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Non-Linear Monte-Carlo Search in Civilization II

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Abstract

This paper presents a new Monte-Carlo search algorithm for very large sequential decision-making problems. We apply non-linear regression within Monte-Carlo search, online, to estimate a state-action value function from the outcomes of random roll-outs. This value function generalizes between related states and actions, and can therefore provide more accurate evaluations after fewer roll-outs. A further significant advantage of this approach is its ability to automatically extract and leverage domain knowledge from external sources such as game manuals. We apply our algorithm to the game of Civilization II, a challenging multi-agent strategy game with an enormous state space and around $10^{21}$ joint actions. We approximate the value function by a neural network, augmented by linguistic knowledge that is extracted automatically from the official game manual. We show that this non-linear value function is significantly more efficient than a linear value function, which is itself more efficient than Monte-Carlo tree search. Our non-linear Monte-Carlo search wins over 78% of games against the built-in AI of Civilization II. 1

1 Introduction

Monte-Carlo search is a simulation-based search paradigm that has been successfully applied to complex games such as Go, Poker, Scrabble, multi-player card games, and real-time strategy games, among others [Gelly et al., 2006; Tesauro and Galperin, 1996; Billings et al., 1999; Sheppard, 2002; Schäfer, 2008; Sturtevant, 2008; Balla and Fern, 2009]. In this framework, the values of game states and actions are estimated by the mean outcome of roll-outs, i.e., simulated games. These values are used to guide the selection of the best action. However, in complex games such as Civilization II, the extremely large action space makes simple Monte-Carlo search impractical, as prohibitively many roll-outs are needed to determine the best action. To achieve good performance in such domains, it is crucial to generalize from the outcome of roll-outs to the values of other states and actions.

Several factors influence a city's production of shields: the terrain within your city radius is most important.

You might find it worthwhile to set Settlers to improving the terrain squares within your city radius.

Beyond terrain, the form of government your civilization chooses can cause each city to spend some of its raw materials as maintenance.

1The code and data for this work are available from http://groups.csail.mit.edu/rbg/code/civ/
that the action *irrigate-land* should be selected if the words “improve terrain” are present in text. However, the challenge in using such information is in identifying which segments of text are relevant for the current game context; for example, the system needs to identify the second sentence in Figure 1 as advice pertinent to the irrigation action. These decisions can be effectively modeled via hidden variables in a non-linear VFA.

We model our non-linear VFA using a four-layer neural network, and estimate its parameters via reinforcement learning within the Monte-Carlo search framework. The first layer of this network represents features of the game state, action, and the game manual. The second layer represents a linguistic model of the game manual, which encodes sentence relevance and the predicate structure of sentences. The third layer corresponds to a set of fixed features which perform simple, predefined transformations on the outputs of the first two layers. The fourth and final layer represents the value function. During Monte-Carlo search, the roll-out scores are used to train the entire value function online, including the linguistic model. The weights of the neural network are updated by error backpropagation, so as to minimize the mean squared error between the value function (the network output) and the roll-out scores.

We apply our technique to Civilization II, a notoriously large and challenging game. It is a cooperative, multi-agent decision-making problem with around $10^{21}$ joint actions and an enormous state space of over $10^{188}$ states. To make the game tractable, we assume that actions of agents are independent of each other given the game state. We use the official game manual as a source of domain knowledge in natural language form, and demonstrate a significant boost to the performance of our non-linear Monte-Carlo search. In full-length games, our method wins over 78% of games against the built-in, hand-crafted AI of Civilization II.

2 Related Work

Monte-Carlo search has previously been combined with *global* non-linear VFA. The original TD-Gammon [Tesauro, 1994] used a multilayer neural network that was trained from games of self-play to approximate the value function. Tesauro and Galperin [1996] subsequently used TD-Gammon’s neural network to score the roll-outs in a simple Monte-Carlo search algorithm; however, the neural network was not adjusted online from these roll-outs. In contrast, our algorithm re-learns its value function, online, from each new set of roll-outs – just as if TD-Gammon had re-trained its neural network after each move, specifically for the subgame of Backgammon starting from that new position.

Monte-Carlo search has previously been extended to the special case of linear VFA [Silver et al., 2008]. Generalizing to non-linear VFA provides two fundamental advantages.

Firstly, due to its greater representational power, it generalizes better from small numbers of roll-outs. This is particularly important in complex games, such as Civilization II, in which simulation is computationally intensive, severely limiting the number of roll-outs. Secondly, non-linear VFA allows for multi-layered representations, such as neural networks, which can automatically learn features of the game state. Furthermore, we show that a multi-layered, non-linear VFA can automatically incorporate domain knowledge from natural language documents, so as to produce better features of the game state, and therefore a better value function and better overall performance.

A number of other approaches have previously been applied to turn-based strategy games [Amato and Shani, 2010; Wender and Watson, 2008; Bergsma and Spronck, 2008; Madeira et al., 2006; Balla and Fern, 2009]. However, given the enormous state and action space in most strategy games, much of this previous work has focused on smaller, simplified or limited components of the game. For example, Amato and Shani [2010] use reinforcement learning to dynamically select between two hard-coded strategies in the game Civilization IV. Wender and Watson [2008] focus on city building in Civilization IV. Madeira et al. [2006] address only the combat aspect of strategy games, learning high-level strategies, and using hard-coded algorithms for low-level control. Balla and Fern [2009] apply Monte-Carlo tree search with some success, but focus only on a tactical assault planning task. In contrast to such previous work, our algorithm learns to control *all* aspects of the game Civilization II, and significantly outperforms the hand-engineered, built-in AI player.

3 Background

Our task is to play and win a strategy game against a given opponent. Formally, we represent the game as a Markov Decision Process (MDP) $(S, A, T, R)$, where $S$ is the set of possible states and $A$ is the space of legal actions. Each state $s \in S$ represents a complete configuration of the game world, including attributes such as available resources and the locations of cities and units. Each action $a \in A$ represents a joint assignment of actions to each city and each unit. At each step of the game, the agent executes an action $a$ in state $s$, which changes the state to $s'$ according to the state transition distribution $T(s'|s, a)$. This distribution incorporates both the opponent’s action selection policy, and the game rules. It is not known explicitly; however, state transitions can be sampled by invoking the game code as a black-box simulator. Each state $s$ has a reward $R(s) \in \mathbb{R}$ associated with it, also provided implicitly by the game code.

A policy $\pi(s, a)$ is a stochastic action selection strategy that gives the probability of selecting action $a$ in state $s$. The *action-value function* $Q^\pi(s, a)$ is the expected final reward after executing action $a$ in state $s$ and then following policy $\pi$. In large MDPs, it is impractical to represent action-values by table-lookup, with a distinct value for every state and action. In such cases, the action-values can be represented by value function approximation – i.e., $Q(s, a) = f(s, a; \theta)$, where $f$ is a differentiable function with parameter vector $\theta$. These parameters can be updated by applying non-linear regression

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2Civilization II was placed #3 in IGN’s 2007 list of the top 100 video games of all time (http://top100.ign.com/2007)

3These measures of the state and action spaces are empirical estimates from our experimental setup. They are based on the average number of units, available unit actions, state attributes and the observed state attribute values.
to the final utilities. Specifically, the parameters are adjusted by gradient descent to minimize the mean-squared error between the action-value and the reward $R(s_t)$ at final state $s_t$ for every observed state $s$ and action $a$.

$$\Delta \theta = -\frac{\alpha}{2} \nabla_{\theta} [R(s_t) - Q(s, a)]^2$$
$$= \alpha [R(s_t) - Q(s, a)] \nabla_{\theta} f(s, a; \theta)$$

(1)

Monte-Carlo Search
Monte-Carlo search is a simulation-based search paradigm for dynamically estimating the action-values from a root state $s_t$. This estimate is based on the results of multiple roll-outs, each of which samples the final reward in a simulated game that starts from $s_t$. Specifically, in each roll-out, actions are selected according to a simulation policy $\pi_t$, and state transitions are sampled from the transition distribution $T$. At the end of the simulation, the reward $R(s_t)$ at the final state $s_t$ is measured, and the action-value function is updated accordingly. As in Monte-Carlo control [Sutton and Barto, 1998], the simulation policy may then be improved, to take account of this new information and direct the simulations towards the highest scoring regions of the state space. After $n$ simulations have been executed, the actual action with highest final reward is selected and played, and a new search begins from root state $s_{t+1}$.

Monte-Carlo tree search (MCTS) [Coulom, 2006] uses a search tree to represent the action-value function. Each node of the search tree contains a single value for the state corresponding to that node. Each simulation traverses the search tree without backtracking. After each simulation, the action-values of all traversed nodes are updated to reflect the new mean reward. If all nodes of the search tree are expanded, this algorithm is equivalent to Monte-Carlo control with table-lookup, applied to the subgame starting from $s_t$. Monte-Carlo tree search has achieved human master-level performance in $9 \times 9$ Go [Gelly et al., 2006].

In linear Monte-Carlo search [Silver et al., 2008] the value function is represented by a linear combination of features $\phi(s, a)$ and a parameter vector $\theta$: $Q(s, a) = \theta \cdot \phi(s, a)$. The parameters are updated by applying online linear regression to the final simulation utilities via gradient descent: $\Delta \theta = \alpha [R(s_t) - Q(s, a)] \phi(s, a)$. This algorithm is equivalent to Monte-Carlo control with linear function approximation [Sutton and Barto, 1998], again applied to the subgame starting from $s_t$. Often, a linear approximation that is specialized to the current subgame can be much more accurate than a global linear approximation; it outperforms a simple Monte-Carlo tree search in $9 \times 9$ Go [Silver et al., 2008].

4 Non-linear Monte-Carlo Search
Non-linear Monte-Carlo search combines Monte-Carlo search with non-linear VFA. The value function is represented by an arbitrary, smooth function approximator. At the end of each roll-out, the parameters of the function approximator are updated online by Equation 1. This produces a non-linear approximation to the current roll-out scores, specialized to the subgame starting from $s_t$. As in other Monte-Carlo search algorithms, the value function is used to improve the simulation policy and guide roll-outs towards the highest reward regions of the search space.

We now describe our approach to non-linear VFA which can be applied effectively in the context of Monte-Carlo search. We represent the action-value function by the output of a multi-layer neural network. The architecture of this network incorporates a linguistic model that is designed to automatically extract and incorporate domain knowledge from game manuals.

Incorporating Text into MC Search
Consider the text shown in Figure 1, which suggests that within your city radius “settlers” should take the action “improve the terrain.” One way to incorporate this kind of textual information is to enrich the action-value function with word features in addition to state and action features. However, adding all the words from a manual is unlikely to help, since only a small portion of the document is likely to be relevant for a given state (see Figure 2). Therefore, the linguistic model needs to identify the most relevant text segment for each state. Moreover, even when the relevant sentence is known, it is important to discriminate between words that describe actions from words that describe state (see Figure 3).

Rather than flooding the representation with all possible text features, we automatically extract, from a natural language document, the feature vector that is most effective in predicting the roll-out rewards. We learn these text features jointly with the action-value function approximation, where both processes are guided by backpropagation of error.

Network Architecture
As shown in Figure 4, our architecture is a four layer neural network. The input layer $\vec{x}$ consists of deterministic, real-valued features $\vec{x}(s_t, a_t, d)$ of the current game state $s_t$, candidate action $a_t$, and document $d$.

The second layer consists of two sets of disjoint units $\vec{y}$ and $\vec{z}$ which encode the sentence-relevance and predicate-labeling decisions respectively. These sets of units operate as stochas-
Figure 4: The structure of our network architecture. Each rectangle represents a collection of units in a layer, and the shaded trapezoids show the connections between layers. A fixed, real-valued feature function \( \mathbf{x}(s, a, d) \) transforms the game state \( s \), action \( a \), and strategy document \( d \) into the input vector \( \mathbf{x} \). The first hidden layer contains two disjoint sets of units \( \mathbf{y} \) and \( \mathbf{z} \) corresponding to linguistic analyses of the strategy document. These are softmax layers, where only one unit is active at any time. The units of the second hidden layer \( \mathbf{f}(s, a, d, y_i, z_j) \) are a set of fixed real valued feature functions on \( s, a, d \) and the active units \( y_i \) and \( z_j \) of \( \mathbf{y} \) and \( \mathbf{z} \) respectively.

The information from these roll-outs is used to select the actual game action. The algorithm re-learns the function approximation for every new game state \( s_t \). This specializes the action-value function to the subgame starting from \( s_t \).

As described in Section 3, we estimate the neural network parameters via gradient descent to minimize the mean-squared error of our function approximation. We perform this minimization by standard error backpropagation, which results in the following online updates for the output layer parameters \( \mathbf{w} \):

\[
\mathbf{w} \leftarrow \mathbf{w} + \alpha_u \left[ Q - R(s_t) \right] \mathbf{f}(s, a, d, y_i, z_j),
\]

where \( \alpha_u \) is a learning rate, and \( Q = Q(s, a, d) \). The corresponding updates for the softmax layer parameters \( \mathbf{u} \) are:

\[
\mathbf{u}_i \leftarrow \mathbf{u}_i + \alpha_u \left[ Q - R(s_t) \right] \mathbf{x} \left( 1 - \mathbf{p}(y_i | \mathbf{x}) \right).
\]

5 Application to Civilization II

We apply our non-linear Monte-Carlo search algorithm to the game of Civilization II, using the official game manual\(^6\) as the source of domain knowledge. Civilization II is a multi-player turn-based strategy game. Each grid location on the map is a tile of either land or sea, and each tile can have multiple terrain and resource attributes—as for example hills, rivers, or coal deposits. Each player in the game controls a civilization consisting of multiple cities and units such as workers, explorers and archers. The player who gains control of the entire world by capturing or destroying all opposing cities and units wins the game.\(^7\) We test our algorithms on the small size two-player game, which is set in a 1000 square map, and we play our algorithm against the built-in AI player.\(^8\)

Strategy documents We use the official game manual of Civilization II as our source of domain knowledge, which contains 2083 sentences of average length 17 words, and has a large vocabulary of 3638 words. We use the Stanford parser [de Marneffe et al., 2006] to generate the dependency parse information for the sentences of this document.

States and Actions We define the game state to be the attributes of each tile in the world map, and the attributes of each player’s civilization, cities and units. The set of legal actions for each civilization, city and unit is state dependent and is defined by the rules. In a 1000 tile Civilization II game, there are 10\(^{21}\) joint actions. To deal with this large action space, we assume that the actions of each unit and city are conditionally independent given the state. Actions of the civilization, cities and units are selected using a \( \epsilon \)-greedy policy with respect to the action-value function approximation. Although our approach does not explicitly coordinate the actions of different units, it can still achieve a certain degree

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\(^6\)www.civfanatics.com/content/civ2/reference/Civ2manual.zip

\(^7\)Civilization games can be won by diplomacy, space flight, or war. While for reasons of manageability we focus on the latter, our method can be applied to all three via a suitable reward function.

\(^8\)The built-in AI of Civilization II is allowed bypass game rules to provide challenging opposition to human players. However, both FreeCiv—the open-source reimplementations used in this work—and our algorithm are constrained to follow the rules of the game.
of coordination implicitly, via the roll-outs. For example, if transport-ship A typically selects action “move to city port X” in the roll-outs, then land-unit B can adapt its action to find the best action (e.g., “board transport-ship at port X”). Feature \( f_1 \) combines state, action, and predicate information of the relevant sentence as input to the final layer.

**Reward Function** Due to the length and complexity of the game, we truncate all roll-outs after 20 steps. At the end of each roll-out we use the ratio of the game scores between the two players as the reward function.

**Features** We use three sets of predefined feature functions to convert the attributes of the game state, actions and text into real valued inputs to layers \( \overrightarrow{y}, \overrightarrow{z} \) and \( Q \) of the neural network.

- **Sentence relevance features** consider attributes of the state, action and document. Some of these features compute text overlap between document words and text labels in the game state and action (e.g., feature \( x_1(\cdot) \) in Figure 5).

- **Predicate labeling features** operate on the words and dependency parse information of the document. These features include the Cartesian product of the candidate predicate label with word attributes such as type, part-of-speech tag, and dependency type.

- **Output layer features** are computed based on the sentence relevance decision \( y_i \) and the predicate labeling \( z_j \), in addition to state \( s \) and action \( a \) (e.g., feature \( f_1(\cdot) \) in Figure 5).

Overall, our method computes 473,200 features, some examples of which are shown in Figure 5. The set of possible features results from taking the Cartesian product of all observed game attributes, all unique words in the game manual, and all possible predicate labels – no explicit feature selection was done.

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8While explicit coordination is clearly desirable, it is not the focus of this paper. We leave it as an avenue for potential future work.

9http://freeciv.wikia.com. Game version 2.2
Table 1: Percentage of victories in 100-step games while playing against the built-in game AI. Results are averaged across 200 independent game runs. All differences are statistically significant.

<table>
<thead>
<tr>
<th>Method</th>
<th>% Wins</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>MC Tree Search</td>
<td>0</td>
<td>0.7</td>
</tr>
<tr>
<td>Linear MC</td>
<td>17.3</td>
<td>2.7</td>
</tr>
<tr>
<td>Non-linear MC</td>
<td>26.1</td>
<td>3.1</td>
</tr>
<tr>
<td>Random text</td>
<td>40.3</td>
<td>3.4</td>
</tr>
<tr>
<td>Non-Linear Text MC</td>
<td>53.7</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Table 2: Percentage of victories in full games played against the built-in AI. Results are averaged across 50 games each.

<table>
<thead>
<tr>
<th>Method</th>
<th>% Wins</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear MC</td>
<td>45.7</td>
<td>7.0</td>
</tr>
<tr>
<td>Non-linear MC</td>
<td>62.2</td>
<td>6.9</td>
</tr>
<tr>
<td>Non-Linear Text MC</td>
<td>78.8</td>
<td>5.8</td>
</tr>
</tbody>
</table>

7 Results

Tables 1 and 2 compare the performance of our model (Non-Linear Text MC) against several baselines. In both the 100-step game and full game evaluations, Non-Linear Text MC significantly outperforms all baselines, winning 53.7% and 78.8% of games respectively. The substantial gain obtained by Non-linear MC over Linear MC further demonstrates the advantages of non-linear value function approximation. Figure 7 shows examples of feature combinations learned by Non-linear MC, providing some intuition for the reasons behind the method’s improved performance. Surprisingly, MC Tree Search failed to win a single game. This illustrates the difficulties faced by search-tree based algorithms in domains with large branching factors. However, it is possible that a more sophisticated MC tree search algorithm could perform better, for example by improving the roll-out policy or controlling the exploration/exploitation trade-off [Gelly et al., 2006]; or by incorporating prior knowledge or using rapid action value estimation [Gelly and Silver, 2007].

Model Complexity vs Computation Time Trade-off One potential disadvantage of non-linear models is the increase in computation time required for action-value function estimation. To explore this trade-off, we vary the number of simulation roll-outs allowed at each game step, recording the win-rate and average computation time per game. Figure 6 shows the results of this evaluation for 100, 200 and 500 roll-outs. Not surprisingly, these results show that the more complex methods have higher computational demands. However, given a limited amount of time per game step, Non-Linear Text MC still produces the best performance, followed by Non-linear MC.

The benefits of automatically extracted domain knowledge The performance gain of Non-Linear Text MC over Non-linear MC suggests that information extracted from manuals is useful. To further validate this hypothesis, we introduce an additional baseline, Random Text, that mirrors the structure of the Non-Linear Text MC network, but is given a randomly generated document as input. The low performance of this baseline confirms our hypothesis that the algorithm does benefit from automatically extracted domain knowledge. For a comprehensive evaluation and analysis of the linguistic aspects of our method, see Branavan et al. [2011].

8 Conclusions and Future Work

This paper presented a new Monte-Carlo search algorithm for large sequential decision-making problems. The key innovation is to apply non-linear VFA, locally in time, to the current set of roll-outs. Our non-linear architecture leverages domain knowledge that is automatically extracted from text. Our learning algorithm simultaneously constructs a linguistic model, computes features of the game state, and estimates the value function, by backpropagation of error. We show that non-linear VFA is significantly more efficient than linear VFA, and that incorporating a linguistic model is significantly more efficient than an equivalent non-linguistic architecture. Our non-linear Monte-Carlo search algorithm wins over 78% of games against the built-in AI of Civilization II.

Our present method makes the strong assumption that units in the game operate independently of each other. While this assumption enables our method to operate tractably, it also limits the type of strategies that can be learned. For example,
due to this assumption, our model has limited unit coordination ability. It attempts to bypass this limitation by learning an early rush strategy—attacking and conquering the opponent early in the game before unit coordination becomes a key requirement. Modeling the value function without this assumption, while challenging, would greatly strengthen the method by allowing it to learn a broader and more robust range of game strategies.

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