Multitask Learning of Signaling and Regulatory Networks with Application to Studying Human Response to Flu

The MIT Faculty has made this article openly available. Please share how this access benefits you. Your story matters.

<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>As Published</td>
<td><a href="http://dx.doi.org/10.1371/journal.pcbi.1003943">http://dx.doi.org/10.1371/journal.pcbi.1003943</a></td>
</tr>
<tr>
<td>Publisher</td>
<td>Public Library of Science</td>
</tr>
<tr>
<td>Version</td>
<td>Final published version</td>
</tr>
<tr>
<td>Accessed</td>
<td>Tue Dec 18 22:20:47 EST 2018</td>
</tr>
<tr>
<td>Citable Link</td>
<td><a href="http://hdl.handle.net/1721.1/92474">http://hdl.handle.net/1721.1/92474</a></td>
</tr>
<tr>
<td>Terms of Use</td>
<td>Creative Commons Attribution</td>
</tr>
<tr>
<td>Detailed Terms</td>
<td><a href="http://creativecommons.org/licenses/by/4.0/">http://creativecommons.org/licenses/by/4.0/</a></td>
</tr>
</tbody>
</table>
Multitask Learning of Signaling and Regulatory Networks with Application to Studying Human Response to Flu

Siddhartha Jain¹, Anthony Gitter²,3*, Ziv Bar-Joseph⁴*

¹ Computer Science Department, Carnegie Mellon University, Pittsburgh, Pennsylvania, United States of America, ² Microsoft Research, Cambridge, Massachusetts, United States of America, ³ Department of Biological Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts, United States of America, ⁴ Lane Center for Computational Biology and Machine Learning Department, Carnegie Mellon University, Pittsburgh, Pennsylvania, United States of America

Abstract

Reconstructing regulatory and signaling response networks is one of the major goals of systems biology. While several successful methods have been suggested for this task, some integrating large and diverse datasets, these methods have so far been applied to reconstruct a single response network at a time, even when studying and modeling related conditions. To improve network reconstruction we developed MT-SDREM, a multi-task learning method which jointly models networks for several related conditions. In MT-SDREM, parameters are jointly constrained across the networks while still allowing for condition-specific pathways and regulation. We formulate the multi-task learning problem and discuss methods for optimizing the joint target function. We applied MT-SDREM to reconstruct dynamic human response networks for three flu strains: H1N1, H5N1 and H3N2. Our multi-task learning method was able to identify known and novel factors and genes, improving upon prior methods that model each condition independently. The MT-SDREM networks were also better at identifying proteins whose removal affects viral load indicating that joint learning can still lead to accurate, condition-specific, networks. Supporting website with MT-SDREM implementation: http://sb.cs.cmu.edu/mtsdrem

Introduction

The relative ease of high-throughput data collection enables profiling a system of interest in many ways with complementary assays, at different times, and under various perturbations to compare and contrast the outcomes. The resulting computational challenge is to develop analysis strategies that maximally leverage these related experiments to improve our ability to reconstruct biologically accurate models.

Even when applied to study the same condition, different types of high-throughput data (e.g., functional genetic screens and gene expression) often times implicate largely disjoint groups of genes or proteins because each experiment highlights different facets of the biological processes and networks involved [1]. Consequently, there has been extensive research to develop techniques for integrating one or more types of condition-specific high-throughput data with general purpose physical interaction networks, such as protein-protein interactions (PPIs), to reconstruct signaling and regulatory networks [1–3] (see [4] for a review). These methods discern how the genes identified in complementary types of experiments relate to one another in a network context and propose new condition-specific regulators that are not directly observed to be relevant in the original data but form connections in the inferred networks.

Due to the dynamic nature of biological systems, especially those controlling stimulus response and development, it is critical to observe genome-wide changes over time [5]. As reviewed in [5], there are now computational approaches that exploit the unique structure in temporal datasets (e.g., time series gene expression) to model dynamic processes and reverse engineer regulatory networks [6,7]. Recent algorithms integrate temporal data and PPI networks to improve signaling pathway prediction by capitalizing on the dynamic information [8,9].

Despite advances in modeling the temporal dimension and different types of assays per condition, there has been considerably less progress made for datasets that contain multiple related perturbations or stimuli. Typically each condition is analyzed in isolation, and a post-processing comparison of the independent models is required to draw conclusions across conditions [9,10]. Individual models of related conditions are required to appreciate the unique aspects of each, but building these models independently ignores that the observations may be generated from structurally similar networks. As an example, consider the case of host gene expression following virus infection. Although different
environmental stress response genes [14]), and additional exam-
of stresses activate a large common set of genes (termed the
expression response [11,12], and other elements of innate immune
receptors (TLRs), which recognize a large number of RNA viruses
affect a similar core set of host proteins. These include Toll-like
viruses do not have identical effects on the host (hence the gene
expression patterns are unique to each virus), they also commonly
affect a similar core set of host proteins. These include Toll-like
receptors (TLRs), which recognize a large number of RNA viruses
and activate a downstream pathway that leads to common expression
response [11,12], and other elements of innate immune
response pathways [13]. Similarly, in yeast several different types
of stresses activate a large common set of genes (termed the
environmental stress response genes [14]), and additional examples
abound in other species.

When modeling such responses, one may be able to take
advantage of these commonalities without sacrificing the ability
to reconstruct individual models for each response. This type of
machine learning is termed Multi-task learning [15] and usually
applies to cases where one learns models for different problems
that share information and/or parameters. A key advantage of
such framework is the ability to utilize additional data from related
conditions when reconstructing networks for a specific response.
This is especially important when reconstructing biological
response networks from high-throughput data because the number of
parameters to fit is very large relative to the number of samples.
In addition, extensive data from a well-characterized condition
may be able to compensate for sparse data in a similar, less-
understood condition.

Multi-task learning has been applied to other problems in the
biological domain including classification [16], genome-wide
association studies [17,18], protein structure [19], and pairwise
protein-protein interaction prediction [20,21]. Multi-commodity
flow [22] and iterative applications of a prize-collecting Steiner
forest algorithm [23] have been used to simultaneously reconstruct
related response or disease networks, but these methods do not
employ multi-task learning. In addition, these previous approaches
operate on static data and cannot account for the dynamic
behaviors that are crucial for understanding many types of
stimulus responses.

Here we present the Multi-Task Signaling and Dynamic
Regulatory Events Miner (MT-SDREM), which uses multi-task
learning to reconstruct response pathways and temporal regulatory
networks. MT-SDREM is equipped to capitalize on the many
dimensions in complex systems biology datasets by integrating
different types of experimental data in each condition, explaining
the time-dependent elements of a response (as observed in gene
expression data), and constraining the inferred networks to be
similar for related conditions or perturbations. Like its single-
condition predecessor [8], MT-SDREM iterates between finding
pathways that connect the upstream proteins that directly interact
with an external stimulus (called source proteins) and the
downstream transcription factors (TFs) that regulate the response
and learning dynamic regulatory networks activated by these TFs.
The learning process involves the simultaneous reconstruction of
several such networks. While a different network is learned for
each condition, the joint learning framework allows sharing and/or
constraining parameters across the different networks which
helps overcome the overfitting problem that is often an issue when
reconstructing biological networks.

We demonstrate how MT-SDREM can be used to gain insights
into a clinically-relevant problem: characterizing the human
response to viral infection. In particular, we explore the differences
between mild, seasonal strains of the influenza A virus, which are
typically H1N1 or H3N2 strains [24], and lethal, pandemic strains
such as the H1N1 1918 Spanish flu and highly pathogenic avian
H5N1 strains. Influenza A strains are subtyped and named by
their hemagglutinin (HA) and neuraminidase (NA) proteins.
Although there are presently 18 known HA subtypes and 11 NA
subtypes [25] only a fraction of these have have infected humans.
Previous studies have characterized some of the differences
between seasonal and pathogenic strains. Seasonal H1N1 and
H3N2 and highly pathogenic H5N1 influenza strains infect
macrophages at similar rates, but H3N2 and H5N1 causes
apoptosis more rapidly than H1N1 [24]. H1N1 also lead to
weaker induction of MAPK signaling pathways than the H3N2
and H5N1 strains [24]. Genomic comparisons of human and
avian influenza strains identified 52 species-associated positions
that could potentially enable an avian strain to cross over to
humans if mutated [26]. Influenza strains also vary in the cells and
tissues they infect [27,28] with highly-virulent strains causing more
widespread inflammation, including in the alveoli [27]. Highly
pathogenic strains have been shown to induce a stronger
inflammatory cytokine response than seasonal influenza [28]
and the host inflammatory response is often more deadly during
infection than the pathogen itself [29]. However, much remains
unknown about the host factors that are required for viral
replication or to mount cellular defenses.

We study three strains of the influenza A virus — seasonal H1N1,
seasonal H3N2, and highly pathogenic avian H5N1 — to explain
how common host proteins react to the viral infection in a similar
manner despite the differences in the temporal transcriptional
programs that are activated. The MT-SDREM networks identified
many known regulators of influenza response and also suggested
putative novel regulators. Because the responses are jointly modeled
using the multi-task setting, MT-SDREM is able to correctly
recover TFs that are important drivers of the immune response that
are missed when each viral strain is analyzed independently [10]
and by previous methods for combining gene expression data across
experiments. In addition, MT-SDREM networks are more
predictive of host genes that are required for viral replication, a
potentially clinically-relevant phenotype [29], than corresponding
independent models or gene prioritization algorithms.

Results and Discussion

MT-SDREM simultaneously infers signaling and dynamic
regulatory networks for multiple related conditions. It extends
the SDREM tool [8,10] which discovers signaling pathways by orienting edges in protein interaction networks. To demonstrate the performance of such multi-task network learning we looked at data from 3 different flu viruses: H1N1, H3N2, and H5N1.

For each of these viruses we obtained time series gene expression measurements of cells infected with the virus. For H1N1 the data is from [30] and contains 10 time points. For H5N1, we obtained data from [31] with 5 time points, and the H3N2 data from [32] had 6 time points. In addition, for each of these viruses we obtained a set of sources (host proteins interacting with the virus proteins) from mass spec experiments. Data for H1N1 is from [33] and literature [30,34] and contains 200 human proteins that were experimentally determined to interact with H1N1 proteins. Data for H3N2 is from [33] and consists of 153 host proteins and source data for H5N1 is from [33] and literature [34–39] and consists of 41 sources.

MT-SDREM reconstructed networks

Joint signaling network. Figure 1 presents the joint signaling network learned for the three conditions (Methods). The top layer (nodes colored in red) are sources for at least one of the conditions. The bottom layer (nodes colored green) are TFs identified in at least one of the conditions, and the middle layer (blue nodes) are signaling proteins linking the sources and TFs in the networks. We colored each node with multiple colors depending on the condition for which it was identified as a top network protein (Methods). The lightest shade for each color represent nodes from the H1N1 reconstructed network, the darkest is from the H5N1 network and the middle shade is for the H3N2 network.

While sources (red shades) are provided as inputs, all other nodes were automatically identified by MT-SDREM. Several of the proteins identified in multiple networks, both as intermediate and as TFs are well known immune response regulators. For example, we identify a pathway from UBE2I (a source for both H1N1 and H3N2) to SUMO1 (signaling protein identified for all strains). SUMO activates E1 and transfers it to conjugating enzyme E2. Then UBE2I interacts with and transfers SUMO to a target viral protein. Indeed, it has been recently shown that SUMO interacts with the key flu protein, NS1, via UBE2I [40]. In addition, TRAF6, part of the TRAF (TNF receptor associated factor) family of proteins, is identified as an important protein for H5N1. Pro-inflammatory cytokines including TNF-α are known to be hyper-induced in H5N1 infected macrophages [41].

We also identify several TFs as common amongst the 3 conditions. SMAD4 is present in all 3 conditions. The SMAD family of TFs is part of the TGFβ pathway which is responsible for regulating macrophage activation and proliferation of T cells [12]. STAT1 and JUN, both key immune response regulators, are also identified in all 3 conditions. We also identify NRG3C1 which produces the GR protein that is known to inhibit T and B cells as well as suppressing phagocyte function [42] (this could be a viral strategy to reduce the effects of immune response). Interestingly, we identify the AKT1 gene in all 3 conditions, part of the PI3K/AKT pathway, which has recently been shown to be activated by the influenza A virus’s NS1 protein [43]. We also identify the PPARG TF which has been linked to immune response by regulation of immune and inflammation related genes [44]. Other TFs belonging to the AP-1 TF complex are also identified for various conditions – ATF2 for H1N1 and H5N1, and FOSL2 for H1N1 and H3N2. NFκB1 and RELA, both part of the NF-κB complex are identified for H1N1 and H5N1 respectively.

Regulatory networks. In addition to the signaling parts of the networks, MT-SDREM also reconstructs dynamic regulatory networks for each of the different flu strains. We show the regulatory network inferred for H1N1 in Figure 2. For space reasons not all TFs presented in Figure 1 are shown for the model in Figure 2, though all TFs that are associated with H1N1 are used by the model. Full list of TF assignments to paths in the regulatory networks is available on the Supporting Website. Corresponding networks for H3N2 and H5N1 are presented in Supplementary Results in S1 Text. Several of the TFs identified as controlling the first splits in both the H1N1 and H3N2 networks belong to the IRF family of TFs, known to regulate interferons, which play an important role in viral immune response [12]. TFs belonging to the FOS, ATF, and JUN families appear in both the H1N1 and H5N1 networks. These TFs are part of the AP-1 TF complex (which is known to regulate gene expression in response to a variety of stimuli including cytokines, and viral infections [45]). We also identify the SMAD family of TFs to play a part in all 3 networks. The STAT family of TFs is found to play a role in all 3 conditions. This family of TFs is part of the JAK-STAT signaling pathway. This is a class of pathways responsible for activating transcription in response to extracellular signals from messengers such as interferons, interleukins, growth factors, etc. [46,47].

In addition to analyzing the TFs identified we performed an enrichment analysis using the Gene Ontology (GO) terms associated with each path in the reconstructed regulatory networks. All p-values that we give below are after correcting for multiple hypothesis testing.

In the H1N1 regulatory network, the gene cluster correspond-
Several proteins that are only predicted for H5N1 response are known to have important roles in H5N1 infection. Knockdown of DDX39B, also known as UAP56, decreased H5N1 viral titre nearly 10 fold in infected cells [49]. MAPK8 (JNK) was strongly induced in H5N1 (and H3N2) infection, but not H1N1 infection [24]. NUP98 recruits the H5N1 protein NS2 to the nucleoli, and disrupting this interaction impedes viral propagation [38]. Mice with wild type MX1 were protected against infection by a highly lethal H5N1 strain relative to mice with defective MX1 [50]. H5N1-derived NS1 stimulates the ERK pathway, increasing cell viability and promoting infection [51]. Through interactions with viral NS1 and another host factor, IVNS1ABP (NS1-BP) can counteract this NS1-induced ERK phosphorylation [51].

Comparison of MT-SDREM with prior work
To test the advantages of multi-task learning we compared MT-SDREM with previous methods that can be used to analyze expression and interaction data. Since we are not aware of prior
Figure 2. H1N1 Regulatory network. Each path represents a set of genes with a similar expression profile. Split nodes are colored green and are annotated with the TFs that are predicted to regulate genes in the paths going out of the split at the time point associated with the split. The blue TFs are up-regulated at that split time point while the red TFs are down-regulated. The black TFs are not differentially expressed at the split point. Note that several of the TFs included in this latter group are likely post-transcriptionally regulated.
doi:10.1371/journal.pcbi.1003943.g002
methods that utilize multi-task learning in biological network reconstruction we first looked at the differences between applying MT-SDREM and applying SDREM separately to each of the three flu datasets. We have also compared MT-SDREM\'s results to a baseline joint ranking of differentially expressed (DE) genes from different experiments in a single analysis. This approach is similar to several previous studies that perform follow up analysis using such joint sets [52].

Since the \( \text{ground truth} \) (complete underlying networks for each condition) is obviously unknown, we used three different types of complementary information for these comparisons. First, we examined the set of TFs identified by each of these methods and determined their relevance to the condition being studied. Next, we used the Gene Ontology (GO) to test the differences in the identified functional categories between the different analysis methods. Expression experiments and RNA interference (RNAi) screens have revealed a multitude of host pathways and processes that are involved in viral host response including MAPK signaling, apoptosis, trafficking, mRNA export, splicing, and proteolysis [30,53,54]. A statistical meta-analysis implicates nearly 3000 host genes [55] in these pathways. Although many processes as a whole are relevant to influenza response, not all genes participating in those processes necessarily are important. Therefore we focused our TF and GO evaluation on immune processes, which were shown to compose a critical component of the host response that kills infected cells, protects uninfected cells, combats viral components, and promotes inflammation [56]. Finally, we used a set of RNAi experiments that were performed for H1N1 and H5N1 to test the ability of these different methods to identify key disease related proteins. In these experiments proteins are knocked down one at a time and the impact on viral load is measured. A protein affecting viral load is likely participating in the host response and so methods that can identify such proteins more accurately are in better agreement with the observed response. The RNAi data for H1N1 was obtained from [30,53,54,57,58] resulting in a total of 980 screen hits, 925 of which were present in our initial interaction network (which contained 16671 genes, Methods). 32 screen hits for H5N1 were obtained from [57], all of which are present in our interaction network.

Comparison of identified TFs

In Table 1 we present the overall and pairwise overlap of the inferred TFs for the 3 conditions (extracted by same mechanism as in SDREM [8,10]) for MT-SDREM and compare it to when SDREM is run independently on the 3 conditions (I-SDREM). Note that the pairwise intersections shown are \textit{in addition} to the overall intersection between all of the 3 conditions.

The shared TFs identified by MT-SDREM among all 3 conditions that are missed by I-SDREM include several that are known to be immune response related. In particular, CEBPA is known to be responsible for regulating a large variety of cell functions including immune and inflammatory response [59]. MT-SDREM also identifies SMAD4 in all three conditions. SMAD family proteins are part of the TGF\(\beta\) pathway as mentioned above. MT-SDREM also identifies RB1 which has been implicated in viral immune response [60]. JUN which is part of the AP-1 TF complex, and PPARG an important TF regulating immune response mentioned above. In contrast, I-SDREM does not identify any TF in the intersection that MT-SDREM does not.

In addition, we also find several immune response related TFs in the pairwise overlaps for MT-SDREM that we do not see for I-SDREM. For the overlap between H1N1 and H3N2, MT-SDREM identifies IRF1/3/5 which are known to regulate interferons and thus important for immune response. For the overlap between H1N1 and H5N1, MT-SDREM finds the the STAT3 gene which is part of the JAK-STAT signaling pathway and ATF2, part of the AP-1 TF complex.

For the pairwise intersection of H1N2 and H3N2, I-SDREM identifies NR3C1 as a TF while MT-SDREM only selects it as an intermediate (signaling) protein. It also identifies another member of the SMAD family (SMAD3 whereas MT-SDREM identifies SMAD4). For H5N2 and H3N1 it identifies AHR whose activation inhibits inflammation [61] and RELA in the intersection of H1N1 and H5N1, which as part of the NF-\(\kappa\)B complex.

We also compared MT-SDREM to the popular TF prediction tool oPossum [62]. Our primary goal when comparing MT-SDREM with oPossum is to highlight the fact that using network information in the multi-task learning framework is useful. The input to oPossum is a list of genes identified by the experiment(s) and using this list it attempts to find overrepresented TF-binding sites. To select a common gene list from all three experiments we ranked the genes for each condition according to their differential expression and then merged the 3 rankings using the Kemeny-Young method [63]. Similar to the number of genes used by MT-SDREM we used the top 3000 in the joint ranking as input to oPossum. In Table 2 we present the comparison. Note that since we used oPossum as the tool for the comparison of MT-SDREM with other methods for integrating data from several conditions, the results shown for Table 2 are different from the intersection results of Table 1. Here, for the MT-SDREM rankings we used the \textit{sum of} \% path flow going through each gene across the 3 networks to rank TFs (Methods). The oPossum TFs are ranked according to their \textit{Z-score}.

While oPossum is able to identify a few relevant TFs, for most of the TFs identified by oPossum, we could not find significant roles in immune response regulation for them. In contrast, several of the shared MT-SDREM TFs that are not identified by oPossum are known to play major roles in immune response as discussed above. These include STAT1/3, JUN/ATF2, CEBPA/B which regulate a large number of immune response genes, RB1 which has been implicated in viral immune response networks [60], PPARG, and SMAD. MT-SDREM also uniquely identifies IRF1 which plays a major role in viral immune response by regulating interferons. oPossum was able to identify only two relevant TFs that were not found by MT-SDREM. These are ZEB1 which regulates the IL2 interleukin, part of the immune response system and AHR, part of the ANTR-AHR complex. See also Tables S13–S15 in S1 Text for condition-specific comparisons using oPossum.

We also tried to compare MT-SDREM with the Inferelator method [6] but following email discussions with the authors of that method determined that such comparison is not feasible since Inferelator requires expression data for a large number of conditions while we only had time series response for three types of infections.

GO enrichment comparisons

To compare the GO enrichment of shared genes/proteins we examined the top 500 genes in the combined MT-SDREM network (ranked using the same sum of \% of path flow going through genes across the 3 networks as we did for the oPossum comparison) with the top 500 genes from the combined ranking of the differentially expressed (DE) genes from each condition (combined using the Kemeny-Young method as explained before). We used FuncAssociate [64,65] to compute standard GO enrichment for the genes. We found \textit{3} categories, only 2 of which were immune response related for which the p-value for DE genes was \( \leq 0.001 \) but which were not present in the MT-SDREM list or if present, their p-value was < 0.01. The categories are listed in Table 4. However, for the vice versa comparison, we found a large
Table 1. TF comparison for I-SDREM and MT-SDREM.

<table>
<thead>
<tr>
<th></th>
<th>H1N1 &amp; H3N2 &amp; H5N1</th>
<th>H1N1 &amp; H3N2</th>
<th>H3N2 &amp; H5N1</th>
<th>H1N1 &amp; H5N1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>I</td>
<td>MT</td>
<td>I</td>
<td>MT</td>
</tr>
<tr>
<td>AR</td>
<td>AR</td>
<td>IRF1</td>
<td>IRF1</td>
<td></td>
</tr>
<tr>
<td>BRCA1</td>
<td>BRCA1</td>
<td>IRF3</td>
<td>IRF3</td>
<td></td>
</tr>
<tr>
<td>ESR1</td>
<td>ESR1</td>
<td>FOSL2</td>
<td>FOSL2</td>
<td></td>
</tr>
<tr>
<td>STAT1</td>
<td>STAT1</td>
<td>CEBPA</td>
<td>IRF5†</td>
<td></td>
</tr>
<tr>
<td>CEBPA†</td>
<td>NR3C1†</td>
<td>TFAP2A†</td>
<td></td>
<td></td>
</tr>
<tr>
<td>EP300†</td>
<td>SMAD3‡</td>
<td>SOX9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>JUN†</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>PPARG†</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>RB1†</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SMAD4†</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SOX9†</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>TP53†</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

TFs predicted to regulate two or all three response networks. Each set of conditions is divided to two columns with the first column containing TFs at the intersection of the SDREM output for the conditions and the second the MT-SDREM results for these conditions. TFs identified by MT-SDREM but not SDREM have a † next to them and vice versa have a ◊ next to them. Note that TFs listed for the pairwise overlap are in addition to the ones listed for the overall overlap. Thus JUN in the I-SDREM column of H3N2 & H5N1 is not highlighted since it was identified by MT-SDREM for all three conditions.

doi:10.1371/journal.pcbi.1003943.t001
Table 2. TF comparison for oPossum and MT-SDREM.

<table>
<thead>
<tr>
<th>oPossum TF</th>
<th>MT-SDREM</th>
</tr>
</thead>
<tbody>
<tr>
<td>MZF1_1–4</td>
<td>EP300</td>
</tr>
<tr>
<td>SPI</td>
<td>TP53</td>
</tr>
<tr>
<td>ZNF354C</td>
<td>BRCA1</td>
</tr>
<tr>
<td>MZF1_5–13</td>
<td>JUN+</td>
</tr>
<tr>
<td>NFYA</td>
<td>ESR1</td>
</tr>
<tr>
<td>ZEB1+</td>
<td>AR</td>
</tr>
<tr>
<td>MIZF</td>
<td>RB1+</td>
</tr>
<tr>
<td>ROAZ</td>
<td>SMAD4+</td>
</tr>
<tr>
<td>GABPA</td>
<td>STAT1+</td>
</tr>
<tr>
<td>TEAD1</td>
<td>CEBPA+</td>
</tr>
<tr>
<td>TLX1-NFIC</td>
<td>PPARG+</td>
</tr>
<tr>
<td>SPIB</td>
<td>STAT3+</td>
</tr>
<tr>
<td>Hand1-Tcfe2a</td>
<td>SMAD3+</td>
</tr>
<tr>
<td>ARNT-AHR+</td>
<td>HIF1A</td>
</tr>
<tr>
<td>ELF5</td>
<td>RELA+</td>
</tr>
<tr>
<td>MYC-MAX</td>
<td>MYC</td>
</tr>
<tr>
<td>TP53</td>
<td>ATF2+</td>
</tr>
<tr>
<td>ELK1</td>
<td>CEBPB+</td>
</tr>
<tr>
<td>REL+</td>
<td>SOX9</td>
</tr>
<tr>
<td>AR</td>
<td>IRF1+</td>
</tr>
</tbody>
</table>

oPossum and MT-SDREM comparison. Immune response related TFs have a * next to them. oPossum TFs are ranked according to their Z-score. MT-SDREM TFs are ranked according to the path flow measure as described in the main text and Supplementary Methods in S1 Text. doi:10.1371/journal.pcbi.1003943.t002

number of categories for which the MT-SDREM p-value was ≤ 0.001 but which were either not enriched for in the DE genes list (most common outcome) or if present, their p-value was ≤ 0.01. A subset of the immune response related categories are listed in Table 3. Note that we find significant enrichment for a very varied set of immune response processes including T cell activation, cytokine production, activation of immune response, etc. as well as categories related to viral genome expression and positive regulation of viral process. The DE genes list is only enriched for negative regulation of viral process and viral genome replication. The complete set of the categories is in S45 Table.

To further compare methods that are based on joint expression analysis to those that are based on joint network learning we looked at the GO enrichment for the top 50 TFs identified by MT-SDREM and oPossum. The top 50 TFs for MT-SDREM are ranked using the joint ranking based on path flow for the 3 conditions as done for the GO comparison above. We used the TF Z-score provided by oPossum to rank TFs for oPossum. We again used FuncAssociate [64,65] to compute standard GO enrichment for the TFs. We obtained only one immune-response related category (interleukin related) for which the p-value for the oPossum TF set was ≤ 0.001 while being ≥ 0.01 for MT-SDREM (presented in Table 6). However we obtained 270 categories in total for which the MT-SDREM p-value was ≤ 0.001 but the p-value for oPossum was ≥ 0.01, a large number of which were immune response related. Due to space constraints, only a subset of these are presented in Table 5. These include ‘positive regulation of immune response’, ‘viral process’, and ‘cytokine-mediated signaling pathway’. The complete list of categories is in S46 Table. See also Tables S14–S25 in S1 Text for several additional comparisons of MT-SDREM and other methods using GO enrichment data.

RNAi screen hits

Using the screen hit data for H1N1 and H5N1 we compared the performance of MT-SDREM, I-SDREM and Endeavour [66,67]. Endeavour is a gene prioritization algorithm which uses a set of seed genes (the sources) to rank genes based on several types of evidence including gene expression, interaction networks derived from various sources, text mining, sequence similarity, and functional annotations. It combines the individual rankings to create a global ranking for all genes. For the MT-SDREM and I-

Table 3. GO categories enriched in MT-SDREM that are not enriched as significantly in Differentially Expressed (DE) genes.

<table>
<thead>
<tr>
<th>GO Category</th>
<th>MT-SDREM p-value</th>
<th>DE genes p-value</th>
<th>GO Category Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>GO:0002218</td>
<td>0.001</td>
<td>NA</td>
<td>activation of innate immune response</td>
</tr>
<tr>
<td>GO:0002684</td>
<td>0.001</td>
<td>NA</td>
<td>positive regulation of immune system process</td>
</tr>
<tr>
<td>GO:0002429</td>
<td>0.001</td>
<td>NA</td>
<td>immune response-activating cell surface receptor signaling pathway</td>
</tr>
<tr>
<td>GO:0046328</td>
<td>0.001</td>
<td>NA</td>
<td>regulation of JNK cascade</td>
</tr>
<tr>
<td>GO:0001816</td>
<td>0.001</td>
<td>NA</td>
<td>cytokine production</td>
</tr>
<tr>
<td>GO:0001959</td>
<td>0.001</td>
<td>NA</td>
<td>regulation of cytokine-mediated signaling pathway</td>
</tr>
<tr>
<td>GO:0042113</td>
<td>0.001</td>
<td>NA</td>
<td>B cell activation</td>
</tr>
<tr>
<td>GO:002110</td>
<td>0.001</td>
<td>NA</td>
<td>T cell activation</td>
</tr>
<tr>
<td>GO:0043923</td>
<td>0.001</td>
<td>NA</td>
<td>positive regulation by host of viral transcription</td>
</tr>
<tr>
<td>GO:0019080</td>
<td>0.001</td>
<td>NA</td>
<td>viral genome expression</td>
</tr>
<tr>
<td>GO:0048524</td>
<td>0.001</td>
<td>NA</td>
<td>positive regulation of viral process</td>
</tr>
<tr>
<td>GO:0007259</td>
<td>0.001</td>
<td>NA</td>
<td>JAK-STAT cascade</td>
</tr>
<tr>
<td>GO:0002573</td>
<td>0.001</td>
<td>NA</td>
<td>myeloid leukemia differentiation</td>
</tr>
</tbody>
</table>

GO comparison between the Differentially Expressed gene list and MT-SDREM gene list for top 500 genes. The enrichment was performed using the FuncAssociate tool [64]. Only categories with MT-SDREM adjusted p-value of ≤ 0.001 and DE genes p-value of ≥ 0.01 are presented. If a p-value for DE genes is NA, that means that that category was not enriched for in the DE genes list. Only select immune response related categories are presented. The full list of the 114 immune-related categories is available in S45 Table on the Supporting Website. doi:10.1371/journal.pcbi.1003943.t003
SDREM results we ranked proteins based on the total number of paths weighted by their score going through them. See Supplementary Methods in S1 Text for details. For Endavour, we configured it to use only BioGRID and HPRD as data sources as those are the only sources we use to construct our PPI network. The expression data is not used by Endavour. We gave the source proteins as the seed genes to Endavour. We further compared these three methods with a baseline method that is condition-independent: ranking nodes by their weighted degree in the PPI network. The results are presented in Figure 3. For H1N1, the top 100 genes in the Endavour ranking include only 20 screen hits (p-value = 4.9E-7). For I-SDREM the number increases to 35 (p-value = 2.0E-19) whereas both I-SDREM and MT-SDREM obtain the highest number of proteins in the overlap 39 (p-value = 1.7E-23). The baseline comparison where we rank by their weighted degree has an overlap of 30 genes (p-value = 9.4E-15). For H5N1, the top 100 genes for Endavour and for ranking by degree include only 5 screen hits (p-value = 1.2E-6) whereas both I-SDREM and MT-SDREM have an overlap of 9 screen hits (p-value = 1.7E-13). See also S1 Text for comparison of RNAi screen hits using GSEA.

We also compared MT-SDREM, I-SDREM with GeneMania [68,69] and concluded that MT-SDREM greatly improves upon the GeneMania results. See Supplementary Results in S1 Text for details.

Conclusions and future work

We developed MT-SDREM a multi-task learning framework that simultaneously reconstructs signaling and dynamic regulatory networks across related conditions. Given the small number of condition-specific samples that are often available (i.e. time series expression data and host-pathogen interaction data) sharing parameters across related conditions allows the reconstruction of more accurate networks while still retaining the ability to explain condition-specific signaling and regulation.

We applied MT-SDREM to reconstruct networks for 3 related influenza A virus infections – H1N1, H3N2, and H5N1. The resulting signaling and regulatory networks were able to identify several known and novel regulators of immune and viral response. Many of these were shared between all conditions including PPARG, FOS, ATF, and JUN. Similarly, we identify key signaling proteins, some shared by all conditions while others are unique to one or two of the conditions. Specifically, we identified the signaling protein SUMO1 as part of pathway from UBE2I for all 3 conditions. This agrees with recent findings that UBE2I interacts with SUMO1 to degrade influenza A’s virus, NS1 which is present in all three strains [70]. We also identified the AKT1 gene, part of the PI3K/AKT pathway that is activated by NS1 in all conditions.

MT-SDREM is the first method to jointly reconstruct such dynamic networks. Comparing MT-SDREM with methods that have been suggested to integrate gene expression data or with methods reconstruct such networks independently for each condition highlighted the advantages of multi-task network learning. MT-SDREM outperformed previous methods in identifying a set of TFs controlling immune response, a set of functionally relevant proteins and a set of proteins whose knockdown affects viral loads.

While MT-SDREM can successfully utilize experiments from similar conditions to reconstruct signaling and regulatory networks, there are still issues we would like to improve in future work. One direction we intend to explore is extending MT-SDREM to allow time based (as opposed to global) sharing of TFs across conditions so that splits representing the same time will be more likely to share TFs compared to other splits. We would also like to improve on the models by using additional types of data, including epigenetic data which can help improve the priors for TF binding at specific time points by making them a function of the epigenetic code.

Table 4. GO categories enriched in DE genes that are not enriched as significantly in MT-SDREM.

<table>
<thead>
<tr>
<th>GO Category</th>
<th>DE p-value</th>
<th>MT-SDREM p-value</th>
<th>GO Category Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>GO:0045071</td>
<td>0.001</td>
<td>NA</td>
<td>negative regulation of viral genome replication</td>
</tr>
<tr>
<td>GO:0048525</td>
<td>0.001</td>
<td>0.019</td>
<td>negative regulation of viral process</td>
</tr>
</tbody>
</table>

GO comparison between the joint DE gene list and the joint MT-SDREM for the top 500 genes. The enrichment was performed using the FuncAssociate tool [64]. Only categories with DE genes adjusted p-value of ≤0.001 and MT-SDREM genes p-value of ≥0.01 are presented. If a p-value for MT-SDREM is NA, that means that the category was not enriched for in the MT-SDREM list. All immune response related categories are presented.

Table 5. GO categories enriched in MT-SDREM TFs that are not enriched as significantly in oPossum TFs.

<table>
<thead>
<tr>
<th>GO Category</th>
<th>MT-SDREM p-value</th>
<th>oPossum p-value</th>
<th>GO Category Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>GO:0009607</td>
<td>0.001</td>
<td>NA</td>
<td>response to biotic stimulus</td>
</tr>
<tr>
<td>GO:0045089</td>
<td>0.001</td>
<td>0.02</td>
<td>positive regulation of innate immune response</td>
</tr>
<tr>
<td>GO:0071357</td>
<td>0.001</td>
<td>NA</td>
<td>cellular response to type I interferon</td>
</tr>
<tr>
<td>GO:0090048</td>
<td>0.001</td>
<td>NA</td>
<td>modulation by virus of host morphology or physiology</td>
</tr>
<tr>
<td>GO:0016032</td>
<td>0.001</td>
<td>NA</td>
<td>viral process</td>
</tr>
<tr>
<td>GO:0019221</td>
<td>0.001</td>
<td>NA</td>
<td>cytokine-mediated signaling pathway</td>
</tr>
<tr>
<td>GO:0032481</td>
<td>0.001</td>
<td>NA</td>
<td>positive regulation of type I interferon production</td>
</tr>
<tr>
<td>GO:0046332</td>
<td>0.001</td>
<td>NA</td>
<td>SMAD binding</td>
</tr>
</tbody>
</table>

GO comparison between the joint oPossum TF list and the joint MT-SDREM TF list for the top 50 TFs. The comparison was performed using the FuncAssociate tool [64]. A subset of the categories for which the MT-SDREM p-value is <0.001 and that of the oPossum list is ≥0.01 or which are not enriched for the oPossum list (represented by NA as the p-value) and which are immune response related are presented. Note that only a subset of the 40 immune-related categories are presented.

The rest of the categories are available in S46 Table on the Supporting Website.

doi:10.1371/journal.pcbi.1003943.t004

doi:10.1371/journal.pcbi.1003943.t005

doi:10.1371/journal.pcbi.1003943.t005
Materials and Methods

MT-SDREM simultaneously investigates and infers regulatory networks and signaling pathways for several biologically related conditions. For this, it uses both condition-specific gene expression and interaction data and general interaction data. We first discuss the input data that the method utilizes and then present the modeling and learning frameworks.

Input Data

We use $C$ to denote the set of conditions that are jointly modeled by MT-SDREM. Below we list the datasets used by MT-SDREM.

1. **Condition-specific: Time series gene expression data** for each of the conditions that are modeled by MT-SDREM.
2. **Condition-specific: Sources $S_c$** - the set of sources or host proteins which are known experimentally to interact with the pathogen/treatment applied when studying condition $c$.
3. **Condition-specific (optional): Screen hits** A list of proteins for each condition whose removal is known to phenotypically impact the response of the cells in that condition.
4. **General and/or condition-specific: TF-gene binding data**: A list of potential TF-gene interactions with an optional probabilistic prior/likelihood for the interaction. If data is available for the specific condition/cell type being studied these can be used, otherwise general data can be used as well. We denote by $\pi_{tg}$ the interaction prior for TF $t$ binding with gene $g$.
5. **General: Protein interaction network**: A list of protein-protein interactions which may be directed or undirected. The method can also use information regarding the confidence in each interaction. We denote such confidence in edge $e$ by $\pi_e$ and by $E$ the set of all edges.

**Protein-protein and protein-DNA interactions.** We obtained a list of protein-protein interactions from BIOGRID [71] and HPRD [72]. We also use Post-translational Modification Annotations from the HPRD dataset. General Protein-DNA

---

**Table 6.** GO categories enriched in oPossum TFs that are not enriched as significantly in MT-SDREM TFs.

<table>
<thead>
<tr>
<th>GO Category</th>
<th>oPossum p-value</th>
<th>MT-SDREM p-value</th>
<th>GO Category Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>GO:0045084</td>
<td>0.001</td>
<td>NA</td>
<td>positive regulation of interleukin-12 biosynthetic process</td>
</tr>
</tbody>
</table>

GO comparison between the joint oPossum TF list and the joint MT-SDREM TF list for the top 50 TFs. The comparison was performed using the FuncAssociate tool [64]. Categories for which the oPossum list p-value is $<0.001$ and that of the MT-SDREM list is $>0.01$ or which are not enriched for the MT-SDREM list (represented by NA as the p-value) and which are immune response related are presented. Note that all immune related categories are presented.

doi:10.1371/journal.pcbi.1003943.t006

---

**Figure 3.** Screen hits overlap for top 100 ranked genes for both H1N1 and H5N1. 925 H1N1 and 32 H5N1 screen hit proteins were present in our network.

doi:10.1371/journal.pcbi.1003943.g003
interactions are from [73] were processed as described in [74]. The top 100 threshold was used for both the interaction network and when analyzing the temporal expression data. As the TF binding predictions are not cell type-specific and as the H1N1 data was aggregated from multiple cell types, we assigned these predictions a relatively low score of 0.5 in the interaction network.

For the PPI network, a probability for every PPI edge was obtained by combining the various types of experimental evidence (Affinity-capture, Yeast 2-Hybrid). See Supplemental Methods in S1 Text for details. The PPI network we construct has 16,671 nodes and 228,159 edges. For 58,322 of these edges we have direction information from the database (most of those edges are TF-gene binding interactions and for the rest, the direction information primarily comes from phosphorylation studies).

**Condition-specific data.** We obtained time series gene expression data for each of the 3 viruses under consideration - H1N1 [30], H3N2 [32], and H5N1 [31] with 10, 6, and 5 time points respectively. The expression data was generated using whole genome microarray. To reduce the level of noise in the gene expression data, for every condition, we only used the top 3000 most differentially expressed genes in the time series dataset for that condition as input to MT-SDREM (see Supplementary Methods in S1 Text for details on how the genes were selected).

We collected the sources (human proteins experimentally determined to interact with the 3 viruses’ proteins) from VirHostNet [33]. There are 200 sources for H1N1, 153 for H3N2, and 41 for H5N1. In addition, we included TLR3, TLR7, TLR8, RIG-I and NLRP3 [75–77] – proteins that either detect influenza viral RNA or influenza infection via other means – as sources for H1N1 and H5N1.

**SDREM.** MT-SDREM extends the Signaling and Dynamic Regulatory Events Miner (SDREM) which has so far only been applied to reconstruct response networks for a single condition at a time [8]. Prior to discussing the multi-task learning procedures we first briefly discuss the SDREM method. SDREM is an iterative procedure that combines regulatory and signaling network reconstruction to model response pathways. For the regulatory part, SDREM uses time series gene expression data with protein-DNA interaction data to identify bifurcation events in a time series (places where the expression of previously co-expressed set of genes diverges – see Figure 2), and the transcription factors (TFs) controlling these split events. While some TFs are transcriptionally activated, others are only activated post-translationally via signaling networks. To explain these TFs, the second part of SDREM links sources (host proteins that directly interact with the virus/treatment) to the TFs determined to regulate the regulatory network. This part of SDREM uses protein-protein interaction (PPI) and protein modification data to infer such pathways – while imposing the constraint that the direction of PPI in the inferred pathways is consistent. These two parts (regulatory and signaling reconstruction) iterate a fixed number of times until the final network is obtained. See [8] for complete details.

**Application of multi-task learning to the inference of signaling and regulatory networks.** As mentioned above, we can run SDREM individually on the expression data for different infections to infer regulatory and signaling cascades for each of these conditions. However, several shared attributes can be jointly learned for these conditions and given the scarcity of data compared to the number of variables (very few time points for each expression experiment with thousands of genes in each model) such an approach can improve the accuracy of the reconstructed networks for each condition. Specifically, the direction of (the originally undirected) PPIs is likely to be similar for all conditions since several pathways are likely used by multiple conditions. Similarly, TFs that are active in response to one virus are more likely to be active in response to other viruses as well. MT-SDREM defines an optimization function that captures these expected similarities while still allowing for a condition-specific response component.

**The multi-task learning objective function.** The objective function commonly used for multi-task learning combines two related goals: First, similar to standard machine learning applications (for example, classification) it tries to minimize the loss (i.e. error) for each task while at the same time regularizing the parameters used by each task to avoid overfitting. Second, it further regularizes the parameters across tasks so that the final parameters are similar. A typical objective function is the following [78]

\[
\arg\min_{w_1,...,w_C} \left\{ \sum_{i=1}^{C} \left( L(y_i, f(w_i^T x_i)) + \lambda_1 ||w_i||_p \right) + \lambda_2 \sum_{i=1}^{C} \sum_{l=1}^{C} ||w_i - w_l||_F \right\} + \frac{1}{2} \lambda_1 \sum_{i=1}^{C} \sum_{l=1}^{C} ||w_i||_F
\]

where \( C \) is the number of tasks, \( L \) is the loss function, \( f \) is a function of the dot product of the task-specific weight vector and the data for the task, and \( p \) is the \( L_p \) norm for the regularization. The part in the left curly braces, \( T_1 \) is the task specific part of the objective function while the part in the right curly braces, \( T_2 \) is the regularization across tasks.

**Multi-task objective for MT-SDREM.** In MT-SDREM, the loss minimizing part, \( T_1 \), is achieved by the regulatory network learning procedure which learns parameters for a IOHMM that uses a logistic regression classifier to compute transition probabilities (Supplementary Methods in S1 Text). The logistic regression classifier is regularized using Lasso to reduce the number of active TFs inferred for each split. Thus in terms of the multi-task objective, \( y_j \) corresponds to the prediction regarding a gene trajectory at any split and \( x_i \) is the TF-gene binding information. \( w_i \) is the set of logistic regression weights learned for each split. Note that the TF-gene binding information \( x_i \) is not specific to each split but is the same for the entire times series.

In addition to expression data, we use signaling network information to infer TFs that are reachable from the infection sources. Such TFs are more likely to explain how the infecting agents affects gene expression and so their weights are increased in our framework. To find such TFs we need to orient the undirected edges and determine a weight for the paths leading to these TFs from sources. These two procedures (edge orientation and TF re-weighting) are shared across tasks and both affect the TF priors used by the logistic regression function. Thus for MT-SDREM, the objective function is:

\[
\arg\min_{w_1,...,w_C} \left\{ L(y_i, f(\phi(w_i^T B)^T x_i)) + \lambda_1 ||w_i||_p \right\} - \rho(B^1,...,B^C)
\]

where \( B \) is the weight matrix learned for TFs for all tasks in the signaling network and \( B^k \) are the weights determined for task \( k \). \( \rho \) is the similarity function used to constrain parameters across tasks which is described below (hence the negative sign in front of it as we are minimizing the objective but we want to maximize the similarity).
An important difference between the standard multi-task learning framework and our method is that while we regularize the within task parameters \((w_i)\), the between task parameters \((B)\) are not explicitly regularized. The reason is that the \(B\)’s are already constrained by the input protein interaction network and so are inherently bounded. See Supplementary Methods in S1 Text for details on the specific terms used in the multi-task learning objective.

Given \(B\), the above equation can be optimized by fitting parameters to the IOHMM and logistic regression function as was previously done in [79]. See Supplement Methods in S1 Text for details.

**Between task regularization.** Next we discuss how we use the signaling network to determine the values for \(r\), the TF weights used to reconstruct the regulatory networks. While the main goal of the regulatory network reconstruction method is to explain the temporal gene expression trajectories using the dynamic activation of TFs, the main objective when reconstructing the signaling network is to explain how these TFs are activated by the infecting viruses. For this, we attempt to link sources (protein interacting with the virus) and targets (TFs controlling virus-specific expression response) using paths in the network. The orientation is determined by specifying edge directionality to optimize the following equation:

\[
\max \sum_{i \in I} \sum_{p \in P_i} I(p) h_P s_i
\]

where \(T\) is the list of TFs predicted to regulate the time series for a specific condition, \(P_i\) is the set of paths that start from a source of this condition and end in TF \(t\), \(h_P\) is the weight of the path which is defined as the multiplication of the probabilities of the edges in the path, and \(s_i\) is the score of the TF \(t\) obtained from the regulatory network reconstruction. \(I(p)\) is an indicator function indicating whether path \(p\) is satisfied or not (a path is satisfied if all the edges in the path are oriented in a direction that links the source to the target) and thus optimizing the above equations requires the assignment of directionality to the PPI edges (see [8,10] for details). Note that a Breadth First Search or a Depth First Search are not enough to solve this since we assume PPI edges may be undirected. Thus, certain paths can contradict each other in terms of the specific edge direction making this a non trivial optimization problem (in fact, it is NP complete – see [79] for details and algorithm for solving this problem).

If we have multiple conditions we can simply run this function independently for each of them leading to the following set of optimization problems:

\[
\max \sum_{i \in I} \sum_{p \in P_i} I(p) h_P s_i \quad \forall c \in C
\]

Here \(c\) goes over each of the conditions and the function is optimized independently for that condition. However, such independent optimization may lead to contradictory directionality assignments. In addition, it does not utilize shared properties between the conditions. Instead, we would like to -

1. Constrain the model to use shared parameters – thus the direction of the edges in the signaling networks is constrained to be the same in all models.

2. Favor pathways which end in TFs that are used in more than one condition.

To achieve the first goal above we attempt to maximize the objectives for each condition using a shared, directed, network. For this we modify the search procedure by assigning edge direction to maximize the sum of the objectives across all networks. See Supplementary methods in S1 Text for details.

The second requirement is more involved since it requires us to change node scores based on TF usage across the conditions. To obtain more shared TFs we add an additional term to the objective function. We introduce a new, global, parameter, \(z\) which is used to increase the weight assigned to shared TFs. See Supplementary methods in S1 Text for details. Also see Table S7 in S1 Text for discussion on the impact of different values of \(z\) on the performance of MT-SDREM.

**Ranking proteins in reconstructed networks**

Following the multi-task learning procedure we arrive at directed, weighted networks for each of the conditions being studied. To further select the key proteins from each of these networks we rank the proteins based on the “path flow” going through a node. The path flow \(f\) through a node \(n\) is defined as follows –

\[
f(n) = \sum_{p \in P} I(p) h_P
\]

where \(P\) is the set of paths containing node \(n\).

To combine the rankings from each condition into a single ranking, we compute the total flow through all the nodes

\[
F_i = \sum_{n \in N} f_i(n)
\]

where \(N\) is the set of genes and \(i\) is the condition and then we computed the % flow \(f_i(n) = \frac{f_i(n)}{F_i}\) through a node. To get the combined score for a gene across conditions, we sum up the condition-specific % flows to get \(s(n) = \sum_{c=1}^{C} f_i(n)\) where \(C\) is the number of conditions. Then we rank the genes in descending order of the final score \(s(n)\).

**Supporting Information**

S35 Table Extension of Table S8 in S1 Text containing all the immune related GO categories for MT-SDREM not present or with p-value $\geq 0.01$ Tensor clustering for the complete network. (XLSX)

S36 Table Extension of Table S9 in S1 Text containing all the immune related GO categories for MT-SDREM not present in or with p-value $\geq 0.01$ Tensor clustering for the top 20,000 edges in the network. (XLSX)

S37 Table Extension of Table S11 in S1 Text containing all the immune related GO categories for MT-SDREM not present in or with p-value $\geq 0.01$ in Tensor clustering for the top 5,000 edges in the network. (XLSX)

S38 Table Extension of Table S16 in S1 Text containing all immune-response related categories for MT-SDREM not present or with p-value $\geq 0.01$ in DE genes for top 500 genes for H1N1. (XLSX)
S39 Table  Extension of Table S18 in S1 Text containing all immune-response related categories for MT-SDREM not present or with p-value ≥0.01 in DE genes for top 500 genes for H3N2. (XLSX)

S40 Table  Extension of Table S20 in S1 Text containing all immune-response related categories for MT-SDREM not present or with p-value ≥0.01 in DE genes for top 500 genes for H5N1. (XLSX)

S41 Table  Extension of Table S21 in S1 Text containing all immune-response related categories for MT-SDREM not present or with p-value ≥0.01 in DE genes for top 1000 genes for the joint list. (XLSX)

S42 Table  Extension of Table S23 in S1 Text containing all immune-response related categories for MT-SDREM not present or with p-value ≥0.01 in DE genes for top 1000 genes for H1N1. (XLSX)

S43 Table  Extension of Table S25 in S1 Text containing all immune-response related categories for MT-SDREM not present or with p-value ≥0.01 in DE genes for top 1000 genes for H3N2. (XLSX)

References


