1. **ATOMS**

The familiar model of an atom is that of a small nucleus composed of protons and neutrons surrounded by rapidly moving electrons. Typically, the atomic diameter is on the order of \(10^{-10}\) m while that of the nucleus is on the order of \(10^{-15}\) m. Protons and neutrons have about the same mass (1.00728 and 1.00867 amu respectively) and each is about 1800 times as heavy as an electron. A neutron is electrically neutral, but a proton has a positive charge \((+1.6 \times 10^{-19}\) coulomb\) which is exactly the opposite of the negative charge of an electron. In a neutral atom, the number of electrons around the nucleus equals the number of protons in the nucleus.

The number of protons in the nucleus (the “atomic number”, \(Z\)) characterizes a chemical element. Atoms of a given element all have the same number of protons, yet may have different masses. The atomic mass number of an atom, \(A\), is given by \(A = Z + N\), where \(N\) is the number of neutrons in the nucleus. Since an element is characterized solely by \(Z\), it follows that atoms of a given chemical element may have a varying number of neutrons. Subspecies of chemical elements with the same \(Z\) but differing \(N\) and \(A\) are called isotopes. The atomic weight of an element is the weighted average of the atomic masses of the various naturally occurring isotopes of the element, and the atomic weight scale is based on a value of exactly 12, after the carbon isotope that has an atomic mass number of 12.

2. **NUCLEI**

The nucleus of an atom weighs less than the sum of the weights of its isolated component particles. The difference between the actual mass and that of the

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*Generally adopted International Unit System.*
components is called the mass defect. The mass defect, $\Delta m$, is related to the binding energy within the nucleus, $\Delta E$ (in Joules), through Einstein’s equation:

$$\Delta E = \Delta m c^2$$

where $c$ is the velocity of light (in m·s$^{-1}$) and $\Delta m$ is the mass defect (in kg). The nuclear forces which bind protons and neutrons together are strong, and the binding energy per nuclear particle (nucleon) amounts to about $1.4 \times 10^{-12}$ Joules. The greatest nuclear binding energy is found in nuclei of medium atomic number (such as Fe) where $N$ is approximately equal to $Z$. For nuclei of larger atomic number, such as uranium, $N$ is about equal to $1.5 \times Z$, and the binding energy per nucleon is less. As a consequence of this decreased nuclear stability, some isotopes (of uranium, for example) are unstable. That is, if the uranium isotope, $^{235}_{92}$U (Z = 92, A = 235), is bombarded with neutrons, the following reaction can take place:

$$^{235}_{92}\text{U} + n \rightarrow ^{94}_{39}\text{Y} + ^{53}_{14}\text{I} + 2n$$

Here the reaction products are smaller nuclei of increased stability. (In the above convention, subscripts indicate the atomic number and the superscripts the mass number.) Notice that one incident neutron generates fission products including two neutrons - the basis for chain reactions in nuclear reactors and nuclear explosions.

Heavy nuclei (even light nuclei) which have an unfavorable ratio in the number of protons and neutrons can spontaneously decay by the emission of $\alpha$ particles (helium ions) or $\beta$ particles (electrons). These nuclei are referred to as radioactive. The rate at which the decay of such unstable nuclei takes place varies greatly and is indicated by the half-life of the material. In one half-life period, half of the unstable nuclei will have emitted radiation and thus will have changed their character (atomic number). In two half-life periods, only $1/4$ of the nuclei will have survived. In three half-lives, only $1/8$ of the original nuclei remain, etc. For example, the half-life of gamma-emitting “radio” cobalt, $^{60}_{27}$Co (used for X-ray therapy), is 5.3 years, whereas that of radioactive $^{14}_{6}$C is 5700 years. (Much more radiation is emitted per second by a given number of Co$^{60}$ atoms than by the same number of C$^{14}$ atoms.)

### 3. EXTRA-NUCLEAR ELECTRONS IN ATOMS

The first atomic theory in quantitative agreement with some experimentally determined facts was proposed in 1913 by Niels Bohr. He postulated (for atomic hydrogen) that:

- The (extra-nuclear) electron can assume only distinct (quantized) energy levels or states.
- In such energy levels, the electrons in motion will not radiate (loose) energy; on changing energy levels, radiation equivalent to the energy difference between the
levels is involved.

\[ E_{\text{rad}} = E_2 - E_1 = h\nu \]

- The stable states of the atom involve motion of the electrons in circular orbits.
- The angular momentum of electrons in orbit (mv\(r\)) is an integral number of \(h/2\pi\) units:

\[ mv\!r = n \frac{h}{2\pi} \]

- Newtonian mechanics applies to orbiting electrons.

A pictorial view of the Bohr atomic model visualizes electrons orbiting at a velocity \(v\) in well-defined spherical orbitals of radius \(r\) around the nucleus. The angular momentum of the orbiting electrons can, as stated above, only assume certain values of \(n \times h/2\pi\) where \(n\) (called the principal quantum number) can assume any positive integer value, i.e. 1, 2, 3, 4, etc. to infinity (fig. 1).

![Figure 1 The Hydrogen Atom According to Bohr.](image)

**The Hydrogen Atom**

Assuming coulombic interaction and the applicability of Newtonian mechanics, the following values may be directly obtained for the hydrogen atom:

---

3
• The radius of an electron orbit (spherical) in hydrogen is given by:

\[ r_n = \frac{n^2 \hbar^2 \epsilon_0}{\pi m e^2} \quad (n = 1, 2, 3, 4, \text{etc.}) \]

\[ r_n = n^2 \times \text{constant} = n^2 (0.529 \times 10^{-10}) \text{ m} \]

It can be seen that the smallest electron orbit in hydrogen - the stable orbit - is given for \( n = 1 \) at \( r_o = 0.529 \text{ Å} \). It is also seen that \( r \) increases with \( n^2 (r = n^2 r_o) \).

• The energy of an orbiting electron characterized by the principal quantum number (n) is given as:

\[ E_n = -\frac{1}{n^2} \times \frac{m e^4}{8 \hbar^2 \epsilon_0^2} = -\frac{1}{n^2} \times \text{constant} \quad \text{[Joule]} \]

This relationship indicates that electron orbits with increasing principal quantum number (n) assume decreasing negative values \( (1/n^2) \) with the limiting value \( (n \to \infty) \) being zero. For convenience, it is frequently customary to express electronic energies in terms of \textit{wave numbers} \( (\nu) \) with the units of \([\text{m}^{-1}]\). This conversion may readily be made since \( E = h \nu \). Thus:

\[ \nu = \frac{1}{\lambda} = -\frac{1}{n^2} \times \frac{m e^4}{8 \hbar^2 \epsilon_0^2} \quad \text{[m}^{-1}] \]

Upon substituting numerical values for all the constants, we obtain:

\[ \nu = -\frac{10973500}{n^2} = -\frac{1}{n^2} \times 10973500 \quad \text{[m}^{-1}] \]

(where \( n \) is again the principal quantum number which may assume the values 1, 2, 3, 4, etc. The value of 10973500 is referred to as the \textit{Rydberg constant} \((R; \text{also } R_H \text{ and } R_\infty)\) to honor the man who obtained its value from spectroscopic studies prior to the establishment of the Bohr model.)

The energy changes associated with electronic transitions and the accompanying emission of radiation (or absorption of radiation) may simply be calculated as
follows:

Emission = \Delta E = (E_{n_1} - E_{n_2}) = h\nu

Here \( n_2 \) is the principal quantum number of the outer orbit and \( n_1 \) is that of the inner orbit. In terms of \( \bar{\nu} \), the wave number, we obtain for emission of radiation:

\[
\bar{\nu} = \left[ -\frac{10973500}{n_1^2} \right] - \left[ -\frac{10973500}{n_2^2} \right]
\]

or

\[
\Delta E = 10973500 \left( \frac{1}{n_2^2} - \frac{1}{n_1^2} \right) \times hc
\]

Absorption = \Delta E = E_{n_2} - E_{n_1}

Electronic transitions (fig. 2) are conveniently represented in so-called term schemes.

**Multi-Electron Systems**

The limitations of the Bohr atom became apparent soon after its establishment. For example, the uranium atom would require 92 electronic orbits and it would have to assume a size which is incompatible with the experimental facts. The first modifications of the Bohr model were made by Sommerfeld, who introduced additional quantum conditions: Taking into account that individual sharp spectral lines split into several lines (of slightly differing \( \lambda \)) if light emission takes place in a magnetic field (Zeeman effect), the following picture emerged from the Bohr atom: electronic spherical orbits (shells)
Lyman series of transitions terminating at n=1

Balmer series of transitions terminating at n=2

Paschen series of transitions terminating at n=3

\( a_0 = 0.529 \text{ Å} \)

\( r_2 = 4a_0 = 2.116 \text{ Å} \)

\( r_3 = 9a_0 = 4.761 \text{ Å} \)

\( r_4 = 16a_0 = 8.464 \text{ Å} \)

\( E_{n=\infty} = 0 \)

\( E_5 = -R \cdot 1/25 \)

\( E_4 = -R \cdot 1/16 \)

\( E_3 = -R \cdot 1/9 \)

\( E_2 = -R \cdot 1/4 \)

\( E_1 = -R \)

Figure 2 Electron Transitions and Related Optical Spectra in Atomic Hydrogen
may have suborbitals (orbits) which are elliptical of varying eccentricity - controlled by an additional quantum number, the orbital quantum number ($l$). The eccentric orbitals may assume only particular spatial orientations controlled by the magnetic number (m), in an external magnetic field. The observed magnetic behavior of the elements required an additional quantization (Uhlenbeck) - the introduction of the spin quantum number ($s$).

According to the Bohr–Sommerfeld quantum theory, electrons move about the nucleus of an atom in well-defined orbits, each of which is characterized by four numbers, called quantum numbers. An electron moving in an orbit close to the nucleus has a larger (negative) energy than one in an outer orbit. Energy is therefore necessary to move an electron from an inner to an outer orbit (with smaller negative energy). Conversely, energy is released (as radiation) during the transition of an electron from an outer to an inner orbit. The (electromagnetic) radiation released consists of discrete entities or quanta, which are called photons. The energy of emitted photons is given by the difference in energy between the two orbits involved and is related to the frequency, $\nu$, or the wavelength, $\lambda$, of the electromagnetic radiation by:

$$E_{\text{photon}} = E_2 - E_1 = h\nu = h(c/\lambda) \quad (c = \lambda\nu)$$

where $h$ is called the Planck's constant, $E_2$ and $E_1$ are the energies of the outer and inner orbits, respectively, and $c$ is the velocity of light. Through (spectroscopic) observations of the frequencies or wavelengths of radiation emitted by an excited atom (atom with an excited electron), the differences of electron energy levels can be determined. Figure 1 shows such energy levels obtained from measurements of the wavelengths of radiation emitted by atomic hydrogen excited electrically in a gas discharge tube.

To specify the spatial location and energies of electrons in an atom requires the use of four quantum numbers. The “principal quantum number”, $n$, determines the size of the shell in which a particular electron orbits around the nucleus; it also largely determines its energy. The value of $n$ is restricted to integral values: $n = 1, 2, 3$ and so forth. A value of $n = 1$ signifies that the electron exists in the lowest energy state and its orbit is in the innermost allowed shell, as close to the nucleus as possible. Successively higher energy states are represented by $n = 2, 3$, etc. It should thus be clear that the principal quantum number of the outermost orbiting electron determines, in principle, the size of a given atom. For convenience, letters are frequently used to characterize the electronic shells of $n = 1, 2, 3, 4$, etc. In letter notation:

- $n = 1 = K$ shell
- $n = 2 = L$ shell
- $n = 3 = M$ shell
- etc.
The second quantum number, \( l \), is referred to as the “orbital” or “azimuthal quantum number.” It specifies the angular momentum of orbiting electrons and, to a minor extent, their energy. \( l \) can only assume integral values ranging from \( l = 0 \) to \( l = (n–1) \) (where \( n \) is the principal quantum number). Accordingly, for \( n = 1 \) (the K shell), \( l \) can only assume a value of 0. For \( n = 2 \), either \( l = 0 \) or \( l = 1 \) is possible, etc. For convenience again, letters are used to specify the electronic state (orbit) in a given shell (characterized by \( n \)) corresponding to the second quantum number:

\[
\begin{align*}
  l = 0 & = s \text{ (orbit)} \\
  l = 1 & = p \text{ (orbit)} \\
  l = 2 & = d \text{ (orbit)} \\
  l = 3 & = f \text{ (orbit)}
\end{align*}
\]

An electron with \( l = 0 \) is in an s–quantum state (in short, it is an s-electron), one with \( l = 1 \) is in a p-state, etc. Thus, an electron with a principal quantum number \( n = 3 \) and an orbital quantum number \( l = 1 \) is called a 3p electron (the electron in the M shell is in a p orbital).

The third quantum number, \( m \), called the “magnetic quantum number”, controls the number of allowed spatial orientations (“degeneracy”) of each orbit characterized by \( l \) in a given shell [characterized by \( n \)]. (Degenerate states are of identical energy. The “degeneracy” disappears in the presence of a magnetic field where different spatial orientation of orbits assume different energy values.) The total number of allowed orbital orientations for any orbital characterized by \( l \) is \( 2l + 1 \), corresponding to \( m \) values of \( l \), \((l–1)\), \((l–2)\), ..., 0, –1, –2, ..., –\( l \). An electronic state with \( l = 0 \) necessarily has only \( m = 0 \) and thus has no directional orientation in space; it is a spherical orbit. On the other hand, a p-state \( (l = 1) \) allows \( m \) values of –1, 0, +1. The resulting three possible orientations are perpendicular to one another (as shown in fig. 4).

The first three quantum numbers \( n, l \) and \( m \) define atomic electron orbitals. They are related respectively to the size, shape, and spatial orientation of the orbital. The fourth quantum number, \( s \), (called the “electron spin quantum number”), can be interpreted as determining for an orbiting electron the direction of electronic spin around its own axis. “\( s \)” can assume values of +1/2 (parallel spin) and –1/2 (anti-parallel spin). For notational purposes, a positive \( s \) is conveniently represented as \( \uparrow \) and a negative \( s \) as \( \downarrow \).

We may now summarize our findings about the electronic states in atoms. Any electron in an atom is defined by four quantum numbers, viz.:

- The principal quantum number \( (n) \), which may have any positive integral value except zero. (In practice, because of the instability of heavy nuclei, atoms containing electrons with \( n \) values greater than 7 are unknown.)
The orbital or azimuthal quantum number \( l \), which is an integer and may have any positive value less than \( n \), including zero.

\[ 0 \leq l < n \]

The magnetic quantum number \( m \), which is also an integer and may have any positive or negative value equal or less than \( l \), including zero.

\[ -l \leq m \leq +l \]

The spin quantum number \( s \) which may only assume one of two values, namely \( +1/2 \) and \( -1/2 \).

\[ s = \pm 1/2 \]

An important law enables us to make use of these quantum rules for the characterization of electronic states in multi-electron systems: the **Pauli Exclusion Principle**. It states that in any atom no two electrons may have the same four quantum numbers. From this principle it follows that each electronic orbital can accommodate at most two electrons differing by their spin quantum number which will be \( +1/2 \) for one electron and \( -1/2 \) for the other electron. (The Pauli principle is based on the fact that the separate existence of any electron depends upon its non-destruction by interference, i.e. on its wave nature.)

A further useful fact that generally simplifies understanding electronic structures is that (with exceptions stated shortly) the quantum states for electrons follow the rule (Aufbau Principle) that the lowest \( m \), \( l \) and \( n \) numbers, consistent with Pauli’s exclusion principle, are selected first by electrons in multi-electron atoms. (For the spin quantum numbers, the \( +1/2 \) value is given priority over the \( -1/2 \) value.) Applicability of this rule is restricted to systems in which the orbitals, defined by a selected set of quantum numbers with lowest possible numerical value, correspond to orbitals of lowest energy since in all instances the lowest energy levels are filled first. The build-up of the electronic states of an atom is obtained by placement of the electrons first in the orbitals of lowest energy (the aufbau principle or “construction principle”).

Wave mechanics (introduced by Schrödinger), unlike the quantum theory based on a planetary model, asserts that an electron in an atom cannot be considered as a particle having an orbit with a definite radius. Instead, there is a probability of an electron being at certain spatial positions. Hence, the location of an electron is best described in terms of its probability density distribution, which is sometimes called an electron cloud. The spatial symmetry of the probability distribution depends upon the electronic state. The electron cloud is spherically symmetric for s–electrons, but more complicated for electrons in a p-state. Examples of these distributions are shown in fig. 3 for 1s and 2p electrons.
Figure 3  Conclusions on Electron Orbital Shapes based on Wave Mechanics:

- 99% contour of 1s electron orbital
- 99% contour of 2s electron orbital
- 2py orbital
- 2pz orbital
- 2px orbital
4. **ENERGY LEVELS AND THE AUFBAU PRINCIPLE**

Consider the atom of an element containing one extra-nuclear electron: hydrogen; for electro-neutrality the charge on the nucleus must be +1. This orbiting electron (in the ground state - the lowest possible, most stable state) will have the lowest available quantum numbers in n, l and m. That is, \( n = 1 \); hence \( l = 0 \) and \( m = 0 \); also, \( s = +1/2 \).

In the two-electron atom helium, one electron will have the same quantum numbers as the electron in hydrogen and the other electron will have quantum numbers \( n = 1, l = 0, m = 0, s = -1/2 \). The element of atomic number 3 (lithium) will have two electrons with the same quantum numbers as the helium electrons, plus one electron with the quantum numbers \( n = 2, l = 0, m = 0, s = +1/2 \). [Note that \( n \) must be 2 for the third electron since states such as \( (n = 1, l = 1) \) or \( (n = 1, l = 0, m = 1) \) or \( (n= 1, l = 0, m = -1) \) are not allowed. Similarly, the quantum numbers for the additional electron in beryllium (atomic number 4) are \( n = 2, l = 0, m = 0, s = -1/2 \). The next electron for boron (atomic number 5) has the values \( n = 2, l = 1, m = -1, s = +1/2 \), and so on.

In applying the aufbau principle to the orbital filling with increasing atomic number we have thus far inferred the tendency of the energies of electrons to follow in the same order as the principal quantum numbers; that is, successive electron shells are filled with increasing \( Z \). This concept does not hold in all instances. For example, electrons with the quantum numbers \( n = 3, l = 2 \) (and various \( m \) values) are of higher energy than those with \( n = 4, l = 0 \). Other inversions occur with \( n = 4 \) and higher. These apparent irregularities in the aufbau principle, the result of an energetic overlap of orbitals in successive shells, lead to partial shell fillings and the appearance of groups of so-called transition elements. The groups are characterized (with minor exceptions) by identical outermost electron shell configurations and therefore do not exhibit, with increasing atomic number, the (expected) change in properties observed on regular shell filling for elements 2-18. (In the transition elements, with increasing atomic number the electrons are accommodated in lower lying shells which remained empty because of the above mentioned energy overlap of their orbitals.) The energy levels of the various orbitals in shells with increasing \( n \) are schematically indicated in fig. 4.

Another factor in the application of the aufbau principle is Hund’s Rule which states that in atoms the electrons tend at first to fill up given orbitals (\( m \) levels) singly (with unpaired spins and spin quantum number equal to +1/2). Only after all \( m \) levels associated with a particular \( l \) value in a given shell have been used for single-electron occupation does doubling of electrons into \( m \) levels occur. Thus the extra electron for carbon (atomic number 6) has the quantum numbers \( n = 2, l = 1, m = 0, s = +1/2 \) rather than \( n = 2, l = 1, m = -1, s = -1/2 \). Both the effects of energy inversion and Hund’s rule are very apparent when considering the electronic configuration of the elements \( Z = 18, 19, 20 \) and 21.
Relative energies of the orbitals in neutral, many-electron atoms. Electrons will always assume lowest available energy states. Accordingly, with increasing atomic numbers, the 4s states will be filled prior to the 3d states, for example.

The s, p, d, and f orbital sets:

<table>
<thead>
<tr>
<th>Types of orbitals</th>
<th>Orbital quantum numbers</th>
<th>Total number of orbitals in set</th>
<th>Total number electrons accommodated.</th>
</tr>
</thead>
<tbody>
<tr>
<td>s</td>
<td>l=0; m=0</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>p</td>
<td>l=1; m=1,0,-1</td>
<td>3</td>
<td>6</td>
</tr>
<tr>
<td>d</td>
<td>l=2; m=2,1,0,-1,-2</td>
<td>5</td>
<td>10</td>
</tr>
<tr>
<td>f</td>
<td>l=3; m=3,2,1,0,-1,-2,-3</td>
<td>7</td>
<td>14</td>
</tr>
</tbody>
</table>

Figure 4
The presently used notation is not the most convenient way of designating the energy levels (and wave functions) occupied by the electrons in atoms. The more informative way is a code written as follows: The principal quantum number is given first, followed by the conventional letter which designates the azimuthal (orbital) quantum number and, in a superscript, the number of electrons with that azimuthal quantum number. The code for the electronic ground state in hydrogen, therefore, is 1s$^1$, for helium 1s$^2$, lithium 1s$^2$2s$^1$, beryllium 1s$^2$2s$^2$, boron 1s$^2$2s$^2$2p$^1$, etc. (See fig. 5 for example.) You will note that the magnetic quantum number has not been specified, but this can be done when required by writing p$_x$ when m = –1, p$_y$ when m = +1 and p$_z$ when m = 0. Similar codes exist for the d and f levels. Usually such subscripts are not specified and in that case a consideration of Hund’s rule will not be required.

An important fact to remember is that the number of electrons in any s, p, d or f level is limited: There are, as you know, a maximum of two electrons in any level with spin numbers +1/2 and –1/2. For the p levels, l is one and, therefore, three m values (–1, 0, +1) are permitted, each with two electrons of spin number +1/2 and –1/2, resulting in a maximum of six p electrons in any p orbital system. The reader should confirm that ten electrons are the maximum in a d system of orbitals and 14 in an f system of orbitals.

5. IONIZATION POTENTIAL

Electrons may be removed from isolated atoms by bombardment with other electrons and by heat, for examples. The work (energy) required to remove the most weakly bound (outermost) electron from an isolated atom is known as the “ionization energy”. This energy is sometimes listed in units of Joules. More often ionization energies are given in terms of the “ionization potential”. The ionization potential is the potential (V) that will accelerate an electron at rest so that it acquires a kinetic energy, sufficient to extract the outermost (most loosely bound) electron from an atom. This potential is 13.595 Volt (as listed in the PT) for the ionization of a hydrogen atom. You can also say the electron is bound to the proton by an (negative) energy equivalent to the energy of an electron accelerated by a potential of 13.595 Volt. [If you make a dimensional analysis, you will recognize that charge (e) times potential (V) has the dimensions of energy (kg·m$^2$·sec$^{-2}$) and 1 electron Volt (1eV) corresponds to 1.6 x 10$^{-19}$ Joules.] (Note that the first ionization energies are given as first ionization potentials (V) in the Periodic Table of the Elements; see also the 3.091 courseware menu.)

It is significant that inert or noble gases have some of the highest ionization potentials. This reflects the fact that these elements have just enough electrons to completely fill a shell or a subshell which form stable configurations. On the other hand, the ionization potentials of alkali metal atoms (Li, Na, etc.) are low - the lowest, that of Cs, is only 3.89 eV. The reason for this is that alkali metal atoms have one outer s-electron beyond the stable electronic structure of an inert gas atom. Consequently this single electron in
## Figure 5  Atomic Electron Affinities (EA)

<table>
<thead>
<tr>
<th>Atom</th>
<th>Orbital electronic configuration</th>
<th>EA, electron volts</th>
<th>Orbital electronic configuration of anion</th>
</tr>
</thead>
<tbody>
<tr>
<td>H</td>
<td>1s(^1)</td>
<td>0.756</td>
<td>(He)</td>
</tr>
<tr>
<td>F</td>
<td>(He), 2s(^2)2p(^5)</td>
<td>3.45</td>
<td>(Ne)</td>
</tr>
<tr>
<td>Cl</td>
<td>(Ne), 3s(^2)3p(^5)</td>
<td>3.61</td>
<td>(Ar)</td>
</tr>
<tr>
<td>Br</td>
<td>(Ar), 4s(^2)3d(^{10})4p(^5)</td>
<td>3.36</td>
<td>(Kr)</td>
</tr>
<tr>
<td>I</td>
<td>(Kr), 5s(^2)4d(^{10})5p(^5)</td>
<td>3.06</td>
<td>(Xe)</td>
</tr>
<tr>
<td>O</td>
<td>(He), 2s(^2)2p(^4)</td>
<td>1.47</td>
<td>(He)(_2)s(^2)2p(^5)</td>
</tr>
<tr>
<td>S</td>
<td>(Ne), 3s(^2)3p(^4)</td>
<td>2.07</td>
<td>(Ne)(_3)s(^2)3p(^5)</td>
</tr>
<tr>
<td>Se</td>
<td>(Ar), 4s(^2)3d(^{10})4p(^4)</td>
<td>(1.7)</td>
<td>(Ar)(_4)s(^2)3d(^{10})4p(^5)</td>
</tr>
<tr>
<td>Te</td>
<td>(Kr), 5s(^2)4d(^{10})5p(^4)</td>
<td>(2.2)</td>
<td>(Kr)(_5)s(^2)4d(^{10})5p(^5)</td>
</tr>
<tr>
<td>N</td>
<td>(He), 2s(^2)2p(^3)</td>
<td>(-0.1)</td>
<td>(He)(_2)s(^2)2p(^5)</td>
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<tr>
<td>P</td>
<td>(Ne), 3s(^2)3p(^3)</td>
<td>(0.78)</td>
<td>(Ne)(_3)s(^2)2p(^4)</td>
</tr>
<tr>
<td>As</td>
<td>(Ar), 4s(^2)3d(^{10})4p(^3)</td>
<td>(0.6)</td>
<td>(Ar)(_4)s(^2)3d(^{10})4p(^4)</td>
</tr>
</tbody>
</table>

The visible spectrum:

<table>
<thead>
<tr>
<th>Wavelength ((\lambda)) in cm</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
</tr>
<tr>
<td>0.1</td>
</tr>
<tr>
<td>(10^{-2})</td>
</tr>
<tr>
<td>(10^{-3})</td>
</tr>
<tr>
<td>(10^{-4})</td>
</tr>
<tr>
<td>(10^{-5})</td>
</tr>
<tr>
<td>(10^{-6})</td>
</tr>
<tr>
<td>(10^{-7})</td>
</tr>
<tr>
<td>(10^{-8})</td>
</tr>
<tr>
<td>(10^{-9})</td>
</tr>
</tbody>
</table>

The visible spectrum:

- ultraviolet
- violet
- blue
- green
- yellow
- orange
- red
- near infrared

Wavelength (nm):

<table>
<thead>
<tr>
<th>Wavelength (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>400</td>
</tr>
<tr>
<td>500</td>
</tr>
<tr>
<td>600</td>
</tr>
<tr>
<td>700</td>
</tr>
<tr>
<td>800</td>
</tr>
</tbody>
</table>

Radio waves, micro waves, infrared, ultraviolet, x rays, gamma rays.
the outermost new shell can be removed relatively easily. (The second and successive ionization potentials of such atoms are increasingly greater.)

From a chemical and physical viewpoint, it is found that whether an atom is neutral or ionized as well as isolated or combined leads to distinctly different characteristics. It should be recognized that the notation used previously for neutral atoms can also be employed for electronic structures of ions. The electronic configurations of an iron atom and two iron ions are shown below.

\[
\begin{align*}
\text{Fe:} & \quad 1s^22s^22p^63s^23p^63d^64s^2 \\
\text{Fe}^{+2}: & \quad 1s^22s^22p^63s^23p^63d^6 \\
\text{Fe}^{+3}: & \quad 1s^22s^22p^63s^23p^63d^5
\end{align*}
\]

(ferrous ion)

(ferric ion)

6. ELECTRON AFFINITY

As we shall see later, the tendency of some atoms to accept, as well as to lose, electrons is important in determining how atoms combine with each other. Whereas removal of an electron always requires the expenditure of energy, acceptance of one extra electron by an atom generally is accompanied by the release of energy. The amount of energy released on acquisition of an electron is called the electron affinity (or “first electron affinity”). The elements on the left of the periodic table (metals) and the inert gases on the outer right have low electron affinities, whereas the non-metals have higher ones. The particularly high electron affinities of halogen atoms (F, Cl, etc.) may be attributed to the fact that these elements all lack one electron which would provide the stable electronic structure of an inert gas. By acquiring an additional electron, they increase their stability since the additional electron goes into the orbital lacking one electron and thus results in a stable, s^2p^6, octet configuration. (See fig. 5.)

7. ATOMIC SIZE

The size, or volume, of an isolated atom is difficult to define explicitly since, in the electron cloud model of the atom, the probability density distribution theoretically reaches zero only at infinity. Nevertheless, the electron density falls off so rapidly at a short distance from the nucleus that some approximation of size can be made. In the hydrogen atom, for example, the electron density is very nearly zero at a distance of 1.2 Å (1.2 x 10^-10 m) from the nucleus. The problem of defining atomic size is simplified in molecules and solids in that rather precise dimensions can be determined from interatomic distances which can be measured by diffraction techniques. Thus, in the H\textsubscript{2} molecule the atoms are only 0.72 Å apart, as determined from the distance between the nuclei. In this case the radius of the hydrogen atoms is taken to be 0.37 Å, even though the size of the H\textsubscript{2} molecule is considerably more than four times this value.
It should be apparent that the atomic radius depends upon whether an atom is isolated or combined with other atoms. The radius of an isolated atom is called the *van der Waals radius*, that of a bound atom in a molecule is the *covalent radius*, and that of a bound atom in a metal is the *metallic radius*. Van der Waals, covalent and metallic radii for some elements are listed in some periodic tables of the elements. The radii of positive ions (cations) and those of negative ions (anions) differ from the van der Waals radii.

**SAMPLE PROBLEM**

For hydrogen, calculate the radius (r) and energy level (E_T) of the electron in the lowest energy state (ground state).

* * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *

**Solution:**

The size of the first allowed orbit can be calculated by requiring that the centrifugal force of the orbiting electron be balanced by the coulombic attraction to the nucleus.

\[ F_{\text{centr}} = \frac{mv^2}{r} \quad F_{\text{att}} = \frac{e^2}{4\pi\varepsilon_0 r^2} \quad \frac{mv^2}{r} = \frac{e^2}{4\pi\varepsilon_0 r^2} \]

According to Bohr, the angular momentum of the electron (mvr) is quantized in units of h/2π:

\[ mvr = \frac{nh}{2\pi} \quad n = 1, 2, 3, ... \]

With these quantum conditions, r for the first allowed orbit becomes:

\[ \frac{mv^2}{r} = \frac{e^2}{4\pi\varepsilon_0 r^2} \]

\[ m^2v^2r^2 = \frac{me^2r}{4\pi\varepsilon_0} \]

\[ \frac{n^2h^2}{4\pi^2} = \frac{me^2r}{4\pi\varepsilon_0} \]

\[ r = \frac{n^2h^2\varepsilon_0}{\pi me^2} = n^2 \times \text{constant} \]

For n = 1:

\[ r_0 = 0.529 \times 10^{-10} \text{ m} = 0.529 \text{ Å} \]

The kinetic energy of the electron is 1/2 mv^2. The potential energy as a function of distance from the nucleus is given by Coulomb’s law as:

\[ -\frac{e^2}{4\pi\varepsilon_0 r} \]
The total energy is the sum of the kinetic and potential energies.

\[ E_T = E_K + E_P \]

\[ E_T = \frac{1}{2}mv^2 - \frac{e^2}{4\pi\varepsilon_0r} \]

The balance of attractive and repulsive forces requires that:

\[ F_{\text{centr}} = F_{\text{att}} \]

Since:

\[ \frac{mv^2}{r} = \frac{e^2}{4\pi\varepsilon_0r^2} \]

Then:

\[ \frac{mv^2}{2} = \frac{e^2}{8\pi\varepsilon_0r} \]

Therefore:

\[ E_T = \frac{e^2}{8\pi\varepsilon_0r} - \frac{e^2}{4\pi\varepsilon_0r^2} = -\frac{e^2}{8\pi\varepsilon_0r} \]

Substitution for \( r \) now gives:

\[ E_T = -\frac{1}{n^2} \times \frac{me^4}{8h^2\varepsilon_0^2} \]

For \( n = 1 \):

\[ E_T = -2.179 \times 10^{-18} \text{ J} \]

\[ E_T = -13.6 \text{ eV} \]
### DEFINITIONS

<table>
<thead>
<tr>
<th>Term</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>ATOM</td>
<td>The basic constituent of matter, consisting of a nucleus surrounded by electrons.</td>
</tr>
<tr>
<td>ATOMIC MASS NUMBER (A)</td>
<td>The combined number of protons and neutrons in a specific nucleus.</td>
</tr>
<tr>
<td>ATOMIC NUMBER (Z)</td>
<td>The number of protons in a specific nucleus, characteristic of a chemical element.</td>
</tr>
<tr>
<td>ATOMIC WEIGHT</td>
<td></td>
</tr>
</tbody>
</table>
1. The weighted mass of the naturally occurring atoms which constitute an element, relative to the value of exactly 12 for C\(^{12}\).  
2. The mass, in grams, of one mole of a chemical element. |
| ELECTRON | A negatively charged subatomic particle. |
| ELECTRON AFFINITY | The amount of energy released when an electron is added to the lowest possible energy level of a neutral atom. |
| ELECTRON DENSITY DISTRIBUTION | The spatial distribution of an electron in an atom, depending upon its set of quantum numbers. |
| ELECTRONIC CONFIGURATION | The shorthand notation used to designate the occupancy of energy levels in an individual atom. |
| ENERGY LEVEL | The discrete energy state of an electron in an atom, depending upon its set of quantum numbers. |
| FIRST IONIZATION POTENTIAL | The work which must be expended to remove an electron from a neutral atom in its ground state. |
| GROUND STATE | The lowest energy state of an atom. All electrons occupy energy levels sequentially from the lowest level. |
| HALF–LIFE | The time required for half of the atoms of an unstable, radioactive isotope to decay or for a reaction to go to 50% completion. |
ION | A charged atom having either an excess or a deficiency of electrons relative to its nuclear charge.

ISOTOPE | The form of an element having the same atomic number but different atomic mass number (or atomic weight) than other forms of the element. As a rule, isotopes of an element exhibit virtually identical chemical behavior, but may exhibit quite different nuclear and physical behaviors.

NEUTRON | A neutral subatomic particle having approximately the same mass as a proton.

NUCLEUS | An extremely dense, small portion of an atom, with a radius of about $10^{-5}$ that of an atom and containing in excess of 99% of the atomic mass.

ORBITAL | A pictorial designation pertaining to the existence of an electron within a subshell, depending upon the magnetic quantum number, $m$. Each orbital may contain a maximum of two electrons having opposite spins- i.e., electron spin quantum numbers of $+1/2$ or $-1/2$.

PAULI EXCLUSION PRINCIPLE | The statement that each electron in an atom must have a specific set of unique quantum numbers.

PERIODIC TABLE | A chart arraying the chemical elements in order of increasing atomic number and in groups having similar chemical behavior and similar outer electronic configurations.

PHOTON | A quantum, or minimum unit, of electromagnetic energy. The energy is equal to Planck’s constant, $h$, times the frequency, $\nu$, of the radiation.

PROTON | A positively charged subatomic particle whose charge is exactly opposite that of an electron and whose mass is about 1800 times that of an electron.

QUANTUM NUMBERS | A series of discrete numbers which catalog the state of an electron and which can be derived from wave mechanics.
| **SHELL** | A pictorial designation pertaining to electrons having the same principal quantum number, $n$, often indicative of the overall energy level of the electron. |
| **SUBSHELL** | A pictorial designation pertaining to the state of electrons within a shell, depending upon the second quantum number, $l$, and indicative of the spatial distribution of the electron. |
EXERCISE FOR THE IDLE MIND

1. Given the following nuclear reaction,
\[ \frac{2}{1}H + \frac{3}{2}He \rightarrow \frac{4}{2}He + \frac{1}{1}H \]
determine the energy change associated with the formation of 1 mole \( \frac{4}{2}He \) (in J/mole). The nuclear masses (in amu) are:
\[ \frac{2}{1}H = 2.01345 \]
\[ \frac{3}{2}He = 3.01493 \]
\[ \frac{4}{2}He = 4.00150 \]
\[ \frac{1}{1}H = 1.00728 \]

2. In all likelihood, the Soviet Union and the United States together in the past exploded about ten hydrogen devices underground per year.
   (a) If each explosion converted about 10 g of matter into an equivalent amount of energy (a conservative estimate), how many kJ of energy were released per device?
   (b) If the energy of these ten devices had been used for propulsion to substitute for gasoline combustion, how many gallons of gasoline would not have had to be burned per year? (One gallon of gasoline releases about \( 1.5 \times 10^5 \) kJ during combustion.)

3. Assuming the element antimony (Sb) has two naturally occurring isotopes (\(^{121}\)Sb and \(^{123}\)Sb) which exist at an abundance of 57.25% and 42.75% respectively, determine the atomic weight of antimony, Sb (amu).

4. How much oxygen (in kg) is required to completely convert 1 mole of \( C_2H_6 \) into \( CO_2 \) and \( H_2O \)?

5. A nucleus of mass number 56 contains 30 neutrons. An “ion” of this element has 23 electrons. Write the symbol of this ion and give the ionic charge as a superscript on the right.

6. What is the complete notation for a nucleus that contains 30 protons and 34 neutrons?

7. At its closest approach Mars is \( 5.6 \times 10^6 \) km from Earth. How long would it take to send a radio message from a space probe on Mars to Earth when the planets are at this closest distance?
8. Magnesium (Mg) has the following isotopic distribution:

- $^{24}\text{Mg}$ 23.985 amu at 0.7870 fractional abundance
- $^{25}\text{Mg}$ 24.986 amu at 0.1013 fractional abundance
- $^{26}\text{Mg}$ 25.983 amu at 0.1117 fractional abundance

What is the atomic weight of magnesium (Mg) according to these data?

9. Calculate the molecular weight of each of the substances listed:

- NH$_4$OH, NaHCO$_3$, CH$_3$CH$_2$OH

10. (a) Determine the velocity of a free electron (in international units) which has a kinetic energy of $2.7 \times 10^{-16}$ Joules. (Ignore relativistic effects.)

(b) Determine the velocity of a lithium ion (Li$^{++}$) which has a kinetic energy of $2.7 \times 10^{-16}$ Joules.

11. For light with a wavelength ($\lambda$) of 408 nm determine:

(a) the frequency

(b) the wave number

(c) the wavelength in Å

(d) the total energy (in Joules) associated with 1 mole of photons

(e) the “color”

12. For “yellow radiation” (frequency, $\nu$, = $5.09 \times 10^{14}$ s$^{-1}$) emitted by activated sodium, determine:

(a) the wavelength ($\lambda$) in [m]

(b) the wave number ($\bar{\nu}$) in [cm$^{-1}$]

(c) the total energy (in kJ) associated with 1 mole of photons

13. (a) Determine the energy required in J/atom to remove the outermost electron from its ground state to infinity (ionization energy) in H, He and Cs.

(b) Calculate the velocity an electron must have to be able to ionize a lithium (Li) atom.

14. Determine if an electron travelling at a velocity of $7.2 \times 10^6$ km/hr is capable of ionizing a hydrogen atom with its orbiting electron in the ground state.

15. What is the energy (in eV) of a photon of ultraviolet light with $\lambda = 340$ nm?

16. For radiation with a wave number ($\bar{\nu}$) $2 \times 10^5$ m$^{-1}$, calculate:

(a) the wavelength in nm;

(b) the frequency.
17. Potassium metal can be used as the active surface in a photodiode because electrons are relatively easily removed from a potassium surface. The energy needed is $2.15 \times 10^5$ J per mole of electrons removed (1 mole = $6.02 \times 10^{23}$ electrons). What is the longest wavelength light (in nm) with quanta of sufficient energy to eject electrons from a potassium photodiode surface?

18. Determine the first ionization energy ($E_I$) in J/atom for calcium. (Make use of the Periodic Table of the Elements.)

19. For red light of wavelength ($\lambda$) $6.7102 \times 10^{-5}$ cm, emitted by excited lithium atoms, calculate:
   (a) the frequency ($\nu$) in s$^{-1}$;
   (b) the wave number ($\nu$) in cm$^{-1}$;
   (c) the wavelength ($\lambda$) in nm;
   (d) the total energy (in Joules) associated with 1 mole photons of the indicated wavelength.

20. What acceleration potential (in Volts) is required to impart to an electron the energy of $2 \times 10^{-16}$ Joules? (Ignore relativistic effects.)

21. Determine for hydrogen the velocity of an electron in an n=4 state.

22. Determine the wavelength of radiation emitted by hydrogen atoms upon electron transitions from n=6 to n=2.

23. Using the “box” notation, give the electron distribution (orbital occupancy) for the following elements in their ground state: N, Li, Mg.

24. Determine the maximum wavelength ($\lambda_{max}$) of a photon which can ionize neon (Ne).

25. Calculate the minimum potential (V) which must be applied to a free electron so that it has enough energy to excite, upon impact, the electron in a hydrogen atom from its ground state to a state of n=5.

26. Determine the wavelength ($\lambda$), in m, of radiation emitted upon the transition of an electron in He$^+$ from the state n=2 to the state n=1.

27. A line of the Lyman series of the spectrum of hydrogen has a wavelength of $9.50 \times 10^{-8}$ m. What was the “upper” quantum state ($n_i$) involved in the associated electron transition?

28. Calculate the “Bohr radius” for He$^+$.
29. What potential difference is required to accelerate a singly charged gaseous ion in a vacuum so that it has an energy equivalent to 20 kcal/mole?

30. Calculate the velocity of 1 MeV protons.

31. Light of wavelength $\lambda = 4.28 \times 10^{-7}$ m interacts with a “motionless” hydrogen atom. During this interaction it transfers all its energy to the orbiting electron of the hydrogen. What is the velocity of this electron after interaction?

32. What is the energy gap (in eV) between the electronic states n=3 and n=8 in a hydrogen atom?

33. What is the minimum velocity an electron must have to still be able to ionize boron (B)?

34. (a) From information provided in your Periodic Table of the Elements, determine the first ionization energies (in Joules) for the horizontal columns (1) Na to Ar and (2) Ca to Cu.
(b) On a graph, plot the values obtained as a function of atomic number and attempt to explain the apparent difference in the change of ionization energy with increasing atomic number for the two series of atoms.

35. Determine the energy gap (in eV) between the electronic states n=7 and n=8 in hydrogen.

36. In a box diagram, give the electron distribution for the following elements in their ground state: Cl, Mg, N, C.

37. Determine the frequency of radiation capable of generating, in atomic hydrogen, free electrons which have a velocity of $1.3 \times 10^6$ m/s.

38. (a) Determine if an energy level of $-1.362 \times 10^{-19}$ J is an allowed electron energy state in atomic hydrogen.
(b) If your answer is yes, determine its principal quantum number (n). If your answer is no, determine n for the “nearest allowed state”.

39. For a proton which has been subjected to an accelerating potential (V) of 15 Volts, determine its deBroglie wavelength.

40. Electrons are accelerated by a potential of 10 Volts.
(a) Determine their velocity.
(b) Determine their deBroglie wavelength ($\lambda_p$).
(c) Will these electrons, on interaction with hydrogen atoms, be able to excite the ground state electrons in hydrogen?
41. How many Hg atoms are in liquid mercury (Hg) which fills a 10 ml graduated cylinder?

42. (a) Balance the equation for the reaction between CO and O₂ to form CO₂.
(b) If 32.0 g of oxygen react with CO to form carbon dioxide (CO₂), how much CO was consumed in this reaction?

43. When solid ammonium sulfate, (NH₄)₂SO₄, is heated, gaseous ammonia (NH₃) and liquid sulfuric acid (H₂SO₄) are formed.
(a) Write the balanced equation for the reaction.
(b) How many grams of (NH₄)₂SO₄ will produce 0.300 mole of ammonia?

44. One mole of electromagnetic radiation (light, consisting of energy packages called photons) has an energy of 171 kJ/mole photons.
(a) Determine the wavelength of this light and its position in the visible spectrum.
(b) Determine the frequency of this radiation (in SI units).

45. How much mass (in kg) must be converted into heat (energy) to increase the temperature of 300 US gallons of water from 14°C to 20°C? (Assume that the energy required to change the water temperature by 1°C remains constant over the indicated temperature range.)

46. Determine the velocity of an electron (in m/s) that has been subjected to an accelerating potential V of 150 Volt. (The energy imparted to an electron by an accelerating potential of one Volt is 1.6 x 10⁻¹⁹ Joules; dimensional analysis shows that the dimensions of charge x potential correspond to those of energy; thus: 1 electron Volt (1eV) = 1.6 x 10⁻¹⁹ Coulomb x 1 Volt = 1.6 x 10⁻¹⁹ Joules.)

47. Determine in units of eV the energy of a photon (hν) with the wavelength of 800 nm.

48. Determine the number of Au atoms in 12 g solid gold (Au) at 400K.

49. Chlorine consists of the following isotopes:

<table>
<thead>
<tr>
<th>mass</th>
<th>fractional abundance</th>
</tr>
</thead>
<tbody>
<tr>
<td>³⁵Cl 34.96885 amu</td>
<td>0.75771 (75.771%)</td>
</tr>
<tr>
<td>³⁷Cl 36.96590 amu</td>
<td>0.24229 (24.229%)</td>
</tr>
</tbody>
</table>

From this data, determine the atomic weight (in amu).

50. (a) Determine the atomic weight of He⁺⁺ from the values of its constituents.
(b) Compare the value obtained in (a) with the value listed in your Periodic Table and explain any discrepancy if such is observed. (There is only one natural ⁴²He isotope.)
51. A photon with a wavelength of $1.00 \times 10^{-8}$ m interacts with hydrogen and expels from orbit an electron in an excited state ($n=2$). Determine the velocity of the liberated electron (prior to energy loss due to interaction with the environment).

52. The average lifetime of an electron in an excited state of hydrogen is $10^{-8}$ sec. How many revolutions does this electron make in the $n=3$ state before dropping back to the ground state?

53. Monochromatic light is shone on atomic hydrogen (H) with all its electrons in the ground state. As a consequence, the gas emits radiation containing six different frequencies. What is the minimum frequency the incident radiation must have to generate the exiting radiation?

54. Derive an expression for the electron orbital radii (as a function of $n$) in hydrogen-like systems comprising a single electron about a nucleus with charge $(t)$.

55. From a standard radio dial, determine the wavelength ranges ($\lambda_{\text{min}}$ to $\lambda_{\text{max}}$) for broadcasts on the:
   (a) AM band
   (b) FM band

56. Determine the orbiting velocity ($v$) of an electron in an excited state characterized by $n=3$.

57. Your latest model Cadillac gets 28 mpg on the way from Boston to New York (239 miles). Assuming you drive with octane as fuel ($C_8H_{18}$) which has a density of 0.679 g/ml, how many kg of oxygen will you have burned up on such a round trip with your car? (The conversion may be formulated as: $x C_8H_{18} + \text{oxygen} \rightarrow y \text{CO}_2 + \text{H}_2\text{O}$.)

58. The electron affinity (E.A.) of chlorine (Cl) is strongly negative. In contrast, it is found to be positive for Ar. Explain the difference in behavior.

59. Write in box notation the electron configurations of the following species:
   $N$, $P^{3+}$, $S$, $S^{4+}$

60. Atoms stabilize by losing and/or gaining electrons: For S (sulfur), what electron configurations do you expect to have higher stability than that associated with the neutral atom? (Are $S^+$ or $S^-$ “more stable states”? They are not; which states are?) Explain the rationale for your answer.

61. List the possible values of the four quantum numbers for a 2p electron in boron.
62. The light of what wavelength is required to excite an electron from its ground state to the lowest excited state?