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On the Accuracy of Interference Models in Wireless Communications

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Abstract—We develop a new framework for measuring and comparing the accuracy of any wireless interference models used in the analysis and design of wireless networks. Our approach is based on a new index that assesses the ability of the interference model to correctly predict harmful interference events, i.e., link outages. We use this new index to quantify the accuracy of various interference models used in the literature, under various scenarios such as Rayleigh fading wireless channels, directional antennas, and blockage (impenetrable obstacles) in the network. Our analysis reveals that in highly directional antenna settings with obstructions, even simple interference models (e.g., the classical protocol model) are accurate, while with omnidirectional antennas, more sophisticated and complex interference models (e.g., the classical physical model) are necessary. Our new approach makes it possible to adopt the appropriate interference model of adequate accuracy and simplicity in different settings.

Index Terms—Interference model, performance evaluation, protocol design, millimeter wave communications.

I. INTRODUCTION

Due to the shared nature of a wireless media, interference plays a critical role in the performance of wireless networks, where the intended signal is combined with other undesired signals transmitted on the same (time, frequency, spatial) channel. The receiver typically decodes the received signal by treating the interference as noise, though advanced receivers may be able to cancel some parts of the interference. Due to the randomness of the channel attenuation and the interferers, successful decoding at the receiver is a random event whose probability depends on the desired signal strength, the ambient noise level accumulated over the operating bandwidth, and the interfering signals strength. Signal-to-interference-plus-noise ratio (SINR) is a common metric to evaluate outage probability (or probability of successful decoding) of a transmission. However, evaluating the outage probability using the SINR model is complex as it depends on the transmission powers, unknown random channel attenuation, medium access control (MAC) protocol used, and the network topology, which is often unknown. Thus, although the SINR interference model is very accurate, using it for the design and analysis of wireless networks is challenging and often results in little insight.

There have been many attempts in the literature to design interference models that accurately capture the effect of interference, yet are tractable for the mathematical analysis. Among the most prominent models, introduced in the literature, are the protocol model of interference [1], the interference ball model [2], and the physical model [1].

The protocol model (PRM) is the simplest model, formalized by the seminal work of Gupta and Kumar [1]. Under the PRM, an outage event occurs if the closest interferer is no farther than a certain distance from the receiver, called the interference range. The interference range depends on the received power from the intended transmitter and a minimum SINR threshold that allows successful signal decoding. Although the PRM is simple, especially for the protocol design and for the MAC layer performance analysis, it fails to capture the effect of interference aggregation (i.e., the sum of the interference power from multiple interferers). Thus, the PRM is generally considered to be overly simplistic. Nonetheless, due to its mathematical tractability, the PRM has been extensively adopted for the analysis of MAC protocols and network performance; e.g., transport capacity [1], delay [3], and collision probability [4].

The interference ball model (IBM) attempts to alleviate the aforementioned limitation of the PRM by considering the aggregated impacts of near-field interferers, located no farther than a certain distance from the receiver. This model has been extensively adopted in performance evaluation and protocol design for wireless networks [2], [5], [6]. The IBM is more accurate than the PRM, but also more complex.

The most accurate and complex interference model is the physical model (PhyM) formalized in [1], which considers the aggregated interference of all transmitters in the entire network. This interference model, also known as the SINR model, is adopted mostly at the physical layer for power control, capacity evaluation, and coverage analysis [1], [7].

Clearly there is a tradeoff between accuracy and complexity of interference models. The proper choice of interference model depends on many parameters such as the receiver design, antenna directionality, network topology, and the choice of medium access protocol. To the best of our knowledge, there has been no systematic method for assessing the accuracy of various interference models, and for choosing the proper interference model for a given network scenario. Most prior works have evaluated the accuracy of different interference models qualitatively, without fully understanding the mutual

1Although PhyM may be mathematically more tractable than both PRM and IBM [7] under very special network settings (e.g., homogenous Poisson field of interferers exhibiting Rayleigh fading channel), PRM and IBM are more favorable interference models for protocol design and for network optimization [4].
impact of different parameters of the physical, medium access, and network layers. This qualitative analysis, however, is often overly simplistic, and may result in the use of interference models that are only marginally more accurate, yet significantly more complex than needed. As we will show throughout this paper, in certain settings, even the simplest interference models are sufficiently accurate and can be used to provide significant insights on the network performance and design.

In this paper, we propose a systematic approach to rigorously quantify the accuracy of interference models in predicting the outage probability. We introduce an accuracy index that takes on real values between 0 and 1, where higher values correspond to higher accuracy. We evaluate this index for PRM and IBM under two example scenarios: (1) Rayleigh fading channel and omnidirectional communications; and (2) deterministic wireless channel, directional communications, and existence of impenetrable obstacles in the environment. The first scenario corresponds to conventional wireless networks \cite{7}, whereas the second scenario corresponds to emerging wireless technologies such as millimeter wave (mmWave) networks with highly directional antennas \cite{8,9}. Although the applications of the proposed index is general and goes much beyond the examples provided in this paper, we use these examples to investigate fundamental properties of this index and also the impact of various network parameters on the accuracy of IBM and PRM. In the first scenario, we derive a tractable closed-form expression for the accuracy index. We show that the accuracy of IBM monotonically increases with the interference range, at the expense of increased complexity. In contrast, we show that there is no such monotonic improvement in the accuracy of PRM. In the second scenario we show that both the PRM and IBM are significantly more accurate with directional antennas and channel blockage. Thus, the PRM can be used in the analysis of mmWave networks. This observation is very promising because the use of the PRM in mmWave networks can significantly improve mathematical tractability, with negligible loss in accuracy of the performance analysis.

The rest of this paper is organized as follows. In Section II we present general assumptions, followed by the introduction of the new interference model accuracy index. We demonstrate the use of this index in Sections III and V. Numerical results are presented in Section V and concluding remarks are provided in Section VI.

II. INTERFERENCE MODEL ACCURACY INDEX

We define a link as a transmitter and its intended receiver, where transmitter (receiver) \( i \) refers to the transmitter (receiver) of link \( i \). Denote by \( \mathcal{I}_i \) the set of interferers of receiver \( i \) (all transmitters excluding the intended transmitter \( i \)), by \( p_i \) the transmission power of transmitter \( i \), by \( \sigma \) the power of white Gaussian noise, by \( d_{ij} \), the distance between transmitter \( i \) and receiver \( j \), and by \( g_{ij}^c \) the channel gain between transmitter \( i \) and receiver \( j \). The channel gain may include average attenuation at a reference distance, distance-dependent component, and fading components. We denote by \( g_{ij}^t \) the antenna gain at transmitter \( i \) toward receiver \( j \), and by \( g_{ij}^r \) the antenna gain at receiver \( j \) toward transmitter \( i \). Thus, the power received by receiver \( j \) from transmitter \( i \) is \( p_i g_{ij}^t g_{ij}^c g_{ij}^r \), and the SINR at receiver \( i \) is given by

\[
\text{SINR}_i = \frac{\sum_{k \in \mathcal{I}_i} p_k g_{ik}^t g_{ik}^c g_{ik}^r}{\sum_{k \in \mathcal{I}_i} p_k g_{ik}^t g_{ik}^c g_{ik}^r + \sigma}.
\]

Note that the SINR depends on the transmission powers, antenna patterns, and network topology. Let \( \beta > 0 \) denote the SINR threshold corresponding to a certain target bit error rate. An outage on link \( i \) occurs when \( \text{SINR}_i \) is lower then \( \beta > 0 \). Different interference models attempt to approximate the probability of outage by ignoring certain components of the interference. In particular, an outage occurs under

- PRM: if there is an interferer no farther than an interference range \( r_{\text{PRM}} = (1 + \Delta)d_{ij} \) of receiver \( i \), where \( \Delta \) is a constant real positive value;
- IBM: if its SINR due to all interferers located no farther than an interference range \( r_{\text{IBM}} \) is less than \( \beta \); and
- PhyM: if its SINR due to all interferers is less than \( \beta \).

In order to present a unified view, we associate two random variables \( a_{ij}^{\text{PRM}} \) and \( a_{ij}^{\text{IBM}} \) to the link between each transmitter \( i \) and receiver \( j \neq i \), where \( a_{ij}^{\text{PRM}} \) is set to 1 if \( d_{ij} \leq r_{\text{PRM}} \), and otherwise 0. Similarly, \( a_{ij}^{\text{IBM}} \) is set to \( +\infty \) if \( d_{ij} \leq (1 + \Delta)d_{ij} \), and otherwise 0. We can define a virtual channel gain as follows:

\[
\begin{align*}
&g_{ij}^{\text{PRM}} = a_{ij}^{\text{PRM}} g_{ij}^c, \\
&g_{ij}^{\text{IBM}} = a_{ij}^{\text{IBM}} g_{ij}^c, \\
&g_{ij}^{\text{PhyM}} = g_{ij}^c, 
\end{align*}
\]

Now, the SINR at receiver \( i \) under interference model \( x \) is given by

\[
\gamma_i^x = \frac{\sum_{k \in \mathcal{I}_i} p_k g_{ik}^t g_{ik}^c g_{ik}^r}{\sum_{k \in \mathcal{I}_i} p_k g_{ik}^t g_{ik}^c g_{ik}^r + \sigma},
\]

where \( x \) is a label denoting PhyM, IBM, or PRM. Finally, there is an outage at receiver \( i \) under model \( x \) if \( \gamma_i^x < \beta \).

Consider the physical model as the reference interference model. We define a binary hypothesis test, where hypotheses \( H_0 \) and \( H_1 \) denote the absence and presence of outage under the reference physical model PhyM. That is, for each receiver \( i \), we have

\[
\begin{cases}
H_0, & \text{if } \gamma_i^{\text{PhyM}} \geq \beta \\
H_1, & \text{if } \gamma_i^{\text{PhyM}} < \beta.
\end{cases}
\]

We can consider a given interference model \( x \) as a detector of the outage events at any given SINR threshold and network parameters. To evaluate the performance of this detector compared to the reference model PhyM, we can use the notions of false alarm and miss-detection. A false alarm corresponds to the event that \( x \) predicts outage under hypothesis \( H_0 \) (i.e., no harmful interference is present); whereas a miss-detection
corresponds to the event that \( x \) fails to predict outage under hypothesis \( H_1 \). Now, the performance of interference model \( x \) can be evaluated using the false alarm and miss-detection probabilities, namely \( p_{fa}^x \) and \( p_{md}^x \). Mathematically speaking,

\[
\begin{align*}
    p_{fa}^x &= \Pr \left[ \gamma < \beta | \gamma_{\text{PhyM}} \geq \beta \right], \\
    p_{md}^x &= \Pr \left[ \gamma \geq \beta | \gamma_{\text{PhyM}} < \beta \right].
\end{align*}
\]  

(4)

The false alarm and miss-detection probabilities quantify the accuracy of any interference model \( x \) compared to the reference physical model. Next, we define our accuracy index to be a convex combination of these probabilities.

**Definition 1 (Interference Model Accuracy Index):** For any constant \( 0 \leq \xi \leq 1 \) and interference model \( x \), the interference model accuracy index is defined as

\[
IMA(x, \xi) = \xi p_{fa}^x + (1 - \xi) p_{md}^x
\]

where \( p_{fa}^x \) and \( p_{md}^x \) are given in (4).

IMA \((x, \xi)\) is a unit-less real-valued quantity ranging within \([0, 1]\), where higher values represent higher similarity between test model \( x \) and the reference physical model.

When \( \xi = \Pr \left[ \gamma_{\text{PhyM}} \geq \beta \right] \), it follows that \( \xi p_{fa}^x + (1 - \xi) p_{md}^x \) is the average decision error under interference model \( x \). Therefore, \( IMA(x, \Pr \left[ \gamma_{\text{PhyM}} \geq \beta \right]) \) is the average probability that interference model \( x \) gives the same decision as the reference physical model.

The proposed index is a universal metric that can be used to quantify the accuracy of different interference models introduced in the literature under different assumptions. We illustrate the use of this index in the next sections, by evaluating the accuracy of IBM and PRM for two example scenarios. For the rest of this paper, we consider \( \xi = \Pr \left[ \gamma_{\text{PhyM}} \geq \beta \right] \), so that \( IMA(x, \xi) \) evaluates the average probability of correct decision under interference model \( x \).

### III. Scenario 1: Rayleigh Fading Channel with Omnidirectional Communications

In this section, we evaluate the accuracy of IBM and PRM for a wireless network exhibiting Rayleigh fading channel and omnidirectional transmission/reception. These assumptions are, arguably, among the most common assumptions in the analysis and design of wireless networks [7]. Under these assumptions, although PhyM is more tractable for the performance analysis than PRM and IBM [7], we can derive closed-form expression for the new accuracy index, which in turn results in characterizing its fundamental properties. Nonetheless, even in this network setting, PRM and IBM are more appealing than PhyM for protocol development and for network optimization [2]. Moreover, notice that we are not proposing IBM or PRM, rather, we are exemplifying the use of our accuracy index with these well-known interference models.

We consider a reference receiver (called the typical receiver and indexed by 0) at the origin of the Polar coordinate, and its intended transmitter having geometrical/spatial length \( d_0 \). We consider a homogeneous Poisson network of interferers (unintended transmitters) on the plane with density \( \lambda_i \) per unit area. For sake of notation simplicity, we drop index 0 from the typical receiver and keep only the indices of the transmitters in (2). All transmitters are active with transmission power \( p \) (no power control). With omnidirectional transmission and reception, there is no antenna gain, so \( g_{ik}^r = g_{ik}^t = 1 \), \( k \in \mathbb{I} \cup \{0\} \). Note that we have adopted this set of assumptions to facilitate illustration of the proposed accuracy index, and extension of this paper with more general set of assumptions is straightforward.

Let \( B(\theta, r_{in}, r_{out}) \) be a geometrical annulus sector with angle \( \theta \), inner radius \( r_{in} \), and outer radius \( r_{out} \) centered at the location of the typical receiver. To model a wireless channel, we consider a constant attenuation \( a \), distance-dependent attenuation with exponent \( \alpha \), and a Rayleigh fading component \( h \). Therefore, the channel attenuation between transmitter \( i \) at radial distance \( d_i \) and the typical receiver is \( g_i^r = a h r_i^{-\alpha} \). We are now ready to illustrate the utility of our interference model accuracy index.

### A. Accuracy of the Interference Ball Model

In this subsection, we derive the accuracy of IBM under the aforementioned system model. We first reformulate the false alarm probability as

\[
P_{fa}^{\text{IBM}} = \Pr \left[ \gamma_{\text{IBM}} < \beta | \gamma_{\text{PhyM}} \geq \beta \right] = \frac{\Pr \left[ \gamma_{\text{IBM}} < \beta \right] }{1 - \Pr \left[ \gamma_{\text{PhyM}} < \beta \right]} .
\]

(6)

Although PhyM considers the impacts of all the interferers, IBM considers the effects of the near-field ones. Consequently, \( \gamma_{\text{PhyM}} \leq \gamma_{\text{IBM}} \), and thus \( \Pr \left[ \gamma_{\text{PhyM}} \geq \beta | \gamma_{\text{IBM}} < \beta \right] \) in the nominator of (6) is equal to 0, resulting in \( P_{fa}^{\text{IBM}} = 0 \).

For the miss-detection probability, we have

\[
P_{md}^{\text{IBM}} = \Pr \left[ \gamma_{\text{IBM}} \geq \beta | \gamma_{\text{PhyM}} < \beta \right] = 1 - \frac{\Pr \left[ \gamma_{\text{IBM}} < \beta \right] }{\Pr \left[ \gamma_{\text{PhyM}} < \beta \right]} \; \Pr \left[ \gamma_{\text{PhyM}} < \beta \right] = 1 - \frac{\Pr \left[ \gamma_{\text{IBM}} < \beta \right] }{\Pr \left[ \gamma_{\text{PhyM}} < \beta \right]} ,
\]

(7)

where the last equality is from \( \gamma_{\text{PhyM}} \leq \gamma_{\text{IBM}} \). Let \( \mathbf{E}_x \) denote expectation over random variable \( x \). Using similar approach as in [5], we have

\[
\Pr \left[ \gamma_{\text{IBM}} < \beta \right] = 1 - \exp \left\{ -\frac{\sigma^2 d_0^2 \lambda}{p a \beta} - \pi \lambda \mathbf{E}_h \left[ \gamma_{\text{IBM}} \right] \left( 1 - e^{-\beta d_0^2 h r_{BM}^{-\alpha}} \right) \right\}
\]

+ \left( \beta d_0^2 h \right)^{2/\alpha} \Gamma \left( 1 - \frac{2}{\alpha}, \beta d_0^2 h r_{BM}^{-\alpha} \right) ,
\]

(8)

where \( \Gamma (\cdot, \cdot) \) is the incomplete Gamma function, and probability density function of \( h \) is \( f_h(x) = e^{-x} \). Detailed derivation steps are avoided from this paper due to space limitation, but are presented in the extended version [10]. Proofs of the following results can be also found in [10].
$Pr[\gamma^{\text{PhysM}} < \beta]$, we evaluate $Pr[\gamma^{\text{IBM}} < \beta]$ at $r_{\text{IBM}} \rightarrow \infty$. 
Therefore, $Pr[\gamma^{\text{PhysM}} < \beta]$ is equal to

$$1 - \exp\left\{-\frac{\sigma^2 d_0^2}{pa} - \pi \lambda_t E_h \left[\left(\beta d_0^2 h / \lambda_s^2\right)^{\frac{2}{\alpha}} \Gamma\left(1 - \frac{2}{\alpha}\right)\right]\right\},$$  

(9)

where $\Gamma(\cdot)$ is the Gamma function. Substituting (8)–(9) into (7), the miss-detection probability follows. Also, from (5), the accuracy of the interference ball model IMA (IBM, $Pr[\gamma^{\text{PhysM}} \geq \beta]$) is derived.

**Result 1 (Perfect Interference Ball Model):** For any constant $0 \leq \xi \leq 1$, IMA (IBM, $\xi$) $\rightarrow 1$ as $r_{\text{IBM}} \rightarrow \infty$.

Result 1 implies that the accuracy of IBM increases with $r_{\text{IBM}}$, and it can be arbitrary accurate for sufficiently large $r_{\text{IBM}}$. The price, however, is more complicated IBM for the protocol development and network optimization (2) as it accounts for more interferers. Also, negotiation with other transmitters (e.g., for joint power control or scheduling) within $r_{\text{IBM}}$ becomes more complicated.

**B. Accuracy of the Protocol Model**

We now consider the PRM and first note that

$$Pr_{\text{fa}}^{\text{PRM}} = Pr[\gamma^{\text{PRM}} < \beta | \gamma^{\text{PhysM}} \geq \beta]$$

$$= 1 - \left(1 - Pr[\gamma^{\text{PRM}} < \beta]\right) \left(1 - Pr[\gamma^{\text{PhysM}} < \beta] \ | \gamma^{\text{PRM}} \geq \beta\right) \bigg/ \left(1 - Pr[\gamma^{\text{PhysM}} < \beta]\right),$$

(10)

and that

$$Pr_{\text{mnd}}^{\text{PRM}} = Pr[\gamma^{\text{PRM}} \geq \beta | \gamma^{\text{PhysM}} < \beta]$$

$$= \left(1 - Pr[\gamma^{\text{PRM}} < \beta]\right) Pr[\gamma^{\text{PhysM}} < \beta | \gamma^{\text{PRM}} \geq \beta] \bigg/ Pr[\gamma^{\text{PhysM}} < \beta].$$

(11)

In the last two equations, note that $Pr[\gamma^{\text{PhysM}} < \beta]$ is derived in (9). In the following, we evaluate $Pr[\gamma^{\text{PRM}} < \beta]$ and $Pr[\gamma^{\text{PhysM}} < \beta | \gamma^{\text{PRM}} \geq \beta]$.

Event $\gamma^{\text{PRM}} < \beta$ occurs if there is at least one interferer inside $B(2\pi, 0, r_{\text{PRM}})$. As $T$ is a homogenous Poisson point process with intensity $\lambda_t$, we have

$$Pr[\gamma^{\text{PRM}} < \beta] = 1 - \exp\left\{-\pi \lambda_t r_{\text{PRM}}^2\right\}.$$  

(12)

Event $\gamma^{\text{PRM}} \geq \beta$ implies that there is no interferer inside $B(2\pi, 0, r_{\text{PRM}})$. Therefore, $Pr[\gamma^{\text{PhysM}} < \beta | \gamma^{\text{PRM}} \geq \beta]$ is given in (13) on the top of page 5 where $I$ is the indicator function taking one over set $\cdot$ and zero otherwise.

Substituting (9) and (12) into (10)–(11), and the results into (5), we can find IMA (PRM, $Pr[\gamma^{\text{PhysM}} \geq \beta]$).

**Result 2 (Miss-detection–False Alarm Tradeoff):** Consider the protocol model of interference with Rayleigh fading channel. Increasing the interference range $\gamma_{\text{PRM}}$ reduces the false alarm probability and increases the miss-detection probability. Decreasing the interference range increases the false alarm probability and reduces the miss-detection probability.

**IV. Scenario 2: Deterministic Channel, Directional Communications, with Obstacles**

In this section, we investigate the accuracy of the IBM and PRM in modeling a wireless network with deterministic channel condition, directional communications, and impenetrable obstacles in the environment. Application areas include modeling and performance evaluation of mmWave networks, where the sparse scattering characteristic of the mmWave frequencies and the narrow-beam operation make the mmWave channel more deterministic compared to that of traditional microwave systems having rich scattering environment and omnidirectional communication (8). Moreover, extreme penetration loss in the mmWave frequencies (e.g., 35 dB due to the human body (8)) justifies the assumption of impenetrable obstacles in Scenario 2.

We assume similar homogenous Poisson network of interferers as in Section [11]. If there is no obstacle on the link between transmitter $i$ and the typical receiver, we say that transmitter $i$ has line-of-sight (LoS) condition with respect to the typical receiver, otherwise it is in non-LoS condition. We assume that transmitter of every link is spatially aligned with its intended receiver, so there is no beam-searching phase. The effects of beam-searching phase is analyzed in [11]. We assume the same operating beamwidth $\theta$ for all devices in both transmission and reception modes. Motivated by the large number of antenna elements in mmWave systems, we neglect the sidelobe radiations from all interference models (PRM, IBM, and PhyM). Moreover, we model the antenna pattern with an ideal sector model, where the antenna gain for each transmitter/receiver is $2\theta/\theta$ in the main lobe (11). With a random number of obstacles, each having random location and size, we see that the link between transmitter $i$ and receiver $j$ with length $d_{ij}$ is in the LoS condition with probability $e^{-d_{ij}/\lambda_o}$, where $\lambda_o$ is the density of obstacles per unit area and $\epsilon$ is a constant value that depends on the average size of the obstacles in the environment (12). Due to the exponential decrease of the LoS probability with the link length, very far transmitters are most likely blocked. As in (6), (12), we assume independent LoS conditions among the typical receiver and all other transmitters. Again, we are using this system model to highlight the fundamental properties of the accuracy index. The exact value of this index can be easily numerically calculated under any system model, not just the one considered in this section.

To evaluate the accuracy of the IBM and PRM, we first note that an interferer can give a significant interference contribution at the typical receiver if: (a) the typical receiver is inside its main lobe, (b) it has LoS condition with respect to the typical receiver, and (c) it is inside the main lobe of the typical receiver. Due to random deployment of the transmitters/receivers, the probability that the typical receiver locates inside the main lobe of a transmitter is $\theta/2\pi$. Moreover, we have independent LoS events among the typical receiver and individual transmitters. Therefore, if the transmitter density per unit area is $\lambda_t$, the interferers for which conditions (a)–
We simulate a spatial Poisson network of interferers and obstacles with density $\lambda_1$ and $\lambda_o$ per unit area. Length of the typical link is 20 m. For Scenario 1 (Section III), we simulate a traditional outdoor microwave network [6] with average attenuation $a = 22.7$ dB at the reference distance 1 m, pathloss index $\alpha = 3.6$, and noise power $\sigma = -111$ dBm (around 2 MHz bandwidth). For Scenario 2 (Section IV), we simulate a mmWave network at 28 GHz [6] with $a = -61.4$ dB, $\alpha = 2.5$, $\sigma = -81$ dBm (around 2 GHz bandwidth), and $\epsilon\lambda_o = 0.008$ [12]. For both scenarios, we consider $p = 20$ dBm transmission power and $\beta = 5$ dB minimum SINR threshold. For the ease of illustration, we define the notion of the average inter-transmitter distance as $d_t = 1/\sqrt{N_t}$.

Fig. 1 illustrates the impact of the interference range on the accuracy of both IBM and PRM under Scenario 1. From Fig. 1(a) increasing $r_{\text{PRM}}$ increases $p_{\text{fa}}^{\text{PRM}}$ and reduces $p_{\text{md}}^{\text{PRM}}$, highlighted as the tradeoff between the miss-detection and false alarm probabilities, stated in Result 2. This tradeoff may lead to increment (see $d_t = 30$) or decrement (see $d_t = 80$) of the accuracy index of the PRM with the interference range. The IBM has zero false alarm probability, not depicted in Fig. 1(a) for sake of clarity of the figure. Moreover, as stated in Result 1, $p_{\text{fa}}^{\text{IBM}}$ decreases with $r_{\text{IBM}}$, leading to a more accurate IBM, as can be confirmed in Fig 1(b). Note that with the same transmitter density and interference range, the PRM has lower miss-detection probability than the IBM; however, better false alarm performance of the IBM leads to less errors in detecting outage events and therefore higher accuracy index.

Fig. 2 shows the accuracy of the IBM and PRM under Scenario 1 against the average inter-transmitter distance $d_t$. Again, we can observe enhancement in the accuracy of the IBM with $r_{\text{IBM}}$, whereas the accuracy index of the PRM shows a complicated behavior as a function of $r_{\text{PRM}}$. Both interference models are very accurate at extremely dense transmitters deployments. In fact, the interference level is so high in...
this case that $\xi = \Pr [\eta^{\text{PhyM}} \geq \beta]$ is almost 0, and therefore the accuracy index is determined only by the miss-detection probability. And, increasing the transmitter density (lower $d_t$) decreases this probability for both IBM and PRM, see Fig. 1(a) improving their accuracy. For ultra sparse transmitter deployments, again, both interference models work accurately, as $\xi \to 1$ in this case and therefore only the false alarm probability will determine the accuracy index. This probability is zero for the IBM, and it gets smaller values (asymptotically zero) for the PRM with higher $d_t$, see Fig. 1(a).

Fig. 3 illustrates the impact of the operating bandwidth and average inter-transmitter distance on the accuracy index of both IBM and PRM under Scenario 2. As expected, directionality and blockage improve the accuracy of both interference models. Surprisingly, the PRM is accurate enough to motivate adopting this model to analyze and design of mmWave networks instead of the PhyM or even the IBM. Compared to the PRM, the PhyM and IBM respectively have less than 5% and 2% higher accuracy in modeling the interference and detecting the outage events, but with substantially higher complexities. These complexities often result in limited (mostly intractable) mathematical analysis and little insight. This highlights the importance of having quantitative (not only qualitative) insight of the accuracy of different interference models we may face in different wireless networks. Thereby, we can adopt a simple yet accurate enough model for link-level and system-level performance analysis.

VI. CONCLUSIONS

We addressed very fundamental questions in analysis and design of wireless networks: how accurate different interference models are and how to select the right one. In particular, we proposed a new index that assesses the accuracy of any interference model in detecting outage events, under any set of assumptions on the communication protocols. Based on this index, we evaluated the accuracy of two prominent interference models, namely the classical protocol and interference...
ball models. Our detailed analysis revealed that, unlike the protocol model, the interference ball model can be arbitrary accurate by adding complexity into the model. Moreover, blockage and directionality can substantially improve the accuracy of both interference models. In such settings, even the simplest interference model may be almost as accurate as the most complex one. This is a promising feature of many future wireless technologies such as millimeter wave networks, which exhibit such blockage and directionality requirements, to significantly improve the mathematical tractability with negligible drop in the interference model accuracy.

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