
http://dx.doi.org/10.1109/TRO.2016.2624754

Institute of Electrical and Electronics Engineers (IEEE)

Author’s final manuscript

Wed Jan 02 20:19:27 EST 2019

http://hdl.handle.net/1721.1/107697

Creative Commons Attribution-Noncommercial-Share Alike

http://creativecommons.org/licenses/by-nc-sa/4.0/
This paper has been accepted for publication in IEEE Transactions on Robotics.

DOI: 10.1109/TRO.2016.2624754

Please cite the paper as:

“Past, Present, and Future of Simultaneous Localization And Mapping: Towards the Robust-Perception Age”,

bibtex:

@article{Cadena16tro-SLAMfuture,
    title = {Past, Present, and Future of Simultaneous Localization And Mapping: Towards the Robust-Perception Age},
    journal = {IEEE Transactions on Robotics},
    year = {2016},
    number = {6},
    pages = {1309–1332},
    volume = {32}
}
Past, Present, and Future of Simultaneous Localization And Mapping: Towards the Robust-Perception Age

Cesar Cadena, Luca Carlone, Henry Carrillo, Yasir Latif, Davide Scaramuzza, José Neira, Ian Reid, John J. Leonard

Abstract—Simultaneous Localization And Mapping (SLAM) consists in the concurrent construction of a model of the environment (the map), and the estimation of the state of the robot moving within it. The SLAM community has made astonishing progress over the last 30 years, enabling large-scale real-world applications, and witnessing a steady transition of this technology to industry. We survey the current state of SLAM and consider future directions. We start by presenting what is now the de-facto standard formulation for SLAM. We then review related work, covering a broad set of topics including robustness and scalability in long-term mapping, metric and semantic representations for mapping, theoretical performance guarantees, active SLAM and exploration, and other new frontiers. This paper simultaneously serves as a position paper and tutorial to those who are users of SLAM. By looking at the published research with a critical eye, we delineate open challenges and new research issues, that still deserve careful scientific investigation. The paper also contains the authors’ take on two questions that often animate discussions during robotics conferences: Do robots need SLAM? and Is SLAM solved?

Index Terms—Robots, SLAM, Localization, Mapping, Factor graphs, Maximum a posteriori estimation, sensing, perception.

MULTIMEDIA MATERIAL

Additional material for this paper, including an extended list of references (bibtex) and a table of pointers to online datasets for SLAM, can be found at https://slam-future.github.io/.

C. Cadena is with the Autonomous Systems Lab, ETH Zürich, Switzerland. e-mail: cesarc@ethz.ch
L. Carlone is with the Laboratory for Information and Decision Systems, Massachusetts Institute of Technology, USA. e-mail: lcarlone@mit.edu
H. Carrillo is with the Escuela de Ciencias Exactas e Ingeniería, Universidad Sergio Arboleda, Colombia, and Pontificia Universidad Javeriana, Colombia. e-mail: henry.carrillo@usa.edu.co
Y. Latif and I. Reid are with the School of Computer Science, University of Adelaide, Australia, and the Australian Center for Robotic Vision. e-mail: yasir.latif@adelaide.edu.au, ian.reid@adelaide.edu.au
J. Neira is with the Departamento de Informática e Ingeniería de Sistemas, Universidad de Zaragoza, Spain. e-mail: jneira@unizar.es
D. Scaramuzza is with the Robotics and Perception Group, University of Zürich, Switzerland. e-mail: adavide@ifi.uzh.ch
J.J. Leonard is with Marine Robotics Group, Massachusetts Institute of Technology, USA. e-mail: jleonard@mit.edu

This paper summarizes and extends the outcome of the workshop “The Problem of Mobile Sensors: Setting future goals and indicators of progress for SLAM” [25], held during the Robotics: Science and System (RSS) conference (Rome, July 2015).

This work has been partially supported by the following grants: MINECO-FEDER DPI2015-68905-P, Grupo DGA T04-FSE; ARC grants DP130104413, CE140100016 and FL130100102; NCCR Robotics; PJJ 6601; EU-FP7-ICT-Project TRADR 609763, EU-H2020-688652 and SERI-15.0284.

I. INTRODUCTION

SLAM comprises the simultaneous estimation of the state of a robot equipped with on-board sensors, and the construction of a model (the map) of the environment that the sensors are perceiving. In simple instances, the robot state is described by its pose (position and orientation), although other quantities may be included in the state, such as robot velocity, sensor biases, and calibration parameters. The map, on the other hand, is a representation of aspects of interest (e.g., position of landmarks, obstacles) describing the environment in which the robot operates.

The need to use a map of the environment is twofold. First, the map is often required to support other tasks; for instance, a map can inform path planning or provide an intuitive visualization for a human operator. Second, the map allows limiting the error committed in estimating the state of the robot. In the absence of a map, dead-reckoning would quickly drift over time; on the other hand, using a map, e.g., a set of distinguishable landmarks, the robot can “reset” its localization error by re-visiting known areas (so-called loop closure). Therefore, SLAM finds applications in all scenarios in which a prior map is not available and needs to be built.

In some robotics applications the location of a set of landmarks is known a priori. For instance, a robot operating on a factory floor can be provided with a manually-built map of artificial beacons in the environment. Another example is the case in which the robot has access to GPS (the GPS satellites can be considered as moving beacons at known locations). In such scenarios, SLAM may not be required if localization can be done reliably with respect to the known landmarks.

The popularity of the SLAM problem is connected with the emergence of indoor applications of mobile robotics. Indoor operation rules out the use of GPS to bound the localization error; furthermore, SLAM provides an appealing alternative to user-built maps, showing that robot operation is possible in the absence of an ad hoc localization infrastructure.

A thorough historical review of the first 20 years of the SLAM problem is given by Durrant-Whyte and Bailey in two surveys [7, 69]. These mainly cover what we call the classical age (1986-2004); the classical age saw the introduction of the main probabilistic formulations for SLAM, including approaches based on Extended Kalman Filters, Rao-Blackwellised Particle Filters, and maximum likelihood estimation; moreover, it delineated the basic challenges connected
to efficiency and robust data association. Two other excellent references describing the three main SLAM formulations of the classical age are the book of Thrun, Burgard, and Fox [64] and the chapter of Stachniss et al. [160]. The subsequent period is what we call the algorithmic-analysis age (2004-2015), and is partially covered by Dissanayake et al. in [64]. The algorithmic analysis period saw the study of fundamental properties of SLAM, including observability, convergence, and consistency. In this period, the key role of sparsity towards efficient SLAM solvers was also understood, and the main open-source SLAM libraries were developed.

We review the main SLAM surveys to date in Table I, observing that most recent surveys only cover specific aspects or sub-fields of SLAM. The popularity of SLAM in the last 30 years is not surprising if one thinks about the manifold aspects that SLAM involves. At the lower level (called the front-end in Section II), SLAM naturally intersects other research fields such as computer vision and signal processing; at the higher level (that we later call the back-end), SLAM is an appealing mix of geometry, graph theory, optimization, and probabilistic estimation. Finally, a SLAM expert has to deal with practical aspects ranging from sensor calibration to system integration.

The present paper gives a broad overview of the current state of SLAM, and offers the perspective of part of the community on the open problems and future directions for the SLAM research. Our main focus is on metric and semantic SLAM, and we refer the reader to the recent survey by Lowry et al. [160], which provides a comprehensive review of vision-based place recognition and topological SLAM.

Before delving into the paper, we first discuss two questions that often animate discussions during robotics conferences: (1) do autonomous robots need SLAM? and (2) is SLAM solved as an academic research endeavor? We will revisit these questions at the end of the manuscript.

Answering the question “Do autonomous robots really need SLAM?” requires understanding what makes SLAM unique. SLAM aims at building a globally consistent representation of the environment, leveraging both ego-motion measurements and loop closures. The keyword here is “loop closure”: if we sacrifice loop closures, SLAM reduces to odometry. In early applications, odometry was obtained by integrating wheel encoders. The pose estimate obtained from wheel odometry quickly drifts, making the estimate unusable after few meters [128, Ch. 6]; this was one of the main thrusts behind the development of SLAM: the observation of external landmarks is useful to reduce the trajectory drift and possibly correct it [183]. However, more recent odometry algorithms are based on visual and inertial information, and have very small drift (< 0.5% of the trajectory length [82]). Hence the question becomes legitimate: do we really need SLAM? Our answer is three-fold.

First of all, we observe that the SLAM research done over the last decade has itself produced the visual-inertial odometry algorithms that currently represent the state of the art, e.g., [163] [175]; in this sense Visual-Inertial Navigation (VIN) is SLAM: VIN can be considered a reduced SLAM system, in which the loop closure (or place recognition) module is disabled. More generally, SLAM has directly led to the study of sensor fusion under more challenging setups (i.e., no GPS, low quality sensors) than previously considered in other literature (e.g., inertial navigation in aerospace engineering).

The second answer regards the true topology of the environment. A robot performing odometry and neglecting loop closures interprets the world as an “infinite corridor” (Fig. I left) in which the robot keeps exploring new areas indefinitely. A loop closure event informs the robot that this “corridor” keeps intersecting itself (Fig. I right). The advantage of loop closure now becomes clear: by finding loop closures, the robot understands the real topology of the environment, and is able to find shortcuts between locations (e.g., point B and C in the map). Therefore, if getting the right topology of the environment is one of the merits of SLAM, why not simply drop the metric information and just do place recognition? The answer is simple: the metric information makes place recognition much simpler and more robust; the metric reconstruction informs the robot about loop closure opportunities and allows discarding spurious loop closures [150]. Therefore, while SLAM might be redundant in principle (an oracle place recognition module would suffice for topological mapping), SLAM offers a natural defense against wrong data association and perceptual aliasing, where similarly looking scenes, corresponding to distinct locations in the environment, would deceive place recognition. In this sense, the SLAM map provides a way to predict and validate future measurements: we believe that this mechanism is key to robust operation.

The third answer is that SLAM is needed for many applications that, either implicitly or explicitly, do require a globally consistent map. For instance, in many military and civilian applications, the goal of the robot is to explore an environment and report a map to the human operator, ensuring that full coverage of the environment has been obtained. Another example is the case in which the robot has to perform structural inspection (of a building, bridge, etc.); also in this case a globally consistent 3D reconstruction is a requirement for successful operation.

This question of “is SLAM solved?” is often asked within the robotics community, c.f. [87]. This question is difficult to answer because SLAM has become such a broad topic that the question is well posed only for a given robot/environment/performance combination. In particular, one can evaluate the maturity of the SLAM problem once the following aspects are specified:

- **robot**: type of motion (e.g., dynamics, maximum speed), available sensors (e.g., resolution, sampling rate), avail-

<table>
<thead>
<tr>
<th>Year</th>
<th>Topic</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>2006</td>
<td>Probabilistic approaches and data association</td>
<td>Durrant-Whyte and Bailey [7, 69]</td>
</tr>
<tr>
<td>2008</td>
<td>Filtering approaches</td>
<td>Aulinas et al. [6]</td>
</tr>
<tr>
<td>2011</td>
<td>SLAM back-end</td>
<td>Grisetti et al. [67]</td>
</tr>
<tr>
<td>2011</td>
<td>Observability, consistency and convergence</td>
<td>Dissanayake et al. [64]</td>
</tr>
<tr>
<td>2012</td>
<td>Visual odometry</td>
<td>Scaramuzza and Fraundorfer [85, 218]</td>
</tr>
<tr>
<td>2016</td>
<td>Multi robot SLAM</td>
<td>Saeedi et al. [110]</td>
</tr>
<tr>
<td>2016</td>
<td>Visual place recognition</td>
<td>Lowry et al. [160]</td>
</tr>
<tr>
<td>2016</td>
<td>SLAM in the Handbook of Robotics</td>
<td>Stachniss et al. [160, Ch. 46]</td>
</tr>
<tr>
<td>2016</td>
<td>Theoretical aspects</td>
<td>Huang and Dissanayake [109]</td>
</tr>
</tbody>
</table>
able computational resources;
- environment: planar or three-dimensional, presence of natural or artificial landmarks, amount of dynamic elements, amount of symmetry and risk of perceptual aliasing. Note that many of these aspects actually depend on the sensor-environment pair: for instance, two rooms may look identical for a 2D laser scanner (perceptual aliasing), while a camera may discern them from appearance cues;
- performance requirements: desired accuracy in the estimation of the state of the robot, accuracy and type of representation of the environment (e.g., landmark-based or dense), success rate (percentage of tests in which the accuracy bounds are met), estimation latency, maximum operation time, maximum size of the mapped area.

For instance, mapping a 2D indoor environment with a robot equipped with wheel encoders and a laser scanner, with sufficient accuracy (< 10 cm) and sufficient robustness (say, low failure rate), can be considered largely solved (an example of industrial system performing SLAM is the Kuka Navigation Solution [145]). Similarly, vision-based SLAM with slowly-moving robots (e.g., Mars rovers [166], domestic robots [114]), and visual-inertial odometry [94] can be considered mature research fields.

On the other hand, other robot/environment/performance combinations still deserve a large amount of fundamental research. Current SLAM algorithms can be easily induced to fail when either the motion of the robot or the environment are too challenging (e.g., fast robot dynamics, highly dynamic environments); similarly, SLAM algorithms are often unable to face strict performance requirements, e.g., high rate estimation for fast closed-loop control. This survey will provide a comprehensive overview of these open problems, among others.

In this paper, we argue that we are entering in a third era of the SLAM system: self-tuning, in that satisfactory operation is enabled by expert tuning of the system parameters (e.g., stopping conditions, thresholds for outlier rejection).

In this position paper. The more experienced researchers can jump directly to the section of interest, where they will find a self-contained overview of the state of the art and open problems.

Paper organization. The paper starts by presenting a standard formulation and architecture for SLAM (Section II). Section III tackles robustness in life-long SLAM. Section IV deals with scalability. Section V discusses how to represent the geometry of the environment. Section VI extends the question of the environment representation to the modeling of semantic information. Section VII provides an overview of the current accomplishments on the theoretical aspects of SLAM. Section VIII broadens the discussion and reviews the active SLAM problem in which decision making is used to improve the quality of the SLAM results. Section IX provides an overview of recent trends in SLAM, including the use of unconventional sensors and deep learning. Section X provides final remarks. Throughout the paper, we provide many pointers to related work outside the robotics community. Despite its unique traits, SLAM is related to problems addressed in computer vision, computer graphics, and control theory, and cross-fertilization among these fields is a necessary condition to enable fast progress.

For the non-expert reader, we recommend to read Durrant-Whyte and Bailey’s SLAM tutorials [7, 69] before delving in this position paper. The more experienced researchers can jump directly to the section of interest, where they will find a self-contained overview of the state of the art and open problems.

II. ANATOMY OF A MODERN SLAM SYSTEM

The architecture of a SLAM system includes two main components: the front-end and the back-end. The front-end abstracts sensor data into models that are amenable for estimation, while the back-end performs inference on the abstracted data produced by the front-end. This architecture is summarized in Fig. 2. We review both components, starting from the back-end.
Maximum a posteriori (MAP) estimation and the SLAM back-end. The current de-facto standard formulation of SLAM has its origins in the seminal paper of Lu and Milios [161], followed by the work of Gutmann and Konolige [101]. Since then, numerous approaches have improved the efficiency and robustness of the optimization underlying the problem [63, 81, 100, 125, 192, 241]. All these approaches formulate SLAM as a maximum a posteriori estimation problem, and often use the formalism of factor graphs [143] to reason about the interdependence among variables.

Assume that we want to estimate an unknown variable $\mathbf{X}$; as mentioned before, in SLAM the variable $\mathbf{X}$ typically includes the trajectory of the robot (as a discrete set of poses) and the position of landmarks in the environment. We are given a set of measurements $Z = \{z_k : k = 1, \ldots, m\}$ such that each measurement can be expressed as a function of $\mathbf{X}$, i.e., $z_k = h_k(\mathbf{X}_k) + \epsilon_k$, where $\mathbf{X}_k \subseteq \mathbf{X}$ is a subset of the variables, $h_k(\cdot)$ is a known function (the measurement or observation model), and $\epsilon_k$ is random measurement noise.

In MAP estimation, we estimate $\mathbf{X}$ by computing the assignment of variables $\mathbf{X}^*$ that attains the maximum of the posterior $p(\mathbf{X}|Z)$ (the belief over $\mathbf{X}$ given the measurements):

$$\mathbf{X}^* = \arg \max_{\mathbf{X}} p(\mathbf{X}|Z) = \arg \max_{\mathbf{X}} p(Z|\mathbf{X}) p(\mathbf{X})$$

(1)

where the equality follows from the Bayes theorem. In (1), $p(Z|\mathbf{X})$ is the likelihood of the measurements $Z$ given the assignment $\mathbf{X}$, and $p(\mathbf{X})$ is a prior probability over $\mathbf{X}$. The prior probability includes any prior knowledge about $\mathbf{X}$; in case no prior knowledge is available, $p(\mathbf{X})$ becomes a constant (uniform distribution) which is inconsequential and can be dropped from the optimization. In that case MAP estimation reduces to maximum likelihood estimation. Note that, unlike Kalman filtering, MAP estimation does not require an explicit distinction between motion and observation model: both models are treated as factors and are seamlessly incorporated in the estimation process. Moreover, it is worth noting that Kalman filtering and MAP estimation return the same estimate in the linear Gaussian case, while this is not the case in general.

Assuming that the measurements $Z$ are independent (i.e., the corresponding noises are uncorrelated), problem (1) factorizes into:

$$\mathbf{X}^* = \arg \max_{\mathbf{X}} p(\mathbf{X}) \prod_{k=1}^{m} p(z_k|\mathbf{X}) = \arg \max_{\mathbf{X}} p(\mathbf{X}) \prod_{k=1}^{m} p(z_k|\mathbf{X}_k)$$

(2)

where, on the right-hand-side, we noticed that $z_k$ only depends on the subset of variables in $\mathbf{X}_k$.

Problem (2) can be interpreted in terms of inference over a factors graph [143]. The variables correspond to nodes in the factor graph. The terms $p(z_k|\mathbf{X}_k)$ and the prior $p(\mathbf{X})$ are called factors, and they encode probabilistic constraints over a subset of nodes. A factor graph is a graphical model that encodes the dependence between the $k$-th factor (and its measurement $z_k$) and the corresponding variables $\mathbf{X}_k$. A first advantage of the factor graph interpretation is that it enables an insightful visualization of the problem. Fig. 3 shows an example of a factor graph underlying a simple SLAM problem. The figure shows the variables, namely, the robot poses, the landmark positions, and the camera calibration parameters, and the factors imposing constraints among these variables. A second advantage is generality: a factor graph can model complex inference problems with heterogeneous variables and factors, and arbitrary interconnections. Furthermore, the connectivity of the factor graph in turn influences the sparsity of the resulting SLAM problem as discussed below.

In order to write (2) in a more explicit form, assume that the measurement noise $\epsilon_k$ is a zero-mean Gaussian noise with information matrix $\Omega_k$ (inverse of the covariance matrix). Then, the measurement likelihood in (2) becomes:

$$p(z_k|\mathbf{X}_k) \propto \exp\left(-\frac{1}{2}||h_k(\mathbf{X}_k) - z_k||^2_{\Omega_k}\right)$$

(3)

where we use the notation $||e||^2_{\Omega} = e^T \Omega e$. Similarly, assume that the prior can be written as: $p(\mathbf{X}) \propto \exp\left(-\frac{1}{2}||h_0(\mathbf{X}) - z_0||^2_{\Omega_0}\right)$, for some given function $h_0(\cdot)$, prior mean $z_0$, and information matrix $\Omega_0$. Since maximizing the posterior is the same as minimizing the negative log-posterior, the MAP estimate in (2) becomes:

$$\mathbf{X}^* = \arg \min_{\mathbf{X}} -\log \left( p(\mathbf{X}) \prod_{k=1}^{m} p(z_k|\mathbf{X}_k) \right) = \arg \min_{\mathbf{X}} \sum_{k=0}^{m} ||h_k(\mathbf{X}_k) - z_k||^2_{\Omega_k}$$

(4)

which is a nonlinear least squares problem, as in most problems of interest in robotics, $h_k(\cdot)$ is a nonlinear function. Note that the formulation (4) follows from the assumption of Normally distributed noise. Other assumptions for the noise distribution lead to different cost functions; for instance, if the noise follows a Laplace distribution, the squared $\ell_2$-norm in (4) is replaced by the $\ell_1$-norm. To increase resilience to outliers, it is also common to substitute the squared $\ell_2$-norm in (4) with robust loss functions (e.g., Huber or Tukey loss) [112].

The computer vision expert may notice a resemblance between problem (4) and bundle adjustment (BA) in Structure from Motion [241]; both (4) and BA indeed stem from a maximum a posteriori formulation. However, two key features
make SLAM unique. First, the factors in (4) are not constrained to model projective geometry as in BA, but include a broad variety of sensor models, e.g., inertial sensors, wheel encoders, GPS, to mention a few. For instance, in laser-based mapping, the factors usually constrain relative poses corresponding to different viewpoints, while in direct methods for visual SLAM, the factors penalize differences in pixel intensities across different views of the same portion of the scene. The second difference with respect to BA is that, in a SLAM scenario, problem (4) typically needs to be solved incrementally: new measurements are made available at each time step as the robot moves.

The minimization problem (4) is commonly solved via successive linearizations, e.g., the Gauss-Newton or the Levenberg-Marquardt methods (alternative approaches, based on convex relaxations and Lagrangian duality are reviewed in Section VII). Successive linearization methods proceed iteratively, starting from a given initial guess \( \mathbf{x} \), and approximate the cost function at \( \mathbf{x} \) with a quadratic cost, which can be optimized in closed form by solving a set of linear equations (the so called normal equations). These approaches can be seamlessly generalized to variables belonging to smooth manifolds (e.g., rotations), which are of interest in robotics [112].

The key insight behind modern SLAM solvers is that the matrix appearing in the normal equations is sparse and its sparsity structure is dictated by the topology of the underlying factor graph. This enables the use of fast linear solvers [125, 126, 146, 204]. Moreover, it allows designing incremental (or online) solvers, which update the estimate of \( \mathbf{x} \) as new observations are acquired [125, 126, 204]. Current SLAM libraries (e.g., GTSAM [61], g2o [146], Ceres [214], iSAM [126], and SLAM++ [204]) are able to solve problems with tens of thousands of variables in few seconds. The hands-on tutorials [61, 97] provide excellent introductions to two of the most popular SLAM libraries; each library also includes a set of examples showcasing real SLAM problems.

The SLAM formulation described so far is commonly referred to as maximum a posteriori estimation, factor graph optimization, graph-SLAM, full smoothing, or smoothing and mapping (SAM). A popular variation of this framework is pose graph optimization, in which the variables to be estimated are poses sampled along the trajectory of the robot, and each factor imposes a constraint on a pair of poses.

MAP estimation has been proven to be more accurate and efficient than original approaches for SLAM based on nonlinear filtering. We refer the reader to the surveys [69] for an overview on filtering approaches, and to [23] for a comparison between filtering and smoothing. We remark that some SLAM systems based on EKF have also been demonstrated to attain state-of-the-art performance. Excellent examples of EKF-based SLAM systems include the Multi-State Constraint Kalman Filter of Mourikis and Roumeliotis [175], and the VIN systems of Kottas et al. [139] and Hesch et al. [105]. Not surprisingly, the performance mismatch between filtering and MAP estimation gets smaller when the linearization point for the EKF is accurate (as it happens in visual-inertial navigation problems), when using sliding-window filters, and when potential sources of inconsistency in the EKF are taken care of [105, 108, 139].

As discussed in the next section, MAP estimation is usually performed on a pre-processed version of the sensor data. In this regard, it is often referred to as the SLAM back-end.

Sensor-dependent SLAM front-end. In practical robotics applications, it might be hard to write directly the sensor measurements as an analytic function of the state, as required in MAP estimation. For instance, if the raw sensor data is an image, it might be hard to express the intensity of each pixel as a function of the SLAM state; the same difficulty arises with simpler sensors (e.g., a laser with a single beam). In both cases the issue is connected with the fact that we are not able to design a sufficiently general, yet tractable representation of the environment; even in the presence of such a general representation, it would be hard to write an analytic function that connects the measurements to the parameters of such a representation.

For this reason, before the SLAM back-end, it is common to have a module, the front-end, that extracts relevant features from the sensor data. For instance, in vision-based SLAM, the front-end extracts the pixel location of few distinguishable points in the environment; pixel observations of these points are now easy to model within the back-end. The front-end is also in charge of associating each measurement to a specific landmark (say, 3D point) in the environment: this is the so called data association. More abstractly, the data association module associates each measurement \( z_k \) with a subset of unknown variables \( X_k \) such that \( z_k = h_k(X_k) + \epsilon_k \). Finally, the front-end might also provide an initial guess for the variables in the nonlinear optimization (4). For instance, in feature-based monocular SLAM the front-end usually takes care of the landmark initialization, by triangulating the position of the landmark from multiple views.

A pictorial representation of a typical SLAM system is given in Fig. 2. The data association module in the front-end includes a short-term data association block and a long-term one. Short-term data association is responsible for associating corresponding features in consecutive sensor measurements; for instance, short-term data association would track the fact that 2 pixel measurements in consecutive frames are picturing the same 3D point. On the other hand, long-term data association (or loop closure) is in charge of associating new measurements to older landmarks. We remark that the back-end usually feeds back information to the front-end, e.g., to support loop closure detection and validation.

The pre-processing that happens in the front-end is sensor dependent, since the notion of feature changes depending on the input data stream we consider.

III. LONG-TERM AUTONOMY I: ROBUSTNESS

A SLAM system might be fragile in many aspects: failure can be algorithmic or hardware-related. The former class includes failure modes induced by limitation of the existing SLAM algorithms (e.g., difficulty to handle extremely dynamic or harsh environments). The latter includes failures due to
to sensor or actuator degradation. Explicitly addressing these failure modes is crucial for long-term operation, where one can no longer make simplifying assumptions about the structure of the environment (e.g., mostly static) or fully rely on on-board sensors. In this section we review the main challenges to algorithmic robustness. We then discuss open problems, including robustness against hardware-related failures.

One of the main sources of algorithmic failures is data association. As mentioned in Section II data association matches each measurement to the portion of the state the measurement refers to. For instance, in feature-based visual SLAM, it associates each visual feature to a specific landmark. Perceptual aliasing, the phenomenon in which different sensory inputs lead to the same sensor signature, makes this problem particularly hard. In the presence of perceptual aliasing, data association establishes erroneous measurement-state matches (outliers, or false positives), which in turn result in wrong estimates from the back-end. On the other hand, when data association decides to incorrectly reject a sensor measurement as spurious (false negatives), fewer measurements are used for estimation, at the expense of estimation accuracy.

The situation is made worse by the presence of unmodeled dynamics in the environment including both short-term and seasonal changes, which might deceive short-term and long-term data association. A fairly common assumption in current SLAM approaches is that the world remains unchanged as the robot moves through it (in other words, landmarks are static). This static world assumption holds true in a single mapping run in small scale scenarios, as long as there are no short term dynamics (e.g., people and objects moving around). When mapping over longer time scales and in large environments, change is inevitable.

Another aspect of robustness is that of doing SLAM in harsh environments such as underwater [73] [131]. The challenges in this case are the limited visibility, the constantly changing conditions, and the impossibility of using conventional sensors (e.g., laser range finder).

**Brief Survey.** Robustness issues connected to incorrect data association can be addressed in the front-end and/or in the back-end of a SLAM system. Traditionally, the front-end has been entrusted with establishing correct data association. Short-term data association is the easier one to tackle: if the sampling rate of the sensor is relatively fast, compared to the dynamics of the robot, tracking features that correspond to the same 3D landmark is easy. For instance, if we want to track a 3D point across consecutive images and assuming that the framerate is sufficiently high, standard approaches based on descriptor matching or optical flow [218] ensure reliable tracking. Intuitively, at high framerate, the viewpoint of the sensor (camera, laser) does not change significantly, hence the features at time \( t + 1 \) (and its appearance) remain close to the ones observed at time \( t \). Long-term data association in the front-end is more challenging and involves loop closure detection and validation. For loop closure detection at the front-end, a brute-force approach which detects features in the current measurement (e.g., image) and tries to match them against all previously detected features quickly becomes impractical. Bag-of-words models [226] avoid this intractability by quantizing the feature space and allowing more efficient search. Bag-of-words can be arranged into hierarchical vocabulary trees [189] that enable efficient lookup in large-scale datasets. Bag-of-words-based techniques such as [53] have shown reliable performance on the task of single session loop closure detection. However, these approaches are not capable of handling severe illumination variations as visual words can no longer be matched. This has led to develop new methods that explicitly account for such variations by matching sequences [173], gathering different visual appearances into a unified representation [48], or using spatial as well as appearance information [106]. A detailed survey on visual place recognition can be found in Lowry et al. [160]. Feature-based methods have also been used to detect loop closures in laser-based SLAM front-ends; for instance, Tipaldi et al. [242] propose FLIRT features for 2D laser scans.

Loop closure validation, instead, consists of additional geometric verification steps to ascertain the quality of the loop closure. In vision-based applications, RANSAC is commonly used for geometric verification and outlier rejection, see [218] and the references therein. In laser-based approaches, one can validate a loop closure by checking how well the current laser scan matches the existing map (i.e., how small is the residual error resulting from scan matching).

Despite the progress made to robustify loop closure detection at the front-end, in presence of perceptual aliasing, it is unavoidable that wrong loop closures are fed to the back-end. Wrong loop closures can severely corrupt the quality of the MAP estimate [238]. In order to deal with this issue, a recent line of research [33] [150] [191] [238] proposes techniques to make the SLAM back-end resilient against spurious measurements. These methods reason on the validity of loop closure constraints by looking at the residual error induced by the constraints during optimization. Other methods, instead, attempt to detect outliers a priori, that is, before any optimization takes place, by identifying incorrect loop closures that are not supported by the odometry [213].

In dynamic environments, the challenge is twofold. First, the SLAM system has to detect, discard, or track changes. While mainstream approaches attempt to discard the dynamic portion of the scene [180], some works include dynamic elements as part of the model [11] [253]. The second challenge regards the fact that the SLAM system has to model permanent or semi-permanent changes, and understand how and when to update the map accordingly. Current SLAM systems that deal with dynamics either maintain multiple (time-dependent) maps of the same location [60], or have a single representation parameterized by some time-varying parameter [140].

**Open Problems.** In this section we review open problems and novel research questions arising in long-term SLAM.

**Failsafe SLAM and recovery:** Despite the progress made on the SLAM back-end, current SLAM solvers are still vulnerable in the presence of outliers. This is mainly due to the fact that virtually all robust SLAM techniques are based on iterative optimization of nonconvex costs. This has two consequences:
first, the outlier rejection outcome depends on the quality of
the initial guess fed to the optimization; second, the system is
inherently fragile: the inclusion of a single outlier degrades the
quality of the estimate, which in turn degrades the capability of
discerning outliers later on. These types of failures lead to
an incorrect linearization point from which recovery is not
trivial, especially in an incremental setup. An ideal SLAM
solution should be fail-safe and failure-aware, i.e., the system
needs to be aware of imminent failure (e.g., due to outliers
or degeneracies) and provide recovery mechanisms that can
re-establish proper operation. None of the existing SLAM
approaches provides these capabilities. A possible way to
achieve this is a tighter integration between the front-end and
the back-end, but how to achieve that is still an open question.

Robustness to HW failure: While addressing hardware fail-
ures might appear outside the scope of SLAM, these failures
impact the SLAM system, and the latter can play a key role
in detecting and mitigating sensor and locomotion failures.
If the accuracy of a sensor degrades due to malfunctioning,
off-nominal conditions, or aging, the quality of the sensor
measurements (e.g., noise, bias) does not match the noise
model used in the back-end (c.f. eq. (3)), leading to poor
estimates. This naturally poses different research questions:
how can we detect degraded sensor operation? how can we
adjust sensor noise statistics (covariances, biases) accordingly?
more generally, how do we resolve conflicting information
from different sensors? This seems crucial in safety-critical
applications (e.g., self-driving cars) in which misinterpretation
of sensor data may put human life at risk.

Metric Relocalization: While appearance-based, as opposed
to feature-based, methods are able to close loops between
day and night sequences or between different seasons, the
resulting loop closure is topological in nature. For metric
relocalization (i.e., estimating the relative pose with respect
to the previously built map), feature-based approaches are still
the norm; however, current feature descriptors lack sufficient
invariance to work reliably under such circumstances. Spatial
information, inherent to the SLAM problem, such as trajectory
matching, might be exploited to overcome these limitations.
Additionally, mapping with one sensor modality (e.g., 3D
lidar) and localizing in the same map with a different sensor
modality (e.g., camera) can be a useful addition. The work
of Wolcott et al. [260] is an initial step in this direction.

Time varying and deformable maps: Mainstream SLAM
methods have been developed with the rigid and static world
assumption in mind; however, the real world is non-rigid both
due to dynamics as well as the inherent deformability of ob-
jects. An ideal SLAM solution should be able to reason about
dynamics in the environment including non-rigidity, work over
long time periods generating “all terrain” maps and be able to
do so in real time. In the computer vision community, there
have been several attempts since the 80s to recover shape
from non-rigid objects but with restrictive applicability. Recent
results in non-rigid SfM such as [91] [96] are less restrictive
but only work in small scenarios. In the SLAM community,
Newcombe et al. [182] have address the non-rigid case for
small-scale reconstruction. However, addressing the problem
of non-rigid maps at a large scale is still largely unexplored.

Automatic parameter tuning: SLAM systems (in particular,
the data association modules) require extensive parameter
tuning in order to work correctly for a given scenario. These
parameters include thresholds that control feature matching,
RANSAC parameters, and criteria to decide when to add new
factors to the graph or when to trigger a loop closing algorithm
to search for matches. If SLAM has to work “out of the box”
in arbitrary scenarios, methods for automatic tuning of the
involved parameters need to be considered.

IV. LONG-TERM AUTONOMY II: SCALABILITY

While modern SLAM algorithms have been successfully
demonstrated mostly in indoor building-scale environments,
in many application endeavors, robots must operate for an
extended period of time over larger areas. These applications
include ocean exploration for environmental monitoring, non-
stop cleaning robots in our ever changing cities, or large-scale
precision agriculture. For such applications the size of the
factor graph underlying SLAM can grow unbounded, due to
the continuous exploration of new places and the increasing
time of operation. In practice, the computational time and
memory footprint are bounded by the resources of the robot.
Therefore, it is important to design SLAM methods whose
computational and memory complexity remains bounded.

In the worst-case, successive linearization methods based
on direct linear solvers imply a memory consumption which
grows quadratically in the number of variables. When using
iterative linear solvers (e.g., the conjugate gradient [62])
the memory consumption grows linearly in the number of
variables. The situation is further complicated by the fact
that, when re-visiting a place multiple times, factor graph
optimization becomes less efficient as nodes and edges are
continuously added to the same spatial region, compromising
the sparsity structure of the graph.

In this section we review some of the current approaches
to control, or at least reduce, the growth of the size of the
problem and discuss open challenges.

Brief Survey. We focus on two ways to reduce the com-
plexity of factor graph optimization: (i) sparsification methods,
which trade off information loss for memory and computa-
tional efficiency, and (ii) out-of-core and multi-robot methods,
which split the computation among many robots/processors.

Node and edge sparsification: This family of methods
addresses scalability by reducing the number of nodes added
to the graph, or by pruning less “informative” nodes and
factors. Ila et al. [115] use an information-theoretic approach
to add only non-redundant nodes and highly-informative mea-
surements to the graph. Johannsson et al. [120], when possi-
bile, avoid adding new nodes to the graph by inducing new
constraints between existing nodes, such that the number of
variables grows only with size of the explored space and not
with the mapping duration. Kretzschmar et al. [141] propose
an information-based criterion for determining which nodes to
marginalize in pose graph optimization. Carlevaris-Bianco and
Eustice [28], and Mazuran et al. [170] introduce the Generic
Linear Constraint (GLC) factors and the Nonlinear Graph
Sparsification (NGS) method, respectively. These methods
operate on the Markov blanket of a marginalized node and compute a sparse approximation of the blanket. Huang et al. [107] sparsify the Hessian matrix (arising in the normal equations) by solving an $\ell_1$-regularized minimization problem.

Another line of work that allows reducing the number of parameters to be estimated over time is the continuous-time trajectory estimation. The first SLAM approach of this class was proposed by Bibby and Reid using cubic-splines to represent the continuous trajectory of the robot [12]. In their approach the nodes in the factor graph represented the control-points (knots) of the spline which were optimized in a sliding window fashion. Later, Furgale et al. [88] proposed the use of basis functions, particularly B-splines, to approximate the robot trajectory, within a batch-optimization formulation. Sliding-window B-spline formulations were also used in SLAM with rolling shutter cameras, with a landmark-based representation by Patron-Perez et al. [196] and with a semi-dense direct representation by Kim et al. [153]. More recently, Mueggler et al. [177] applied the continuous-time SLAM formulation to event-based cameras. Bosse et al. [21] extended the continuous 3D scan-matching formulation from [19] to a large-scale SLAM application. Later, Anderson et al. [4] and Dubé et al. [67] proposed more efficient implementations by using wavelets or sampling non-uniform knots over the trajectory, respectively. Tong et al. [243] changed the parametrization of the trajectory from basis curves to a Gaussian process representation, where nodes in the factor graph are actual robot poses and any other pose can be interpolated by computing the posterior mean at the given time. An expensive batch Gauss-Newton optimization is needed to solve for the states in this first proposal. Barfoot et al. [3] then proposed a Gaussian process with an exactly sparse inverse kernel that drastically reduces the computational time of the batch solution.

**Out-of-core (parallel) SLAM**: Parallel out-of-core algorithms for SLAM split the computation (and memory) load of factor graph optimization among multiple processors. The key idea is to divide the factor graph into different subgraphs and optimize the overall graph by alternating local optimization of each subgraph, with a global refinement. The corresponding approaches are often referred to as submapping algorithms, an idea that dates back to the initial attempts to tackle large-scale maps [18]. Ni et al. [187] and Zhao et al. [267] present submapping approaches for factor graph optimization, organizing the submaps in a binary tree structure. Grisetti et al. [98] propose a hierarchy of submaps: whenever an observation is acquired, the highest level of the hierarchy is modified and only the areas which are substantially affected are changed at lower levels. Some methods approximately decouple localization and mapping in two threads that run in parallel like Klein and Murray [135]. Other methods resort to solving different stages in parallel: inspired by [223], Strasdat et al. [235] take a two-stage approach and optimize first a local pose-features graph and then a pose-pose graph; Williams et al. [259] split factor graph optimization in a high-frequency filter and low-frequency smoother, which are periodically synchronized.

**Distributed multi robot SLAM**: One way of mapping a large-scale environment is to deploy multiple robots doing SLAM, and divide the scenario in smaller areas, each one mapped by a different robot. This approach has two main variants: the centralized one, where robots build submaps and transfer the local information to a central station that performs inference [65, 210], and the decentralized one, where there is no central data fusion and the agents leverage local communication to reach consensus on a common map. Nerurkar et al. [181] propose an algorithm for cooperative localization based on distributed conjugate gradient. Araguez et al. [5] investigate consensus-based approaches for map merging. Knuth and Barooah [137] estimate 3D poses using distributed gradient descent. In Lazaro et al. [151], robots exchange portions of their factor graphs, which are approximated in the form of condensed measurements to minimize communication. Cunningham et al. [54] use Gaussian elimination, and develop an approach, called DDF-SAM, in which each robot exchanges a Gaussian marginal over the separators (i.e., the variables shared by multiple robots). A recent survey on multi-robot SLAM approaches can be found in [216].

While Gaussian elimination has become a popular approach it has two major shortcomings. First, the marginals to be exchanged among the robots are dense, and the communication cost is quadratic in the number of separators. This motivated the use of sparsification techniques to reduce the communication cost [197]. The second reason is that Gaussian elimination is performed on a linearized version of the problem, hence approaches such as DDF-SAM [54] require good linearization points and complex bookkeeping to ensure consistency of the linearization points across the robots. An alternative approach to Gaussian elimination is the Gauss-Seidel approach of Choudhary et al. [47], which implies a communication burden which is linear in the number of separators.

**Open Problems.** Despite the amount of work to reduce complexity of factor graph optimization, the literature has large gaps on other aspects related to long-term operation.

**Map representation:** A fairly unexplored question is how to store the map during long-term operation. Even when memory is not a tight constraint, e.g. data is stored on the cloud, raw representations as point clouds or volumetric maps (see also Section V) are wasteful in terms of memory; similarly, storing feature descriptors for vision-based SLAM quickly becomes cumbersome. Some initial solutions have been recently proposed for localization against a compressed known map [163], and for memory-efficient dense reconstruction [156].

**Learning, forgetting, remembering:** A related open question for long-term mapping is how often to update the information contained in the map and how to decide when this information becomes outdated and can be discarded. When is it fine, if ever, to forget? In which case, what can be forgotten and what is essential to maintain? Can parts of the map be “off-loaded” and recalled when needed? While this is clearly task-dependent, no grounded answer to these questions has been proposed in the literature.

**Robust distributed mapping:** While approaches for outlier rejection have been proposed in the single robot case, the literature on multi robot SLAM barely deals with the problem of outliers. Dealing with spurious measurements is particularly challenging for two reasons. First, the robots might not share a common reference frame, making it harder to detect and
reject wrong loop closures. Second, in the distributed setup, the robots have to detect outliers from very partial and local information. An early attempt to tackle this issue is [84], in which robots actively verify location hypotheses using a rendezvous strategy before fusing information. Indelman et al. [177] propose a probabilistic approach to establish a common reference frame in the face of spurious measurements.

Resource-constrained platforms: Another relatively unexplored issue is how to adapt existing SLAM algorithms to the case in which the robotic platforms have severe computational constraints. This problem is of great importance when the size of the platform is scaled down, e.g., mobile phones, micro aerial vehicles, or robotic insects [261]. Many SLAM algorithms are too expensive to run on these platforms, and it would be desirable to have algorithms in which one can tune a “knob” that allows to gently trade off accuracy for computational cost. Similar issues arise in the multi-robot setting: how can we guarantee reliable operation for multi-robot teams when facing tight bandwidth constraints and communication dropout? The “version control” approach of Cieslewski et al. [49] is a first study in this direction.

V. REPRESENTATION I: METRIC MAP MODELS

This section discusses how to model geometry in SLAM. More formally, a metric representation (or metric map) is a symbolic structure that encodes the geometry of the environment. We claim that understanding how to choose a suitable metric representation for SLAM (and extending the set or representations currently used in robotics) will impact many research areas, including long-term navigation, physical interaction with the environment, and human-robot interaction.

Geometric modeling appears much simpler in the 2D case, with only two predominant paradigms: landmark-based maps and occupancy grid maps. The former models the environment as a sparse set of landmarks, the latter discretizes the environment in cells and assigns a probability of occupation to each cell. The problem of standardization of these representations in the 2D case has been tackled by the IEEE RAS Map Data Representation Working Group, which recently released a standard for 2D maps in robotics [113]; the standard defines the two main metric representations for planar environments (plus topological maps) in order to facilitate data exchange, benchmarking, and technology transfer.

The question of 3D geometry modeling is more delicate, and the understanding of how to efficiently model 3D geometry during mapping is in its infancy. In this section we review metric representations, taking a broad perspective across robotics, computer vision, computer aided design (CAD), and computer graphics. Our taxonomy draws inspiration from [80, 209, 221], and includes pointers to more recent work.

Landmark-based sparse representations. Most SLAM methods represent the scene as a set of sparse 3D landmarks corresponding to discriminative features in the environment (e.g., lines, corners) [179]; one example is shown in Fig. 4(left). These are commonly referred to as landmark-based or feature-based representations, and have been widespread in mobile robotics since early work on localization and mapping, and in computer vision in the context of Structure from Motion [2, 244]. A common assumption underlying these representations is that the landmarks are distinguishable, i.e., sensor data measure some geometric aspect of the landmark, but also provide a descriptor which establishes a (possibly uncertain) data association between each measurement and the corresponding landmark. Previous work also investigates different 3D landmark parameterizations, including global and local Cartesian models, and inverse depth parametrization [174]. While a large body of work focuses on the estimation of point features, the robotics literature includes extensions to more complex geometric landmarks, including lines, segments, or arcs [162].

Low-level raw dense representations. Contrary to landmark-based representations, dense representations attempt to provide high-resolution models of the 3D geometry; these models are more suitable for obstacle avoidance, or for visualization and rendering, see Fig. 4(right). Among dense models, raw representations describe the 3D geometry by means of a large unstructured set of points (i.e., point clouds) or polygons (i.e., polygon soup [222]). Point clouds have been widely used in robotics, in conjunction with stereo and RGB-D cameras, as well as 3D laser scanners [190]. These representations have recently gained popularity in monocular SLAM, in conjunction with the use of direct methods [118, 184, 203], which estimate the trajectory of the robot and a 3D model directly from the intensity values of all the image pixels. Slightly more complex representations are surfel maps, which encode the geometry as a set of disks [104, 257]. While these representations are visually pleasant, they are usually cumbersome as they require storing a large amount of data. Moreover, they give a low-level description of the geometry, neglecting, for instance, the topology of the obstacles.

Boundary and spatial-partitioning dense representations. These representations go beyond unstructured sets of low-level primitives (e.g., points) and attempt to explicitly represent surfaces (or boundaries) and volumes. These representations lend themselves better to tasks such as motion or footstep planning, obstacle avoidance, manipulation, and other physics-based reasoning, such as contact reasoning. Boundary representations (b-reps) define 3D objects in terms of their surface boundary. Particularly simple boundary representations are plane-based models, which have been used for mapping by Castle et al. [44] and Kaess [124, 162]. More general b-reps include curve-based representations (e.g., tensor product of NURBS or B-splines), surface mesh models (connected sets...
of polygons), and implicit surface representations. The latter specify the surface of a solid as the zero crossing of a function defined on \( \mathbb{R}^3 \) \cite{et al.}; examples of functions include radial-basis functions \cite{et al.}, signed-distance function \cite{et al.}, and truncated signed-distance function (TSDF) \cite{et al.}. TSDF are currently a popular representation for vision-based SLAM in robotics, attracting increasing attention after the seminal work \cite{et al.}. Mesh models have been also used in \cite{et al.} \cite{et al.}.

Spatial-partitioning representations define 3D objects as a collection of contiguous non-intersecting primitives. The most popular spatial-partitioning representation is the so-called spatial-occupancy enumeration, which decomposes the 3D space into identical cubes (voxels), arranged in a regular 3D grid. More efficient partitioning schemes include octree, Polygonal Map octree, and Binary Space-Partitioning tree \cite{et al.} \cite{et al.}. In robotics, octree representations have been used for 3D mapping \cite{et al.}, while commonly used occupancy grid maps \cite{et al.} can be considered as probabilistic variants of spatial-partitioning representations. In 3D environments without hanging obstacles, 2.5D elevation maps have been also used \cite{et al.}. Before moving to higher-level representations, let us better understand how sparse (feature-based) representations (and algorithms) compare to dense ones in visual SLAM.

**Which one is best: feature-based or direct methods?** Feature-based approaches are quite mature, with a long history of success \cite{et al.}. They allow to build accurate and robust SLAM systems with automatic relocation and loop closing \cite{et al.}. However, such systems depend on the availability of features in the environment, the reliance on detection and matching thresholds, and on the fact that most feature detectors are optimized for speed rather than precision. On the other hand, direct methods work with the raw pixel information and dense-direct methods exploit all the information in the image, even from areas where gradients are small; thus, they can outperform feature-based methods in scenes with poor texture, defocus, and motion blur \cite{et al.} \cite{et al.}. However, they require high computing power (GPUs) for real-time performance. Furthermore, how to jointly estimate dense structure and motion is still an open problem (currently they can be only be estimated subsequently to one another). To avoid the caveats of feature-based methods there are two alternatives. Semi-dense methods overcome the high-computation requirement of dense method by exploiting only pixels with strong gradients (i.e., edges) \cite{et al.} \cite{et al.}; semi-direct methods instead leverage both sparse features (such as corners or edges) and direct methods \cite{et al.} and are proven to be the most efficient \cite{et al.}; additionally, because they rely on sparse features, they allow joint estimation of structure and motion.

**High-level object-based representations.** While point clouds and boundary representations are currently dominating the landscape of dense mapping, we envision that higher-level representations, including objects and solid shapes, will play a key role in the future of SLAM. Early techniques to include object-based reasoning in SLAM are “SLAM++” from Salas-Moreno et al. \cite{et al.}, the work from Civera et al. \cite{et al.}, and Dame et al. \cite{et al.}. Solid representations explicitly encode the fact that real objects are three-dimensional rather than 1D (i.e., points), or 2D (surfaces). Modeling objects as solid shapes allows associating physical notions, such as volume and mass, to each object, which is definitely important for robots which have to interact the world. Luckily, existing literature from CAD and computer graphics paved the way towards these developments. In the following, we list few examples of solid representations that have not yet been used in a SLAM context:

- **Parameterized Primitive Instancing:** relies on the definition of families of objects (e.g., cylinder, sphere). For each family, one defines a set of parameters (e.g., radius, height), that uniquely identifies a member (or instance) of the family. This representation may be of interest for SLAM since it enables the use of extremely compact models, while still capturing many elements in man-made environments.

- **Sweep representations:** define a solid as the sweep of a 2D or 3D object along a trajectory through space. Typical sweeps representations include translation sweep (or extrusion) and rotation sweep. For instance, a cylinder can be represented as a translation sweep of a circle along an axis that is orthogonal to the plane of the circle. Sweeps of 2D cross-sections are known as generalized cylinders in computer vision \cite{et al.}, and they have been used in robotic grasping \cite{et al.}. This representation seems particularly suitable to reason on the occluded portions of the scene, by leveraging symmetries.

- **Constructive solid geometry:** defines complex solids by means of boolean operations between primitives \cite{et al.}. An object is stored as a tree in which the leaves are the primitives and the edges represent operations. This representation can model fairly complicated geometry and is extensively used in computer graphics.

We conclude this review by mentioning that other types of representations exist, including feature-based models in CAD \cite{et al.}, dictionary-based representations \cite{et al.}, affordance-based models \cite{et al.}, generative and procedural models \cite{et al.}, and scene graphs \cite{et al.}. In particular, dictionary-based representations, which define a solid as a combination of atoms in a dictionary, have been considered in robotics and computer vision, with dictionary learned from data \cite{et al.} or based on existing repositories of object models \cite{et al.} \cite{et al.}.

**Open Problems.** The following problems regarding metric representation for SLAM deserve a large amount of fundamental research, and are still vastly unexplored.

**High-level, expressive representations in SLAM:** While most of the robotics community is currently focusing on point clouds or TSDF to model 3D geometry, these representations have two main drawbacks. First, they are wasteful of memory. For instance, both representations use many parameters (i.e., points, voxels) to encode even a simple environment, such as an empty room (this issue can be partially mitigated by the so-called voxel hashing \cite{et al.}). Second, these representations do not provide any high-level understanding of the 3D geometry. For instance, consider the case in which the robot has to figure out if it is moving in a room or in a corridor. A point cloud does not provide readily usable information about the type of environment (i.e., room vs. corridor). On the other hand, more sophisticated models (e.g., parameterized primitive instancing) would provide easy ways to discern the two scenes (e.g., by looking at the parameters...
VI. REPRESENTATION II: SEMANTIC MAP MODELS

Semantic mapping consists in associating semantic concepts to geometric entities in a robot’s surroundings. Recently, the limitations of purely geometric maps have been recognized and this has spawned a significant and ongoing body of work in semantic mapping of environments, in order to enhance robot’s autonomy and robustness, facilitate more complex tasks (e.g. avoid muddy-road while driving), move from path-planning to task-planning, and enable advanced human-robot interaction [9 26 217]. These observations have led to different approaches for semantic mapping which vary in the numbers and types of semantic concepts and means of associating them with different parts of the environments. As an example, Pronobis and Jensfelt [206] label different rooms, while Pillai and Leonard [201] segment several known objects in the map. With the exception of few approaches, semantic parsing at the basic level was formulated as a classification problem, where simple mapping between the sensory data and semantic concepts has been considered.

Semantic vs. topological SLAM. As mentioned in Section I, topological mapping drops the metric information and only leverages place recognition to build a graph in which the nodes represent distinguishable “places”, while edges denote reachability among places. We note that topological mapping is radically different from semantic mapping. While the former requires recognizing a previously seen place (disregarding whether that place is a kitchen, a corridor, etc.), the latter is interested in classifying the place according to semantic labels. A comprehensive survey on vision-based topological SLAM is presented in Lowry et al. [160], and some of its challenges are discussed in Section III. In the rest of this section we focus on semantic mapping.

Semantic SLAM: Structure and detail of concepts. The unlimited number of, and relationships among, concepts for humans opens a more philosophical and task-driven decision about the level and organization of the semantic concepts. The detail and organization depend on the context of what, and where, the robot is supposed to perform a task, and they impact the complexity of the problem at different stages. A semantic representation is built by defining the following aspects:

• Level/Detail of semantic concepts: For a given robotic task, e.g. “going from room A to room B”, coarse categories (rooms, corridor, doors) would suffice for a successful performance, while for other tasks, e.g. “pick up a tea cup”, finer categories (table, tea cup, glass) are needed.
• Organization of semantic concepts: The semantic concepts are not exclusive. Even more, a single entity can have an unlimited number of properties or concepts. A chair can be “movable” and “sittable”; a dinner table can be “movable” and “unsittable”. While the chair and the table are pieces of furniture, they share the movable property but with different usability. Flat or hierarchical organizations, sharing or not some properties, have to be designed to handle this multiplicity of concepts.

Brief Survey. There are three main ways to attack semantic mapping, and assign semantic concepts to data.

SLAM helps Semantics: The first robotic researchers working on semantic mapping started by the straightforward approach of segmenting the metric map built by a classical SLAM system into semantic concepts. An early work was that of Mozos et al. [176], which builds a geometric map using a...
2D laser scan and then fuses the classified semantic places from each robot pose through an associative Markov network in an offline manner. Similarly, Lai et al. [148] build a 3D map from RGB-D sequences to then carry out an offline object classification. An online semantic mapping system was later proposed by Pronobis et al. [206], who combine three layers of reasoning (sensory, categorical, and place) to build a semantic map of the environment using laser and camera sensors. More recently, Cadena et al. [26] use motion estimation, and interconnect a coarse semantic segmentation with different object detectors to outperform the individual systems. Pillai and Leonard [201] use a monocular SLAM system to boost the performance in the task of object recognition in videos.

**Semantics helps SLAM:** Soon after the first semantic maps came out, another trend started by taking advantage of known semantic classes or objects. The idea is that if we can recognize objects or other elements in a map then we can use our prior knowledge about their geometry to improve the estimation of that map. First attempts were done in small scale by Castle et al. [44] and by Civera et al. [50] with a monocular SLAM with sparse features, and by Dame et al. [56] with a dense map representation. Taking advantage of RGB-D sensors, Salas-Moreno et al. [217] propose a SLAM system based on the detection of known objects in the environment.

**Joint SLAM and Semantics inference:** Researchers with expertise in both computer vision and robotics realized that they could perform monocular SLAM and map segmentation within a joint formulation. The online system of Flint et al. [79] presents a model that leverages the Manhattan world assumption to segment the map in the main planes in indoor scenes. Bao et al. [9] propose one of the first approaches to jointly estimate camera parameters, scene points and object labels using both geometric and semantic attributes in the scene. In their work, the authors demonstrate the improved object recognition performance and robustness, at the cost of a run-time of 20 minutes per image-pair, and the limited number of object categories makes the approach impractical for online robot operation. In the same line, Häne et al. [102] solve a more specialized class-dependent optimization problem in outdoors scenarios. Although still offline, Kundu et al. [147] reduce the complexity of the problem by a late fusion of the semantic segmentation and the metric map, a similar idea was proposed earlier by Sengupta et al. [219] using stereo cameras. It should be noted that [147] and [219] focus only on the mapping part and they do not refine the early computed poses in this late stage. Recently, a promising online system was proposed by Vineet et al. [251] using stereo cameras and a dense map representation.

**Open Problems.** The problem of including semantic information in SLAM is in its infancy, and, contrary to metric SLAM, it still lacks a cohesive formulation. Fig. 5 shows a construction site as a simple example where we can find the challenges discussed below.

**Consistent semantic-metric fusion:** Although some progress has been done in terms of temporal fusion of, for instance, per frame semantic evidence [219, 251], the problem of consistently fusing several sources of semantic information with metric information coming at different points in time is still open. Incorporating the confidence or uncertainty of the semantic categorization in the already well known factor graph formulation for the metric representation is a possible way to go for a joint semantic-metric inference framework.

**Semantic mapping is much more than a categorization problem:** The semantic concepts are evolving to more specialized information such as affordances and actionability of the entities in the map and the possible interactions among different active agents in the environment. How to represent these properties, and interrelationships, are questions to answer for high level human-robot interaction.

**Ignorance, awareness, and adaptation:** Given some prior knowledge, the robot should be able to reason about new concepts and their semantic representations, that is, it should be able to discover new objects or classes in the environment, learning new properties as result of active interaction with other robots and humans, and adapting the representations to slow and abrupt changes in the environment over time. For example, suppose that a wheeled-robot needs to classify whether a terrain is drivable or not, to inform its navigation system. If the robot finds some mud on a road, that was previously classified as drivable, the robot should learn a new class depending on the grade of difficulty of crossing the muddy region, or adjust its classifier if another vehicle stuck in the mud is perceived.

**Semantic-based reasoning:** As humans, the semantic representations allow us to compress and speed-up reasoning about the environment, while assessing accurate metric representations takes us some effort. Currently, this is not the case for robots. Robots can handle (colored) metric representation but they do not truly exploit the semantic concepts. Our robots

---

1. The term *affordances* refers to the set of possible actions on a given object/environment by a given agent [24], while the term *actionability* includes the expected utility of these actions.
2. Reasoning in the sense of localization and mapping. This is only a sub-area of the vast area of Knowledge Representation and Reasoning in the field of Artificial Intelligence that deals with solving complex problems, like having a dialogue in natural language or inferring a person’s mood.
are currently unable to effectively, and efficiently localize and continuously map using the semantic concepts (categories, relationships and properties) in the environment. For instance, when detecting a car, a robot should infer the presence of a planar ground under the car (even if occluded) and when the car moves the map update should only refine the hallucinated ground with the new sensor readings. Even more, the same update should change the global pose of the car as a whole in a single and efficient operation as opposed to update, for instance, every single voxel.

VII. NEW THEORETICAL TOOLS FOR SLAM

This section discusses recent progress towards establishing performance guarantees for SLAM algorithms, and elucidates open problems. The theoretical analysis is important for three main reasons. First, SLAM algorithms and implementations are often tested in few problem instances and it is hard to understand how the corresponding results generalize to new instances. Second, theoretical results shed light on the intrinsic properties of the problem, revealing aspects that may be counter-intuitive during empirical evaluation. Third, a true understanding of the structure of the problem allows pushing the algorithmic boundaries, enabling to extend the set of real-world SLAM instances that can be solved.

Early theoretical analysis of SLAM algorithms were based on the use of EKF; we refer the reader to [64, 255] for a comprehensive discussion, on consistency and observability of EKF SLAM. Here we focus on factor graph optimization approaches. Besides the practical advantages (accuracy, efficiency), factor graph optimization provides an elegant framework which is more amenable to analysis.

In the absence of priors, MAP estimation reduces to maximum likelihood estimation. Consequently, without priors, SLAM inherits all the properties of maximum likelihood estimators: the estimator in (4) is consistent, asymptotically Gaussian, asymptotically efficient, and invariant to transformations in the Euclidean space [171 Theorems 11-1,2]. Some of these properties are lost in presence of priors (e.g., the estimator is no longer invariant [171 page 193]).

In this context we are more interested in algorithmic properties: does a given algorithm converge to the MAP estimate? How can we improve or check convergence? What is the breakdown point in presence of spurious measurements?

Brief Survey. Most SLAM algorithms are based on iterative nonlinear optimization [63, 99, 125, 126, 192, 204]. SLAM is a nonconvex problem and iterative optimization can only guarantee local convergence. When an algorithm converges to a local minimum, it usually returns an estimate that is completely wrong and unsuitable for navigation (Fig. 6). State-of-the-art iterative solvers fail to converge to a global minimum of the cost for relatively small noise levels [122, 123].

Failure to converge in iterative methods has triggered efforts towards a deeper understanding of the SLAM problem. Huang and collaborators [110] pioneered this effort, with initial works discussing the nature of the nonconvexity in SLAM. Huang et al. [111] discuss the number of minima in small pose graph optimization problems. Knuth and Barooah [138] investigate the growth of the error in the absence of loop closures. Carlone [29] provides estimates of the basin of convergence for the Gauss-Newton method. Carlone and Censi [32] show that rotation estimation can be solved in closed form in 2D and show that the corresponding estimate is unique. The recent use of alternative maximum likelihood formulations (e.g., assuming Von Mises noise on rotations [34, 211]), has enabled even stronger results. Carlone and Dellaert [31, 66] show that under certain conditions (strong duality) that are often encountered in practice, the maximum likelihood estimate is unique and pose graph optimization can be solved globally, via (convex) semidefinite programming (SDP). A very recent overview on theoretical aspects of SLAM is given in [109].

As mentioned earlier, the theoretical analysis is sometimes the first step towards the design of better algorithms. Besides the dual SDP approach of [31, 66], other authors proposed convex relaxation to avoid convergence to local minima. These contributions include the work of Liu et al. [159] and Rosen et al. [211]. Another successful strategy to improve convergence consists in computing a suitable initialization for iterative nonlinear optimization. In this regard, the idea of solving for the rotations first and to use the resulting estimate to bootstrap nonlinear iteration has been demonstrated to be very effective in practice [20, 50, 122, 123]. Khosoussi et al. [130] leverage the (approximate) separability between translation and rotation to speed up optimization.

Recent theoretical results on the use of Lagrangian duality in SLAM also enabled the design of verification techniques: given a SLAM estimate these techniques are able to judge whether such estimate is optimal or not. Being able to ascertain the quality of a given SLAM solution is crucial to design failure detection and recovery strategies for safety-critical applications. The literature on verification techniques for SLAM is very recent: current approaches [31, 66] are able to perform verification by solving a sparse linear system and are guaranteed to provide a correct answer as long as strong duality holds (more on this point later).

We note that these results, proposed in a robotics context, provide a useful complement to related work in other communities, including localization in multi agent systems [148, 199, 202, 245, 254], structure from motion in computer vision [86, 95, 103, 168], and cryo-electron microscopy [224, 225].

Open Problems. Despite the unprecedented progress of the last years, several theoretical questions remain open.

Generality, guarantees, verification: The first question regards the generality of the available results. Most results on guaranteed global solutions and verification techniques have been proposed in the context of pose graph optimization. Can these results be generalized to arbitrary factor graphs? Moreover, most theoretical results assume the measurement noise to be isotropic or at least to be structured. Can we generalize existing results to arbitrary noise models?
Given estimate in presence of outliers remain open.

of verification techniques that can certify the correctness of a
global techniques that are resilient to outliers and the design
tools for the non-Gaussian noise case [212], the design of
the work on robust SLAM (Section III) and new modeling
result of this kind applies in the presence of outliers. Despite
provide strong guarantees for pose graph optimization, no
in the presence of spurious measurements. While recent results
insight in sensor design and active SLAM (Section VIII).

This theoretical investigation would also provide fundamental
this question would define the domain of applications in
structure, does strong duality hold?”. The capability to answer
the question “given a set of sensors (and the corresponding measurement noise statistics) and a factor graph
shows trajectory estimates for two simulated benchmarking problems, namely
sphere-a and torus, in which the robot travels on the surface of a sphere
and a torus. The top row reports the correct trajectory estimate, corresponding
to the global optimum of the optimization problem. The bottom row shows
incorrect trajectory estimates resulting from convergence to local minima.
Recent theoretical tools are enabling detection of wrong convergence episodes,
and are opening avenues for failure detection and recovery techniques.

Weak or Strong duality? The works [31, 36] show that when
strong duality holds SLAM can be solved globally; moreover, they provide empirical evidence that strong duality holds in
most problem instances encountered in practical applications.
The outstanding problem consists in establishing a priori
conditions under which strong duality holds. We would like
to answer the question “given a set of sensors (and the corresponding measurement noise statistics) and a factor graph
structure, does strong duality hold?”. The capability to answer
this question would define the domain of applications in
which we can compute (or verify) global solutions to SLAM.
This theoretical investigation would also provide fundamental
insights in sensor design and active SLAM (Section VII).

Resilience to outliers: The third question regards estimation
in the presence of spurious measurements. While recent results
provide strong guarantees for pose graph optimization, no
result of this kind applies in the presence of outliers. Despite
the work on robust SLAM (Section III) and new modeling
tools for the non-Gaussian noise case [212], the design of
global techniques that are resilient to outliers and the design of
verification techniques that can certify the correctness of a
given estimate in presence of outliers remain open.

VIII. ACTIVE SLAM

So far we described SLAM as an estimation problem that
is carried out passively by the robot, i.e. the robot performs
SLAM given the sensor data, but without acting deliberately to
collect it. In this section we discuss how to leverage a robot’s
motion to improve the mapping and localization results.

The problem of controlling robot’s motion in order to mini-
mize the uncertainty of its map representation and localization
is usually named active SLAM. This definition stems from the
well-known Bajcsy’s active perception [8] and Thrun’s robotic

Brief Survey. The first proposal and implementation of
an active SLAM algorithm can be traced back to Feder [77]
while the name was coined in [152]. However, active SLAM
has its roots in ideas from artificial intelligence and robotic
exploration that can be traced back to the early eighties
(c.f. [10]). Thrun in [239] concluded that solving the
exploration-exploitation dilemma, i.e., finding a balance be-
 tween visiting new places (exploration) and reducing the
uncertainty by re-visiting known areas (exploitation), provides
a more efficient alternative with respect to random exploration
or pure exploitation.

Active SLAM is a decision making problem and there are
several general frameworks for decision making that can be
used as backbone for exploration-exploitation decisions. One
of these frameworks is the Theory of Optimal Experimental
Design (TOED) [198] which, applied to active SLAM [41, 43],
allows selecting future robot action based on the predicted
map uncertainty. Information theoretic [154, 208] approaches
have been also applied to active SLAM [40, 232]; in this
case decision making is usually guided by the notion of
information gain. Control theoretic approaches for active SLAM
include the use of Model Predictive Control [152, 153]. A
different body of works formulates active SLAM under the
formalism of Partially Observably Markov Decision Process
(POMDP) [123], which in general is known to be computa-
tionally intractable; approximate but tractable solutions for
active SLAM include Bayesian Optimization [169] or efficient
Gaussian beliefs propagation [195], among others.

A popular framework for active SLAM consists of selecting
the best future action among a finite set of alternatives. This
family of active SLAM algorithms proceeds in three main
steps [15, 35]: 1) The robot identifies possible locations to
explore or exploit, i.e. vantage locations, in its current estimate
of the map; 2) The robot computes the utility of visiting each
vantage point and selects the action with the highest utility;
and 3) The robot carries out the selected action and decides
if it is necessary to continue or to terminate the task. In the
following, we discuss each point in details.

Selecting vantage points: Ideally, a robot executing an active
SLAM algorithm should evaluate every possible action in
the robot and map space, but the computational complexity
of the evaluation grows exponentially with the search space
which proves to be computationally intractable in real applica-
tions [24, 169]. In practice, a small subset of locations in the
map is selected, using techniques such as frontier-based explo-
ration [127, 262]. Recent works [250] and [116] have proposed
approaches for continuous-space planning under uncertainty
that can be used for active SLAM; currently these approaches
can only guarantee convergence to locally optimal policies.
Another recent continuous-domain avenue for active SLAM
algorithms is the use of potential fields. Some examples are
[249], which uses convolution techniques to compute entropy
and select the robot’s actions, and [222], which resort to the
solution of a boundary value problem.

Computing the utility of an action: Ideally, to compute the
utility of a given action the robot should reason about the
volution of the posterior over the robot pose and the map,
taking into account future (controllable) actions and future
active SLAM is only a means to achieve an intended goal. Additionally, having a stopping criteria is a necessity because at some point it is provable that more information would lead not only to a diminishing return effect but also, in case of contradictory information, to an unrecoverable state (e.g. several wrong loop closures). Uncertainty metrics from TOED, which are task oriented, seem promising as stopping criteria, compared to information-theoretic metrics which are difficult to compare across systems [39].

**Performance guarantees:** Another important avenue is to look for mathematical guarantees for active SLAM and for near-optimal policies. Since solving the problem exactly is intractable, it is desirable to have approximation algorithms with clear performance bounds. Examples of this kind of effort is the use of submodularity [93] in the related field of active sensors placement.

IX. NEW FRONTIERS: SENSORS AND LEARNING

The development of new sensors and the use of new computational tools have often been key drivers for SLAM. Section [IX-A] reviews unconventional and new sensors, as well as the challenges and opportunities they pose in the context of SLAM. Section [IX-B] discusses the role of (deep) learning as an important frontier for SLAM, analyzing the possible ways in which this tool is going to improve, affect, or even restate, the SLAM problem.

A. New and Unconventional Sensors for SLAM

Besides the development of new algorithms, progress in SLAM (and mobile robotics in general) has often been triggered by the availability of novel sensors. For instance, the introduction of 2D laser range finders enabled the creation of very robust SLAM systems, while 3D lidars have been a main thrust behind recent applications, such as autonomous cars. In the last ten years, a large amount of research has been devoted to vision sensors, with successful applications in augmented reality and vision-based navigation.

Sensing in robotics has been mostly dominated by lidars and conventional vision sensors. However, there are many alternative sensors that can be leveraged for SLAM, such as depth, light-field, and event-based cameras, which are now becoming a commodity hardware, as well as magnetic, olfaction, and thermal sensors.

**Brief Survey.** We review the most relevant new sensors and their applications for SLAM, postponing a discussion on open problems to the end of this section.

**Range cameras:** Light-emitting depth cameras are not new sensors, but they became commodity hardware in 2010 with the advent the Microsoft Kinect game console. They operate according to different principles, such as structured light, time of flight, interferometry, or coded aperture. Structure-light cameras work by triangulation; thus, their accuracy is limited by the distance between the cameras and the pattern projector (structured light). By contrast, the accuracy of Time-of-Flight (ToF) cameras only depends on the time-of-flight measurement device; thus, they provide the highest range accuracy (sub millimeter at several meters). ToF cameras became commercially available for civil applications around the year 2000 but only began to be used in mobile robotics in 2004 [256]. While the first generation of ToF and structured-light cameras was characterized by low signal-to-noise ratio and high price, they soon became popular for video-game applications, which contributed to making them affordable for robots.
and improving their accuracy. Since range cameras carry their own light source, they also work in dark and untextured scenes, which enabled the achievement of remarkable SLAM results [133].

**Light-field cameras:** Contrary to standard cameras, which only record the light intensity hitting each pixel, a light-field camera (also known as plenoptic camera), records both the intensity and the direction of light rays [185]. One popular type of light-field camera uses an array of micro lenses placed in front of a conventional image sensor to sense intensity, color, and directional information. Because of the manufacturing cost, commercially available light-field cameras still have relatively low resolution (< 1MP), which is being overcome by current technological effort. Light-field cameras offer several advantages over standard cameras, such as depth estimation, noise reduction [57], video stabilization [227], isolation of distractors [58], and specularity removal [119]. Their optics also offers wide aperture and wide depth of field compared with conventional cameras [14].

**Event-based cameras:** Contrarily to standard frame-based cameras, which send entire images at fixed frame rates, event-based cameras, such as the Dynamic Vision Sensor (DVS) [156] or the Asynchronous Time-based Image Sensor (ATIS) [205], only send the local pixel-level changes caused by movement in a scene at the time they occur.

They have five key advantages compared to conventional frame-based cameras: a temporal latency of 1ms, an update rate of up to 1MHz, a dynamic range of up to 140dB (vs 60-70dB of standard cameras), a power consumption of 20mW (vs 1.5W of standard cameras), and very low bandwidth and storage requirements (because only intensity changes are transmitted). These properties enable the design of a new class of SLAM algorithms that can operate in scenes characterized by high-speed motion [89] and high-dynamic range [132, 207], where standard cameras fail. However, since the output is composed of a sequence of asynchronous events, traditional frame-based computer-vision algorithms are not applicable. This requires a paradigm shift from the traditional computer vision approaches developed over the last fifty years. Event-based real-time localization and mapping algorithms have recently been proposed [132, 207]. The design goal of such algorithms is that each incoming event can asynchronously change the estimated state of the system, thus, preserving the event-based nature of the sensor and allowing the design of microsecond-latency control algorithms [178].

**Open Problems.** The main bottleneck of active range cameras is the maximum range and interference with other external light sources (such as sun light); however, these weaknesses can be improved by emitting more light power.

Light-field cameras have been rarely used in SLAM because they are usually thought to increase the amount of data produced and require more computational power. However, recent studies have shown that they are particularly suitable for SLAM applications because they allow formulating the motion estimation problem as a linear optimization and can provide more accurate motion estimates if designed properly [65].

Event-based cameras are revolutionary image sensors that overcome the limitations of standard cameras in scenes characterized by high dynamic range and high speed motion. Open problems concern a full characterization of the sensor noise and sensor non-idealities: event-based cameras have a complicated analog circuitry, with nonlinearities and biases that can change the sensitivity of the pixels, and other dynamic properties, which make the events susceptible to noise. Since a single event does not carry enough information for state estimation and because an event camera generate on average 100,000 events a second, it can become intractable to do SLAM at the discrete times of the single events due to the rapidly growing size of the state space. Using a continuous-time framework [12], the estimated trajectory can be approximated by a smooth curve in the space of rigid-body motions using basis functions (e.g., cubic splines), and optimized according to the observed events [172]. While the temporal resolution is very high, the spatial resolution of event-based cameras is relatively low (QVGA), which is being overcome by current technological effort [155]. Newly developed event sensors overcome some of the original limitations: an ATIS sensor sends the magnitude of the pixel-level brightness; a DAVIS sensor [155] can output both frames and events (this is made possible by embedding a standard frame-based sensor and a DVS into the same pixel array). This will allow tracking features and motion in the blind time between frames [144].

We conclude this section with some general observations on the use of novel sensing modalities for SLAM.

**Other sensors:** Most SLAM research has been devoted to range and vision sensors. However, humans or animals are able to improve their sensing capabilities by using tactile, olfaction, sound, magnetic, and thermal stimuli. For instance, tactile cues are used by blind people or rodents for haptic exploration of objects, olfaction is used by bees to find their way home, magnetic fields are used by homing pigeons for navigation, sound is used by bats for obstacle detection and navigation, while some snakes can see infrared radiation emitted by hot objects. Unfortunately, these alternative sensors have not been considered in the same depth as range and vision sensors to perform SLAM. Haptic SLAM can be used for tactile exploration of an object or of a scene [237, 263]. Olfaction sensors can be used to localize gas or other odor sources [167]. Although ultrasound-based localization was predominant in early mobile robots, their use has rapidly declined with the advent of cheap optical range sensors. Nevertheless, animals, such as bats, can navigate at very high speeds using only echo localization. Thermal sensors offer important cues at night and in adverse weather conditions [165]. Local anomalies of the ambient magnetic field, present in many indoor environments, offer an excellent cue for localization [248]. Finally, pre-existing wireless networks, such as WiFi, can be used to improve robot navigation without any prior knowledge of the location of the antennas [78].

**Which sensor is best for SLAM?** A question that naturally arises is: what will be the next sensor technology to drive future long-term SLAM research? Clearly, the performance of a given algorithm-sensor pair for SLAM depends on the sensor and algorithm parameters, and on the environment [228]. A complete treatment of how to choose algorithms and sensors to achieve the best performance has not been found
yet. A preliminary study by Censi et al. [45], has shown that the performance for a given task also depends on the power available for sensing. It also suggests that the optimal sensing architecture may have multiple sensors that might be instantaneously switched on and off according to the required performance level or measure the same phenomenon through different physical principles for robustness [68].

B. Deep Learning

It would be remiss of a paper that purports to consider future directions in SLAM not to make mention of deep learning. Its impact in computer vision has been transformational, and, at the time of writing this article, it is already making significant inroads into traditional robotics, including SLAM.

Researchers have already shown that it is possible to learn a deep neural network to regress the inter-frame pose between two images acquired from a moving robot directly from the original image pair [52], effectively replacing the standard geometry of visual odometry. Likewise it is possible to localize the 6DoF of a camera with regression forest [247] and with deep convolutional neural network [129], and to estimate the depth of a scene (in effect, the map) from a single view solely as a function of the input image [271 70 158].

This does not, in our view, mean that traditional SLAM is dead, and it is too soon to say whether these methods are simply curiosities that show what can be done in principle, but which will not replace traditional, well-understood methods, or if they will completely take over.

Open Problems. We highlight here a set of future directions for SLAM where we believe machine learning and more specifically deep learning will be influential, or where the SLAM application will throw up challenges for deep learning.

Perceptual tool: It is clear that some perceptual problems that have been beyond the reach of off-the-shelf computer vision algorithms can now be addressed. For example, object recognition for the imagenet classes [213] can now, to an extent, be treated as a black box that works well from the perspective of the roboticist or SLAM researcher. Likewise semantic labeling of pixels in a variety of scene types reaches performance levels of around 80% accuracy or more [72].

We have already commented extensively on a move towards more semantically meaningful maps for SLAM systems, and these black-box tools will hasten that. But there is more at stake: deep networks show more promise for connecting raw sensor data to understanding, or connecting raw sensor data to actions, than anything that has preceded them.

Practical deployment: Successes in deep learning have mostly revolved around lengthy training times on supercomputers and inference on special-purpose GPU hardware for a one-off result. A challenge for SLAM researchers (or indeed anyone who wants to embed the impressive results in their system) is how to provide sufficient computing power in an embedded system. Do we simply wait for the technology to catch up, or do we investigate smaller, cheaper networks that can produce “good enough” results, and consider the impact of sensing over an extended period?

Online and life-long learning: An even greater and important challenge is that of online learning and adaptation, that will be essential to any future long-term SLAM system. SLAM systems typically operate in an open-world with continuous observation, where new objects and scenes can be encountered. But to date deep networks are usually trained on closed-world scenarios with, say, a fixed number of object classes. A significant challenge is to harness the power of deep networks in a one-shot or zero-shot scenario (i.e. one or even zero training examples of a new class) to enable life-long learning for a continuously moving, continuously observing SLAM system.

Similarly, existing networks tend to be trained on a vast corpus of labelled data, yet it cannot always be guaranteed that a suitable dataset exists or is practical to label for the supervised training. One area where some progress has recently been made is that of single-view depth estimation: Garg et al. [90] have recently shown how a deep network for single-view depth estimation can be trained simply by observing a large corpus of stereo pairs, without the need to observe or calculate depth explicitly. It remains to be seen if similar methods can be developed for tasks such as semantic scene labelling.

Bootstrapping: Prior information about a scene has increasingly been shown to provide a significant boost to SLAM systems. Examples in the literature to date include known objects [56, 217] or prior knowledge about the expected structure in the scene, like smoothness as in DTAM [184], Manhattan constraints as in [79], or even the expected relationships between objects [9]. It is clear that deep learning is capable of distilling such prior knowledge for specific tasks such as estimating scene labels or scene depths. How best to extract and use this information is a significant open problem. It is more pertinent in SLAM than in some other fields because in SLAM we have solid grasp of the mathematics of the scene geometry – the question then is how to fuse this well-understood geometry with the outputs of a deep network. One particular challenge that must be solved is to characterize the uncertainty of estimates derived from a deep network.

SLAM offers a challenging context for exploring potential connections between deep learning architectures and recursive state estimation in large-scale graphical models. For example, Krishan et al. [142] have recently proposed Deep Kalman Filters; perhaps it might one day be possible to create an end-to-end SLAM system using a deep architecture, without explicit feature modeling, data association, etc.

X. Conclusion

The problem of simultaneous localization and mapping has seen great progress over the last 30 years. Along the way, several important questions have been answered, while many new and interesting questions have been raised, with the development of new applications, new sensors, and new computational tools.

Revisiting the question “is SLAM necessary?”, we believe the answer depends on the application, but quite often the answer is a resounding yes. SLAM and related techniques, such
as visual-inertial odometry, are being increasingly deployed in a variety of real-world settings, from self-driving cars to mobile devices. SLAM techniques will be increasingly relied upon to provide reliable metric positioning in situations where infrastructure-based solutions such as GPS are unavailable or do not provide sufficient accuracy. One can envision cloud-based location-as-a-service capabilities coming online, and maps becoming commoditized, due to the value of positioning information for mobile devices and agents.

In some applications, such as self-driving cars, precision localization is often performed by matching current sensor data to a high definition map of the environment that is created in advance. If the a priori map is accurate, then online SLAM is not required. Operations in highly dynamic environments, however, will require dynamic online map updates to deal with construction or major changes to road infrastructure. The distributed updating and maintenance of visual maps created by large fleets of autonomous vehicles is a compelling area for future work.

One may even devise examples in which SLAM is unnecessary altogether and can be replaced by other techniques, e.g., visual servoing for local control and stabilization, or “teach and repeat” to perform repetitive navigation tasks. A more general way to choose the most appropriate SLAM system is to think about SLAM as a mechanism to compute a sufficient statistic that summarizes all past observations of the robot, and in this sense, which information to retain in this compressed representation is deeply task-dependent.

As to the familiar question “is SLAM solved?”, in this position paper we argue that, as we enter the robust-perception age, the question cannot be answered without specifying a robot/environment/performance combination. For many applications and environments, numerous major challenges and important questions remain open. To achieve truly robust perception and navigation for long-lived autonomous robots, more research in SLAM is needed. As an academic endeavor with important real-world implications, SLAM is not solved.

The unsolved questions involve four main aspects: robust performance, high-level understanding, resource awareness, and task-driven inference. From the perspective of robustness, the design of fail-safe, self-tuning SLAM systems is a formidable challenge with many aspects being largely unexplored. For long-term autonomy, techniques to construct and maintain large-scale time-varying maps, as well as policies that define when to remember, update, or forget information, still need a large amount of fundamental research; similar problems arise, at a different scale, in severely resource-constrained robotic systems.

Another fundamental question regards the design of metric and semantic representations for the environment. Despite the fact that the interaction with the environment is paramount for most applications of robotics, modern SLAM systems are not able to provide a tightly-coupled high-level understanding of the geometry and the semantic of the surrounding world; the design of such representations must be task-driven and currently a tractable framework to link task to optimal representations is lacking. Developing such a framework will bring together the robotics and computer vision communities.

Besides discussing many accomplishments and future challenges for the SLAM community, we also examined opportunities connected to the use of novel sensors, new tools (e.g., convex relaxations and duality theory, or deep learning), and the role of active sensing. SLAM still constitutes an indispensable backbone for most robotics applications and despite the amazing progress over the past decades, existing SLAM systems are far from providing insightful, actionable, and compact models of the environment, comparable to the ones effortlessly created and used by humans.

ACKNOWLEDGMENT

We would like to thank all the contributors and members of the Google Plus community, especially Liam Paul, Ankur Handa, Shane Griffith, Hilario Tomé, Andrea Censi, and Raul Mur Artal, for their inputs towards the open problems in SLAM. We are also thankful to all the speakers of the RSS workshop for their inputs towards the discussion of the open problems in SLAM. We are also indebted to Guoquan (Paul) Huang and Udo Frese for the discussions during the preparation of this document, and Guillermo Gallego and Jeff Delmerico for their early comments on this document.

REFERENCES


