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## Pauli paramagnetism of an ideal Fermi gas

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We show how to use trapped ultracold atoms to measure the magnetic susceptibility of a two-component Fermi gas. The method is illustrated for a noninteracting gas of <sup>6</sup>Li, using the tunability of interactions around a wide Feshbach resonance. The susceptibility versus effective magnetic field is directly obtained from the inhomogeneous density profile of the trapped atomic cloud. The wings of the cloud realize the high-field limit where the polarization approaches 100%, which is not accessible for an electron gas.

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### I. INTRODUCTION

Ultracold atoms can be prepared with almost complete control over their density, temperature, and interactions. They serve as model systems for exploring unsolved problems in many-body physics as well as for demonstrating well-known textbook physics, such as ideal, noninteracting gases that do not exist in nature. For example, several phenomena related to Pauli blocking of fermions were clearly demonstrated only after the advent of ultracold Fermi gases [1]. Here we use the tunability of atomic interactions near Feshbach resonances to create a noninteracting Fermi gas with two components. This is a realization of an ideal, noninteracting free-electron gas (FEG) with spin-up and spin-down components, as assumed in the simple theory of metals. We demonstrate how such an ideal Fermi gas will respond to effective magnetic fields, which is described by Pauli paramagnetism.

The paper is mainly pedagogical. It explains how paramagnetism is observed in trapped atomic samples which have an inhomogeneous density due to the harmonic confinement potential. Furthermore, these atomic samples realize a canonical ensemble in the fixed atom numbers  $N_\uparrow$  and  $N_\downarrow$  of the two components, whereas in metals and solid-state physics,  $N_\uparrow - N_\downarrow$  is the magnetization determined by the applied external magnetic field. In all previous studies of paramagnetism, the magnetization was weak since the applied magnetic field times the magnetic moment was much smaller than the Fermi energy [2–5]. With ultracold atoms, we can easily realize the strong-field case where the chemical-potential difference is larger than the Fermi energy and therefore fully polarizes the gas. Besides its pedagogical purpose, this paper experimentally demonstrates Pauli paramagnetism in a truly noninteracting system exactly described by basic theory, whereas measurements even in simple metals revealed major discrepancies due to interaction effects [2–5].

### II. CONCEPT

Pauli paramagnetism explains the magnetization of a free-electron gas with two spin states, neglecting the contribution

from orbital motion. In a FEG, the applied field shifts the energies of the two spin states in opposite directions, as in Fig. 1(a). For a uniform FEG at temperature  $T = 0$ , the total number  $N_{\uparrow(\downarrow)}$  of electrons in each spin state inside a volume  $V$  is given by

$$N_{\uparrow(\downarrow)} = \int_{\mp\mu_B B}^{E_F} g(E \pm \mu_B B) dE, \quad (1)$$

where  $g(E) = \frac{V}{4\pi^2} \left(\frac{2m}{\hbar^2}\right)^{3/2} E^{1/2}$  is the density of states,  $E_F$  is the Fermi energy,  $m$  is the mass of an electron,  $\mu_B$  is the Bohr magneton, and  $\hbar$  is Planck's constant. The magnetic susceptibility  $\chi$  is defined as  $\mu_B \partial \Delta n / \partial B$ , where  $\Delta n \equiv n_\uparrow - n_\downarrow = (N_\uparrow - N_\downarrow) / V$ . As a dimensionless quantity, we consider the normalized susceptibility

$$\bar{\chi} = \frac{\partial (\Delta n / n)}{\mu_B \partial (B / E_F [n / 2])}, \quad (2)$$

where the polarization  $\Delta n / n$  is used as a more meaningful measure of magnetization.  $E_F [n] = \hbar^2 (6\pi^2 n)^{2/3} / 2m$ , and the total density is  $n \equiv n_\uparrow + n_\downarrow = (N_\uparrow + N_\downarrow) / V$ .

Here we experimentally simulate Pauli paramagnetism using trapped fermionic alkali atoms. The two lowest hyperfine states of <sup>6</sup>Li,  $|F = 1/2, m_F = 1/2\rangle \equiv |\uparrow\rangle$  and  $|F = 1/2, m_F = -1/2\rangle \equiv |\downarrow\rangle$ , represent the two spin states of an electron. This atomic system is different from free-electron systems: (1) Due to the slow dipolar relaxation [1], the population in each spin state is conserved and, therefore, (2) an external magnetic field does not lead to any magnetization; it only shifts the energies of the two spin states (only in the case of strongly magnetic dipolar gases such as Cr the dipolar relaxation is fast, and therefore the spin populations follow an external magnetic field [6]).

To realize the effective magnetic field, we introduce density imbalance while preparing the system [7,8], as illustrated in Fig. 1(b). In the grand-canonical description of a system with fixed atom number, a Lagrange multiplier (called the chemical potential) ensures the correct expectation value for the atom number. In our case, the atom numbers in both spin states are fixed. In a grand-canonical description, this leads to two Lagrange multipliers,  $\widehat{\mu}_\uparrow$  and  $\widehat{\mu}_\downarrow$  (the two chemical potentials for the two spin states), or to one Lagrange multiplier for the total number and the other  $\widehat{\Delta\mu} = \widehat{\mu}_\uparrow - \widehat{\mu}_\downarrow$  for the population difference. Under the external magnetic field  $B$ ,  $\widehat{\Delta\mu}(B)$  is a

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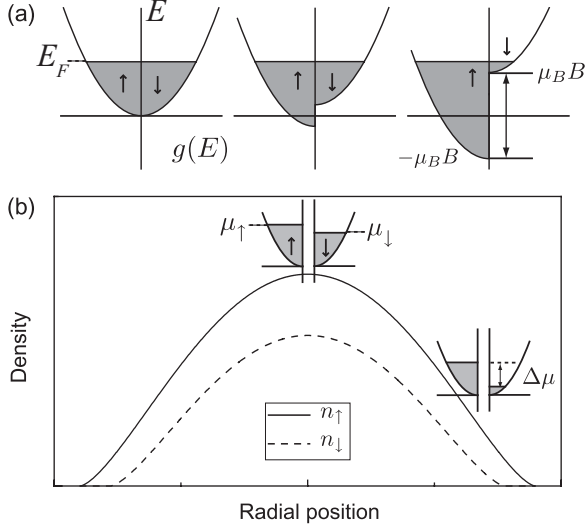


FIG. 1. Comparison between a FEG and a trapped two-component Fermi gas at temperature  $T = 0$ . (a) Response of the FEG to an external magnetic field  $B$ . Electrons in the two spin states are filled up to the Fermi energy  $E_F$ . An external magnetic field  $B$  shifts the energy of the two states in opposite directions and produces the density difference, or magnetization. (b) Density distributions  $n_\uparrow$  and  $n_\downarrow$  of a two-component trapped Fermi gas at  $T = 0$ . As discussed in the text, the local density polarization and corresponding normalized effective magnetic field varies across the atomic cloud. This is illustrated in the diagrams next to the curve for  $n_\uparrow$ , where the gaps between the two spin states represent the absence of spin-flip processes in the system mentioned in the text.

function of  $B$  in the form of  $\widehat{\Delta\mu}(B) = \Delta\mu + \mu_B B(g_\uparrow - g_\downarrow)$ , where  $\Delta\mu = \widehat{\Delta\mu}(B = 0)$  and  $\mu_B g_{\uparrow(\downarrow)} B$  is the field-dependent energy of each state. The resultant population imbalance in thermal equilibrium is the response to the sum of this multiplier and the contribution from the external magnetic field,  $-\mu_B B(g_\uparrow - g_\downarrow)$ , which is obviously canceled out by the second additive component in this multiplier. Therefore, the *effective* magnetic field determining the population imbalance does not depend on the external magnetic field. For example, a balanced gas ( $\Delta\mu = 0$ ) always has zero effective magnetic field, independent of the applied field.

For a uniform Fermi gas at  $T = 0$ , the number in each spin state determines chemical potential  $\mu_{\uparrow(\downarrow)}$  [9] and satisfies

$$N_{\uparrow(\downarrow)} = \int_0^{\mu_{\uparrow(\downarrow)}} g(E) dE = \int_{\mp\Delta\mu/2}^{\tilde{\mu}} g(E \pm \Delta\mu/2) dE, \quad (3)$$

where  $\tilde{\mu} = (\mu_\uparrow + \mu_\downarrow)/2$  and  $\Delta\mu = \mu_\uparrow - \mu_\downarrow$ .  $g(E)$  is the same as in Eq. (1) if  $m$  is taken to be the mass of a  ${}^6\text{Li}$  atom. A comparison with Eq. (1) shows that the chemical-potential difference  $\Delta\mu$  is the effective magnetic field that takes the place of the magnetic field in a FEG. With this effective magnetic field, the magnetic susceptibility can be written as

$$\chi = \frac{\partial \Delta n}{\partial \Delta\mu}. \quad (4)$$

We show now how a single atomic density profile in a harmonic trap  $V(\vec{r})$  can be used to determine the normalized susceptibility as a function of magnetic field. In the local-

density approximation, the density at each point in the trap is that of the corresponding uniform gas with modified chemical potentials  $\mu_{\uparrow(\downarrow)}(\vec{r}) = \mu_{\uparrow(\downarrow)}^s - V(\vec{r})$  [1,10], where  $\mu_{\uparrow(\downarrow)}^s$  is global chemical potential defined for the whole trapped cloud, which constrains the total number of atoms in each spin state. This concept has been used to determine the equation of state of interacting Fermi gases [8,11–13]. Here we are interested in

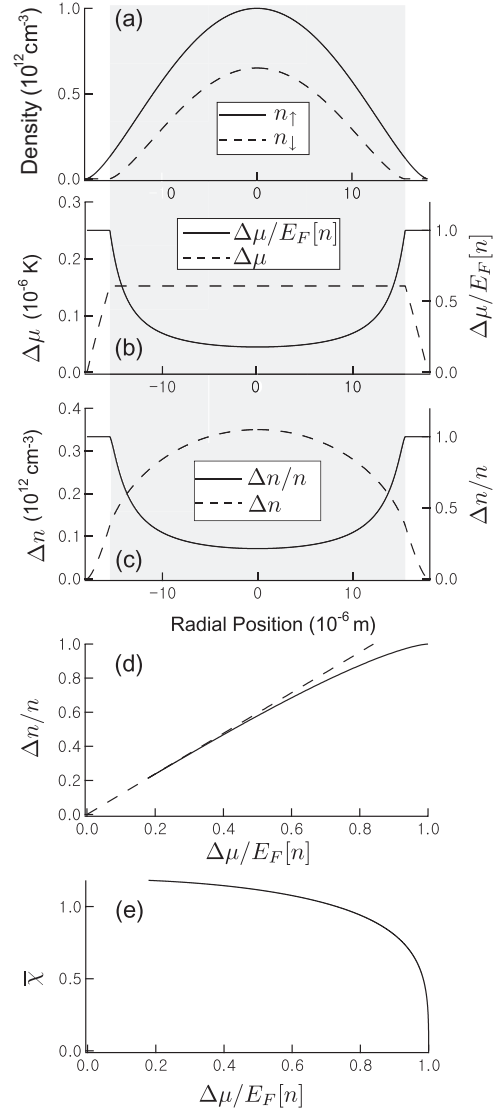


FIG. 2. Determination of the susceptibility  $\bar{\chi}$  from atomic density profiles. (a) Simulated density profiles of a two-component Fermi gas in a spherically symmetric harmonic trap at zero temperature. The total population imbalance  $\delta \equiv (N_\uparrow - N_\downarrow)/(N_\uparrow + N_\downarrow) = 21\%$ . The shaded area corresponds to the partially polarized region where  $\bar{\chi}$  is well defined. (b) The local chemical-potential difference  $\Delta\mu$  with (solid line) and without (dashed line) normalization by the Fermi energy  $E_F[n]$ . For the fully polarized gas,  $\overline{\Delta\mu} = \Delta\mu/E_F[n] = 1$  according to the definition in the text. (c) The density difference  $\Delta n$  with (solid line) and without (dashed line) normalization by the total density  $n$ . (d) Normalized density difference  $\overline{\Delta n}$  vs normalized chemical-potential difference  $\overline{\Delta\mu}$ . For the fully polarized gas,  $\overline{\Delta n} = \overline{\Delta\mu} = 1$ . A linear fit at low  $\overline{\Delta\mu}$  (dashed line) gives  $\bar{\chi} = 3/2^{4/3} \approx 1.19$ . (e) Normalized magnetic susceptibility  $\bar{\chi}$  vs the normalized chemical-potential difference  $\overline{\Delta\mu}$ .

the normalized magnetic susceptibility which is the slope of the normalized density difference versus the normalized chemical difference [14]. We demonstrate this procedure first using simulated density profiles (Fig. 2).

As  $\mu_{\uparrow(\downarrow)}(\vec{r})$  varies across the cloud, the chemical-potential difference  $\Delta\mu(\vec{r}) \equiv \mu_{\uparrow}(\vec{r}) - \mu_{\downarrow}(\vec{r}) = \mu_{\uparrow}^g - \mu_{\downarrow}^g$  remains constant, as shown in Fig. 2(b). However, the total density  $n(\vec{r}) = n_{\uparrow}(\vec{r}) + n_{\downarrow}(\vec{r})$  changes across the cloud and, consequently, the local Fermi energy  $E_F[n(\vec{r})]$  as well, with  $E_F[n]$  being the same as in Eq. (1) if  $m$  is taken to be the mass of  ${}^6\text{Li}$ . The normalized magnetic susceptibility  $\bar{\chi}$  depends on the dimensionless effective magnetic field  $\overline{\Delta\mu} = \Delta\mu(\vec{r})/E_F[n(\vec{r})]$ , which does vary across the cloud, from small values near the center to the saturated value of one at the edges. From Fig. 2(d), a single set of atomic density profiles contains a range of polarizations  $\overline{\Delta n} = \Delta n/n$  and normalized effective magnetic fields  $\overline{\Delta\mu}/E_F[n]$ . The slope of the  $\overline{\Delta n}$  vs  $\overline{\Delta\mu}$  yields the normalized susceptibility

$$\bar{\chi} = \partial(\overline{\Delta n})/\partial(\overline{\Delta\mu}). \quad (5)$$

The normalization of  $\bar{\chi}$  in Eq. (5) is chosen to ensure  $\overline{\Delta n} = \overline{\Delta\mu} = 1$  for a fully polarized gas. The slope near the origin, corresponding to small values of  $\overline{\Delta\mu}$ , gives  $\bar{\chi}(T=0) \equiv \bar{\chi}_0 = 3/2^{4/3} \approx 1.19$  [15]. As shown in Fig. 2(e), the susceptibility decreases with increasing  $\overline{\Delta\mu}$  and drops to zero when the Fermi gas reaches full polarization.

### III. EXPERIMENT AND RESULTS

An ultracold one-component Fermi gas of  ${}^6\text{Li}$  in the state  $|F=3/2, m_F=3/2\rangle$  is prepared by sympathetic cooling with bosonic  ${}^{23}\text{Na}$  atoms [16,17].  ${}^6\text{Li}$  atoms are then loaded into an optical dipole trap followed by radio-frequency (rf) transfer to  $|F=1/2, m_F=1/2\rangle$  using an rf Landau-Zener sweep at 300 G. A superposition of the two lowest hyperfine ground states,  $|F=1/2, m_F=1/2\rangle \equiv |\uparrow\rangle$  and  $|F=1/2, m_F=-1/2\rangle \equiv |\downarrow\rangle$ , is prepared by a rf sweep at 300 G, and holding here for 500 ms results in an incoherent mixture.

Further cooling is provided by lowering the optical trapping potential, which leads to radial evaporation (axial confinement is provided magnetically). We increase the magnetic field in 200 ms to 528 G, where the scattering length is zero [18], leading to a noninteracting two-component Fermi gas. The oscillation frequencies of the final trapping potential are  $\omega_y =$

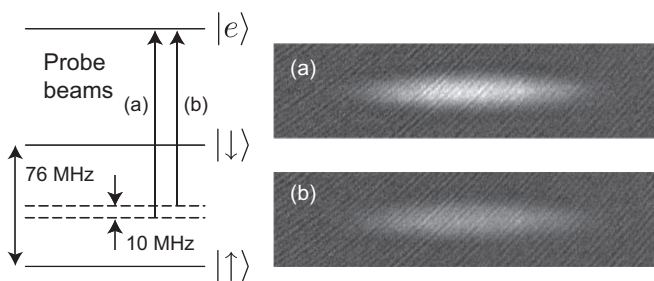


FIG. 3. Double-shot phase contrast imaging.  $|e\rangle$  is the  $2P_{3/2}$  excited state in  ${}^6\text{Li}$ . Two successive images are taken at two different imaging frequencies, (a) and (b). Corresponding CCD images are shown on the right.

$2\pi \times 35$  Hz axially and  $\omega_x = \omega_z = 2\pi \times 390$  Hz radially. The total population imbalance  $\delta \equiv (N_{\uparrow} - N_{\downarrow})/(N_{\uparrow} + N_{\downarrow})$  is about 33%. The final temperature is about  $0.22T/T_F$ , where

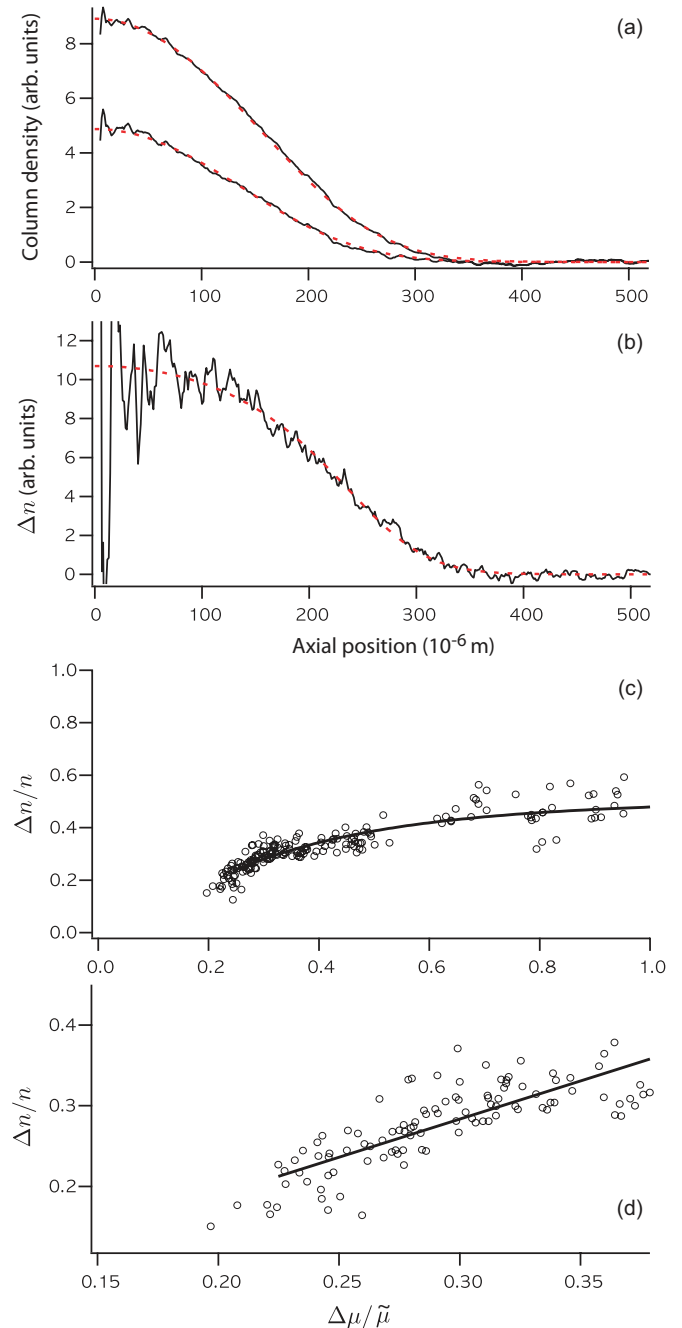


FIG. 4. (Color online) Experimental determination of  $\bar{\chi}$ . Representative profiles of (a) 2D column densities for  $|\uparrow\rangle$  (upper solid curve) and  $|\downarrow\rangle$  (lower solid curve). The temperature and chemical potential are obtained from the fit (dotted curves) as discussed in the text. Each elliptical average is plotted vs the axial position (long axis of the ellipse). (b) 3D density difference obtained from a single double-shot image. The dotted curve is a theoretical curve based on the chemical potentials and the temperature obtained from the 2D fit in (a). (c) The normalized 3D density difference is plotted as a function of the normalized chemical-potential difference. The solid line is the theoretical prediction. (d) The linear fit at low  $\overline{\Delta\mu}$  gives the low-field susceptibility  $\bar{\chi} = 0.95(1)$ .

$k_B T_F = E_F[n/2]$  with  $n$  being the total peak density and  $k_B$  being the Boltzmann constant.

To obtain the density profile of each spin state of  ${}^6\text{Li}$ , we use a double-shot phase contrast imaging technique that involves two images taken at two different imaging frequencies [8,17] (see Fig. 3). One frequency is tuned to the average of the two resonant transition frequencies for  $|\uparrow\rangle$  and  $|\downarrow\rangle$  states to the  $2P_{3/2}$  electronically excited state. The resulting phase contrast picture is a measure of the density difference  $\Delta n = n_\uparrow - n_\downarrow$ . To measure the density of each component, a second image is taken of the same cloud at a frequency detuned towards the  $|\uparrow\rangle$  transition by 10 MHz. The two images can be taken in quick succession because of the nondestructive nature of phase contrast imaging.

For dispersive imaging techniques such as phase contrast imaging, it is crucial to carefully focus the imaging system, since the atomic cloud refracts the probe light (in contrast to resonant absorption imaging). One can check this by comparing in-trap profiles of  $|\uparrow\rangle$  atoms imaged at positive and negative detunings of 60 MHz and find the focal position which minimizes the difference [17].

Figure 4 shows the experimental results. The camera images provide two-dimensional (2D) column densities  $n_{2D}$ , which integrate the density distribution along the line of sight. To reduce the noise for the following analysis, we take advantage of the symmetry of the trap and perform quadrant averaging and elliptical averaging: First, the four quadrants around the center of the images are averaged. Second, the data is averaged along elliptical contours. The aspect ratio of the ellipses is determined from in-trap images [8]. The temperature and global chemical-potential for each component are obtained by fitting 2D densities with theoretical noninteracting density profiles. Since the temperature  $T$  is small but non-negligible, data are fitted with finite-temperature Fermi gas 2D distribution in a harmonic trap given by

$$n_{2D}(x, y) = -\frac{m(k_B T)^2}{2\pi\hbar^3\omega_z} \text{Li}_2[-e^{[\mu^s - m(\omega_x^2 x^2 + \omega_y^2 y^2)/2]/k_B T}], \quad (6)$$

where  $\text{Li}_n(z)$  is the  $n$ th-order polylogarithm.  $z$  is the axis along the line of sight. Since the majority component has a better signal-to-noise ratio, we determine the temperature and chemical potential first for this component, and keep the temperature as a fixed parameter in the fit of the minority profile. Three-dimensional (3D) densities [Fig. 4(b)] are obtained by performing the inverse Abel transformation of the column densities [8]. The linear fit of  $\overline{\Delta n}$  as a function of  $\overline{\Delta\mu}$  at small  $\overline{\Delta\mu}$  gives the low-field susceptibility at finite temperature [Fig. 4(d)]. For finite but low temperatures, the

low-field susceptibility is known to vary as [19]

$$\overline{\chi} = \overline{\chi}_0 \left[ 1 - \frac{\pi^2}{12} \left( \frac{T}{T_F} \right)^2 \right]. \quad (7)$$

$T/T_F$  changes from 0.24 to 0.35 within the fitting region in Fig. 4(d), affecting the susceptibility by about 3%. For  $T/T_F = 0.29$ , this theoretical calculation gives  $\overline{\chi} = 1.108$  and the experimentally obtained value is 0.95(1) in Fig. 4(d). The discrepancy between the experimental and theoretical value is most likely due to a residual dispersion effect leading to systematic uncertainty estimated to be 10–20% [20,21]. We did not attempt to quantify this effect since this paper is mainly pedagogical and a dispersion effect depending on the imbalance as well as two detunings would be time consuming to quantify.

Figure 4(c) illustrates that we can easily approach the high-field limit of a fully polarized gas  $\overline{\Delta\mu} \approx 1$ . Note that  $\overline{\Delta n}$  is smaller than 1 because at finite temperature the minority component extends beyond its Thomas-Fermi radius. In a metallic free-electron gas, with a typical Fermi temperature of 10 000 K, the high-field region would require magnetic fields of 10 000 Tesla, which is 200 times stronger than the strongest continuous laboratory magnetic fields.

#### IV. CONCLUSIONS

We have demonstrated how the *ideal-gas* magnetic susceptibility can be measured in ultracold Fermi gases. After considering finite-temperature effects, the experimental results are in quantitative agreement with the prediction from Pauli paramagnetism. Since the local spin polarization varies across the trapped atomic cloud, a single density profile gives the susceptibility for both low and high effective magnetic fields. This method can be applied to the study of magnetic properties of strongly interacting Fermi gases, which are of current interest [22–25]. Such measurements could address the possible existence of a ferromagnetic transition in a repulsive Fermi gas [16] for which the spin susceptibility would diverge at the phase transition [26].

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[1] W. Ketterle and M. W. Zwierlein, *Ultracold Fermi Gases, Proceedings of the International School of Physics Enrico Fermi, Course CLXIV* (IOS, Amsterdam, 2008).  
 [2] R. T. Schumacher and C. P. Slichter, *Phys. Rev.* **101**, 58 (1956).  
 [3] R. T. Schumacher and W. E. Vehse, *J. Phys. Chem. Solids* **24**, 297 (1963).  
 [4] S. Schultz and G. Dunifer, *Phys. Rev. Lett.* **18**, 283 (1967).

[5] J. A. Kaeck, *Phys. Rev.* **175**, 897 (1968).  
 [6] M. Fattori, T. Koch, S. Goetz, A. Griesmaier, S. Hensler, J. Stuhler, and T. Pfau, *Nature Phys.* **2**, 765 (2006).  
 [7] Y. Shin, M. W. Zwierlein, C. H. Schunck, A. Schirotzek, and W. Ketterle, *Phys. Rev. Lett.* **97**, 030401 (2006).  
 [8] Y.-i. Shin, C. H. Schunck, A. Schirotzek, and W. Ketterle, *Nature (London)* **451**, 689 (2008).

- [9] From now on, the chemical potential for each component does not retain the additive term canceled by the contribution from the external magnetic field.
- [10] S. Giorgini, L. P. Pitaevskii, and S. Stringari, *Rev. Mod. Phys.* **80**, 1215 (2008).
- [11] M. J. H. Ku, A. T. Sommer, L. W. Cheuk, and M. W. Zwierlein, *Science* **335**, 563 (2012).
- [12] M. Horikoshi, S. Nakajima, M. Ueda, and T. Mukaiyama, *Science* **327**, 442 (2010).
- [13] N. Navon, S. Nascimbene, F. Chevy, and C. Salomon, *Science* **328**, 729 (2010).
- [14] Reference [23] determined the susceptibility for a Fermi gas near unitarity from the equation of state.
- [15] Reference [23] used a different normalization, where the normalized susceptibility is  $3/2$  at low field.
- [16] G.-B. Jo, Y.-R. Lee, J.-H. Choi, C. A. Christensen, T. H. Kim, J. H. Thywissen, D. E. Pritchard, and W. Ketterle, *Science* **325**, 1521 (2009).
- [17] Y.-R. Lee, M.-S. Heo, J.-H. Choi, T. T. Wang, C. A. Christensen, T. M. Rvachov, and W. Ketterle, *Phys. Rev. A* **85**, 063615 (2012).
- [18] K. M. O'Hara, S. L. Hemmer, S. R. Granade, M. E. Gehm, J. E. Thomas, V. Venturi, E. Tiesinga, and C. J. Williams, *Phys. Rev. A* **66**, 041401 (2002).
- [19] R. Pathria and P. Beale, *Statistical Mechanics*, 2nd ed. (Butterworth-Heinemann, Bodmin, 1996).
- [20] In Ref. [17], even for optimized focusing, we found a small difference in the cloud profiles for different detunings since the cloud is an extended object. This dispersion effect affects the compressibility by about 10%. This systematic error could be almost completely eliminated by averaging the measured compressibility for positive and negative detuning.
- [21] For the susceptibility measurement, the two spin components give opposite dispersive effects that partially cancel each other out. However, since we take data at smaller detuning than in Ref. [17], we expect similar dispersion distortions of the cloud shape.
- [22] J. Meineke, J.-P. Brantut, D. Stadler, T. Muller, H. Moritz, and T. Esslinger, *Nature Phys.* **8**, 455 (2012).
- [23] S. Nascimbene, N. Navon, S. Pilati, F. Chevy, S. Giorgini, A. Georges, and C. Salomon, *Phys. Rev. Lett.* **106**, 215303 (2011).
- [24] A. Sommer, M. Ku, G. Roati, and M. W. Zwierlein, *Nature (London)* **472**, 201 (2011).
- [25] C. Sanner, E. J. Su, W. Huang, A. Keshet, J. Gillen, and W. Ketterle, *Phys. Rev. Lett.* **108**, 240404 (2012).
- [26] A. Recati and S. Stringari, *Phys. Rev. Lett.* **106**, 080402 (2011).