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2.626 Fundamentals of Photovoltaics  
Fall 2008

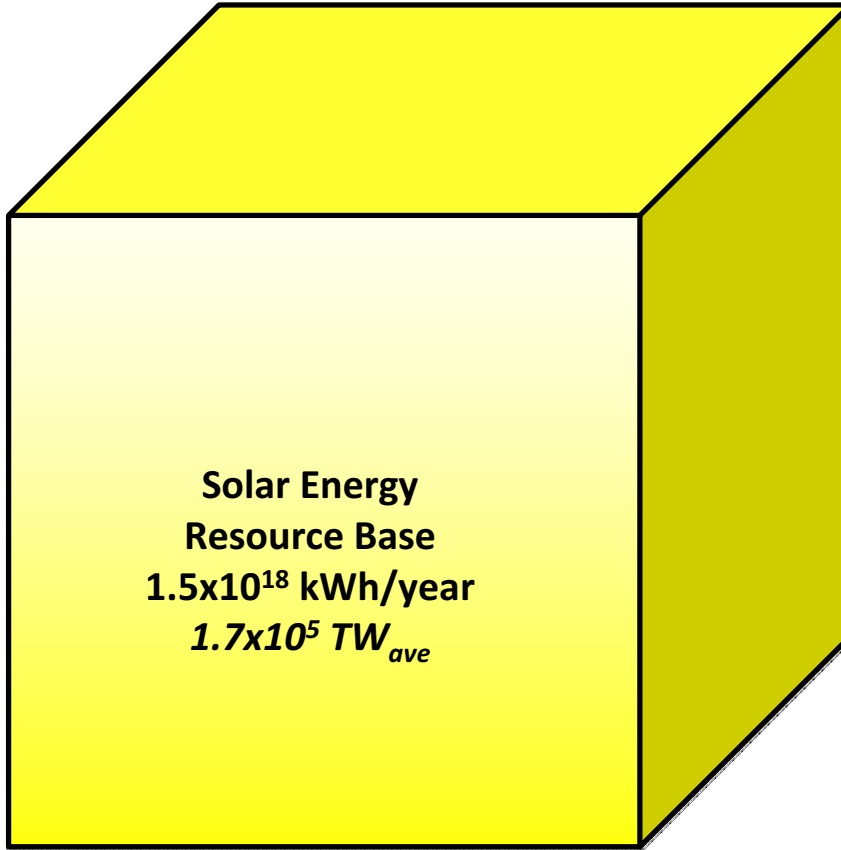
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# Solar Resource

Lecture 1 – 2.626

Tonio Buonassisi

# Solar Resource Base



**Wind Energy  
Resource Base**  
 $6 \times 10^{14}$  kWh/year  
 $72$  TW<sub>ave</sub>

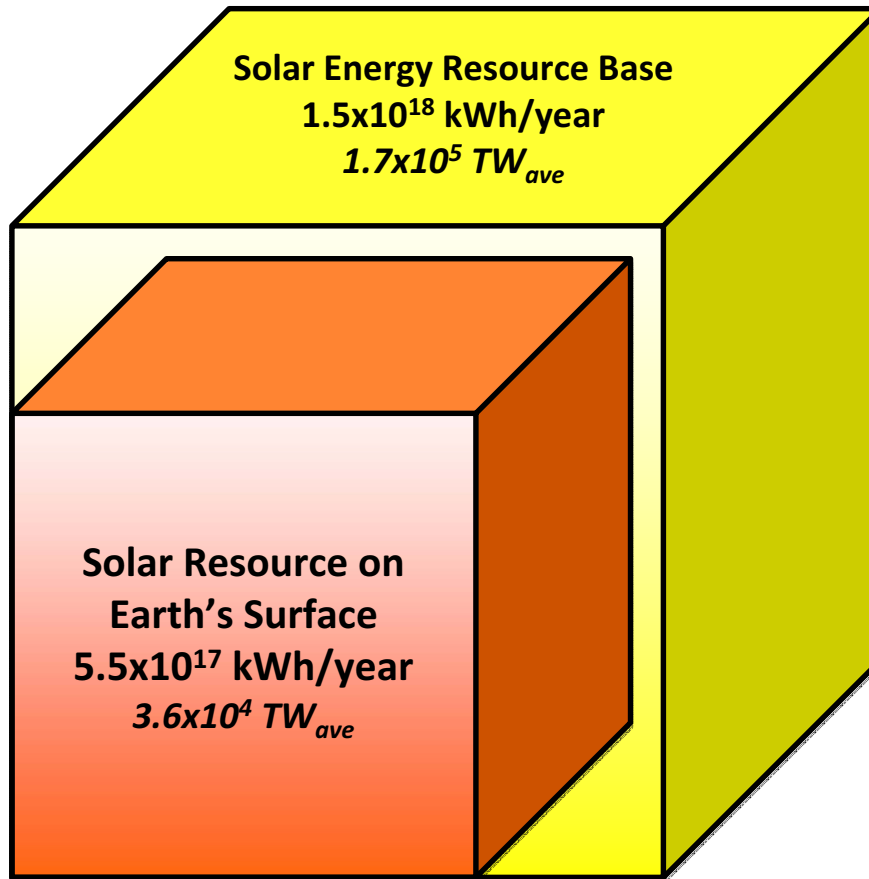


**Human Energy Use  
(mid- to late-century)**  
 $4 \times 10^{14}$  kWh/year  
 $50$  TW<sub>ave</sub>

## References:

Wind Energy: C.L. Archer and M.Z. Jacobson, *J. Geophys. Res.* **110**, D12110 (2005).

# Solar Resource Base



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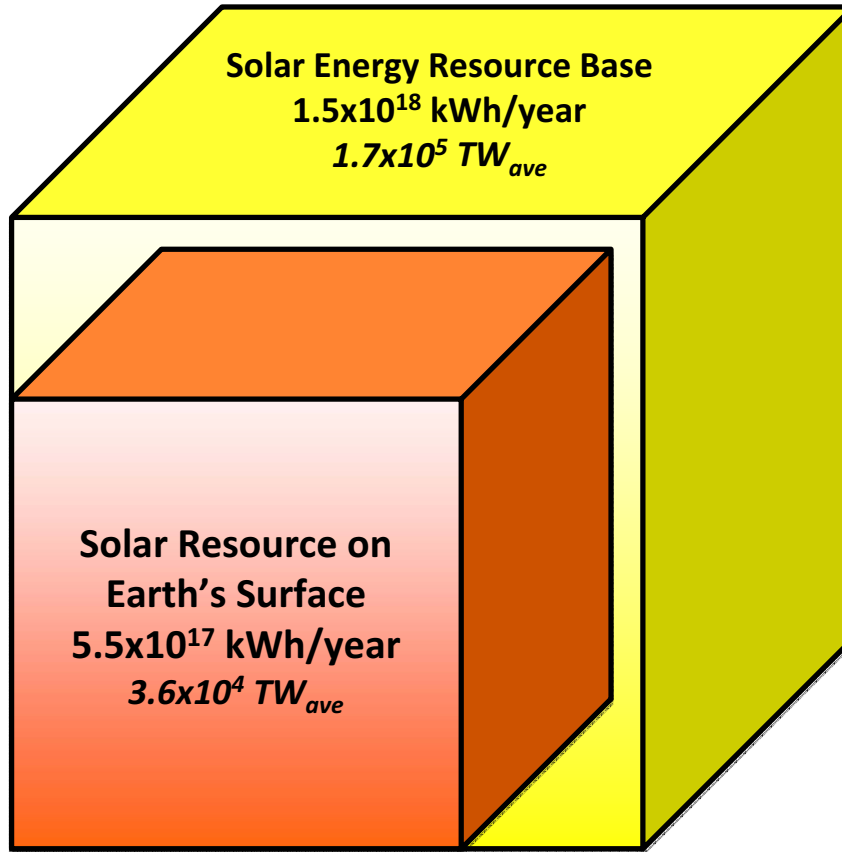


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# Solar Resource Base



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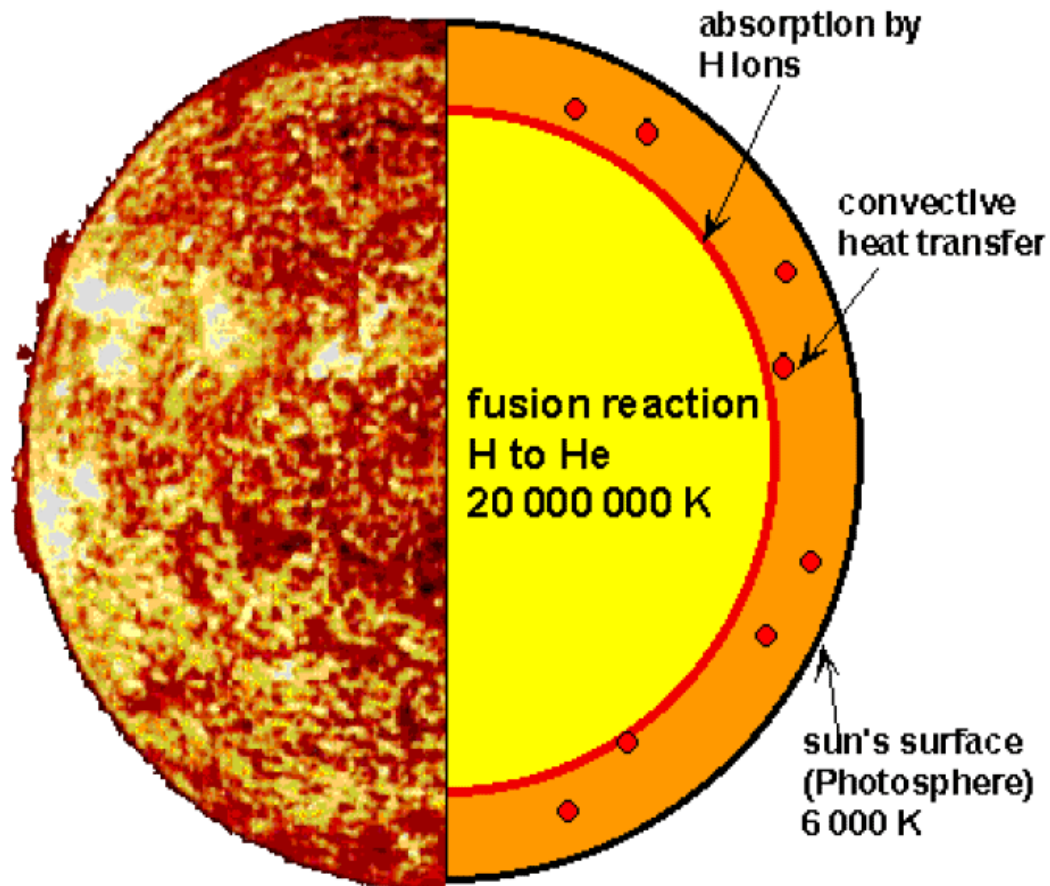
## References:

Wind Energy: C.L. Archer and M.Z. Jacobson, *J. Geophys. Res.* **110**, D12110 (2005).

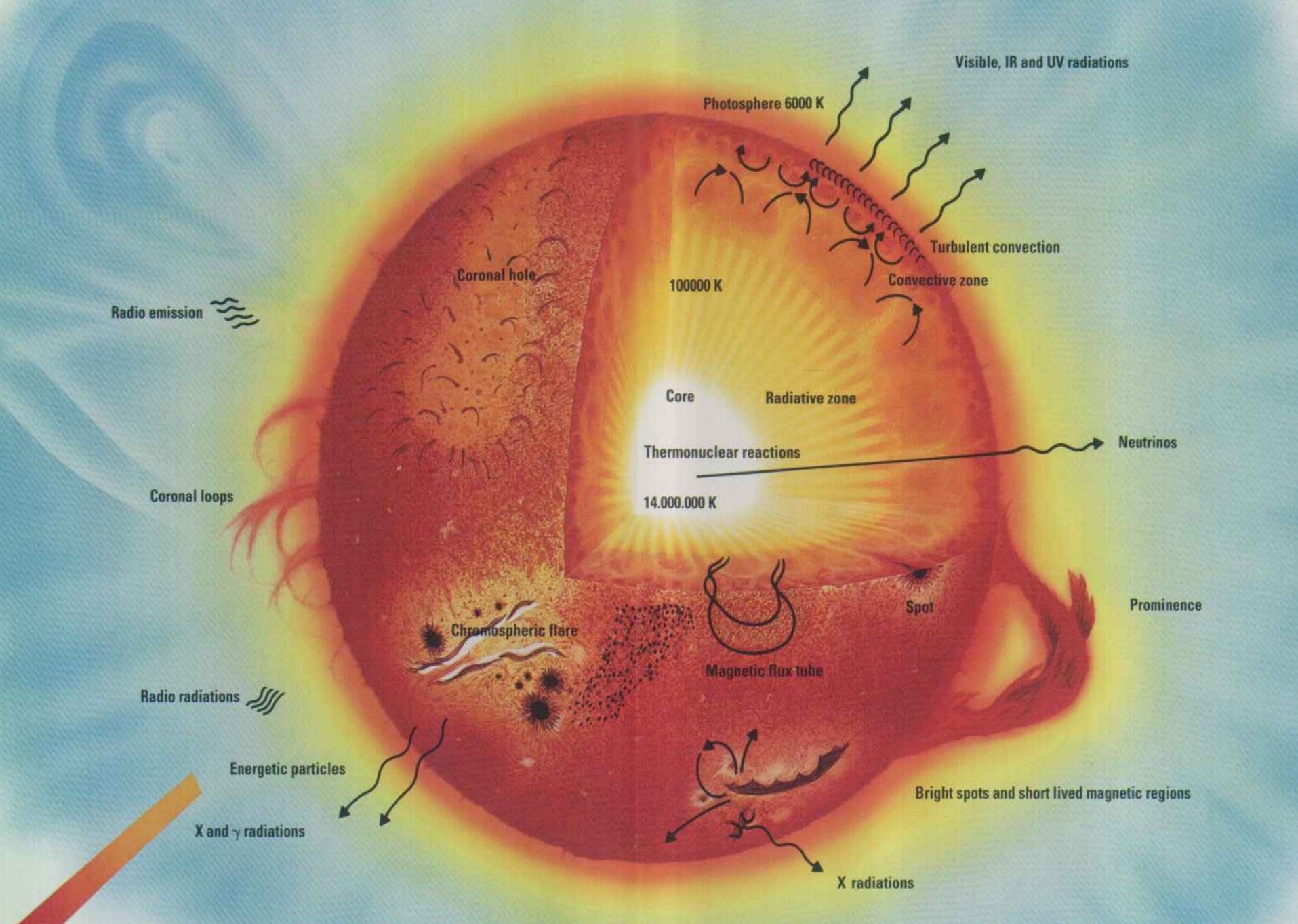
# The Sun

A nuclear fusion power plant ca.  $1.5 \times 10^8$  km ( $9.3 \times 10^7$  miles) away.

*All power and life on Earth, from photosynthesis to fossil fuels, originates from the Sun.*



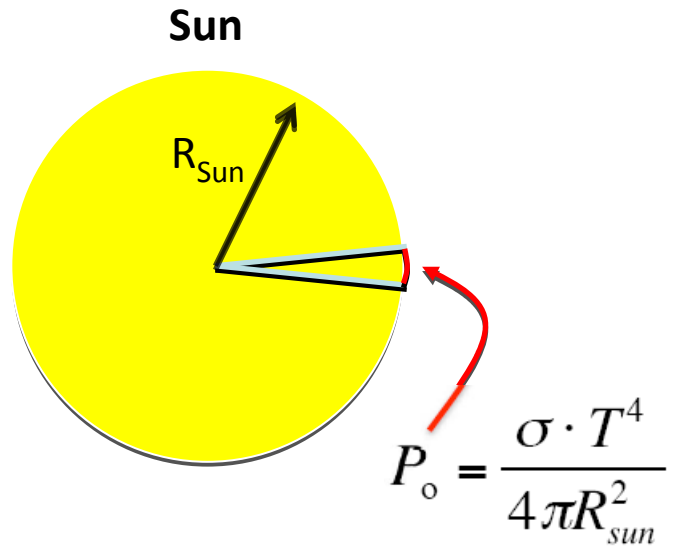
Courtesy Christiana Honsberg and Stuart Bowden. Used with permission.



Courtesy NASA.

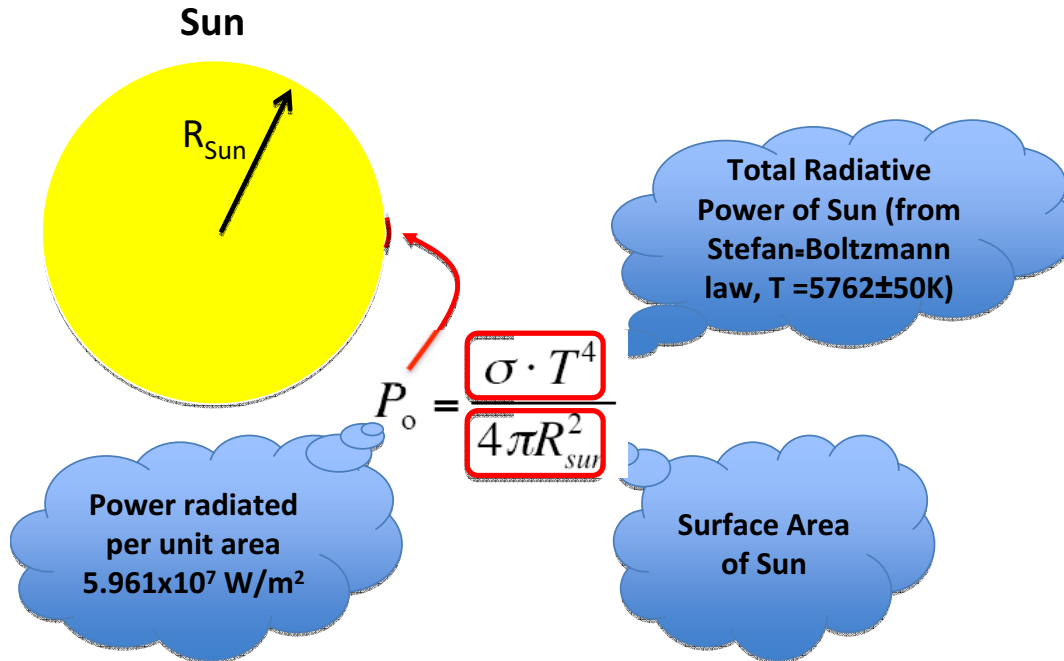
<http://www.solarviews.com/cap/sun/sundiag.htm>

# Quantifying Solar Power



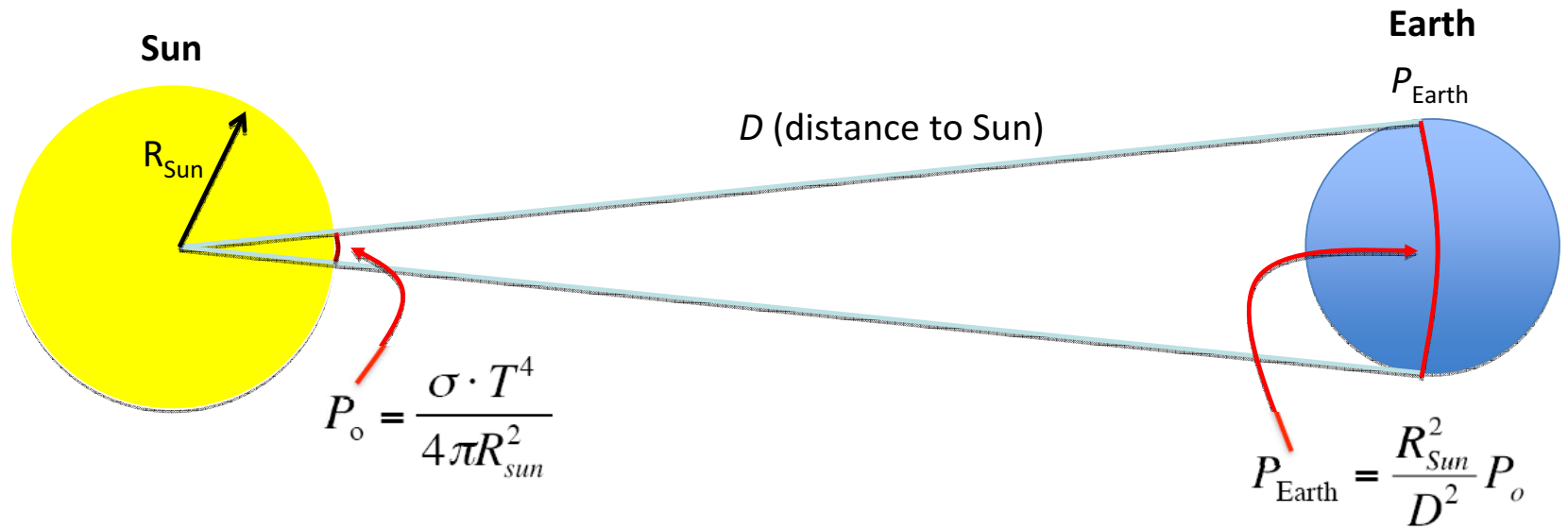


# Quantifying Solar Power



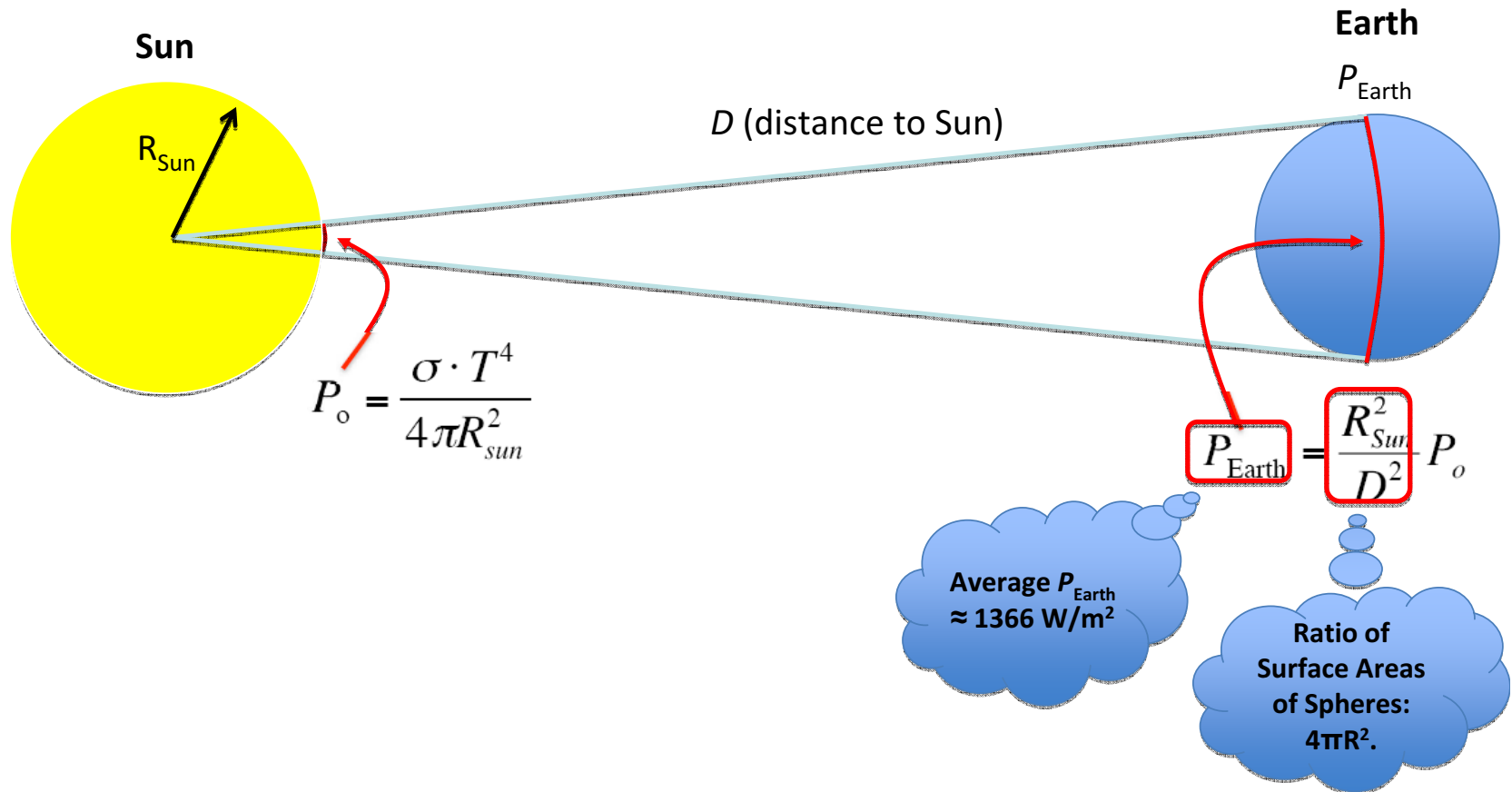
# Quantifying Solar Power

not to scale!



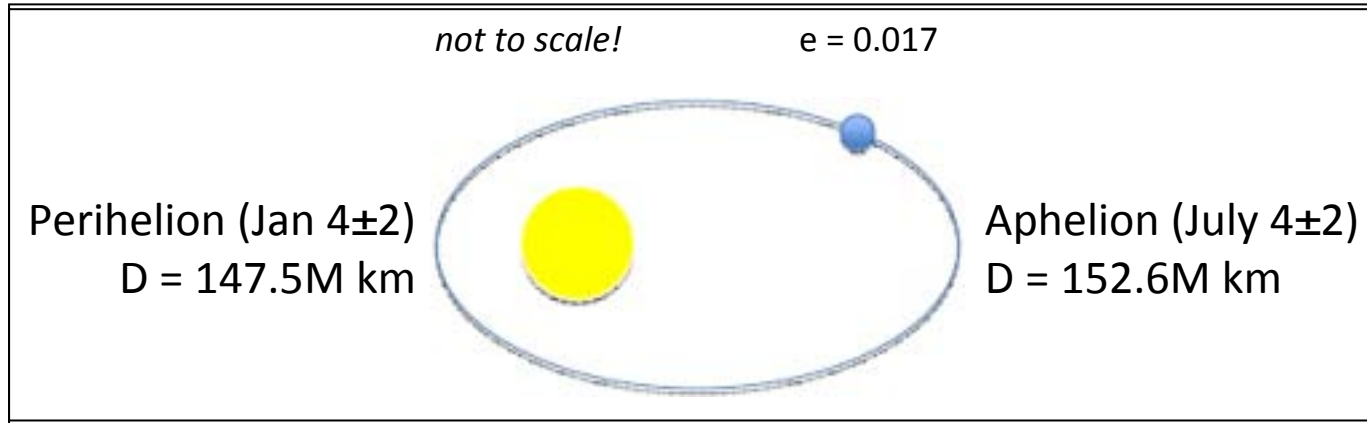
# Quantifying Solar Power

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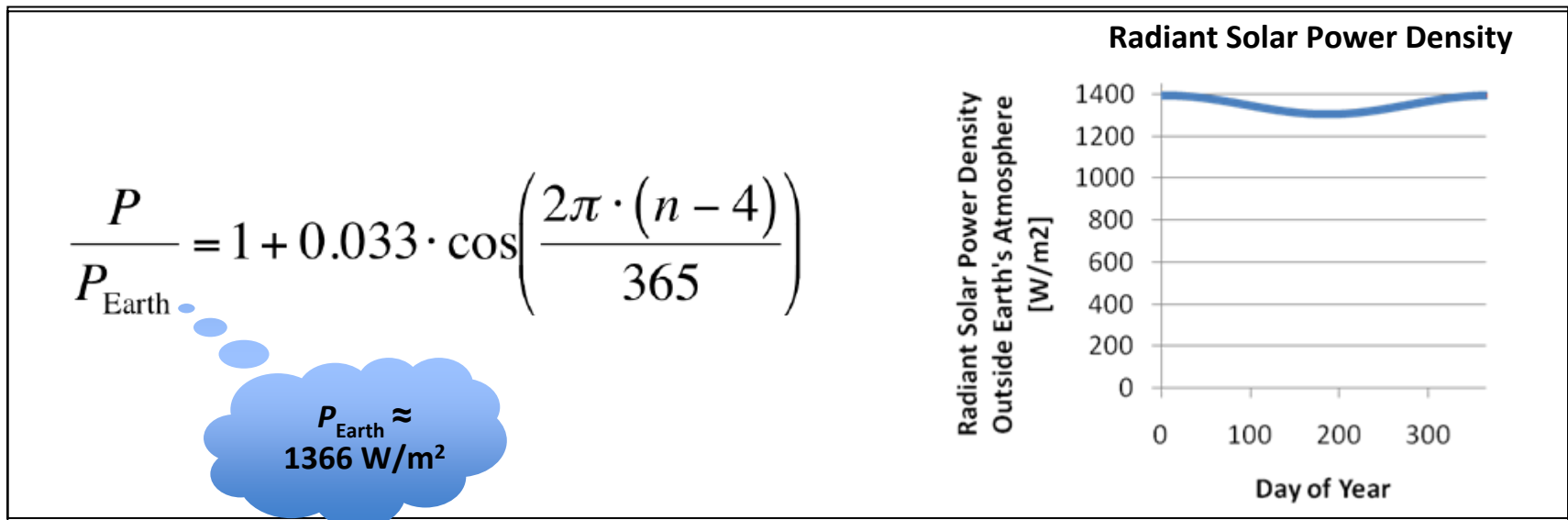


# Orbit Ellipticity

The Earth's orbit around the Sun is slightly elliptical...



... resulting in a slight periodic change in the radiant solar power density as a function of season.



# Orbit Ellipticity

*Other planets can have greater orbital ellipticity, greater variability in solar irradiance.*

TABLE 2 Solar Irradiance at the Planets

Planet	Solar Irradiance, $W \cdot m^{-2}$		
	Mean	Perihelion	Aphelion
Mercury	9116.4	14447.5	6271.1
Venus	2611.0	2646.4	2575.7
Earth	1366.1	1412.5	1321.7
<b>Mars</b>	<b>588.6</b>	<b>715.9</b>	<b>491.7</b>
Jupiter	50.5	55.7	45.9
Saturn	15.04	16.76	13.53
Uranus	3.72	4.11	3.37
Neptune	1.510	1.515	1.507
Pluto	0.878	1.571	0.560



Courtesy NASA.

<http://rredc.nrel.gov/solar/spectra/am0/ASTM2000.html>

# Comprehensive Model

For our friends following along by phone, please access:

<http://pvcdrom.pveducation.org/>

Click:

Chapter 2: Properties of Sunlight

*Terrestrial Solar Radiation*

*Motion of the Sun*

# Question: How do I angle my solar panels?

Incidence of sunlight changes depending on location, time of year, local weather.

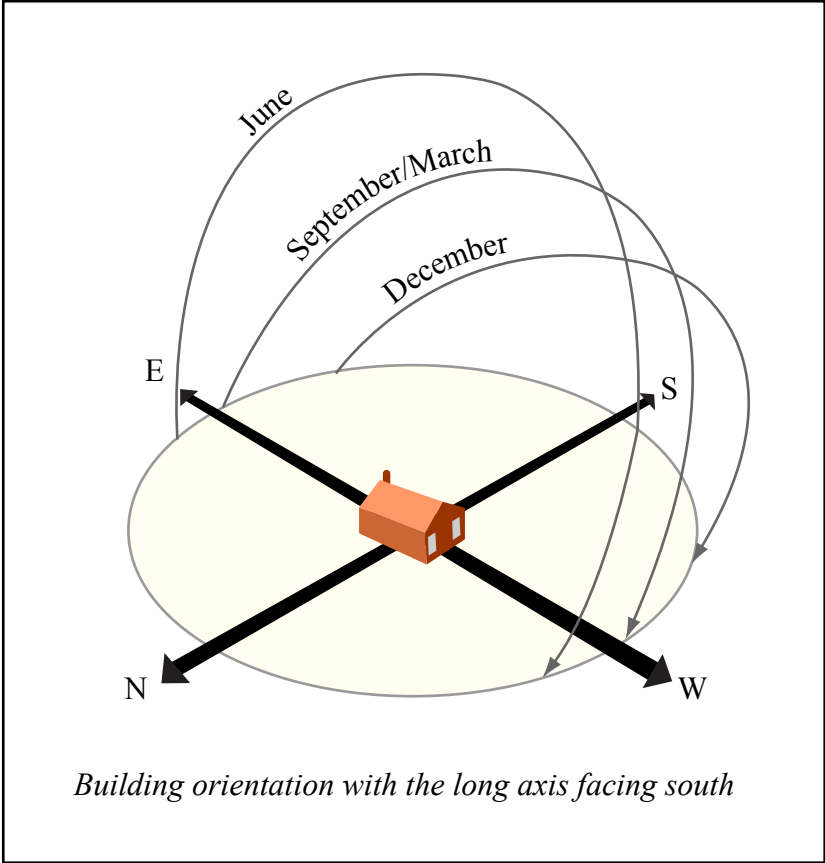
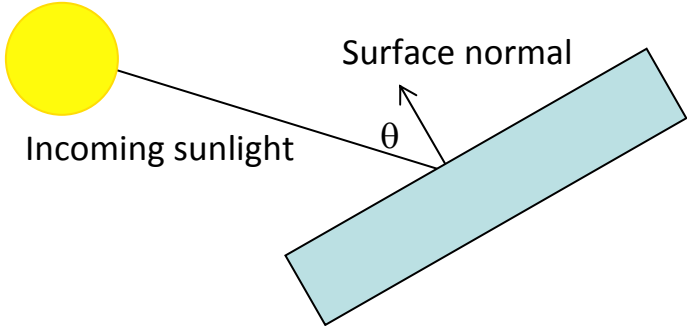


Figure by MIT OpenCourseWare.

## Angles Matter!



The closer  $\theta = 0^\circ$ , the greater the amount of sunlight absorbed!

# Atmospheric Absorption

- Causes.
- Estimating the effects.
- The solar spectrum on Earth.



# Atmospheric Absorption

Courtesy NASA.

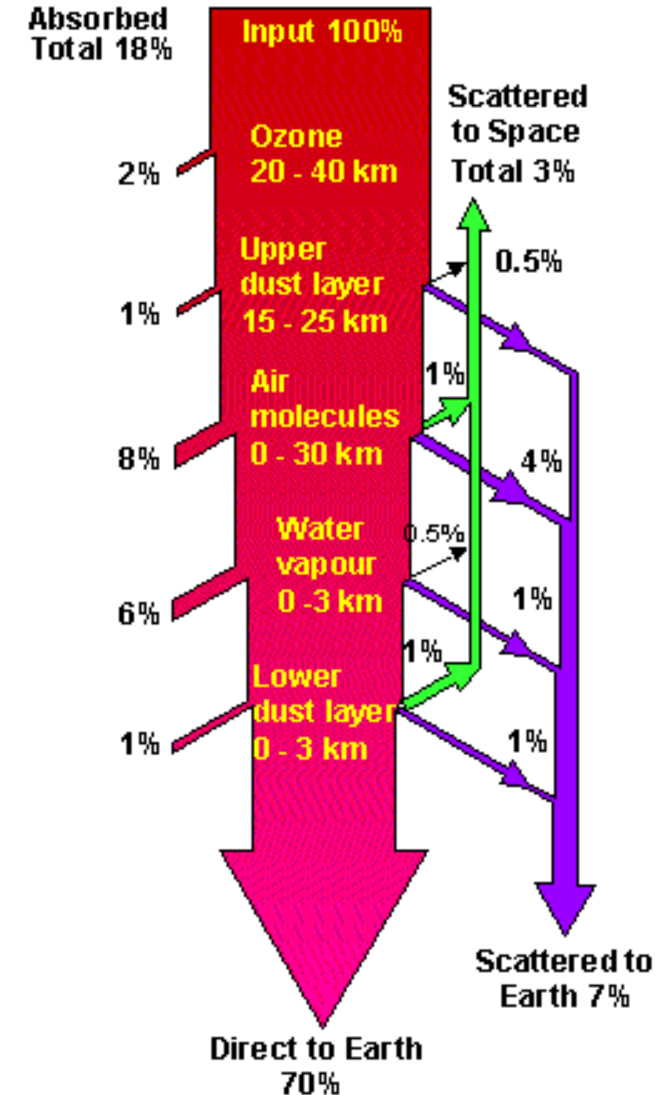


<http://www.gsfc.nasa.gov/gsfc/earth/pictures/2002/1203apollo17/earth.jpg>

# ATMOSPHERIC EFFECTS

Atmospheric effects have several impacts on the solar radiation at the Earth's surface. The major effects for photovoltaic applications are:

- A reduction in the power of the solar radiation due to absorption, scattering and reflection in the atmosphere;
- A change in the spectral content of the solar radiation due to greater absorption or scattering of some wavelengths;
- The introduction of a diffuse or indirect component into the solar radiation; and
- Local variations in the atmosphere (such as water vapor, clouds and pollution) which have additional effects on the incident power, spectrum and directionality.



Courtesy Christiana Honsberg and Stuart Bowden. Used with permission.

Typical clear sky absorption and scattering of incident sunlight (after Hu and White, 1983).

# ATMOSPHERIC EFFECTS

IPCC's assessment on the quantity of insolation (incoming solar radiation) reaching the Earth's surface.

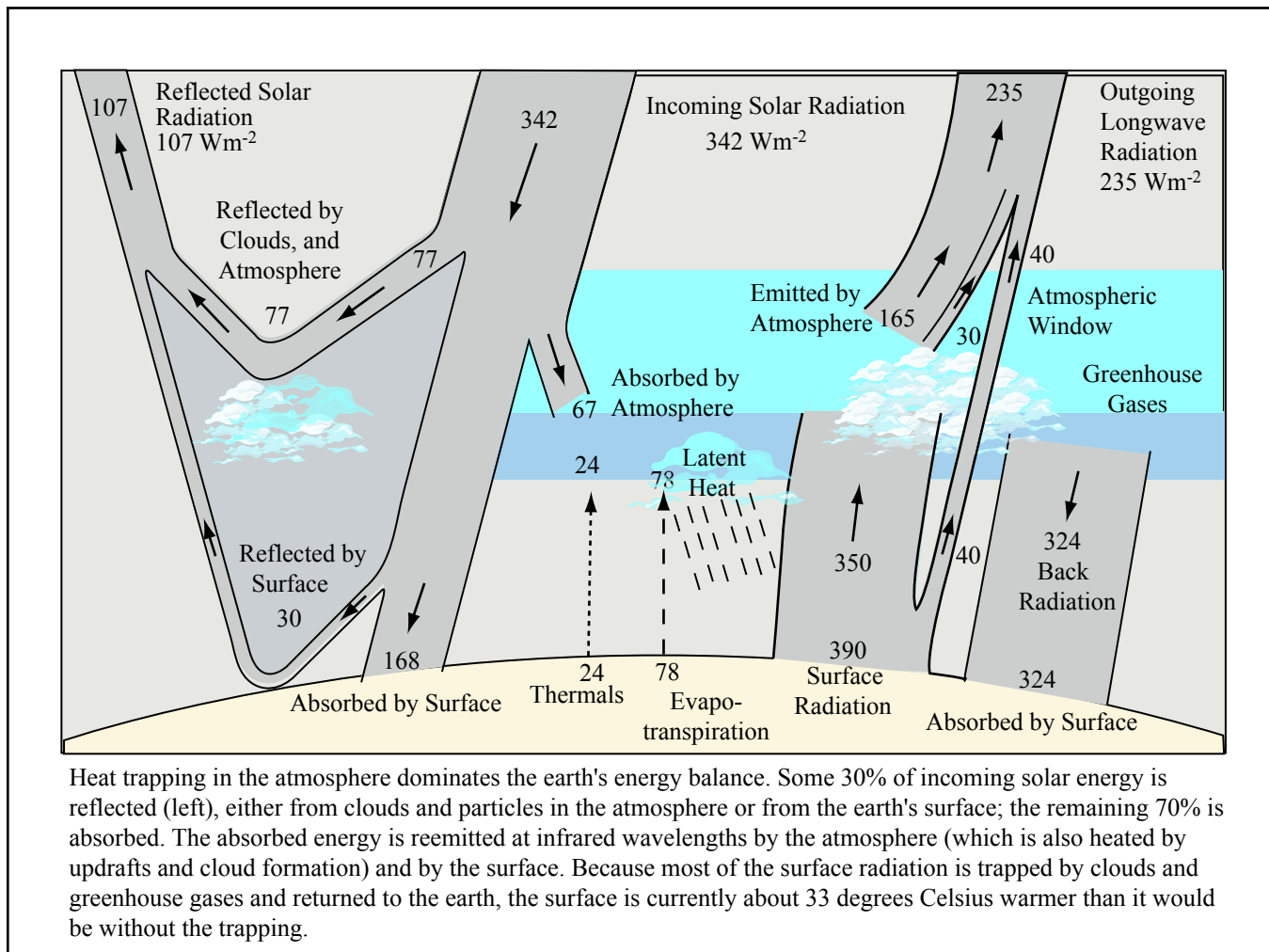


Figure by MIT OpenCourseWare.

# ATMOSPHERIC EFFECTS

Perhaps more intuitive means of demonstrating insolation evolution (figure courtesy of Spencer Ahrens).

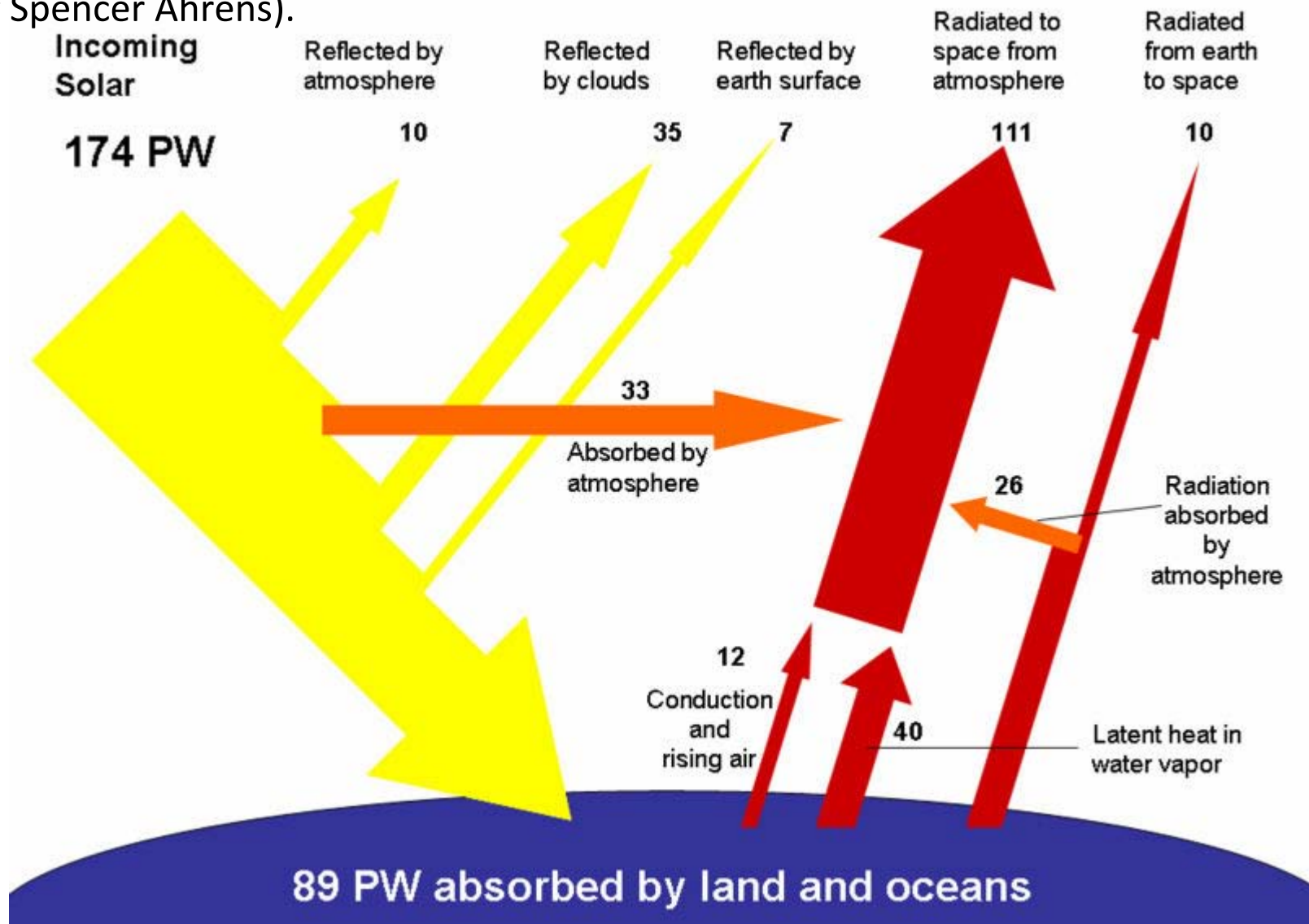


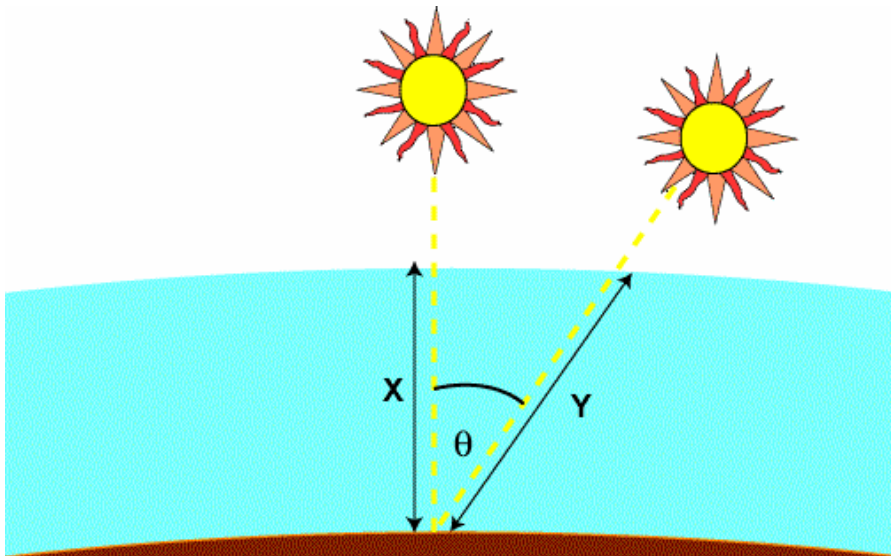
Image by Frank van Mierlo.

# AIR MASS

The Air Mass is the path length which light takes through the atmosphere normalized to the shortest possible path length (that is, when the sun is directly overhead). The Air Mass quantifies the reduction in the power of light as it passes through the atmosphere and is absorbed by air and dust. The Air Mass is defined as:

$$AM = \frac{1}{\cos(\theta)}$$

*Valid for small to medium  $\theta$*



AM1: Sun directly overhead

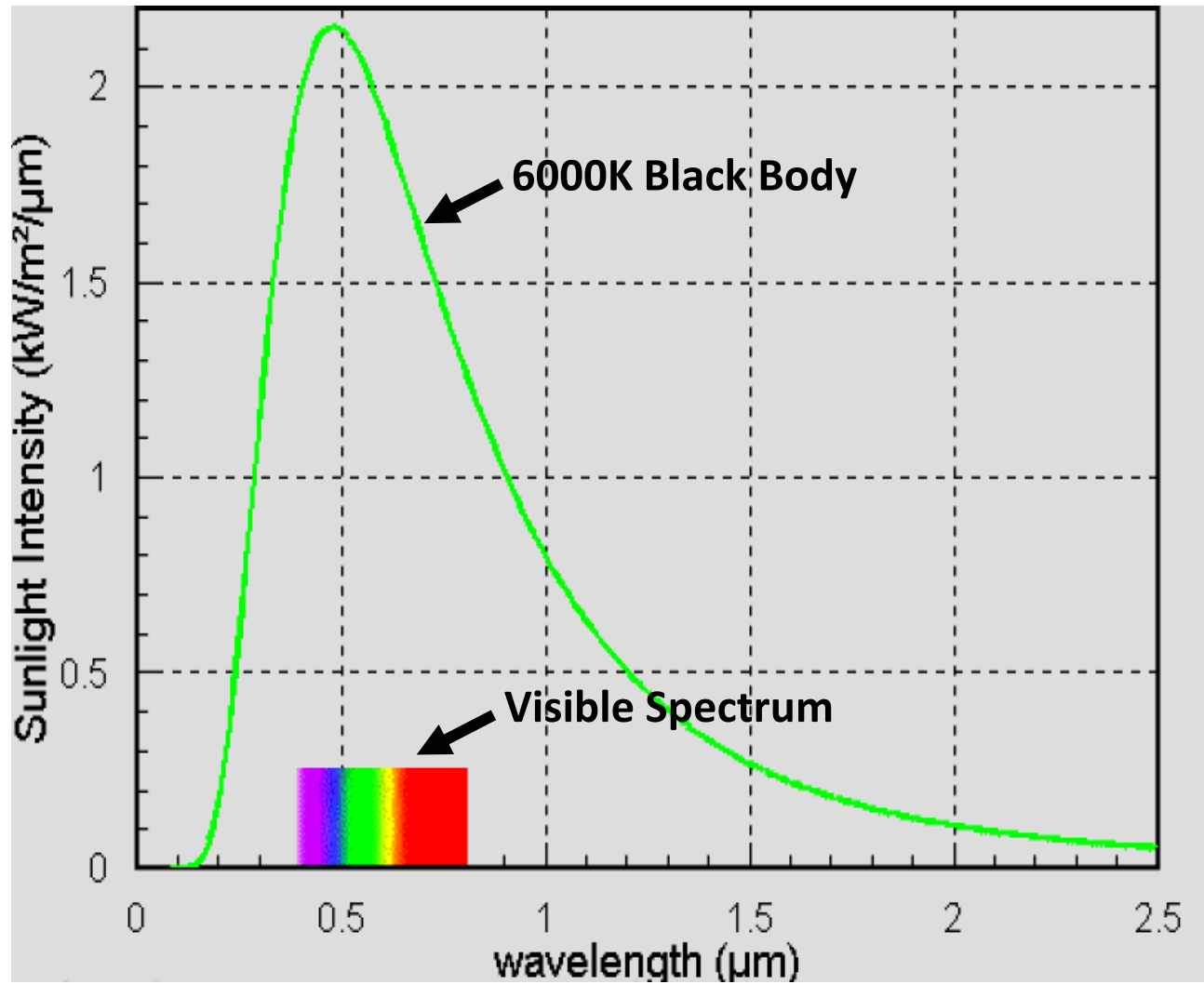
AM1.5G: “Conventional”

G (Global): Scattered and direct sunlight

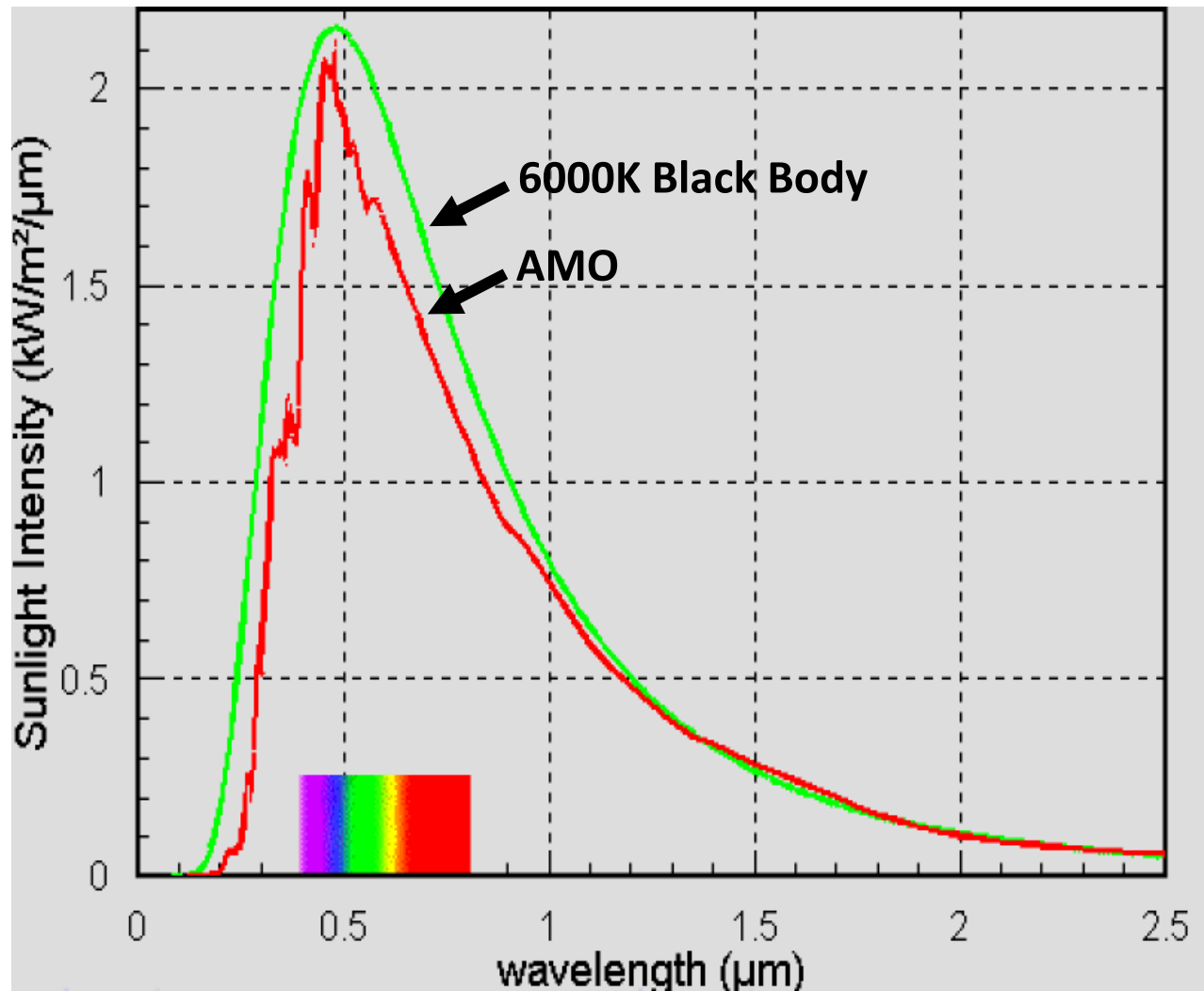
D (Direct): Direct sunlight only

AM0: Just above atmosphere (space applications)

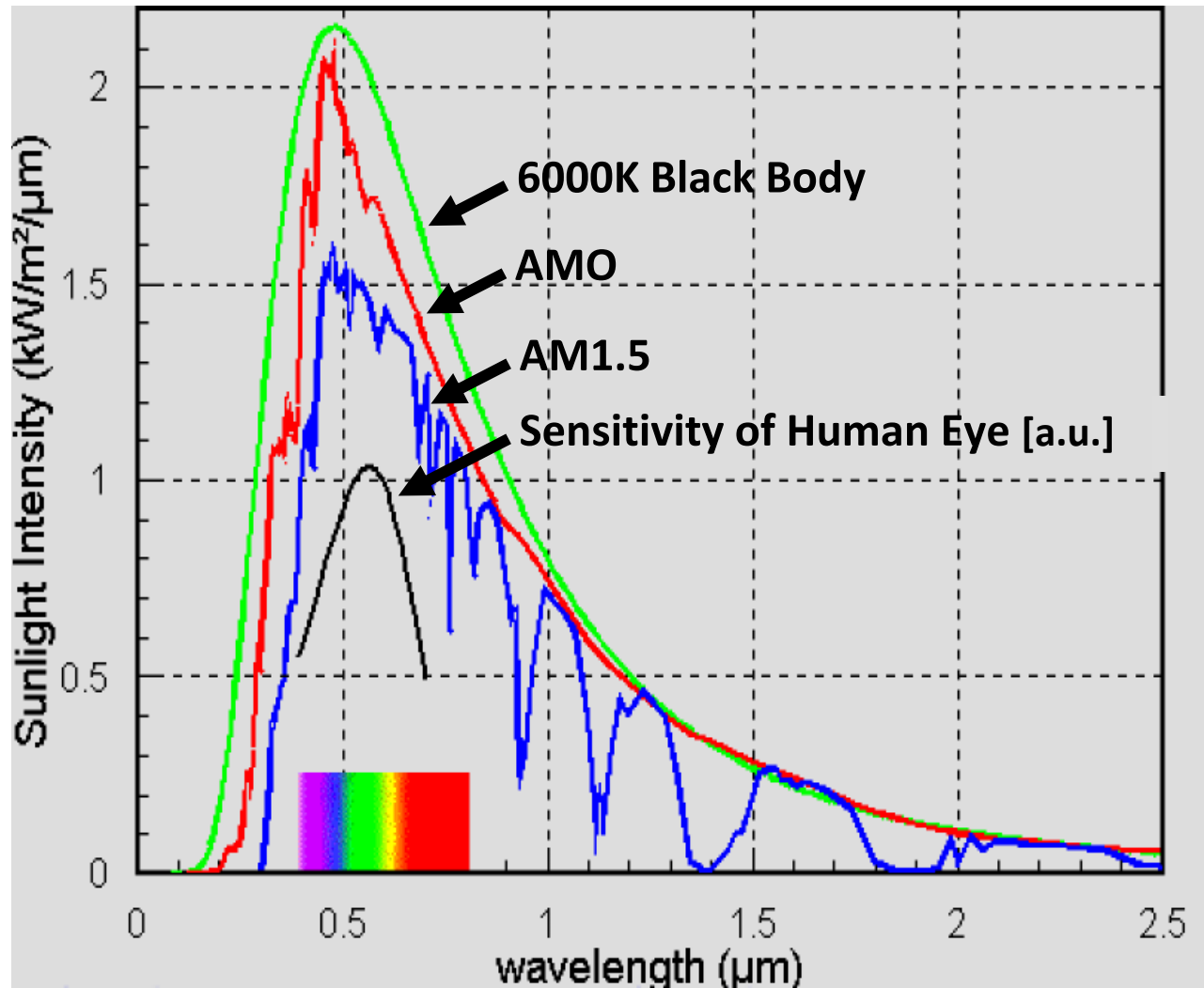
# SOLAR SPECTRUM



# SOLAR SPECTRUM

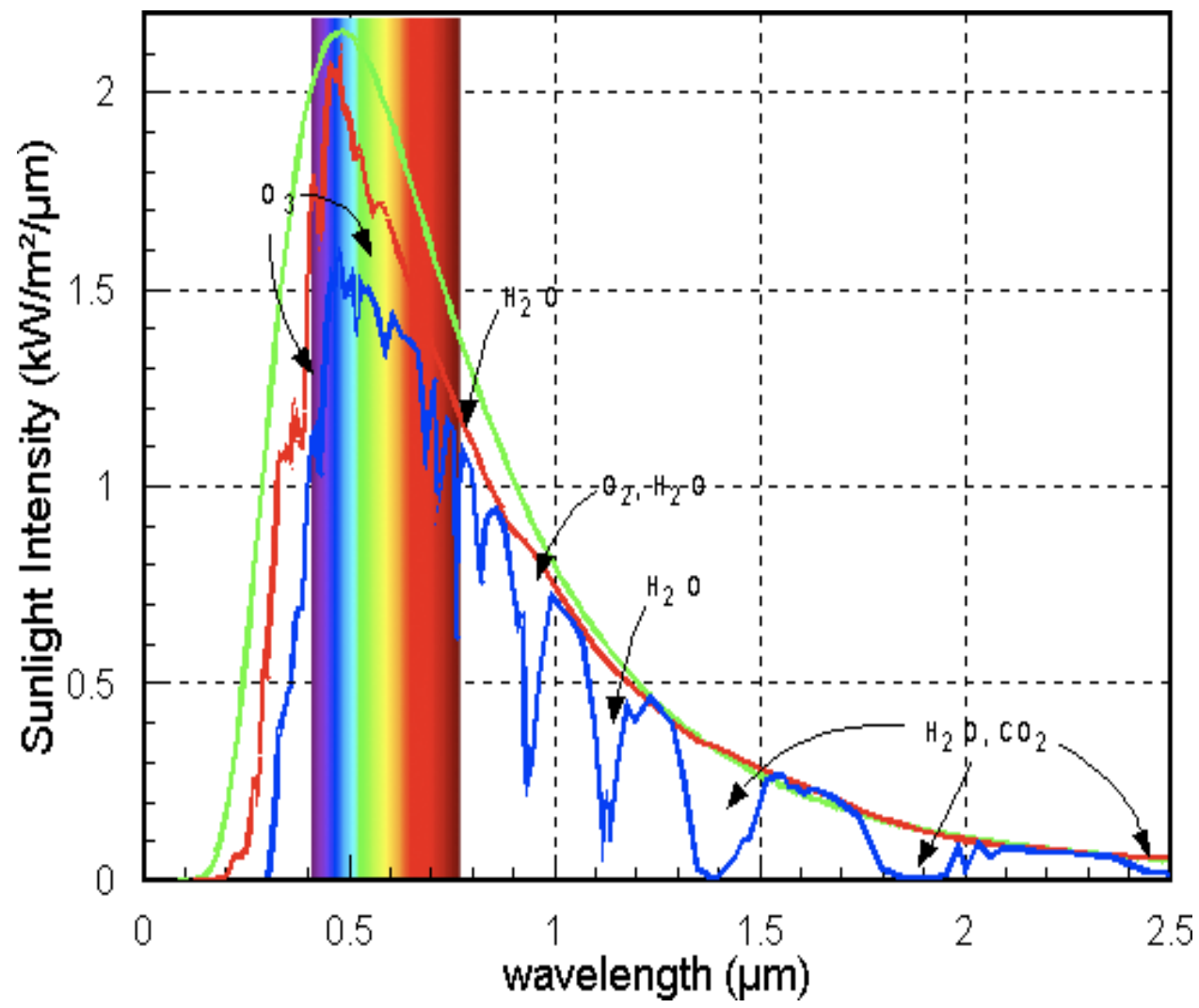


# SOLAR SPECTRUM





# SOLAR SPECTRUM

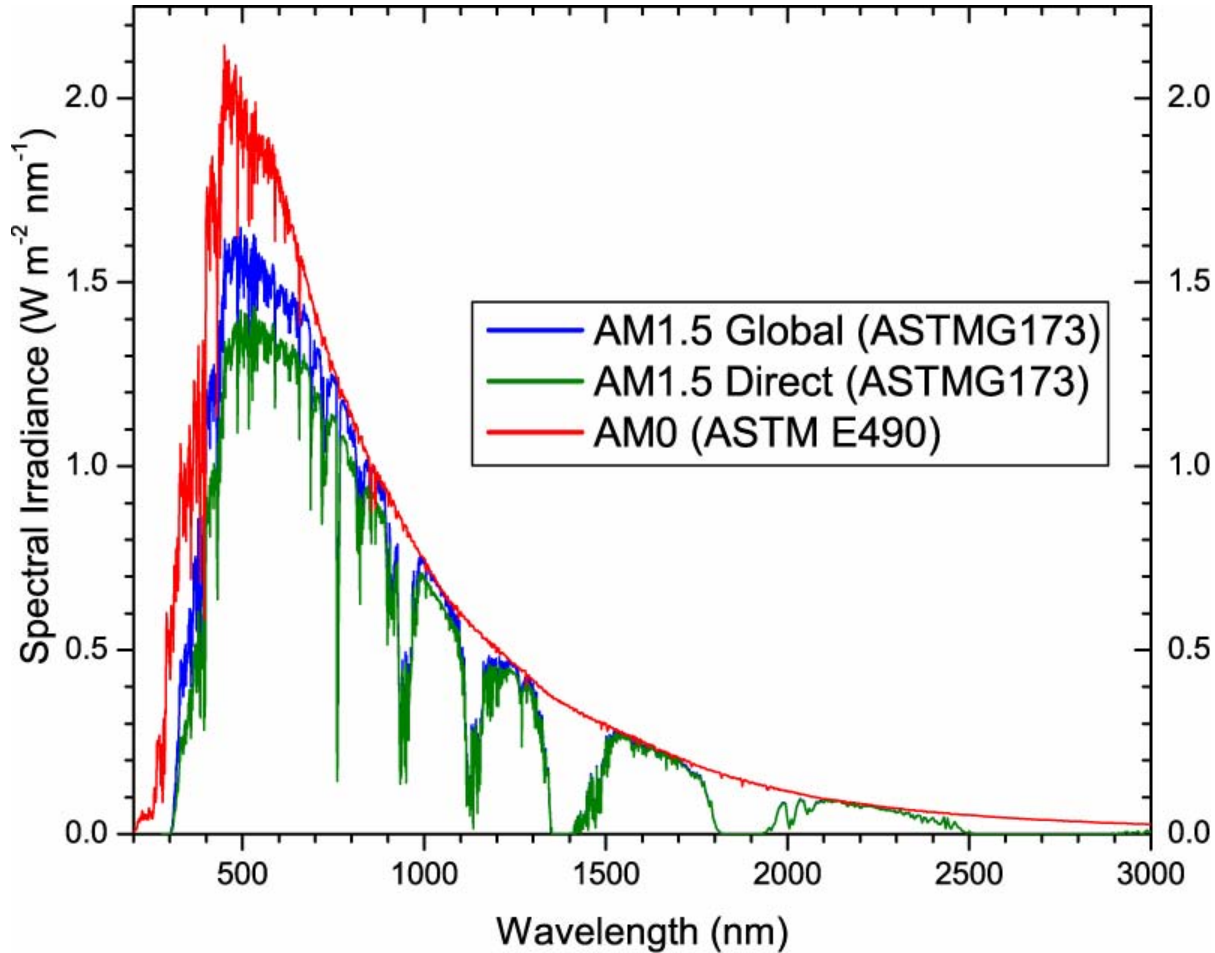


# SOLAR SPECTRUM

AM1.5 Global: Used for testing of Flat Panels (Integrated power intensity: 1000 W/m<sup>2</sup>)

AM1.5 Direct: Used for testing of concentrators (900 W/m<sup>2</sup>)

AM0: Outer space (1366 W/m<sup>2</sup>)



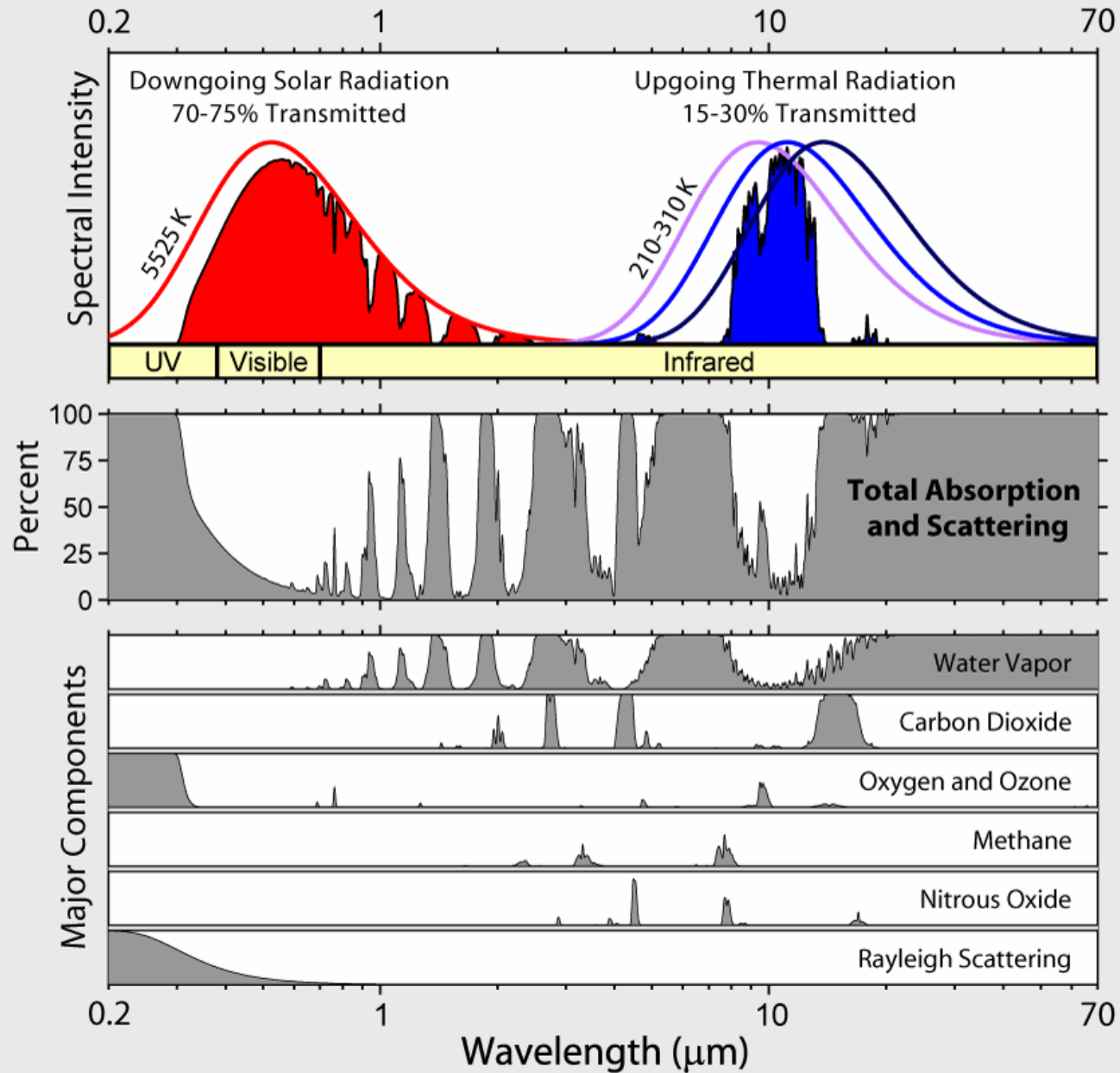
The above charts, in Excel files:

[http://www.udel.edu/igert/pvcdrom/APPEND/AM0AM1\\_5.xls](http://www.udel.edu/igert/pvcdrom/APPEND/AM0AM1_5.xls)

Source of data:

<http://www.nrel.gov/rredc/smarts/>

# Radiation Transmitted by the Atmosphere



# INSOLATION

Insolation: Incoming Solar Radiationation

Typically given in units of:

*Energy per Unit Area per Unit Time*

**(kWh/m<sup>2</sup>/day)**

Helpful when designing or projecting PV systems: Expected yield

Affected by: latitude, local weather patterns, etc.

# Measuring Global/Direct Insolation



Courtesy DOE/NREL, Credit – David Parsons.

Courtesy DOE/NREL, Credit – Tom Stoffel.



Equipment for solar irradiance measurements <[http://www.nrel.gov/data/pix/searchpix\\_visual.html](http://www.nrel.gov/data/pix/searchpix_visual.html)>

# Solar Insolation Maps

- United States
- Europe
- Africa
- World

Map removed due to copyright restrictions. Please see PV Solar Radiation (Flat Plaste, Facing South, Latitude Tilt), [[January](#)], [NREL](#).

Map removed due to copyright restrictions. Please see PV Solar Radiation (Flat Plaste, Facing South, Latitude Tilt), [[February](#)], [NREL](#).



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Map removed due to copyright restrictions. Please see PV Solar Radiation (Flat Plaste, Facing South, Latitude Tilt), [[June](#)], [NREL](#).

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Map removed due to copyright restrictions. Please see PV Solar Radiation (Flat Plate, Facing South, Latitude Tilt), [[December](#)], [NREL](#).

# The difference between concentrating and non-concentrating solar resources

(concentrating solar power requires direct sunlight!)

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Map removed due to copyright restrictions. Please see [[Direct Normal Solar Radiation \(Two-Axis Tracking Concentrator\), Annual](#)], NREL.

Map removed due to copyright restrictions. Please see [[Direct Normal Solar Radiation \(Two-Axis Tracking Concentrator\), Annual](#)], NREL.

Map removed due to copyright restrictions. Please see [[PV Solar Radiation \(Flat Plate, Facing South, Latitude Tilt\), January](#)], NREL.

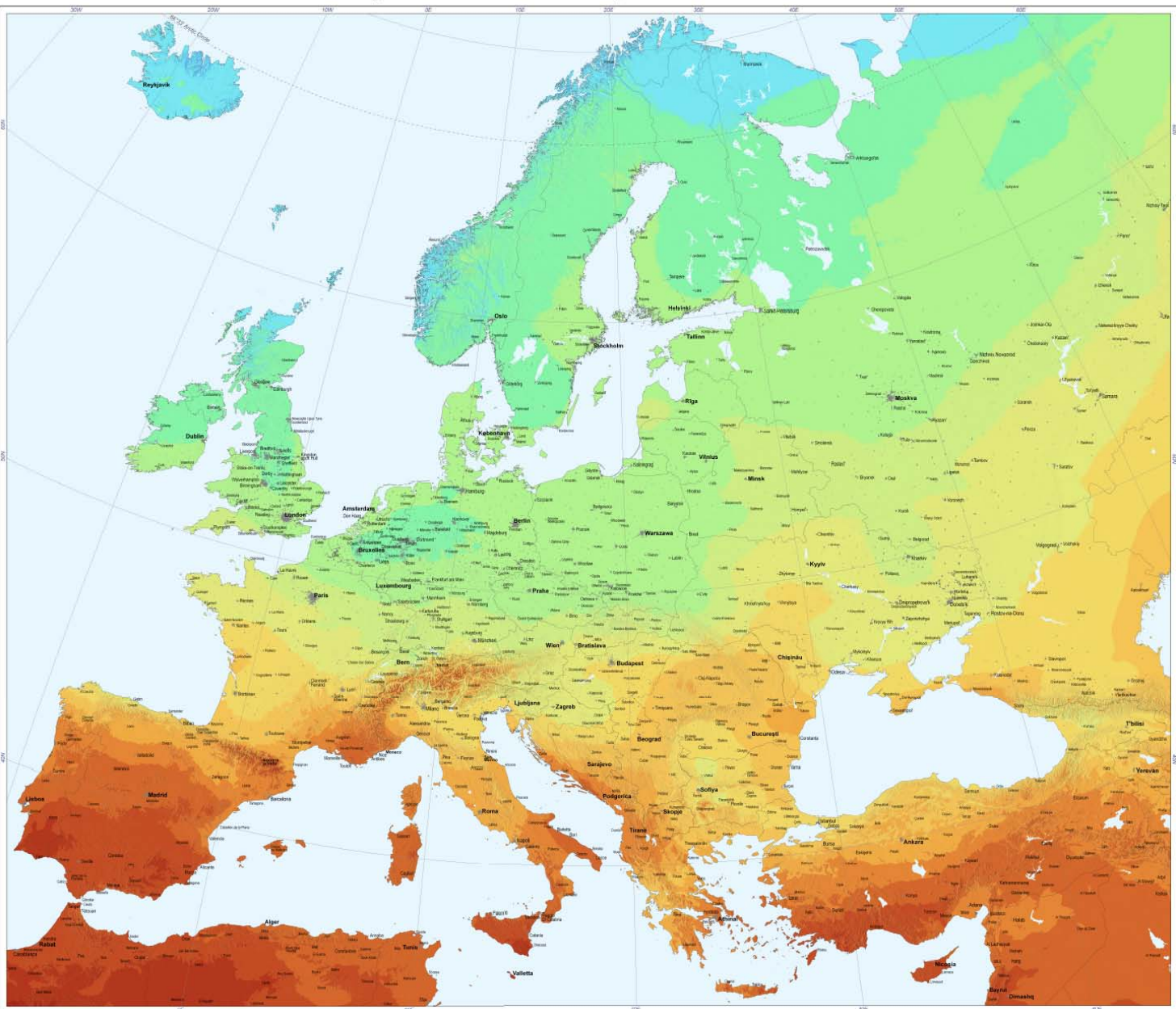
Map removed due to copyright restrictions. Please see [[Direct Normal Solar Radiation \(Two-Axis Tracking Concentrator\), January](#)], NREL.



Map removed due to copyright restrictions. Please see [[PV Solar Radiation \(Flat Plate, Facing South, Latitude Tilt\), July](#) ], NREL.

Map removed due to copyright restrictions. Please see [[Direct Normal Solar Radiation \(Two-Axis Tracking Concentrator\), July](#)], NREL.

# Photovoltaic Solar Electricity Potential in European Countries



Global irradiation [kWh/m<sup>2</sup>]  
 <450 500 600 700 800 900 1000 1100 1200 1300 1400 1500 1600 1700 1800 1900 2000 2100 2200>  
 Yearly sum of global irradiation incident on optimally-inclined south-oriented photovoltaic modules  
 Yearly sum of solar electricity generated by 1 kWp system with optimally-inclined modules and performance ratio 0.75  
 Solar electricity [kWh/kWp]

## Optimum inclination of PV modules to maximize yearly energy yield



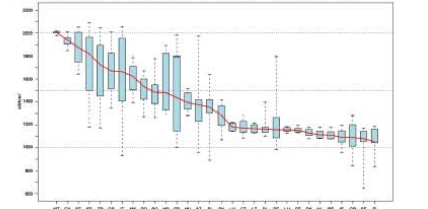
## Orography and country names with ISO codes



**Data description**  
 The PVGIS database is developed from measurements at 566 meteorological stations by combination of solar radiation model r\_sun and spatial interpolation. It contains monthly and yearly averages representing the period 1981-1999.  
 Grid resolution (enhanced by terrain): 1 km x 1 km  
 Map projection: Lambert azimuthal equal area, WGS 84, lat 48°, lon 16°

**Ancillary data**  
 » GISCO database © Eurostat 2006  
 » CORINE Land Cover 2000 (<http://repositorio.eionet.europa.eu/CLC2000>)  
 » Global Land Cover 2000 (<http://www.gvm.jrc.it/glc2000/>)  
 » Digital terrain model SRTM-30 (<http://srtm.usgs.gov/>)  
 » City Population © Thomas Breakey 2006 (<http://www.citypopulation.de>)  
 Note: the delineation of the international boundaries and geographical names must not be considered authoritative

## Comparison of yearly global irradiation incident on optimally-inclined photovoltaic modules in 25 European Union member countries and 5 candidate countries



The country averages are connected by the red line. The minima/maxima in each country are shown as dashed lines, while the boxes show the range in which 90% of built-up areas in the country fit.

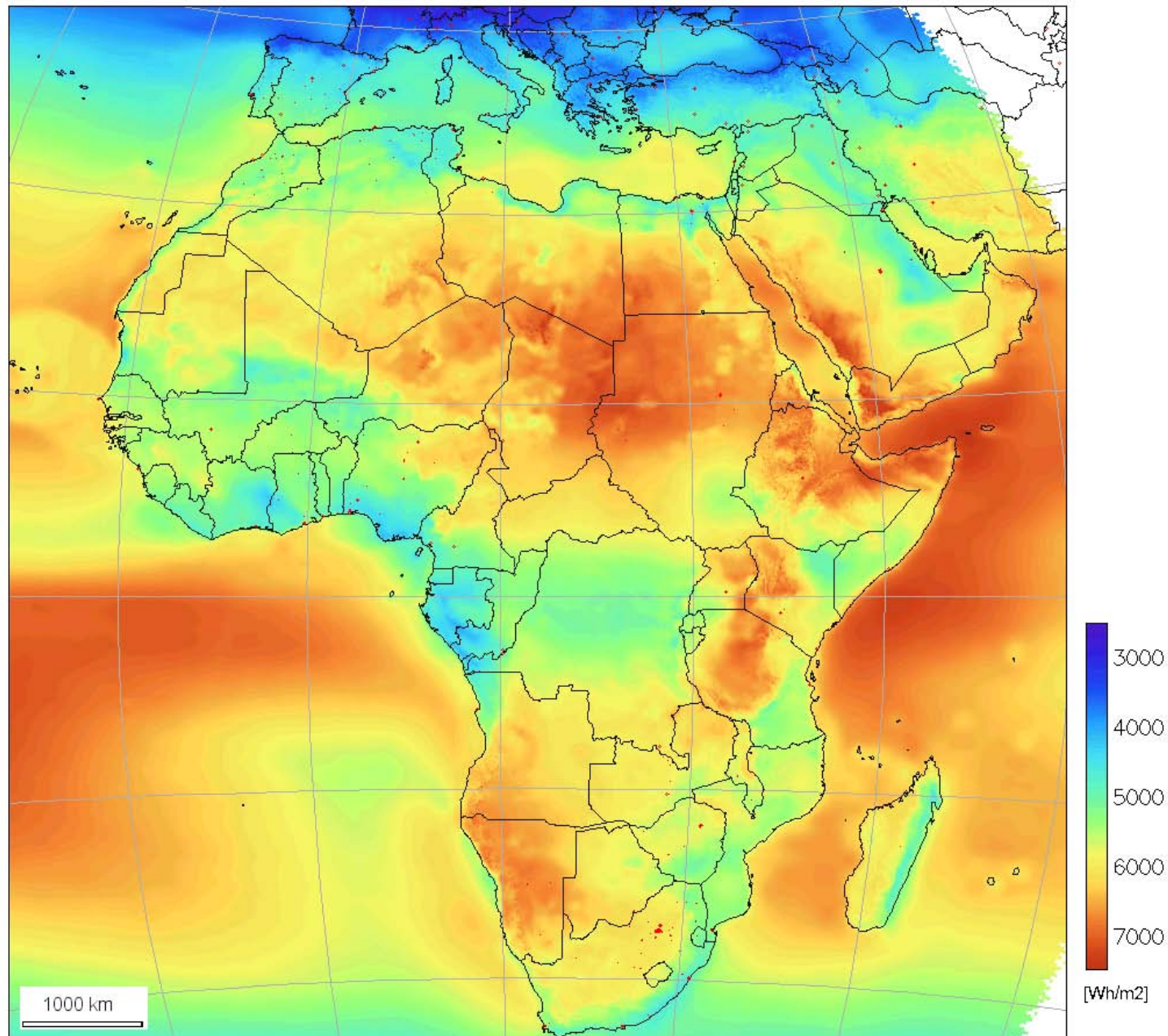
**Authors**  
 Marcel Sili, Thomas A. Huld, Ewan D. Durig, Tomáš Čebecauer  
 European Commission - DG Joint Research Centre, Institute for Environment and Sustainability  
 Renewable Energies Unit, TP 450, I-21020 Ispra (VA), Italy  
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# Germany & U.S. : A quick comparison

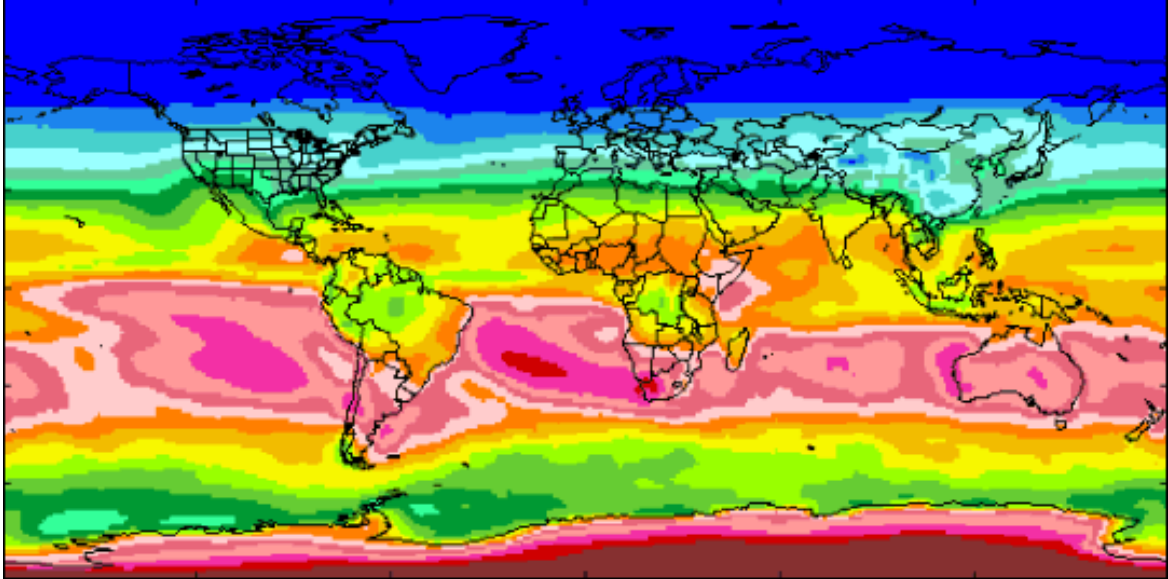
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[http://citysustainable.com/images/SEIA\\_compare\\_germany\\_us.jpg](http://citysustainable.com/images/SEIA_compare_germany_us.jpg)



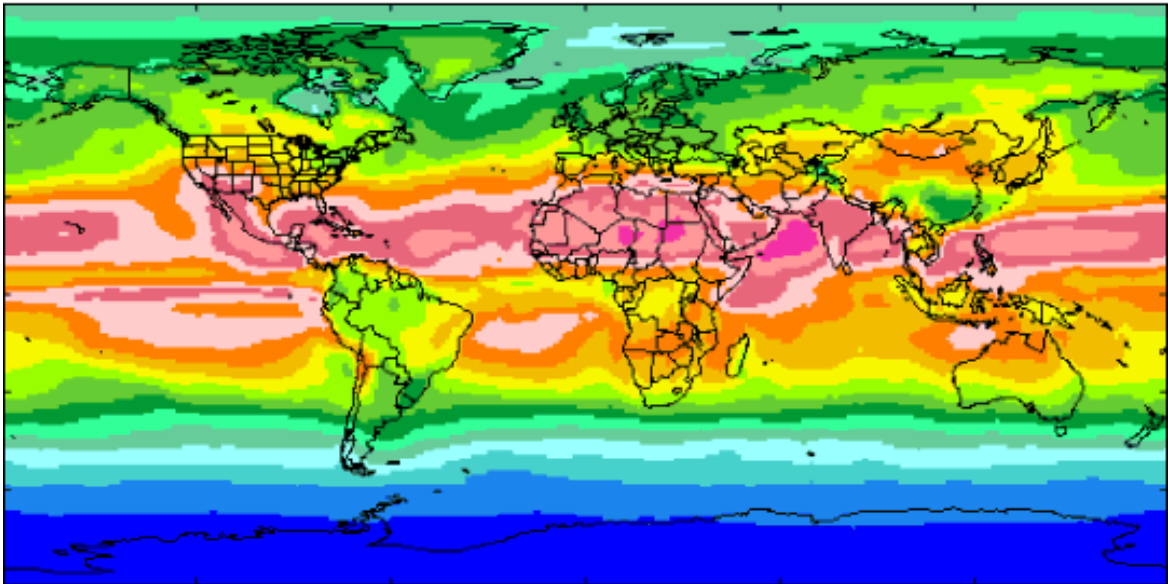
Global horizontal irradiation (1985-2004)  
(annual average of daily sums, Gh)



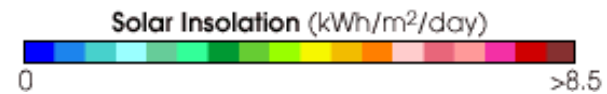
# Global Insolation Data



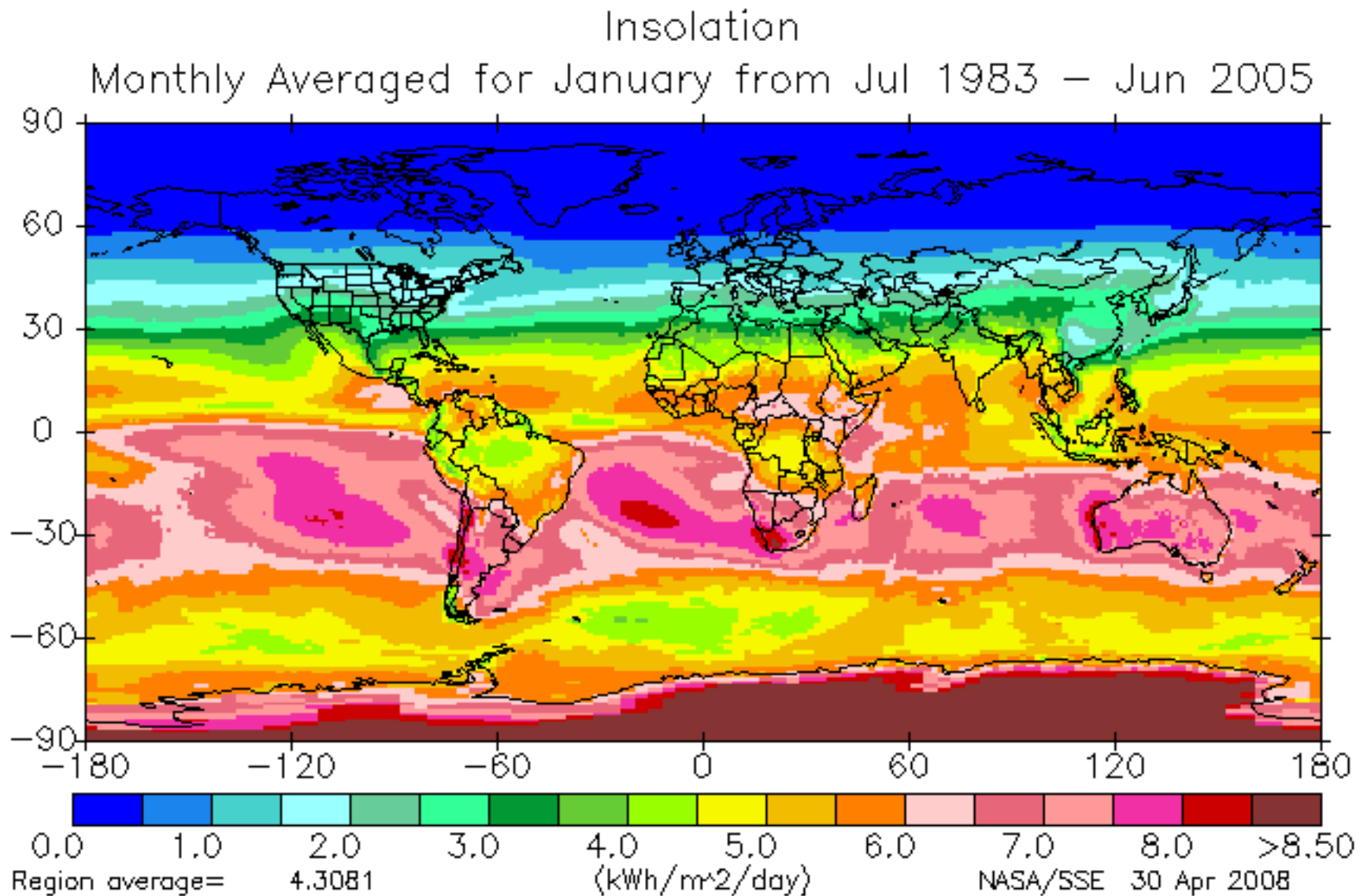
January 1984-1993



April 1984-1993



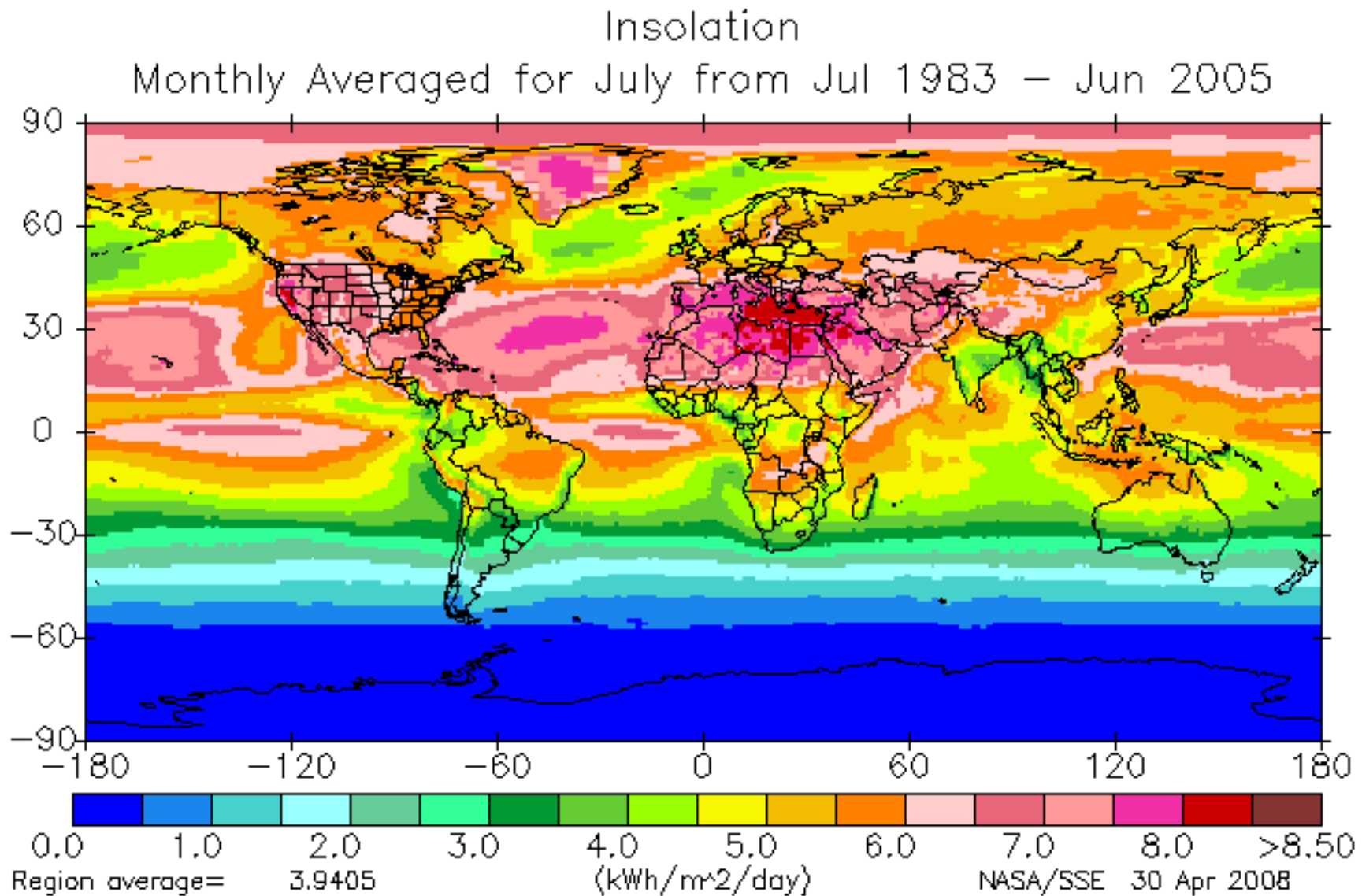
# Global Insolation Data



<http://eosweb.larc.nasa.gov/sse/>

Image courtesy NASA Earth Observatory.

# Global Insolation Data



<http://eosweb.larc.nasa.gov/sse/>

Image courtesy NASA Earth Observatory.



# Global Insolation

Insolation at AM0: Resource determined by latitude ( $\sim \cos \theta$ ).

Image removed due to copyright restrictions. Please see <http://en.wikipedia.org/wiki/File:Insolation.png>

Average Surface Insolation: Determined by atmospheric absorption, local weather patterns...

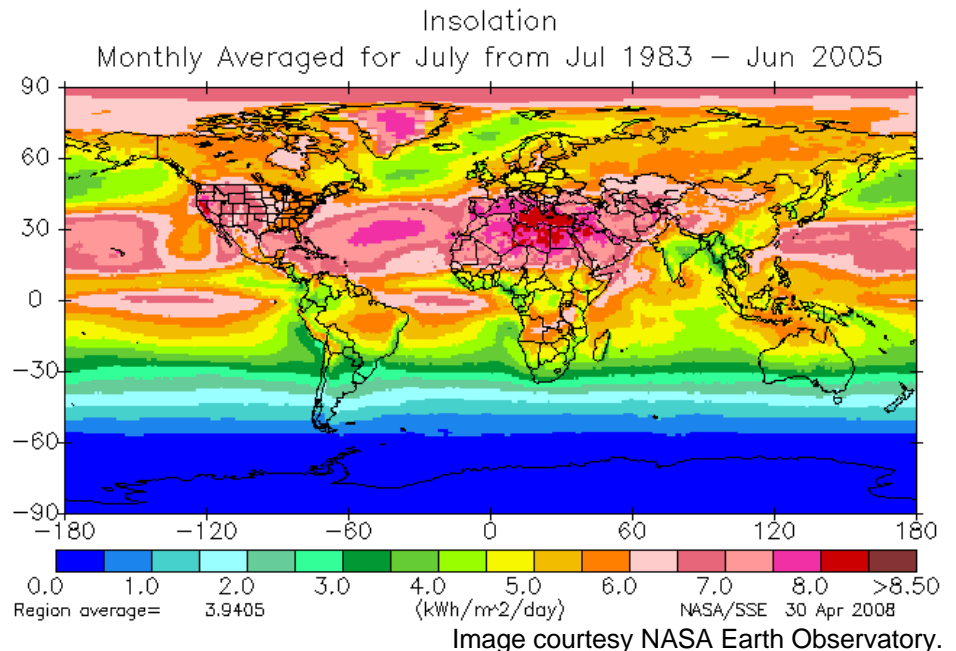
# Estimating Solar System Outputs

# Estimating System Output from Insolation Maps

Q: Let's say I have a 2.2 kW<sub>p</sub> photovoltaic array. How much energy will it produce in a year?

A: Let's say our location receives, on average, 4 kWh/m<sup>2</sup>/day from the Sun. The calculation is then straightforward:

$$\text{Energy Output} = \frac{(2200 \text{ W}_p) \times (4.0 \text{ kWh/m}^2/\text{day})}{1000 \text{ W}_p/\text{m}^2} = 8.8 \text{ kWh/day} \approx 3200 \text{ kWh/year}$$



# Estimating System Output from Insolation Maps

Q: Let's say I have a 2.2 kW<sub>p</sub> photovoltaic array. How much energy will it produce in a year?

A: Let's say our location receives, on average, 4 kWh/m<sup>2</sup>/day from the Sun. The calculation is then straightf

System size

Insolation at site of installation

$$\text{Energy Output} = \frac{(2200 \text{ W}_p) \times (4.0 \text{ kWh/m}^2/\text{day})}{1000 \text{ W}_p/\text{m}^2} = 8.8 \text{ kWh/day} \approx 3200 \text{ kWh/year}$$

AM 1.5G

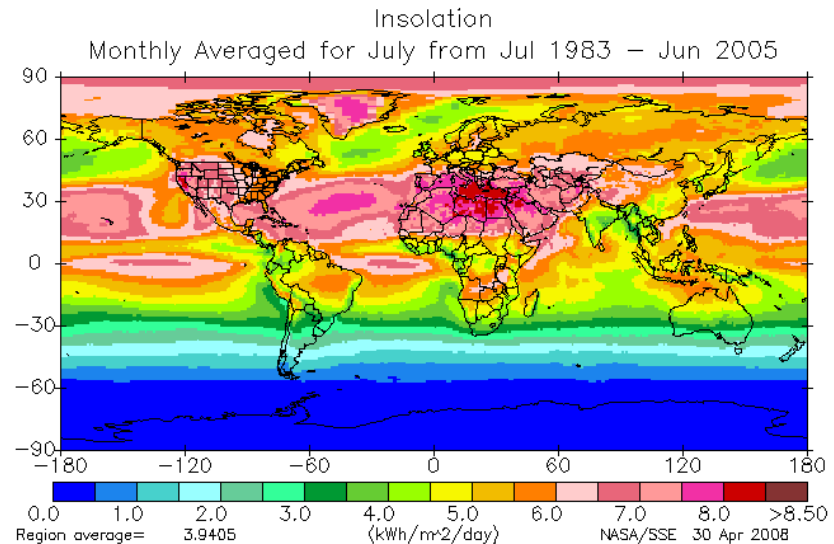


Image courtesy NASA Earth Observatory.

# Actual System Outputs

Actual system outputs may be significantly lower, due to suboptimal system performance, design, installation, shading losses, etc.:

See, e.g.,

<http://soltrex.masstech.org/systems.cfm>

Image removed due to copyright restrictions.  
Please see any site listed at  
<http://soltrex.masstech.org/systems.cfm>

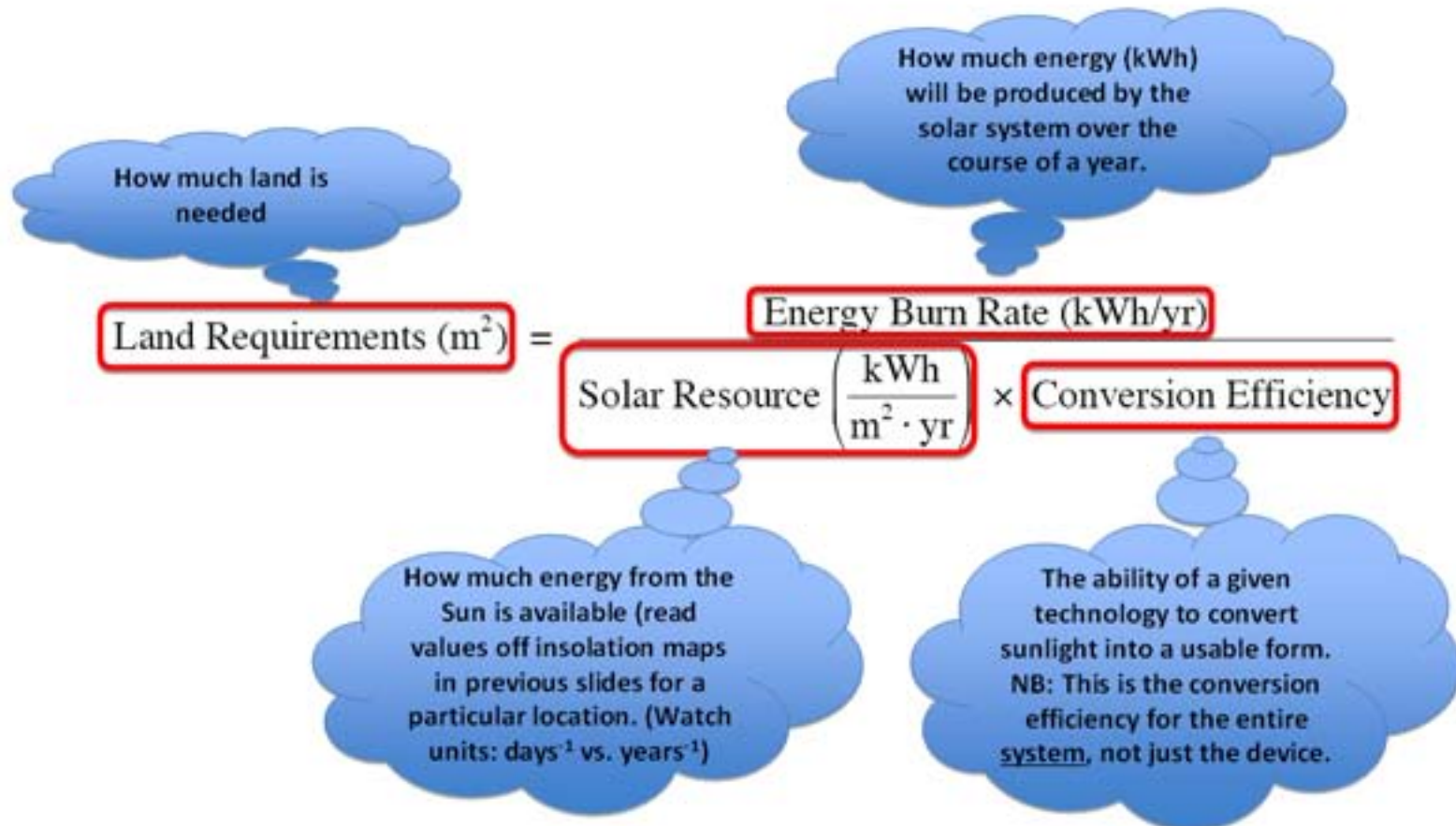
# Estimating Solar Land Area Requirements

Here's the equation to use, when calculating the area of land needed to produce a certain amount of energy over a year, given a technology with a certain conversion efficiency.

$$\text{Land Requirements (m}^2\text{)} = \frac{\text{Energy Burn Rate (kWh/yr)}}{\text{Solar Resource} \left( \frac{\text{kWh}}{\text{m}^2 \cdot \text{yr}} \right) \times \text{Conversion Efficiency}}$$

# Estimating Solar Land Area Requirements

Here's the equation to use, when calculating the area of land needed to produce a certain amount of energy over a year, given a technology with a certain conversion efficiency.



# Test Case

Given:

1. An energy burn rate of  $4 \text{ TW}_{\text{ave}}$  ( $3.5 \times 10^{13} \text{ kWh/yr}$ )  
*(forward-projected U.S. energy consumption, including waste heat)*
2. An insolation value of  $6 \text{ kWh/m}^2/\text{day}$   
*(typical year-average value for flat panel in Nevada; CPV  $\sim 7 \text{ kWh/m}^2/\text{day}$ )*
3. System conversion efficiency of 12%  
*(including all system losses)*

Using:

$$\begin{aligned} \text{Land Requirements (m}^2\text{)} &= \frac{\text{Energy Burn Rate (kWh/yr)}}{\text{Solar Resource} \left( \frac{\text{kWh}}{\text{m}^2 \cdot \text{yr}} \right) \times \text{Conversion Efficiency}} \\ &= \frac{(3.5 \times 10^{13} \text{ kWh/yr})}{\left( 2192 \frac{\text{kWh}}{\text{m}^2 \cdot \text{yr}} \right) \times (0.12)} \approx 1.3 \times 10^5 \text{ km}^2 \end{aligned}$$

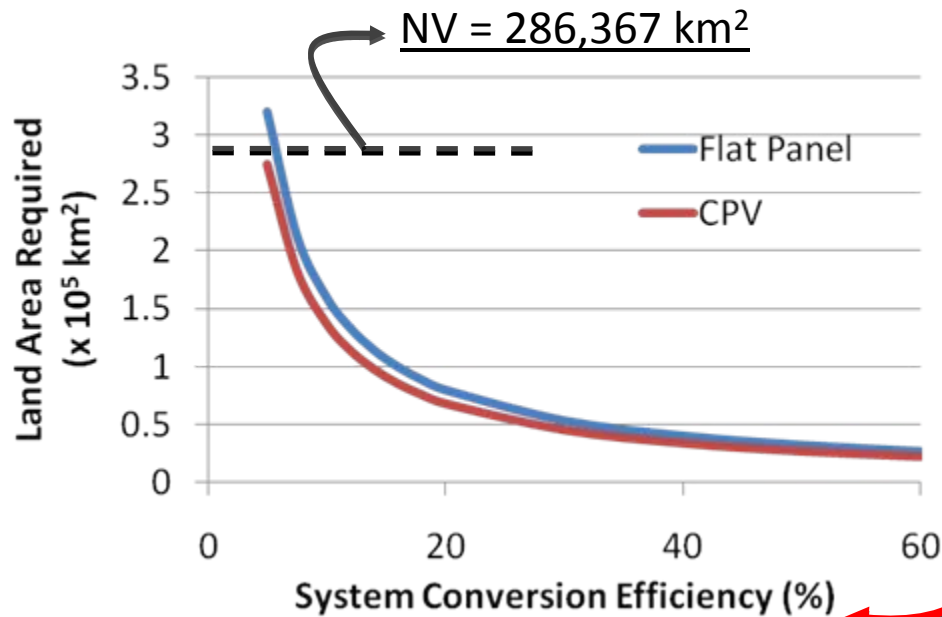
Compare land requirement to power entire U.S. on today's solar technology ( $\sim 130,000 \text{ km}^2$ ), to total area of Nevada ( $286,367 \text{ km}^2$ ).



# Test Case

Note that the land area requirement is a hyperbolic function of system conversion efficiency.

$$\text{Land Requirements (m}^2\text{)} = \frac{\text{Energy Burn Rate (kWh/yr)}}{\text{Solar Resource (} \frac{\text{kWh}}{\text{m}^2 \cdot \text{yr}} \text{)} \times \text{Conversion Efficiency}}$$



# Estimating Solar Land Area Requirements

Image removed due to copyright restrictions. Please see [http://commons.wikimedia.org/wiki/File:Solar\\_land\\_area.png](http://commons.wikimedia.org/wiki/File:Solar_land_area.png)

6 Circles at  $3 \text{ TW}_e$  Each =  $18 \text{ TW}_e$