

18.440 PROBLEM SET SIX

A. FROM TEXTBOOK CHAPTER FIVE:

1. Problems: 14, 17, 33
2. Theoretical Exercises: 9, 12, 15, 19, 29, 30

B. At time zero, a single bacterium in a dish divides into two bacteria. This species of bacteria has the following property: after a bacterium B divides into two new bacteria B_1 and B_2 , the subsequent length of time until each B_i divides is an exponential random variable of rate $\lambda = 1$, independently of everything else happening in the dish.

1. Compute the expectation of the time T_n at which the number of bacteria reaches n .
2. Compute the variance of T_n .
3. Are both of the answers above unbounded, as functions of n ? Give a rough numerical estimate of the values when $n = 10^{50}$.

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18.440 Probability and Random Variables
Spring 2011

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