**1.021, 3.021, 10.333, 22.00 Introduction to Modeling and Simulation**

**Part I – Continuum and particle methods**

# **Applications to biophysics and bionanomechanics (cont'd)**

Lecture 11

Markus J. Buehler

**Laboratory for Atomistic and Molecular Mechanics Department of Civil and Environmental Engineering Massachusetts Institute of Technology**



**Massachusetts Institute of Technology** 

# Content overview



- Particle4. Quantum modeling of materials
- 5. From Atoms to Solids
- 6. Basic properties of materials
- 7. Advanced properties of materials
- 8. What else can we do?

# Overview: Material covered so far…

- $\blacksquare$ **Lecture 1: Broad introduction to IM/S**
- $\blacksquare$  **Lecture 2**: **Introduction to atomistic and continuum modeling** (multi-scale modeling paradigm, difference between continuum and atomistic approach, case study: diffusion)
- $\blacksquare$  **Lecture 3**: **Basic statistical mechanics – property calculation I** (property calculation: microscopic states vs. macroscopic properties, ensembles, probability density and partition function)
- $\blacksquare$  **Lecture 4**: **Property calculation II** (Monte Carlo, advanced property calculation, introduction to chemical interactions)
- $\blacksquare$ **Lecture 5: How to model chemical interactions I (example: movie of copper** deformation/dislocations, etc.)
- $\blacksquare$ **Lecture 6: How to model chemical interactions II** (EAM, a bit of ReaxFF—chemical reactions)
- $\blacksquare$ **Lecture 7: Application to modeling brittle materials I**
- $\blacksquare$ **Lecture 8: Application to modeling brittle materials II**
- $\blacksquare$ **Lecture 9: Application – Applications to materials failure**
- $\blacksquare$ **Lecture 10: Applications to biophysics and bionanomechanics**
- Г **Lecture 11: Applications to biophysics and bionanomechanics (cont'd)**

### **Lecture 11: Applications to biophysics and bionanomechanics (cont'd)**

#### **Outline:**

- 1. Force fields for proteins: (brief) review
- 2. Fracture of protein domains Bell model
- 3. Examples materials and applications

### **Goal of today's lecture:**

- ٠ Fracture model for protein domains: "Bell model"
- $\blacksquare$  Method to apply loading in molecular dynamics simulation (nanomechanics of single molecules)
- Applications to disease and other aspects

1. Force fields for proteins: (brief) review

# Chemistry, structure and properties are linked

**Chemical structure**



#### **Presence of various chemical bonds:**

- Covalent bonds (C-C, C-O, C-H, C-N..)
- Electrostatic interactions (charged amino acid side chains)
- H-bonds (e.g. between H and O)
- vdW interactions (uncharged parts of molecules)

### Model for covalent bonds

$$
\phi_{\text{stretch}} = \frac{1}{2} k_{\text{stretch}} (r - r_0)^2
$$
\n
$$
\phi_{\text{bend}} = \frac{1}{2} k_{\text{bend}} (\theta - \theta_0)^2
$$
\n
$$
\phi_{\text{rot}} = \frac{1}{2} k_{\text{rot}} (1 - \cos(\theta))
$$

Courtesy of the EMBnet Education & Training Committee. Used with permission. Images created for the CHARMM tutorial by Dr. Dmitry Kuznetsov (Swiss Institute of Bioinformatics) for the EMBnet Education & Training committee ([http://www.embnet.org](http://www.embnet.org/))

#### [http://www.ch.embnet.org/MD\\_tutorial/pages/MD.Part2.html](http://www.ch.embnet.org/MD_tutorial/pages/MD.Part2.html) 7

**Summary: CHARMM potential (pset #3)**  
\n
$$
U_{total} = U_{Elec} + U_{covalent} + U_{yetallic} + U_{vdw} + U_{H-bond}
$$
\n
$$
U_{Elec}: \text{ Coulomb potential } \phi(r_{ij}) = \frac{q_i q_j}{\varepsilon_i r_{ij}}
$$
\n
$$
U_{covalent} = U_{\text{stretch}} + U_{bend} + U_{rot} \begin{cases} \phi_{\text{stretch}} = \frac{1}{2} k_{\text{stretch}} (r - r_0)^2 \\ \phi_{\text{total}} = \frac{1}{2} k_{\text{bend}} (\theta - \theta_0)^2 \\ \phi_{\text{rot}} = \frac{1}{2} k_{\text{rot}} (1 - \cos(\theta)) \end{cases}
$$
\n
$$
U_{vdw}: \text{ LJ potential } \phi(r_{ij}) = 4\varepsilon \left[ \left( \frac{\sigma}{r_{ij}} \right)^{12} - \left( \frac{\sigma}{r_{ij}} \right)^{6} \right]
$$
\n
$$
U_{H-bond}: \phi(r_{ij}) = D_{H-bond} \left[ 5 \left( \frac{R_{H-bond}}{r_{ij}} \right)^{12} - 6 \left( \frac{R_{H-bond}}{r_{ij}} \right)^{10} \right] \cos^4(\theta_{\text{DHA}})
$$

# 2. Fracture of protein domains – Bell model

#### Experimental techniques



Courtesy of Elsevier, Inc., [http://www.sciencedirect.com](http://www.sciencedirect.com/). Used with permission.

### *How to apply load to a molecule*

*(in molecular dynamics simulations)*

# Steered molecular dynamics (SMD)

*Steered molecular dynamics used to apply forces to protein structures*



## Steered molecular dynamics (SMD)



### SMD mimics AFM single molecule experiments

#### *Atomic force microscope*



14

*SMD is a useful approach to probe the nanomechanics of proteins (elastic deformation, "plastic" – permanent deformation, etc.)*

*Example: titin unfolding (CHARMM force field)*

# Unfolding of titin molecule



Titin I27 domain: Very resistant to unfolding due to parallel H-bonded strands



Keten and Buehler, 2007

Force (pN)



# Protein unfolding - CHARMM



CHARMM modeling

Comparison – CHARMM vs. ReaxFF



M. Buehler, JoMMS, 2007

### *Application to alpha-helical proteins*

# Vimentin intermediate filaments

Image courtesy of Bluebie Pixie on Flickr. License: CC-BY.



## Alpha-helical protein: stretching



A: First H-bonds break (turns open)

- B: Stretch covalent backbone
- C: Backbone breaks

M. Buehler, JoMMS, 2007

#### Coarse-graining approach **Describe interaction between "beads" and not "atoms"**

Same concept as force fields for atoms

$$
U\left(\stackrel{\rightarrow}{R}\right) = U_T + U_B,
$$

$$
U_T = \sum_{pairs} \phi_T(r) \text{ and } U_B = \sum_{angles} \phi_B(\varphi).
$$

$$
\phi_B(\varphi) = \frac{1}{2} K_B (\varphi - \varphi_0)^2
$$

$$
\frac{\partial \phi_T}{\partial r}(r) = H(r_{break} - r) \begin{cases} k_T^{(1)}(r - r_0) & r_1 > r \\ R_1 + k_T^{(2)}(r - r_1) & r_1 \le r < r_2 \\ R_2 + R_1 + k_T^{(3)}(r - r_2) & r_2 \le r < r_3 \\ R_3 + R_2 + R_1 + k_T^{(4)}(r - r_3) & r_3 \le r \end{cases}
$$

#### See also:<http://dx.doi.org/10.1371/journal.pone.0006015>

## *Case study: From nanoscale filaments to micrometer meshworks*

# Movie: MD simulation of AH coiled coil

Image removed due to copyright restrictions. Please see <http://dx.doi.org/10.1103/PhysRevLett.104.198304>.

See also: Z. Qin, ACS Nano, 2011, and Z. Qin BioNanoScience, 2010.

## *What about varying pulling speeds?*

*Changing the time-scale of observation of fracture*

# Variation of pulling speed



Image by MIT OCW. After Ackbarow and Buehler, 2007.

Force at angular point $f_{\rm AP}$ =fracture force



### *General results…*

# Rupture force vs. pulling speed



Reprinted by permission from Macmillan Publishers Ltd: Nature Materials. Source: Buehler, M. ,and Yung, Y. "Chemomechanical Behaviour of Protein Constituents." *Nature Materials* 8, no. 3 (2009): 175-88. © 2009.

#### Buehler *et al*., *Nature Materials*, 2009

### *How to make sense of these results?*

# A few fundamental properties of bonds

- $\blacksquare$ Bonds have a "bond energy" (energy barrier to break)
- **EXTHERIANG PROXIMUS** Telationship gives probability for energy barrier to be overcome, given a temperature

$$
p = \exp\left(-\frac{E_b}{k_B T}\right)
$$

 $\blacksquare$ All bonds vibrate at frequency  $\omega$ 



Probability for bond rupture (Arrhenius relation)



Probability for bond rupture (Arrhenius relation)  $f=f_{\sf AP}$ 



Probability for bond rupture (Arrhenius relation)

$$
p = \exp\left(-\frac{E_b - f \cdot x_B}{k_B T}\right)
$$

Off-rate = probability times vibrational frequency

$$
\chi = \omega_0 \cdot p
$$



 $\omega_0 = 1 \times 10^{13}$  1/sec



bond vibrations

Probability for bond rupture (Arrhenius relation)

$$
p = \exp\left(-\frac{E_b - f \cdot x_B}{k_B T}\right)
$$

Off-rate = probability times vibrational frequency

$$
\chi = \omega_0 \cdot p = \omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right)
$$

*"How often bond breaks per unit time"*



 $\omega_0 = 1 \times 10^{13}$  1/sec



bond vibrations

Probability for bond rupture (Arrhenius relation)

$$
p = \exp\left(-\frac{E_b - f \cdot x_B}{k_B T}\right)
$$

Off-rate = probability times vibrational frequency

$$
\chi = \omega_0 \cdot p = \omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) = \frac{1}{\tau} \qquad \omega_0 = 1 \times 10^{13} \text{ 1/sec}
$$

 $\tau =$  bond lifetime (inverse of off-rate)

 $\mathcal{X}_h$ 

 $f x_h$ 

 $E_{_h}$ 



#### $\Delta x\,/\,\Delta t = v \quad$  pulling speed (at end of molecule)



 $\Delta x\,/\,\Delta t = v \quad$  pulling speed (at end of molecule)

# Structure-energy landscape link



$$
\Delta x = x_b
$$
  
\n
$$
\Delta t = \tau \qquad \tau = \left[ \omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \right]^{-1}
$$



Bond breaking at  $\ x_{b}$  (lateral applied displacement):

$$
\chi \cdot x_b = \omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = \Delta x / \Delta t = v
$$
  
= 1/ $\tau$  pulling speed

Bell model  

$$
\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = v
$$

Solve this expression for *f* :

$$
\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = v
$$

Solve this expression for *f* :

$$
-\frac{(E_b - f \cdot x_b)}{k_b \cdot T} + \ln(\omega_0 \cdot x_b) = \ln v \longleftarrow \ln(.)
$$
  
\n
$$
-E_b + f \cdot x_b = k_b \cdot T (\ln v - \ln(\omega_0 \cdot x_b))
$$
  
\n
$$
f = \frac{E_b + k_b \cdot T (\ln v - \ln(\omega_0 \cdot x_b))}{x_b} = \frac{k_b \cdot T}{x_b} \ln v + \frac{k_b \cdot T}{x_b} \left(\frac{E_b}{k_b \cdot T} - \ln(\omega_0 \cdot x_b)\right)
$$
  
\n
$$
f = \frac{k_b \cdot T}{x_b} \ln v - \frac{k_b \cdot T}{x_b} \left(\ln(\omega_0 \cdot x_b) - \frac{E_b}{k_b \cdot T}\right)
$$
  
\n
$$
f = \frac{k_b \cdot T}{x_b} \ln v - \frac{k_b \cdot T}{x_b} \ln\left(\omega_0 \cdot x_b \cdot \exp\left(-\frac{E_b}{k_b \cdot T}\right)\right)
$$

# Simplification and grouping of variables

*Only system parameters, [distance/length]*

$$
f(v; x_b, E_b) = \frac{k_b \cdot T}{x_b} \cdot \ln v - \frac{k_b \cdot T}{x_b} \cdot \ln \left( \omega_0 \cdot x_b \cdot \exp \left( - \frac{E_b}{k_b \cdot T} \right) \right)
$$

$$
=: v_0 = \omega_0 \cdot x_b \cdot \exp \left( - \frac{E_b}{k_b \cdot T} \right)
$$

$$
\omega_0 \cdot \exp\left(-\frac{(E_b - f \cdot x_b)}{k_b \cdot T}\right) \cdot x_b = v
$$

Results in:

$$
f(v; x_b, E_b) = \frac{k_b \cdot T}{x_b} \cdot \ln v - \frac{k_b \cdot T}{x_b} \cdot \ln v_0 = a \cdot \ln v + b
$$

$$
a = \frac{k_B \cdot T}{x_b}
$$

$$
b = -\frac{k_B \cdot T}{x_b} \cdot \ln v_0
$$

# $f\sim \ln v~$  behavior of strength



 $E_b$ = 5.6 kcal/mol and  $x_b$ = 0.17  $\rm \AA$  (results obtained from fitting to the simulation data)

### Scaling with  $E<sub>b</sub>$ : shifts curve



### Scaling with  $x<sub>b</sub>$ : changes slope



## Simulation results



Courtesy of IOP Publishing, Inc. Used with permission. Source: Fig. 3 from Bertaud, J., Hester, J. et al. "Energy Landscape, Structure and Rate Effects on Strength Properties of Alpha-helical Proteins." *J Phys.: Condens. Matter* 22 (2010): 035102. doi:10.1088/0953-8984/22/3/035102.



Bertaud, Hester, Jimenez, and Buehler, *J. Phys. Cond. Matt.,* 2010

## *Mechanisms associated with protein fracture*

# Change in fracture mechanism

WANN

**FDM**: Sequential HB breaking

**SDM**: Concurrent HB breaking (3..5 HBs)

**Simulation span: 250 ns Reaches deformation speed O(cm/sec)**



51Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Ackbarow, Theodor, et al. "Hierarchies, Multiple Energy Barriers, and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.

# Analysis of energy landscape parameters

#### Table 1. Summary of the differences between the SDM and FDM, for AH1, AH2, and BS



The values in parentheses in the AH columns represent the results for AH2.

#### Energy single H-bond: <sup>≈</sup>3-4 kcal/mol

#### *What does this mean???*

Courtesy of National Academy of Sciences, U. S. A. Used with permissi on. Source: Ackbarow, Theodor, et al. " Hierarchies, Multiple Energy Barriers, and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.



# H-bond rupture dynamics: mechanism



and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.



# H-bond rupture dynamics: mechanism



Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Ackbarow, Theodor, et al. "Hierarchies, Multiple Energy Barriers, and Robustness Govern the Fracture Mechanics of Alpha-helical and Betasheet Protein Domains." *PNAS* 104 (October 16, 2007): 16410-5. Copyright 2007 National Academy of Sciences, U.S.A.

- I: All HBs are intact
- II: Rupture of 3 HBs simultaneously; **within** τ <sup>≈</sup> **20 ps**
- III: Rest of the AH relaxes slower deformation…

3. Examples – materials and applications

*E.g. disease diagnosis, mechanisms, etc.*

# Genetic diseases – defects in protein materials

- $\blacksquare$ **Defect at DNA level causes structure modification**
- Question: how does such a structure modification influence material behavior / material properties?



### Structural change in protein molecules can lead to fatal diseases

- Single point mutations in IF structure causes severe diseases such as **rapid aging disease progeria – HGPS**  (*Nature*, 2003; *Nature*, 2006, *PNAS*, 2006)
- Cell nucleus loses stability under mechanical (e.g. cyclic) loading, failure occurs at heart (fatigue)

Genetic defect:

Image of patient removed due to copyright restrictions.

substitution of a single DNA base: Amino acid guanine is switched to adenine

### Structural change in protein molecules can lead to fatal diseases

- Single point mutations in IF structure causes severe diseases such as **rapid aging disease progeria – HGPS**  (*Nature*, 2003; *Nature*, 2006, *PNAS*, 2006)
- $\blacksquare$ Cell nucleus loses stability under cyclic loading
- Failure occurs at heart (fatigue)

Experiment suggests that mechanical properties of nucleus change



Courtesy of National Academy of Sciences, U. S. A. Used with permission. Source: Dahl, et al. "Distinct Structural and Mechanical Properties of the Nuclear Lamina in Hutchinson–Gilford Progeria Syndrome." *PNAS* 103 (2006): 10271-6. Copyright 2006 National Academy of Sciences, U.S.A.

# Mechanisms of *progeria*



Source: Dahl, et al. "Distinct Structural and Mechanical Properties of the Nuclear Lamina in Hutchinson–Gilford Progeria Syndrome." *PNAS* 103 (2006): 10271-6. Copyright 2006 National Academy of Sciences, U.S.A.

### Deformation of red blood cells



Courtesy of Elsevier, Inc., [http://www.sciencedirect.com](http://www.sciencedirect.com/). Used with permission.

### Stages of malaria and effect on cell stiffness



**capillaries in the lung**

# Cell deformation



 $(b)$ 

Courtesy of Elsevier, Inc., [http://www.sciencedirect.com](http://www.sciencedirect.com/). Used with permission.

# Deformation of red blood cells



Courtesy of Elsevier, Inc., [http://www.sciencedirect.com](http://www.sciencedirect.com/). Used with permission.

# Mechanical signature of cancer cells (AFM)



Reprinted by permission from Macmillan Publishers Ltd: Nature Nanotechnology. Source: Cross, S., Y. Jin, et al. "Nanomechanical Analysis of Cells from Cancer Patients." *Nature Nanotechnology* 2, no. 12 (2007): 780-3. © 2007.

3.021J / 1.021J / 10.333J / 18.361J / 22.00J Introduction to Modeling and Simulation Spring 2011

For information about citing these materials or our Terms of use, visit:<http://ocw.mit.edu/terms>.