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ABSTRACT

We search for electron anti-neutrinos (νe) from long- and short-duration gamma-ray bursts (GRBs) using data taken by the Kamioka Liquid Scintillator Anti-Neutrino Detector (KamLAND) from 2002 August to 2013 June. No statistically significant excess over the background level is found. We place the tightest upper limits on νe flux from GRBs below 7 MeV and place first constraints on the relation between νe luminosity and effective temperature.

Key words: gamma-ray burst; general – neutrinos

1. INTRODUCTION

Gamma-ray bursts (GRBs) are the most luminous phenomena in the universe. The duration of GRBs (ΔtGRB) varies from 10 ms to 1000 s, with a roughly bimodal distribution for so-called long GRBs of ΔtGRB ≳ 2 s and short GRBs of ΔtGRB ≲ 2 s. The progenitors of most short GRBs are widely thought to be mergers of neutron star–neutron star or black hole–neutron star binaries (Mészáros 2006). A favored model of long GRB progenitors is a catastrophic collapse of a massive star into a black hole (Mészáros 2006). These models are supported by observations of afterglows and identification of host galaxies for short GRBs (Villasenor et al. 2005; Fox et al. 2005) and observations of supernovae associated with long GRBs (Woosley et al. 1999; Hjorth et al. 2003). Both scenarios would result in the formation of a compact rotating black hole with an accretion disk at MeV or higher temperatures, which generates collimated relativistic fireball jets leading to GRBs. Although such a fireball model is promising and attractive, the initial condition and generation mechanism of the fireball jets are still unknown, since it is difficult to observe the optically thick center region of GRBs by electromagnetic waves.

A potential scheme to directly explore the GRB center region is the use of thermal neutrinos and gravitational waves (GWs; Suwa & Murase 2009; Sekiguchi et al. 2011), since they have strong transmissivity. Thermal neutrinos are sensitive to thermodynamic profiles of the accretion disk, and GWs are sensitive to the dynamics of progenitors. Both are complementary observations to probe GRBs. Super-Kamiokande (SK) and Sudbury Neutrino Observatory (SNO) searched for MeV neutrinos related to GRBs and placed constraints on the upper fluence limits (Fukuda et al. 2002; Aharmin et al. 2014). Others placed limits on high-energy neutrinos produced in the fireball jets (Achterberg et al. 2008; Thrane et al. 2009; Abbasi et al. 2011; Avrorin et al. 2011; Vieregg et al. 2011; Adrián-Martínez et al. 2013). GWs from GRBs were studied by a GW detector network (Aasi et al. 2014).

In this paper, we present a study of electron anti-neutrinos (νe) of a few tens of MeV energy produced by thermal processes from the GRB center region, especially the accretion disk (Nagataki & Kohri 2002; Caballero et al. 2009; Sekiguchi & Shibata 2011), with the Kamioka Liquid Scintillator Anti-Neutrino Detector (KamLAND). We constrain the relation between the νe’s luminosity (L) and effective temperature (T), as well as νe fluence, for the first time. The L–T relationship can be used to directly compare with theoretical predictions. These limits and constraints are established using redshift-
measured GRBs. We adopt the standard ΛCDM cosmology with Ω_m = 0.315, Ω_Λ = 0.685, and H_0 = 67.3 km s^{-1} Mpc^{-1} (Ade et al. 2014) throughout this paper.

2. KamLAND DETECTOR

The KamLAND detector is located ~1 km under the peak of Mt. Ikenoyama (36.42 N, 137:31 E) near Kamioka, Japan. The 2700 m water equivalent of vertical rock overburden reduces the cosmic-ray muon flux by almost five orders of magnitude. A schematic diagram of KamLAND is shown in Figure 1. The primary target volume consists of 1 kton of ultra-pure liquid scintillator (LS) contained in a 13 m diameter spherical balloon made of 135 μm thick transparent nylon ethylene vinyl alcohol copolymer composite film. The LS consists of 80% dodecane and 20% pseudocumene (1, 2, 4-trimethylbenzene) by volume, and 1.36 ± 0.03 g l^{-1} of the fluor PPO (2, 5-diphenyloxazole). A buffer comprising 57% isoparaffin and 43% dodecane oils by volume, which fills the region between the balloon and the surrounding 18 m diameter spherical stainless-steel outer vessel, shields the LS from external radiation. The specific gravity of the buffer oil is adjusted to be 0.04% lower than that of the LS. An array of photomultiplier tubes (PMTs)—1325 specially developed fast PMTs masked to 17-inch diameter and 554 older 20-inch diameter PMTs reused from the Kamiokande experiment (Kume et al. 1983)—are mounted on the inner surface of the outer vessel, providing 34% photocathode coverage. This inner detector is shielded by a 3.2 kton water-Cherenkov veto detector.

KamLAND uses the inverse beta-decay reaction to detect π^0:

\[ π^0 + p → e^+ + n. \]  

(1)

This process has a delayed-coincidence (DC) event-pair signature that offers powerful background suppression. The energy deposited by the positron, which generates the DC pair’s prompt event, is the sum of the e^+ kinetic energy and annihilation γ energies, \( E_π(=E_{e^+} + 2m_e) \), and related to the incident π^0 energy by \( E_π = \langle E_{e^+} \rangle + \delta + E_{e^CM} E_{e^CM}/m_p \), where \( E_{e^CM} \) and \( E_{e^CM} \) are neutrino and electron energy in the center-of-mass frame, respectively, and \( \delta = (m_n^2 - m_e^2 - m_π^2)/2m_p \) (Strumia & Vissani 2003). In the low-energy \( (E_π < 20\ MeV) \) range, we can approximate the above relation by \( E_π = E_p + \delta E \), where \( \delta E = 0.78\ MeV \). We use this approximation also above 20 MeV and comment on the associated uncertainty later. The delayed event in the DC pair is generated by a 2.2 (4.9) MeV γ-ray produced when the neutron captures on a proton \((^{12}\text{C})\). The mean neutron capture time is 207.5 ± 2.8 μs (Abe et al. 2010). The angular distribution of the positron emission is nearly isotropic. Unlike in a water-Cherenkov detector, the scintillation light is also isotropic. As a result, the positron signal does not provide the incoming π^0 source direction. Due to the extremely low cross section of π^0, the Earth does not shadow MeV-energy extraterrestrial π^0. The detector therefore has isotropic sensitivity to GRBs.

The event energy and vertex reconstruction are based on the timing and charge distributions of scintillation photons recorded by the PMTs. The reconstruction algorithms are calibrated with on-axis and off-axis radioactive sources deployed from a glove box installed at the top of the detector. The radioactive sources are \(^{60}\text{Co}, ^{68}\text{Ge}, ^{203}\text{Hg}, ^{65}\text{Zn}, ^{241}\text{Am}^{9}\text{Be}, ^{137}\text{Cs}, \) and \(^{210}\text{Po}^{13}\text{C} \), providing energy and vertex calibration (Berger et al. 2009; Banks et al. 2015). The overall vertex reconstruction resolution is ~12 cm/√(<E(MeV)>), and energy resolution is 6.4%/√(<E(MeV)>). The energy reconstruction of positrons with \( E_p > 7.5\ MeV \) (i.e., \( E_π > 8.3\ MeV \)) is verified by using tagged \(^{12}\text{B} \) β^- decays generated via muon spallation (Abe et al. 2010).

In 2011 September, the KamLAND-Zen double-beta (ββ) decay search experiment was launched (Gando et al. 2012). This experiment makes use of KamLAND’s extremely low background. The KamLAND detector was modified to include a ββ source, 13 tons of Xe-loaded LS (Xe-LS) contained in a 3.08 m diameter inner balloon (IB), at the center of the detector.

3. EVENT SELECTION

3.1. KamLAND DC Events

In this analysis, we use KamLAND data collected from 2002 August 3 to 2013 June 4. During the majority of this period, KamLAND was measuring π^0 from nuclear power plants with a spectrum up to about 8 MeV (Gando et al. 2011a, 2013) and geological π^0 from the Earth’s deep interior (Araki et al. 2005; Gando et al. 2011b, 2013). Following the Fukushima reactor accident in 2011 March, all Japanese reactors were subject to a protracted shutdown. The data set is divided into two periods. Period I refers to data that were taken until the IB installation in 2011 September. Period II refers to the data taken after the IB installation, which mostly coincided with the low reactor π^0 flux.

In Period I, we search only for π^0 events with \( E_{\text{low}}^1(= 7.5\ MeV) \leq E_p \leq 100\ MeV \), which corresponds to the energy range of interest for GRBs with almost zero contamination from the reactor π^0 flux. During Period II, the reactor signal is minimal, allowing a reduction of the energy threshold to \( E_{\text{low}}^2 = 0.9\ MeV \).

For the DC event pair selection, we apply the following series of selection cuts: the prompt energy is required to be
\( E_{\text{low}}^k \leq E_p \leq 100 \text{ MeV} \) in Period \( k \), and the delayed energy to be \( 1.8 \text{ MeV} \leq E_q \leq 2.6 \text{ MeV} \) for neutron capture on protons or \( 4.4 \text{ MeV} \leq E_d \leq 5.6 \text{ MeV} \) for neutron capture on \(^{12}\text{C} \), a fiducial volume cut of \( R \leq 6 \text{ m} \) from the center of the balloon on both prompt and delayed events, a spatial correlation cut of \( \Delta R \leq 1.6 \text{ m} \), and a time separation cut of \( 0.5 \mu s \leq \Delta T \leq 1.0 \text{ ms} \). Spallation cuts were used to reduce backgrounds from long-lived isotopes, e.g., \(^{\text{3}}\text{Li} \) \((\tau = 257 \text{ ms} \) and \( Q = 13.6 \text{ MeV} \)), that are generated by cosmic muons passing through the scintillator. In Period II, we have to use an additional spatial cut for delayed events to avoid backgrounds from the IB and its support material as shown in Figure 1 (Gando et al. 2013), and a second-level cut using a likelihood discriminator to reduce accidental backgrounds in the low-energy region (Gando et al. 2011a). The selection efficiency \((\epsilon^I_f)\) is evaluated from Monte Carlo simulation separately for Period I \((k = I)\) and Period II \((k = II)\) due to these additional cuts. Note that \( \epsilon^I_f \) depends on \( E_p \) because of the energy-dependent second-level cut. The number of target protons in \( R \leq 6 \text{ m} \) is estimated to be \( N_T = (5.98 \pm 0.12) \times 10^{31} \).

The total livetime during Period I was 6.91 yr, and 55 DC events were observed during this period. In Period II, KamLAND found 88 DC events with 1.2 yr livetime. The livetime is defined as the integrated period of time that the detector was sensitive to \( E_p \) and includes corrections for calibration periods, detector maintenance, daily run switch, etc. The event rates are \( 9.1 \times 10^{-4} \) and \( 8.4 \times 10^{-3} \) events per hour in Periods I and II, respectively.

### 3.2. GRB Events

We use GRB events observed by one or more of \( \text{SWIFT}, \ HETE-2, \ \text{Ulysses}, \ \text{INTEGRAL}, \ \text{AGILE}, \ \text{MAXI}, \) and \( \text{Fermi} \) based on the Gamma-ray Coordinates Network.\(^{19}\) Initial selection criteria are the requirement that the GRB be in the time period between 2002 August 3 and 2013 June 4 and the existence of redshift and GRB-duration time measurements. At this stage, 256 long GRB and 21 short GRB events are left. Subsequently, all the KamLAND runs\(^{20}\) that include GRB events must have passed basic quality criteria (e.g., not a calibration run and stable operation). This leaves 175 long GRBs and 17 short GRBs in Period I. Period II contains 38 long GRBs and one short GRB. One can see our GRB list online.\(^{21}\)

### 4. DATA ANALYSIS

The average number of DC events and GRB events per 3 months is shown in Figure 2. In this figure, one can see a “step” before and after the launch of the \( \text{SWIFT} \) satellite (2004 November) for GRB events. In contrast, there is no time dependence of the DC event rate during each period. We therefore decided to analyze all of the KamLAND data regardless of the GRB event rate.

#### 4.1. Coincidence Analysis

We conduct a time-coincidence analysis between the redshift-measured GRB samples and the KamLAND DC events for long and short GRBs. The coincidence search time window between a GRB event and a KamLAND DC event is defined as \(-t_p + T_{\text{GRB}} \leq T_{\text{DC}} \leq T_{\text{GRB}} + \Delta t_{\text{GRB}} + t_p + t_f(z)\), where \( T_{\text{DC}} \) and \( T_{\text{GRB}} \) are the absolute times of the KamLAND DC and GRB events, respectively. \( \Delta t_{\text{GRB}} \) is the measured GRB duration time, \( t_p \) is 150 s corresponding to a model-dependent but reasonable time difference between the thermal neutrino production and the GRB photon production (Y. Sekiguchi & Y. Suwa 2012, private communication; K. Toma 2014, private communication), and \( t_f(z) \) is the relativistic flight-time delay of MeV neutrinos due to non-zero neutrino mass (Choubey & King 2003; Li et al. 2005):

\[
 t_f(z) = \frac{1}{2} \int_0^z \frac{dz'}{(1 + z')^2 H(z') \Omega_{\Lambda} + (1 + z')^3 \Omega_m} \]

with the assumption of \( m_\nu = m_{\text{heaviest}} = 87.2 \text{ meV} \) from \( \sum m_\nu \leq 0.23 \text{ eV} \) (Ade et al. 2014) and \( E_\tau \geq 8.3 \text{ MeV} \) in Period I and \( E_\tau \geq 1.8 \text{ MeV} \) in Period II. All parameters of the time window are fixed before the coincidence search. The total window length for the long GRBs is 25.2 hr (18.3 hr in Period I and 6.82 hr in Period II). The short GRBs sum to a total of 1.45 hr of on-time window (1.33 hr in Period I and 0.11 hr in Period II).

No coincidence DC events were found in the above time window for both long and short GRBs. We estimate the expected accidental coincidence of DC events to be \( 7.4 \times 10^{-2} \) and \( 2.2 \times 10^{-3} \) for long and short GRBs, respectively. For long GRBs, the background spectrum is shown in Figure 3 with several expected spectra from our 90\% upper limits (see 4.3). In the absence of a signal, the Feldman–Cousins (FC) upper limits on the DC events are \( N_{90} = 2.365 \) and 2.435 with 90\% confidence level (CL) for long and short GRBs, respectively.

If we use a much longer, exotic time window, e.g., \( t_p = 6 \text{ hr} \), four coincidence DC events are found for long GRBs.
However, the expected accidental coincidence of DC events is 3.4. There is therefore no statistical evidence for the detection of $\pi_e$ from long GRBs.

4.2. Fluence Upper Limits

There is no established neutrino production model for GRBs. We translate our FC limits to model-independent upper limits on $\pi_e$ fluence, $\Psi(E_\pi)$, at the detector using a Green’s function, which represents the upper limits on monoenergetic neutrinos at that specific energy. We use the same methodology to estimate $\Psi(E_\pi)$ as SK (Fukuda et al. 2002) and SNO (Aharmim et al. 2014):

$$\Psi(E_\pi) = \frac{N_{90}}{\sum_k N_{90}^k I_k(E_{\pi})},$$

where $N_{90}^k$ is the number of GRBs and $I_k(E_{\pi})$ is the effective number of DC events per one GRB with a monoenergetic spectrum in the period $k$:

$$I_k(E_{\pi}) = N_T \int_{E_{\text{low}}}^{100 \text{MeV}} E_\pi \sigma_{\text{IBD}}(E_{\pi}) \eta(E_{\pi}) dE_{\text{exp}}$$

and

$$\eta(E_{\pi}) = \frac{1}{\sqrt{2\pi} \sigma \sigma'} \exp \left(-\frac{(E_{\text{exp}} - E_{\text{vis}})^2}{2 \sigma^2 \sigma'^2} \right).$$

$\epsilon_t$ is the mean livetime-to-runtime ratio, and $E_{\text{exp}}$ and $E_{\text{vis}}$ are the expected and measured prompt energies, respectively. $\sigma_{\text{IBD}}(E)$ is the differential cross section of the inverse beta decay. $\sigma(E)$ corresponds to the energy resolution of 6.4%/$\sqrt{E}$ (MeV).

The 90% CL upper limits on $\Psi(E_{\pi})$ from KamLAND are shown for both long and short GRBs together in Figure 4 with the results from SK (Fukuda et al. 2002) and SNO (Aharmim et al. 2014). Note that the results from SK and SNO treated long and short GRBs as the same. Below 7 MeV, our analysis provides the best limits so far.

4.3. Constraint on Luminosity and Effective Temperature ($L$–$T$)

$N_{90}$ can be translated to constrain the $\pi_e$’s luminosity ($L$) and effective temperature ($T$) in the accretion disk using the assumption that the $\pi_e$ flux follows the Fermi–Dirac distribution described:

$$\Psi(E_{\pi}, T, L) = \frac{120}{7\pi^4 T^4} \frac{E_{\text{vis}}^2}{\exp \left(\frac{E_{\text{vis}}}{T}\right) + 1}.$$  

The expected total fluence at the detector is in Period $k$,

$$\Psi^k(E_{\pi}, T, L) = \sum_{i=\text{low}}^{100 \text{MeV}} \frac{1 + z_i}{4\pi d_i^2} \Psi ((1 + z_i)E_{\pi}, T, L),$$

where $z_i$ and $d_i$ are the redshift and luminosity distance of the $i$th GRB, respectively. The luminosity and effective temperature upper limits ($T_{\text{up}}$, $L_{\text{up}}$) are then connected to $N_{90}$:

$$N_{90} = \sum_k \int_{E_{\text{low}}}^{100 \text{MeV}} \Psi^k(T_{\text{up}}, L_{\text{up}}, E_{\text{vis}}) dE_{\text{vis}}.$$  

With the assumption of $E_{\pi} = E_{\text{exp}} + \delta E$, the results obtained from KamLAND are shown in Figure 5. The upper limit spectra ($\sum_k \Psi^k(T_{\text{up}}, L_{\text{up}}, E_{\text{vis}})$) with $T_{\text{up}} = 5, 10, 15$ MeV are shown in Figure 3.

The limits are six orders of magnitude higher than the supernova $\pi_e$ luminosity and several orders of magnitude higher than theoretical studies predict. Nagataki & Kohri (2002)
analytically show that a collapsar emits $E_p$ with $L = 10^{52} \, \text{erg}$ and $T = 5 \, \text{MeV}$ in a total accretion mass of $30 \, M_\odot$, an initial mass of $3 \, M_\odot$, and a mass accretion rate of $0.1 \, M_\odot \, \text{s}^{-1}$. Caballero et al. (2009) numerically predict $L = 3.5 \times 10^{52} \, \text{erg}$ for $0.15 \, \text{s}$ with $T = 7.5 \, \text{MeV}$ for black hole–neutron star mergers. Here we assumed that the averaged $E_p$ energy corresponds to $3.15 \, T$. Recently, Sekiguchi presented $L = 1.5–3 \times 10^{52} \, \text{erg} \, \text{s}^{-1}$ for $2–3 \, \text{s}$ with an averaged $E_p$ energy of $20–30 \, \text{MeV}$ for a merger of binary neutron stars using state-of-the-art numerical simulations (Sekiguchi & Shibata 2011).

Finally, we comment about the approximation, $E_p = E_p^{\text{exp}} + \delta E$. Above $20 \, \text{MeV}$, this approximation is not suitable. In addition, the effect of the recoiling neutron ($E_n$) to $E_p$ is no longer negligible. This effect adds a substantial energy bias, $\sim 10\%$, but the uncertainty of $L_{\text{up}}$ is much smaller than $10\%$. The amount of the error has no impact on our result and discussion.

5. SUMMARY

We find no evidence for $E_p$ associated with our sample of GRBs in KamLAND. We placed the lowest observational bound on the $E_p$ fluence below $7 \, \text{MeV}$. The relation of $L-T$, which characterizes the GRB accretion disk, is constrained. The obtained upper limits are significantly higher than several theoretical predictions (Nagataki & Kohri 2002; Sekiguchi & Shibata 2011). However, our result is the first constraint that can be directly compared to theoretical studies.

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