## Controlling Physical Layer Parameters for Mobile Ad-Hoc Networks

by

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Submitted to the Department of Electrical Engineering and Computer Science

in partial fulfillment of the requirements for the degree of

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#### Abstract

This thesis investigates the use of software radios for ad-hoc networking to improve spectrum utilization and battery life. An API that provides a mechanism for a network node to request services from the software radio layer and a framework that permits a physical layer to be constructed based on these needs are also presented. In addition, this framework is used to analyze the 802.11 wireless standard to identify some of its limitations.

Thesis Supervisor: Robert Morris Title: Assistant Professor .

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## Contents

1	Intr	oducti	on	13
	1.1	Limita	tions in Current Wireless Ad-Hoc Systems	14
	1.2	How S	oftware Radio Overcomes these Limitations	14
	1.3	Relate	d Work	15
	1.4	Thesis	Scope	16
	1.5	Road I	Map	16
<b>2</b>	Bac	kgrour	nd	17
	2.1	Overvi	iew	17
	2.2	Modul	ation	17
		2.2.1	Bandwidth Efficiency	18
		2.2.2	Error Performance Curves	19
	2.3	Chann	el Coding	21
		2.3.1	Block Coding	21
		2.3.2	Convolutional Coding	22
		2.3.3	Coding Gain	22
	2.4	System	n Operation	22
3	Soft	ware I	Radio Architecture	25
	3.1	Overvi	iew	25
	3.2	Frame	work	26
		3.2.1	Regulatory Limits	26
		3.2.2	Channel Constraints	27
		3.2.3	User Requirements	27
	3.3	Perform	mance Metrics	27
		3.3.1	Latency	28
		3.3.2	Energy Consumption	28
		3.3.3	Data Rate	29
		3.3.4	Probability of Error	29
	3.4	Physic	al Layer Design	29
		3.4.1	Modulation and Coding Choices	29
		3.4.2	Tradeoffs	31
		3.4.3	Selection Process	32
		3.4.4	Assumptions	33
		3.4.5	Example	33

4	802	.11 Framework
	4.1	Overview
	4.2	802.11 Physical Layer
	4.3	Regulatory Constraints
	4.4	Frequency Hopping Implementation
		4.4.1 Frame Format
	4.5	Performance Metrics
		4.5.1 Latency
		4.5.2 Energy Consumption
		4.5.3 Data Rate
		4.5.4 Probability of Error
	4.6	Possible Improvements with Software Radio
	_	
5	Cor	iclusion
	5.1	Summary
	5.2	Future Work
ß	Anr	ondix
U	App	
	6.1	Calculating Minimum Transmit Power
		6.1.1 Transmit power for FSK and (207, 187) Reed Solomon
		6.1.2 Transmit power for 802.11 2.4 GHz at 200 m

# List of Figures

1-1	Mobile ad-hoc network diagram.	13
2-1	Transformation from bits to waveforms.	17
2-2	Error performance curves for several modulation schemes	20
2-3	Possible codeword mapping for a (4,2) block code	21
2-4	Hamming distance between two different codewords	22
2-5	Coding Gain.	23
2-6	System Operation Movement.	23
3-1	Software radio architecture.	25
3-2	Signal processing chain.	26
3-3	Energy consumption for different modulation schemes for a node lo-	
	cated 200 meters (400-byte packet transmitting at 2.4 GHz).	32
3-4	Physical layer design considerations.	32
4-1	Frequency Hopping Spectrum Utilization	38
4-2	802.11 Frame Format.	39
4-3	Error Performance Curves for 2-GFSK and 4-GFSK in 802.11	42

## List of Tables

2.1	Phase shift mapping for QPSK	18
2.2	Probability of bit errors for various modulations	20
3.1	Constraints imposed by regulation.	26
3.2	Constraints imposed by the channel.	27
3.3	Parameters specified by user	27
3.4	Set of possible modulations and coding schemes	30
3.5	Latency and cycles for several different modulation schemes. $\ldots$ .	30
3.6	Latency and cycles for several different coding schemes	30
3.7	Latency and energy consumption for DQPSK and different coding	
	schemes	31
4.1	Constraints imposed by the FCC.	38
4.2	Frequency Hopping Parameters	39

# Chapter 1 Introduction

A mobile ad-hoc network is a collection of wireless nodes that can communicate with each other without any dependence on a fixed infrastructure or centralized administration (see Figure 1-1). Nodes within transmission range can communicate directly with each other, but those out of range must rely on other nodes to forward along packets to their final destination. Because they can be deployed quickly and require no extra planning, ad-hoc networks are often useful for establishing temporary workgroups in classroom settings, business meetings, or disaster relief situations[1].



Figure 1-1: Mobile ad-hoc network diagram.

Mobile ad-hoc networks have also been widely used for tactical military communication systems. The United States Defense Advanced Research Project Agency (DARPA) has sponsored projects such as the Near-Term Digital Radio (NTDR) system to control infantry, armor, and artillery units in battlefield scenarios where no communication infrastructure exists[5]. In addition, the current GloMo program is investigating the use of multimedia voice, data, and video traffic with ad-hoc mobile radio networks[9].

## 1.1 Limitations in Current Wireless Ad-Hoc Systems

There are several limitations in current wireless ad-hoc network systems, which include the inability to adjust to interference, available bandwidth, and different networking standard implementations. Because these systems are usually designed for certain channel characteristics, they have difficulty adjusting to different environments. The examples presented below helps illustrate some of these limitations.

A node operating in a crowded lecture hall encounters very different noise and interference levels than a small classroom. Modulation and channel coding schemes that make efficient use of the available bandwidth should therefore be adjusted to suit these different environments. A node in a crowded lecture hall, for instance, might choose to boost the amount of error correction, while a node in a small classroom might switch to a modulation technique that encodes more data at the expense of a lower tolerance to noise. In current wireless ad-hoc networks, there is very little flexibility to make such dynamic adjustments.

In battlefield situations, infantry and tank battalions are often moving across various terrains and obstacles, causing their communication links to suffer from varying path loss, multipath fading, and signal quality degradation[9]. Because each vehicle acts as a network node and a router, adjustments that can provide additional reliability to the communication link need to be done quickly. Current ad-hoc networks focus on improving reliability at the routing layer[14] [13], but do not allow physical layer parameters such as transmit power, modulation, error control rate, and symbol transmission rate to be easily modified.

Another significant problem facing current ad-hoc network systems involves interoperability. A wireless device supporting the Bluetooth ad-hoc networking standard cannot exchange data messages with a card supporting the 802.11 standard. Similarly, different branches of military and law enforcement agencies have different communication devices that cannot inter-operate with each other, which poses a significant problem during joint operations such as disaster relief, riot control, and drug interdiction[18].

## 1.2 How Software Radio Overcomes these Limitations

Software radio technology attempts to perform all the physical and link layer processing on general purpose processors. A handheld with an analog-to-digital (A/D) converter, for instance, would digitize the RF spectrum of interest and perform the signal processing entirely in software. Dedicated signal processors (DSPs) and application specific integrated circuits (ASICs) to perform down conversion, low-pass filtering, and demodulation would not be needed.

A handheld device in an ad-hoc network currently has an extremely limited battery life. As a result, the additional computational requirements in software radio technology impose too much of a burden to make it practical for today's use. However, with expected advances in low power processors and battery technology, we expect this situation to change in the next three to five years.

There are significant advantages for software radio in ad-hoc networks. Rather than choosing transmission parameters that are suited for certain channel conditions, adjusting transmitter power, modulation, and coding can result in more efficient spectrum and energy use. Such flexibility in making adjustments provides a tremendous advantage for ad-hoc networks, which typically have ill-defined network boundaries, limited spectral bandwidth, and network topologies that constantly change [1].

## 1.3 Related Work

Much research in software radio technology has developed from the SpectrumWare project at the MIT Laboratory of Computer Science. The project explored how a software-oriented signal processing approach could be used for wireless communications. A protocol for mobile hosts to coordinate the transition to a different physical layer was developed in [2]. In addition, the design issues of implementing a software-based frequency hopping spread spectrum radio were explored in [15].

In addition, there has been research investigating the design of architectures that can adapt to different heterogenous wireless networks. A handoff system that allows mobile devices to move seamlessly across different networks is introduced in [19]. Although this system allows a user to move from his office to other parts of a building without connectivity being dropped, it requires the individual to bring the equipment that provides the coverage, such as a WaveLAN card or a Metricom Ricochet modem. A software radio, in contrast, could implement all these standards and eliminate the need for multiple pieces of equipment.

Research has also focused on different medium access control (MAC) protocols for adjusting transmit power levels. A MAC protocol called Power Controlled Multiple Access (PCMA) proposes to use the signal strength of a received control message to limit the transmit power of nearby stations [10]. The work in [20] explores how power control can also be combined with a multiple channel scheme to provide more efficient spectrum usage, and research by [16] examines how varying power based on node densities can be used for large packet radio networks. Finally, the tradeoffs between MAC retransmission and transmit power are studied in [4]. Other parameters of the physical layer such as modulation and coding, however, are not considered.

In [7], the RTS/CTS protocol is modified in the IEEE 802.11 wireless standard to allow the receiver to choose the rate at which a packet is to be transmitted. The physical layer prefaces every packet with a header, which allows for dynamic rate adjustments. The paper assumes that different modulation schemes can be supported in the physical layer, but does not address how such functionality can be provided.

### 1.4 Thesis Scope

The goal of this thesis is to demonstrate how software radio technology in ad-hoc networking can improve spectrum utilization and battery life. The design and framework of a system that allows a user to specify physical layer parameters based on the current needs of the system is introduced. This framework is then applied to the 802.11 standard and used to identify limitations in this specification.

## 1.5 Road Map

The next chapter provides a brief introduction about digital communications and discusses how hardware-based radio implementations are limited. Chapter 3 discusses the API and framework that provides parameters to be adjusted in the physical layer. Chapter 4 examines the current 802.11 standard with this framework.

## Chapter 2

## Background

In this section, we briefly review the fundamental aspects of digital communications that are important to the design of wireless ad-hoc systems. We discuss the various physical layer parameters such as modulation and channel coding that help determine the overall system performance. Finally, we examine how system operation is affected by a fixed modulation and channel coding scheme.

## 2.1 Overview

A signal in a communications system undergoes a series of different transformations before transmission occurs. The incoming bits are first grouped into symbols, which then map to a finite set of sinusoidal waveforms. The limited number of waveforms allows them to be distinguished by the receiver and translated back into binary digits.



Figure 2-1: Transformation from bits to waveforms.

## 2.2 Modulation

Modulation is the process in which digital symbols are converted to sinusoidal waveforms. Varying the amplitude, frequency, and phase allows different waveforms to be created. The general form of these waveforms is represented as follows:

$$s(t) = A(t) \cdot \cos[\omega_0 t + \phi(t)] \tag{2.1}$$

A(t) = amplitude at time t  $\omega_0 = carrier frequency$  $\phi(t) = phase at time t$  There are several common digital modulation schemes, which include phase shift keying (PSK), frequency shift keying (FSK), and amplitude shift keying (ASK). In these schemes, either the amplitude, frequency, or phase is varied. One form of phase shift keying known as Quadrature Phase Shift Keying (QPSK) varies the phase to represent four different symbols. To represent the symbol '10', for instance, QPSK shifts the phase by 180°. Table 2.1 summarizes this mapping.

Symbol	Waveform Equation
00	$s(t) = A(t) \cdot \cos[\omega_0 t]$
01	$\mathbf{s}(\mathbf{t}) = \mathbf{A}(\mathbf{t}) \cdot \cos[\omega_0 \mathbf{t} + 90^o]$
10	$\mathbf{s}(\mathbf{t}) = \mathbf{A}(\mathbf{t}) \cdot \cos[\omega_0 \mathbf{t} + 180^o]$
11	$\mathbf{s}(\mathbf{t}) = \mathbf{A}(\mathbf{t}) \cdot \cos[\omega_0 \mathbf{t} + 270^o]$

Table 2.1: Phase shift mapping for QPSK

The number of waveforms needed depends on the number of bits used to represent symbols. For instance, QPSK requires two bits to represent four different waveforms. In the general case, if k bits per symbol are used, then  $2^k$  waveforms are needed. We often refer this technique as M-ary signalling, where M equals  $2^k$ .

Other modulation schemes are variations of phase, frequency, and amplitude modulation. A modulation technique known as Amplitude Phase Keying (APK) varies the amplitude and phase of the sinuosoid to produce different sets of waveforms. In Quadrature Amplitude Modulation (QAM), two amplitude-modulated sinusoids, 90° degrees are out of phase with each other, are used to transmit data.

#### 2.2.1 Bandwidth Efficiency

We can determine the overall efficiency for a particular modulation, expressed as bits/s/Hz, by measuring the number of bits transmitted in a given amount of time divided by the bandwidth used. If there are k bits per symbol and  $T_s$  represents the duration for a symbol to be transmitted, the data rate can be calculated by dividing these two quantities. The efficiency can then be determined by dividing by the total amount of bandwidth, expressed as Hz, that is used. Equation 2.2 represents this calculation.

$$\frac{R}{W} = \frac{k}{WT_s} bits/s/Hz$$
(2.2)

R = data rate (bits/s)W = bandwidth (Hz) k = bits per symbol (bits)  $T_s = \text{symbol duration (s)}$ 

For instance, for MPSK modulation, the bandwidth efficiency is  $log_2 M$  bits/s/Hz [17], where M represents the number of waveforms used. As M increases, the band-

width efficiency also increases. The increased bandwidth efficiency, however, comes at a cost of increased bit energy to noise ratio,  $\frac{E_b}{N_0}$ .

The bandwidth efficiency can also be used to calculate the maximum data rate that can be supported by the modulation. The bandwidth of the channel can be multiplied by this ratio. For 64-QAM, the theoretical maximum bandwidth efficiency is  $log_{10}64 = 12$  bits/s/Hz. For a 2 MHz channel, the maximum data rate would be 24 Mbps (12 bits/s/Hz · 2 MHz).

#### 2.2.2 Error Performance Curves

An important property of a given modulation technique is the required bit energy to noise ratio  $\left(\frac{E_b}{N_0}\right)$  needed to achieve a certain level of performance. Performance is measured in terms of the number of errors occur per bits sent. A desired probability of  $10^{-5}$ , for instance, means that an error occurs less than once for every  $10^5$  bits transmitted.

The fraction  $\frac{E_b}{N_0}$  can be determined by multiplying the received signal strength with the bandwidth and dividing it by the product of the noise level and data rate. We note that an increase in noise or data rate results in a decrease in  $\frac{E_b}{N_0}$ . We also observe that  $\frac{E_b}{N_0}$  increases with signal power and bandwidth. Equation 2.3 represents this calculation:

$$\frac{E_b}{N_0} = \frac{S}{N} \left(\frac{W}{R}\right) \tag{2.3}$$

S = received signal power (W or dB)

N = noise level (W or dB for a bandwidth of 1 Hz)

R = data rate (Mbps)

W = bandwidth (Hz)

If the noise is distributed uniformly across a certain bandwidth, then the expression simplifies to the following:

$$\frac{E_b}{N_0} = \frac{S}{N} (\frac{1}{R}) \tag{2.4}$$

Table 2.2 lists approximated bit error rates for many different types of modulations [17] [3]. The table is divided into two different columns: coherent and noncoherent detection. In coherent modulation schemes, the receiver uses knowledge of the phase for detection. Coherent modulation schemes tend to have a lower  $\frac{E_b}{N_0}$  requirement for the same probability of bit error than non-coherent modulation schemes, but additional circuitry is required in order to track the signal and usually results in increased complexity and higher cost.

The function Q(x), known as the complementary error function, is defined as follows [17]:

$$Q(x) \simeq \frac{1}{\sqrt{2\pi}} \int_x^\infty exp(-\frac{u^2}{2})du$$
(2.5)

Modulation	Coherent detection	Noncoherent detection
BPSK	$Q \left[ \sqrt{2(\frac{E_b}{N_0})} \right]$	Requires coherent detection
FSK	$\mathrm{Q} \left[ \sqrt{rac{E_b}{N_0}}  ight]$	$\frac{1}{2} e^{-(\frac{1}{2})(\frac{E_b}{N_0})}$
DPSK	Not used in practice	$\frac{1}{2}e^{-(\frac{E_b}{N_0})}$
QPSK	$Q \left[ \sqrt{2(\frac{E_b}{N_0})} \right]$	Requires coherent detection
M-QAM	$\frac{2(1-M^{-1})}{\log_2 M}$ Q $\left[\sqrt{\left(\frac{3\log_2 M}{M^2-1}\right)\frac{2E_b}{N_0}}\right]$	Requires coherent detection

Table 2.2: Probability of bit errors for various modulations.

Figure 2-2 is a figure of the plotted error performance curves for various modulations, including PSK, 2-FSK, 4-FSK, 4-QAM, and 8-QAM. For any of these performance curves, we note that reducing the probability of error requires an increase in  $\frac{E_b}{N_0}$ . An increase can only occur if a higher transmission power is used or the noise level is reduced. We also observe that the error performance curve for 4-FSK is shifted to the right of 2-FSK, which indicates that performance degrades when encoding more bits per symbol for this particular modulation.



Figure 2-2: Error performance curves for several modulation schemes.

### 2.3 Channel Coding

Channel coding refers to the various signal transformations that can be performed to enable transmitted signals to better withstand the effects of various channel impairments, such as noise and interference[17]. One form of channel coding is known as forward error correction (FEC), which adds redundant information to data that is being transmitted. There are two major types of forward error correction, which include block and convolutional coding.

#### 2.3.1 Block Coding

Block codes are often referred to as (n, k) codes because an encoder takes a data block of k bits and maps them to a larger block of n bits. The (n - k) bits, which are added to each data block, are the redundant bits added. These bits are also known as parity or check bits, because they provide a mechanism for error detection or correction.

In block codes, there are  $2^n$  possible codewords but only  $2^k$  sequences that map to this larger set. In a (4,2) block code, for instance, there are  $2^4$  or 16 possible codewords but only  $2^2$  sequences. Figure 2-3 demonstrates a possible mapping. An



Figure 2-3: Possible codeword mapping for a (4,2) block code.

important consideration when choosing an appropriate mapping is the Hamming distance, which is defined as the minimum number of bits that are different between any two codewords in the set. Figure 2-4 illustrates this concept.

A code's ability to detect and correct errors is dependent on the Hamming distance, since the maximum number of errors that can be detected and corrected is determined by this value. Equations 2.6 and 2.7 specifies the maximum number of errors that can be detected and corrected.

$$e_{detect} = d_{min} - 1 \tag{2.6}$$

01111 Hamming distance = 4 10001

Figure 2-4: Hamming distance between two different codewords.

$$e_{correct} = \left\lceil \frac{d_{min} - 1}{2} \right\rceil \tag{2.7}$$

#### 2.3.2 Convolutional Coding

Another type of forward error correction is known as convolutional coding, which uses shift registers and adders to generate codewords. There are two parameters associated with these type of codes: the code rate and constraint length. The code rate, k/n, represents the ratio of the number of bits into the encoder to the number of channel symbols output by the encoder in a given cycle. The constraint length, K, represents the number of stages in a shift register.

Convolutional codes typically are more powerful, but are much more computationally expensive to decode. During the decoding process, the most likely sequence of possible codewords is chosen, usually using the Viterbi algorithm [17]. An important parameter of this process is the minimum free distance  $(d_f)$ , which affects the number of correctable bits for a convolutional code:

$$e_{correct} = \left\lceil \frac{d_f - 1}{2} \right\rceil \tag{2.8}$$

#### 2.3.3 Coding Gain

The coding gain, expressed as decibels (dB), specifies the difference in  $\frac{E_b}{N_0}$  needed to achieve the same error probability with a coding scheme. Figure 2-5 illustrates this concept.

In general, convolutional codes have much higher coding gains for the same ratio k/n than block codes. The tradeoff, as mentioned previously, is that convolutional decoding tends to require much more complexity.

### 2.4 System Operation

System performance is influenced by the choice of modulation and coding scheme. Movement along the error performance curve results in various tradeoffs. First, increasing transmitter power will also cause an increase in  $\frac{E_b}{N_0}$ , which helps to improve bit error probability. The tradeoff is shorter battery life because of the higher power



Figure 2-5: Coding Gain.

dissipation. This movement is reflected in the movement between points a and b in Figure 2-6.



Figure 2-6: System Operation Movement.

Movements between points c and d, however, require changes to the modulation and coding scheme. As shown in Figure 2-6, a lower error probability might be achievable with a different pair with the same  $\frac{E_b}{N_0}$  requirement. Hardware-based radio implementations do not provide such flexibility. Software radio technology, however, would allow a system's modulation and coding to be changed by programmable means [17]. Such capability would allow systems to adapt their physical layers to better suit different environments.

## Chapter 3

## Software Radio Architecture

The software radio approach for a physical layer design is presented in this section. We introduce a framework that describes the various considerations that must be made in choose an appropriate modulation and coding pair. Finally, we provide an example of how this framework might be used for ad-hoc network situations.

### 3.1 Overview

The proposed approach is to perform much of the signal processing tasks of the physical layer in software. An RF frontend takes a wideband of spectrum and downconverts it to an intermediate frequency (IF), which can then be sampled by an A/D converter. The samples can then be processed in the operating system. Figure 3-1 illustrates this architecture.



Figure 3-1: Software radio architecture.

All modulation and coding schemes are implemented as modules. Each of these modules, instantiated as a C++ class, can then be connected into a signal processing chain. Figure 3-2 demonstrates an example of a signal processing chain that could be created.

Because of this modular design, a range of modulation and channel coding schemes can then be supported. A change from 2-PSK to 2-FSK modulation, for instance, simply requires the two different modules to be substituted. The substitution can occur by disconnecting the input and output ports of the original module and reconnecting it to the new module.



Figure 3-2: Signal processing chain.

## 3.2 Framework

There are three major categories that impose constraints on the selection of an appropriate modulation and coding pair: regulatory limits, channel conditions, and user requirements. Regulatory limits are relatively static, while channel conditions and user requirements often vary in ad-hoc network situations. We discuss each of these categories in further detail.

#### 3.2.1 Regulatory Limits

In the United States, regulatory limits are imposed by the Federal Communications Commission (FCC). The set of rules and regulations are described in Title 47 in the Code of Federal Regulations (CFR), which establish maximum power emission limits and specify harmful interference levels. Part 15.247 concerning the 902-928 MHz, 2400-2483.5 MHz, and 5725-5850 MHz bands also contain provisions about the use of spread-spectrum technology.

Constraint	Variable	Units
Bandwidth	BW	hertz (Hz)
TX Power	$P_{tx}$	watts (W)

Table 3.1: Constraints imposed by regulation.

The major regulatory limits that affect the selection of modulation and coding scheme are maximum bandwidth and maximum transmission power. Limits on bandwidth affects the achievable data rate, while limits on transmission power places constraints on the maximum signal strength that can be received. We represent these terms as BW and  $P_{tx}$ , respectively. Table 3.1 summarizes these constraints.

#### 3.2.2 Channel Constraints

The Shannon-Hartley capacity theorem provides insight into the maximum data rate of a channel. Capacity is defined as bits/s and depends on the signal-to-noise ratio (SNR) and bandwidth (W). Equation 3.1 represents the upper bound on the maximum achievable data rate, assuming that the only noise present in the system can be modeled as a Gaussian process.

$$C = W \log_2\left(1 + \frac{S}{N}\right) \tag{3.1}$$

We observe that only bandwidth and the signal-to-noise ratio (SNR) affects the achievable data rate. Maximum bandwidth is constrained by regulation, as we noted in the previous section. The signal-to-noise-ratio, on the other hand, is affected by several factors, including the current noise and interference level, transmit distance, and attenuation that occurs during signal propagation.

Constraint	Variable	Units
Noise Power	$N_0$	watts (W)
Transmit Distance	$d_{tx}$	meters (m)

Table 3.2: Constraints imposed by the channel.

#### 3.2.3 User Requirements

Varying applications will have different degrees of tolerance for latency, data rate, error rate, and energy consumption. For instance, a bit error rate of  $10^{-3}$  is considered acceptable for a voice link but  $10^{-7}$  may be required for a data link. We summarize these varying constraints in Table 3.3.

Constraint	Variable	Units
Latency	$ au_{L_{user}}$	s/packet
Data Rate	$R_{user}$	bits/s
Bit Error Rate	$p_{e_{user}}$	bit errors/ total bits
Energy Consumption	$P_{d_{user}}$	joules/packet

Table 3.3: Parameters specified by user.

## **3.3** Performance Metrics

We use these four constraints to help define the amount of latency, energy consumption, data rate, and probability of error for a given modulation and coding pair. A user's specified requirements is compared with the set of available of combinations to find a an appropriate match.

#### 3.3.1 Latency

Latency is defined in terms of the processing delay of a packet through the physical layer. In dedicated signal processing systems, incoming samples arrive at a constant rate and are processed with a fixed delay between when a sample enters the system and when the output based on that sample leaves [8]. In a software radio based architecture, such guarantees may not be possible because virtual memory, multiple levels of caching, and competition for the I/O may add jitter to the expected amount of time for a sample to be processed.

The latency, however, can still be approximated by evaluating the amount of time it takes to process the coding and modulation on a packet. We then add the propagation delay to this sum, which is dependent on the packet size and the data rate. The latency per packet for a given modulation and coding, denoted as  $\tau_L$ , is therefore represented in Equation 3.2.

$$\tau_L = (\tau_{mod} + \tau_{coding}) \cdot N_{packet} + \frac{N_{packet}}{R}$$
(3.2)

where  $\tau_{mod}$  and  $\tau_{coding}$  represents the amount of seconds needed to compute the modulation and coding per bit,  $N_{packet}$  equals the number of bits per packet, and R refers to the data rate in bits per second.

#### 3.3.2 Energy Consumption

Another important metric is the amount of energy needed to compute and send a packet. The total energy depends on several factors, including data rate. Data rate influences how long the transmitter must remain on, so a faster data rate results in less energy needed. For instance, assuming 30 mW is used for transmission, the amount of energy needed to send a 1500-byte packet at 1 Mbps is 360  $\mu$ J. At 9600 bits/s, the amount of energy needed is 38 mJ.

Energy consumption also depends on the amount of time needed to compute the coding and modulation for the packet. We can represent this value by multiplying the nominal core power of a processor by the cycle count and clock period of the processor. The amount of energy consumed, therefore, is defined in Equation 3.3.

$$P_d = P_{tx} \cdot \left(\frac{N_{packet}}{R}\right) + P_{processor} \cdot CLK \cdot (C_{mod} + C_{coding}) \cdot N_{packet}$$
(3.3)

where  $P_{tx}$  equals the transmit power level in watts, R represents the data rate in bits/s,  $P_{processor}$  represents the average power dissipation of the processor in joules per second, CLK equals the clock period of the processor (seconds/clock cycle),  $C_{mod}$  and  $C_{coding}$  is the cycles needed to compute the modulation and coding per bit, and  $N_{packet}$  equals the number of bits per packet.

#### 3.3.3 Data Rate

The maximum data rate that can actually be achieved is bounded not only by the Shannon capacity limit but also the modulation and coding scheme used. A modulation has a certain bandwidth efficiency, defined as bits/s/Hz, so the fastest that can be achieved is simply this value multiplied by the total amount of bandwidth available.

The effective data rate is reduced by the amount of overhead needed to transmit the packet. The ratio  $\frac{N_{payload}}{N_{packet}}$  represents the fraction of bits used for the payload, and coding rate  $R_c$  represents the percentage bits not used for error correction. Thus, the maximum data rate can be expressed as follows:

$$R_{max} = B_{efficiency} \cdot BW \cdot \frac{N_{payload}}{N_{packet}} \cdot R_c$$
(3.4)

where  $B_{efficiency}$  represents the bandwidth efficiency in bits/s/Hz, BW equals the bandwidth in Hz,  $N_{payload}$  equals the number of bits in the payload, and  $N_{packet}$  is the number of bits in the packet, and  $R_c$  refers to the percentage of bits not used for error correction.

#### 3.3.4 Probability of Error

The final constraint is the probability of error, which measures how often a packet has to be retransmitted. The probability of error for a chosen moduation and channel code can be determined by calculating  $\frac{E_b}{N_0}$  and using its associated error performance curve. The calculated  $\frac{E_b}{N_0}$  will be a function of transmitted power, noise power, and distance.

$$p_e = P_b\left(P_{tx}, N_0, d_{tx}\right) = P_b\left(\frac{E_b}{N_0}\right) \tag{3.5}$$

### **3.4** Physical Layer Design

The framework presented can be used to control physical layer parameters that more accurately reflects current channel conditions and user requirements. In this section, we discuss the various tradeoffs involved in selecting an appropriate modulation and coding pair.

#### **3.4.1** Modulation and Coding Choices

Tables 3.4 shows a set of possible modulation and coding schemes that might be supported. The maximum theoretical bandwidth efficiency, which defines the most number of bits that can be transmitted per hertz, is included for the modulation schemes. An upper bound of the coding gain, which defines the reduction in  $\frac{E_b}{N_0}$  to achieve the same level of probability with an uncoded modulation technique, is noted for each of the channel codes.

Modulation	Bandwidth Efficiency	Channel Code	Coding Gain
	(bits/s/Hz)		$(\gamma_c)$
2-FSK	1	(23, 12) Golay	$1.64 \ (2.15 \ \mathrm{dB})$
BPSK	1	(207, 187) Reed Solomon	2.00 (3  dB)
4-PSK	2	rate $\frac{1}{2}$ convolutional, K = 5	3.5 (5.44  dB)
8-PSK	3		
16-QAM	4		
16-PSK	4		

Table 3.4: Set of possible modulations and coding schemes.

Several modulation and coding schemes were implemented as C++ modules and benchmarked with the GNU profiler. The profiling program generates information about how much time each module spends processing a sample, which can then later be used to determine the total amount of latency and amount of power consumed per bit. Tables 3.5 and 3.6 shows several of these benchmarked values performed on a Pentium III 1 GHz machine.

Modulation	Latency	Cycles
2-FSK	8.89 $\mu$ s/sample (8.89 $\mu$ s/bit)	8890 cycles/bit
DQPSK	$2.24 \ \mu s/sample (1.12 \ \mu s/bit)$	1120 cycles/bit

Table 3.5: Latency and cycles for several different modulation schemes.

In order to calculate the total latency for a packet, the latency first needs to be converted to cycles per bit. For modulation schemes, the sample size depends on the number of bits used to encode a symbol. 2-FSK, for instance, processes one bit per sample. DQPSK, on the other hand, processes two bit per sample.

Since a (n, k) channel code processes k bits at a time, the number of seconds per bit can be calculated by dividing the latency by k. For the (23, 12) Golay code, for instance, the latency per bit is equal to 22.2 ns/bit (266.67 ns/sample / 12).

Coder	Latency	Cycles
(23, 12) Golay	266.67  ns/sample (22.2  ns/bit)	222  cycles/bit
(207, 187) Reed Solomon	.107  ms/sample (572  ns/bit)	5721 cycles/bit
$\frac{1}{2}, K = 5$ convolutional	7722.57 ns/sample (7722.57 ns/bit)	7722.57 cycles/bit

Table 3.6: Latency and cycles for several different coding schemes.

The cycles needed to compute the modulation or coding scheme can be determined by first dividing the number of bits processed per sample by the total time spent to process the sample. The clock speed of the processor divided by this value then yields the number of cycles per bit. For 4-PSK, the number of cycles is equal to 112 cycles/bit (1 GHz / (2 bit/sample / 2.24 us/sample). Similarly, the number of cycles for (23, 12) Golay code is 222 cycles/bit (1 GHz / (12 bits/sample / 266.67 ns/sample)).

#### 3.4.2 Tradeoffs

There are various tradeoffs to consider in trying to satisfy the equations presented in the framework. Increasing data rate reduces latency and energy, but causes the probability of error to increase. Increasing transmit power comes at the expense of battery life, but reduces the probability of error. Finally, the various computational requirements have different effects on latency, energy consumption, data rate, and probability of error. We consider the various options in this section.

Data Rate vs. Probability of Error. Increasing the data rate decreases both latency and energy consumption. The data rate determines the propagation delay for a packet, so doubling the rate causes the delay to decrease by the same amount. Energy consumption is also slightly decreased, because the transmitter stays on for less amount of time. The latency and energy consumption for DQPSK and various coding schemes with different data rates (assuming a 400-byte packet transmitting at 30 mW on a Pentium III 1 GHz machine) is shown in Table 3.7.

Modulation/Coding	9600 bps	1 Mbps
DQPSK (uncoded)	336.9 ms / 39.0 $\mu$ J	$31.6 \text{ ms} / 35.9 \ \mu\text{J}$
DQPSK/(23, 12) Golay	$337.6 \text{ ms}/110.0 \ \mu\text{J}$	$75.0 \text{ ms}/106.9 \ \mu\text{J}$
DQPSK/(207, 187) Reed Solomon	355.2 ms / 1869.7 $\mu \mathrm{J}$	$25.1 \text{ s}/1866.6 \ \mu\text{J}$

Table 3.7: Latency and energy consumption for DQPSK and different coding schemes.

Increasing the data rate, however, comes at the expense of probability of error. We note from Equation 2.3 that increases in data rate also causes the  $\frac{E_b}{N_0}$  to lower by the same amount. For BPSK modulation, doubling the data rate causes the  $\frac{E_b}{N_0}$  ratio to decrease by a factor of two.

**Transmit power**  $(P_{tx})$  vs. **Probability of Error**. Because  $\frac{E_b}{N_0}$  is proportional to the received signal power (as expressed in Equation 2.3), an increase in transmitted power causes the probability of error for a chosen modulation and coding scheme to decrease. This improvement, however, comes at the expense of energy.

Figure 3-3 charts the probability of error versus power dissipation requirements for a node transmitting to another node located 200 meters apart at 2.4 GHz. The required received signal power, after accounting for distance (see Appendix 6.1), is used to determine the minimum amount of power needed to transmit for a particular modulation scheme. The number of joules needed for this transmission is then added to the number of joules needed to perform the computation, as specified in Equation 3.3.



Figure 3-3: Energy consumption for different modulation schemes for a node located 200 meters (400-byte packet transmitting at 2.4 GHz).

Latency and Energy Consumption vs. Probability of Error. Convolutional codes tend to produce coding gains for probability of errors at  $10^{-5}$  of between 4.0-5.0 dB. In contrast, block codes, which include both Reed Solomon and Golay codes, produce about 2.0-4.0 dB coding gains [3]. However, as shown in Tables 3.4 and 3.6, the improvement comes at a cost at both latency and energy. A (24, 12) Golay code requires 222 cycles/bit, while a rate  $\frac{1}{2}$  convolutional code requires approximatley 10157 cycles/bit. Channel codes which produce higher coding gains, which translate to a lower probability of error, tend to require more processing.

#### 3.4.3 Selection Process



Figure 3-4: Physical layer design considerations.

We propose a method for choosing a particular modulation and coding pair. First, the physical layer must be provided with the following information: desired data rate, bit error rate, latency, and power dissipation. This information is then incorporated with the regulatory limits and channel conditions, as shown in Figure 3-4.

The next step is to choose a coding/modulation pair with the bandwidth efficiency and coding rate that could support the required data rate. We then use equation 3.2 to see if the pair meets the user imposed latency constaint. If the inequality is not satisfied, then we choose another pair and start over the process.

If the latency equation is met, the next step is to determine the transmit power required. Because all of the parameters in inequality 3.5 are known except for  $P_{tx}$ , we can determine the minimum transmit power required to meet the probability of error constraint by solving for  $P_{tx}$ .

The value calculated for  $P_{tx}$  can be used to check that the power constraint of inequality 3.3 is met. If not, then several options can be considered. The first is to lower transmit power at the cost of causing a higher bit error rate. The second option is to increase data rate at the expense of probability of error. Alternatively, the power constraint can be relaxed. Lastly, a different modulation and coding scheme might be attempted.

If there is no pair that adequately meets the requirements, then a metric for deciding the closest match might be needed. One option, for instance, is to minimize the bit error rate at the expense of the other parameters.

#### 3.4.4 Assumptions

There are several assumptions in this framework. First, the choice of a particular modulation scheme often depends on other characteristics besides their maximum theoretical bandwidth efficiency. Quadrature Amplitude Modulation (QAM), for instance, tends to be more susceptible to amplitude and phase distortion than PSK or FSK [12]. The choice of modulation, therefore, may need to include other factors besides maximum data rate.

Second, calculating the minimum transmit power based on the required  $\frac{E_b}{N_0}$  is assumed to minimize power dissipation. Lower transmit power, which results in higher bit error rates, may cause more packet retransmissions that the amount of energy consumed may be higher than transmitting at a higher power level [4]. In addition, the optimal transmit power may actually be to choose an algorithm that delivers a constant, pre-determined amount to the intended receiver [16].

Finally, the distance is assumed to be known by using the received signal strength from a previous transmission exchanged between the nodes. If this previous transmission incurs significant multipath distortion, the amplitude of the signal may provide an incorrect estimate of distance. In addition, the two nodes may not have communicated previously or may not know about each other's existence.

#### 3.4.5 Example

Suppose that the maximum bandwidth available (BW) is 500 kHz, maximum transmit power allowed  $(P_{tx})$  is 1 watt, noise level  $(N_0)$  equals  $2.00 \cdot 10^{-17}$  W, and the distance between two nodes  $(d_{tx})$  is 500 meters. The user also specifies the maximum

tolerable latency  $(\tau_{L_{user}})$ , maximum power dissipation  $(P_{d_{user}})$ , minimum data rate  $(R_{user})$ , and the minimum bit error rate  $(p_{e_{user}})$ :

Maximum latency  $(\tau_{L_{user}}) = \leq 70 \text{ ms per packet}$ Maximum energy consumption  $(P_{d_{user}}) = \leq 5.4 \text{ mJ per packet}$ Minimum data rate  $(R_{user}) \geq 115,200 \text{ bps}$ Minimum BER  $(p_{e_{user}}) \geq 10^{-5}$ 

From the available modulation and coding schemes listed in Table 3.4, we first try choosing 2-FSK and the rate  $\frac{1}{2}$  convolutional code. The maximum data rate that can be supported by this particular pair (assuming the payload comprises of entire packet) can be calculated using Equation 3.4. Since this value is equal to 250,000 bps, the modulation can support the required data rate.

$$R_{max} = 1bits/s/Hz \cdot 500kHz \cdot 1 \cdot \frac{1}{2}$$
$$= 250,000bps$$

The latency constraint specified in 3.2 is first checked to see if it meets the user's requirements (assuming a 400-byte packet):

$$\tau_L = (\tau_{mod} + \tau_{coding}) \cdot N_{packet} + \frac{N_{packet}}{R}$$
  
= (8.89\mus/bit + 7722.57ns/bit) \cdot 3200bits +  $\frac{3200bits}{115,200bps}$   
= 80.9ms/packet

Because the user has requested a latency of less than 70 ms, this modulation and coding pair is not appropriate. The next step is to find another pair that does meet this constraint. 2-FSK and a (207, 187) Reed Solomon coder would be one candidate, since it has a calculated latency of approximately 56.3 ms and maximum data rate of 452 kbps.

The next step would be to determine the minimum transmit power. For FSK, the approximate  $\frac{E_b}{N_0}$  for a bit error rate of  $10^{-5}$  based on Figure 2-2 is equal to 12.5 dB, or 17.78. With a (207, 187) code that provides a 3.0 dB coding gain, this ratio translates into approximately a transmit power of 50.1 mW (see Appendix 6.1.1)

The next step is to see if the power constraint is held. The processor that performs the modulation and coding is assumed to be a Pentium III 1 GHz machine with an average power dissipation of 100 mW. Using 3.3, the amount of energy consumed would be calculated as follows:

$$P_d = P_{tx} \cdot \left(\frac{N_{packet}}{R}\right) + P_{processor} \cdot CLK \cdot (C_{mod} + C_{coding}) \cdot N_{packet}$$

$$= 50.1 \cdot 10^{-3} W \cdot \left(\frac{3200 bits}{115,200 bps}\right) + 100 \cdot 10^{-3} W \cdot \left(\frac{1}{10^9 cycles/s}\right) (8890 + 5721 cycles) \cdot 3200$$
  
= 6.07mJ

Because this amount is too large for the user's specified requirement, we have several options. The first is to try a different modulation and coding pair, which would mean to restart the entire process. The second option is to attempt to increase the data rate to reduce the amount of energy consumed during transmission.

However, increasing the rate from 115,200 bps to 192,000 bps results in a 2.2 dB change ( $10log_{10}$  192000 -  $10log_{10}$  115200). This rate change would drop the error probability from  $10^{-5}$  to  $10^{-4}$  (according to Figure 2-2). However, even with this rate change, energy consumption is only reduced to 5.51 mJ, which still does not meet the user requirements.

The next option is to try to recalculate the minimum transmit power needed for a lower error probability, such as  $10^{-3}$ . The resulting amount would be 23.1 mW, which would result in a total energy consumption of 5.31 mJ. Therefore, for this particular modulation and coding scheme, the probability of error and/or data rate would need to be sacrificed to reduce the energy consumption.

## Chapter 4

## 802.11 Framework

## 4.1 Overview

In this section, we evaluate the advantages that a software radio might provide to the 802.11 wireless LAN standard. We use the framework to help identify areas which have limited flexibility and discuss some of the tradeoffs involved.

## 4.2 802.11 Physical Layer

There are three different specifications for the 802.11 physical layer: frequency hopping spread spectrum (FHSS), direct sequence spread spectrum (DSSS), and infrared. The frequency hopping spread spectrum operates by transmitting a short burst on one frequency and then changing to another short period of time in a predefined pattern known only to both the transmitter and receiver [1]. A direct sequence spread spectrum system, on the other hand, distributes the energy of the signal over a large bandwidth. Infrared systems, in contrast, vary the intensity of the current in an infrared emitter.

### 4.3 Regulatory Constraints

The Federal Communications Commission (FCC) imposes many regulation limits on the unlicensed 2.4 GHz band, which is designated in the United States for industrial, scientific, and medical (ISM) purposes. Many different wireless LAN standards, including 802.11, operate over this band for transmitting and receiving data. As a result, systems which use the 2.4 GHz band must be designed to handle any possible sources of interference.

The FCC also imposes limits on transmit power. For devices that do not employ spread spectrum technology, a maximum transmit power of .75 mW is allowed. Frequency hopping and direct sequence systems, which are forms of spread spectrum technology, are limited to 1 watt[6]. Table 4.1 lists the bandwidth and transmit power limitations imposed by the FCC. However, there are also other regulatory constraints that pertain only to frequency hopping spread-spectrum devices. First, frequency hopping devices are allowed to occupy at most 5 MHz of bandwidth. They must also "hop" across a minimum of 15 channels which span across a total of 75 MHz in bandwidth. Finally, the system must not spend more than 400 ms in a particular channel within a 30 second period.

Constraint	Value
Bandwidth $(BW)$	75 MHz (direct sequence spread spectrum)
	5 MHz (frequency hopping spread spectrum)
TX Power $(P_{tx})$	1 W (spread spectrum)
	.75 mW (non spread-spectrum)

Table 4.1: Constraints imposed by the FCC.

## 4.4 Frequency Hopping Implementation

The 802.11 frequency hopping implementation divides the 2.4 GHz band into 78 frequencies, each occupying 1 MHz of bandwidth (see Figure 4-1). A pseudorandom generator defines the hopping sequence pattern, which consists of 26 channels. The maximum time spent in any channel is specified for 224  $\mu$ s.



Figure 4-1: Frequency Hopping Spectrum Utilization.

To achieve the 1 Mbps and 2 data rates, a modulation scheme known as Gaussian Frequency Shift Keying (GFSK) is used. GFSK is a form of frequency modulation (FM), in which different symbols are represented by variations in the carrier frequency. The major difference is that GFSK modulation first filters the binary data with a

pulse-shaping filter. This filter is needed in order to limit the bandwidth of the signal to 1 MHz.

The 802.11 standard supports up to eight transmit power levels, but there is no specific requirement. Instead, the standard states that an implementation which uses a transmit power of more than 100 mW must also support one power level below that amount. In many FHSS wireless LAN cards, transmit power is fixed at 100 mW.

Data Rate	1 Mbps (2-GFSK)
	2 Mbps (4-GFSK)
Transmit Power	Up to 8 different levels
	(if one level $> 100 \text{ mW}$ , another must be $< 100 \text{ mW}$ )
Hopping Sequence	3 sets of 26 channels (minimum hop distance of 6 channels)

Table 4.2: Frequency Hopping Parameters.

#### 4.4.1 Frame Format

The frame format defines how data is transmitted at the physical layer. It contains information about the type of modulation and data rate employed, in addition to a field that specifies the length of the payload. Figure 4-2 contains a diagram of the format.



Figure 4-2: 802.11 Frame Format.

The frame is divided into three sections: preamble, header, and payload. The preamble includes the synchronization and start of frame delimiter, which is used by the receiver to detect the presence of a signal. The header provides information about the type of modulation and data rate that will be used to send the payload, in addition to the size of the payload. Finally, the payload includes the data that needs to be transmitted.

### 4.5 Performance Metrics

The feasibility of implementing a software-based frequency hopping system has already been demonstrated in [15]. However, the benefits for ad-hoc networks has not been closely examined. In this section, we apply the framework and discuss areas in which a software radio architecture could provide additional benefits.

#### 4.5.1 Latency

The header and payload are transmitted separately. While the header is always transmitted with a fixed modulation and data rate, the payload can be transmitted at 1 or 2 Mbps data rate. As a result, the latency for sending the preamble and header is 192  $\mu$ s.

Modules for GFSK and CRC-16 were also implemented and benchmarked on a Pentium III 1 GHz machine. The computational cost for GFSK modulation is about 8.89  $\mu$ s/bit (8890 cycles/bit), while CRC-16 takes approximately 1708.9 ns/bit (1708.9 cycles/bit). The latency, therefore, can be represented as follows:

$$\tau_L = (\tau_{GFSK} + \tau_{CRC-16}) \cdot N_{packet} + 192\mu s + \frac{N_{packet}}{R}$$

$$\tau_L = (8.89\mu s/bit + 1708.98ns/bit) \cdot N_{packet} + 192\mu s + \frac{N_{packet}}{R}$$

$$\tau_L = (10.5 \cdot \mu s/bit) \cdot N_{packet} + 192\mu s + \frac{N_{packet}}{R}$$

$$(4.1)$$

where  $N_{packet}$  equals the number of bits per packet (usually 3200 bits), and R refers to either 1 or 2 Mbps.

#### 4.5.2 Energy Consumption

Additional power is required to keep parts of an 802.11 network card active for transmission or reception [4], but we only consider the energy consumption for sending a packet. There are actually two separate transmissions that take place, since the header and payload are sent separately. The amount of energy consumed can be represented as follows:

$$P_{d} = P_{tx} \cdot \left(\frac{N_{packet}}{R}\right) + P_{processor} \cdot CLK \cdot \left(C_{GFSK} + C_{CRC-16}\right) \cdot N_{packet}$$
(4.2)  
$$= P_{tx} \cdot \left(\frac{N_{packet}}{R}\right) + P_{processor} \cdot CLK \cdot \left(8890 cycles/bit + 1708.9 cycles/bit\right) \cdot N_{packet}$$
$$= P_{tx} \cdot \left(\frac{N_{packet}}{R}\right) + P_{processor} \cdot CLK \cdot \left(10598.9 cycles/bit\right) \cdot N_{packet}$$

where  $P_{tx}$  equals approximately 100 mW, R represents 1 or 2 Mbps,  $P_{processor}$  is assumed to be 100 mW, CLK equals  $10^{-9}$  s/clock cycle (for a Pentium III 1 GHz),  $C_{GFSK}$  and  $C_{CRC-16}$  is the cycles needed to compute the modulation and coding per bit, and  $N_{packet}$  equals the number of bits per packet (usually 3200 bits).

#### 4.5.3 Data Rate

The 802.11 standard uses a fixed transmission symbol rate of 1 Msymbols/s, but varies the modulation scheme with either 2-GFSK and 4-GFSK. Therefore, the maximum data rate is either 1 or 2 Mbps. No forward error correction is used, so the coding rate  $R_c$  equals 1. The effective data rate can therefore be represented as follows:

$$R_{max} = 1 or 2M bps \cdot \frac{N_{payload}}{N_{packet}}$$

$$\tag{4.3}$$

where  $N_{payload}$  equals the number of bits in the payload and  $N_{packet}$  equals  $N_{payload}$  plus 128 bits for the preamble and header.

#### 4.5.4 Probability of Error

The error performance curves for 2-GFSK and 4-GFSK are plotted using MATLAB in Figure 4-3 (See Appendix 6.1.3). GFSK modulation has a parameter known as the modulation index, which is defined as the frequency separation for representing different symbols multiplied by the data rate [24]. In 2-GFSK, this modulation index is set to .32, which means that the frequencies used to represent a logical '0' and '1' are separated by 320 kHz (.32  $\cdot$  1 Mbps). In 4-GFSK, the average modulation index is .144, which means the frequencies to represent the different symbols are separated by 288 kHz (.144  $\cdot$  2 Mbps) [11].

#### 4.6 Possible Improvements with Software Radio

There are several ways that flexibility in a software radio might provide additional benefits. We discuss each of these possibilities in this section.

Higher Data Rates. A header is always sent at 1 Mbps before the payload, incurring a minimum of 192  $\mu$ s (192 bits / 1 Mbit/s). This mechanism is used to allow different data rates to be supported. Because transmitting at 2 Mbps is considered quite unreliable for frequency hopping spread spectrum systems except in optimal quality conditions, supporting 4-GFSK modulation is consider an optional requirement [21]. As a result, this extra latency provides no major benefit.

A software radio-based implementation, on the other hand, might be able to take advantage of the existing support in the 802.11 standard to vary the modulation and data rate. Unfortunately, the number of modulation schemes that can be supported is quite limited because coherent detection is hard to maintain. The receiver must reacquire phase lock each time after a hop takes place [17], which is difficult because



Figure 4-3: Error Performance Curves for 2-GFSK and 4-GFSK in 802.11.

they occur every 224  $\mu$ s. As a result, modulation schemes such as 16-QAM, which can encode four bits per symbol, cannot be used in these situations.

Another possibility is to provide support for higher data rates by modifying the physical layer to use direct sequencing instead of frequency hopping. Direct sequence spectrum systems can support coherent modulation techniques and provide the ability to achieve much higher data rates such as the 5.5 and 11 Mbps specified in the 802.11b standard. Instead of hopping in different parts of the 75 MHz band, 802.11b direct sequence systems multiply an incoming bitstream by a spreading code before modulation that increases the bandwidth to 11 MHz.

A frequency hopping based software radio can turn into a direct sequencing system simply by modifying its signal processing chain. Instead of having a module that generates a sinusoidal waveform and samples it according to the current hop frequency [15], a module that performs the spreading operation can be used instead. No hardware redesign is required, since these modules are implemented entirely in software.

A general purpose processor currently does not have the capability to provide such high data rates, however. A module that implements the despreading operation was implemented and measured to have a maximum throughput of 1.72 Mbps, which is well short of the high data rates provided in the 802.11b standard. In addition, the demodulator requires correlating an incoming waveform against 64 possibilities, which incurs a tremendous computational cost and causes high latency and energy consumption.

Maximizing Bandwidth Usage. Until recently, the FCC restricted the maximum channel bandwidth of frequency hopping systems to 1 MHz. Current 802.11 implementations still conform to these regulations, even though the maximum bandwidth has now increased to 5 MHz. A software radio, however, could take advantage of such regulatory changes to provide both higher data rates while reducing energy consumption.

A doubling of bandwidth, as shown in Equation 4.3, results in an increase in the maximum data rate for 1 Mbps to 2 Mbps. In optimal conditions, this increase might even allow 4-GFSK modulation to attain 4 Mbps data rates. Because the maximum channel bandwidth is 5 MHz, the maximum data rate would also increase to 10 Mbps.

By increasing the amount of bandwidth used, however, a frequency hopping system becomes more susceptible to multipath interference caused by signal reflections. The multipath effects in a 1 MHz channel is relatively constant and can be mitigated by increasing transmit power. In cases where severe distortion is encountered, the system simply hops to another channel and retransmits. Over a much wider bandwidth such as 3 MHz, the channel effects are significantly different [23]. FSK modulation is also extremely sensitive to these varying effects, so retransmissions and increased transmit power may not be possible to compensate for multipath distortion.

Improving Error Probability. The current 802.11 physical layer only appends a CRC checksum at the end of the header. The payload is also only appended with a checksum, so more than one bit error in the packet will trigger a retransmission. Because the probability of error can change considerably for a mobile node moving between different environments, these retransmissions can occur quite regularly. A 2 dB increase in noise, for instance, shifts the probability of error from  $10^{-4}$  to  $10^{-3}$  for 2-GFSK.

One approach is to attempt to compensate by adding forward error correction to the packet. If the bit error rate decreases by some threshold, a block code might be added. A convolutional code might be used for more powerful error correction or if the bit error rate continues to decline.

The disadvantage is that error correction would reduce the maximum data rate. A rate 1/2 convolutional code, for instance, as shown in Equation 4.3 would reduce the maximum data rate in half. In addition, the amount of energy consumed to perform error correction may actually be higher than simply retransmitting the packet.

Decreasing Energy Consumption. Although the 802.11 standard can support up to eight transmit power levels, usually only one or two levels are actually provided. In many cases, the transmit power is fixed at 100 mW, which means that the maximum range for a node transmitting at 1 Mbps and a probability of error of  $10^{-4}$  is approximately 100 meters (see Appendix 6.1.2). Because transmit power is limited to 1 W by the FCC, the maximum range would be approximately 230 meters.

The ability to adjust power levels would provide the ability to help reduce energy consumption. The amount of power could be adjusted according to the distance from the node or based on node density [16]. Work done by [4] also attempts to identify the optimal tradeoff point between lowering transmit power and forcing retransmissions.

## Chapter 5

## Conclusion

## 5.1 Summary

In this paper, we have discussed various applications for software radio technology in ad-hoc networks. We have introduced a framework that demonstrates how a physical layer can be created based on user requirements, channel conditions, and regulatory limits. Finally, we have applied this framework to the 802.11 standard to help examine how software radios might improve performance.

### 5.2 Future Work

Much of the focus in this thesis has focused on providing the ability to support different modulation and channel codes. Trellis-coded modulation and adaptive equalization techniques might also be incorporated with this framework. In addition, turbo codes, which provide the closest theoretical performance to the Shannon capacity limit, have also not been included in this analysis.

By using this framework, a more sophisticated radio for handheld devices might be designed. A platform might be constructed that provides a user with the ability to adjust manually the modulation and channel coding. This platform can then be used to better understand how the flexibility of software radios influence the performance of various access protocols and routing algorithms in ad-hoc networks.

There are several issues that should be examined when developing this testbed. First, how changes in modulation and coding scheme will be coordinated between the transmitter and receiver need to be considered. The 802.11 standard, for instance, varies the modulation on a packet basis. As a result, a preamble must be sent ahead of the payload, which contributes additional latency and overhead. One alternate approach would be to vary the modulation and coding for every other packet.

Next, more research might be done to devise a way for two different nodes to share a common library of modulation and channel coding schemes. Because there is no centralized management system in ad-hoc networks, nodes have no way of coordinating with other nodes on the type of modulation and coding schemes that can be supported. Therefore, they must either support the same set or devise a protocol in which signal processing code can be exchanged and linked with their own code [2].

Because of the limitations in battery life in handheld devices, the processing requirements may also be too high to implement in any practical system. However, an understanding of these limitations would still be useful to be able to project the feasibility of such a prototype. With rapid improvements in processors and battery life technology, such a prototype might be possible in the next three to five years.

## Chapter 6

## Appendix

### 6.1 Calculating Minimum Transmit Power

The minimum transmit power between two nodes depends on the modulation scheme, the desired probability of error, noise level, data rate, and the distance between the nodes. The first step is to determine the required  $\frac{E_b}{N_0}$  at the receiver for a given probability of error. Once this value is known, the required signal-to-noise ratio,  $\frac{S}{N}$ , can be calculated using Equation 2.4:

$$\frac{E_b}{N_0} = \left(\frac{S}{N}\right) \left(\frac{1}{R}\right)$$

$$\frac{S}{N} = \left(\frac{E_b}{N_0}\right) (R)$$
(6.1)

Next, the received signal power,  $P_{rx}$ , can be calculated by multiplying the amount of noise present in the system by  $\frac{S}{N}$ . The noise level can include the thermal noise and aggregate noise caused by concurrent transmissions too week to cause a collision [7]. Thermal noise is approximated using the following equation:

$$N_0 = kT \tag{6.2}$$

where k is Boltzmann's constant  $(1.38 \cdot 10^{-23} \text{ Joules/Kelvin})$  and T is the temperature (290 K for room temperature).

The required received power,  $P_{rx}$ , therefore can be calculated as follows:

$$P_{rx} = \left(\frac{S}{N}\right)(N_0) \tag{6.3}$$

The amount of transmit power also depends on the propagation model used. In the free space model, there exists a clear line-of-sight between the transmitter and receiver. The received signal power in this situation is defined as follows [7]:

$$P_r(d) = \frac{P_{tx} \cdot G_{tx} \cdot A^2}{(4\pi d)^2 L}$$
(6.4)

where  $P_{tx}$  is the transmitted signal power,  $G_{tx}$  and  $G_{rx}$  are the antenna gains of the transmitter and receiver, L is the system loss, and  $\lambda$  is the wavelength ( $\frac{c}{f}$  where c =  $3 \cdot 10^8$  m/s and f = frequency in Hz). For the purposes of this analysis,  $G_{tx} = G_{rx} = 1$  and L=1. The total amount needed to transmit, therefore, is calculated as follows:

$$P_{tx} = (P_{rx}) \left(\frac{4\pi d}{\lambda}\right)^2 \tag{6.5}$$

In decibels (dB), this expression simplifies to:

$$P_{tx} = P_{rx}(dB) + 20log_{10}(\frac{4\pi d}{\lambda})$$
(6.6)

Fade margins (approximately 30 dB) to combat multipath interference and receiver noise (approximately 8 dB) also may also need to be taken into account. If so, the minimum transmit power would be calculated as follows:

$$P_{tx} = P_{rx}(dB) + 20\log_{10}(\frac{4\pi d}{\lambda}) + P_{fade}(dB) + P_{rcv}(dB)$$
(6.7)

where  $P_{rx}$  can be determined from Equation 6.3.

#### 6.1.1 Transmit power for FSK and (207, 187) Reed Solomon

No fade margins and receiver noise is taken into account in this calculation. The (207, 187) Reed Solomon code is assumed to produce a 3.0 dB coding gain, so it is subtracted from the required  $\frac{E_b}{N_0}$ .

$$\frac{E_b}{N_0} = 12.5dB - 3.0dB = 9.5dB = 8.9$$
  

$$\lambda = \frac{3.0 \cdot 10^8 ms}{2.4GHz} = .125m$$
  

$$d = 500m$$
  

$$R = 115, 200bps$$

$$\frac{S}{N} = \left(\frac{E_b}{N_0}\right)(R)$$
$$\frac{S}{N} = (8.9) (115, 200)$$

= 1,025,280

$$P_{rx} = \left(\frac{S}{N}\right)(N_0)$$
  
= (1,025,280) (2.00 \cdot 10^{-17})  
= 2.05 \cdot 10^{-11}W = -106.89dB

$$P_{tx} = P_{rx}(dB) + 20log_{10}(\frac{4\pi d}{\lambda})$$
  
= -106.89dB + 20log\_{10}(\frac{4\*pi\*500m}{.125})  
= -106.89dB + 94.0dB  
= -12.9dB = 51.4mW

#### 6.1.2 Transmit power for 802.11 2.4 GHz at 200 m

The calculation below is an approximation, assuming that the required  $\frac{E_b}{N_0}$  is equal to 17 dB. A fade margin to compensate for multipath distortion of 30 dB is also added.

$$\frac{E_b}{N_0} = 17dB = 50.00(BER \approx 10^{-4})$$
$$\lambda = \frac{3.0 \cdot 10^8 ms}{2.4GHz} = .125m$$
$$d = 100m$$
$$R = 1,000,000bps$$

$$\frac{S}{N} = \left(\frac{E_b}{N_0}\right)(R)$$
  
$$\frac{S}{N} = (50.00) (1,000,000)$$
  
$$= 50,000,000$$

$$P_{rx} = \left(\frac{S}{N}\right)(N_0)$$
  
= (50,000,000) (1.38 \cdot 10^{-23} J/K \cdot 290K)  
= 2.01 \cdot 10^{-13} W = -127 dB

Noise is also added to the receiver, so we add 8 dB to the previous quantity:

$$P_{rx} = -127.0dB + 8dB$$
$$= -119.0dB$$

$$P_{tx} = P_{rx}(dB) + 20log_{10}(\frac{4\pi d}{\lambda}) + P_{fademargin}$$
  
= -119dB + 20log\_{10}  $\left(\frac{4*pi*100m}{.125}\right) + 30dB$   
= -119dB + 80.0dB + 30dB  
= -8.95dB = 127mW

#### 6.1.3 Error Performance Curves for 802.11

The error performance curves for GFSK modulations was developed based on a model discussed in [22]. The FSK transmitter accepts a binary data stream and maps them to symbols. Modulation occurs by varying the phase according to the modulation index multiplied by the symbol.

Next, to simulate the effects of a channel, white gaussian noise is added to the waveform. The amount of noise to add is determined by the  $\frac{E_b}{N_0}$  ratio and the energy per bit of the waveform. Energy per bit of the waveform can be calculated by squaring the real and imaginary parts separately and adding them together.

The waveform is then demodulated based on calculating the phase differences between the received signals and dividing by the modulation index. Because the received signal also has noise, a decision about the most likely symbol that was transmitted must be made. This decision is based on comparing the distance between each possible symbol and finding the closest one received.

Error performance is determined by comparing these symbol decisions against the actual symbols transmitted. The average error rate is stored based on five iterations for a stream of 40,000 bits. These average rates are determined for  $\frac{E_b}{N_0}$  between 10-30 dB.

```
% Modulation Index = .32 for 2-GFSK
[Two_GFSK_BER] = CalcErrPerformance(.32, Two_GFSK);
% Modulation Index = .144 for 4-GFSK
[Four_GFSK_BER] = CalcErrPerformance(.144, Four_GFSK);
semilogy(LogEbNo, Two_GFSK_BER, 'ro--');
hold
semilogy(LogEbNo, Four_GFSK_BER, 'bx--');
xlabel('Eb/No (dB)');
ylabel('Pb = probability of bit error');
axis([10 26 10<sup>-4</sup> 10<sup>0</sup>])
legend('2-GFSK (h =.32)', 4-GFSK (h\=.144)');
% -----
% CalcErrPerformance
% ModIndex: should be either .32 (2-GFSK) or .144 (4-GFSK)
% SymbolSet: should be 2-level or 4-level PAM
function [AvgBER] = CalcErrPerformance(ModIndex, SymbolSet)
%
   ModIndex=.32;
%
   SymbolSet=[0 1 2 3];
  LogEbNo = 10:30; % Eb/NO from 10, 11, 12, 13, ..., 30 dB
  nIters = 5; % Number of iterations
  for EbNoIndex=1:length(LogEbNo)
   for iters = 1:nIters
    BitStreamLength = 40000;
                                               % Number of samples
  % PAM Symbol Mapper
  % Generate random symbols
    pam = SymbolSet(randint(BitStreamLength,1,length(SymbolSet))+1);
  \% Modulate the signal -- derivative of phase is equal to the frequency
    m = pam;
    Waveform(1) = exp (j*(ModIndex*m(1)));
    for i=2:length(m)
      Waveform(i) = Waveform(i-1) * exp(j*ModIndex*m(i));
    end
  % Additive White Gaussian Noise (AWGN) Filter
```

```
% Generate Gaussian noise vector
 n = rand(1, length(Waveform)) + j*rand(1, length(Waveform));
% Generate noise for this amount of Eb/No
 EbNo = 10^{(LogEbNo(EbNoIndex)/10)};
 Eb1 = sum(real(Waveform) .* real(Waveform))/(BitStreamLength);
 Eb2 = sum(imag(Waveform) .* imag(Waveform))/(BitStreamLength);
 No = (Eb1+Eb2)/EbNo;
 % Scale noise by the amount
 Waveform = Waveform + sqrt(No/2)*n;
  SymbolStream = Waveform;
% Limiter -- normalize received vectors to the unit circle
  for i = 1:length(SymbolStream)
   x = real(SymbolStream(i));
   y = imag(SymbolStream(i));
   LimiterOutput(i) = (x + j*y) / (sqrt(x^2+y^2));
  end
% Discriminator -- determine frequency based on the instantaneous phase
  Normalized_Vectors = LimiterOutput;
  DemodulatedBits (1) = angle(Normalized_Vectors(1)) / ModIndex;
  for i=2:length(Normalized_Vectors)
    y = Normalized_Vectors(i) * conj(Normalized_Vectors(i-1));
    theta = angle(y);
   DemodulatedBits(i) = theta / ModIndex;
  end
% Bit decision maker -- which symbol?
  % generate columns for comparison
    symbol_block=repmat(transpose(SymbolSet),1,length(DemodulatedBits));
    demod_block=repmat(DemodulatedBits,length(SymbolSet),1);
  % Use minimum distance to decide the best symbol
    [y,d] = min((symbol_block - demod_block) .^ 2);
    bits = SymbolSet(d);
    Errors= sum(bits ~= pam);
    BER(iters) = Errors / BitStreamLength;
   end
  AvgBER(EbNoIndex) = sum(BER)/nIters;
end
```

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