1.021, 3.021, 10.333, 22.00 Introduction to Modeling and Simulation

Part I – Continuum and particle methods

# Applications to biophysics and bionanomechanics (cont'd)

Lecture 11

Markus J. Buehler

Laboratory for Atomistic and Molecular Mechanics Department of Civil and Environmental Engineering Massachusetts Institute of Technology

#### Massachusetts Institute of Technology

### Content overview

Partic	le and continuum methods	Lectures 2-13
1.	Atoms, molecules, chemistry	
2.	Continuum modeling approaches and solution approaches	
3.	Statistical mechanics	
4.	Molecular dynamics, Monte Carlo	
5.	Visualization and data analysis	
6.	Mechanical properties – application: how things fail (and how to prevent it)	
7.	Multi-scale modeling paradigm	
8.	Biological systems (simulation in biophysics) – how proteins work and how to model them	

#### **II.** Quantum mechanical methods

- 1. It's A Quantum World: The Theory of Quantum Mechanics
- 2. Quantum Mechanics: Practice Makes Perfect
- 3. The Many-Body Problem: From Many-Body to Single-Particle
- 4. Quantum modeling of materials
- 5. From Atoms to Solids
- 6. Basic properties of materials
- 7. Advanced properties of materials
- 8. What else can we do?

Lectures 14-26

#### Overview: Material covered so far...

- Lecture 1: Broad introduction to IM/S
- Lecture 2: Introduction to atomistic and continuum modeling (multi-scale modeling paradigm, difference between continuum and atomistic approach, case study: diffusion)
- Lecture 3: Basic statistical mechanics property calculation I (property calculation: microscopic states vs. macroscopic properties, ensembles, probability density and partition function)
- Lecture 4: Property calculation II (Monte Carlo, advanced property calculation, introduction to chemical interactions)
- Lecture 5: How to model chemical interactions I (example: movie of copper deformation/dislocations, etc.)
- Lecture 6: How to model chemical interactions II (EAM, a bit of ReaxFF—chemical reactions)
- Lecture 7: Application to modeling brittle materials I
- Lecture 8: Application to modeling brittle materials II
- Lecture 9: Application Applications to materials failure
- Lecture 10: Applications to biophysics and bionanomechanics
- Lecture 11: Applications to biophysics and bionanomechanics (cont'd)

# Lecture 11: Applications to biophysics and bionanomechanics (cont'd)

#### **Outline:**

- 1. Force fields for proteins: (brief) review
- 2. Fracture of protein domains Bell model
- 3. Examples materials and applications

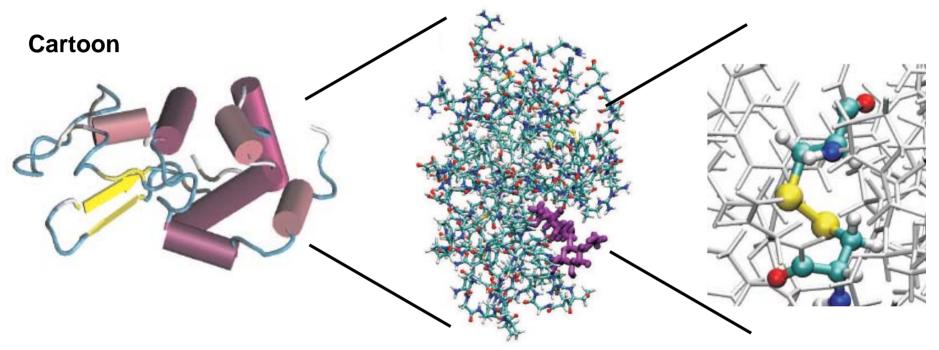
#### Goal of today's lecture:

- Fracture model for protein domains: "Bell model"
- Method to apply loading in molecular dynamics simulation (nanomechanics of single molecules)
- Applications to disease and other aspects

1. Force fields for proteins: (brief) review

## Chemistry, structure and properties are linked

**Chemical structure** 



#### **Presence of various chemical bonds:**

- Covalent bonds (C-C, C-O, C-H, C-N..)
- Electrostatic interactions (charged amino acid side chains)
- H-bonds (e.g. between H and O)
- vdW interactions (uncharged parts of molecules)

#### Model for covalent bonds

$$\phi_{\text{stretch}} = \frac{1}{2} k_{\text{stretch}} (r - r_0)^2$$

$$\phi_{\text{bend}} = \frac{1}{2} k_{\text{bend}} (\theta - \theta_0)^2$$

$$\phi_{\text{rot}} = \frac{1}{2} k_{\text{rot}} (1 - \cos(\theta))$$

Courtesy of the EMBnet Education & Training Committee. Used with permission. Images created for the CHARMM tutorial by Dr. Dmitry Kuznetsov (Swiss Institute of Bioinformatics) for the EMBnet Education & Training committee (http://www.embnet.org)

#### http://www.ch.embnet.org/MD\_tutorial/pages/MD.Part2.html

Summary: CHARMM potential (pset #3)  

$$U_{total} = U_{Elec} + U_{Covalent} + U_{Metallic} + U_{vdW} + U_{H-bond}$$

$$U_{Elec} : \text{ Coulomb potential } \phi(r_{ij}) = \frac{q_i q_j}{\varepsilon_1 r_{ij}}$$

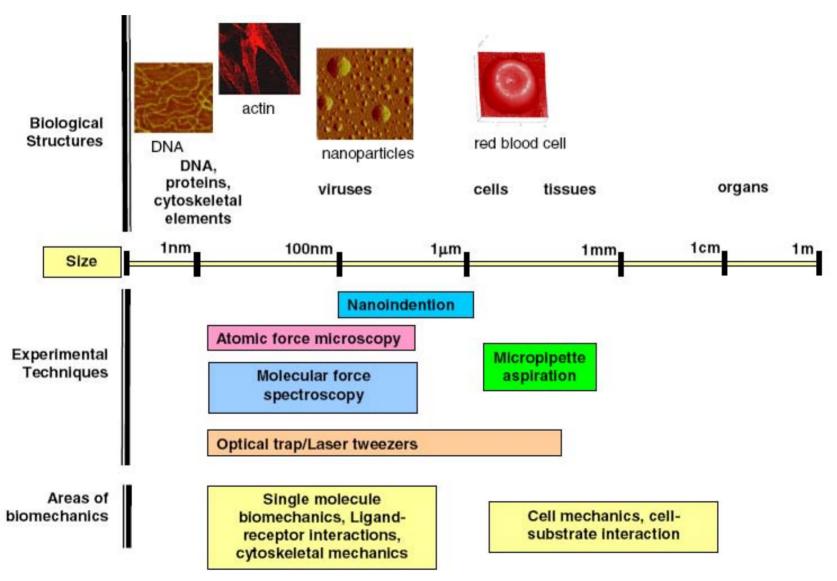
$$U_{Covalent} = U_{stretch} + U_{bend} + U_{rot} \begin{cases} \phi_{stretch} = \frac{1}{2} k_{stretch} (r - r_0)^2 \\ \phi_{bend} = \frac{1}{2} k_{bend} (\theta - \theta_0)^2 \\ \phi_{rot} = \frac{1}{2} k_{rot} (1 - \cos(\theta)) \end{cases}$$

$$U_{vdW} : \text{ LJ potential } \phi(r_{ij}) = 4\varepsilon \left[ \left( \frac{\sigma}{r_{ij}} \right)^{12} - \left( \frac{\sigma}{r_{ij}} \right)^6 \right]$$

$$U_{H-bond} : \phi(r_{ij}) = D_{H-bond} \left[ 5 \left( \frac{R_{H-bond}}{r_{ij}} \right)^{12} - 6 \left( \frac{R_{H-bond}}{r_{ij}} \right)^{10} \right] \cos^4(\theta_{DHA})$$

## 2. Fracture of protein domains – Bell model

#### **Experimental techniques**



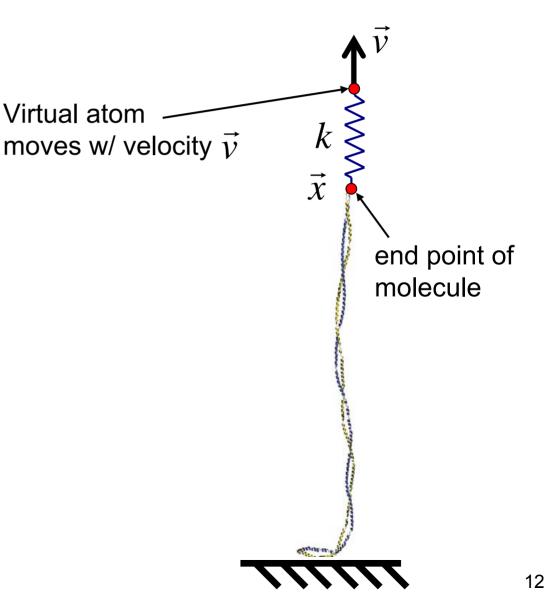
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#### How to apply load to a molecule

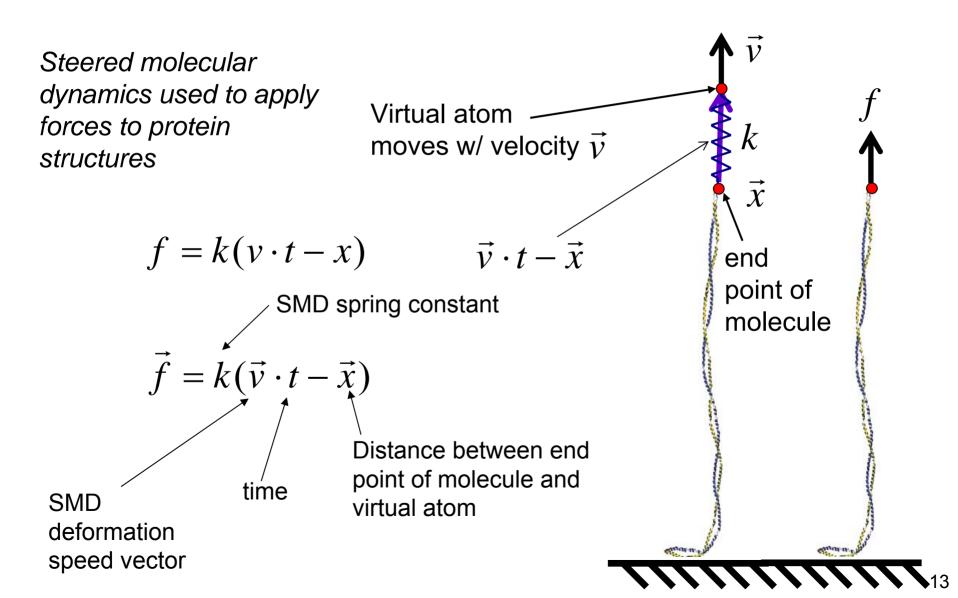
(in molecular dynamics simulations)

#### Steered molecular dynamics (SMD)

Steered molecular dynamics used to apply forces to protein structures

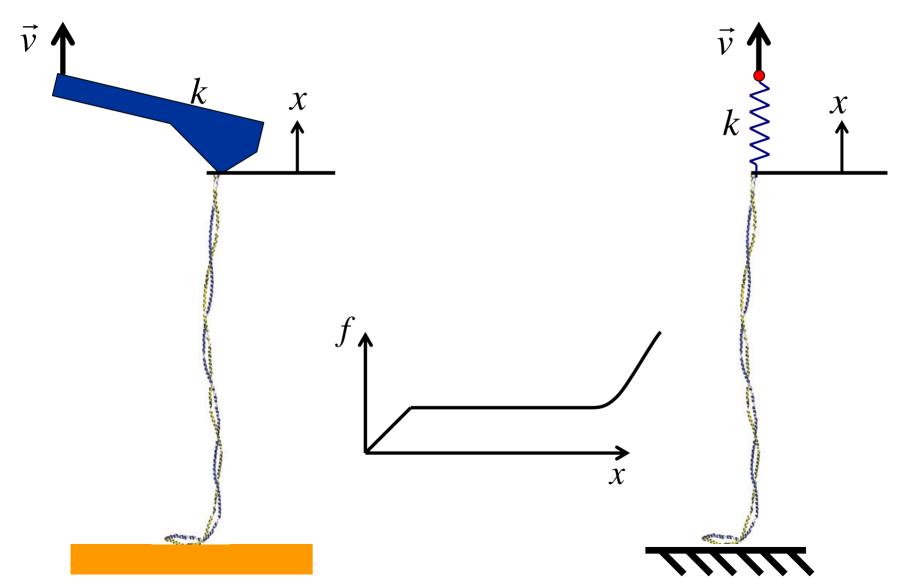


#### Steered molecular dynamics (SMD)



#### SMD mimics AFM single molecule experiments

#### Atomic force microscope

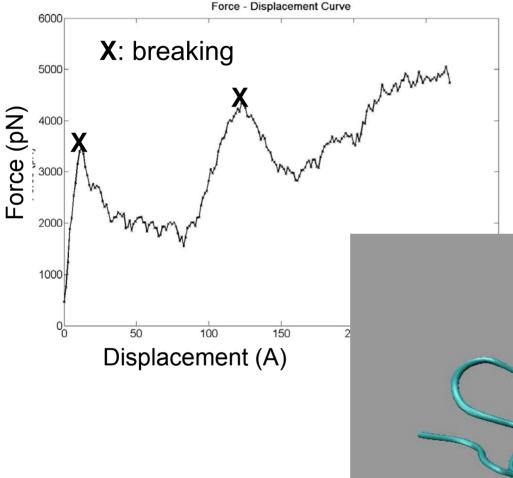


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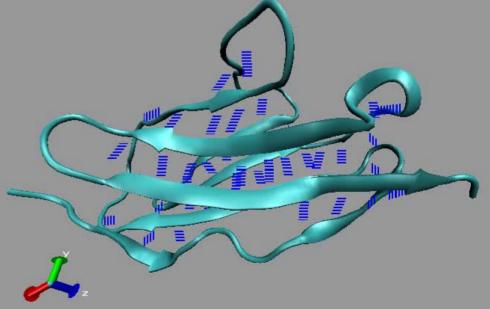
SMD is a useful approach to probe the nanomechanics of proteins (elastic deformation, "plastic" – permanent deformation, etc.)

Example: titin unfolding (CHARMM force field)

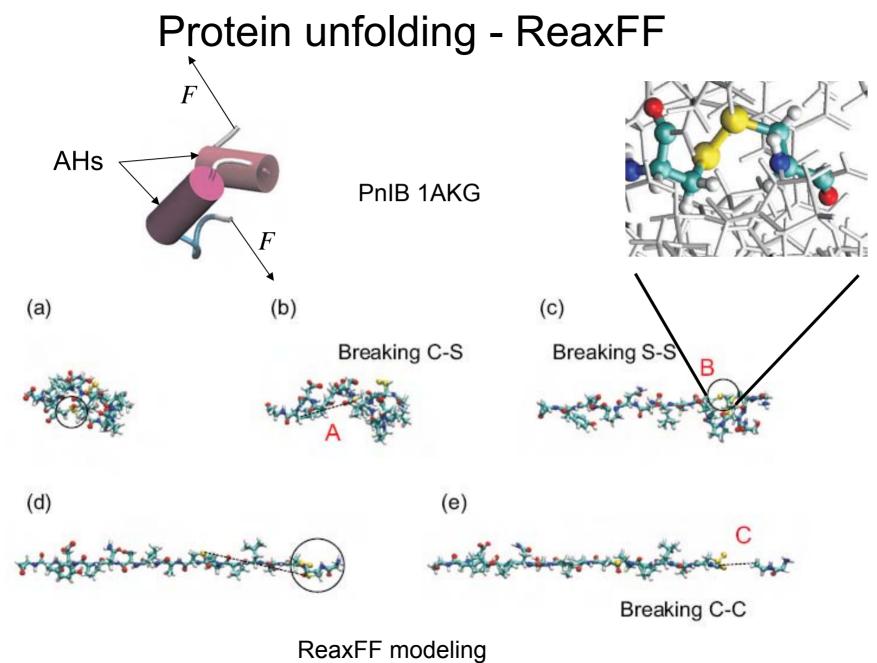
# Unfolding of titin molecule



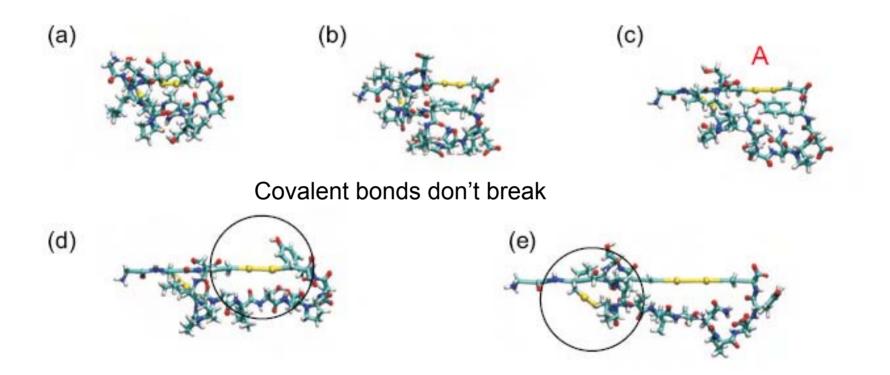
Titin I27 domain: Very resistant to unfolding due to parallel H-bonded strands



Keten and Buehler, 2007

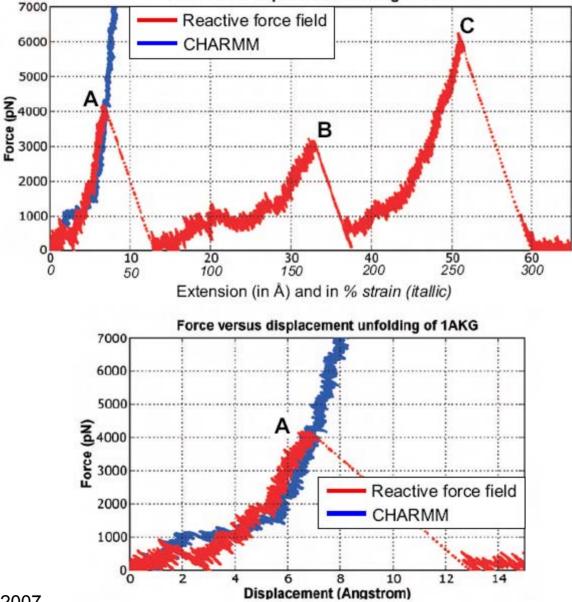


### Protein unfolding - CHARMM



CHARMM modeling

Comparison – CHARMM vs. ReaxFF

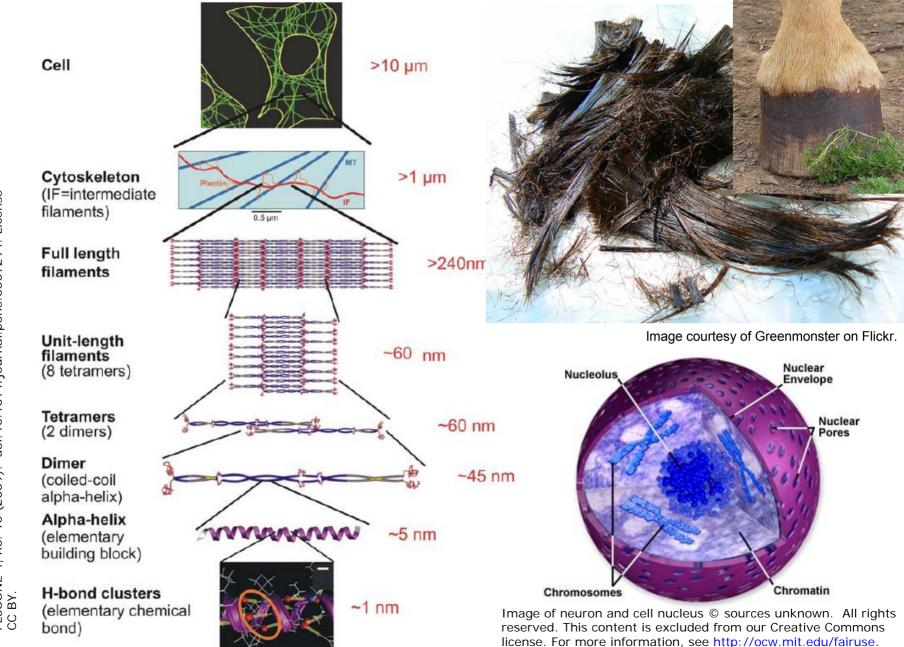


M. Buehler, JoMMS, 2007

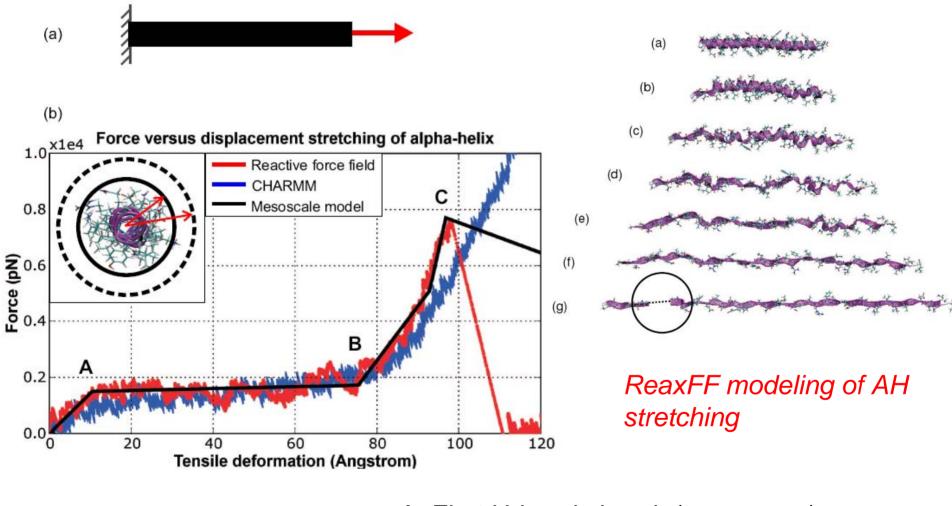
#### Application to alpha-helical proteins

#### Vimentin intermediate filaments

Image courtesy of Bluebie Pixie on Flickr. License: CC-BY.



#### Alpha-helical protein: stretching



- A: First H-bonds break (turns open)
- B: Stretch covalent backbone
- C: Backbone breaks

M. Buehler, JoMMS, 2007

#### Coarse-graining approach Describe interaction between "beads" and not "atoms"

Same concept as force fields for atoms

$$U\left(\vec{R}\right) = U_T + U_B,$$

$$U_{T} = \sum_{pairs} \phi_{T}(r) \text{ and } U_{B} = \sum_{angles} \phi_{B}(\varphi).$$

$$\phi_{B}(\varphi) = \frac{1}{2} K_{B}(\varphi - \varphi_{0})^{2}$$

$$= H(r_{break} - r) \begin{cases} k_{T}^{(1)}(r - r_{0}) & r_{1} > r_{1} \\ R_{1} + k_{T}^{(2)}(r - r_{1}) & r_{1} \le r < r_{1} \\ R_{1} + k_{T}^{(2)}(r - r_{1}) & r_{1} \le r < r_{1} \end{cases}$$

$$\frac{\partial \phi_T}{\partial r}(r) = H(r_{break} - r) \begin{cases} R_1 + k_T^{(2)}(r - r_1) & r_1 \le r < r_2 \\ R_2 + R_1 + k_T^{(3)}(r - r_2) & r_2 \le r < r_3 \\ R_3 + R_2 + R_1 + k_T^{(4)}(r - r_3) & r_3 \le r \end{cases}$$

#### See also: http://dx.doi.org/10.1371/journal.pone.0006015

#### Case study: From nanoscale filaments to micrometer meshworks

#### Movie: MD simulation of AH coiled coil

Image removed due to copyright restrictions. Please see http://dx.doi.org/10.1103/PhysRevLett.104.198304.

See also: Z. Qin, ACS Nano, 2011, and Z. Qin BioNanoScience, 2010.

#### What about varying pulling speeds?

Changing the time-scale of observation of fracture

### Variation of pulling speed

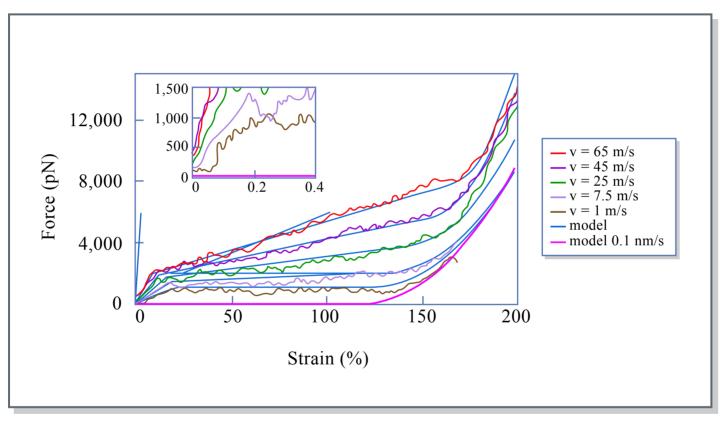
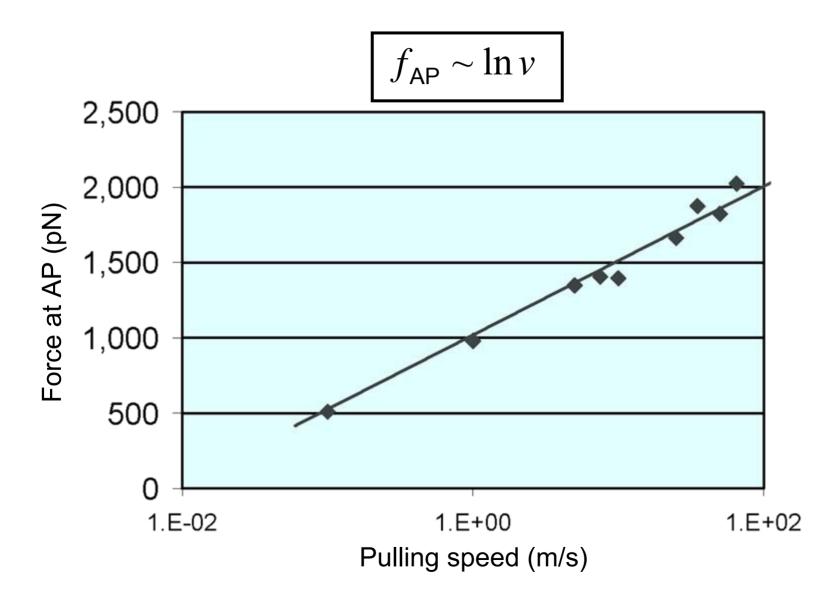


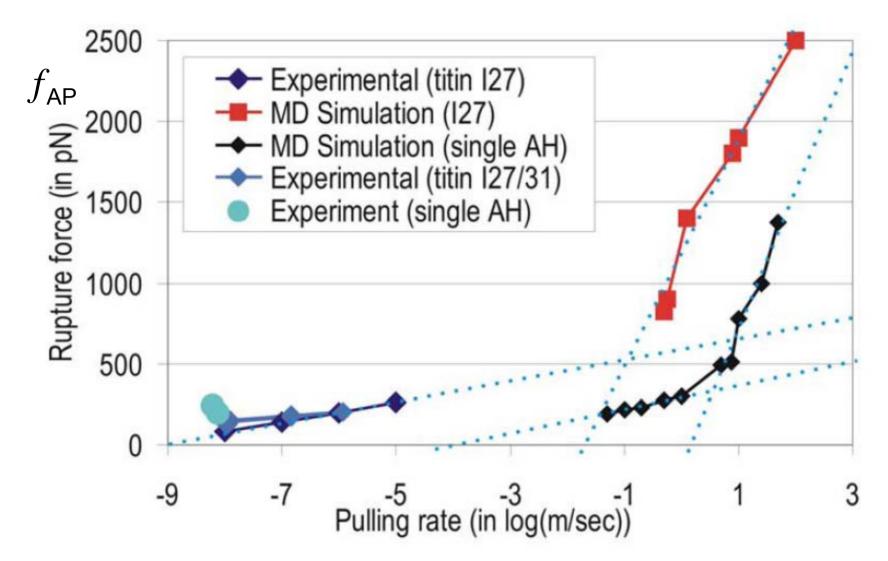
Image by MIT OCW. After Ackbarow and Buehler, 2007.

Force at angular point  $f_{AP}$  = fracture force



#### General results...

#### Rupture force vs. pulling speed



Reprinted by permission from Macmillan Publishers Ltd: Nature Materials. Source: Buehler, M. ,and Yung, Y. "Chemomechanical Behaviour of Protein Constituents." *Nature Materials* 8, no. 3 (2009): 175-88. © 2009.

#### Buehler et al., Nature Materials, 2009

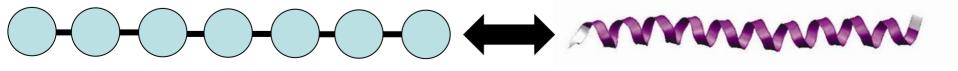
#### How to make sense of these results?

#### A few fundamental properties of bonds

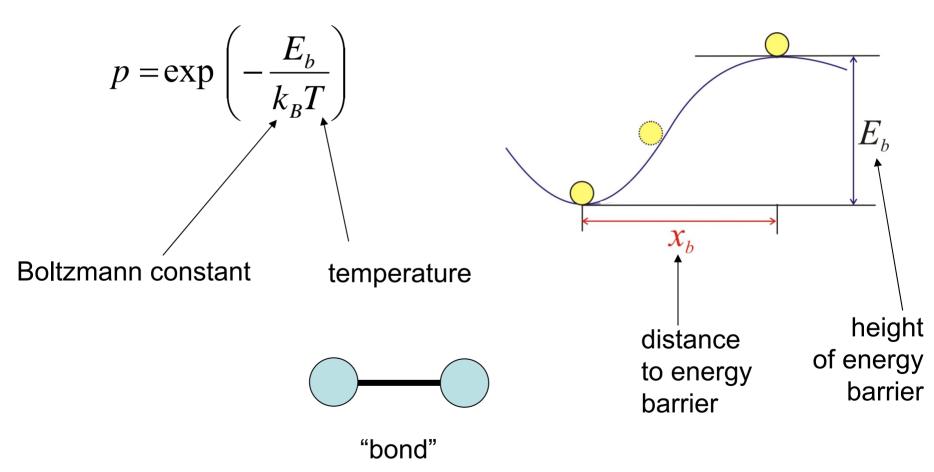
- Bonds have a "bond energy" (energy barrier to break)
- Arrhenius relationship gives probability for energy barrier to be overcome, given a temperature

$$p = \exp\left(-\frac{E_b}{k_B T}\right)$$

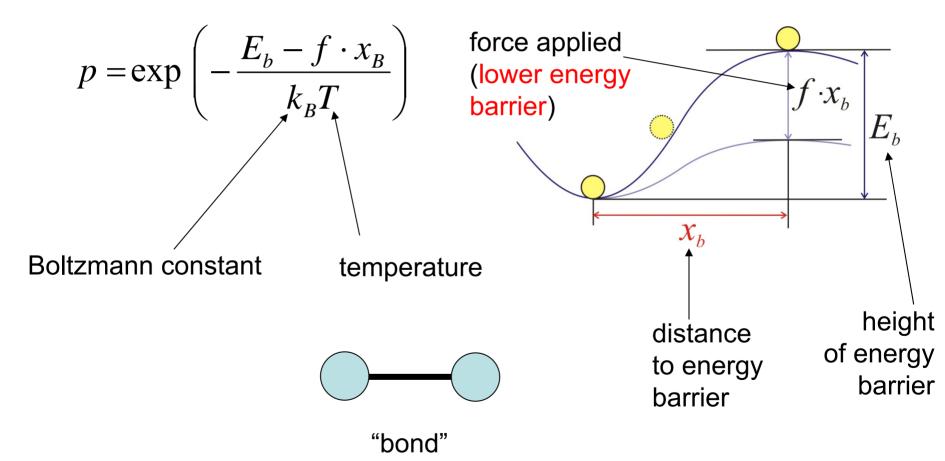
All bonds vibrate at frequency *w*



Probability for bond rupture (Arrhenius relation)



Probability for bond rupture (Arrhenius relation)  $f = f_{AP}$ 

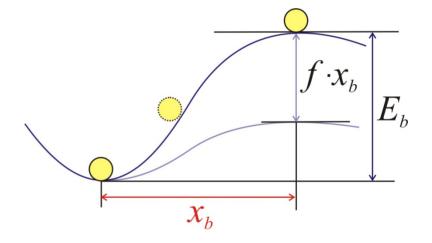


Probability for bond rupture (Arrhenius relation)

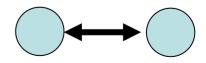
$$p = \exp\left(-\frac{E_b - f \cdot x_B}{k_B T}\right)$$

Off-rate = probability times vibrational frequency

$$\chi = \omega_0 \cdot p$$



 $\omega_0 = 1 \times 10^{13} \, 1 / \text{sec}$ 



bond vibrations

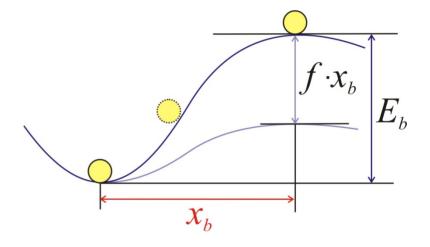
Probability for bond rupture (Arrhenius relation)

$$p = \exp\left(-\frac{E_b - f \cdot x_B}{k_B T}\right)$$

Off-rate = probability times vibrational frequency

$$\chi = \omega_0 \cdot p = \omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right)$$

"How often bond breaks per unit time"



 $\omega_0 = 1 \times 10^{13} \, 1/\mathrm{sec}$ 



bond vibrations

Probability for bond rupture (Arrhenius relation)

$$p = \exp\left(-\frac{E_b - f \cdot x_B}{k_B T}\right)$$

Off-rate = probability times vibrational frequency

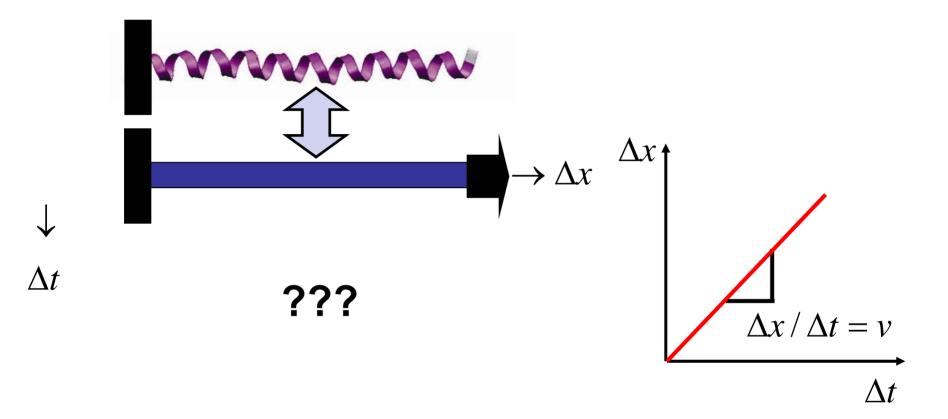
$$\chi = \omega_0 \cdot p = \omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) = \frac{1}{\tau} \qquad \omega_0 = 1 \times 10^{13} \, 1/\sec^2$$

 $au = ext{bond lifetime}$ (inverse of off-rate)

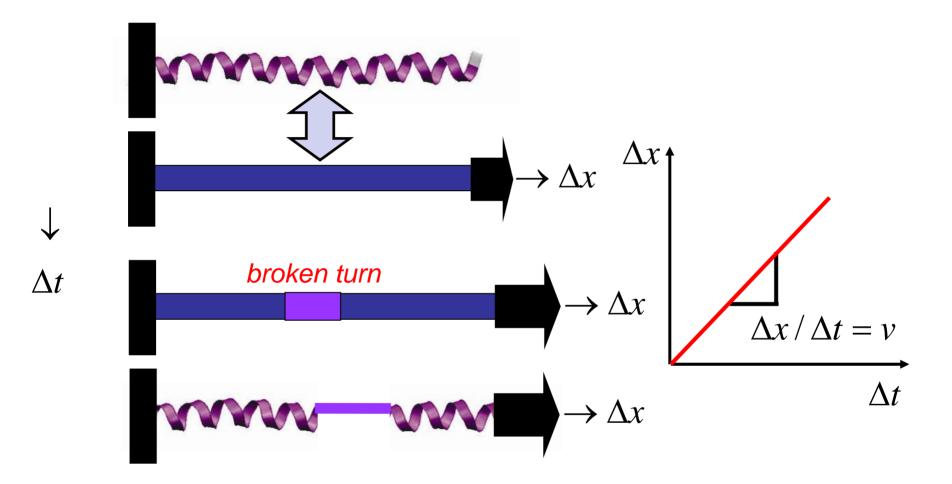
 $X_{b}$ 

 $f \cdot x_b$ 

 $E_{h}$ 

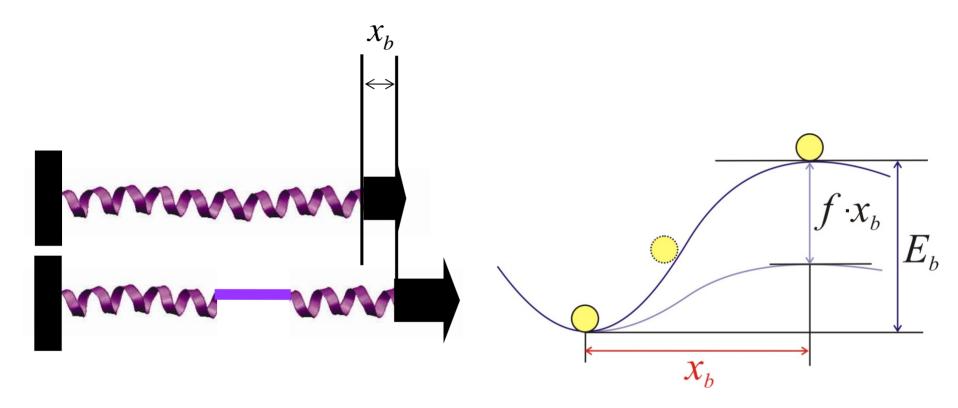


#### $\Delta x / \Delta t = v$ pulling speed (at end of molecule)

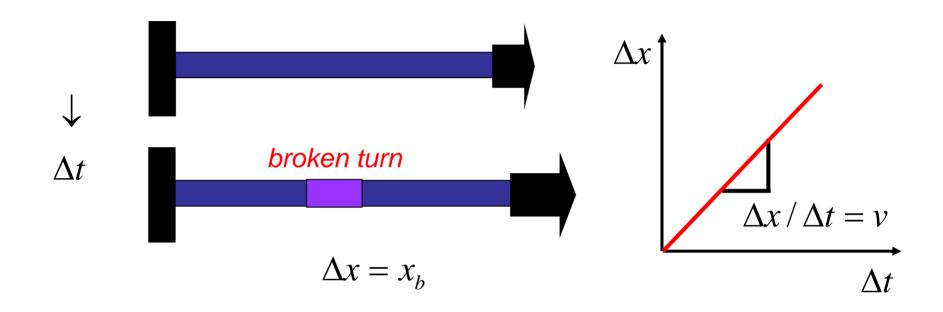


 $\Delta x / \Delta t = v$  pulling speed (at end of molecule)

## Structure-energy landscape link



$$\Delta x = x_b$$
  
$$\Delta t = \tau \qquad \tau = \left[\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right)\right]^{-1}$$



Bond breaking at  $x_b$  (lateral applied displacement):

Bell model  

$$\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = v$$

Solve this expression for f:

$$\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = v$$

Solve this expression for f:

$$-\frac{(E_{b}-f\cdot x_{b})}{k_{b}\cdot T} + \ln(\omega_{0}\cdot x_{b}) = \ln v \quad \text{in(..)}$$

$$-E_{b}+f\cdot x_{b} = k_{b}\cdot T\left(\ln v - \ln(\omega_{0}\cdot x_{b})\right)$$

$$f = \frac{E_{b}+k_{b}\cdot T\left(\ln v - \ln(\omega_{0}\cdot x_{b})\right)}{x_{b}} = \frac{k_{b}\cdot T}{x_{b}}\ln v + \frac{k_{b}\cdot T}{x_{b}}\left(\frac{E_{b}}{k_{b}\cdot T} - \ln(\omega_{0}\cdot x_{b})\right)$$

$$f = \frac{k_{b}\cdot T}{x_{b}}\ln v - \frac{k_{b}\cdot T}{x_{b}}\left(\ln(\omega_{0}\cdot x_{b}) - \frac{E_{b}}{k_{b}\cdot T}\right)$$

$$f = \frac{k_{b}\cdot T}{x_{b}}\ln v - \frac{k_{b}\cdot T}{x_{b}}\ln\left(\omega_{0}\cdot x_{b}\cdot \exp\left(-\frac{E_{b}}{k_{b}\cdot T}\right)\right)$$

$$43$$

## Simplification and grouping of variables

Only system parameters, [distance/length]

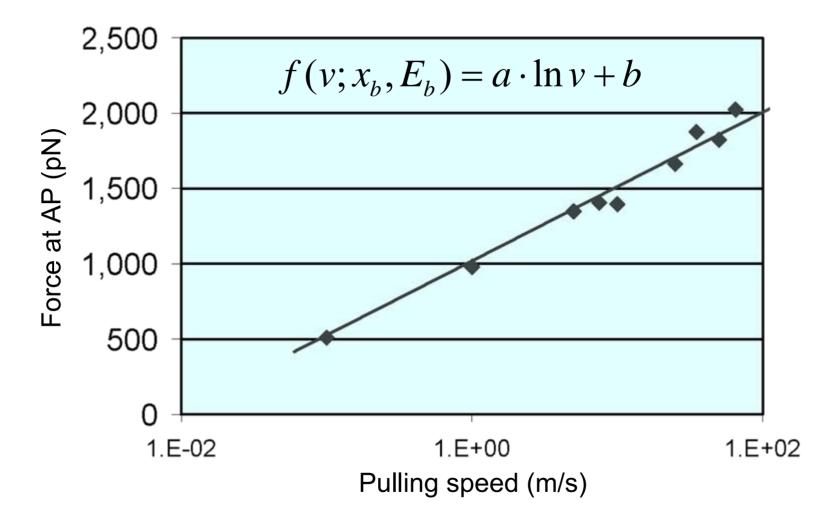
$$f(v; x_b, E_b) = \frac{k_b \cdot T}{x_b} \cdot \ln v - \frac{k_b \cdot T}{x_b} \cdot \ln \left( \omega_0 \cdot x_b \cdot \exp\left(-\frac{E_b}{k_b \cdot T}\right) \right)$$
$$=: v_0 = \omega_0 \cdot x_b \cdot \exp\left(-\frac{E_b}{k_b \cdot T}\right)$$

$$\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = v$$

Results in:

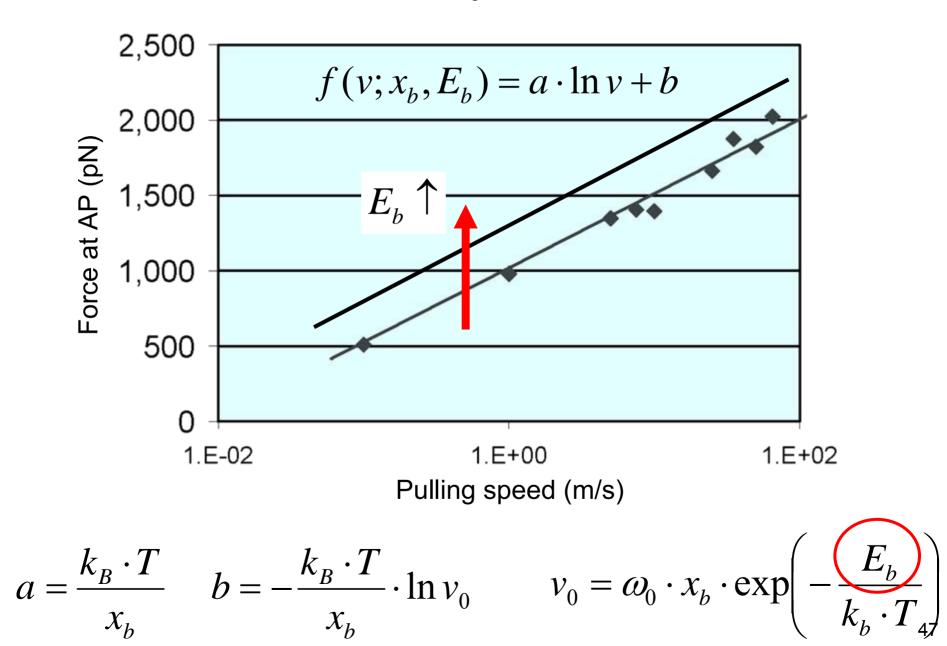
$$f(v; x_b, E_b) = \frac{k_b \cdot T}{x_b} \cdot \ln v - \frac{k_b \cdot T}{x_b} \cdot \ln v_0 = a \cdot \ln v + b$$
$$a = \frac{k_B \cdot T}{x_b}$$
$$b = -\frac{k_B \cdot T}{x_b} \cdot \ln v_0$$

## $f \sim \ln v$ behavior of strength

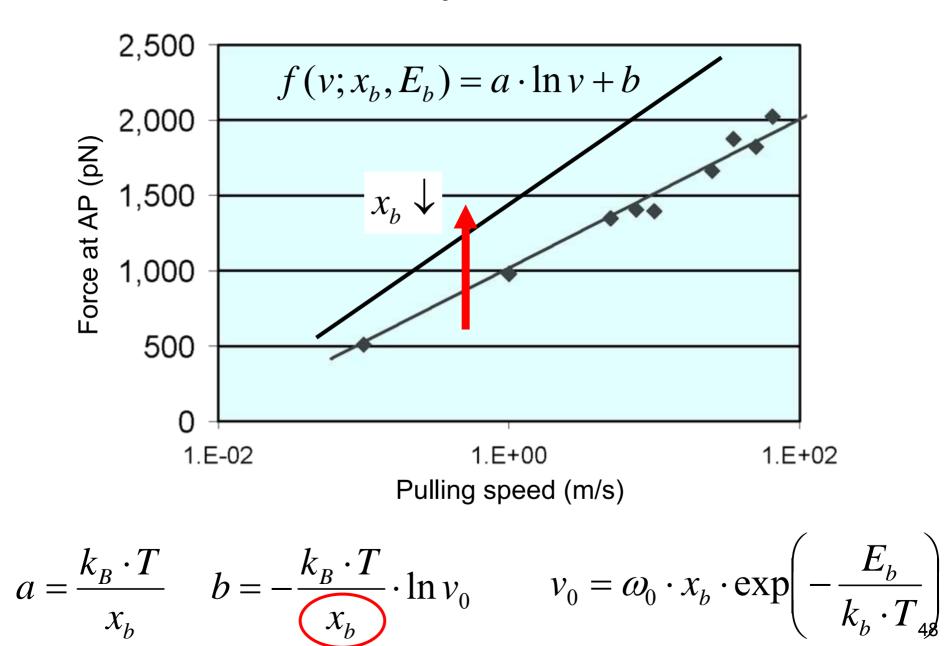


 $E_b = 5.6$  kcal/mol and  $x_b = 0.17$  Å (results obtained from fitting to the simulation data)

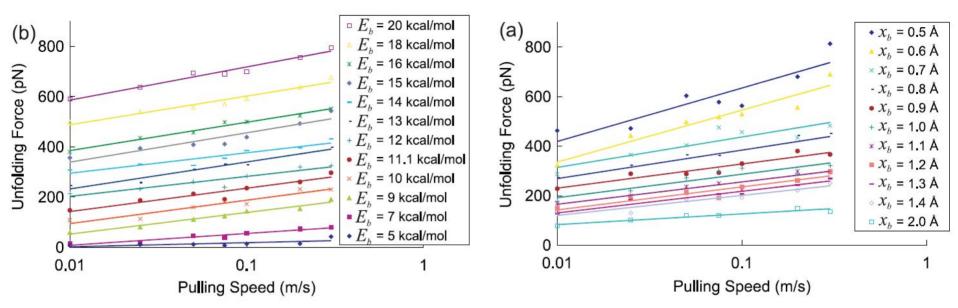
## Scaling with $E_b$ : shifts curve



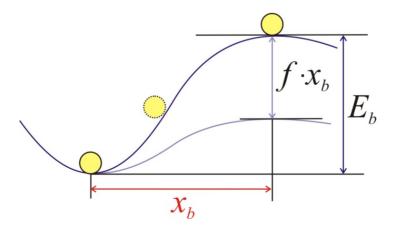
## Scaling with *x<sub>b</sub>*: changes slope



## Simulation results



Courtesy of IOP Publishing, Inc. Used with permission. Source: Fig. 3 from Bertaud, J., Hester, J. et al. "Energy Landscape, Structure and Rate Effects on Strength Properties of Alpha-helical Proteins." *J Phys.: Condens. Matter* 22 (2010): 035102. doi:10.1088/0953-8984/22/3/035102.



Bertaud, Hester, Jimenez, and Buehler, J. Phys. Cond. Matt., 2010

# Mechanisms associated with protein fracture

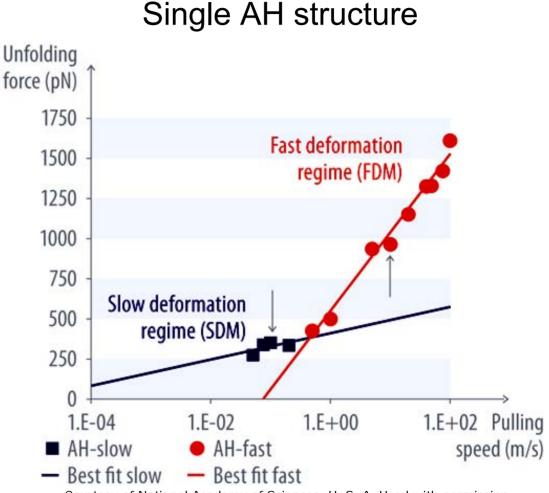
## Change in fracture mechanism

mm

**FDM**: Sequential HB breaking

**SDM**: Concurrent HB breaking (3..5 HBs)

Simulation span: 250 ns **Reaches deformation speed O(cm/sec)** 



Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Ackbarow, Theodor, et al. "Hierarchies, Multiple Energy Barriers, and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." PNAS 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.

## Analysis of energy landscape parameters

#### Table 1. Summary of the differences between the SDM and FDM, for AH1, AH2, and BS

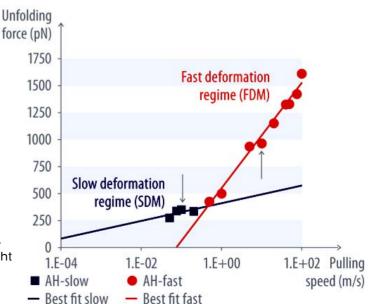
Parameter	AH1 (AH2) domain		BS domain	
	SDM	FDM	SDM	FDM
Pulling speed, m/s	v < 0.4 (4)	v > 0.4 (4)	<i>v</i> < 10	v > 10
Unfolding force, pN	F < 350 (400)	F > 350 (400)	<i>F</i> < 4,800	F > 4,800
E <sub>b</sub> , kcal/mol	11.1 (9.11)	4.87 (3.08)	11.08	1.82
x <sub>b</sub> , Å	1.2 (1.19)	0.2 (0.11)	0.138	0.019
HB-breaking mechanism	Simultaneous	Sequential	Simultaneous	Sequential

The values in parentheses in the AH columns represent the results for AH2.

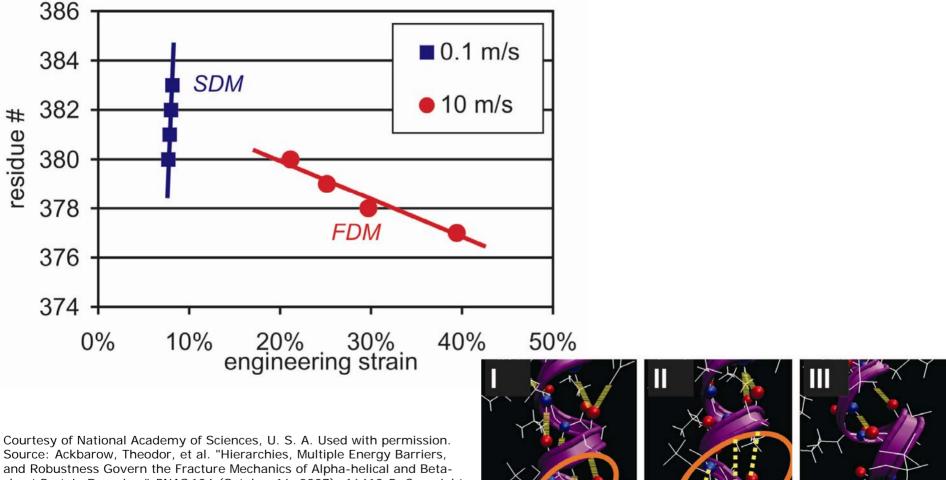
#### Energy single H-bond: ≈3-4 kcal/mol

#### What does this mean???

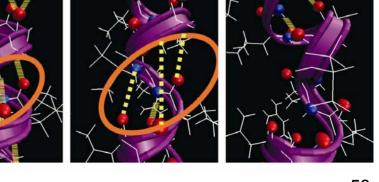
Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Ackbarow, Theodor, et al. "Hierarchies, Multiple Energy Barriers, and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.



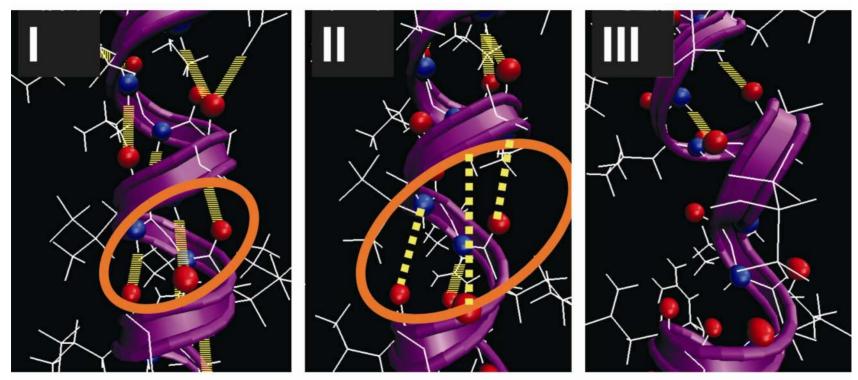
## H-bond rupture dynamics: mechanism



and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.



## H-bond rupture dynamics: mechanism



Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Ackbarow, Theodor, et al. "Hierarchies, Multiple Energy Barriers, and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.

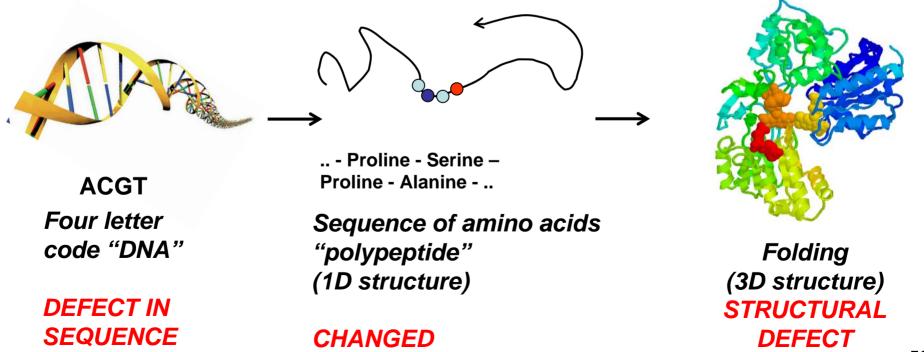
- I: All HBs are intact
- II: Rupture of 3 HBs simultaneously; within  $\tau \approx 20 \text{ ps}$
- III: Rest of the AH relaxes slower deformation...

3. Examples – materials and applications

E.g. disease diagnosis, mechanisms, etc.

# Genetic diseases – defects in protein materials

- Defect at DNA level causes structure modification
- Question: how does such a structure modification influence material behavior / material properties?



## Structural change in protein molecules can lead to fatal diseases

- Single point mutations in IF structure causes severe diseases such as rapid aging disease progeria – HGPS (*Nature*, 2003; *Nature*, 2006, *PNAS*, 2006)
- Cell nucleus loses stability under mechanical (e.g. cyclic) loading, failure occurs at heart (fatigue)

Genetic defect:

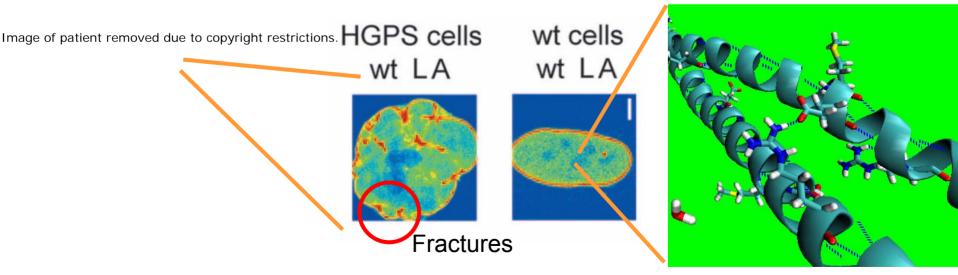
substitution of a single DNA base: Amino acid guanine is switched to adenine

Image of patient removed due to copyright restrictions.

## Structural change in protein molecules can lead to fatal diseases

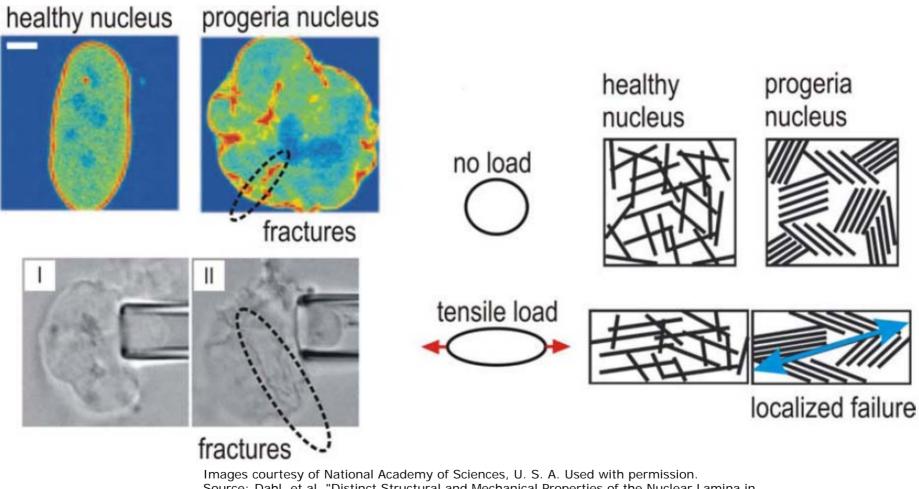
- Single point mutations in IF structure causes severe diseases such as rapid aging disease progeria – HGPS (*Nature*, 2003; *Nature*, 2006, *PNAS*, 2006)
- Cell nucleus loses stability under cyclic loading
- Failure occurs at heart (fatigue)

Experiment suggests that mechanical properties of nucleus change



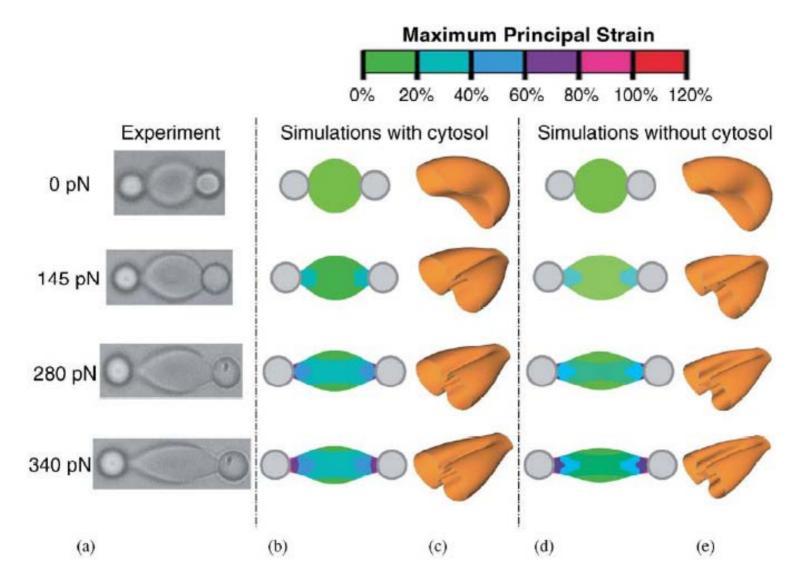
Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Dahl, et al. "Distinct Structural and Mechanical Properties of the Nuclear Lamina in Hutchinson–Gilford Progeria Syndrome." *PNAS* 103 (2006): 10271-6. Copyright 2006 National Academy of Sciences, U.S.A.

## Mechanisms of progeria



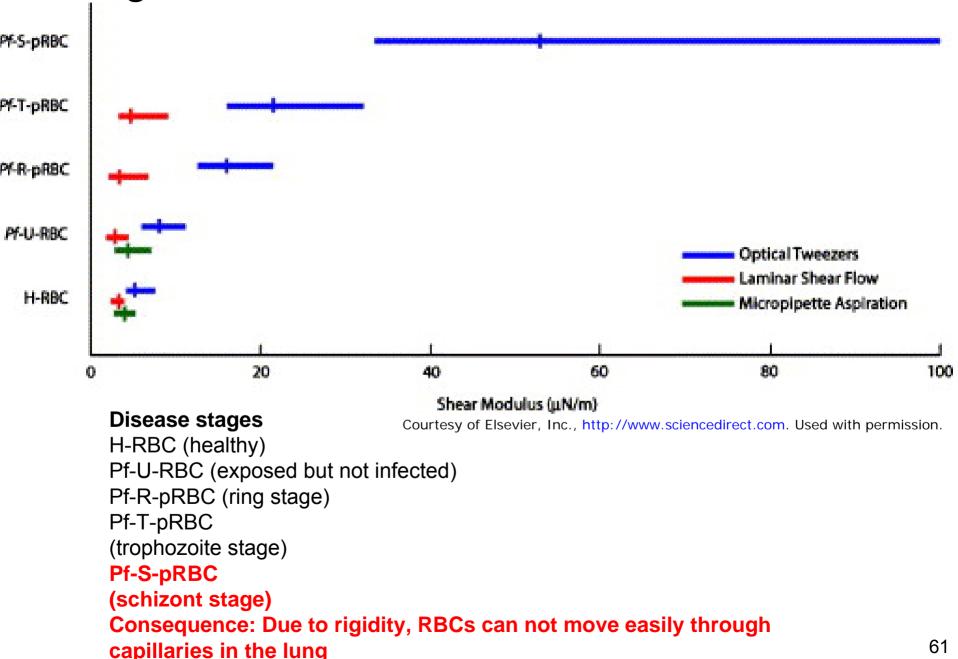
Source: Dahl, et al. "Distinct Structural and Mechanical Properties of the Nuclear Lamina in Hutchinson–Gilford Progeria Syndrome." *PNAS* 103 (2006): 10271-6. Copyright 2006 National Academy of Sciences, U.S.A.

### Deformation of red blood cells

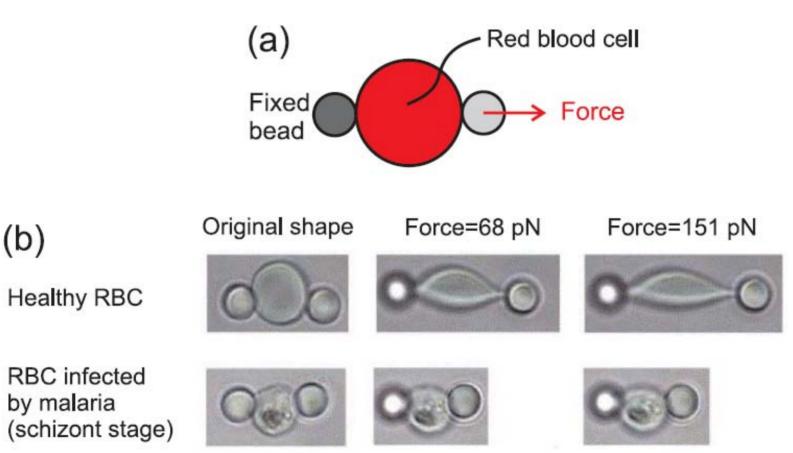


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## Stages of malaria and effect on cell stiffness

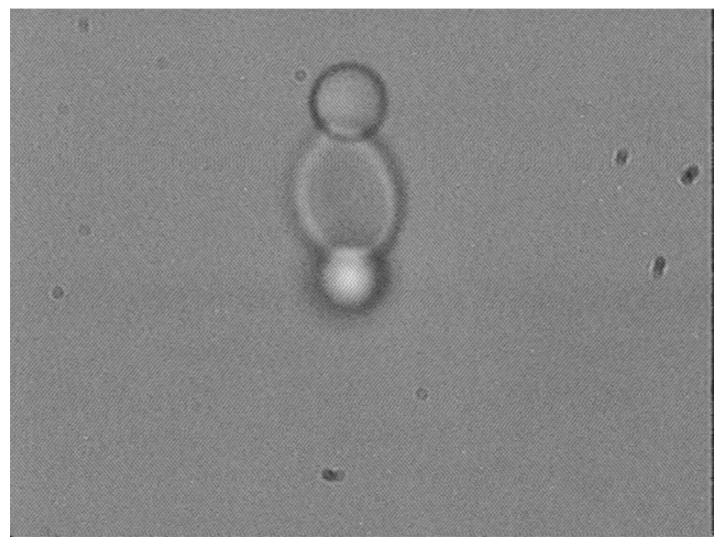


## **Cell deformation**



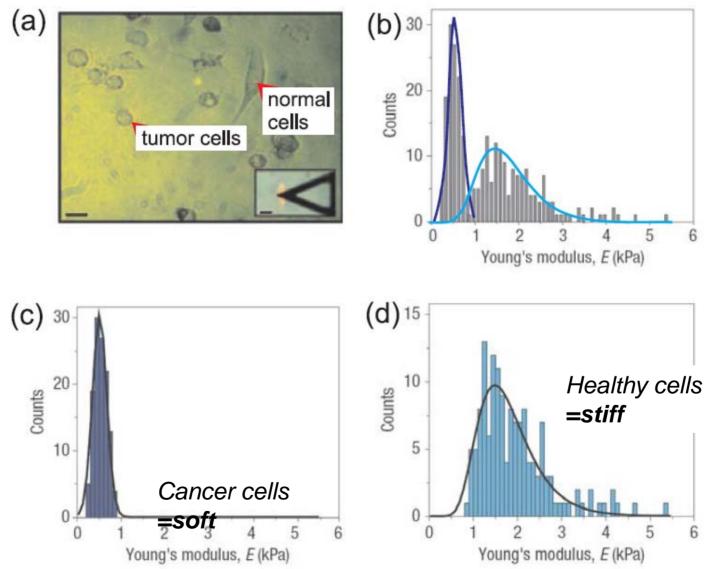
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## Deformation of red blood cells



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## Mechanical signature of cancer cells (AFM)



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