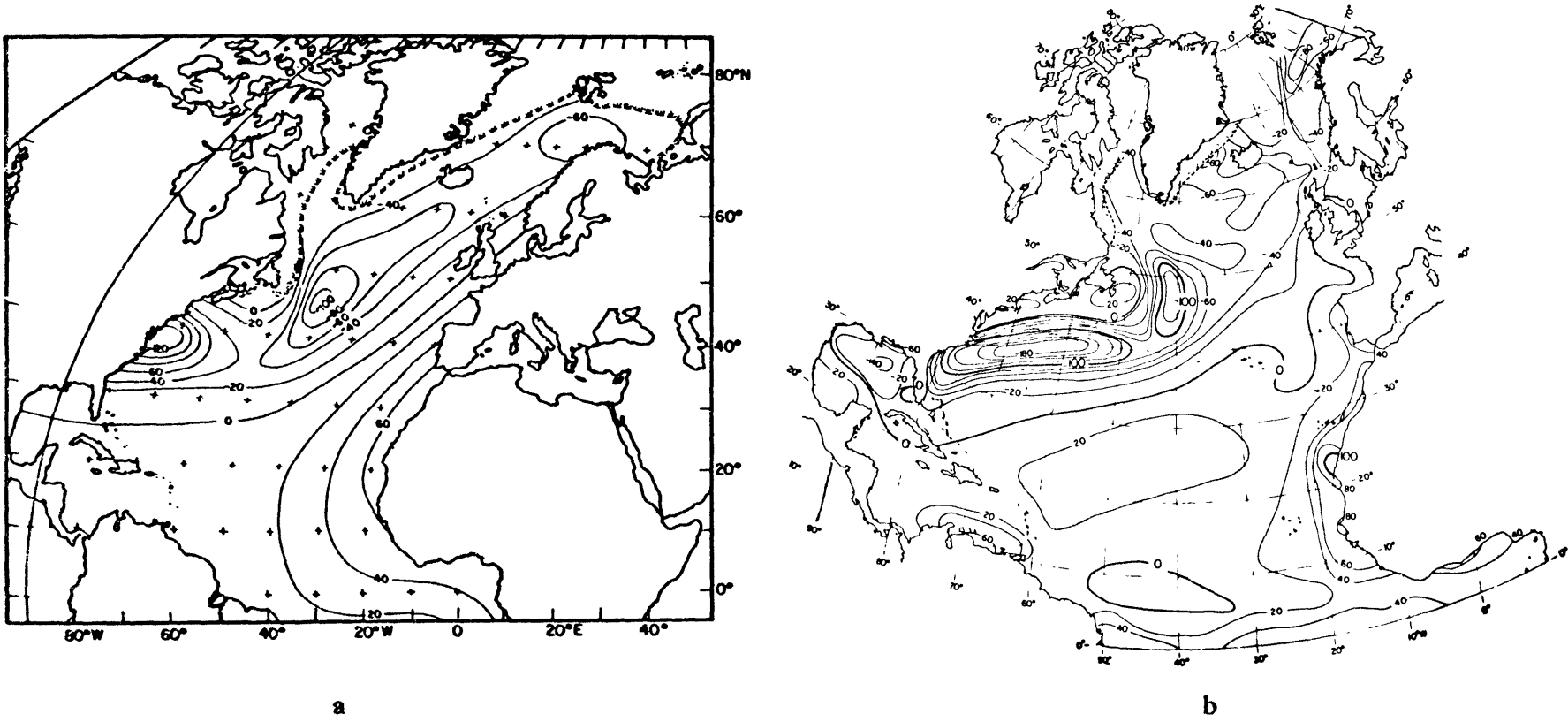


Fig. 12. Vertical Heat Flux for North Atlantic;  
 a. from Budyko (1963)    b. from Bunker & Worthington  
 (1976)

kcal cm<sup>-2</sup>yr<sup>-1</sup>. It is seen that the largest negative value is in the region of the Gulf Stream where there are strong losses of heat in winter. The cold returning current in the interior of the ocean experiences a relatively mild warming. Fig. 12a shows results of a similar calculation by Budyko (1963).

The results presented in Figs. 10 and 12 are strongly coupled. Immediately northward of the axis of greatest heat loss to the atmosphere is the intense front in the sea surface temperature field. In the region of mild vertical heat flow in the interior of the ocean the temperature field is much flatter. Regions of high positive values of the heat flux near the west coast of Africa are also regions of strong oceanic temperature gradients.

In the interest of gaining a better understanding of the mechanisms by which our present climate is shaped and with the long-term goal being climate prediction, more must be known of global air-sea interaction. We will look for the equilibrium response of an ocean model to a number of fixed external conditions.

## II. The Model

This paper reports a study of limited air sea interaction with a simple model. Attention is directed to the thermal response of an idealized ocean model to a given atmospheric state. The ocean is allowed to transport heat in the wind-driven surface layers. Transport processes across the ocean-atmosphere interface are crudely parameterized. Changes in the oceanic state are not allowed to feed back on the atmosphere.

The ocean model is based on Parsons' (1969) study of Gulf Stream separation. There he considered a two-layer, wind-driven, steady-state, mid-latitude  $\beta$ -plane ocean within a square basin. The geometry of the model is presented in Fig. 1. We will consider the southern and northern walls to correspond roughly to  $10^\circ\text{N}$  and  $50^\circ\text{N}$ . The two immiscible layers of fluid are homogeneous and incompressible; the lower layer is of slightly greater density than the upper layer ( $\rho_{LL} \gtrsim \rho_{UL}$ ) and has five times as much mass. Pressure is assumed hydrostatic and the lower layer fluid is assumed inert except when directly driven by the wind in the situation where upon layer fluid does not completely cover the basin. The horizontal components of the velocity are assumed uniform within the layers. Friction is modeled as an interfacial drag proportional to the upper layer velocity and as bottom friction in the case of the directly-driven lower layer.

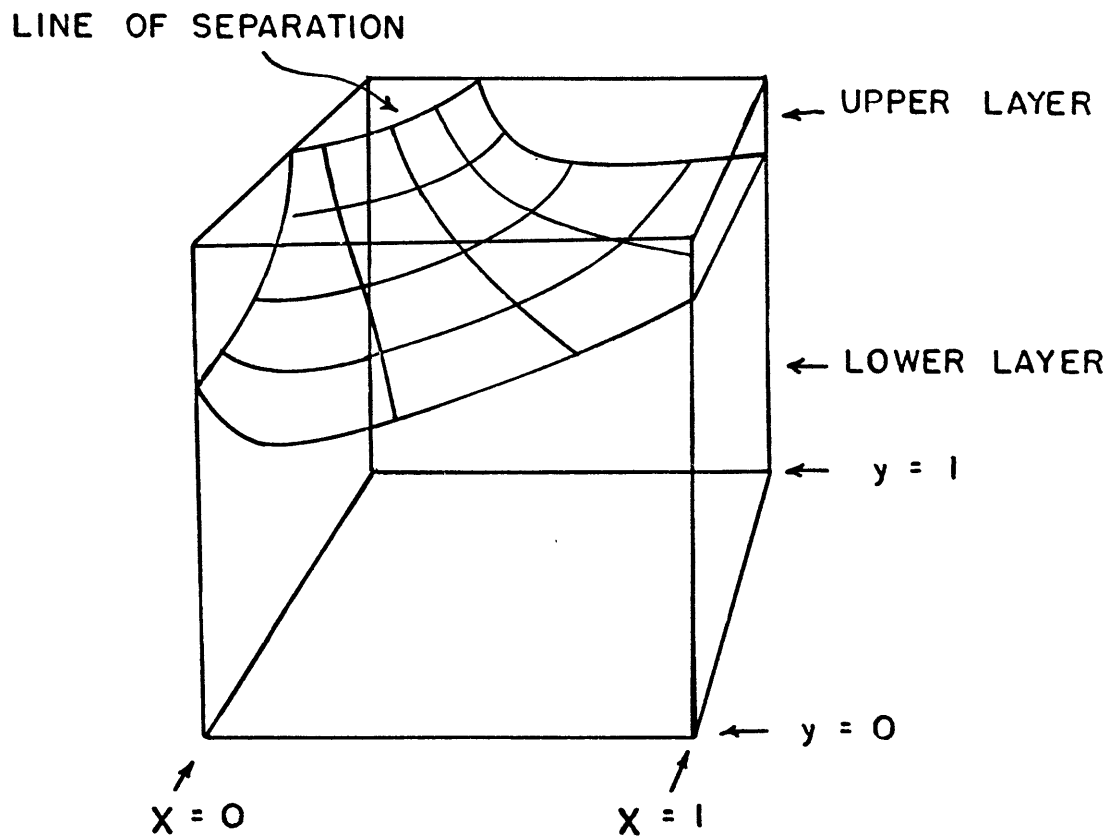


Fig. 1. Schematic of Model



For the upper layer, the vertically integrated equations of motion and mass continuity are:

$$D(\underline{u} \cdot \nabla) \underline{u} + f \hat{k} \times D \underline{u} = -g' D \nabla D + \underline{\tau} / \rho_0 - K \underline{u} \quad (1)$$

$$\nabla \cdot (D \underline{u}) = 0 \quad (2)$$

$D$  is the upper layer depth,  $\underline{u} = (u, v)$  is the horizontal velocity vector with Cartesian components in the eastward and northward directions, respectively.  $f$  is the Coriolis parameter, taken as a linear function of latitude in the  $\beta$ -plane approximation,  $g' = g(1 - \rho_{ul}/\rho_{LL})$  is reduced gravity,  $g$  is actual gravity,  $K$  is a drag coefficient.  $\underline{\tau}$  is the wind stress which we will assume to be in the zonal direction, i.e.,  $\underline{\tau} = (\tau_x, 0)$ . We will further fix the stress distribution to be  $\tau_x = -W \cos(y/L)$  with  $W$  variable. The equations for the directly-driven lower layer are analogous with the variables taking on their lower layer values and reduced gravity being replaced by actual gravity.

The equations are non-dimensionalized with scales characteristic of variations over the length of the basin. We will assume that the Rossby number is small and will therefore discard the inertial terms. The result is the following set of equations expressed in terms of an upper layer transport streamfunction:

$$-f \frac{\partial \psi}{\partial x} = -D \frac{\partial D}{\partial x} + \frac{\epsilon}{D} \frac{\partial \psi}{\partial y} + \lambda \tau_x \quad (3)$$

$$-f \frac{\partial \psi}{\partial y} = -D \frac{\partial D}{\partial y} - \frac{\epsilon}{D} \frac{\partial \psi}{\partial x} \quad (4)$$

$$\psi \text{ is defined by } D \underline{u} = -\hat{k} \times \nabla \psi \quad (5)$$

$\epsilon = \kappa / \beta L d$  is a non-dimensional friction parameter and  $\lambda = L w / g' \rho d^2$  is a non-dimensional wind stress parameter.  $d$  is the mean upper layer depth and  $L$  is the length of the basin.

The system is solved using boundary layer techniques. The frictional terms are assumed small outside of narrow boundary layer regions. The total amount of water in each layer is constant. As a result, if the curl of the wind stress is large enough, the deepening of the thermocline in the center of the basin may force the withdrawal of upper layer water from the shallowest region - the north-west corner of the basin. Vorticity balance in the boundary layer between the advection of planetary vorticity and the frictional input of vorticity can only be achieved if the boundary layer is on the western side of the ocean. Our scaling has presupposed the boundary layer to be frictionally controlled.

The equations for the boundary layer are found by scaling east-west variations by the boundary layer thickness  $\epsilon$ . The frictional and wind stress terms in the first equation are found to be relatively small in this region.

Thus, geostrophic balance holds for the flow parallel to the boundary. All three terms are of comparable magnitude in the second equation.

The boundary conditions are no normal flow through solid walls. The interior solution is a broad anticyclonic gyre with eastward flow in the upper half, westward flow in the lower half and a southward component to the flow everywhere. By continuity, all of the flow in the interior has to be returned to the north in the western boundary layer.

The phenomenon of separation in the model can be interpreted as a breakdown of the circulation which occurs when the wind stress is turned on strong enough that the Sverdrup transport in the interior becomes too large to be returned by the western boundary layer, which scaling shows to be geostrophic. For geostrophic balance to continue to hold, the upper layer depth at the western coast must become negative. To avoid this we require that the boundary layer separate from the coast at the latitude where the depth goes to zero. This effectively limits the area of the interior which is acted on by the wind stress and reduces the southward interior flow to the point at which it can just be accomplished geostrophically by the separated current.

The mathematical analysis of the model results in three asymptotically valid solutions. The regions of their validity are the western boundary layer, the separated boundary layer and the region to the south and east of these.

A uniformly valid approximation to the solution may be obtained by combining the asymptotically valid solutions with formulas of the form

$$X_{\text{unif}} = X_{\text{bl}} + X_{\text{int}} - X_{\text{match}} \quad (6)$$

where  $X_{\text{match}}$  represents the limit of either the interior or the boundary layer solution as it leaves its region of validity.

Conservation of mass in the upper layer gives a condition which allows determination of the upper layer depth at the eastern wall.

$$1 = \iint D(x, y, h, \lambda) dx dy \quad (7)$$

Extending Parson's work, we will derive a separate solution for the flow in the directly-driven lower layer in the northwest corner of the basin. The streamfunction is assumed zero on the lower layer side of the line of separation - no momentum transfer is allowed to the inert lower layer covered by the upper layer. This assumption is motivated by a study by Kamenkovich and Reznik (1972) in which the streamfunction was allowed to vary at the surfaced interface in a similar two-layer model. They found that the lower layer flow diminished very rapidly with distance from the line of separation in the region where

the upper layer exists. Veronis (1973) has used a similar assumption in his study of the world ocean circulation.

A western boundary layer is required to return the Sverdrup flow in the directly-driven lower layer. The velocities here are much smaller than in the upper layer due to the greater depth of fluid, larger effective gravity and the small wind stress curl near the northern boundary. These factors also preclude separation of the lower layer western boundary layer from the coast for reasonable stress magnitudes. The solutions in each of the five regions are given in the Appendix.

It should be stated that use was made of Parsons' circulation model not because it incorporates state-of-the-art understanding of ocean dynamics. It does not. Parsons' choice for the force balance in the boundary layers in which the frictional terms dominate the inertial terms is not realistic for large-scale oceanic flows. In the real ocean the inertial forces seem to be dominant. There is also an inconsistency in the model in which the submerged lower layer receives no momentum transfer from the layer above, despite the interfacial friction which is assumed to act on the upper layer. A similar inconsistency exists in the manner in which we model the flow in the directly-driven lower layer by not allowing lateral transfers of momentum across the line of separation. The effect of the energetic

mesoscale eddy field on the large-scale dynamics has also not been included.

While acknowledging these limitations, it is felt that the ocean model is sufficiently realistic to give an adequate representation of the flow in the real ocean. It captures the concentrated northward currents near the western boundaries and the contrasting slow southward interior flows. These features are essential to the ocean's heat transporting capability. Use of a more sophisticated model of ocean dynamics would affect details of the equilibrium ocean temperature patterns but not the qualitative nature of the processes which force these patterns.

Attention is confined to the effects of the wind-driven surface circulation in the horizontal transport of heat. Other mechanisms of heat transport will be neglected. It will be necessary to model the vertical transport of heat across the air-sea interface. A mechanism must also be postulated to distribute the heat within the ocean.

Allowance for the transfer of heat between the atmosphere and the ocean will be made by postulating a linear heat transfer law. The heat transport into the ocean will be assumed proportional to the difference between the fixed surface level atmospheric temperature and the ocean temperature.

This parameterization is motivated by a study by Haney (1971) in which he proposed a similar form for an ocean model surface thermal boundary condition. Haney

conducted a heat budget analysis of the ocean surface appropriate to zonally and time averaged atmospheric conditions. His parameterization takes into account solar radiation, net longwave radiation and sensible and latent heat fluxes. It can be expressed as a linear law if the atmospheric temperature is replaced by a slightly higher effective atmospheric temperature to include the effects of solar radiation and atmospheric moisture on the flux.

Through an analysis of observations he arrives at a value of the coupling coefficient which slowly varies with latitude and for the region we are considering ( $10^{\circ}\text{N} - 50^{\circ}\text{N}$ ) has a mean value of about  $30,000 \text{ cal cm}^{-2}\text{yr}^{-1}\text{.}^{\circ}\text{C}^{-1}$ . In a later paper (Haney, 1975) he presents results of calculations of the coupling coefficient presumably using different data and arrives at a value of about  $18,000 \text{ cal cm}^{-2}\text{yr}^{-1}\text{.}^{\circ}\text{C}^{-1}$ . Takano (1975) employs a similar parameterization and uses a value of approximately  $6000 \text{ cal cm}^{-2}\text{yr}^{-1}\text{.}^{\circ}\text{C}^{-1}$ . Evidently, an appropriate value of the constant is difficult to determine. The law gives the proper direction of heat flow and gives results which are easy to interpret.

Vertical heat transport within the ocean is modeled by assuming this surface level of the ocean to be well mixed. We will impose the condition that this surface mixed layer be non-divergent so that there will be no advection of heat out of the layer. This condition is satisfied by choosing the mixed layer depth to be proportional to the thermocline

depth, or the lower layer depth where the upper layer is absent. In the upper layer region just south of the line of separation the mixed layer is quite shallow. This tends to increase the ratio of vertical heat transfers to advection and thus compensates to a degree for the increase in advection in the region due to the high velocities near the line of separation. Additionally, the base of the mixed layer will not be allowed to conduct heat. The mean depth of the mixed layer is taken to be 100 m.

The thermodynamic equation for the model ocean vertically integrated over the depth of the mixed layer is:

$$\rho C_p h \frac{dT_0}{dt} = C_{HF} (T_A - T_0) \quad (8)$$

where  $C_p$  is the heat capacity of water,  $h$  is the mixed layer depth,  $C_{HF}$  is a constant of proportionality,  $T_A$  is the atmospheric temperature and  $T_0$  is the oceanic temperature.



### III. Numerical Solution

Numerical solutions to the model equations are obtained in the following manner. Solutions will be found on a square grid with variable resolution. Given values of the wind stress parameter  $\lambda$ , the fixed distribution of wind stress and the depth of the upper layer at the eastern wall  $h$ , the position of the line of separation between upper and lower layer water is evaluated from Eq. C1 (in Appendix). The gridpoints which are adjacent to the line of separation are identified.

The values of the interior solution for the depth are evaluated at all gridpoints in the upper layer from Eq. A2. The interior solution for the streamfunction is evaluated at all points not on the walls from Eq. A1. Similarly, the western boundary layer solutions (Eqs. B1 and B2) are calculated at the upper layer gridpoints.

Because the separated boundary solution is expressed in terms of natural coordinates, its evaluation is not as straightforward. For each gridpoint it is necessary to find the point on the line of separation from which the normal to the line of separation includes the gridpoint. The interior value of layer depth at that point on the separation curve is then calculated from Eq. C2, as is the normal distance from the gridpoint to the separation curve. At this point the values of the separated solutions for the

streamfunction and depth may be directly evaluated from Eqs. C3 and C4.

The three solutions are then combined to give uniformly valid approximations with the formula:

$$\chi_{\text{unif}} = \chi_{\text{int}} + \chi_{\text{SBL}} - \chi_{\text{SBL}\infty} + \chi_{\text{WBL}} - \chi_{\text{WBL}\infty} \quad (9)$$

where  $\chi_{\text{SBL}\infty}$  and  $\chi_{\text{WBL}\infty}$  represent the values of the boundary layer solutions at an infinite distance from the boundary on the normal containing a given gridpoint.

Once the solutions in the different regions have been ascertained and combined to give the uniformly valid approximation at the gridpoints, the total depth of upper layer fluid must be calculated to see if it equals one in non-dimensional units. In general it will not and the depth at the eastern wall is adjusted, the circulation is reevaluated and the total amount of upper layer fluid is rechecked until self-consistency is found.

A similar procedure is carried out to find the uniformly valid solutions for the lower layer, except that there is no boundary layer at the line of separation so only interior (Eqs. D1 and D2) and western boundary solutions (Eqs. E1 and E2) must be considered. These are combined with formulas of the form of Eq. 6. The depth of the lower layer at the line of separation in the interior solution is taken to be equal to the sum of the mean depths of the upper and lower layers.

Solutions for the lower layer equations are found with the equations nondimensionalized using scales appropriate to the lower layer. The resulting streamfunction and depth fields were converted to the upper layer scalings for further unified treatment.

It is then possible to find the velocity field with a centered finite difference form of Eq. 5. As illustrated in Fig. 2, points which are less than a grid interval away from the line of separation in either the x- or y-directions or both must be treated separately with an interpolation method. For such points the x-distance (for north-south velocities) or y-distance (for east-west velocities) from the gridpoint to the line of separation is calculated and an interpolation is done to find the streamfunction an equal distance to the other side of the gridpoint. The calculated distance and streamfunction are then used in a finite difference velocity calculation centered at the gridpoint.

The narrowness and intensity of the boundary currents dictate a high degree of resolution on the western side of the ocean. For simplicity a uniform grid was used. Below we will describe the integration of the thermodynamic equation which will involve finding the time for a parcel to cycle around the basin on a given streamline. We determine the degree of resolution required in the model by examining the streamline traversal times as a function of

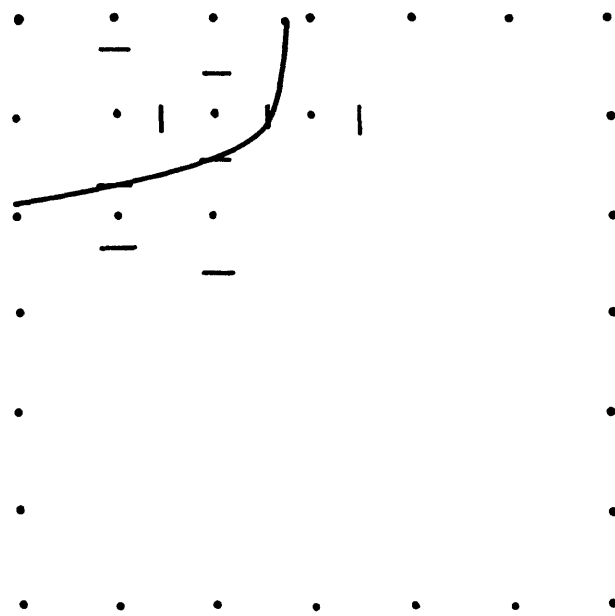


Fig. 2. Interpolation for velocities near line of Separation

resolution. These are presented in Table 1.

As the resolution increases, the traversal times for the individual streamlines decrease until the boundary currents are adequately detected. Little noticeable improvement occurs with resolutions greater than about 50 points in each direction (grid spacing of 120 km). For the sake of economy the model was tested with the resolution equal to 10. The cases presented in this paper were run with a resolution of 50.

We have adopted values of the circulation parameters presented by Parsons in his study. They are: mean upper layer depth  $d$  of 300 m, length of basin  $L$  of 6000 km,  $\epsilon = 0.03$ ,  $g = 1000 \text{ cm s}^{-2}$ ,  $g' = 2 \text{ cm s}^{-2}$ . We will consider a broad range of wind stress parameters ( $0.40 \leq \lambda \leq 0.80$ ), a subset of those  $\lambda$ 's considered by Parsons. In addition  $\lambda_{LL} = \lambda_{UL} / 12500$  and  $\epsilon_{LL} = \epsilon_{UL} / 5$ .

Fig. 3 gives the distribution of upper and lower layer water at the surface for different values of the wind stress parameter. As  $\lambda$  increases the thermocline depth increases, the increased upper layer depth compensates for the loss of upper layer area and mass conservation requires little change in depth at the eastern wall.

The steady-state wind-driven ocean circulation is shown in Figs. 4-6, a-c. Fig. 4 gives the mass transport streamfunction. Fig. 5 gives the depth of the upper layer

TABLE 1

Traversal times in years for parcels on streamlines  
used in temperature integration ( $\lambda = 0.45$ )

Resolution	10	20	30	40	50	60	70	80	90	100
Non-dimensional Streamline Value										
Upper Layer										
0.1	54.2	36.8	30.2	28.0	26.1	25.4	24.7	24.5	24.1	23.9
0.2	33.8	26.8	22.9	21.1	21.2	20.7	20.5	20.3	20.1	20.2
0.3	25.6	21.7	19.6	18.4	18.6	18.4	18.1	18.1	18.1	18.1
0.4	23.8	18.5	16.6	16.7	16.6	16.5	16.4	16.5	16.5	16.5
0.5	20.3	16.1	15.7	15.0	15.1	15.2	15.0	15.1	15.2	15.1
0.6	17.2	14.4	13.9	13.7	13.6	13.7	13.8	13.8	13.8	13.8
0.7	14.7	12.6	12.0	12.4	12.3	12.2	12.5	12.6	12.5	12.7
0.8	11.7	11.1	11.1	11.2	11.3	11.0	11.1	11.2	11.5	11.5
0.9	10.4	8.7	9.3	9.2	9.9	9.8	10.1	10.0	10.2	10.1
1.0	7.6	8.1	8.3	8.6	8.4	8.6	8.7	8.7	9.0	8.9
Lower Layer										
0.04	210.	152.	127.	116.	111.	108.	102.	122.	102.	112.
0.08	115.	84.6	82.2	75.0	72.9	68.8	69.8	78.6	68.1	81.2
0.12	71.7	62.6	58.7	54.2	55.6	52.7	54.6	56.7	51.3	63.2

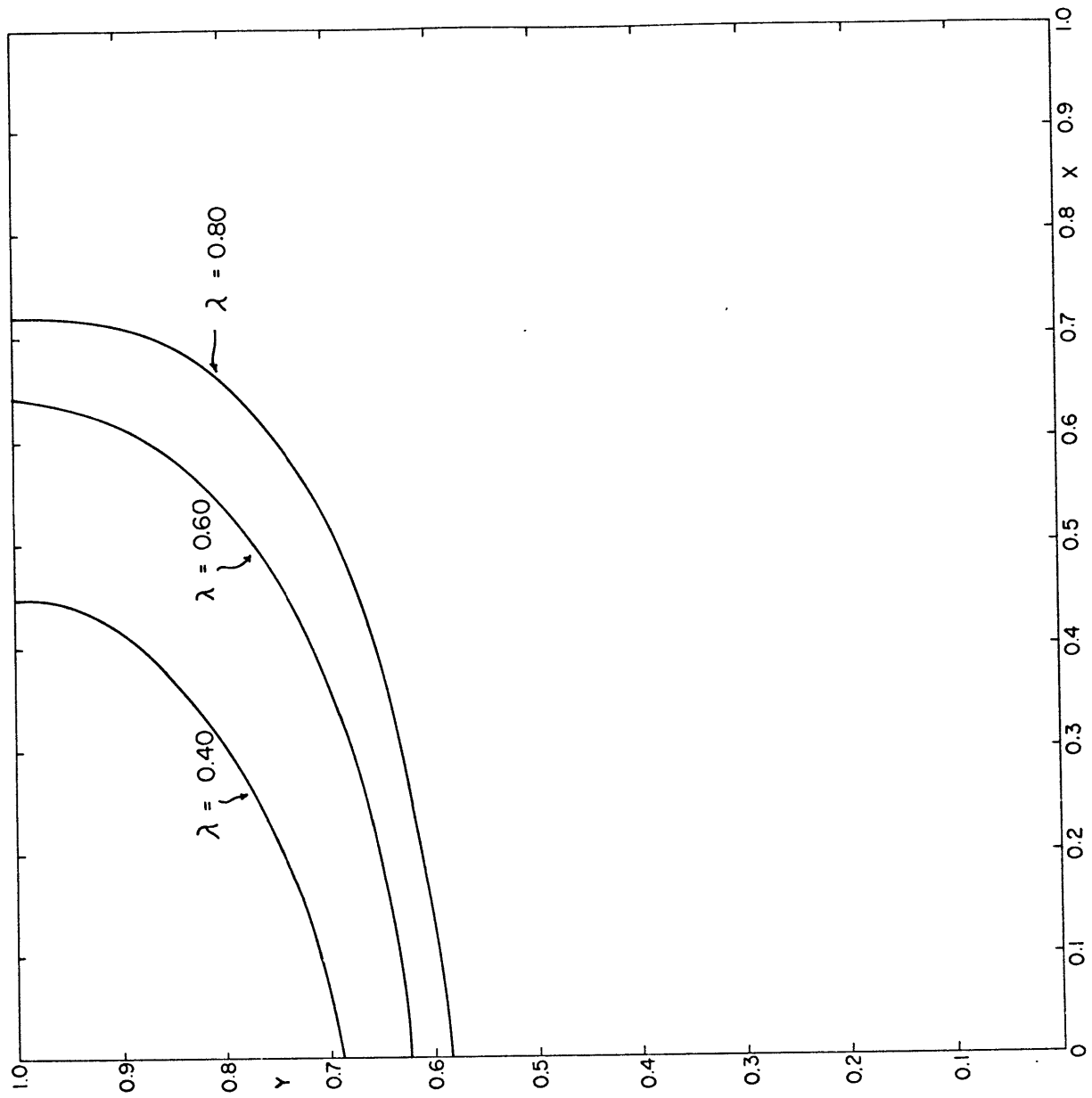


Fig. 3. Line of separation vs.  $\lambda$

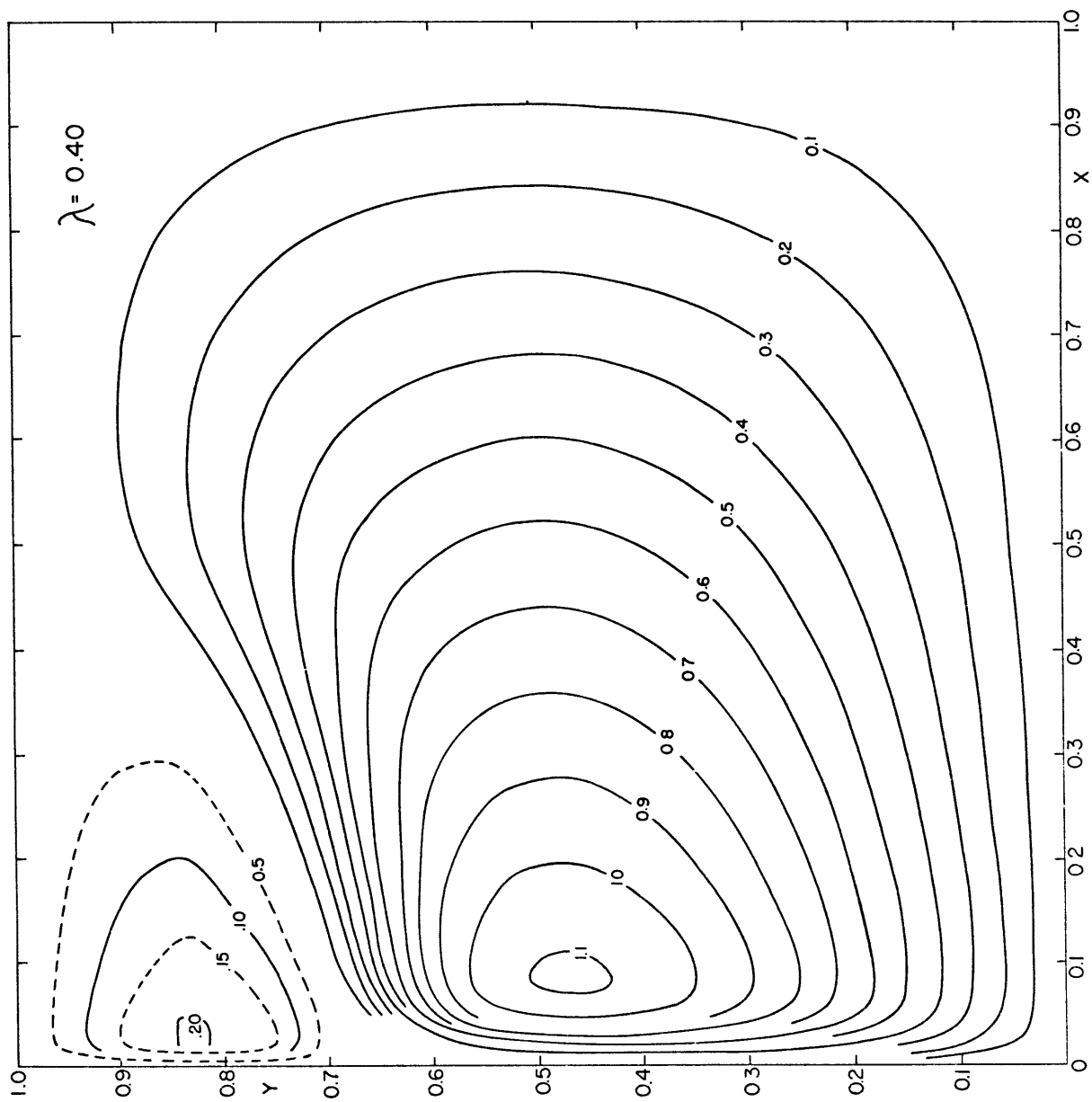


Fig. 4a. Non-dimensional Streamfunction ( $\lambda = 0.40$ )



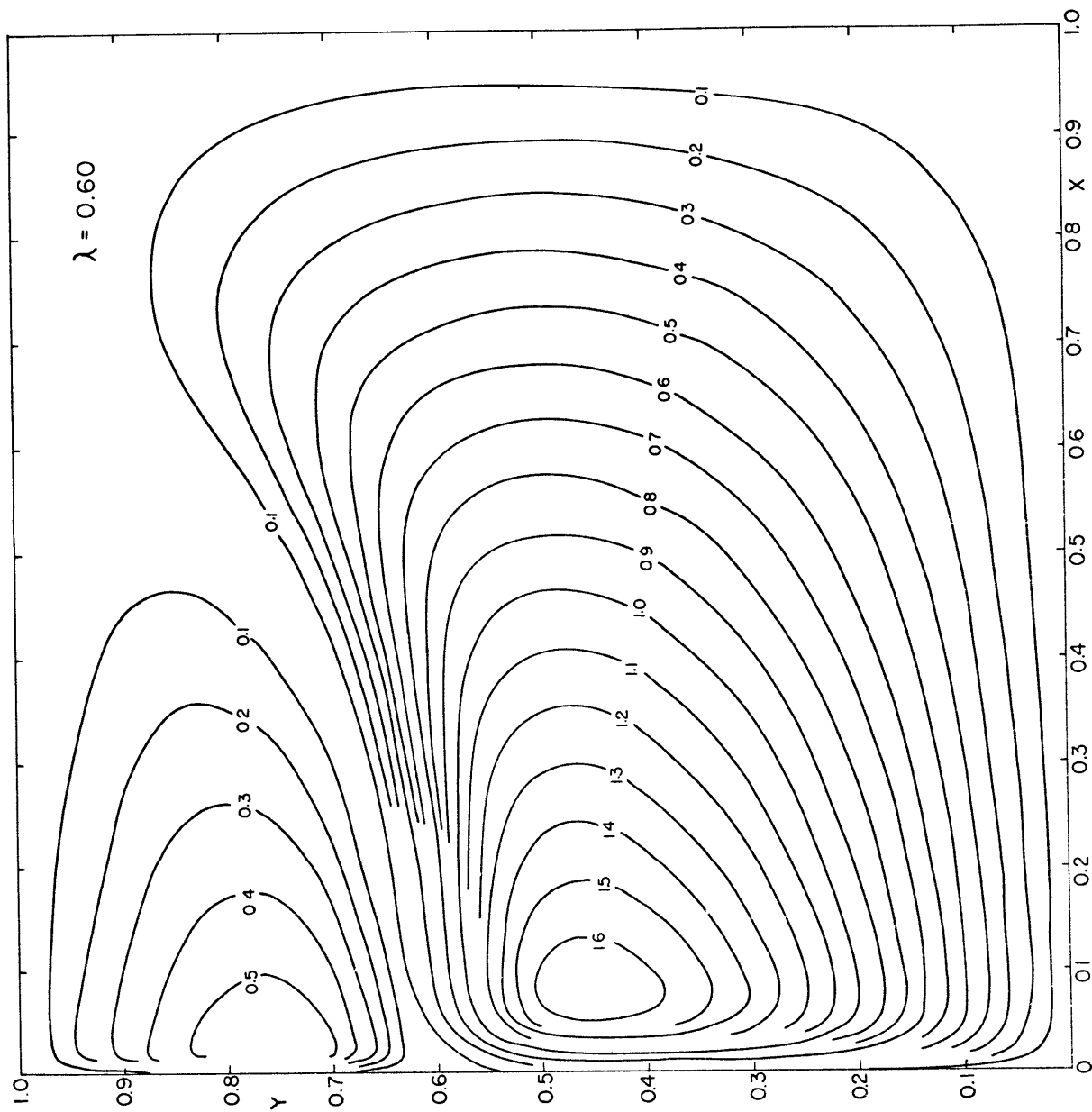


Fig. 4b. Non-dimensional Streamfunction ( $\lambda = 0.60$ )

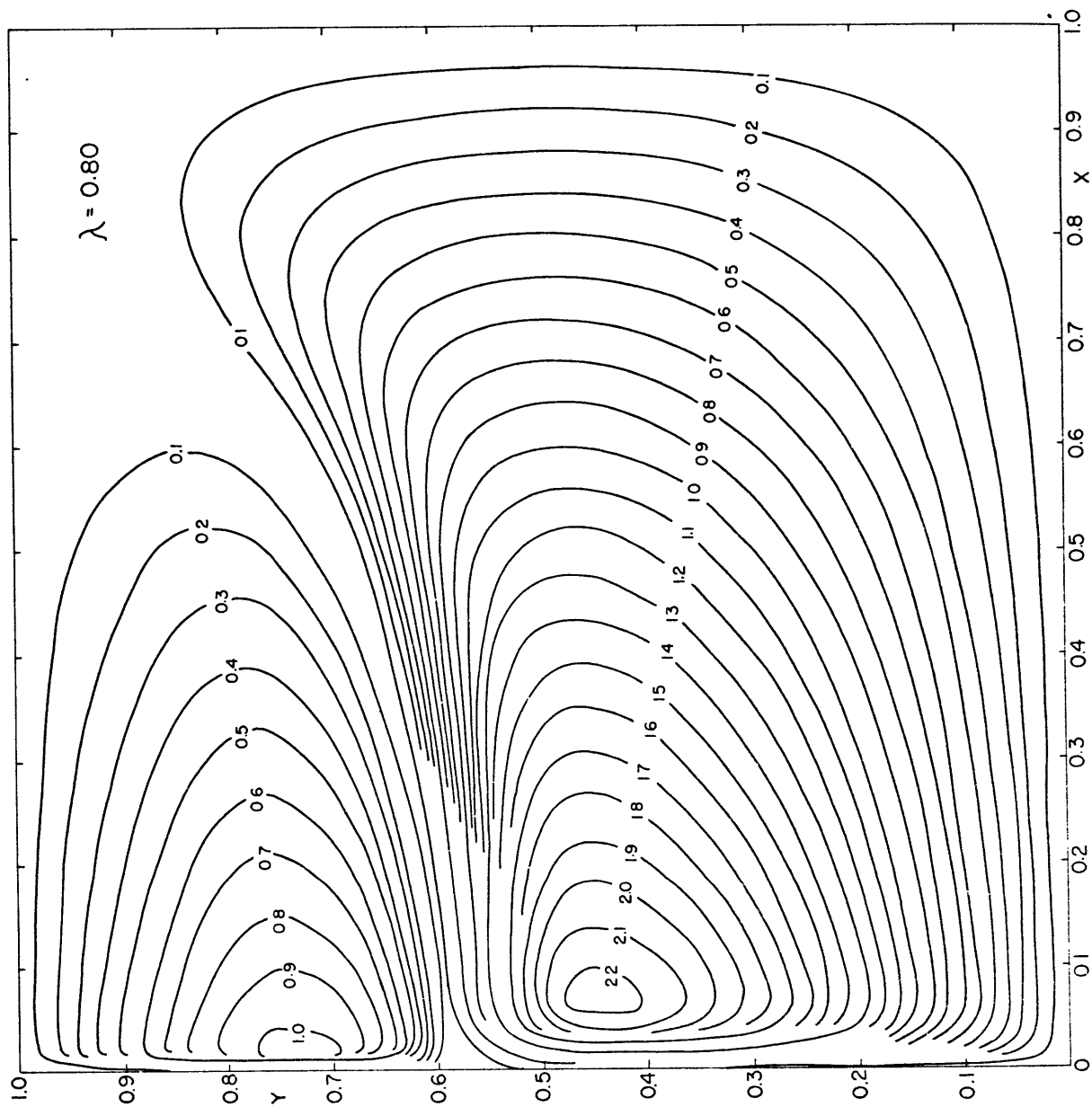
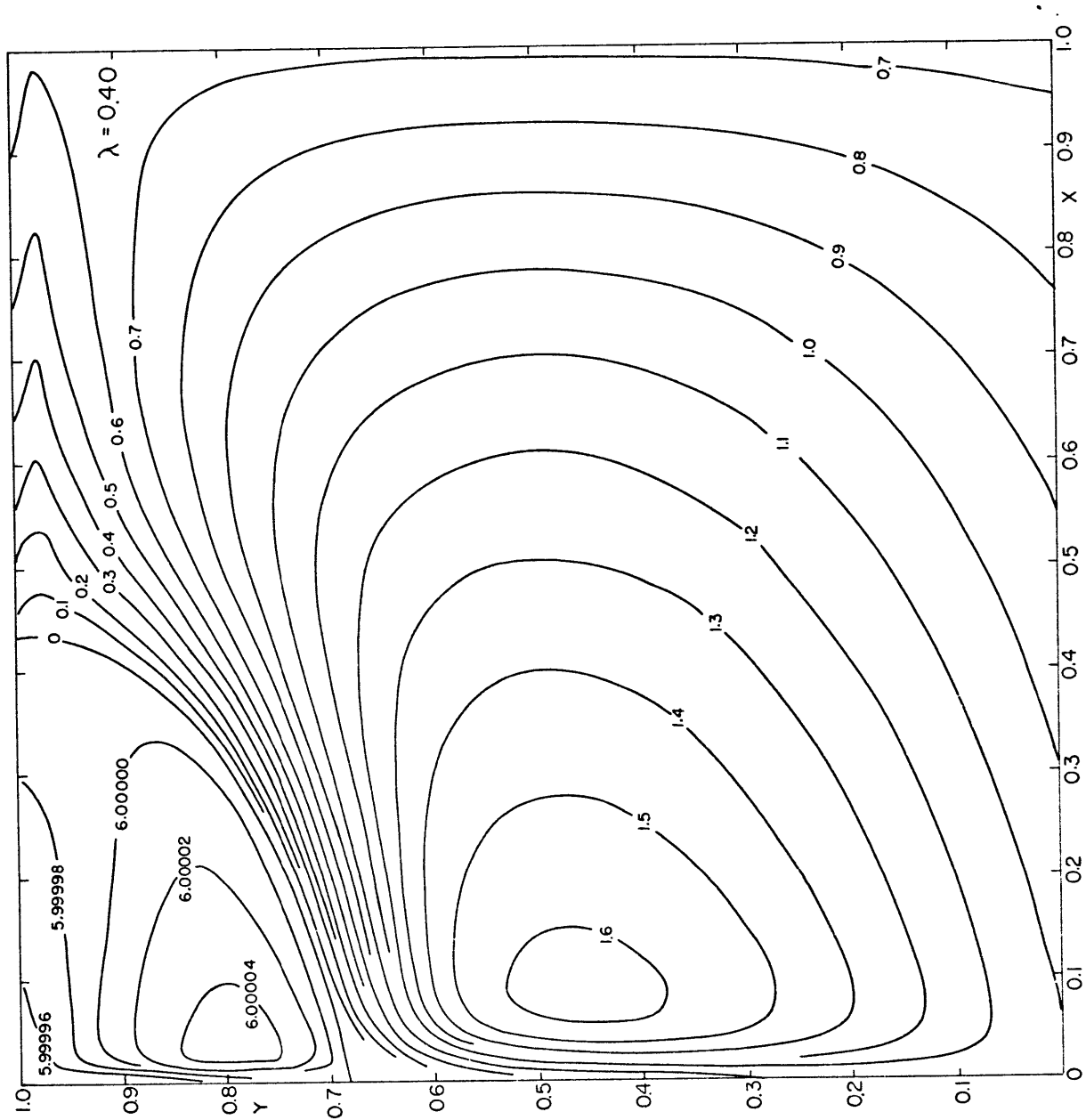


Fig. 4c. Non-dimensional Streamfunction ( $\lambda = 0.80$ )



**Fig. 5a.** Non-dimensional Surface Layer Depth ( $\lambda = 0.40$ )

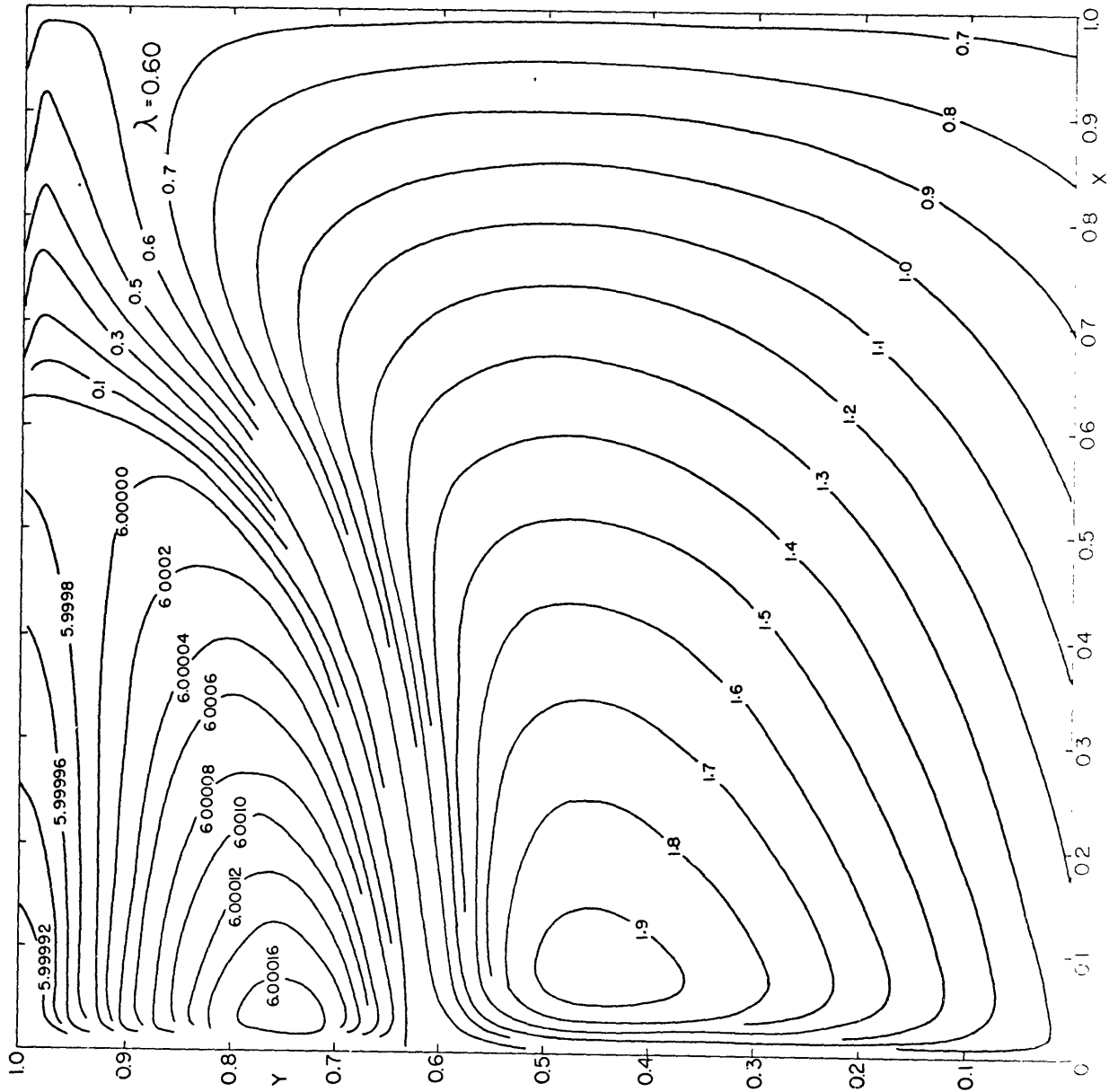
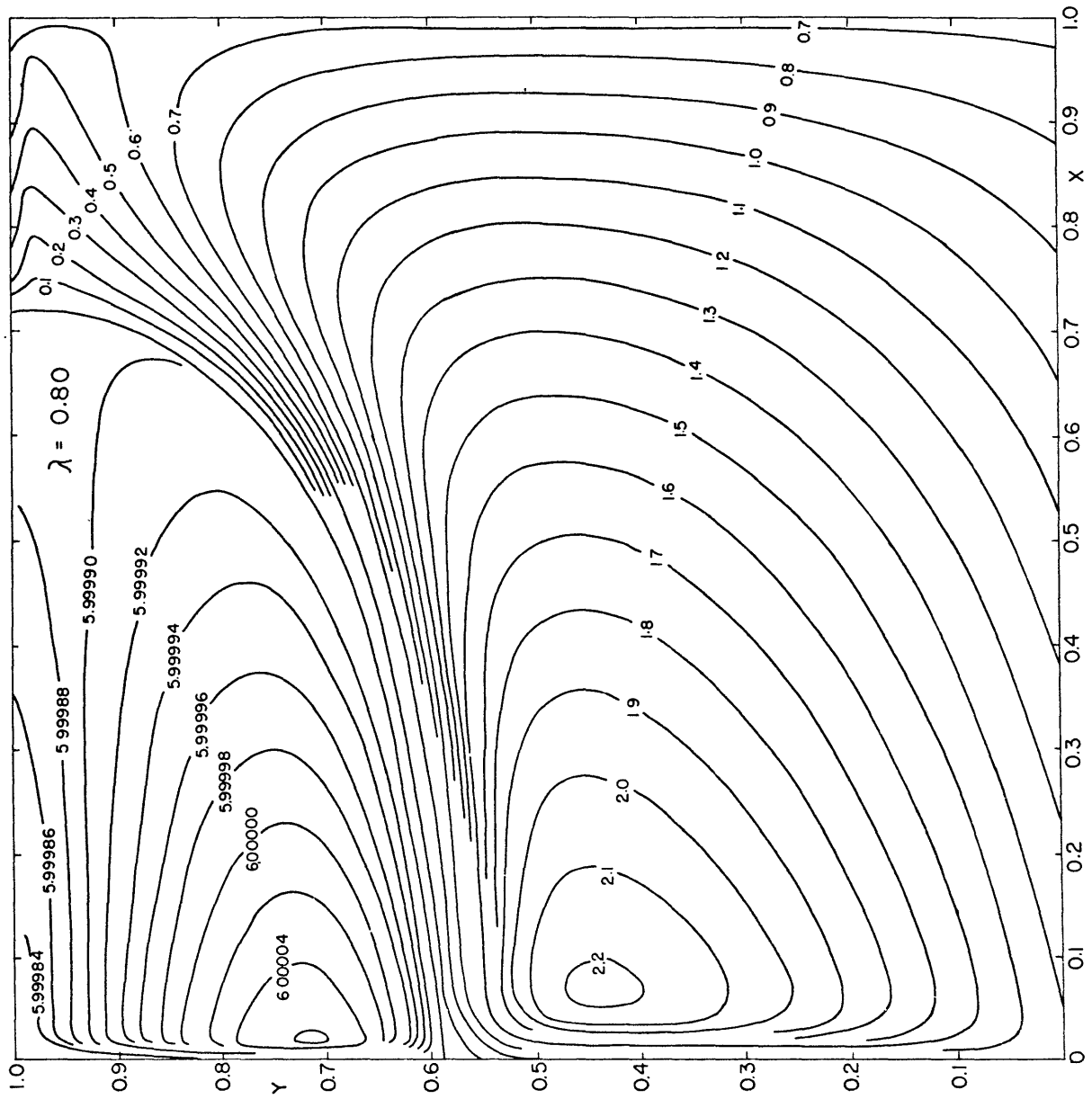


Fig. 5b. Non-dimensional Surface Layer Depth ( $\lambda = 0.60$ )



**Fig. 5c.** Non-dimensional Surface Layer Depth ( $\lambda = 0.80$ )

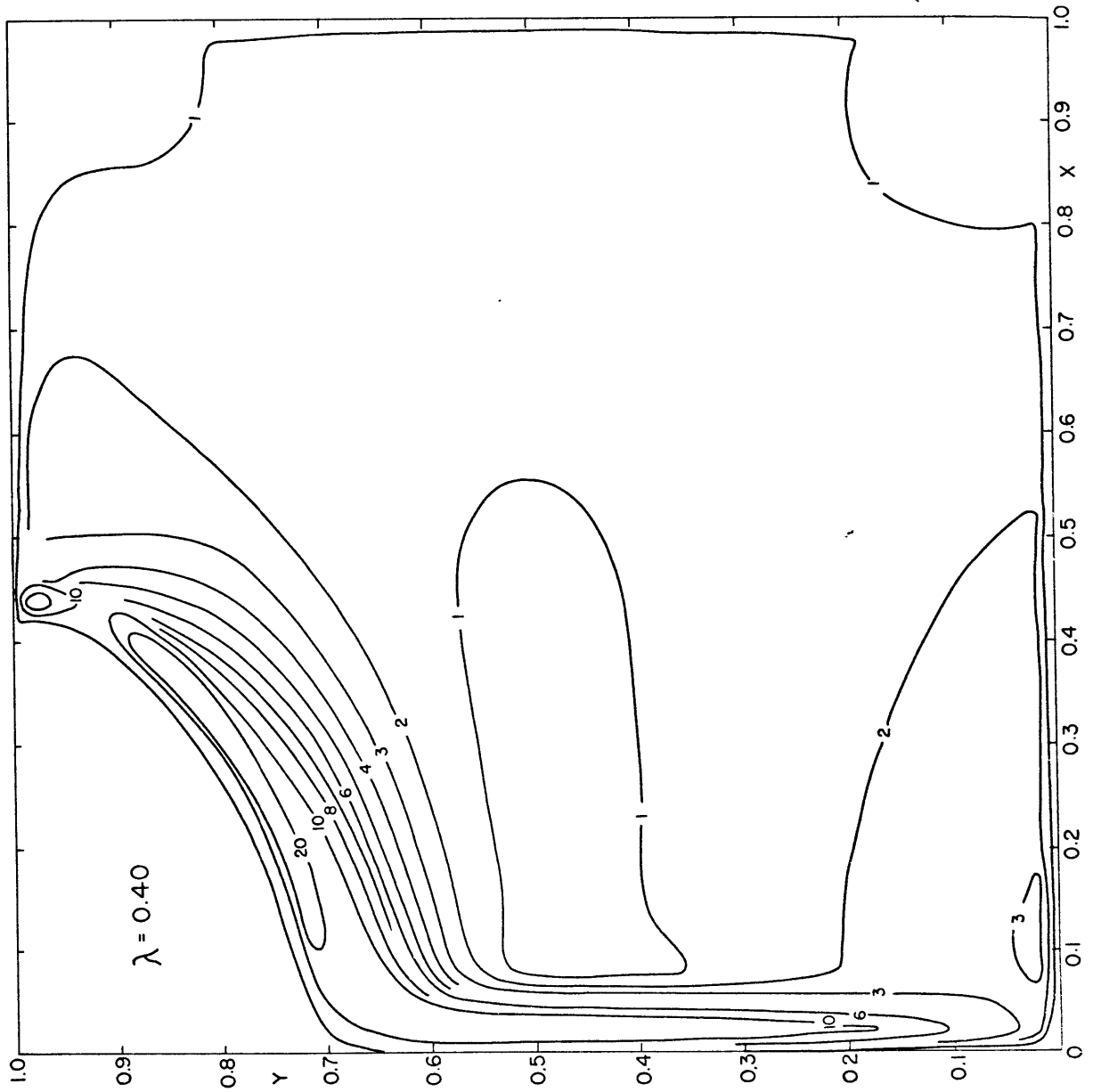
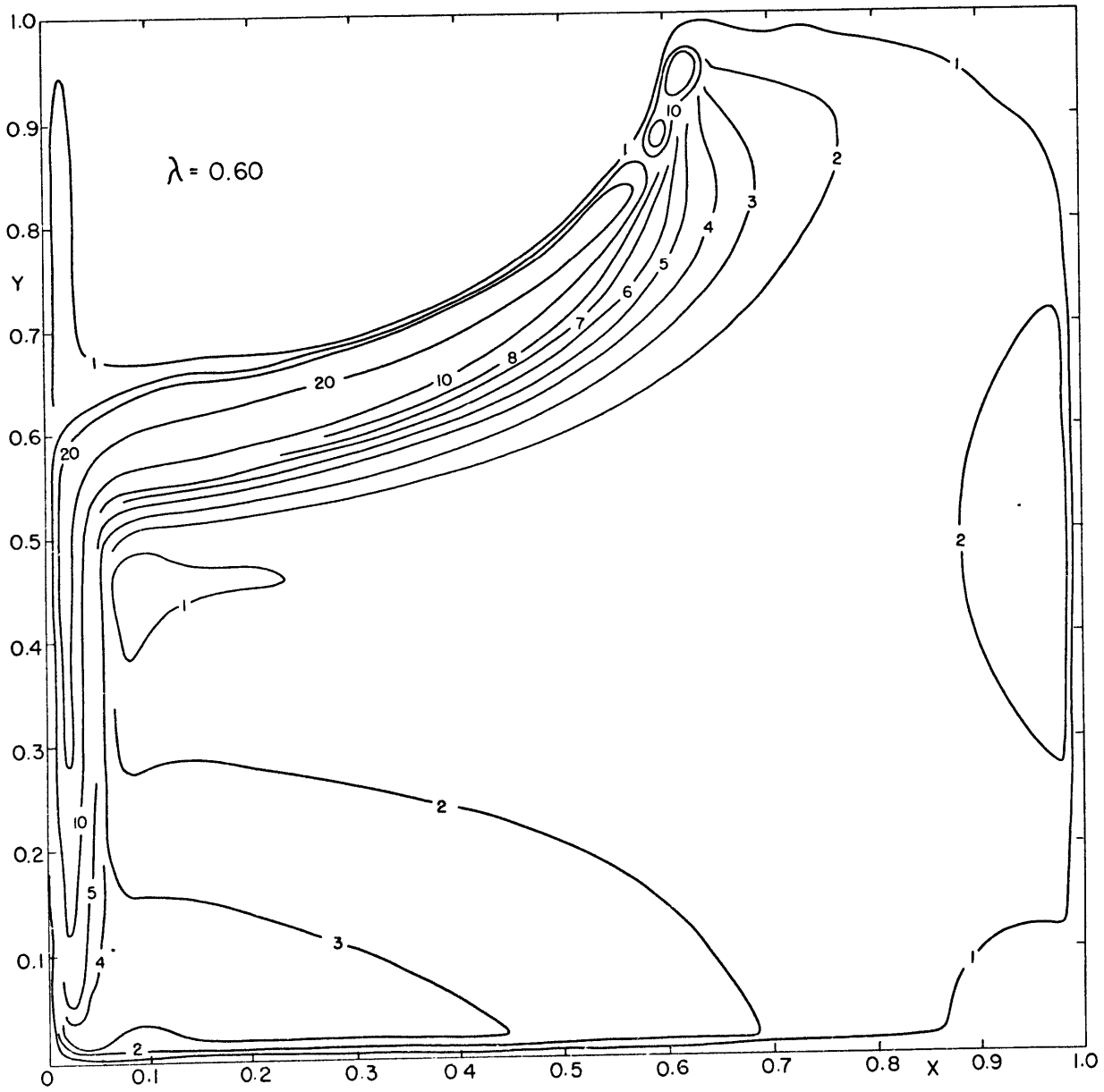


Fig. 6a. Non-dimensional Surface Layer Speeds ( $\lambda = 0.40$ )

Fig. 6b. Non-dimensional Surface Layer Speeds ( $\lambda = 0.60$ )



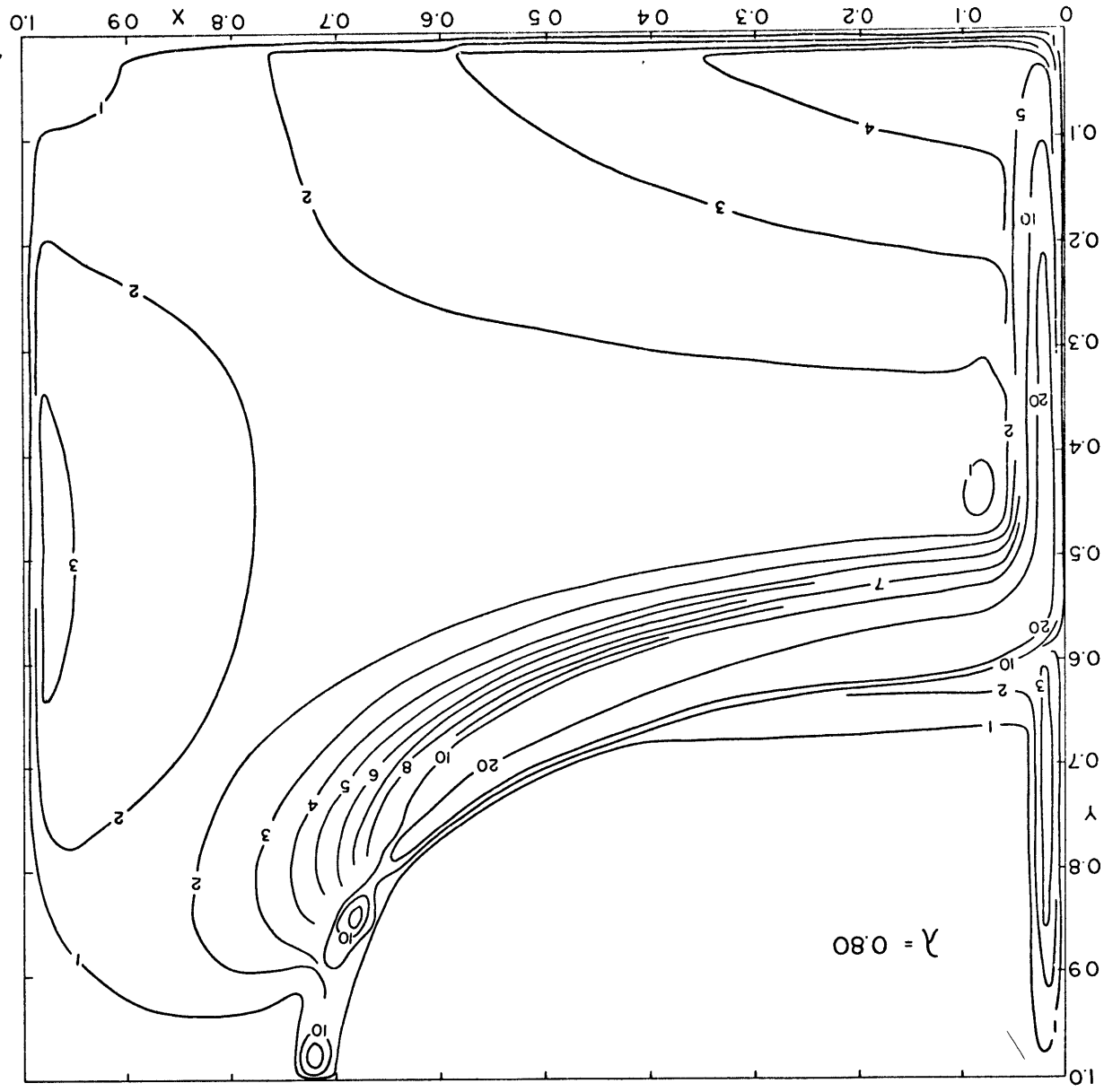


Fig. 6c. Non-dimensional Surface Layer Speeds ( $\lambda = 0.80$ )



where it exists and the depth of the surfaced lower layer in the northwest corner of the basin. Fig. 6 gives the distribution of particle speeds; a, b, and c correspond to  $\lambda = 0.40, 0.60, \text{ and } 0.80$ , respectively. The quantities in Figs. 4-6 are presented in non-dimensional units. To convert to dimensional form, multiply the displayed values in Fig. 4 by  $1.75 \times 10^{13} \text{ cm}^3 \text{ s}^{-1}$ , those in Fig. 5 by  $3 \times 10^4 \text{ cm}$  and those in Fig. 6 by  $0.9697 \text{ cm s}^{-1}$ .

Examination of Figs. 4-6 shows that the circulation increases, the thermocline deepens and higher flow speeds result from increasing the wind stress parameter. The change in the lower layer is more dramatic due to the combined effects of stronger wind, greater area of water exposed to the wind and southward penetration into an area of greater wind stress curl.

Integration of the oceanic thermal equation is done by a Lagrangian technique. We follow individual parcels around streamlines calculating the temperature change from the vertical flux of heat into the parcel. We thus do not explicitly calculate the heat advection term. The major advantage of this method is that it places a large number of points in the boundary layers where the streamlines are close together.

In the upper layer, ten equally spaced streamlines are selected in the interval between the maximum value of the streamfunction and zero. Similarly, three equally spaced

streamlines are chosen in the lower layer. A search is conducted for crossings of individual streamlines with horizontal gridlines (grid crossings). Velocities and depths are interpolated onto these grid crossings. The distances between grid crossings along streamlines are calculated. The traversal times between grid crossings are then found using the velocities at the grid crossings and the distances between the crossings. We assume that the velocity at a given crossing holds along the streamline halfway to the upstream and downstream crossings. We then sum the traversal times around streamlines to arrive at the total traversal times for parcels of fluid around particular streamlines.

Each streamline is then divided into an equal number of segments with the property that on a given streamline the segment traversal time is uniform. The segment endpoints (streamline points) will be the points at which the thermodynamic equation will be integrated. This procedure makes the thermodynamic integration very direct. Fig. 7 schematically illustrates the above calculations. The cases presented in this paper were run with 200 integration points per streamline.

An atmospheric temperature distribution and an initial oceanic temperature distribution are specified. The temperatures at the streamline points are then stepped forward in time, the values at the end of a time step being equal to the

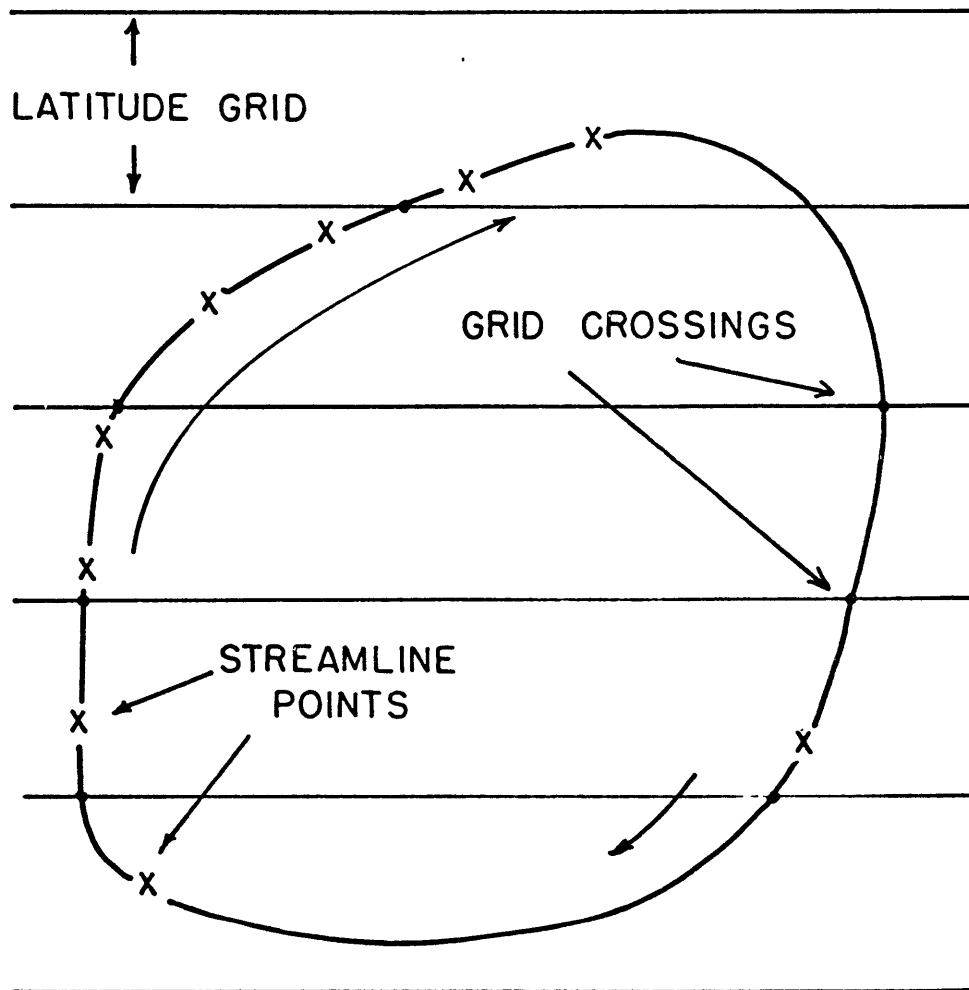


Fig. 7. Determination of Integration Points for Thermodynamic Equation

values at the upstream gridpoints after the previous time step plus the heat added during the time step. This heat addition, according to our linear law, is proportional to the difference between the average atmospheric temperature at the two points and the oceanic temperature at the upstream point.

It is only meaningful to discuss equilibrium solutions with this method. The time step varies with streamline because we have taken the same number of points along every streamline and the total traversal time varies with streamline. Therefore, since the temperature field on each streamline is evolving in its own time frame, the overall temperature field after an arbitrary amount of integration time is, in general, unknown.

Testing for convergence of the ocean temperature integration is handled in the following fashion. Equilibration occurs because of the damping nature of the forcing. The effect of the heat flow term is to diminish temperature differences between the atmosphere and the ocean. Areas of rapid currents in which parcels travel great distances during the thermal forcing decay time are the only regions in which significant differences between the oceanic and atmospheric temperatures occur.

When the process is simulated in finite difference form the major problem we encountered was an oscillatory instability. If the temperature of a given parcel was

sufficiently far from the atmospheric temperature and the time step was large enough, the parcel would greatly overshoot the equilibrium point.

This problem was solved by decreasing the time steps of integration by increasing the number of points around the streamlines so that unrealistically large forcings for long periods of time were not present and oscillatory damping or simple damping was realized.

At each integration point on a given streamline for each time step we compared the  $\Delta T_0$  of the parcel during the time step as it moved from the upstream gridpoint to the same  $\Delta T_0$  from the previous time step. If for all streamline points the absolute value of the change in the  $\Delta T_0$ 's from the previous time step was less than a threshold value the streamline was said to have converged and integration was discontinued on that particular streamline. Table 2 depicts for a standard case the number of time steps and the total time for equilibration for each of the streamlines used in the integration as a function of the convergence threshold value. For the cases we have run the tolerance was set to  $10^{-8}$  °C, the minimum resolvable by our single precision calculation.

Given the equilibrium distribution of oceanic temperature it is possible to calculate a number of quantities. The first thing that we looked for was the northward flux of heat in the surface layer across a latitude wall in the basin.

TABLE 2

$$\lambda = 0.45 \quad C_{HF} = 8000 \text{ cal cm}^{-2} \text{ yr}^{-1} \text{ } ^\circ\text{C}^{-1}$$

ATMOSPHERIC TEMPERATURE DIFFERENCE  
BETWEEN N-S WALLS = 24 °C

INTEGRATION TIME FOR CONVERGENCE IN YEARS

NUMBER OF TIME STEPS FOR CONVERGENCE

NON-DIMENSIONAL STREAMLINE VALUE

	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0	0.04	0.08	0.12
CONVERGENCE THRESHOLD													
$1. \times 10^{-1}$	1.8 14	1.2 11	0.5 5	0.2 2	0.2 2	0.1 2	0.1 2	0.1 2	0.1 2	0.1 2	1.1 2	0.7 2	0.6 2
$1. \times 10^{-2}$	5.2 40	4.8 45	4.2 45	3.7 45	3.3 43	2.8 41	2.2 36	1.7 31	1.0 20	0.8 2	16.1 29	9.1 25	5.0 18
$1. \times 10^{-3}$	8.4 64	7.7 73	7.3 79	7.0 84	6.7 88	6.4 94	6.0 98	5.7 102	5.3 107	4.6 111	32.7 59	26.3 72	22.3 80
$1. \times 10^{-4}$	11.0 84	10.4 98	10.1 109	9.9 120	9.8 130	9.9 146	9.9 161	9.9 175	9.7 196	9.2 220	49.9 90	43.4 119	39.5 142
$1. \times 10^{-5}$	13.8 106	13.1 123	13.3 143	13.3 161	13.8 182	13.9 204	14.3 233	14.4 255	14.3 291	14.1 337	67.1 121	60.9 167	56.7 204
$1. \times 10^{-6}$	16.9 130	20.1 189	21.6 233	20.0 241	20.1 265	23.3 342	23.4 381	22.5 399	21.2 430	21.8 521	84.3 152	78.8 216	74.5 268
$1. \times 10^{-7}$	19.3 148	21.9 206	23.1 249	25.7 310	23.6 312	26.6 391	31.6 515	29.1 517	31.1 632	34.5 823	117. 211	109. 298	110. 394
$1. \times 10^{-8}$	19.3 148	21.9 206	23.1 249	26.0 314	23.7 313	26.6 391	31.6 515	29.1 517	31.1 632	34.5 823	134. 241	144. 396	129. 462

This was done by interpolating the equilibrium temperature from the streamline points back onto the grid crossings. Latitude lines were then broken up into segments on which the northward speed, mixed layer depth and oceanic temperature were taken to be that of the grid crossing within the segment. After eliminating slight net mass flows across latitude lines and subtracting the zonally averaged values of temperature, these quantities were then summed across the width of the basin, appropriately weighted by segment length. This calculation requires special treatment of latitude lines which intersect the line of separation.

It was decided to numerically analyze and contour the large number of maps desired. The contouring routine required values on a regular grid of points. Therefore, we needed to objectively analyze our solution for the oceanic temperature at the streamline points onto our original square grid. Since we had at our disposal a potentially infinite number of data points, the particular objective analysis scheme chosen was not crucial.

A Cressman-type analysis scheme was chosen. This scheme consists of an initial guess field which is corrected using the data during a sequence of scans. The difference between the data and a bilinear interpolation from the four corners of the grid box containing the data point is computed for all gridpoints. These anomalies are used to correct the analyzed field at all gridpoints within a specified scan

radius of the data point. The scanned area is elliptical in shape with an east-west major axis to better resolve zonally coherent patterns and the weight given a correction from a given data point decays with distance from the data point. We simplified Cressman's scheme by eliminating data quality checks and initial smoothing operations.

The adjustable parameters (weights, scan radius, eccentricity) for the analysis scheme were varied until the routine gave the best agreement with hand analyzed maps. Because of the extremely large number of data points (2600 in the results presented) in our 6000 km square grid, changes in the analysis parameters caused only extremely subtle changes in the results. Tracings were made of the computer maps to give the displayed results.

Use was made of our analyzed oceanic temperatures along with the specified atmospheric temperatures, which were analytic functions of  $x$  and  $y$  and could be easily evaluated at gridpoints and streamline points, to give the vertical heat flux into the ocean in the final state from the linear heat flux law.



#### IV. Experiments

Equilibrium thermal states of the model ocean were calculated subject to a variety of fixed atmospheric configurations. Three distributions of atmospheric temperature were chosen. They are all zonally uniform with uniform meridional temperature gradients. The atmospheric temperatures at the southern walls of the basin are fixed at 30°C; the temperatures at the Northern wall are 12°C, 6°C, and 0°C, respectively. We will call these the weak, medium and strong gradient cases; the gradients are representative of those over the North Atlantic for summer, annual average and winter conditions (Figs. 8 a-c).

Results will be presented for the eleven different case outlined in Table 3. The first case is a control run. Following the control run are results which show the model response to differing heat flux constants, wind stress magnitudes and atmospheric temperatures. Then we present results from two composite cases in which the forcings are intended to simulate perpetual summer and winter conditions. The last two cases show some behavior of the model with significantly different values of  $C_{HF}$ .

The wind stress parameter was varied over a range ( $0.40 \leq \lambda \leq 0.80$ ) which included Parsons' value ( $\lambda = 0.45$ ) and was wide enough to give a good visual depiction of model sensitivity. Haney (1971, 1974) and Takano (1975) have

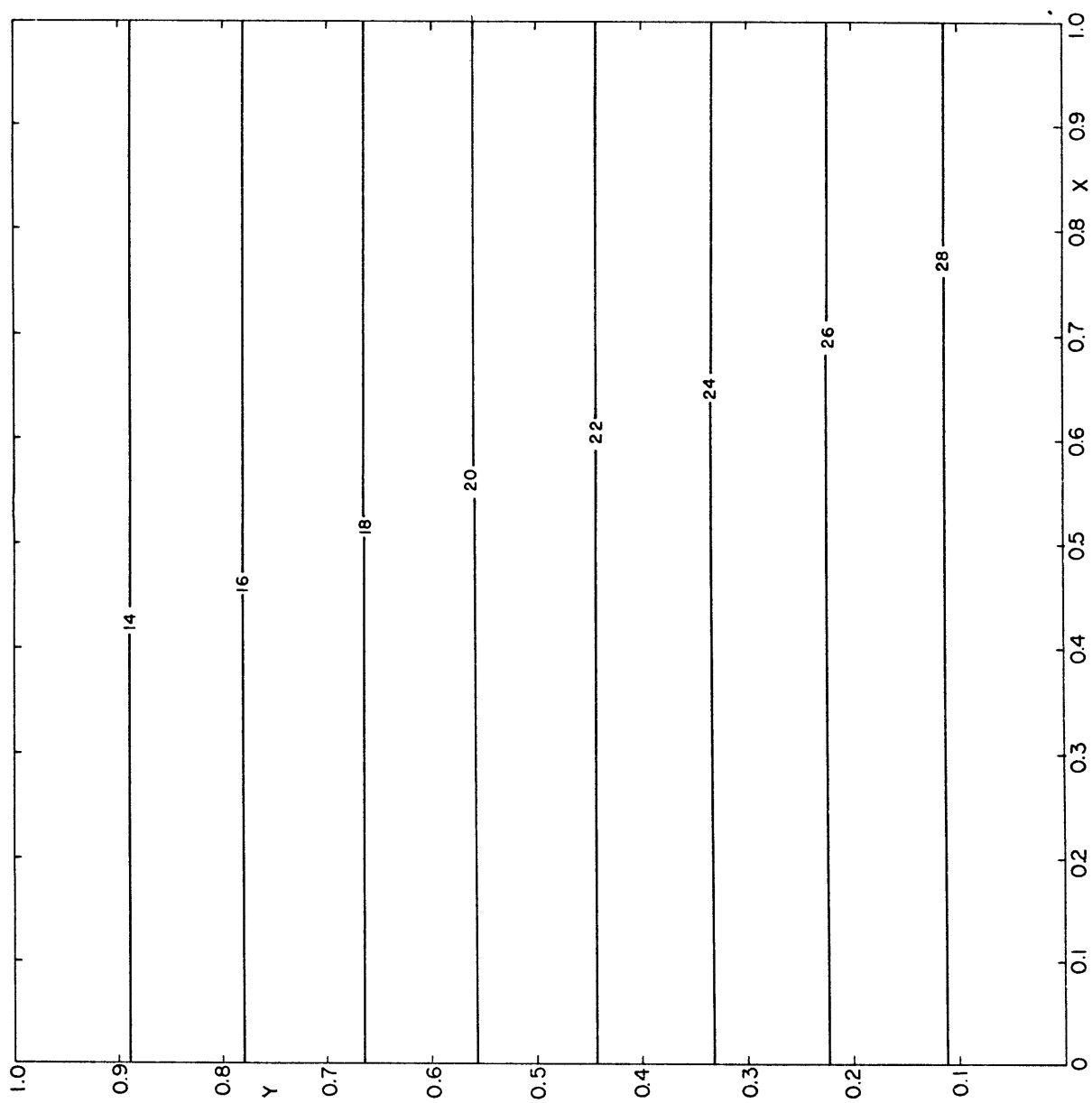


Fig. 8a. Atmospheric Temperature in °C ( $\Delta T_A = 18^\circ\text{C}$ )

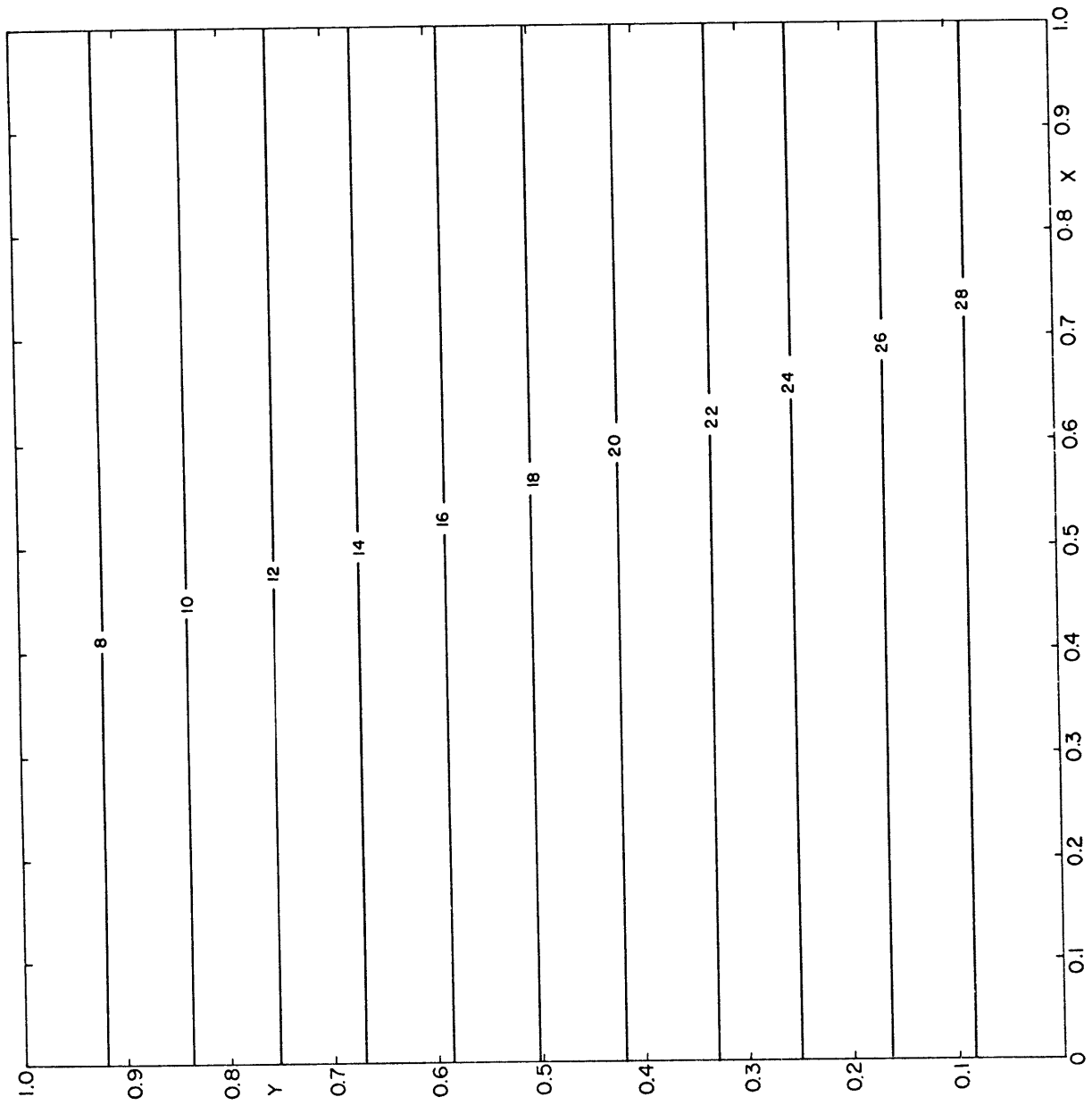


Fig. 8b. Atmospheric Temperature in °C ( $\Delta T_a = 24^\circ\text{C}$ )

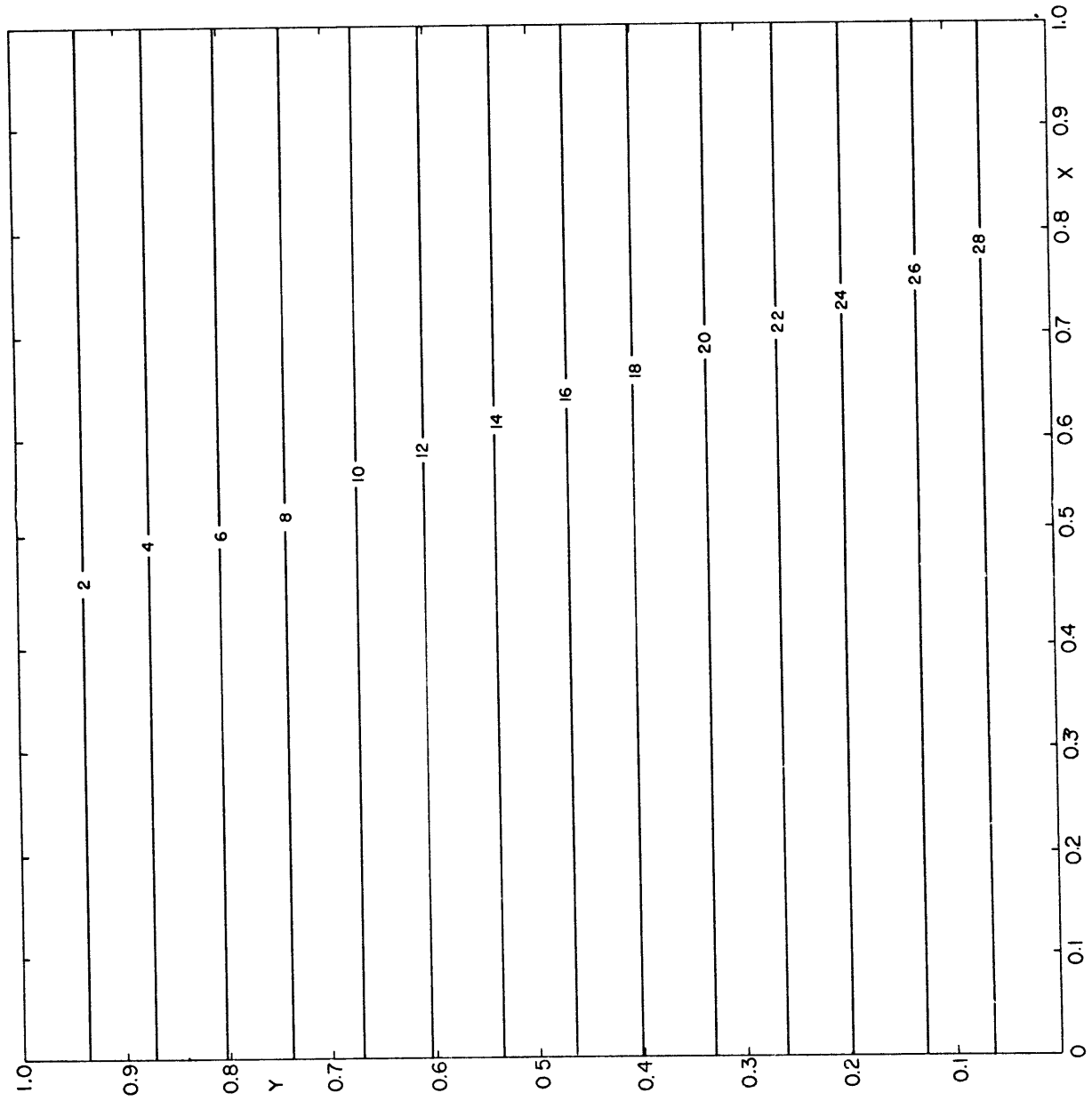


Fig. 8c. Atmospheric Temperature in °C ( $\Delta T_A = 30^\circ\text{C}$ )

TABLE 3

Case	$\lambda$	$C_{HF}$ (cal cm <sup>-2</sup> yr <sup>-1</sup> °C <sup>-1</sup> )	$\Delta T_A$ (°C)
1	0.60	6000	24
2	0.60	8000	24
3	0.60	4000	24
4	0.80	6000	24
5	0.40	6000	24
6	0.60	6000	18
7	0.60	6000	30
8	0.40	4000	18
9	0.80	8000	30
10	0.60	2000	24
11	0.60	20000	24

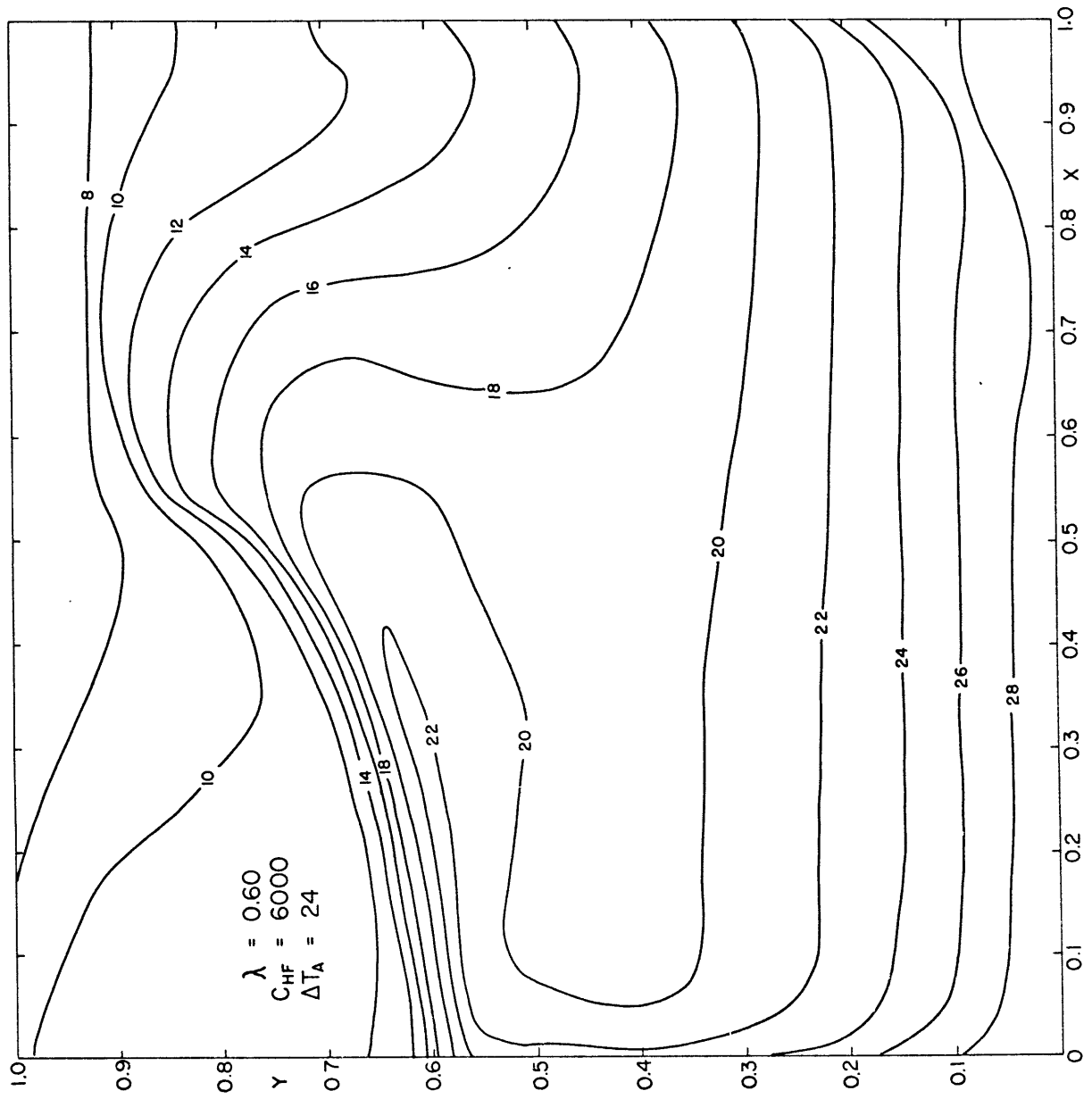


Fig. 9a. Equilibrium Oceanic Temperature in °C (Case 1)

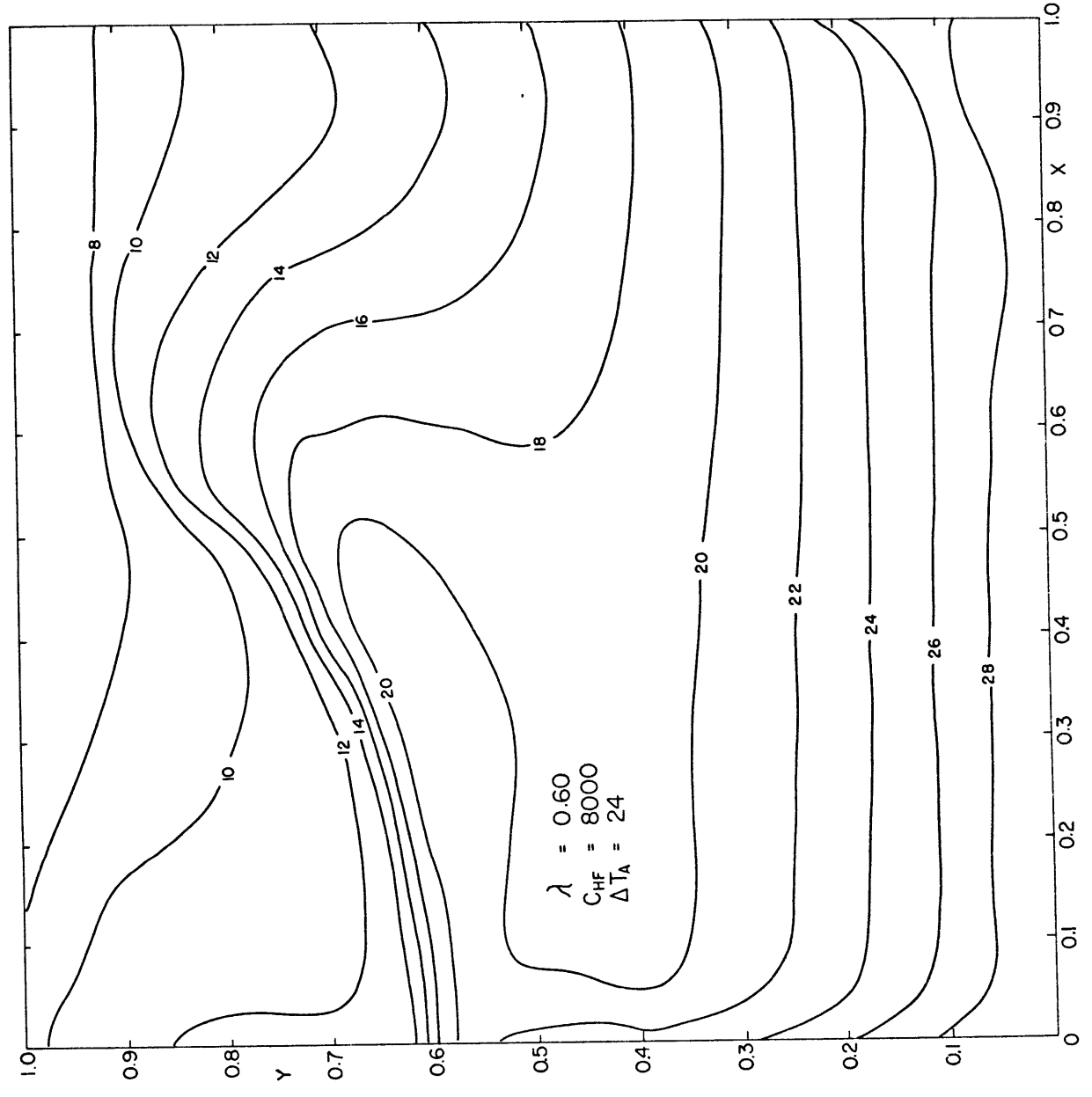


Fig. 9b. Equilibrium Oceanic Temperature in °C (Case 2)

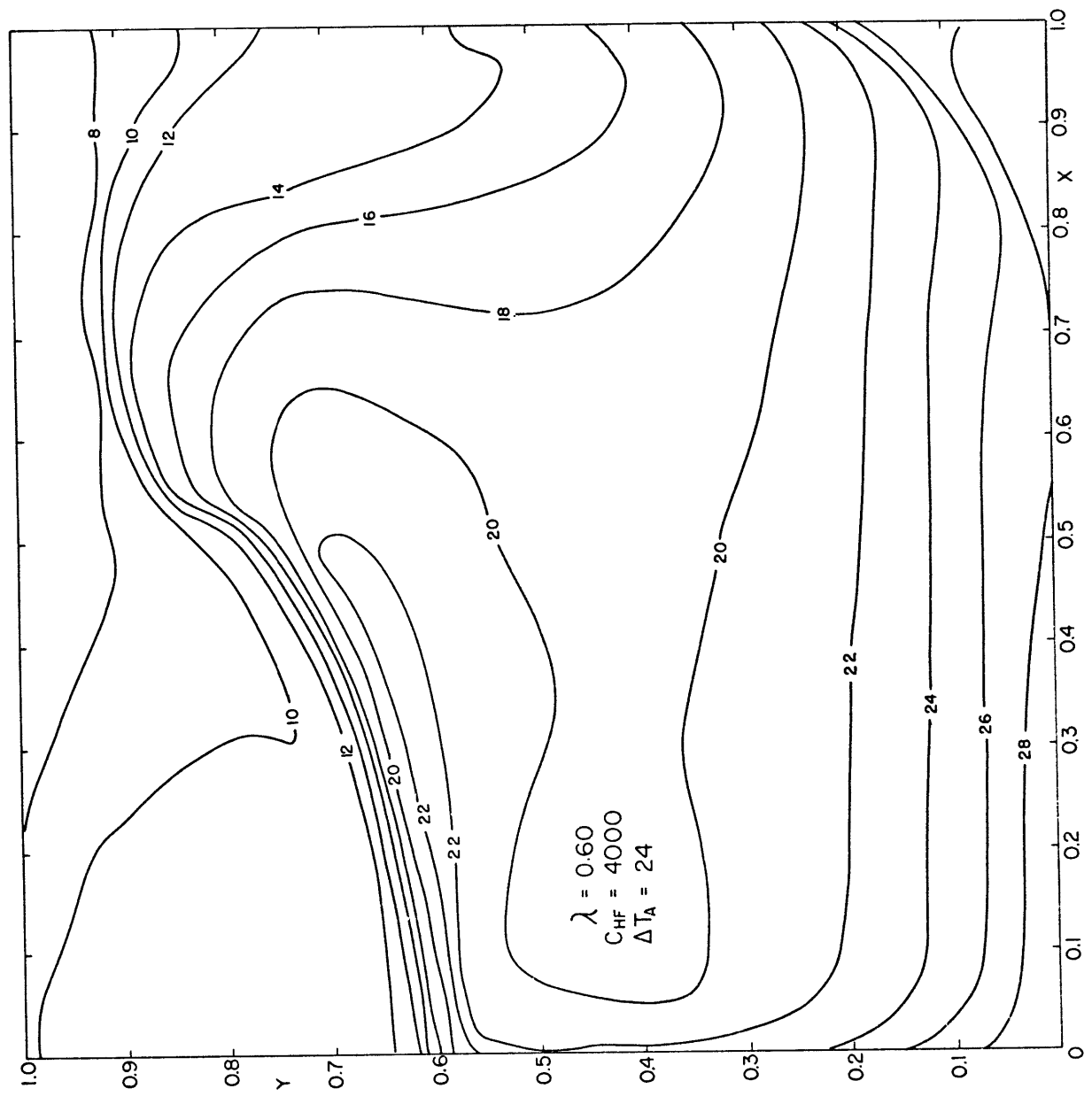


Fig. 9c. Equilibrium Oceanic Temperature in °C (Case 3)



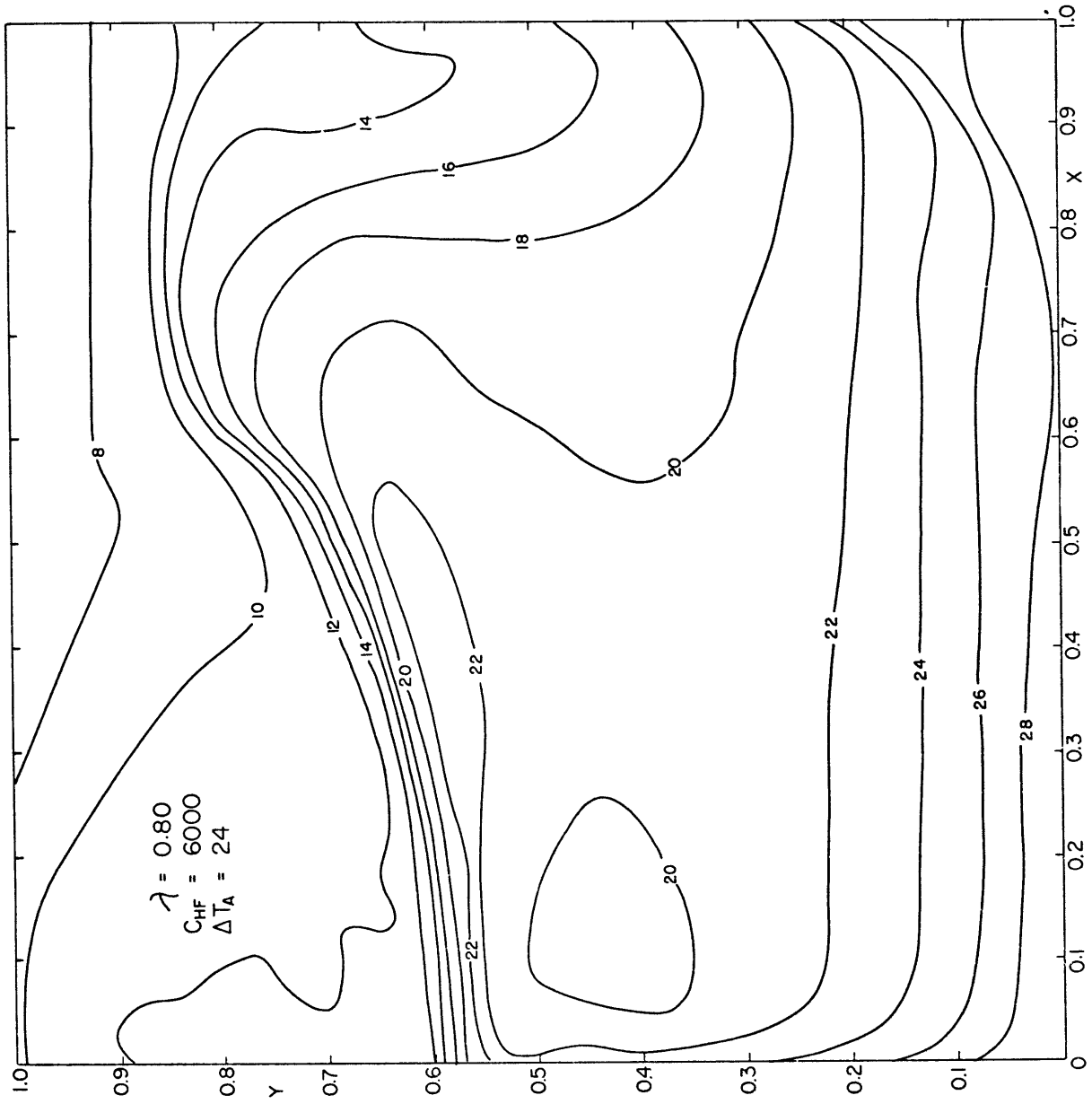


Fig. 9d. Equilibrium Oceanic Temperature in °C (Case 4)

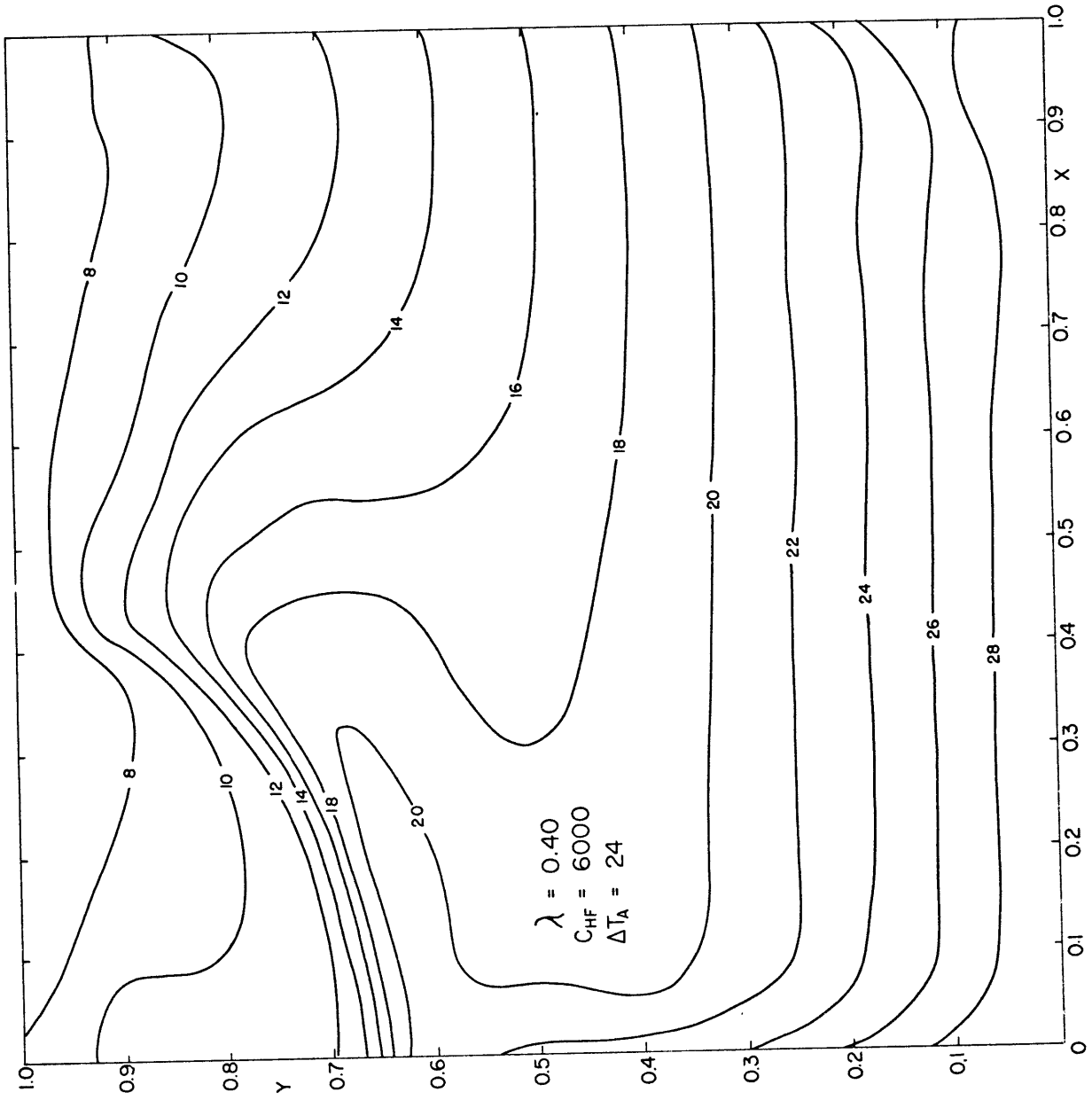


Fig. 9e. Equilibrium Oceanic Temperature in °C (Case 5)

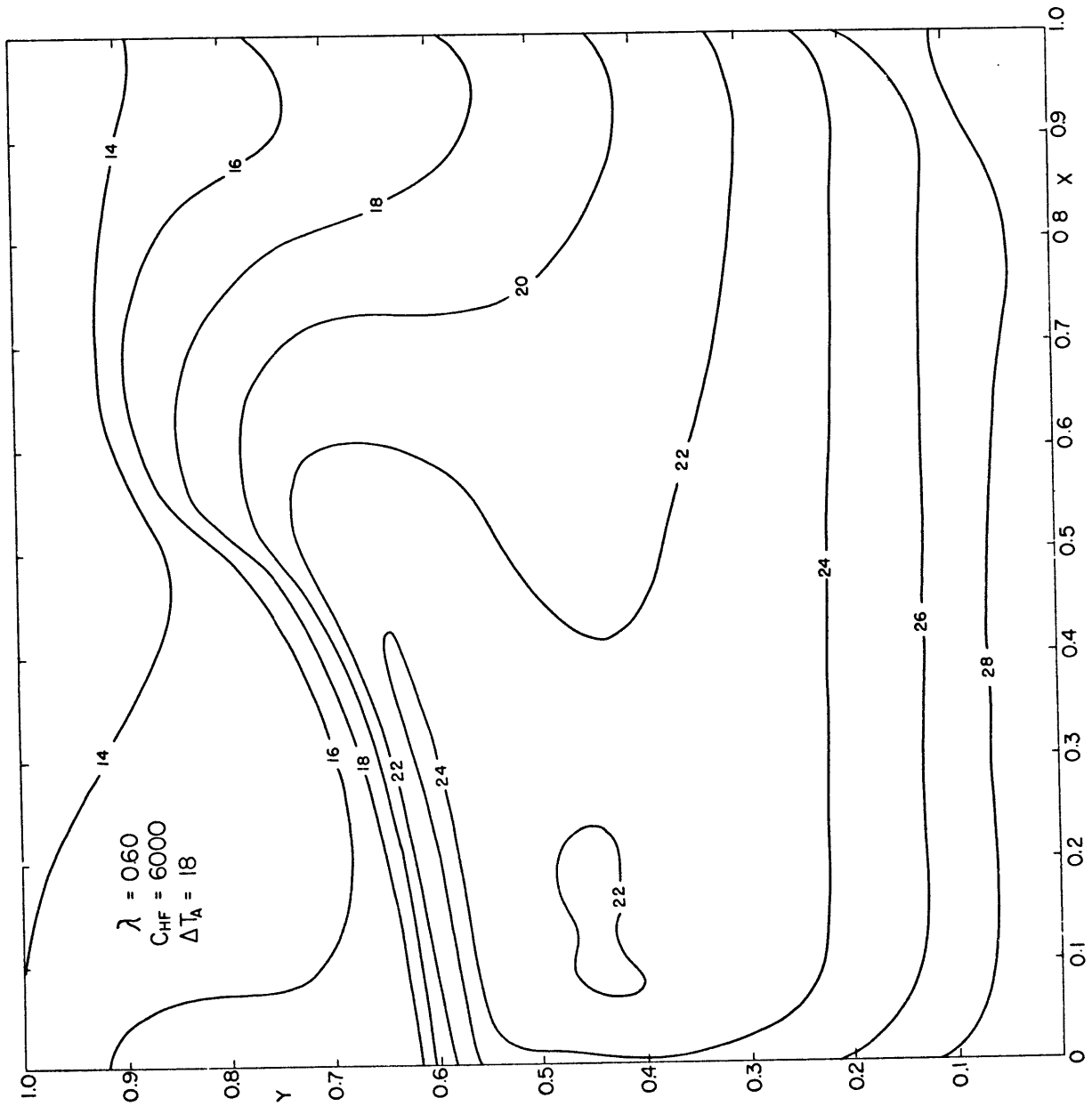


Fig. 9f. Equilibrium Oceanic Temperature in °C (Case 6)

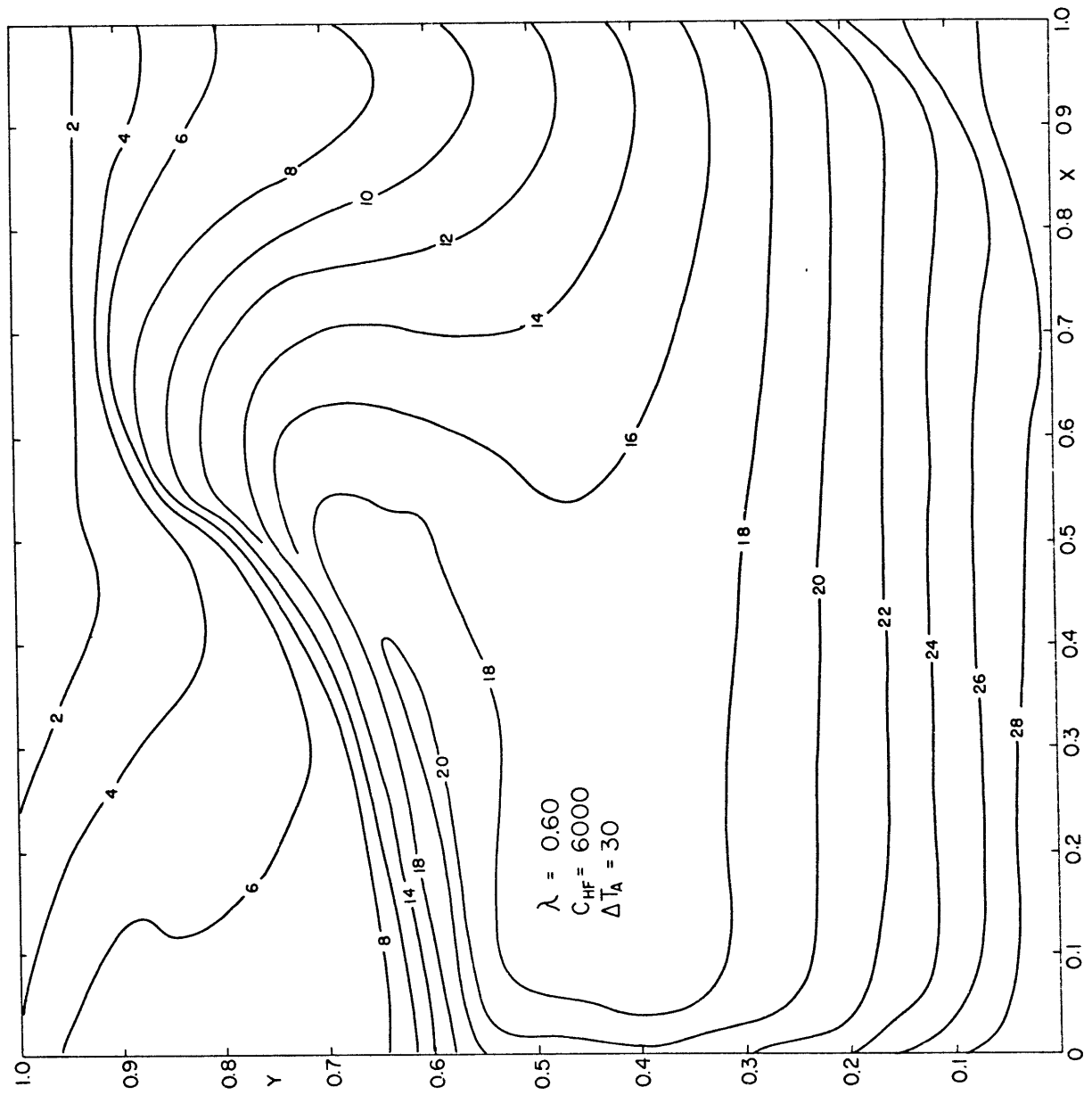


Fig. 9g. Equilibrium Oceanic Temperature in °C (Case 7)

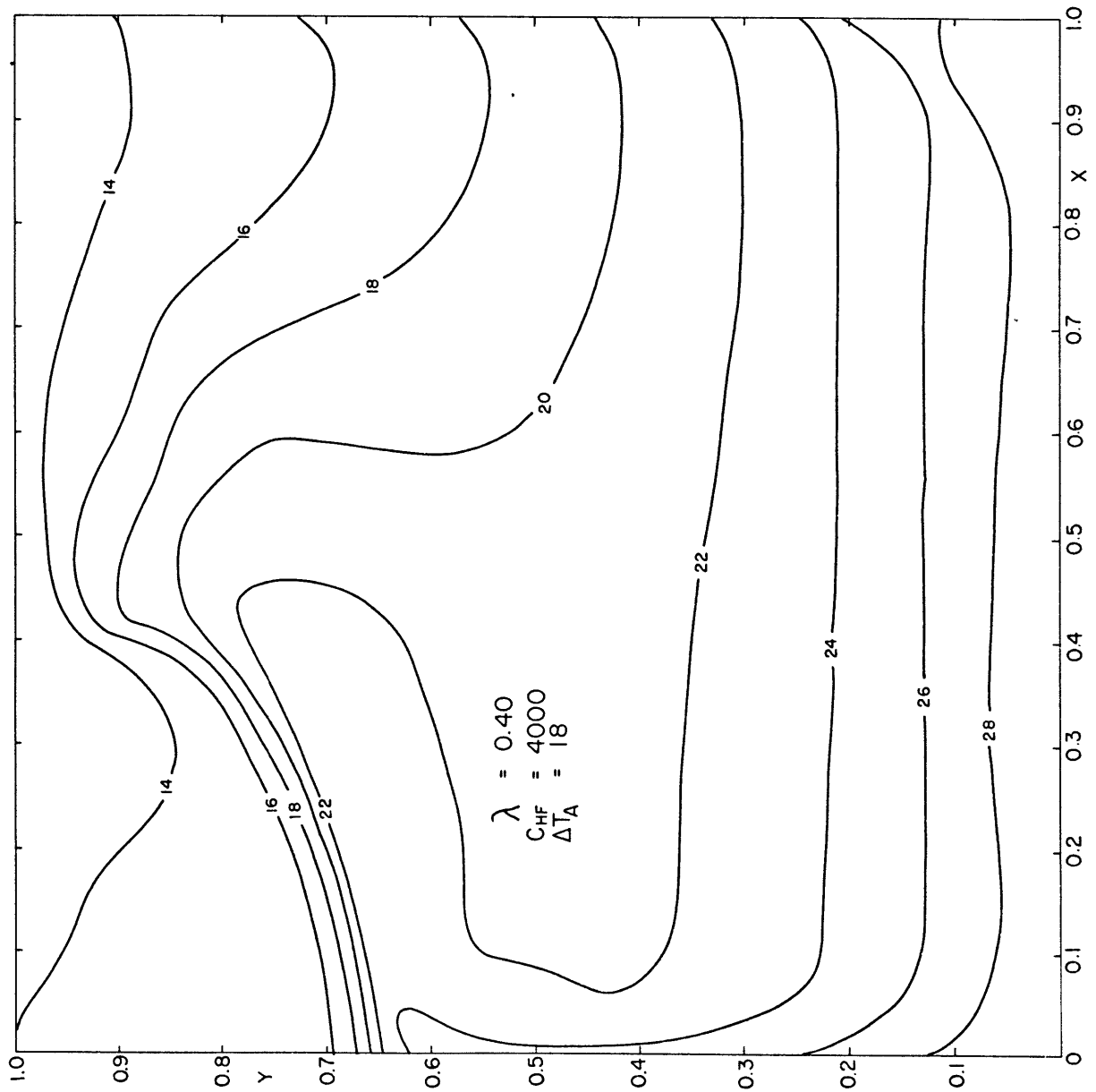


Fig. 9h. Equilibrium Oceanic Temperature in °C (Case 8)

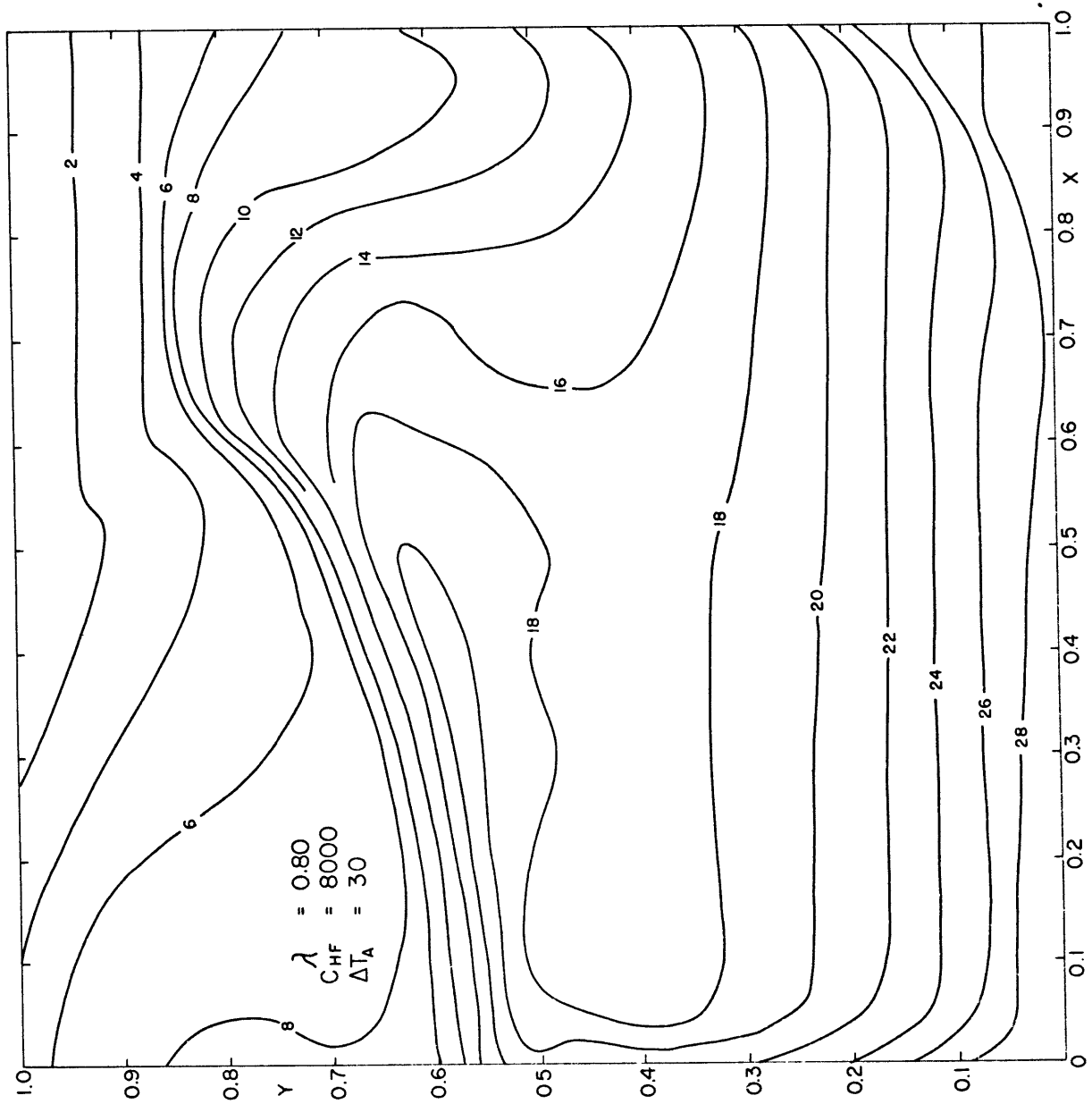


Fig. 9i. Equilibrium Oceanic Temperature in °C (Case 9)

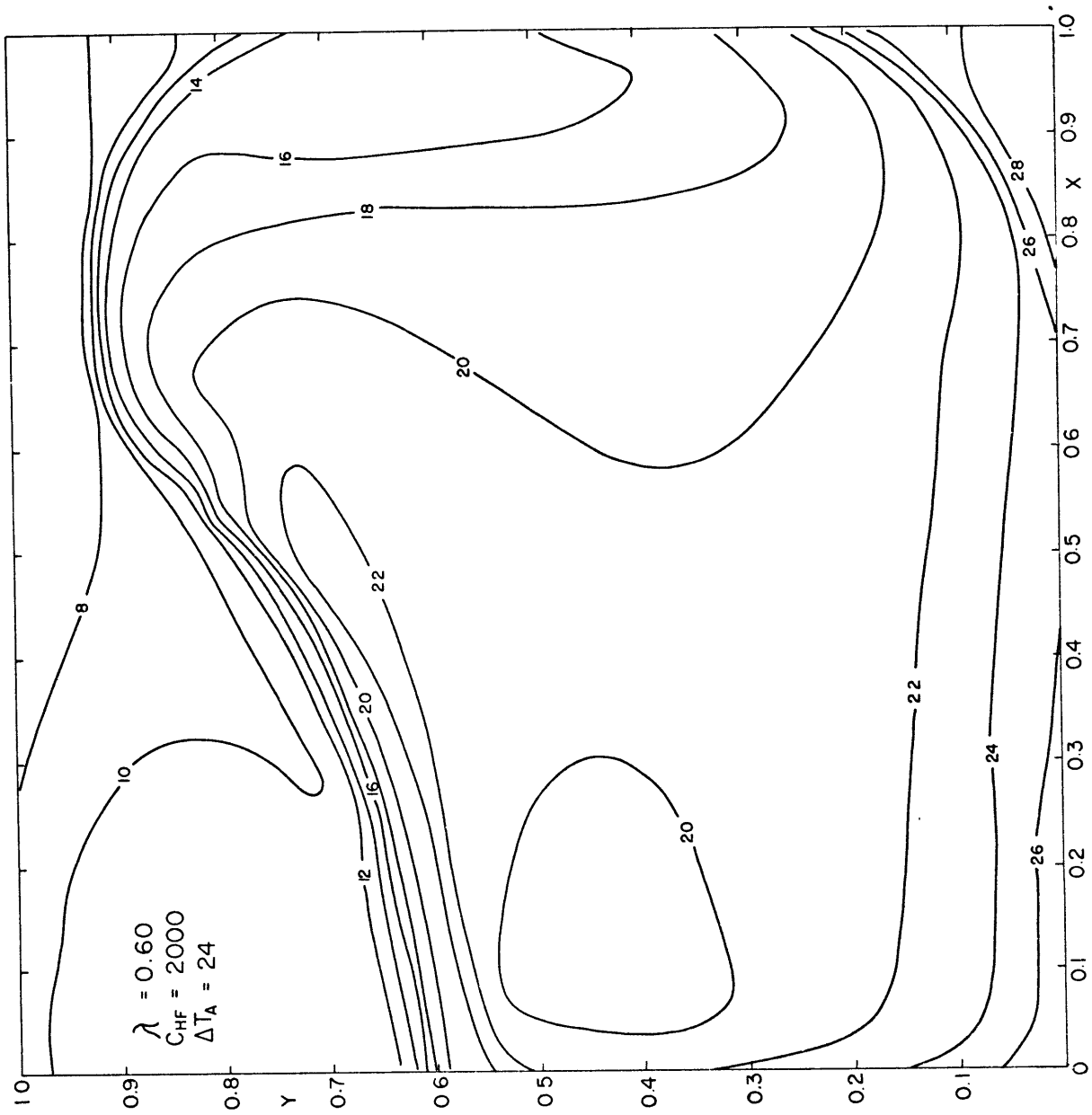


Fig. 9j. Equilibrium Oceanic Temperature in °C (Case 10)

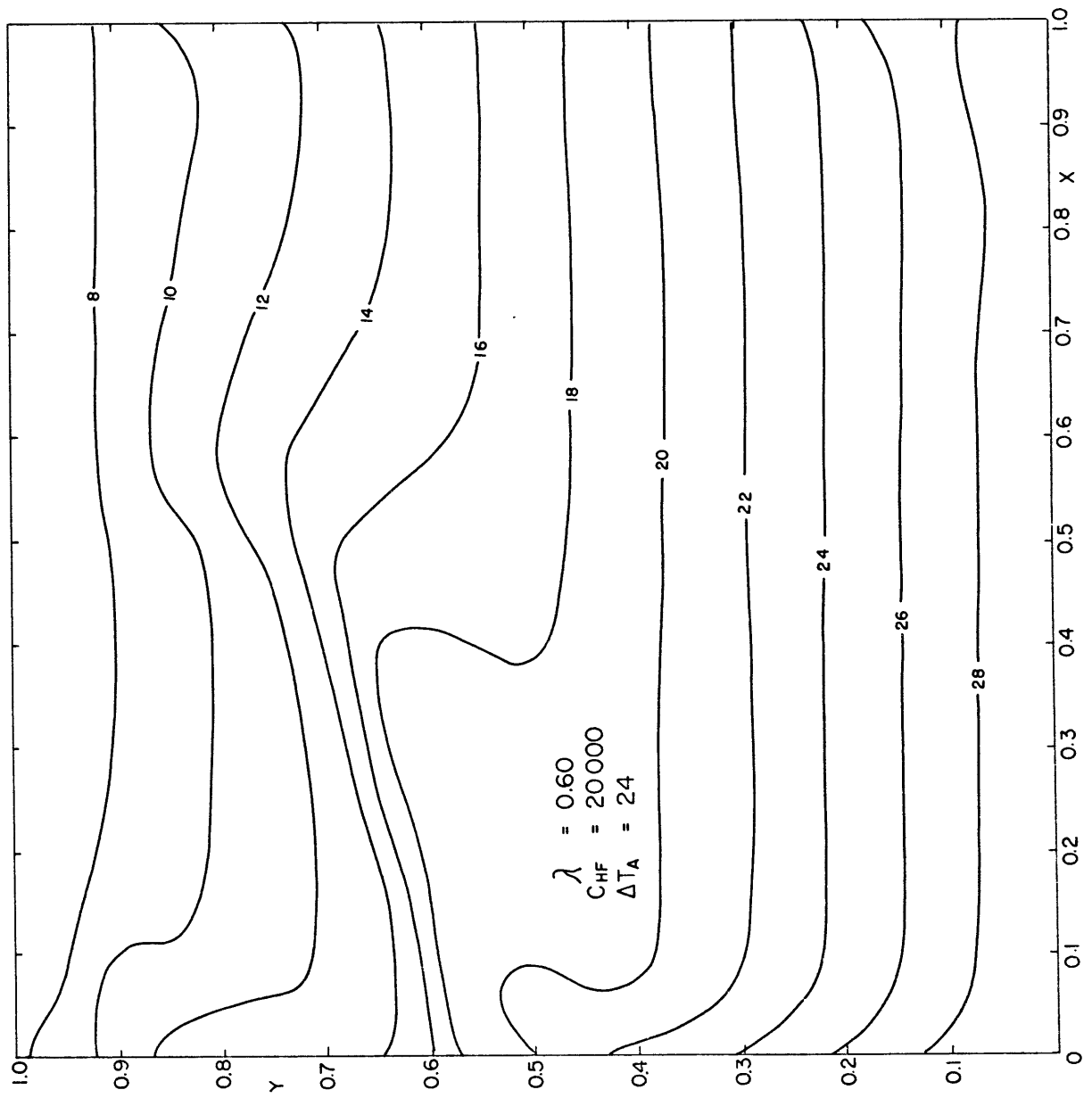


Fig. 9k. Equilibrium Oceanic Temperature in °C (Case 11)



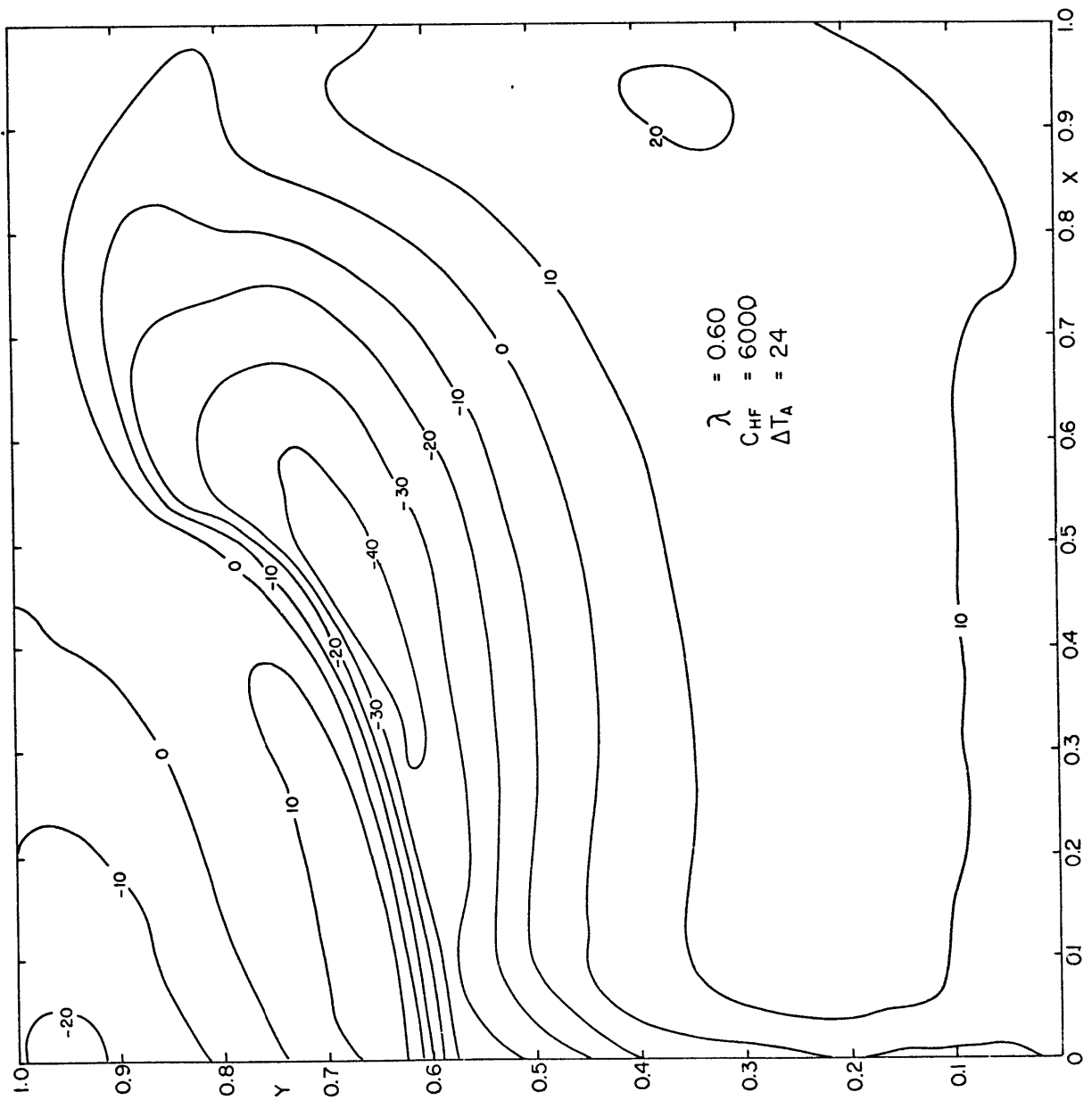


Fig. 11a. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$   
(Case 1)

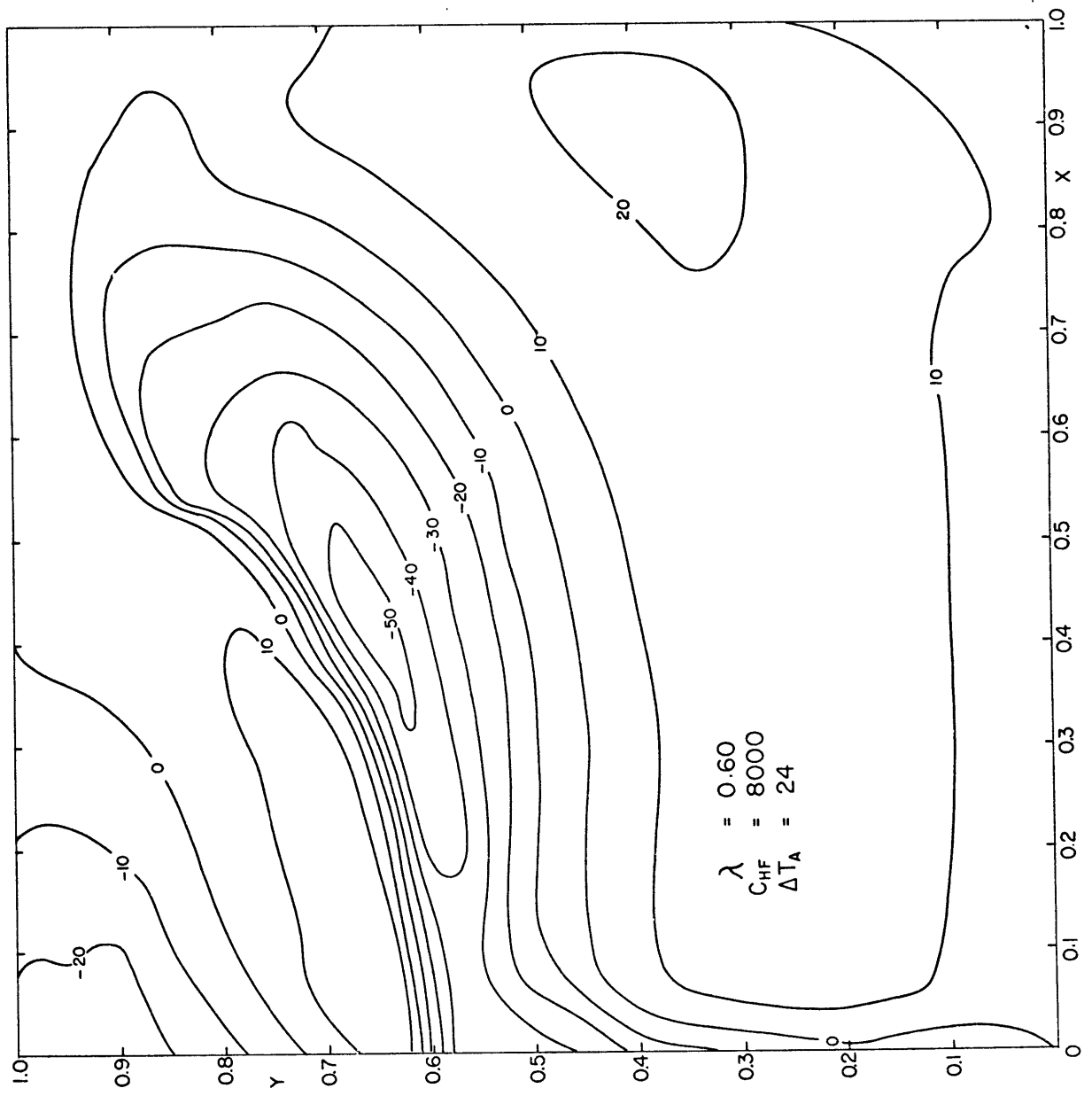


Fig. 11b. Equilibrium Vertical Heat Flux in kcal cm<sup>-2</sup> yr<sup>-1</sup> (Case 2)

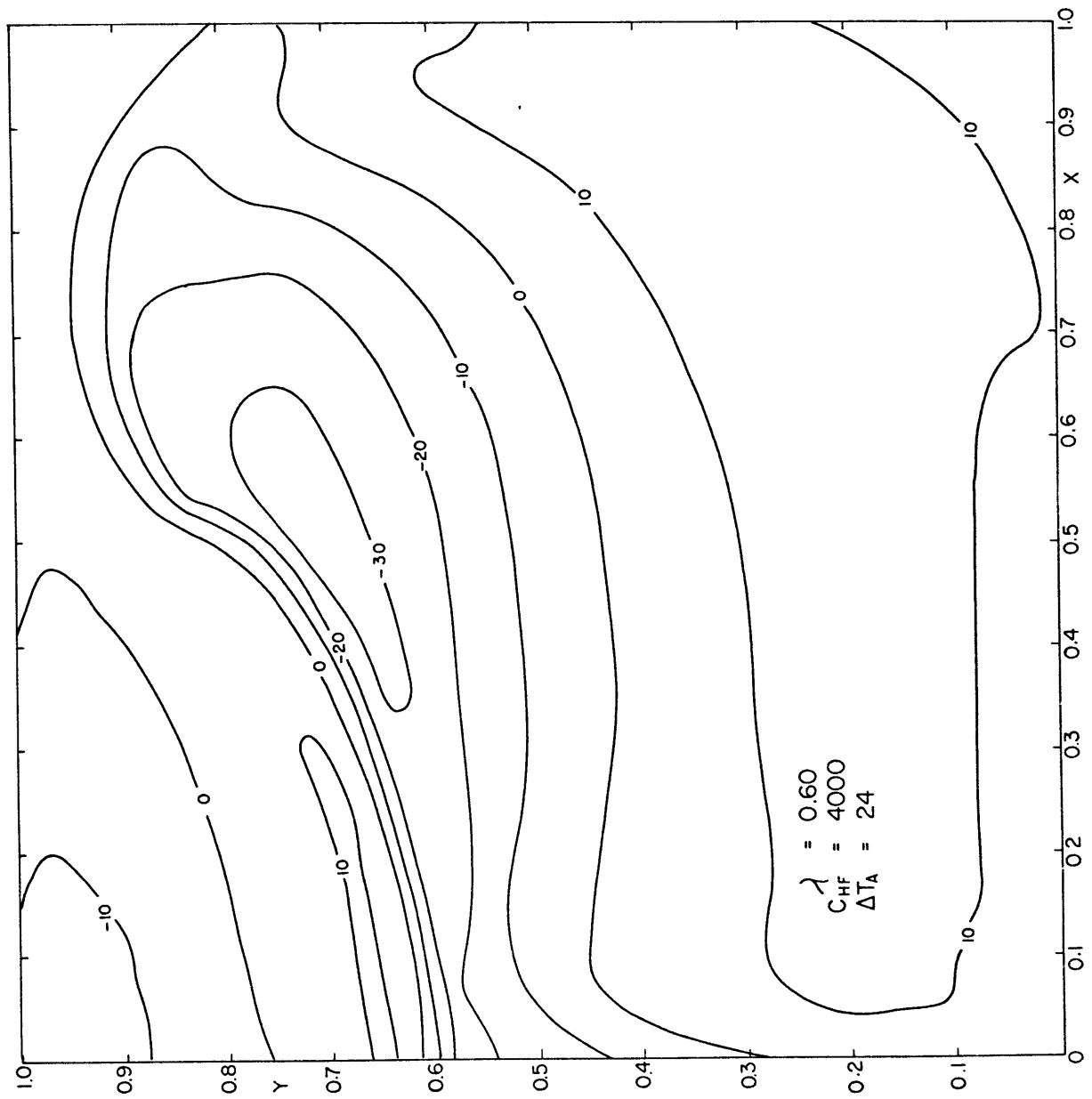


Fig. 11c. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{ yr}^{-1}$   
(Case 3)

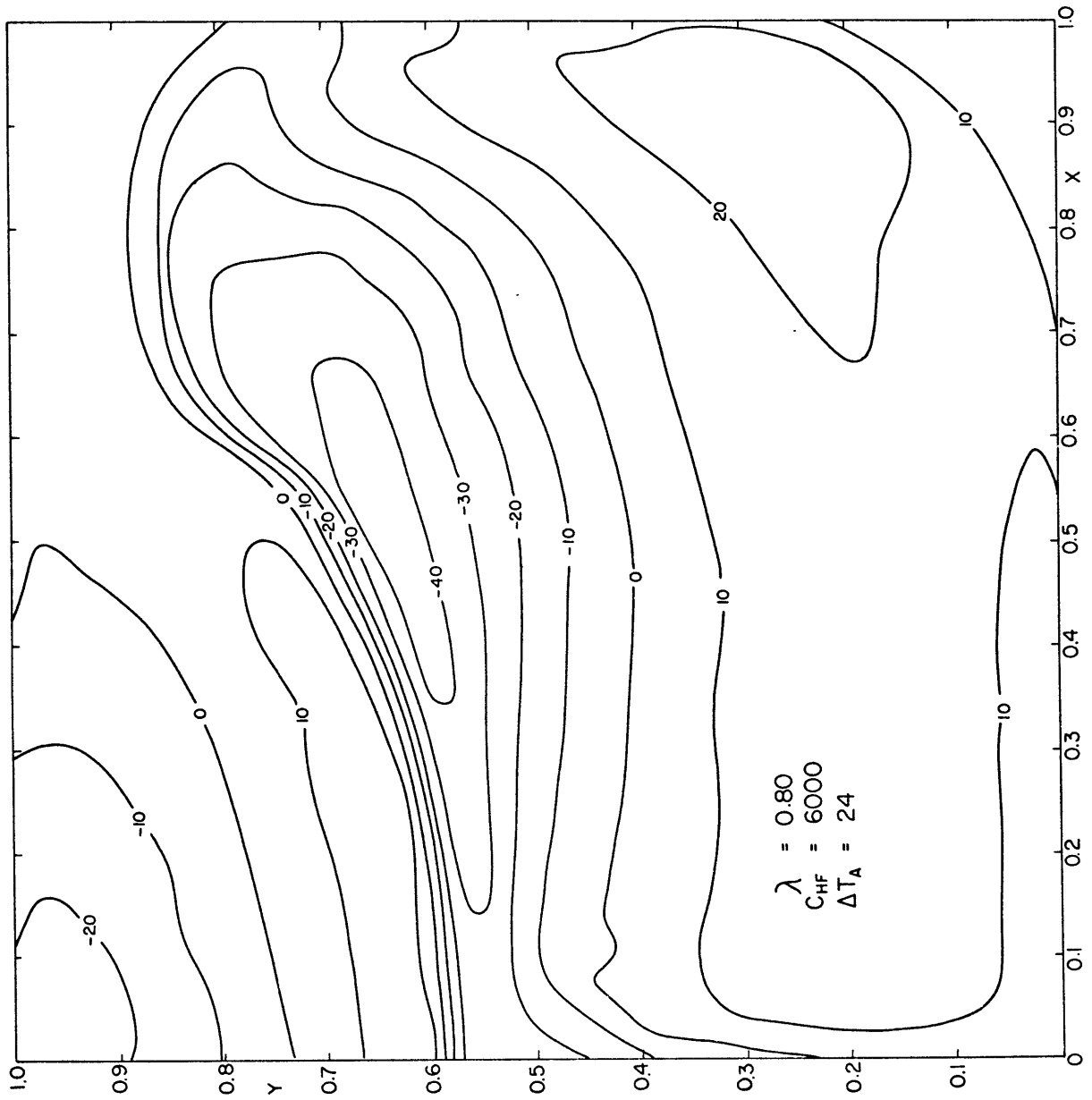


Fig. 11d. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$   
(Case 4)

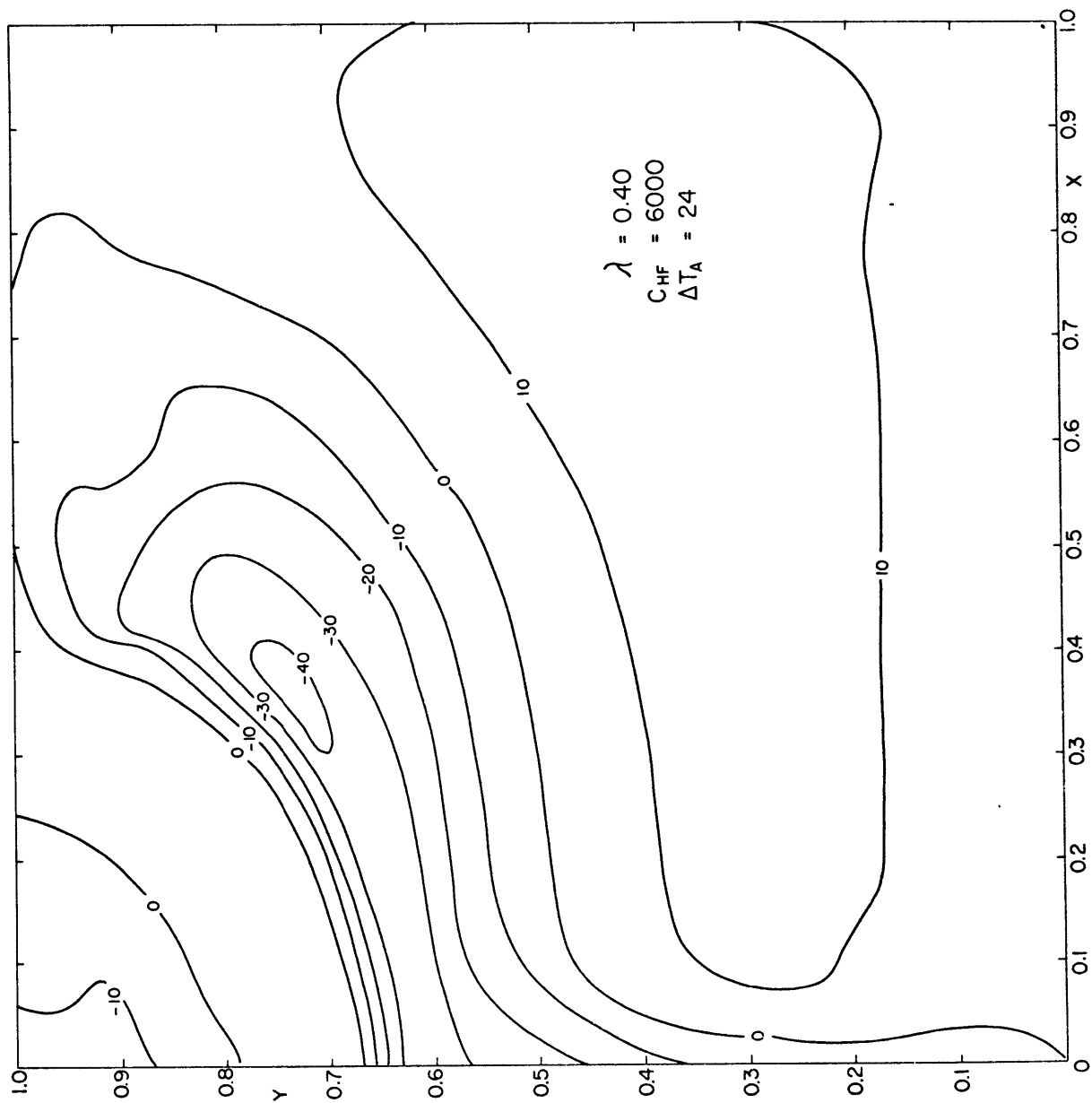


Fig. 11e. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$   
(Case 5)

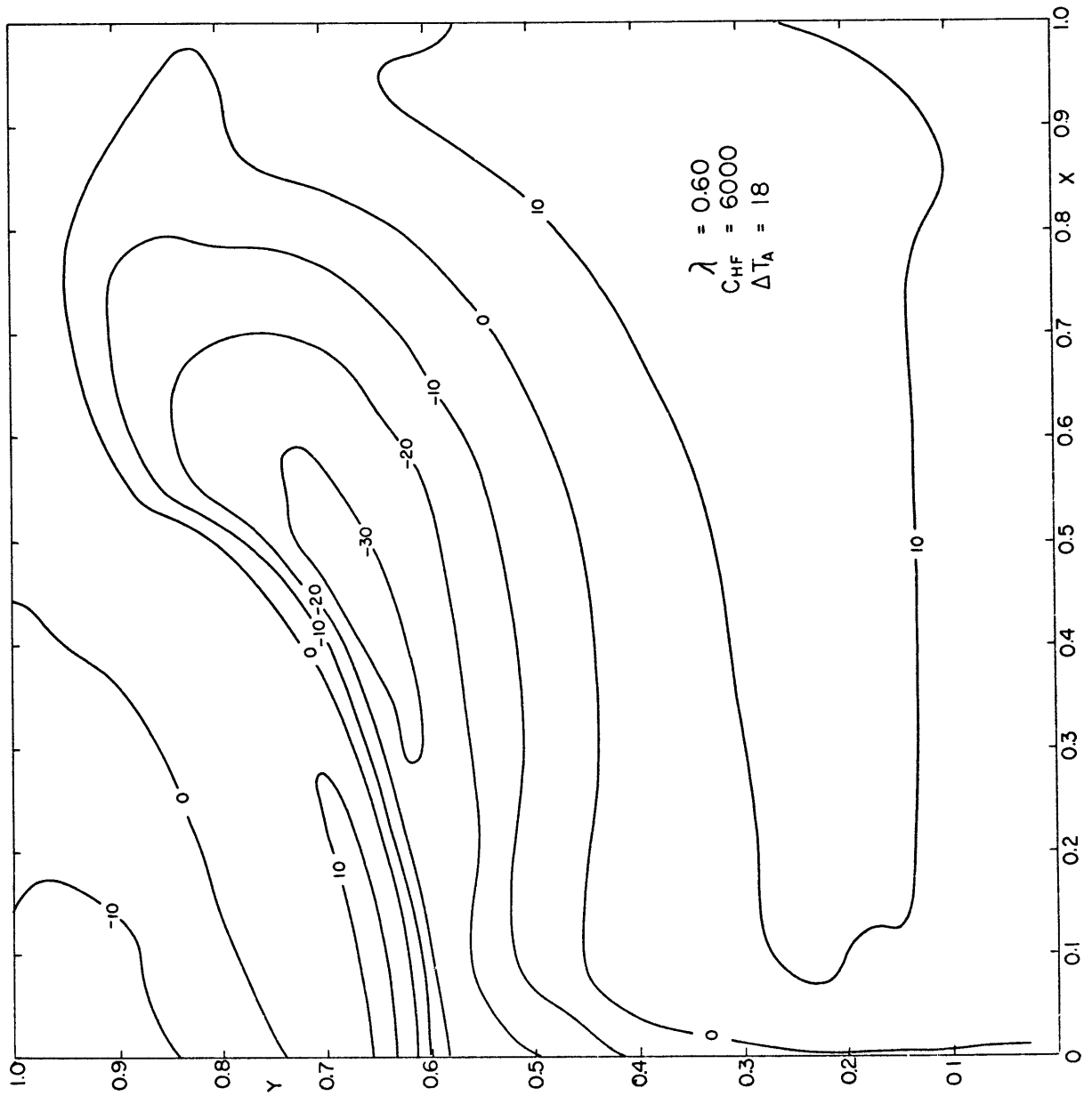


Fig. 11f. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$   
(Case 6)

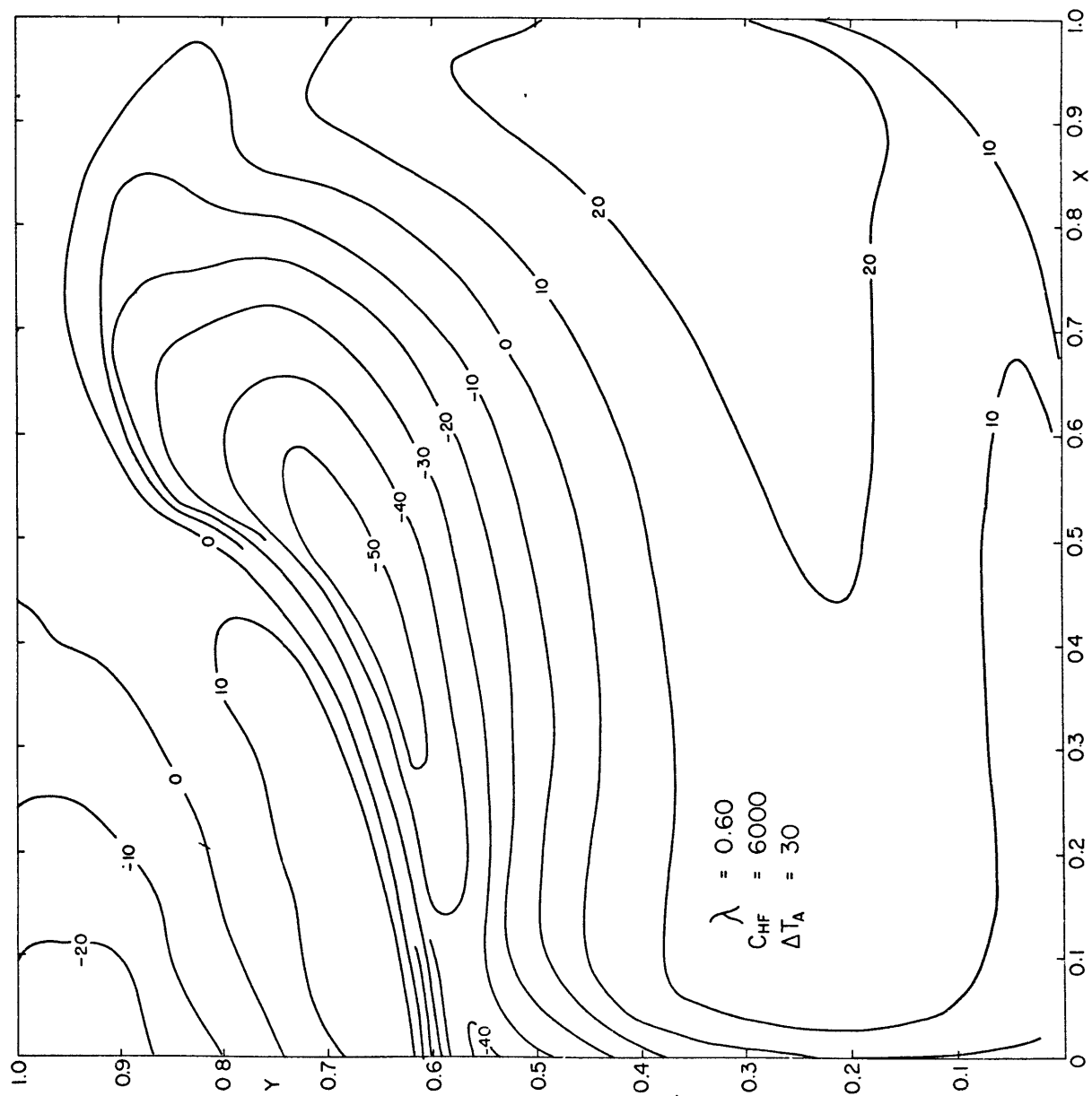


Fig. 11g. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$   
(Case 7)

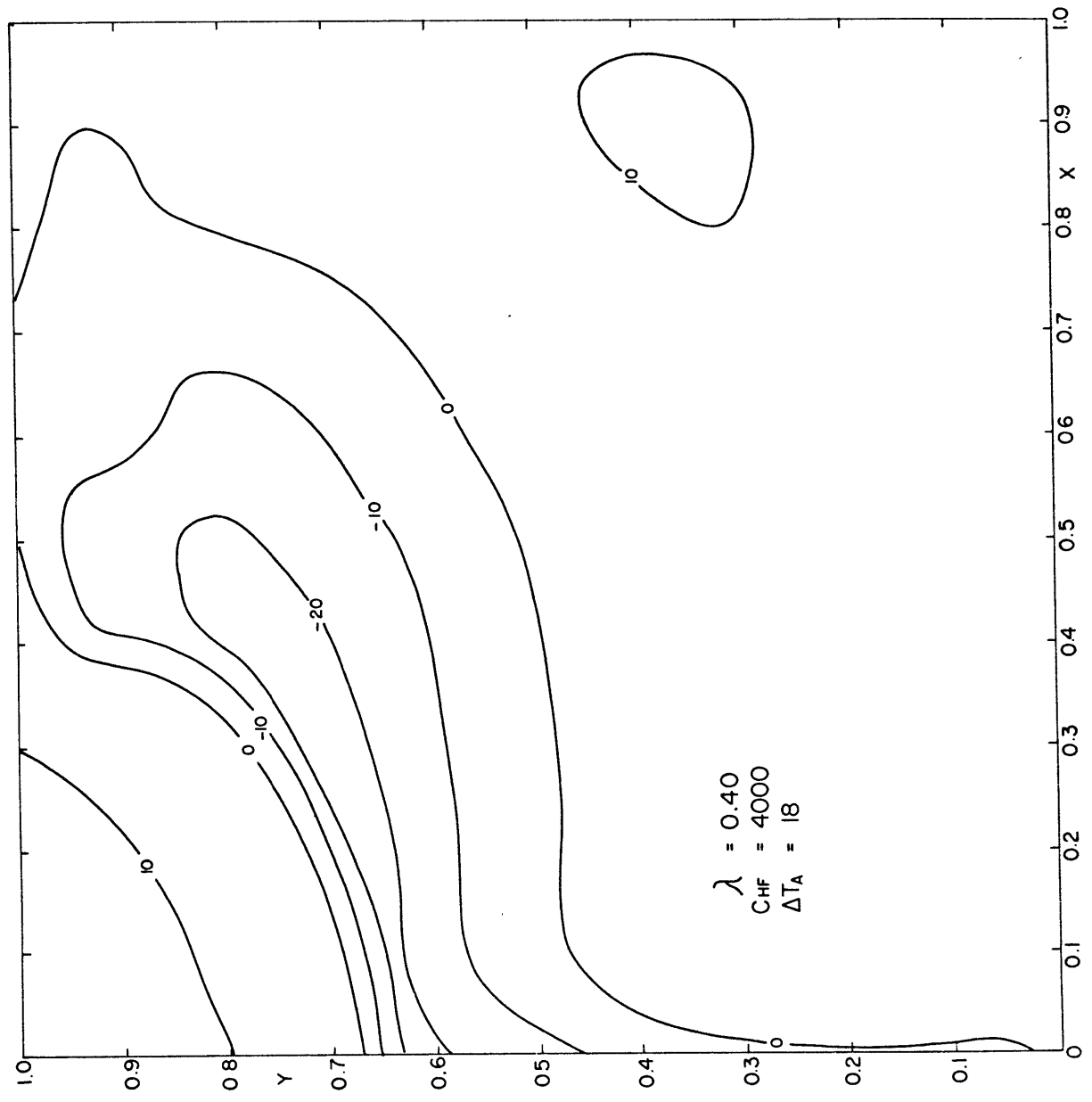


Fig. 11h. Equilibrium Vertical Heat Flux in kcal cm<sup>-2</sup> yr<sup>-1</sup> (Case 8)



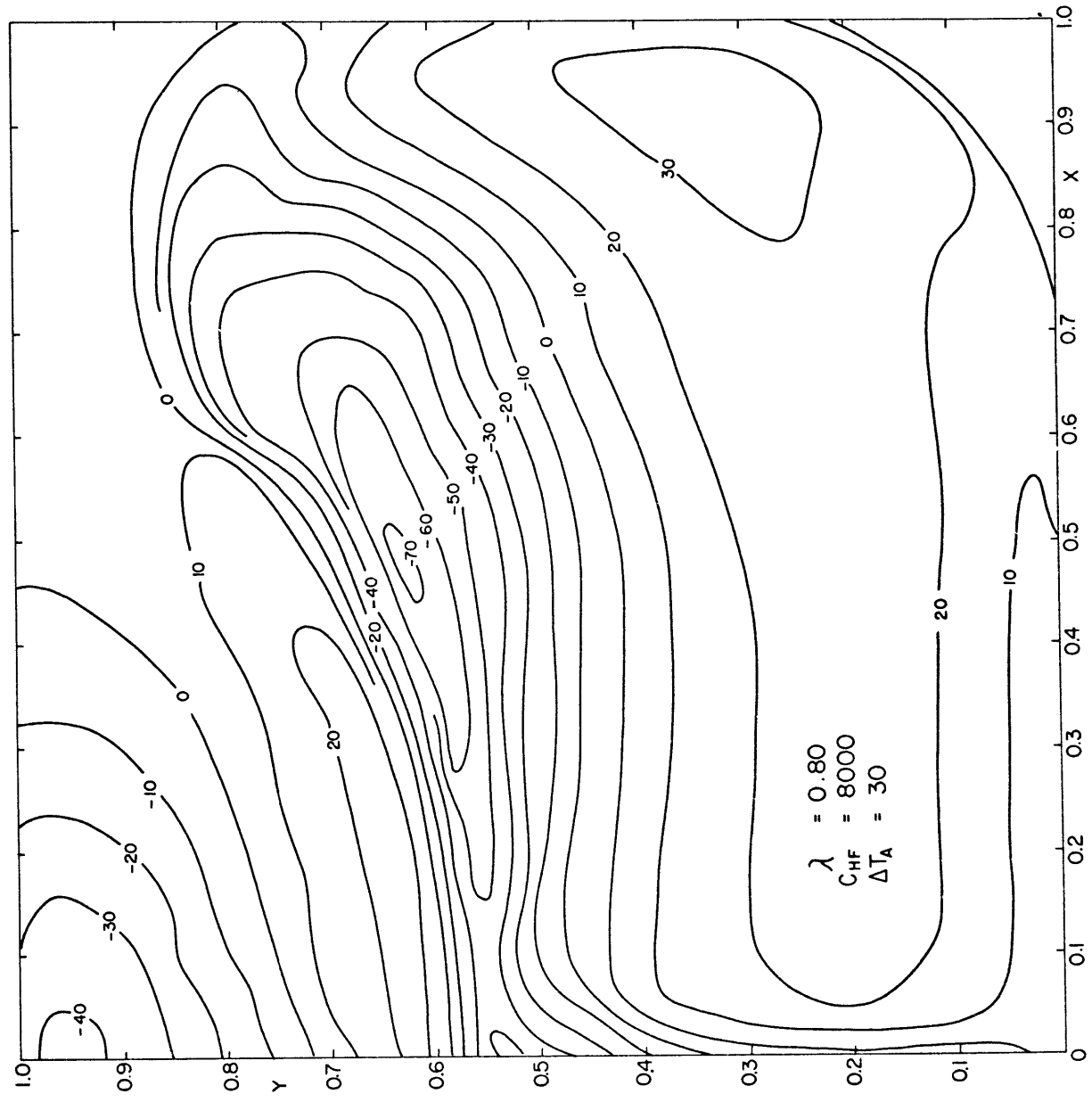


Fig. 11i. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$  (Case 9)

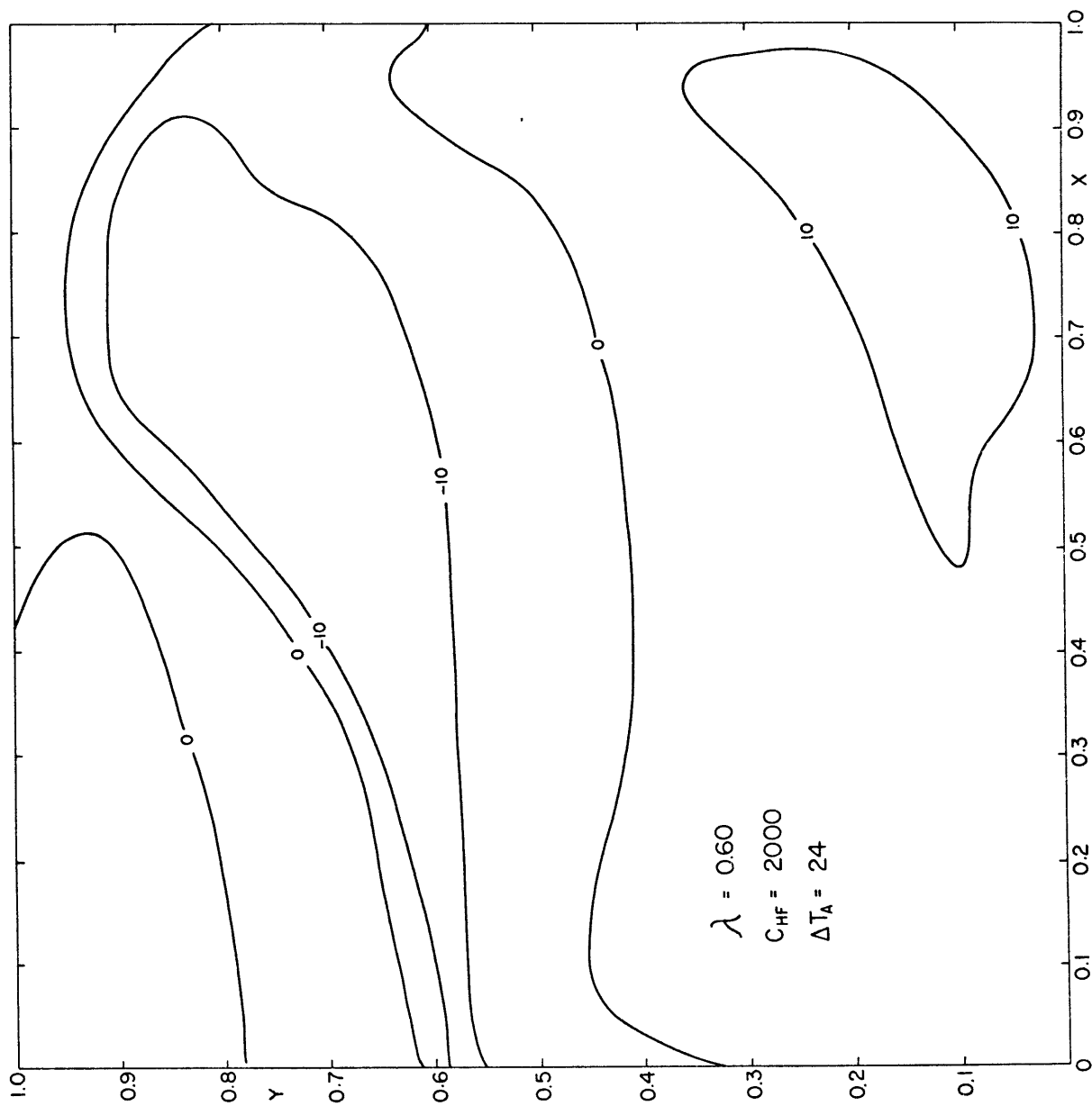


Fig. 11j. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{yr}^{-1}$   
(Case 10)

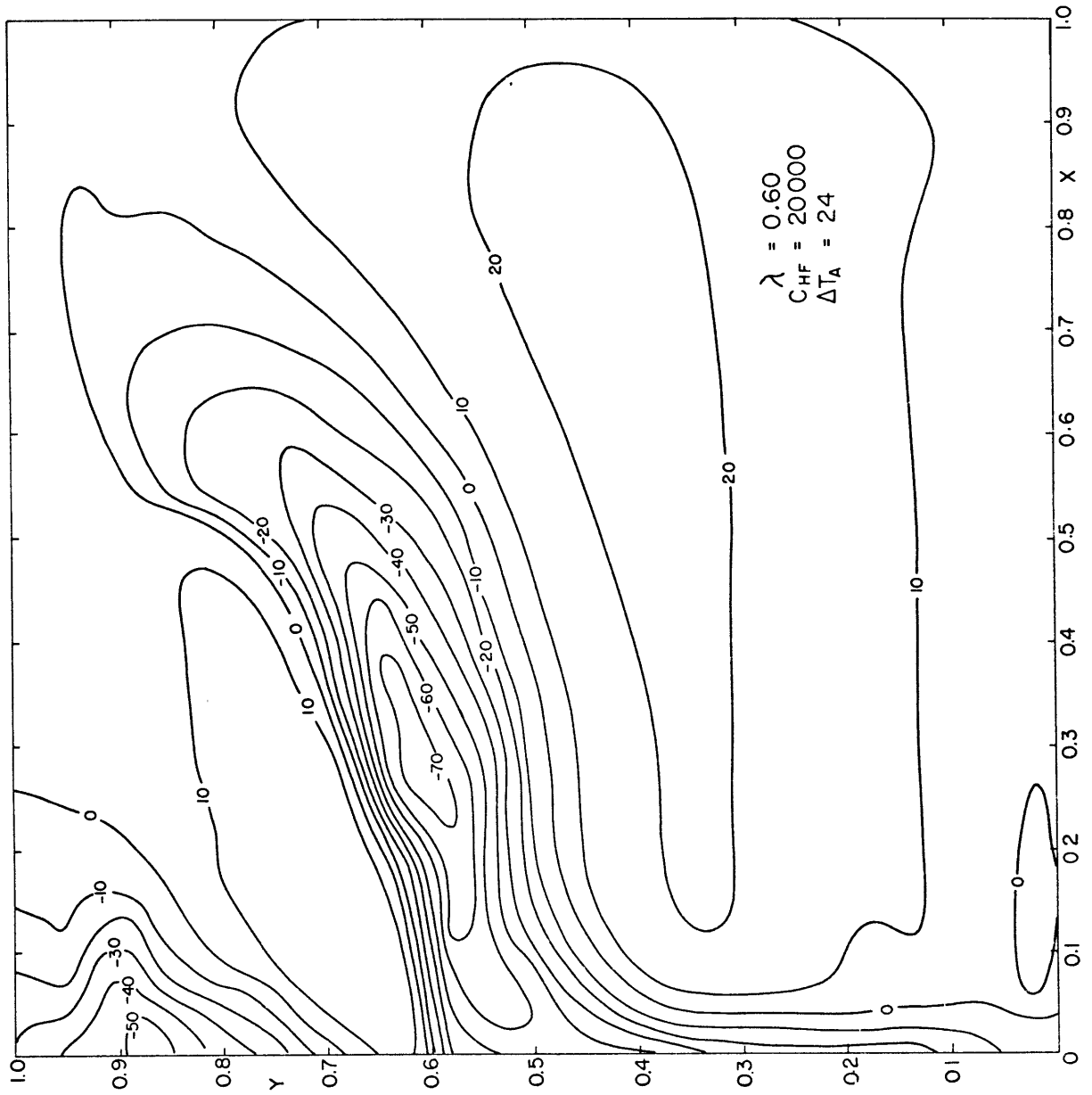


Fig. 11k. Equilibrium Vertical Heat Flux in  $\text{kcal cm}^{-2} \text{ yr}^{-1}$   
(Case 11)

used similar parameterizations for the vertical heat flux. The standard values for  $C_{HF}$  we used ( $4000 \text{ cal cm}^{-2} \text{ yr}^{-1} \text{ } ^\circ\text{C}^{-1} \leq C_{HF} \leq 8000 \text{ cal cm}^{-2} \text{ yr}^{-1} \text{ } ^\circ\text{C}^{-1}$ ) are within the range assumed in these studies and have the same percentage variation as our values of  $\lambda$ .

The equilibrium balance is between horizontal advection of heat and vertical transfers to the atmosphere. Comparing Figs. 8b and 9a, it is seen that in the southeastern half of the basin the equilibrium oceanic temperatures are quite reflective of the overlying atmospheric temperatures, with the pattern slightly shifted in the flow direction. In the remainder of the basin there is a significant deviation from the overlying temperatures as a consequence of the strong heat advection in the boundary currents.

On crossing the line of separation the sense of the heat advection reverses. This increases the intensity of the front which primarily develops in the upper layer due to the differential heat advection between the core of the boundary current and the slower moving water towards the line of separation.

Figs. 10a and 10b, taken from the U.S. Naval Oceanographic Atlas show sea surface temperatures in the North Atlantic for the month along the western boundary, and the predominantly zonal character of the isotherms in the central part of the basin. Fig. 9a compares less well with the August sea surface temperatures in Fig. 10b. The observed

predominantly zonal temperature gradient in the southeastern North Atlantic in summer cannot be likened to any feature in Fig. 9a.

Corresponding to the temperature distributions in Figs. 8b and 9a is the equilibrium vertical heat flux from the atmosphere to the ocean according to the linear heat flux law, given in Fig. 10a. In the vicinity of the boundary currents there is a strong heat flow to the atmosphere. In the majority of the basin there is a weak heat flow into the ocean. The distribution is similar to that of Fig. 12b from Bunker and Worthington (1976) which was calculated from climatological data using aerodynamic transport laws. Bunker and Worthington included the effects of atmospheric stability in their drag coefficients, greatly enhancing the vertical flux in the Gulf Stream region. We do not take stability into account. Budyko's (1963) distribution in Fig. 12a was derived with no consideration of stability. This helped to weaken the intense Gulf Stream feature in his results.

Figs. 9b, 9c and 11b, 11c show the effects of first increasing and then decreasing the heat flux constant. This effectively increases and then decreases the ratio of vertical transfers to advection. In the high constant case (Case 2), the temperatures in the ocean interior are more representative of the overlying atmospheric temperatures and the warm

water tongue has less of a northward penetration than in Case 3, the low constant case. The vertical heat fluxes are stronger in Case 2 than in Case 3 and the maximum is displaced slightly further upstream.

Cases 4 (Figs. 9d, 11d) and 5 (Figs. 9e, 11e) use higher and lower values of the wind stress parameter than the control. In these runs there are changes in the geometry as well as changes in the local ratio of vertical transfers to advection. The high wind stress case (Case 4) is characterized by a stronger warm water tongue which extends further to the north and east than in the low wind stress case (Case 5). The greater eastward penetration of the warm tongue is due to the more east-west orientation of the line of separation near the separation point in Case 4 coupled with the greater particle velocities. The equilibrium vertical fluxes are greater in magnitude in Case 4 and the area of negative values (heat transfer out of the ocean) is larger than in Case 5.

Cases 6 (Figs. 9f, 11f) and 7 (Figs. 9g, 11g) present results using the weak and strong gradient atmospheric temperature distributions. These cases are primarily shown for visual comparisons with other results. Because our thermodynamic equation is linear in the temperature, changing the gradient of temperature will only change the equilibrium temperature gradients and vertical heat fluxes by a proportionate amount.

Cases 8 (Figs. 9h, 11h) and 9 (Figs. 9i, 11i) are composite runs intended to explore the extreme behavior of the model with values of the parameters examined in isolation above. We combined the parameters which gave the highest and the lowest values of the equilibrium heat flux. With certain qualifications, these cases might be identified with perpetual summerlike (Case 8) and winterlike (Case 9) atmospheric conditions. In winter the stronger gradients and winds (greater  $\lambda$ ). These stronger atmospheric winds coupled with the decreased atmospheric gravitational stability due to the relatively warmer oceans would lead to stronger turbulent heat transfers at the air-sea interface (greater heat flux constant). Neglect of seasonal changes in oceanic heat storage capability might invalidate this argument.

Cases 8 and 9 do exhibit the smallest and the largest magnitudes of equilibrium vertical heat flux. If we compare Figs. 9h with 10b and 9i with 10a certain properties of the observed seasonal change in sea surface temperature do seem evident in the model results. Among these are the stronger overall gradient in winter and the larger meridional extent of isotherms on the eastern side (northeastern in the model).

As realistic values of the heat flux constant are somewhat difficult to determine, we present Cases 10 (Figs. 9j, 11j) and 11 (Figs. 9k, 11k) in which this parameter has been

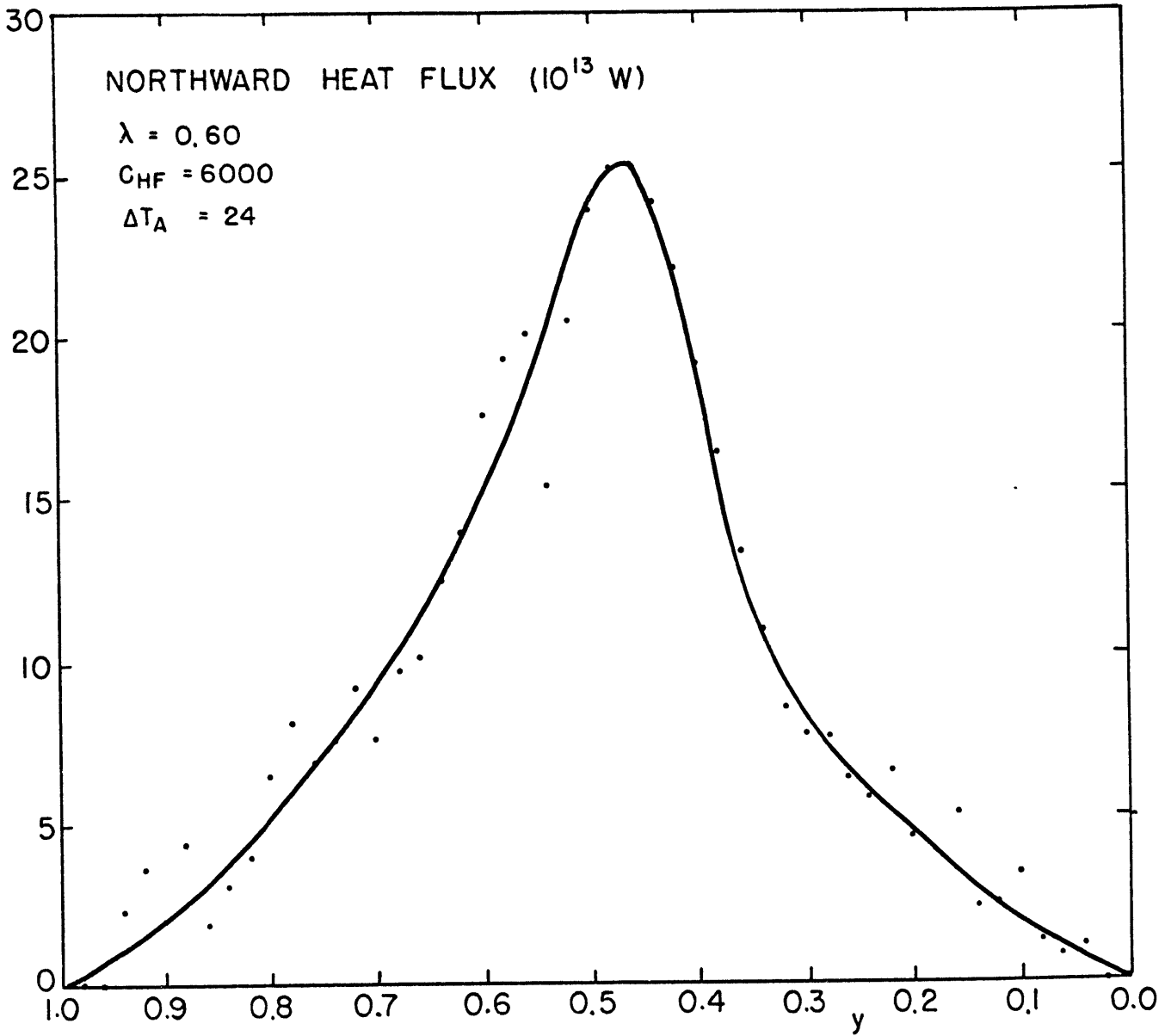
varied over a wider range than in Cases 2 and 3. For high  $C_{HF}$  the tongue of warm water is strongly suppressed. For low  $C_{HF}$  the isotherms on the eastern side of the basin have a large north-south extent.

Fig. 13 shows the northward flux of heat across a latitudinal wall in the basin for Case 1. The barriers at the furthest meridional extents of the basin force the heat flux to vanish there. The model values of the northward heat flux are of the same order of magnitude as present observational estimates for the world ocean (cf. Oort and Vonder Haar, 1976).

Fig. 14 shows the northward heat flux as a function of latitude and wind stress. In the active center region we see an interesting progressive change in the northward flux distribution as  $\lambda$  increases from 0.35 to 0.85. The north side of the peak becomes increasingly squeezed towards the center as the area of surfaced lower layer increases. The peak fluxes increase for low values of  $\lambda$  and then gradually decrease. Depending on the latitude and the value of  $\lambda$  an increase in the wind stress driving may lead to either an increase or a decrease in the oceanic heat flux. This has relevance to the feedback in the atmosphere-ocean dynamical system in which changes in oceanic heat transports due to changes in wind driving modify the energy supply for the atmospheric circulation. Fig. 14 shows that for our model this feedback has both positive and negative values



Fig. 13. Equilibrium Northward Heat Flux vs. Latitude for Case 1.



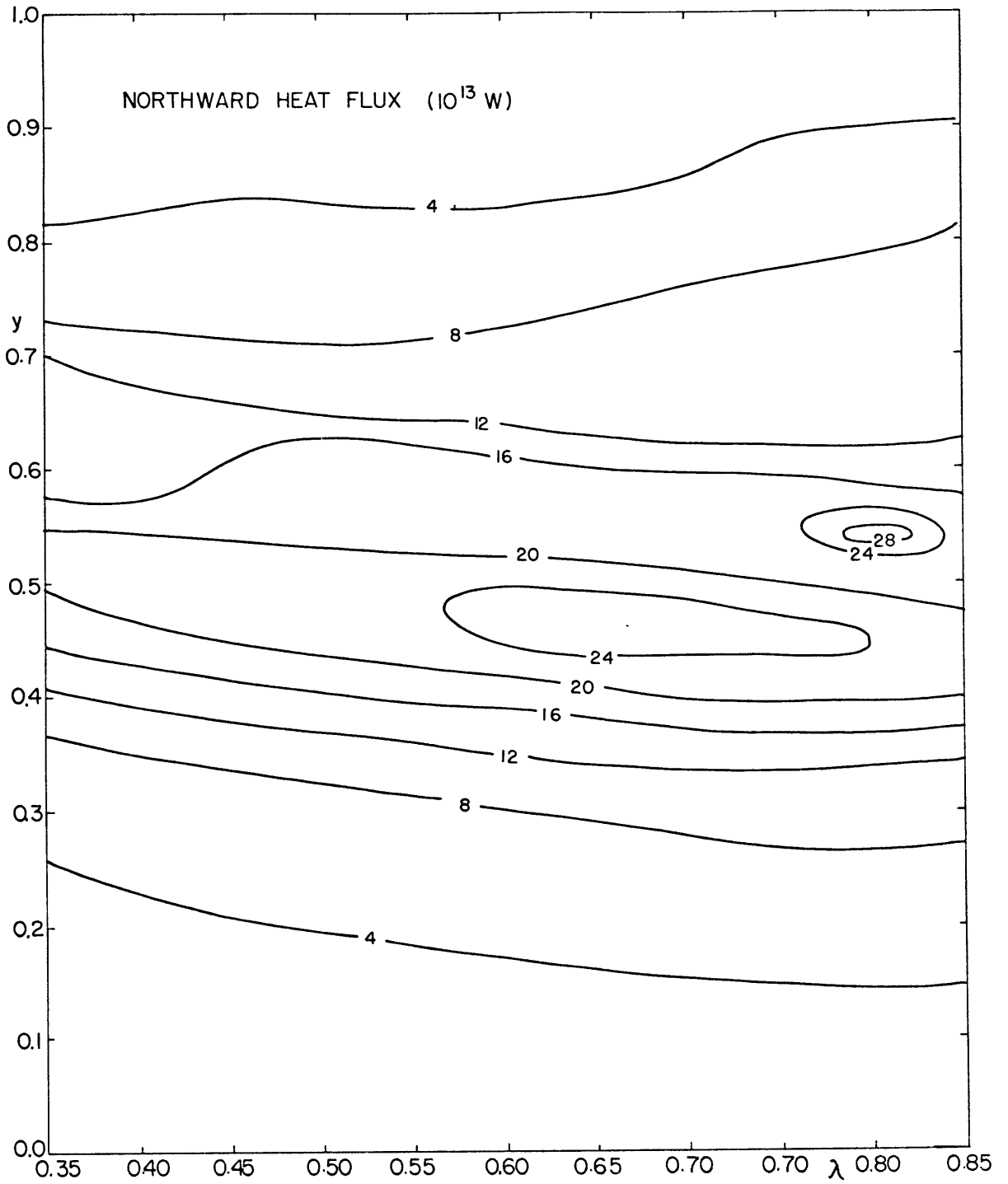


Fig. 14. Equilibrium Northward Heat Flux vs. latitude and  $\lambda$

in different regions of parameter space.

We have also tested the sensitivity of the northward heat flux to the heat flux constant and meridional temperature gradient. Fig. 15 shows the northward flux as a function of  $y$  and  $C_{HF}$ . For the values of  $C_{HF}$  chosen the northward flux increases with  $C_{HF}$ . As  $C_{HF}$  becomes very large (outside of the range of values presented) the ocean temperatures approach the atmospheric temperatures and for our zonally uniform distribution of atmospheric temperatures the northward flux goes to zero. Fig. 16 gives the northward flux as a function of  $y$  and  $\Delta T_A$ . There is a linear increase in the flux with  $\Delta T_A$  due to the linear nature of the thermodynamic equation.

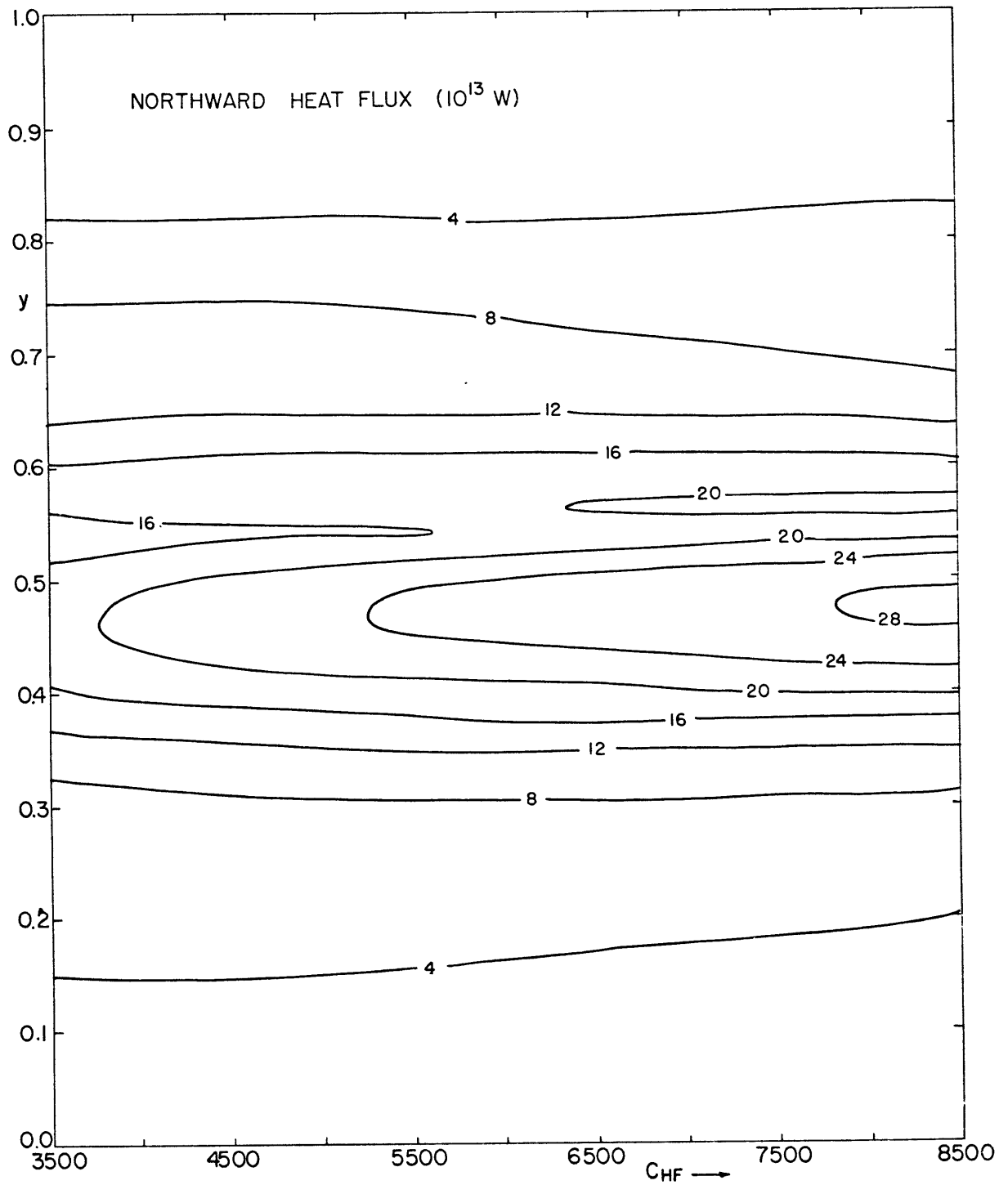


Fig. 15. Equilibrium Northward Heat Flux vs. latitude and  $C_{HF}$

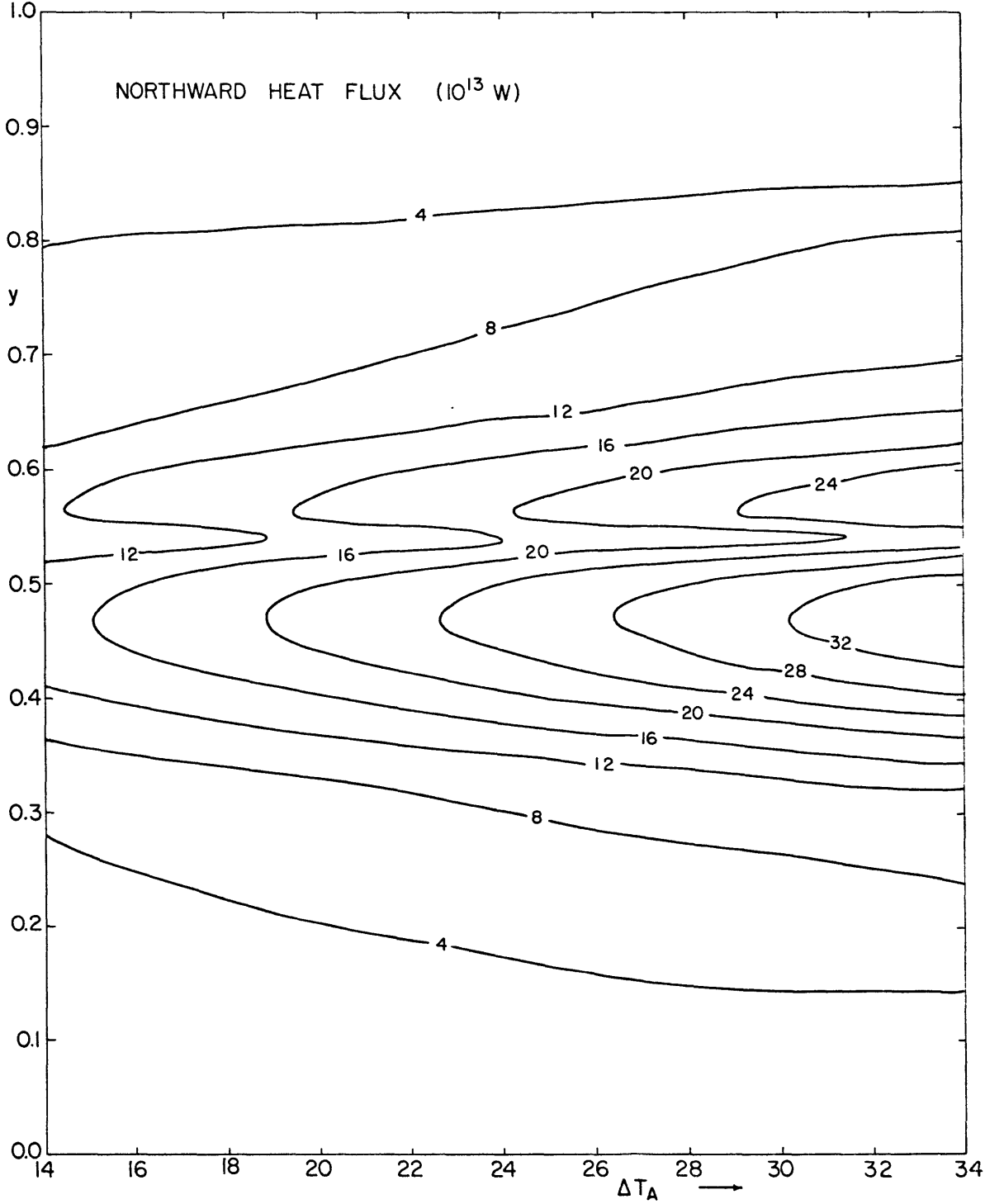


Fig. 16. Equilibrium Northward Heat Flux vs. latitude and  $\Delta T_A$

## V. Conclusions

We have presented results from a simple model of air-sea interaction. Atmospheric boundary conditions for the ocean model were idealized and held fixed. The large-scale steady-state ocean circulation was calculated. A Lagrangian temperature integration was performed to find the steady-state temperatures of the ocean surface layer. Vertical and northward heat fluxes were calculated.

Significant qualitative agreement was found between calculated results and observations, particularly in the general patterns of the oceanic temperature and the vertical heat flux. The sensitivity of the model results to the external conditions was tested and perpetual seasons were simulated. The dependence of the model heat flux on the wind stress was examined. A large number of figures is presented to allow extensive visual intercomparisons of model results.

The major value of a study of this type would seem to be the insight it provides for understanding the basic processes involved in large-scale air-sea interaction. We have assumed a thermal balance of horizontal heat advection being counteracted by vertical heat transfers. The qualitative agreement between the observed ocean temperatures and air-sea heat fluxes and the model results suggests that the major processes active have been sufficiently well

represented to give correct general patterns. We suggest that the seasonal variations in the North Atlantic sea-surface temperatures are due primarily to suppressed vertical heat fluxes in summer due to increased stability. For the Atlantic it seems clear that dynamic processes are equally as important as vertical heat transfers at the air-sea interface in determining the equilibrium sea surface temperature patterns.

The variation of the model northward heat flux with changes in the wind stress parameter suggest that, although this is generally the case, there may not always be a negative feedback between atmospheric wind driving of the surface ocean circulation and resultant effects of heat transports by these circulations on the atmospheric baroclinicity. Strong enough driving of the ocean leads to homogenization of the sea surface temperatures and reduction of the northward heat transports despite stronger circulations.

This study leaves many questions unanswered due to the extreme crudeness of the model. More sophisticated treatments of oceanic heat storage and turbulent transfer between the ocean and the atmosphere are needed to verify the results even within this very limited-interaction framework.

## APPENDIX

## SOLUTIONS TO MODEL CIRCULATION EQUATIONS

$$\gamma = (\tau, 0) \quad \gamma = -\cos(\pi y)$$

## A. Interior - Upper Layer

$$\psi = \lambda(1-x)\tau_y \quad (1)$$

$$D^2 = h^2 + 2\lambda(1-x)f^2(\tau/f)_y \quad (2)$$

## B. Western Boundary Layer - Upper Layer

$$D = D_0(1 - Be^{-\eta}) / (1 + Be^{-\eta}) \quad (1) \quad B = (D_1 - D_0) / (D_1 + D_0)$$

$$\psi = (D^2 - D_0^2) / 2f \quad (2) \quad \eta = \frac{\lambda D_1}{\epsilon}, \quad D_0^2 = h^2 - 2\lambda\tau, \quad D_1^2 = h^2 + 2\lambda f^2 \left(\frac{\tau}{f}\right)_y$$

## C. Separated Boundary Layer - Upper Layer

$$\text{Line of Surfacing } x = X(y) = 1 - \frac{h^2}{2\lambda\tau} \quad (1) \quad D_1^2 = \frac{h^2 f \tau_y}{\tau} \quad (2)$$

$$D = D_0(1 - e^{-\eta}) / (1 + e^{-\eta}) \quad (3) \quad \eta = \frac{\lambda f_s D_1}{\epsilon} \quad \psi = \frac{D^2}{2f} \quad (4) \quad f_s = \text{gradient of } f \text{ along line of separation}$$

## D. Interior - Lower Layer

$$\psi' = \lambda' \tau_y (X - x) \quad (1)$$

$$D'^2 = h'^2 + 2\lambda'(X - x)f^2(\tau/f)_y \quad (2)$$

$$D_1'^2 = h'^2 + 2\lambda' f^2 (\tau/f)_y X$$

## E. Western Boundary Layer - Lower Layer

$$D' = D'_0(1 - B'e^{-\eta'}) / (1 + B'e^{-\eta'}) \quad (1)$$

$$\eta' = \frac{\lambda' D'_1}{\epsilon'}$$

$$B' = (D'_1 - D'_0) / (D'_1 + D'_0)$$

$$\psi' = (D'^2 - D_0'^2) / 2f \quad (2)$$

$$D_0'^2 = h'^2 - 2\lambda'\tau X$$



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