1.021, 3.021, 10.333, 22.00 : Introduction to Modeling and Simulation : Spring 2011

Part II – Quantum Mechanical Methods : Lecture 7

#### Advanced Prop. of Materials: What else can we do?

Jeffrey C. Grossman



Department of Materials Science and Engineering Massachusetts Institute of Technology

## Part II Outline

#### theory & practice

- It's A Quantum World: The Theory of Quantum Mechanics
- 2. Quantum Mechanics: Practice Makes Perfect
- **3.** From Many-Body to Single-Particle; Quantum Modeling of Molecules
- **4.** From Atoms to Solids
- 5. Quantum Modeling of Solids: Basic Properties
- 6. Advanced Prop. of Materials: What else can we do?

#### example applications

#### 7. Nanotechnology

- 8. Solar Photovoltaics: Converting Photons into Electrons
- **9.** Thermoelectrics: Converting Heat into Electricity
- **10.** Solar Fuels: Pushing Electrons up a Hill
- I. Hydrogen Storage: the Strength of Weak Interactions

#### **12.** Review

#### Lesson outline

- Review some stuff
- Optical properties
- Magnetic properties
- Transport properties
- Vibrational properties

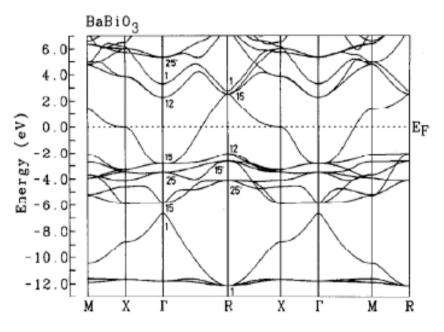
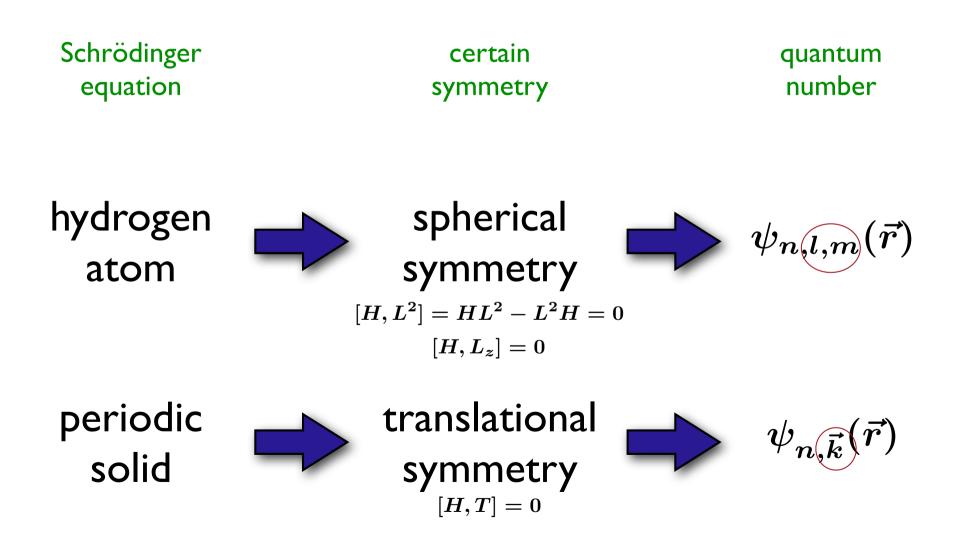
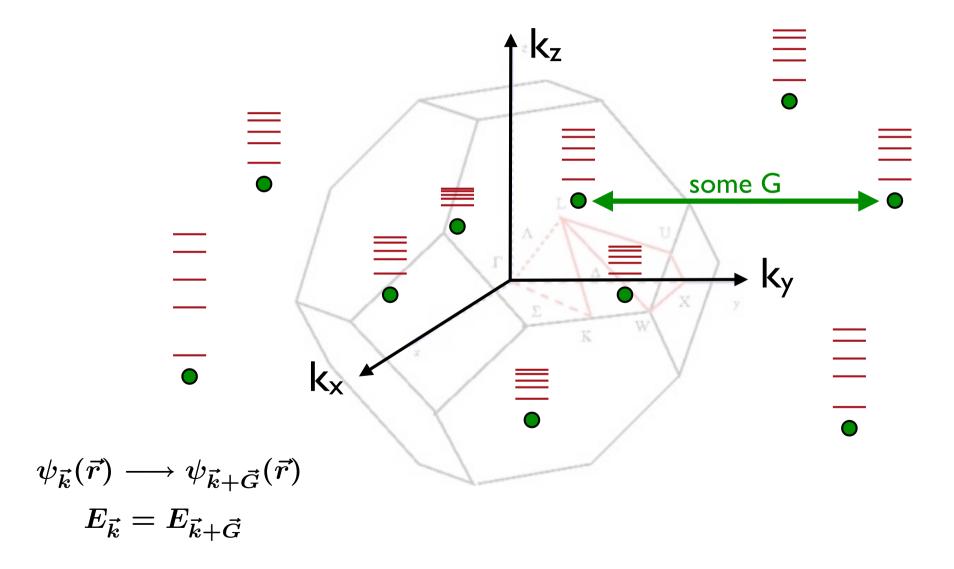


Fig. 3. Self-consistent APW energy band structure for BaBiO<sub>3</sub>.

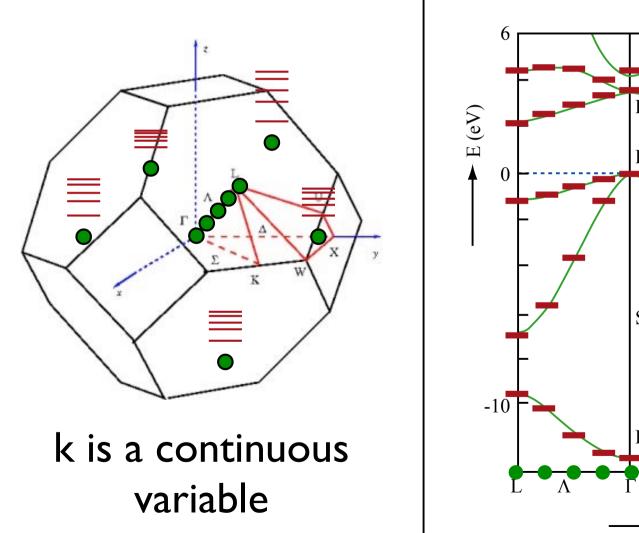
Courtesy of Elsevier, Inc., http://www.sciencedirect.com. Used with permission.





#### Review: The band structure

Silicon



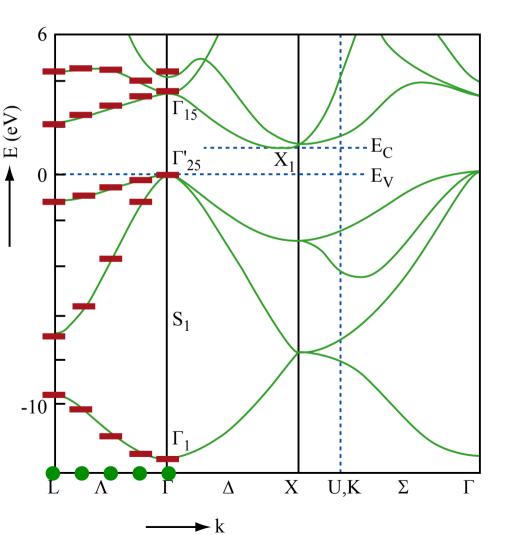
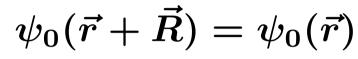
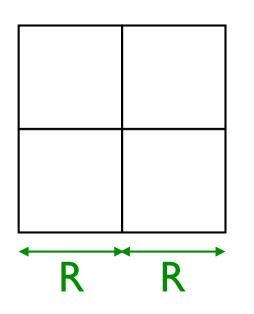


Image by MIT OpenCourseWare.



periodic over unit cell



R

$$\psi_{ec{G}/2}(ec{r}+2ec{R})=\psi_{ec{G}/2}(ec{r})$$

periodic over larger domain

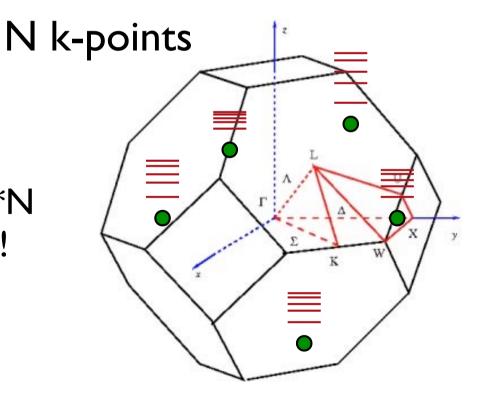
choose certain k-mesh e.g. 8x8x8 N=512

Π			
Π			
П			
П			
П			



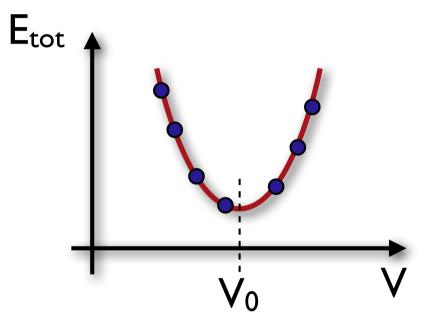
Distribute all electrons over the lowest states.

You have (electrons per unit cell)\*N electrons to distribute!



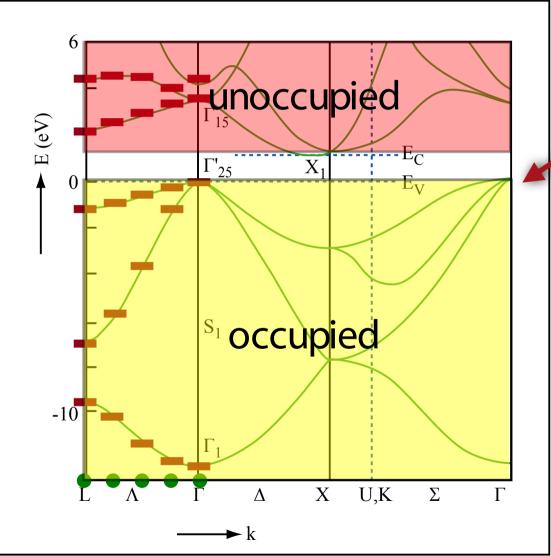
## Structural properties

finding the stress/pressure and the bulk modulus



$$p=-rac{\partial E}{\partial V} \qquad \sigma_{ ext{bulk}}=-Vrac{\partial p}{\partial V}=Vrac{\partial^2 E}{\partial V^2}$$

## The Fermi energy



Fermi energy

#### each band can hold:

2N electrons and you have (electrons per unit cell)\*N

#### or

two electrons and you have (electrons per unit cell)

Image by MIT OpenCourseWare.

## Electrical properties

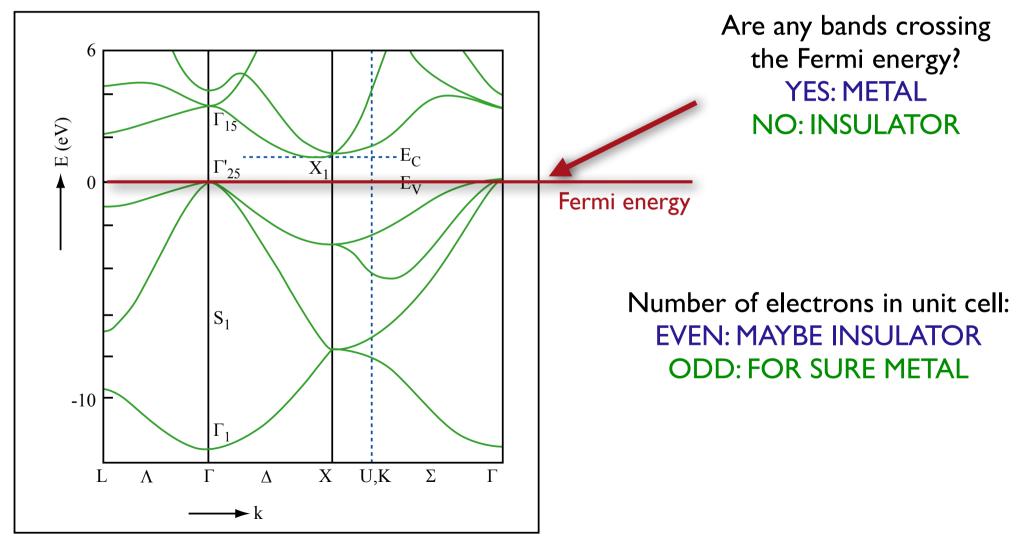
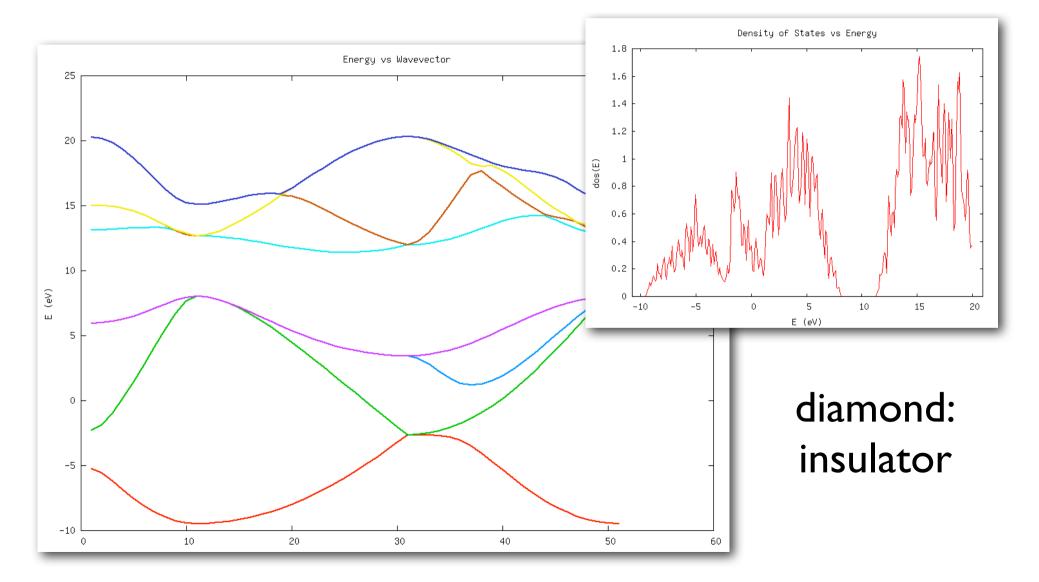
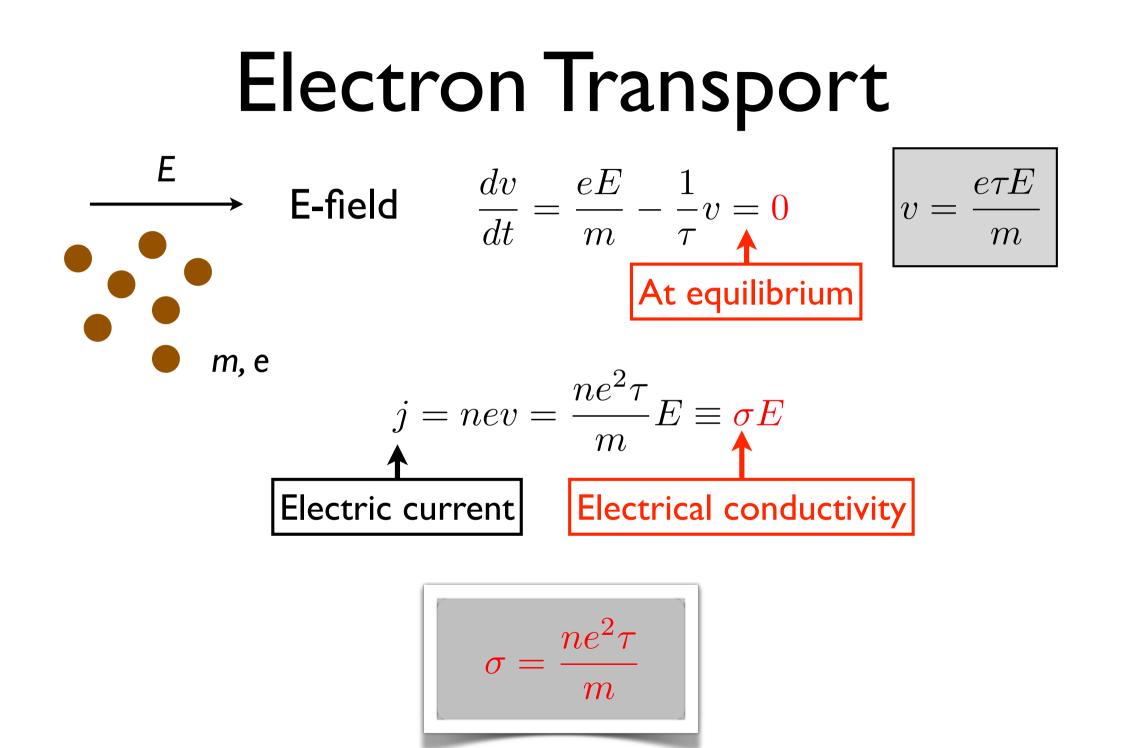


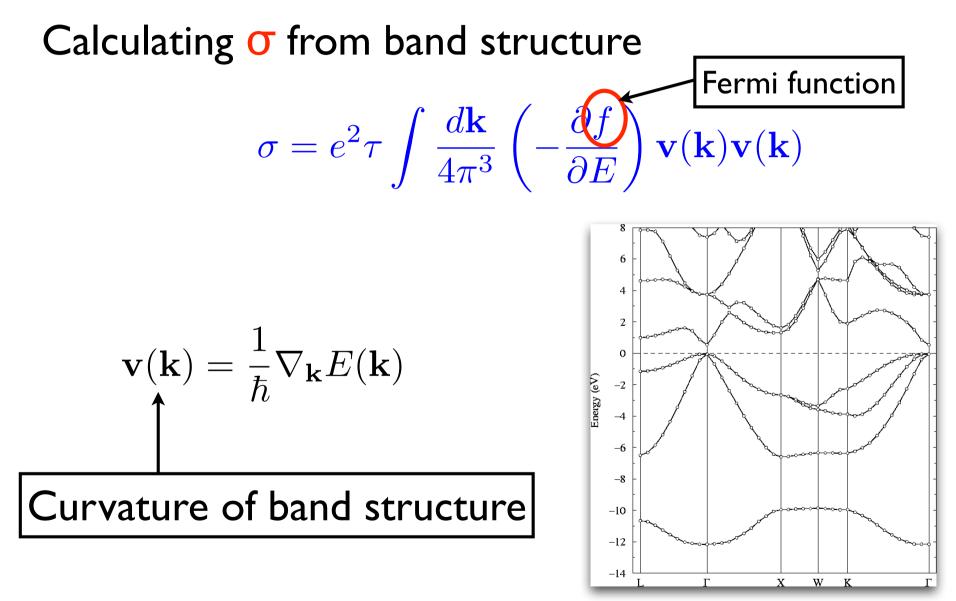
Image by MIT OpenCourseWare.

#### **Electrical properties**





#### **Electron Transport**



© source unknown. All rights reserved. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/fairuse.

#### Simple optical properties

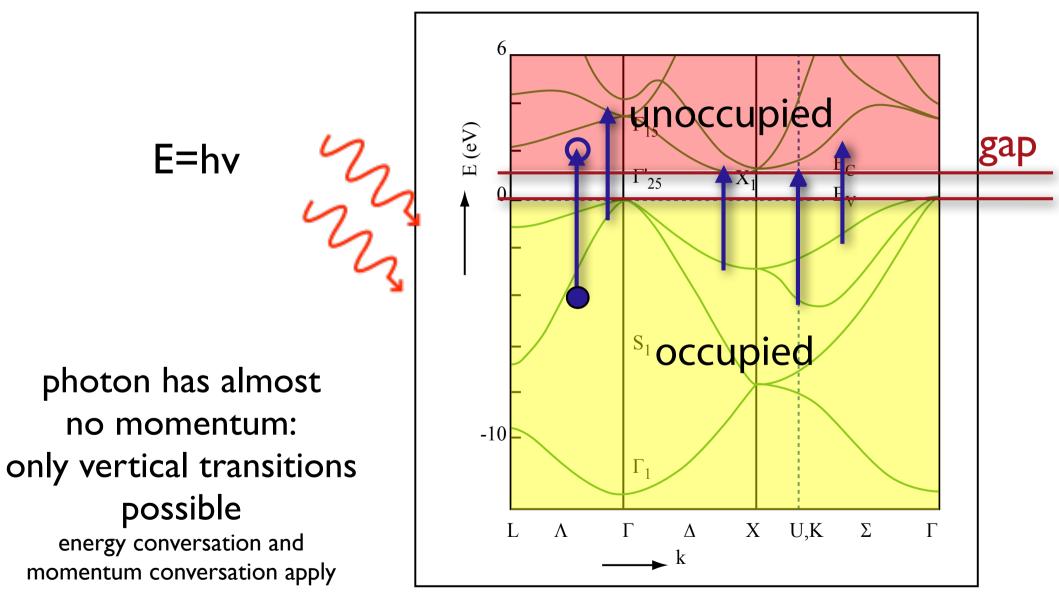


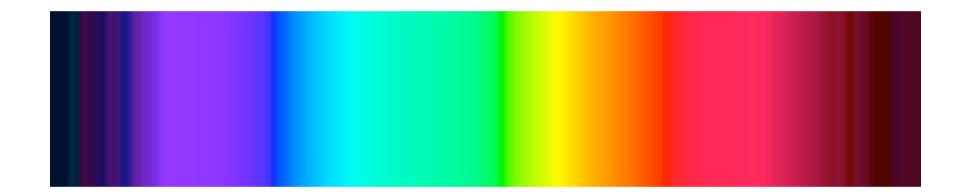
Image by MIT OpenCourseWare.

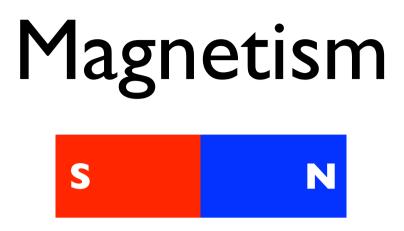
#### Silicon Solar Cells Have to Be Thick (\$\$\$)

It's all in the bandstructure!

Please see graph at http://www.tf.uni-kiel.de/matwis/amat/semi\_en/kap\_2/illustr/si\_banddiagram.gif.

## Simple optical properties



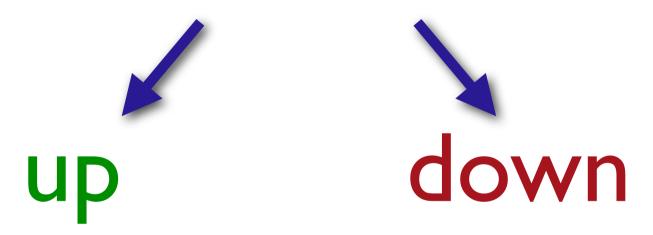


Origin of magnetism: electron spin An electron has a magnetic moment of  $\mu_B$ , Bohr magneton.

 $\oint_{\substack{n \uparrow \\ n_{\uparrow}}} \int_{\substack{n \downarrow}} \mu = \mu_B (n_{\uparrow} - n_{\downarrow})$ 

## Magnetization

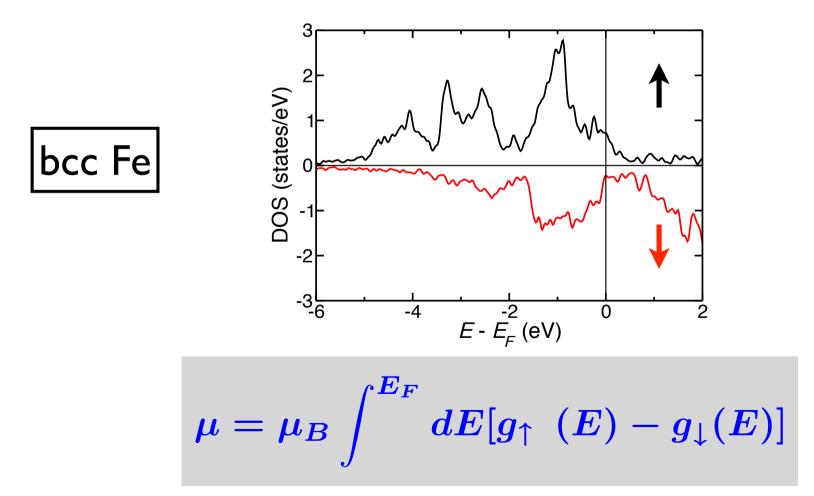
#### spin-polarized calculation: separate density for electrons with spin



Integrated difference between up and down density gives the magnetization.

#### Magnetism

In real systems, the density of states needs to be considered.



#### Quantum Molecular Dynamics



...and let us, as naturedirects, begin first withfirst principles.Aristotle (Poetics, I)

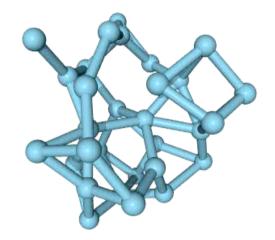


# F=ma $\int \frac{\partial E_n}{\partial \lambda} = \int \psi_n^* \frac{\partial \hat{H}}{\partial \lambda} \psi_n d\tau$

#### Carbon Nanotube Growth

Carbon nanotube growth: http://en.wikipedia.org/wiki/Carbon\_nanotube.

#### Silicon Nanocluster Growth



Silicon nanocluster growth: © source unknown. All rights reserved. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/fairuse.

#### Water

Henry Cavendish was the first to describe correctly the composition of water (2 H + I O), in 1781.

He reported his findings in terms of phlogiston (later the gas he made was proven to be hydrogen) and dephlogisticated air (later this was proven to be oxygen).

Cavendish was a pretty neat guy.

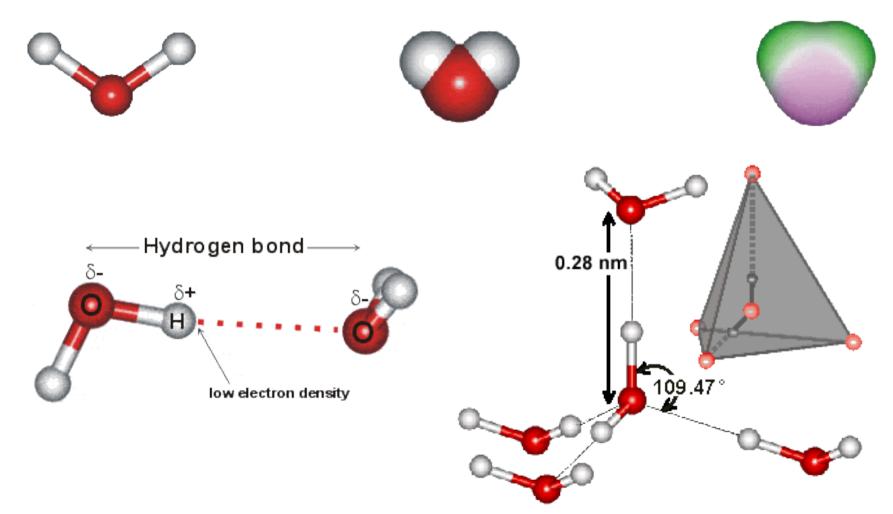


A University dropout, he also compared the conductivities of electrolytes and expressed a version of Ohm's law.

His last major work was the first measurement of Newton's gravitational constant, with the mass and density of the Earth. The accuracy of this experiment was not improved for a century.

#### Water

Which of the following is the correct picture for  $H_2O$ ?



© Martin Chaplin. License: CC-BY-SA-ND. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/fairuse.

Cool water site: http://www.lsbu.ac.uk/water/

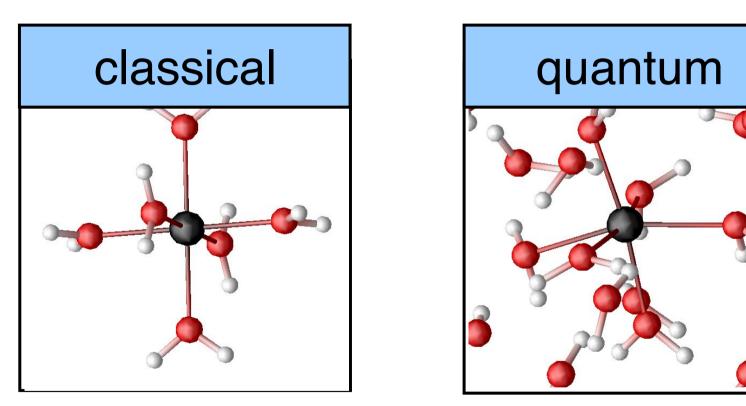
#### Classical or Quantum?

Please see the second table at <u>http://www.science.oregonstate.edu/~hetheriw/</u><u>astro/rt/info/water/water\_models.html</u>.

More than 50 classical potentials in use today for water.

Which one is best?

### Mg++ in Water

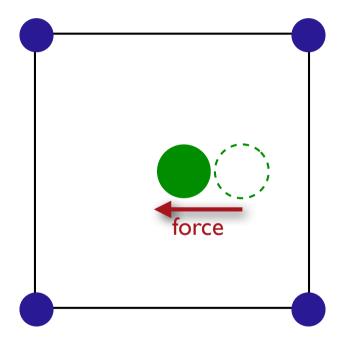


© Martin Chaplin. License: CC-BY-SA-ND. This content is excluded from our Creative Commons license. For more information, see http://ocw.mit.edu/fairuse.

#### **Important Differences!**

## Vibrational properties

## lattice vibrations are called: phonons



What is the frequency of this vibration?

## Vibrational properties

animated phonons on the web

http://dept.kent.edu/projects/ksuviz/ leeviz/phonon/phonon.html

- sound in solids determined by acoustical phonons (shock waves)
- some optical properties related to optical phonons
- heat capacity and transport related to phonons

## Summary of properties

structural properties

electrical properties

optical properties

magnetic properties

vibrational properties

#### Literature

- Charles Kittel, Introduction to Solid State Physics
- Ashcroft and Mermin, Solid State Physics
- wikipedia, "phonons", "lattice vibrations", ...

3.021J / 1.021J / 10.333J / 18.361J / 22.00J Introduction to Modeling and Simulation Spring 2011

For information about citing these materials or our Terms of use, visit: http://ocw.mit.edu/terms.